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(71) Applicant (for all designated States except US): **LSI CORPORATION** [US/US]; 1621 McCarthy Boulevard, Milpitas, CA 95035 (US).

(72) Inventor; and

(75) Inventor/Applicant (for US only): **GUNNAM, Kiran** [IN/US]; 371 Elan Village Lane, Apt. 226, San Jose, CA 95134 (US).

(74) Agents: **MENDELSON, Steve et al.**; Mendelsohn & Associates, P.C., 1500 John F. Kennedy Blvd., Suite 405, Philadelphia, PA 19102 (US).

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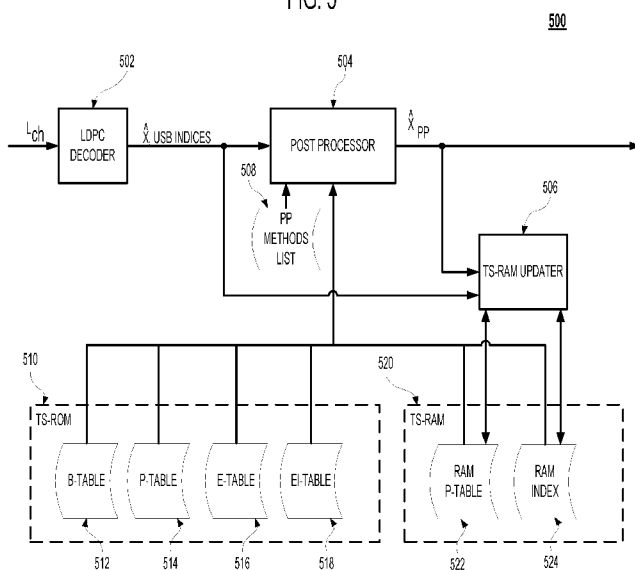
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(54) Title: RAM LIST-DECODING OF NEAR CODEWORDS

FIG. 5



(57) Abstract: Certain embodiments of the present invention are efficient run-time methods for creating and updating a RAM list of dominant trapping-set profiles for use in (LDPC) list decoding. A decoded correct codeword is compared to a near codeword to generate a new trapping-set profile, and the profile written to RAM. Record is kept of how many times RAM has been searched since a profile was last matched. Profiles that have not been matched within a specified number of searches are purge-eligible. Purge-eligible profiles are further ranked on other factors, e.g., number of times a profile has been matched since it was added, number of unsatisfied check nodes, number of erroneous bit nodes. If there is insufficient free space in RAM to store a newly-discovered profile, then purge-eligible profiles are deleted, beginning with the lowest-ranked profiles, until either (i) sufficient free space is created or (ii) there are no more purge-eligible profiles.

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RAM LIST-DECODING OF NEAR CODEWORDS

[0001] Cross-Reference to Related Applications

[0002] This application claims the benefit of the filing date of U.S. provisional application no. 61/089,297, filed on 08/15/08 as attorney docket no. 08-0241-PR, the teachings of which are incorporated herein by reference in its entirety.

[0003] The subject matter of this application is related to U.S. patent application no. XX/xxx,xxx filed on the same date as this application as attorney docket no. 08-1293, the teachings of which are incorporated herein by reference in their entirety.

BACKGROUND OF THE INVENTION

[0004] Field of the Invention

[0005] The invention relates to digital signal processing, and, in particular, to a data-encoding method known as low-density parity check (LDPC) coding.

[0006] Description of the Related Art

[0007] Communication is the transmission of information by a transmitter to a receiver over a communications channel. In the real world, the communications channel is a noisy channel, outputting to the receiver a distorted version of the information received from the transmitter. A hard disk (HD) drive is one such noisy channel, accepting information from a transmitter, storing that information, and then, possibly, transmitting a more or less distorted copy of that information to a receiver.

[0008] The distortion introduced by a communications channel such as an HD drive might be great enough to cause a channel error, i.e., where the receiver interprets the channel output signal as a 1 when the channel input signal was a 0, and vice versa. Channel errors reduce throughput, and are thus undesirable. Hence, there is an ongoing need for tools which detect and/or correct channel errors. Low-density parity check (LDPC) coding is one method for the detection and correction of channel errors. LDPC codes are among the known near-Shannon-limit codes that can achieve very low bit-error rates (BER) for low signal-to-noise ratio (SNR) applications. LDPC decoding is distinguished by its potential for parallelization, low implementation complexity, low decoding latency, as well as less-severe error-floors at high SNRs. LDPC codes are considered for virtually all the next-generation communication standards.

SUMMARY OF THE INVENTION

[0009] In certain embodiments, the present invention comprises methods for decoding encoded data encoded with a graph-based code. The method comprises (i) performing decoding on the encoded data to generate a candidate decoded codeword and (ii) performing, if the candidate decoded codeword is not a decoded correct codeword, a trapping-set (TS)-RAM list-decoding method to attempt to generate the decoded correct codeword. The TS-RAM list-decoding method accesses one or more TS profiles stored

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in RAM memory, each TS profile corresponding to a different trapping set.

[0010] In other embodiments, the present invention is an apparatus for decoding encoded data encoded with a graph-based code. The apparatus comprises (i) a decoder adapted to perform decoding on the encoded data to generate a candidate decoded codeword, (ii) RAM memory, and (iii) a trapping-set (TS)-RAM list decoder adapted to perform, if the candidate decoded codeword is not a decoded correct codeword, a TS-RAM list-decoding method to attempt to generate the decoded correct codeword. The TS-RAM list decoder accesses one or more TS profiles stored in the RAM memory, each TS profile corresponding to a different trapping set.

BRIEF DESCRIPTION OF THE DRAWINGS

[0011] Other aspects, features, and advantages of the invention will become more fully apparent from the following detailed description, the appended claims, and the accompanying drawings in which like reference numerals identify similar or identical elements.

[0012] **FIG. 1** is a block diagram of a portion of a typical hard disk (HD) drive **100** that utilizes LDPC coding.

[0013] **FIG. 2(A)** depicts LDPC H matrix **200**, and **FIG. 2(B)** is a Tanner graph of H matrix **200**.

[0014] **FIG. 3** is a flowchart of typical LDPC decoding method **300** used by decoder **112**.

[0015] **FIG. 4** is a block diagram of an off-line trapping-set (TS) simulation tool **400** for identifying trapping sets and recording various information about those trapping sets.

[0016] **FIG. 5** is a block diagram of an LDPC decoding system **500** according to one embodiment of the present invention.

[0017] **FIG. 6** is an exemplary layout of ROM P-Table **514** of **FIG. 5**.

[0018] **FIG. 7** is an exemplary layout of B-Table **512** of **FIG. 5**.

[0019] **FIG. 8** is an exemplary layout of E-Table **516** of **FIG. 5**.

[0020] **FIG. 9** is an exemplary layout of EI-Table **518** of **FIG. 5**.

[0021] **FIG. 10** is an exemplary layout of RAM P-Table **522** of **FIG. 5**.

[0022] **FIG. 11** is an exemplary layout of RAM Index Table **524** of **FIG. 5**.

[0023] **FIG. 12** is a flowchart of exemplary process **1200** used by LDPC decoding system **500** of **FIG. 5**.

[0024] **FIG. 13** is a flowchart of exemplary TS-ROM list-decoding process **1206** of **FIG. 12** implemented by post-processor **504** of **FIG. 5**.

[0025] **FIG. 14** is a flowchart of exemplary TS-ROM search process **1314** of **FIG. 13**.

[0026] **FIG. 15** is a flowchart of exemplary TS-RAM list-decoding process **1208** of **FIG. 12**.

[0027] **FIG. 16** is a flowchart of exemplary TS-RAM update process **1216** of **FIG. 12**.

DETAILED DESCRIPTION

[0028] **FIG. 1** is a block diagram of a portion of a typical hard disk (HD) drive **100** that utilizes LDPC coding. HD drive **100** comprises platters **102** and read channel **104**. Read channel **104** comprises LDPC encoder **106**, write processor **108**, read processor **110**, and LDPC decoder **112**. Path **114** is the noisy channel between LDPC encoder **106** and LDPC decoder **112**.

[0029] Information words to be written to platters **102** are processed by LDPC encoder **106** to yield LDPC codewords. LDPC codewords are sent to write processor **108**, which comprises a number of modules, e.g., a BPSK (binary phase-shift keying) encoder, a digital-to-analog converter, etc. Output **116** of write processor **108** is written to platters **102**.

[0030] Signals **118** read from platters **102** are sent to read processor **110**, which comprises a number of modules, e.g., a pre-amplifier, a continuous-time filter, a fixed-impulse response filter, a detector, an analog-to-digital converter, etc. Read processor **110** outputs log-likelihood ratio (LLR) values L_{ch} to LDPC decoder **106**, which in turn outputs decoded information words. Additionally, LDPC decoder **106** sends E_{LDPC} values back to read processor **110**. E_{LDPC} are defined by Equation 6 below, and represent intermediate calculated LLR values. Read processor **110** uses the E_{LDPC} values to tune its performance, a process known as turbo-decoding.

[0031] **LDPC Encoding**

[0032] LDPC encoder **106** appends to the bits of an information word a number of parity bits specified by the LDPC code, to yield a codeword. The bits in an information word are known as variable bits, and the number of those variable bits is denoted K . The total number of bits in an LDPC codeword is denoted N . Thus, the number of parity bits is given by $N - K$. The rate of a particular LDPC code is K / N , i.e., the ratio of the information word length to the codeword length. Thus, an LDPC code which appends six parity bits to each three-bit information word to yield a nine-bit codeword has a rate of 1/3. In the case of a typical HD drive, the information word length K is 4096 bits (the length of a typical HD drive sector), and the number of parity bits is approximately 410 bits, for a codeword length of 4506 bits and a rate of 0.9.

[0033] Each parity bit in an LDPC codeword is associated with one or more other (variable or parity) bits in that codeword in a particular way as specified by the particular LDPC code, and the value assigned to a parity bit is set so as to satisfy the LDPC code. Typical LDPC codes specify that associated bits satisfy a parity check constraint, e.g., the sum of the associated bits is an even number, i.e., sum modulo 2 = 0.

[0034] **The LDPC Code**

[0035] A particular LDPC code is defined by a two-dimensional matrix of 1s and 0s known as the parity check matrix, or H matrix, or simply **H**. **H** is known, a priori, by both the LDPC encoder and

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decoder. \mathbf{H} comprises N columns and $N - K$ rows, i.e., a column for every bit of the codeword, and a row for every parity bit. Each 1 in \mathbf{H} represents an association between the codeword bit of the column and the parity bit of the row. For example, a 1 at the third row, seventh column of \mathbf{H} means that the third parity check bit is associated with the seventh bit of the codeword. The modulo 2 sum of the value of a check bit and all variable bits associated with that check bit should be 0.

[0036] The number of 1s in a column of \mathbf{H} is known as the weight w_c of that column. Similarly, the number of 1s in a row of \mathbf{H} is known as the weight w_r of that row. The LDPC code defined by an \mathbf{H} wherein all columns have the same w_c and all rows have the same w_r is known as a regular LDPC code. An LDPC code defined by an \mathbf{H} where w_c and/or w_r are not the same across all columns and/or rows, respectively, is known as an irregular LDPC code.

[0037] A defining characteristic of typical LDPC codes is that \mathbf{H} is “sparse,” i.e., the elements of \mathbf{H} are mostly 0s with few 1s. Research has shown that \mathbf{H} matrices typically need $w_c \geq 3$ in order to perform well, and that irregular LDPC codes outperform regular LDPC codes.

[0038] FIG. 2(A) depicts LDPC H matrix 200. H matrix 200 comprises $N = 9$ columns and $N - K = 6$ rows. Thus, \mathbf{H} matrix 200 defines an LDPC code which accepts a three-bit information word, appends six parity bits, and outputs a nine-bit codeword. Thus, the rate of this particular LDPC code is 3/9 or 1/3. The LDPC code defined by \mathbf{H} matrix 200 is regular, with a w_c of two, and a w_r of three.

[0039] Channel Output: Log-Likelihood Ratios

[0040] Returning to FIG. 1, the path 114 between LDPC encoder 106 and LDPC decoder 112 is a noisy channel, and, as such, decoder 112 does not receive a perfect copy of the codewords outputted by LDPC encoder 106. Instead, read processor 110 outputs one or more L_{ch} values, where each L_{ch} value corresponds to a bit in the channel input codeword.

[0041] Each L_{ch} value is a log-likelihood ratio (LLR). An LLR is a data structure comprising a number of bits, where a single sign bit indicates the hard decision (i.e., read processor 110's best guess as to whether the original bit was a 1 or a 0), and the remaining magnitude bits indicate read processor 110's degree of confidence in that hard decision. More precisely, the LLR represents $\log \frac{p_0}{p_1}$, where p_0 is the probability that the sample represents a 0, and p_1 is the probability that the sample represents a 1.

[0042] For example, read processor 110 might output each L_{ch} value as a five-bit data structure, where the most-significant bit is a sign bit which indicates the hard-decision value, and the 16 values of the four magnitude bits indicate the confidence of the hard decision. Thus, for example, in one typical

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scheme, an LLR value of binary 00000 would indicate a hard-decision value of 0 with least confidence, a value of binary 01111 would indicate a hard-decision value of 0 with maximum confidence, binary 10000 would be unused, binary 10001 would indicate a hard-decision value of 1 with least confidence, and a value of binary 11111 would indicate a hard-decision value of 1 with maximum confidence.

[0043] **LDPC Decoding: Belief Propagation**

[0044] **FIG. 3** is a flowchart of typical LDPC decoding method **300** used by decoder **112**. LDPC decoder **112** receives N number of L_{ch} values and outputs decoded information word. The heart of decoding method **300** is an iterative, two-phase message-passing algorithm called belief propagation. Belief propagation is best explained with the use of a visualization called a Tanner graph.

[0045] **FIG. 2(B)** is a Tanner graph of **H** matrix **200**. In general, a Tanner graph comprises 1) a number of bit nodes n equal to the number of columns in **H** (and thus equal to the number of variable bits), 2) a number of check nodes m equal to the number of rows in **H** (and thus equal to number of parity bits), 3) lines, also known as edges, each of which connects a single bit node to a single check node, 4) for each bit node n , the original L_{ch} value received from a receiver, and 5) for each bit node n , a calculated hard-decision output value \hat{x}_n . Tanner graph **2(B)** comprises nine bit nodes $n_0 - n_8$, six check nodes $m_0 - m_5$, 18 edges **202** connecting bit nodes to check nodes, nine L_{ch} values, and nine \hat{x}_n values.

[0046] The edges in a Tanner graph represent the relationships between (i.e., variable) bit nodes n and check nodes m , i.e., edges represent 1s in **H**. For example, in **FIG. 2(B)**, an edge **202** connects first bit node n_0 to fourth check node m_3 , meaning that there is a 1 in the first column, fourth row of **H** matrix **200** in **FIG. 2(A)**.

[0047] A Tanner graph is a bipartite graph, i.e., an edge can connect a bit node to only a check node, and cannot connect a bit node to another bit node, or a check node to another check node. The set of all bit nodes n connected by edges to a particular check node m is denoted $N(m)$. The set of all check nodes m connected by edges to a particular bit node n is denoted $M(n)$.

[0048] The index of a particular (bit or check) node is its ordinal sequence in the graph. The degree of a (bit or check) node is the number of edges connected to that node. Thus, the degree of bit node n in a Tanner graph is equal to the weight w_c of column n in the corresponding **H** matrix, and the degree of check node m in a Tanner graph is equal to the weight w_r of row m in the corresponding **H** matrix.

[0049] Returning to **FIG. 3**, processing starts at step **302** and proceeds to step **304**, decoder initialization. Decoder initialization **304** comprises setting all edges (e.g., **202** of **FIG. 2(B)**) connected to bit node n to the corresponding L_{ch} value associated with bit node n , and setting the \hat{x}_n value of bit

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node n to the hard-decision value of bit node n 's L_{ch} . Thus, for example, in **FIG. 2(B)**, if the L_{ch} value associated with bit node n_0 is +5, then, at step **304**, the two edges **202** connecting bit node n_0 to check nodes m_0 and m_3 are set to +5, and bit node n 's \hat{x}_n value is set to 1. An alternative way of expressing the first part of this step is that bit node n_0 sends a message of +5 to each check node m in set $M(n_0)$. A message sent from a bit node n to a check node m is denoted Q_{nm} , where Q_{nm} is in the form of an LLR. The state of a decoder which has just been initialized is referred to as state 0.

[0050] Step **304** then sends to syndrome check step **306** a vector \hat{x} comprising N \hat{x}_n values.

Vector \hat{x} is a codeword candidate. Syndrome check step **306** calculates syndrome vector z using the following Equation 1:

$$z = \hat{x}H^T \quad (1)$$

where H^T is the transpose of the H matrix. If z is a 0 vector, then vector \hat{x} has satisfied all the parity check constraints defined by H , i.e., \hat{x} is a valid codeword. In that case, processing proceeds to cyclic-redundancy check (CRC) check **318**.

[0051] If, instead, z is not a 0 vector, then vector \hat{x} fails one or more of the parity check constraints, which are typically referred to as unsatisfied check nodes or USCs. The number of elements in syndrome vector z that are not 0 scalar values is the number b of USCs in vector \hat{x} . Further, the indices of the non-zero scalar elements of syndrome vector z are the indices of the USCs in vector \hat{x} .

[0052] If vector \hat{x} fails syndrome check **306**, then processing continues to the first of one or more decoding iterations **308**. Decoding iteration **308** comprises three steps: 1) a belief-propagation check-node update step **310**, 2) a belief-propagation bit-node update step **312**, and 3) a syndrome check step **314**, which is identical to step **306**.

[0053] In belief-propagation check-node update step **310**, each check node m uses the Q_{nm} messages received from all bit nodes n in set $N(m)$ to calculate messages, denoted R_{mn} , according to the following Equations 2, 3, and 4:

$$R_{mn}^{(i)} = \delta_{mn}^{(i)} \max(\kappa_{mn}^{(i)} - \beta, 0) \quad (2)$$

$$\kappa_{mn}^{(i)} = |R_{mn}^{(i)}| = \min_{n' \in N(m) \setminus n} |Q_{n'm}^{(i-1)}| \quad (3)$$

$$\delta_{mn}^{(i)} = \left(\prod_{n' \in N(m) \setminus n} \text{sgn}(Q_{n'm}^{(i-1)}) \right) \quad (4)$$

where i is the decoding iteration, $N(m) \setminus n$ is set $N(m)$ excluding bit node n , and β is a positive constant, the value of which depends on the code parameters. The calculated R_{mn} messages are then sent

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back along those same edges to all bit nodes n in set $N(m)$. Like Q_{nm} messages, R_{mn} messages are LLRs.

[0054] Next, in belief-propagation bit-node update step 312, each bit node n calculates Q_{nm} messages according to the following Equation 5:

$$Q_{nm}^{(i)} = L_n^{(0)} + \sum_{m' \in M(n) \setminus m} R_{m'n}^{(i)} \quad (5)$$

where $L_n^{(0)}$ is the L_{ch} value for bit node n , and $M(n) \setminus m$ is set $M(n)$ excluding check node m . Bit node n then sends the calculated Q_{nm} messages to all check nodes m in set $M(n)$.

[0055] Also during bit-node update step 312, each bit node n updates its \hat{x}_n value according to the following Equations 6 and 7:

$$E_n^{(i)} = \sum_{m' \in M(n)} R_{mn'}^{(i)} \quad (6)$$

$$P_n = L_n^{(0)} + E_n^{(i)} \quad (7)$$

If $P_n \geq 0$, then $\hat{x}_n = 0$, and if $P_n < 0$, then $\hat{x}_n = 1$. The values generated by Equation 6 are also referred to as E-values or E_{LDPC} values. Typically, E_{LDPC} values are sent back to the read processor (e.g., read processor 110 of FIG. 1) as part of a tuning process known as turbo-decoding. The values generated by Equation 7 are referred to as P-values. The specific belief-propagation algorithm represented by Equations 2 – 7 is known as the min-sum algorithm.

[0056] Note that \hat{x}_n is updated during each decoding iteration 308 and finally outputted by decoding process 300. The original LLR values L_{ch} remain unchanged during decoding process 300. In other words, during each decoding iteration 308, each bit node n casts its vote as to the proper value of all the other bit nodes n to which it is associated via a check node m . For example, in FIG. 2(B), bit node n_0 is associated with check nodes m_0 and m_3 . Therefore, n_0 will cast its vote as to the proper values of the bit nodes associated with check nodes m_0 and m_3 , i.e., n_3 , n_5 , n_6 , and n_7 . The greater the magnitude value of bit node n 's L_{ch} value (i.e., the greater the confidence), the more bit node n 's vote counts. The net effect of this vote-casting is that the \hat{x}_n value of a bit node with a low L_{ch} magnitude value (i.e., confidence) will change and conform to the beliefs of the high-confidence bit nodes with which that bit node is associated. In other word, if a bit node's L_{ch} value contains an erroneous hard-decision value and low magnitude, then the combined votes of the other bit nodes will tend, after one or more iterations, to correct that erroneous hard-decision value.

[0057] Bit-node update step 312 sends to syndrome check step 314 a vector \hat{x} constructed out of the

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current \hat{x}_n values of the decoder. The syndrome check of step 314 is identical to the syndrome check of step 306 discussed above. If vector \hat{x} passes syndrome check 314, then vector \hat{x} is sent to CRC step 318.

[0058] LDPC Decoding: Cyclic Redundancy Check and Mis-Satisfied Check Nodes

[0059] Passing syndrome check 306 or 314 means only that vector \hat{x} is a valid codeword, but not necessarily the decoded correct codeword (DCCW). It is possible for an LDPC decoder to generate a valid codeword which is not the DCCW. In that case, there are no USCs in vector \hat{x} , but there are mis-satisfied check nodes (MSCs). Thus, to ensure that valid vector \hat{x} is the DCCW, process 300 passes vector \hat{x} to cyclic redundancy check (CRC) 318. A CRC check is a checksum operation which can detect alteration of data during transmission or storage.

[0060] If vector \hat{x} passes the CRC check, then vector \hat{x} is the DCCW, and process 300 sets global variable *DCCW* to true, outputs vector \hat{x} , and terminates at step 320. Otherwise, vector \hat{x} is not the DCCW, and process 300 sets global variable *DCCW* to false, outputs vector \hat{x} , and terminates at step 320. Global variable *DCCW* informs other decoding processes (e.g., TS-ROM list-decoding process 1206 of FIG. 12, discussed below) whether or not the DCCW has been generated.

[0061] Returning to step 314, if vector \hat{x} fails the syndrome check, then vector \hat{x} still contains one or more USCs. The typical method for resolving USCs is to perform another decoding iteration 308. However, there might exist one or more USCs in a particular vector \hat{x} which will never be satisfied in a reasonable amount of time. Thus, LDPC decoders are typically limited in how many decoding iterations they can perform on a particular vector \hat{x} . Typical values for the maximum number of iterations range from 50 to 200.

[0062] In FIG. 3, step 316 determines whether the maximum number of iterations has been reached. If not, then another decoding iteration 308 is performed. If, instead, the maximum number of iterations has been reached, then decoder process 300 has failed, i.e., the decoder is a “failed decoder.” In that case, process 300 sets global variable *DCCW* to false, outputs vector \hat{x} , and terminates at step 320.

[0063] If vector \hat{x} of a failed decoder contains a small number (e.g., less than 16) of USCs, then vector \hat{x} is referred to as a near codeword (NCW). If vector \hat{x} of a failed decoder contains a large number (e.g., greater than 15) of USCs, then vector \hat{x} is referred to as an invalid codeword (ICW).

[0064] Two typical methods for handling a failed decoding process are 1) to request a re-send of the corresponding data or 2) to pass vector \hat{x} to one or more post-processing (PP) methods. Typically, the number *b* of USCs in vector \hat{x} dictates which of these two methods will be used. A large *b* (e.g., greater than 16) is typically handled by a re-send or other post-processing method, while small *b* values are handled by error-floor mitigation post-processing methods.

[0065] BER, SNR, and Error Floors

[0066] The bit-error rate (BER) of an LDPC decoder is a ratio which expresses how many erroneously decoded bits will be generated for x number of bits processed. Thus, for example, a decoder with a BER of 10^{-9} will, on average, generate one erroneous bit for every billion bits processed. The smaller the BER, the better the decoder. The BER of an LDPC decoder increases (worsens) when the decoder fails, i.e., terminates without converging on the decoded correct codeword DCCW.

[0067] The BER of an LDPC decoder is strongly influenced by the signal-to-noise ratio (SNR) of the decoder's input signal. A graph of BER as a function of SNR typically comprises two distinct regions: an initial "waterfall" region where the BER improves (decreases) rapidly given a unit increase in SNR, and a subsequent "error floor" region where unit increases in SNR yield only modest improvements in BER. Thus, achieving significant BER improvements in the error floor region requires methods other than SNR increase.

[0068] One method for improving the error-floor characteristics of an LDPC decoding is to increase the codeword length. However, increasing codeword length also increases the memory and other computing resources required for LDPC decoding. Thus, if such resources are strictly limited, as is typically the case with the read-channel devices on HD drives, then other methods must be found to yield the necessary error-floor improvement.

[0069] Another scarce resource is processing cycles. Typically, to achieve a specified throughput, an HD drive budgets a fixed number of read-channel processing cycles for decoding a codeword. Methods which exceed that budget (i.e., off-the-fly methods) decrease the throughput. More desirable are on-the-fly methods which recover the DCCW within the clock-cycle allotment and thus do not decrease the throughput.

[0070] **Trapping Sets and Dominant Trapping Sets**

[0071] An (a, b) trapping set is a set of b USCs which a decoder cannot satisfy within the maximum number of iterations, and the a erroneous bit nodes (EBNs) associated with those USCs. The majority of trapping sets comprise fewer than five USCs and fewer than ten EBNs. Trapping sets have a significant impact on the error-floor characteristics of an LDPC decoder, i.e., when an LDPC decoder fails to converge on the DCCW, it is often because of a trapping set.

[0072] One way to improve the error-floor characteristics of an LDPC decoder is to (i) examine the USCs in the \hat{x} vector of a failed decoder and identify trapping sets (if any), (ii) identify the EBNs associated with those USCs, (iii) flip one or more EBNs associated with those trapping sets, and (iv) re-start the decoder. In one possible implementation, if an LDPC decoder has just been initialized, i.e., the decoder is in state 0, then flipping an EBN comprises (i) inverting the hard-decision value of that EBN's L_{ch} value, i.e., 1 becomes 0, and vice versa, and (ii) setting the magnitude bits, i.e., the confidence, of that same L_{ch} value to maximum, e.g., all ones. If the decoder is in some state other than state 0, then flipping an EBN comprises (i) determining the hard-decision value of the EBN's P-value (defined by

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Equation 7 above), (ii) setting the hard-decision values of that EBN's L_{ch} value, P-value, and all associated Q_{nm} LLRs to the opposite of the hard-decision value of step (i), and (iii) setting the magnitude bits of that EBN's L_{ch} value, P-value, and all associated Q_{nm} LLRs to maximum. Often, flipping one or two EBNs will "break" the trapping set, and the re-started decoder will converge on the DCCW.

[0073] Different trapping sets, when broken, will yield different improvements in error-floor characteristics. Dominant trapping sets (DTSs) refer to the minimal set of trapping sets, the breaking of which yields a specified improvement in BER/error-floor characteristics. For example, DTS-1 refers to the minimal set of trapping sets which will yield a single order of magnitude improvement in BER, e.g., from 10^{-9} to 10^{-10} , while DTS-3 would yield three orders of magnitude improvement in BER, e.g., 10^{-10} to 10^{-13} .

[0074] List Decoding of Near Codewords

[0075] List decoding is one post-processing method for detecting and breaking trapping sets. In list decoding, an observed trapping set in vector \hat{x} is matched against a list or lists of known trapping sets. A trapping-set list typically contains the indices of all the USCs in each trapping set in the list and the indices of one or more EBNs associated with those USCs. If a trapping set is found in the list which matches the observed trapping set, then the EBN index value(s) are retrieved from the list. Then, those bit nodes are flipped, and the decoding process 300 of FIG. 3 is restarted.

[0076] Trapping-Set Simulation

[0077] The trapping-set list required for list decoding is typically generated off line using software and hardware simulation tools. FIG. 4 is a block diagram of an off-line trapping-set (TS) simulation tool 400 for identifying trapping sets and recording various information about those trapping sets. Tool 400 might be implemented, for example, in a field-programmable gate array (FPGA). LDPC correct codeword (CCW) 402 is sent to channel and signal model 404, which emulates the behavior of noisy channel 114 in FIG. 1. Channel and signal model 404 outputs L_{ch} values 406 to LDPC decoder 408. If LDPC decoder 408 generates a near codeword (NCW) 410, then NCW 410 is sent to syndrome check module 412 and mismatch location recorder 414. Syndrome check 412 outputs the indices 416 of all USCs in NCW 410. Mismatch location recorder 414 compares NCW 410 to CCW 402 and outputs the indices 418 of all EBNs in NCW 410. USC indices 416 plus EBN indices 418 constitute trapping-set (TS) information 420.

[0078] For a given LDPC implementation, all possible trapping sets might number in the millions. However, achieving a significant (i.e., an order of magnitude or more) improvement in the error floor of that implementation typically requires only a subset of all possible trapping sets, i.e., the dominant trapping sets (DTSs). Thus, off-line TS simulation tool 400 includes DTS- N compiler 422, which takes as its input TS information 420 and generates DTS- N information 424.

[0079] DTS-*N* compiler **422** uses a three-step process: collection, ranking, and evaluation. The trapping set collection method utilizes deterministic noise impulses based on the structure of the code graph to detect trapping sets. The collected trapping sets are then ranked by distance-to-error boundary (DEB) values, where trapping sets with low DEB values contribute more to the error floor. Importance sampling is then used to evaluate the trapping sets and confirm the predicted rankings.

[0080] In practice, such FPGA-based offline simulations can take up to a year to perform. For example, to identify the trapping sets that will yield a BER of 10^{-15} for a 4Gb/s HD drive requires running an offline-simulation tool (e.g., tool **400** of **FIG. 4**) for approximately 289 days. Typically, this time constraint is not a problem, as there is often a one- to two-year delay between the final design of an HD drive read channel and the mass-fabrication of chips.

[0081] **Trapping Set Read-Only Memory (TS-ROM)**

[0082] Thus, using an off-line TS simulation tool like tool **400** of **FIG. 4**, it is possible *a priori* to identify one or more trapping sets or dominant trapping sets that will yield an improvement in the error-floor characteristics for a particular LDPC implementation. One way to implement list decoding in a run-time environment is to store offline-generated trapping-set information **420** of **FIG. 4** in a trapping-set read-only memory (TS-ROM) and couple that TS-ROM with a list decoder program. The TS-ROM list decoder program compares the USCs observed in \hat{x} to trapping sets stored in TS-ROM. If a match is found, then the TS-ROM list decoder program flips the appropriate bit-node values in the LDPC decoder and re-starts the decoder.

[0083] Typically, TS-ROM information is stored randomly in a singly- or doubly-linked list, where the list is searched using a brute-force sequential search. Typically, each (a, b) trapping set occupies $(2 + a + b)$ records in the TS-ROM list. Thus, for a (4,4) trapping-set profile (i.e., four USCs and four EBNs), there would be ten records: one record indicating that there are four USCs, followed by four individual USC records, then a record indicating that there are four EBNs, followed by four individual EBN records. The typical TS-ROM list implementation stores approximately 100 trapping sets, and does not store any information about mis-satisfied check nodes.

[0084] For such a TS-ROM implementation to be economically practical, a single TS-ROM must be able to achieve the required error-floor improvement in a large number of implementations. However, trapping sets vary from implementation to implementation, even when the same LDPC code is implemented. For example, even if the LDPC code used on two HD drives were the same, the trapping sets associated with the HD drives may differ. Specifically, research has shown that trapping sets are influenced by an HD drive's jitter profile, inter-symbol interference characteristics, and pulse-shaping scheme. These factors can vary not only between HD drives of different manufacturers, but also between different HD drive models from the same manufacturer and even variations between different production runs of the same model. Thus, trapping sets can vary even between two identical-model hard drives. It is

impractical to simulate the LDPC trapping sets of so many different HD drives. Yet, a TS-ROM loaded with only those trapping sets common to a large class of HD drives might not yield the required level of error-floor improvement when paired with a particular HD drive.

[0085] One method for improving the performance of TS-ROM is to supplement the information generated by an FPGA-based offline-simulation tool (e.g., tool 400 of FIG. 4) with results obtained from test models of the fabricated device. Typically, once a circuit design has been finalized, a limited number of test models of that design will be fabricated and distributed for testing before mass-production commences. While it might take a year to determine the trapping sets which will yield a BER of 10^{-15} for a particular HD drive implementation, it only takes a day to determine the trapping sets which will yield a BER of 10^{-12} . Thus, the test models are run in LDPC test mode for a limited period of time, and any discovered trapping sets are stored. Any discovered trapping sets not already in TS-ROM are added to TS-ROM. By using the actual device that will be distributed to consumers, this method captures trapping sets that may have eluded an FPGA-based offline-simulation tool (e.g., tool 400 of FIG. 4).

[0086] **Trapping Set Random-Access Memory (TS-RAM)**

[0087] One run-time alternative to the static trapping-set list of TS-ROM is to store trapping-set information in a trapping-set random-access memory (TS-RAM) and turn the off-line trapping-set simulation tool 400 of FIG. 4 into a run-time trapping-set collection and analysis tool running on the actual, individual device (e.g., an HD drive). Instead of receiving initial values from a channel and signal model (e.g., model 404 of FIG. 4), the run-time tool would process the actual signal of that particular device. The run-time tool would include list-decoder functionality; i.e., it would attempt to match observed USCs to stored trapping-set information in TS-RAM, and, if a match were found, use the stored information to change decoder bit-node values and restart the decoder. If a match were not found, then the run-time tool would analyze the observed trapping set, i.e., identify the EBNs associated with the USCs, and determine if the observed trapping set met threshold requirements for storage in TS-RAM (e.g., membership in a DTS- N).

[0088] Theoretically, the TS-RAM tool described above could adapt to the trapping-set profile of any implementation. The reality is that the trapping set/dominant trapping set simulation performed by off-line simulation tool 400 of FIG. 4 is computationally complex. In particular, constructing dominant trapping sets out of possibly millions of trapping sets is especially complex. This complexity makes the TS-RAM tool described above unsuitable for most HD drives. Typically, HD drives output data at high rates (e.g., 4 gigabits per second) and demand very low BER/error-floor rates (e.g., 10^{-13} to 10^{-15}), but offer only modest computing resources in their firmware.

[0089] Furthermore, the TS-RAM tool, like the off-line simulation tool 400 of FIG. 4, requires the correct codeword (CCW) to generate EBN indices. CCWs are readily available in the off-line simulation environment, but not in the run-time environment.

[0090] According to certain embodiments of the present invention, methods are performed for the organization of stored trapping-set profiles in ROM. Trapping-set profiles are ranked by dominance, i.e., by their impact on the error-floor characteristics of an LDPC decoder. More-dominant trapping-set profiles contain information about both unsatisfied check nodes (USCs) and mis-satisfied check nodes (MSCs), while less-dominant trapping-set profiles contain only information about USCs. Trapping-set profile information is then organized into a number of linked, hierarchical data tables which allow for the rapid location and retrieval of most-dominant matching trapping-set profiles using a pointer-chase search.

[0091] According to certain embodiments of the present invention, efficient run-time methods are performed for the collection and identification of dominant trapping-sets in RAM. Newly-discovered trapping sets are stored in RAM, if possible, and then sorted or ranked on any one or more of the following factors: number of times RAM has been searched since a trapping set was last matched; total number of times a trapping set has been matched since it was added to RAM; number of unsatisfied check nodes; and number of erroneous bit nodes. Low-ranked trapping-set profiles are deleted from RAM to make space for newly-discovered trapping-set profiles. Thus, in addition to or instead of using a high-computational-complexity offline method for the *a priori* identification of dominant trapping sets, such as that used in DTS-*N* compiler 422 of FIG. 4, these embodiments of the present invention perform low-computational-complexity *a posteriori* methods wherein as many newly-discovered trapping sets are stored as possible, and non-dominant trapping-set profiles winnowed out by periodic ranking and deletion.

[0092] Embodiments of the present invention typically are on-the-fly methods, i.e., they are able to recover the DCCW within the clock-cycles budgeted for LDPC decoding, and thus do not negatively impact system throughput.

[0093] FIG. 5 is a block diagram of an LDPC decoding system 500 according to one embodiment of the present invention. In an HD drive of the present invention analogous to prior-art HD drive 100 of FIG. 1, LDPC decoding system 500 of FIG. 5 would be implemented as part of an LDPC decoder analogous to LDPC decoder 112 of FIG. 1. To that extent, the input L_{ch} values of FIG. 5 are analogous to the decoder input L_{ch} values of FIG. 1, and the output \hat{x}_{pp} vector of FIG. 5 is analogous to the decoded information word of FIG. 1.

[0094] LDPC decoder 502 receives L_{ch} values, performs LDPC decoding process 300 of FIG. 3, and outputs vector \hat{x} to post-processor 504 and TS-RAM updater 506. Post-processor 504 is connected to post-processing (PP) methods list 508, which is a memory that contains one or more executable programs representing post-processing methods, e.g., TS-ROM list decoding, TS-RAM list decoding, etc. If post-processor 504 needs to perform a particular PP method, post-processor 504 reads the executable program from PP methods list 508 and runs that program. Post-processor 504 might perform any number

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of these PP methods in parallel or serially. Post-processor **504** outputs vector \hat{x}_{pp} , which, in addition to being output from LDPC decoding system **500**, is also sent to TS-RAM updater **506**.

[0095] The Data Tables

[0096] During execution, a particular PP method might need to access data structures separate from the PP method executable program code. In particular, TS-ROM and TS-RAM list-decoding methods access one or more lists of trapping-set information stored in TS-ROM **510** and TS-RAM **520**, respectively.

[0097] In the exemplary embodiment of **FIG. 5**, TS-ROM **510** comprises four tables: B-Table **512**, P-Table **514**, E-Table **516**, and EI-Table **518**. TS-RAM **520** comprises two tables, RAM P-Table **522** and RAM Index **524**. A table is a two-dimensional matrix of digital data organized into one or more equally sized rows (records) and one or more equally sized columns (fields). The records of a table are ordinarily numbered from top to bottom beginning with zero. This number is the record number.

[0098] P-Tables **514** and **522** contain information regarding USCs and their related EBNs. B-Table **512** contains pointer information for ROM P-Table **514**. EI-Table **518** contains information regarding MSCs, and E-Table **516** contains pointer information for EI-Table **518**. RAM Index Table **524** contains pointer information for RAM B-Table **522**.

[0099] **FIG. 6** is an exemplary layout of ROM P-Table **514** of **FIG. 5**. ROM P-Table **514** contains trapping-set profile information, i.e., USC and EBN indices. ROM P-Table **514** comprises a number of records (rows), one for each USC of each stored trapping set. Record number **602** is the ordinal location of a record in P-Table **514**, beginning with 0.

[00100] Each record in ROM P-Table **514** comprises three fields: LAYER **604**, USC_INDEX **606**, and EBN_INDEX **608**. Some LDPC decoders are configured to execute a set of update operations in parallel, otherwise known as a layer. LAYER **604** indicates the number of the decoding layer that contained the USC. USC_INDEX **606** contains the index of the USC. EBN_INDEX **608** contains the indices of one or two EBNs associated with the USC.

[00101] ROM P-Table **514** is sorted first on b (i.e., the number of USCs in \hat{x}), e.g., all trapping sets with $b = 2$ come first, followed by all $b = 3$ trapping sets, etc. Thus, there will be two records for each trapping set (e.g., **610**, **612**) in the $b = 2$ range, eventually followed by three-record sets for trapping sets with $b = 3$ (e.g., **614**, **616**), four-record sets for trapping sets with $b = 4$ (**618**, **620**), and so forth.

[00102] Within each b range, trapping sets are sorted by dominance, i.e., the effect that the trapping set has on error-floor characteristics. Those trapping sets which have a greater effect on error-floor characteristics occur at the beginning of the b range, and those which have a lesser effect occur near the end. The records for a particular trapping set are then sorted by USC_INDEX **606**.

[00103] **FIG. 7** is an exemplary layout of B-Table **512** of **FIG. 5**. B-Table **512** contains, for each b value in ROM P-Table **514**, pointers to the first occurrences of that b value in ROM P-Table **514** and in

E-Table **516**, and the number of records in E-Table **516** for that b value. Thus, there is a single record in B-Table **512** for each b value, where the b value is indicated by record number **702**. However, records numbers **702** start with 0, while b values typically start at two or higher. Thus, in this exemplary embodiment of the present invention, an offset is added to record number **702** to yield the corresponding b value. For example, if only trapping sets with $b \geq 2$ are stored, then an offset of 2 would be added to each record number to arrive at the corresponding b value.

[00104] Field PTABLE_START_OFFSET **704** contains the location of the first occurrence of a particular b value in ROM P-Table **514**. Field ETABLE_START_OFFSET **706** contains the location of the first occurrence of a particular b value in E-Table **516**. Field NUM_ETABLE_ENTRIES **708** contains the number of records in E-Table **516** for this particular b value.

[00105] FIG. 8 is an exemplary layout of E-Table **516** of FIG. 5. E-Table **516** contains pointers to MSC records in EI-Table **518**. Each record in E-Table **516** has a record number **802**, an EITABLE_START_ADDRESS field **804**, and an EITABLE_END_ADDRESS field **806**. EITABLE_START_ADDRESS field **04** contains a pointer to the first occurrence of the corresponding data in EI-Table **518**, and EITABLE_END_ADDRESS field **806** contains a pointer to the last occurrence of the corresponding data in EI-Table **518**.

[00106] FIG. 9 is an exemplary layout of EI-Table **518** of FIG. 5. EI-Table **518** stores the indices of EBNs associated with MSCs. Each record in EI-Table **518** has a record number **902** and contains two fields: BLOCK_COLUMN field **904** and B_INDEX field **906**. BLOCK_COLUMN field **904** indicates the block column where the EBN is located, and B_INDEX field **906** is the index of the EBN.

[00107] FIG. 10 is an exemplary layout of RAM P-Table **522** of FIG. 5. RAM P-Table **522** stores the profiles of newly-identified trapping sets that are not found in ROM P-Table **514**. Each row (i.e., record) in RAM P-Table **522** has a record number **1002** and comprises two fields: two-bit TAG field **1004** and R_WORD field **1006**. The four possible values of TAG field **1004** indicate the record type and the structure of data within R_WORD field **1006**. If TAG field **1004** has a value of 11, then the record is a primary record that contains information pertaining to an entire trapping set. If TAG field **1004** has a value of 10, then the record is a secondary record and contains information pertaining to a particular USC within a trapping-set profile. If TAG field **1004** has a value of 00 or 01, then the R_WORD field **1006** is empty, i.e., this record is available to store the profile information for newly-identified trapping sets. A trapping-set profile typically comprises a single primary record followed by b secondary records.

[00108] If the record is a primary record, then R_WORD field **1006** contains four sub-fields: (i) b -value subfield **1008**, (ii) a -value subfield **1010**, which records the number of trapping set EBNs, (iii) LAST_HIT_NUM subfield **1012**, which indicates the number of the TS-RAM search which last matched this trapping set, and (iv) HIT_COUNTER subfield **1014**, which records how many times this particular trapping-set profile has been matched to an observed trapping set since this trapping set was stored in TS-

RAM.

[00109] If a record is a secondary record, then R_WORD field **1006** contains the layer (LAYER field **1016**) and index (USC_INDEX field **1018**) of a single USC within a trapping set, and the indices (EBN_INDEX field **1020**) of one or more EBNs associated with that USC.

[00110] **FIG. 11** is an exemplary layout of RAM Index Table **524** of **FIG. 5**. There is a record in RAM Index Table **524** for each trapping set profile in RAM P-Table **522**. Each record in RAM Index Table **524** comprises a single field, RAM_PTABLE_OFFSET **1102**. RAM_PTABLE_OFFSET **1102** is a pointer to the start of a particular trapping-set profile in RAM P-Table **524**, i.e., RAM_PTABLE_OFFSET **1102** contains the record number **1002** of **FIG. 10** of a trapping-set profile primary record. The records in RAM Index Table **524** are sorted by dominance, so that the first record in RAM Index Table **524** points to the most-dominant trapping set in RAM P-Table **522**, and the last record in RAM Index **524** points to the least-dominant record in RAM P-Table **522**.

[00111] **FIG. 12** is a flowchart of exemplary process **1200** used by LDPC decoding system **500** of **FIG. 5**. Processing starts at step **1202** and proceeds to step **1204**, LDPC decoding of L_{ch} values by LDPC decoder **502** of **FIG. 5**. If the LDPC decoding at step **1204** yields the DCCW, then process **1200** terminates at step **1218**. Otherwise, processing proceeds to step **1206**, TS-ROM list decoding (performed by post-processor **504** of **FIG. 5**).

[00112] If step **1206** yields the DCCW, then process **1200** terminates at step **1218**. Otherwise, processing proceeds to step **1208**, TS-RAM list decoding (performed by post-processor **504** of **FIG. 5**). If step **1208** yields the DCCW, then process **1200** terminates at step **1218**. Otherwise, processing proceeds to one or more additional post-processing methods **1210**, **1212**, ..., **1214** (performed by post-processor **504** of **FIG. 5**), which operate in an analogous manner.

[00113] If TS-RAM list decoding **1208** or any of the additional post-processing methods **1210**, **1212**, ..., **1214** yields the DCCW, then processing proceeds to step **1216**, where TS-RAM **520** of **FIG. 5** is possibly updated by TS-RAM updater **508**. Processing then terminates at step **1218**.

[00114] **FIG. 1200** displays one possible sequencing of post-processing methods **1207** – **1214**.

Almost any sequence of post-processing methods could be employed, although some sequences are more practical than others. For example, it is desirable to sequence TS-ROM list decoding before TS-RAM list decoding to ensure that trapping sets already stored in ROM are not duplicated in RAM.

[00115] TS-ROM List Decoding

[00116] **FIG. 13** is a flowchart of exemplary TS-ROM list-decoding process **1206** of **FIG. 12** implemented by post-processor **504** of **FIG. 5**. Processing starts at step **1302** and proceeds to step **1304**, where process **1206** determines if the number $b_{observed}$ of USCs observed in the vector \hat{x} received from LDPC decoder **1204** of **FIG. 12** is greater than 0 and less than the maximum number b_{max} of USCs that

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can be efficiently handled by process **1206**. If $b_{observed} = 0$, then there are no USCs in vector \hat{x} (i.e., \hat{x} is a near-codeword mis-correction), and hence there is no trapping set to match. If step **1304** evaluates false, then process **1206** terminates. Otherwise, processing continues to step **1306**.

[00117] At step **1306**, the current state of the decoder is stored and labeled State 1. Processing then continues to step **1308**, where the observed USCs are sorted, first by decoding layer, then by index. Next, at step **1310**, the following four values are fetched from B-Table **512** of **FIG. 5** and stored:

- (1) PTABLE_START_OFFSET field **704** of **FIG. 7** for $b = b_{observed}$;
- (2) PTABLE_START_OFFSET field **704** of **FIG. 7** for $b = b_{observed} + 1$;
- (3) ETABLE_START_OFFSET field **706** of **FIG. 7** for $b = b_{observed}$; and
- (4) NUM_ETABLE_ENTRIES field **708** of **FIG. 7** for $b = b_{observed}$.

The first value instructs process **1206** where to begin its search for matching trapping-set information (i.e., USC and EBN indices) in P-Table **514** of **FIG. 5**, and the second value instructs process **1206** when to end its search. Similarly, the third and fourth values instruct process **1206** where to begin and end its search for extended information (i.e., MSC indices).

[00118] Thus, for example, if $b_{observed} = 5$, then process **1206** fetches the values of PTABLE_START_OFFSET field **704** of **FIG. 7** for $b = 5$ and $b = 6$, and the values of ETABLE_START_OFFSET field **706** of **FIG. 7** and NUM_ETABLE_ENTRIES field **708** of **FIG. 7** for $b = 5$.

[00119] Next, at step **1312**, process **1206** selects P-Table **514** of **FIG. 5** and goes to the address indicated by the stored value of PTABLE_START_OFFSET for $b = b_{observed}$. Next, at step **1314**, TS-ROM is searched for a trapping set which matches the observed USCs.

[00120] **FIG. 14** is a flowchart of exemplary TS-ROM search process **1314** of **FIG. 13**. Process **1314** starts at step **1402** and, at step **1404**, searches for the next record in P-Table **514** of **FIG. 5** which is an isomorphic match for the observed USCs. An isomorphic match for a particular set of observed USCs would be a trapping set where the number of USCs and distances between those USCs are the same as the observed USCs. Thus, if the observed USCs are [1,3,10], then [1,3,10] is a match, and [2,4,11] is an isomorphic match, as are [3,5,12], [4,6,13], and so forth. If no match is found, then process **1314** terminates with a status of no match **1406**.

[00121] If, instead, a match is found at step **1404**, then, at step **1408**, the value of EBN_INDEX field **608** of **FIG. 6** of the matching P-Table record is stored. The EBN_INDEX field contains the indices of one and perhaps two erroneous bit nodes associated with this matched trapping set.

[00122] Next, process **1314** attempts to locate any extended information, i.e., the indices of EBNs associated with mis-satisfied check nodes (MSCs) in this matching trapping set. Extended information is

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kept in EI-Table 518. However, extended information is not kept for all trapping sets stored in P-Table 514, but only for a subset of trapping sets in each b range. That subset corresponds to the more-dominant trapping sets in a particular b range, i.e., those trapping sets which have a more-significant impact on error-floor characteristics. As discussed above, in P-Table 514, the trapping sets within a particular b range are sorted by dominance; thus, extended information is kept only for the first x records within that b range. The beginning and end of each b range in EI-Table 518 is indicated by the fields ETABLE_START_OFFSET 706 and NUM_ETABLE_ENTRIES 708 in B-Table 512.

[00123] Process 1314 maintains an internal count of trapping sets as it searches through the records of ROM P-Table 514. Thus, for example, if process 1314 were searching through $b = 2$ trapping sets in P-Table 514 of FIG. 6, process 1314 would identify records 0 and 1 as trapping set 0 (e.g., trapping set 610 of FIG. 6), records 2 and 3 as trapping set 1 (e.g., trapping set 612 of FIG. 6), and so forth. This trapping-set number is referred to as TSNUM.

[00124] At step 1410, TSNUM is compared to the value of NUM_ETABLE_ENTRIES field that was stored in step 1310 of FIG. 13. If TSNUM is greater than the value of NUM_ETABLE_ENTRIES, then no extended information is available, and process 1314 terminates with a status of match, no extended information 1412.

[00125] If, instead, at step 1410, TSNUM is found to be less than or equal to the stored value of NUM_ETABLE_ENTRIES, then extended information exists for this matched trapping set. In step 1414, TSNUM is added to the stored value of ETABLE_START_OFFSET to yield variable ETABLE_ENTRY_ADDRESS.

[00126] Next, at step 1416, process 1314 selects E-Table 516 of FIG. 5, goes to the record with an address equal to the value of variable ETABLE_ENTRY_ADDRESS, and stores the values of EITABLE_START_ADDRESS field 804 of FIG. 8 and EITABLE_END_ADDRESS field 806 of FIG. 8.

[00127] Next, at step 1418, process 1314 selects EI-Table 518 of FIG. 5, and stores the values of the BLOCK_COLUMN fields 904 of FIG. 9 and B_INDEX fields 906 of FIG. 9 of every record between the stored EITABLE_START_ADDRESS and EITABLE_END_ADDRESS values. Finally, process 1314 exits with a status of match with extended information 1420.

[00128] Returning to FIG. 13, if step 1314 terminates with a status of no match, then process 1206 terminates at step 1316.

[00129] If step 1314 terminates with a status of match, no extended information, then process 1206 possesses the USC indices and some of the EBN indices associated with this trapping set, but no extended information (i.e., indices of EBNs associated with MSCs). In this case, step 1318 flips the bit nodes at those EBN indices, and iterative LDPC decoding is performed at step 1320. The process of step 1320 is the same as process 300 of FIG. 3 except that decoder initialization step 304 and initial syndrome

check step 306 are skipped. If step 1320 converges on the DCCW, then process 1206 terminates at step 1316. Otherwise, at step 1322, the decoder is restored to State 1, and a next matching trapping set is sought at step 1314.

[00130] If step 1314 terminates with a status of match with extended information, then process 1206 possesses the indices of all the EBNs associated with the matched trapping set. In this case, it is not necessary to perform belief propagation (e.g., steps 310 and 312 of FIG. 3). Instead, at step 1324, the EBNs are flipped, and the resulting vector \hat{x} is submitted to a syndrome check 1326. If vector \hat{x} fails the syndrome check at step 1326, then process 1206 proceeds to step 1322. If, instead, vector \hat{x} passes the syndrome check (i.e., vector \hat{x} is a valid codeword), then, at step 1328, a CRC check is performed on vector \hat{x} to determine if it is in fact the correct codeword. If vector \hat{x} passes CRC check 1328 (i.e., vector \hat{x} is the DCCW), then process 1206 terminates at step 1316. If vector \hat{x} fails CRC check 1328, then process 1206 proceeds to step 1322.

[00131] TS-RAM List Decoding

[00132] Another PP method utilized by post-processor 504 of FIG. 5 is TS-RAM list decoding 1208 of FIG. 12, i.e., list decoding of trapping sets using trapping-set information stored in volatile memory, such as random-access memory. TS-RAM list decoding is similar to TS-ROM list decoding in that RAM P-Table 522 of FIG. 5 stores USC and EBN information for selected trapping sets. However, unlike ROM P-Table 514, RAM P-Table 522 is altered during run-time by TS-RAM updater 506 of FIG. 5. Hence, only the most-important information is stored, e.g., USC and EBN indices. No extended information (e.g., EI-Table 518 of FIG. 5) is maintained in TS-RAM.

[00133] Nor are the profiles in RAM P-Table 522 sorted in any fashion. Instead, a separate RAM Index Table 524 of FIG. 16 maintains a list of the addresses of the trapping-set profiles stored in RAM P-Table 522, sorted by dominance.

[00134] FIG. 15 is a flowchart of exemplary TS-RAM list-decoding process 1208 of FIG. 12. Processing begins at step 1502 and proceeds to step 1504, which is identical in purpose and operation to step 1304 of FIG. 13. If step 1504 evaluates false, then process 1208 terminates at step 1506; otherwise, processing continues to step 1508, where the current decoder state is recorded and labeled State 1. Processing then continues to step 1510.

[00135] At step 1510, process 1208 goes to the most-dominant trapping-set profile in RAM P-Table 522 of FIG. 5. Specifically, since RAM Index Table 524 ranks the profiles in RAM P-Table 522 by dominance, process 1208 goes to the first record in RAM Index Table 524 and retrieves the value of RAM_PTABLE_OFFSET field 1102 of FIG. 11. Then, process 1208 moves the pointer in RAM P-Table 522 to that stored offset value.

[00136] At step 1512, process 1208 increments global variable RAM_SEARCH_COUNT which keeps track of the total number of TS-RAM searches performed, i.e., the total number of times process

1208 has been executed. Also, at step **1512**, process **1208** examines the profiles in RAM P-Table **522**, in the order indicated by RAM Index Table **524**, i.e., in order of decreasing dominance, for an isomorphic match for the observed USCs. If no match is found, then processing continues to step **1514**.

[00137] If, instead, at step **1512**, a match is found, then, at step **1516**, the LAST_HIT_NUM field **1012** of **FIG. 10** of the matched profile is set to the value of global variable RAM_SEARCH_COUNT, and the HIT_COUNTER field **1014** of **FIG. 10** is incremented by 1. Then, at step **1518**, the values of EBN_INDEX fields **1020** of **FIG. 10** are stored. Step **1520** flips the bit nodes located at the EBN_INDEX values, and, at step **1522**, LDPC decoding is performed. Step **1522** is identical to step **1320** of **FIG. 13**. If decoding process **1522** converges on the DCCW, then processing continues to step **1514**; otherwise, at step **1524**, the decoder is reset to State 1, and processing then continues to step **1512** where another isomorphic match is sought in P-Table **522**.

[00138] At step **1514**, process **1208** updates RAM Index Table **524** of **FIG. 11**. Specifically, step **1514** sorts all TS-RAM profiles in RAM P-Table **522** on any combination of fields in RAM P-Table **522**, e.g., LAST_HIT_NUM **1012**, HIT_COUNTER field **1014**, number of USC nodes field **1008**, and number of EBNs field **1010**. Then the addresses of all the sorted profiles, i.e., record numbers **1002** of all primary records, are stored as records in RAM Index Table **524** of **FIG. 11**. The profile addresses are stored in RAM Index Table **524** in the same order in which they were sorted in step **1514** (e.g., from most dominant to least dominant).

[00139] Once step **1514** has completed, processing terminates at step **1506**.

[00140] TS-RAM Updater

[00141] As explained in the discussion of process **1200** of **FIG. 12**, if any post-processing method other than TS-ROM list decoding **1206** arrives at the DCCW, that might mean that a new trapping set has been discovered. If so, then step **1216** might attempt to add that new trapping set to RAM P-Table **522** of **FIG. 5**.

[00142] In one embodiment, step **1216** is a low-complexity process for retaining dominant trapping sets in TS-RAM **520**. Specifically, in this embodiment, step **1216** does not perform exhaustive calculations to determine dominant trapping sets *a priori*, such as the calculations performed by DTS-*N* compiler **422** of **FIG. 4**, but instead (i) ranks TS-RAM trapping sets on any combination of one or more factors, e.g., how many times TS-RAM has been searched since the trapping set was last matched, the total number of times a trapping set has been matched, the number of USCs, the number of EBNs, etc., and then (ii) purges the lowest-ranked trapping sets to make space for newly-discovered trapping sets. Ranking trapping sets in TS-RAM **520** using these factors is typically considerably less complex than the analysis performed by off-line simulation tools (e.g., compiler **422** of **FIG. 4**).

[00143] **FIG. 16** is a flowchart of exemplary TS-RAM update process **1216** of **FIG. 12**. Processing starts at step **1602** and proceeds to step **1604** where it is determined whether a DCCW was generated by

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TS-RAM list-decoding process **1208** of **FIG. 12**. If so, then no trapping-set profile needs to be added to TS-RAM, and process **1216** terminates at step **1608**.

[00144] If, instead, step **1604** evaluates no/false, then it means that some post-processing method other than TS-ROM or TS-RAM list decoding arrived at the DCCW, and thus a new trapping set has been discovered and should be appended to RAM. At step **1610** the trapping-set profile is generated. A trapping-set profile comprises the indices of the trapping-set USBs, and the indices of the EBNs associated with those USBs. The USB indices have already been generated by LDPC decoder **502** of **FIG. 5**. To generate the EBN indices, step **1610** compares the DCCW \hat{x}_{pp} generated by post-processor **504** to vector \hat{x} generated by LDPC decoder **502**.

[00145] At step **1612**, it is determined whether there is enough free space to append the new trapping-set profile. If so, then, at step **1614**, the new trapping-set profile is appended to RAM P-Table **522**, and process **1216** proceeds to step **1616**.

[00146] If, however, at step **1612**, there is not enough free space in RAM P-Table **522** to append the new trapping-set profile, then, at step **1618**, the lowest-ranked purge-eligible trapping-set profile is purged. In this example, the purge-eligibility of a profile is determined by the number of times RAM has been searched since that profile was last matched, i.e., the value of global variable RAM_SEARCH_COUNT less the value of the profile's LAST_HIT_NUM field. If the number of intervening searches is greater than a specified threshold, then the profile is purge-eligible. Assuming that all profiles are ranked first by purge-eligibility, all purge-eligible records will be at the end of RAM Index Table **524** of **FIG. 11**.

[00147] Thus, at step **1618**, the last record in index RAM Index Table **524** is selected, and the value of RAM_PTABLE_OFFSET field **1102** is retrieved. If the profile located in RAM P-Table **522** at the stored offset value (indicated by the retrieved RAM_PTABLE_OFFSET value) is purge-eligible, then the primary record and associated secondary records located at that stored offset value in RAM P-Table **522** are deleted. At step **1620**, RAM Index Table MSB is updated, and control then loops back to step **1612**, where it is determined whether there is enough free space in RAM P-Table **522** to append the new trapping-set profile. The processing of step **1620** is identical to the processing of step **1514** of **FIG. 15**.

[00148] If, instead, at step **1618**, the lowest-ranked profile is not purge-eligible, then processing continues to step **1616**. At step **1616**, RAM Index Table **523** is updated, and processing terminates at step **1608**. The processing of step **1616** is identical to the processing of step **1514** of **FIG. 15**.

[00149] Although the present invention has been described in the context of hard disk drives that implement LDPC coding and decoding, the invention is not so limited. In general, the present invention can be implemented in any suitable communication path that involves LDPC coding and decoding.

[00150] Further, although the exemplary belief-propagation algorithm used above is the offset min-sum algorithm (OMS), the present invention is not so limited, and can be used with any belief-

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propagation variant, e.g., sum-product algorithm (SPA) or the Bahl-Cocke-Jelinek-Raviv (BCJR) algorithm.

[00151] Yet further, although the belief-propagation example used above employed a specific decoding schedule (flooding schedule) where all check nodes were updated during a single check-node update step, followed by all bit nodes being updated in a single bit-node update step, the present invention is not so limited, and can be used with any decoding schedule, e.g., row-serial schedule, column-serial schedule, and row-column serial schedule.

[00152] Yet further, although the exemplary LDPC decoder used above was a non-layered decoder, the present invention is not so limited, and can be used with both layered and non-layered decoders.

[00153] Yet further, although the exemplary TS-RAM implementation given above assumed storing trapping-set profiles in RAM within the read channel of an HD drive, the present invention is not so limited. A RAM P-Table (e.g., 522 of FIG. 5) can also be stored on the platters of an HD drive, or stored in a separate memory such as flash memory.

[00154] Yet further, although the exemplary TS-ROM implementation given above is described in the context of read-only memory, the present invention is not so limited. In general, the term "ROM" as used in both the specification and the claims should be interpreted to refer to any data-storage device storing static TS-profile data, whether or not the data in that device is capable of being modified.

[00155] Yet further, although embodiments of the present invention have been described in the context of LDPC codes, the present invention is not so limited. Embodiments of the present invention could be implemented for any code which can be defined by a graph, e.g., tornado codes, structured IRA codes, since it is graph-defined codes which suffer from trapping sets.

[00156] Although the present invention was described in terms of receiving log-likelihood ratios, the present invention is not so limited. Embodiments of the present invention may be envisioned in which other soft values such as likelihood ratios or hard-decision values are processed.

[00157] The present invention can be embodied in the form of methods and apparatuses for practicing those methods. The present invention can also be embodied in the form of program code embodied in tangible media, such as magnetic recording media, optical recording media, solid state memory, floppy diskettes, CD-ROMs, hard drives, or any other machine-readable storage medium, wherein, when the program code is loaded into and executed by a machine, such as a computer, the machine becomes an apparatus for practicing the invention. The present invention can also be embodied in the form of program code, for example, whether stored in a storage medium, loaded into and/or executed by a machine, or transmitted over some transmission medium or carrier, such as over electrical wiring or cabling, through fiber optics, or via electromagnetic radiation, wherein, when the program code is loaded into and executed by a machine, such as a computer, the machine becomes an apparatus for practicing the invention. When implemented on a general-purpose processor, the program code segments combine with

the processor to provide a unique device that operates analogously to specific logic circuits.

[00158] Unless explicitly stated otherwise, each numerical value and range should be interpreted as being approximate as if the word "about" or "approximately" preceded the value of the value or range.

[00159] It will be further understood that various changes in the details, materials, and arrangements of the parts which have been described and illustrated in order to explain the nature of this invention may be made by those skilled in the art without departing from the scope of the invention as expressed in the following claims.

[00160] The use of figure numbers and/or figure reference labels in the claims is intended to identify one or more possible embodiments of the claimed subject matter in order to facilitate the interpretation of the claims. Such use is not to be construed as necessarily limiting the scope of those claims to the embodiments shown in the corresponding figures.

[00161] It should be understood that the steps of the exemplary methods set forth herein are not necessarily required to be performed in the order described, and the order of the steps of such methods should be understood to be merely exemplary. Likewise, additional steps may be included in such methods, and certain steps may be omitted or combined, in methods consistent with various embodiments of the present invention.

[00162] Although the elements in the following method claims, if any, are recited in a particular sequence with corresponding labeling, unless the claim recitations otherwise imply a particular sequence for implementing some or all of those elements, those elements are not necessarily intended to be limited to being implemented in that particular sequence.

[00163] Reference herein to "one embodiment" or "an embodiment" means that a particular feature, structure, or characteristic described in connection with the embodiment can be included in at least one embodiment of the invention. The appearances of the phrase "in one embodiment" in various places in the specification are not necessarily all referring to the same embodiment, nor are separate or alternative embodiments necessarily mutually exclusive of other embodiments. The same applies to the term "implementation."

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CLAIMS

We claim:

1. A method for decoding encoded data encoded with a graph-based code, the method comprising:
 - (a) performing decoding on the encoded data to generate a candidate decoded codeword; and
 - (b) performing, if the candidate decoded codeword is not a decoded correct codeword, a trapping-set (TS)-RAM list-decoding method to attempt to generate the decoded correct codeword, wherein the TS-RAM list-decoding method accesses one or more TS profiles stored in RAM memory, each TS profile corresponding to a different trapping set.
2. The invention of claim 1, further comprising:
 - (c) updating the RAM memory to store a new TS profile.
3. The invention of claim 2, wherein:

if the TS-RAM list decoding fails to generate the decoded correct codeword, then step (b) further comprises performing an other decoding method to attempt to generate the decoded correct codeword; and

if the other decoding method generates the decoded correct codeword, then step (c) comprises generating the new TS profile based on the candidate decoded codeword and the decoded correct codeword.
4. The invention of claim 2, wherein step (c) comprises:
 - (c1) selecting, for purging, one or more TS profiles previously stored in the RAM memory;
 - (c2) purging the selected one or more TS profiles from the RAM memory; and
 - (c3) storing the new TS profile in the RAM memory.
5. The invention of claim 4, wherein step (c1) comprises selecting a TS profile for purging based on one or more of:
 - (i) a number of times the RAM memory has been searched during previous performances of the TS-RAM list-decoding method since the selected TS profile has been matched during previous performances of the TS-RAM list-decoding method;
 - (ii) a total number of times (e.g., HIT_COUNTER) that the selected TS profile has been matched during previous performances of the TS-RAM list-decoding method since the selected TS profile was stored in the RAM memory;
 - (iii) a number (e.g., b) of unsatisfied check nodes in the selected TS profile; and

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(iv) a number (e.g., a) of erroneous bit nodes in the selected TS profile.

6. The invention of claim 5, wherein step (c1) comprises selecting the TS profile for purging based on the number of times the RAM memory has been searched during previous performances of the TS-RAM list-decoding method since the selected TS profile has last been matched during previous performances of the TS-RAM list-decoding method.

7. The invention of 4, wherein step (c1) comprises searching the stored TS profiles in a sequence specified by a separate RAM Index Table.

8. The invention of claim 1, wherein each TS profile comprises:
a number (e.g., b) of unsatisfied check nodes in the corresponding trapping set;
identification (e.g., USC_INDEX) of each unsatisfied check node in the corresponding trapping set; and
identification (e.g., EBN_INDEX) of at least one erroneous bit node for each unsatisfied check node in the corresponding trapping set.

9. The invention of claim 8, wherein each TS profile further comprises:
a number (e.g., a) of erroneous bit nodes in the corresponding trapping set;
a number of times (e.g., HIT_COUNTER) that the TS profile has been matched during previous performances of the TS-RAM list-decoding method since the TS profile was stored in the RAM memory; and
the number of the most recent performance of the TS-RAM list-decoding method that matched this particular profile.

10. The invention of claim 1, wherein:
if the candidate decoded codeword is not the decoded correct codeword, then the candidate decoded codeword identifies an observed trapping set comprising a set of one or more observed unsatisfied check nodes; and

the TS-RAM list-decoding method comprises:

- (b1) searching through the RAM memory for a stored TS profile that matches the observed trapping set;
- (b2) modifying one or more erroneous bit nodes for the LDPC-encoded data, wherein the one or more modified erroneous bit nodes are identified by the matched TS profile; and
- (b3) performing LDPC decoding on the modified LDPC-encoded data.

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11. The invention of claim 10, wherein the stored TS profile matches the observed trapping set when the one or more unsatisfied check nodes of the stored TS profile form an isomorphic match with the one or more observed unsatisfied check nodes of the observed trapping set.

12. The invention of claim 10, wherein step (b1) comprises searching the stored TS profiles in a sequence specified by a separate RAM Index Table.

13. The invention of claim 1, further comprising:

(c) sorting the TS profiles stored in the RAM memory based on dominance of the corresponding trapping sets.

14. The invention of claim 13, wherein the dominance of a trapping set is based on one or more of:

(i) a number of times (e.g., LAST_HIT_NUM) the RAM memory has been searched during previous performances of the TS-RAM list-decoding method since the corresponding TS profile has been matched during previous performances of the TS-RAM list-decoding method;

(ii) a total number of times (e.g., HIT_COUNTER) that the corresponding TS profile has been matched during previous performances of the TS-RAM list-decoding method since the corresponding TS profile was stored in the RAM memory;

(iii) a number (e.g., b) of unsatisfied check nodes in the trapping set; and

(iv) a number (e.g., a) of erroneous bit nodes in the trapping set.

15. The invention of claim 14, wherein a first trapping set having a first TS profile is more dominant than a second trapping set having a second TS profile if (i) the number of times the RAM memory has been searched during previous performances of the TS-RAM list-decoding method since the first TS profile has been matched during previous performances of the TS-RAM list-decoding method is less than (ii) the number of times the RAM memory has been searched during previous performances of the TS-RAM list-decoding method since the second TS profile has been matched during previous performances of the TS-RAM list-decoding method.

16. The invention of claim 13, further comprising:

(d) storing the addresses of the sorted TS profiles in a separate RAM Index Table such that the order of the addresses in the separate RAM index table is based on the sorting results of step (c).

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17. The invention of claim 1, wherein the graph-based code is a Low-Density Parity Check (LDPC) code.

18. An apparatus for decoding encoded data encoded with a graph-based code, the apparatus comprising:

a decoder adapted to perform decoding on the encoded data to generate a candidate decoded codeword;

RAM memory; and

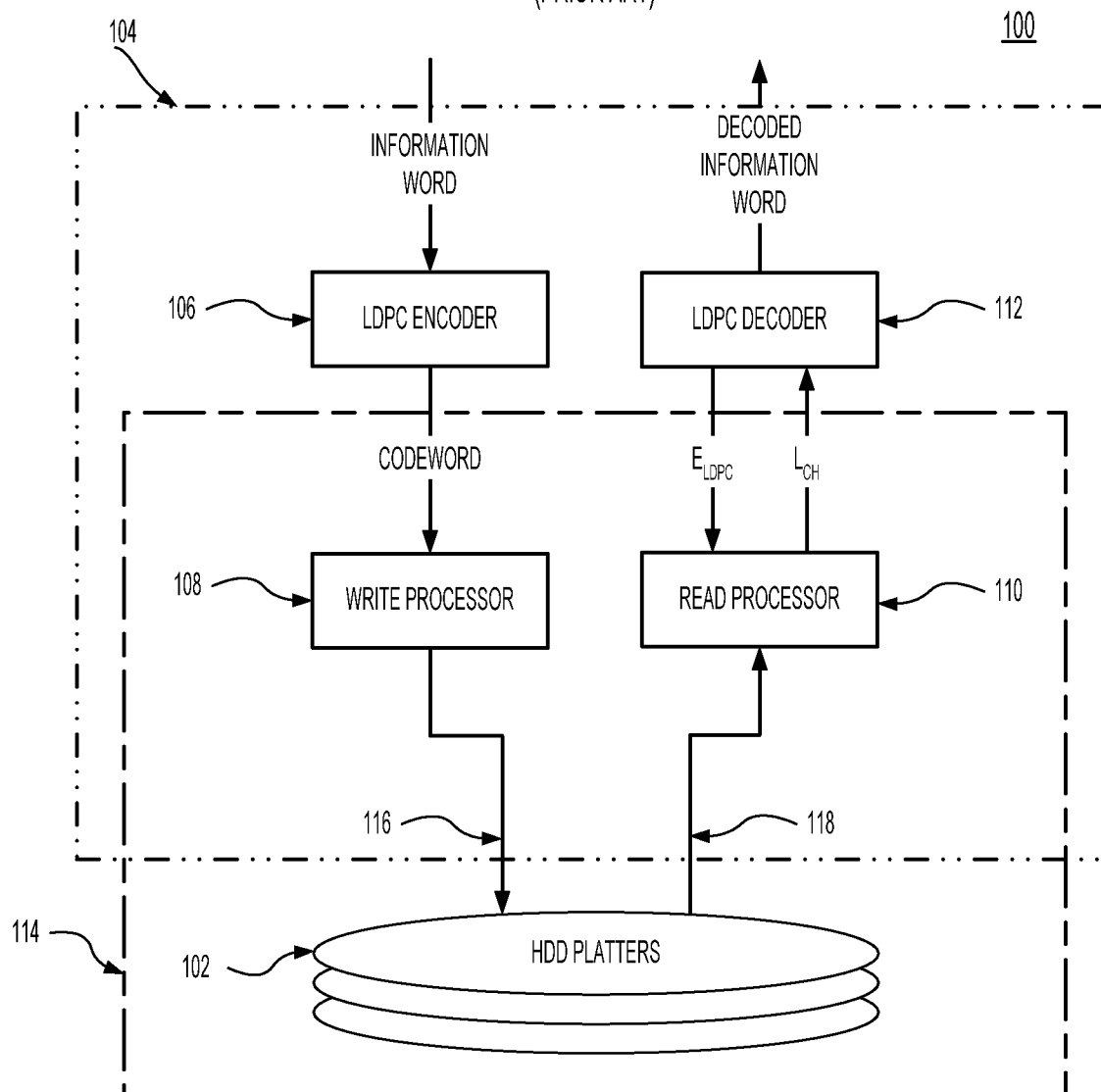
a trapping-set (TS)-RAM list decoder adapted to perform, if the candidate decoded codeword is not a decoded correct codeword, a TS-RAM list-decoding method to attempt to generate the decoded correct codeword, wherein the TS-RAM list decoder accesses one or more TS profiles stored in the RAM memory, each TS profile corresponding to a different trapping set.

19. The invention of claim 18, further comprising:

a TS-RAM updater adapted to update the RAM memory to store a new TS profile.

20. The invention of claim 18, wherein the graph-based code is a Low-Density Parity Check (LDPC) code.

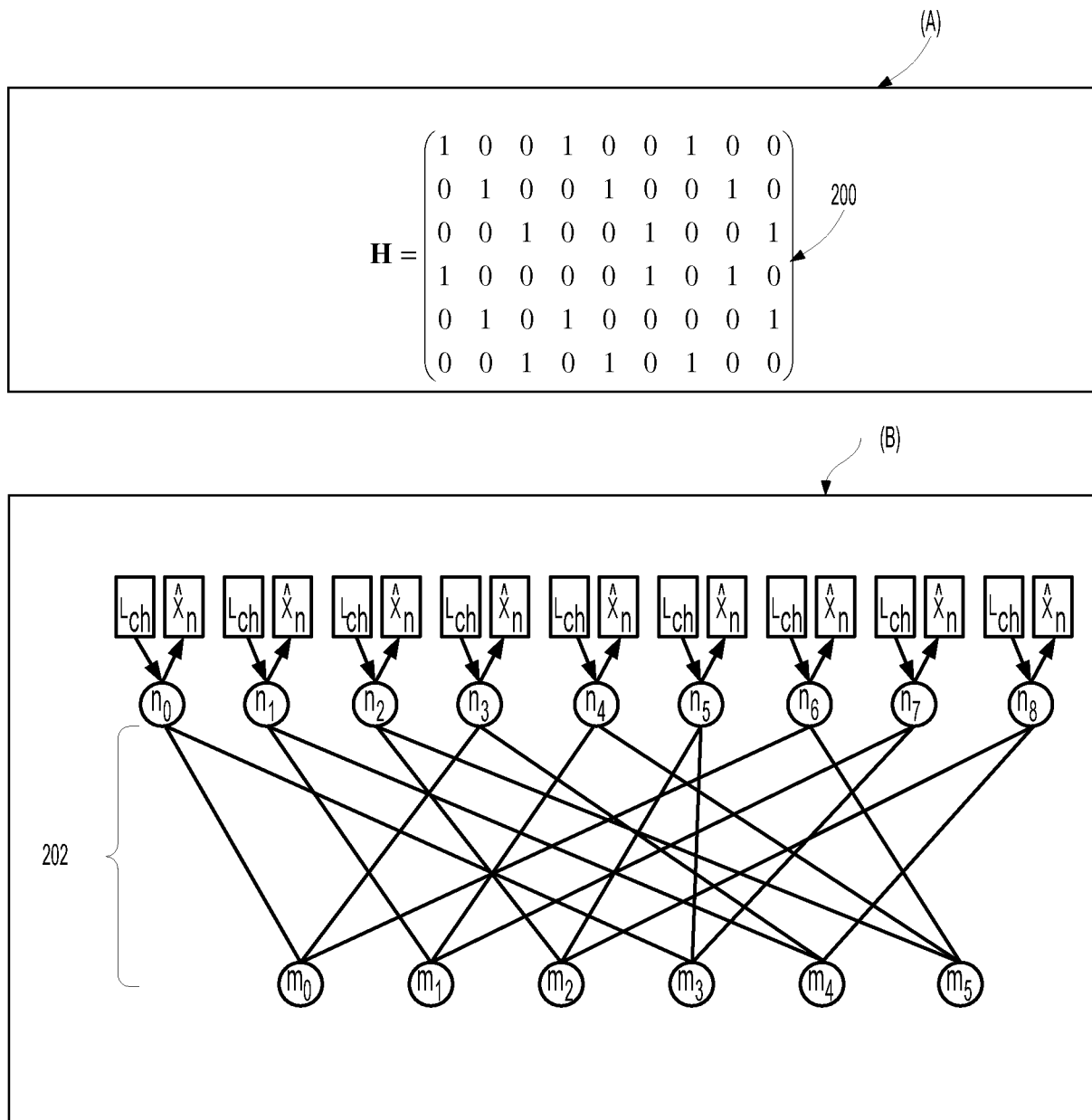
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FIG. 1
(PRIOR ART)

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FIG. 2

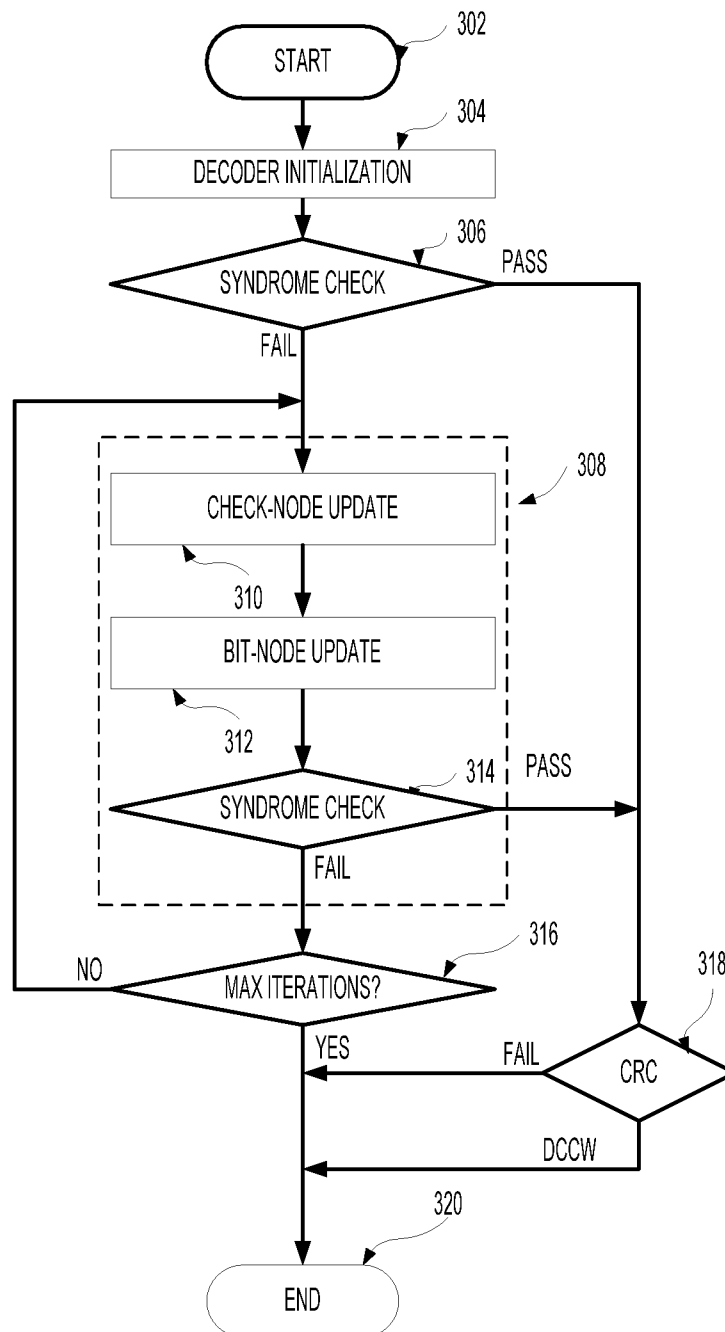
(PRIOR ART)



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FIG. 3

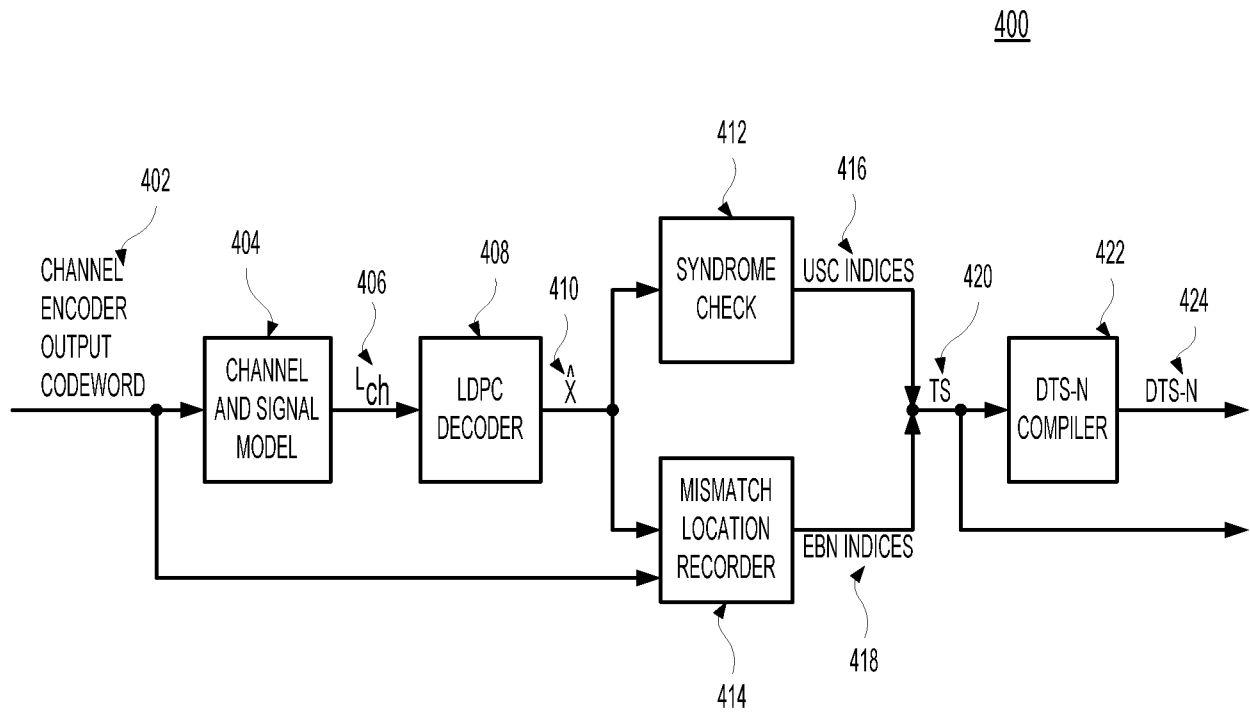
(PRIOR ART)

300

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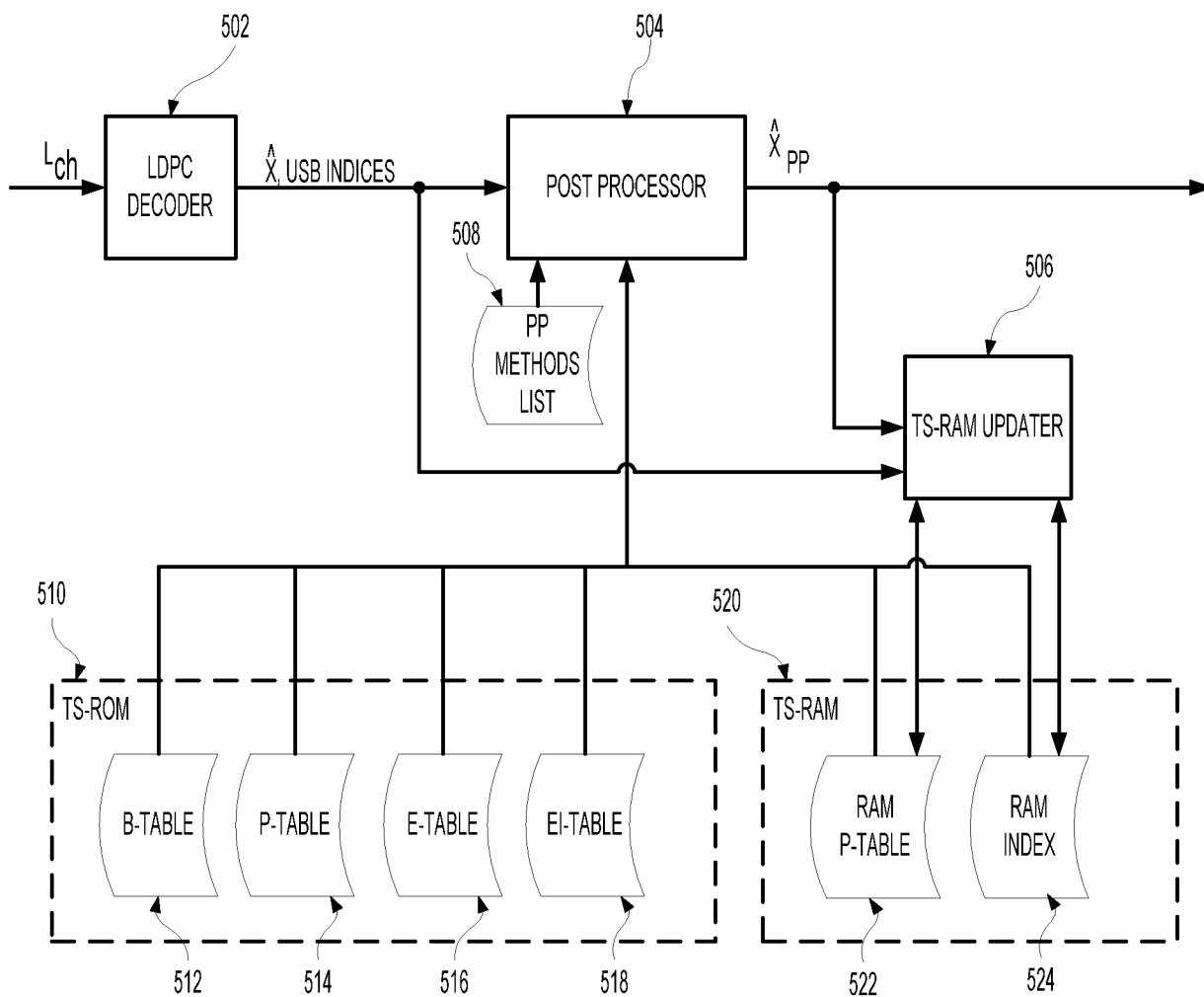
FIG. 4

(PRIOR ART)



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FIG. 5

500

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FIG. 6

514

	604	606	608	
602	LAYER	USC_INDEX	EBN_INDEX	
0				610
1				
2				
3				612
•	•	•	•	
•	•	•	•	
•	•	•	•	
				614
				616
	•	•	•	
	•	•	•	
	•	•	•	
				618
				620
	•	•	•	
	•	•	•	
	•	•	•	

FIG. 7

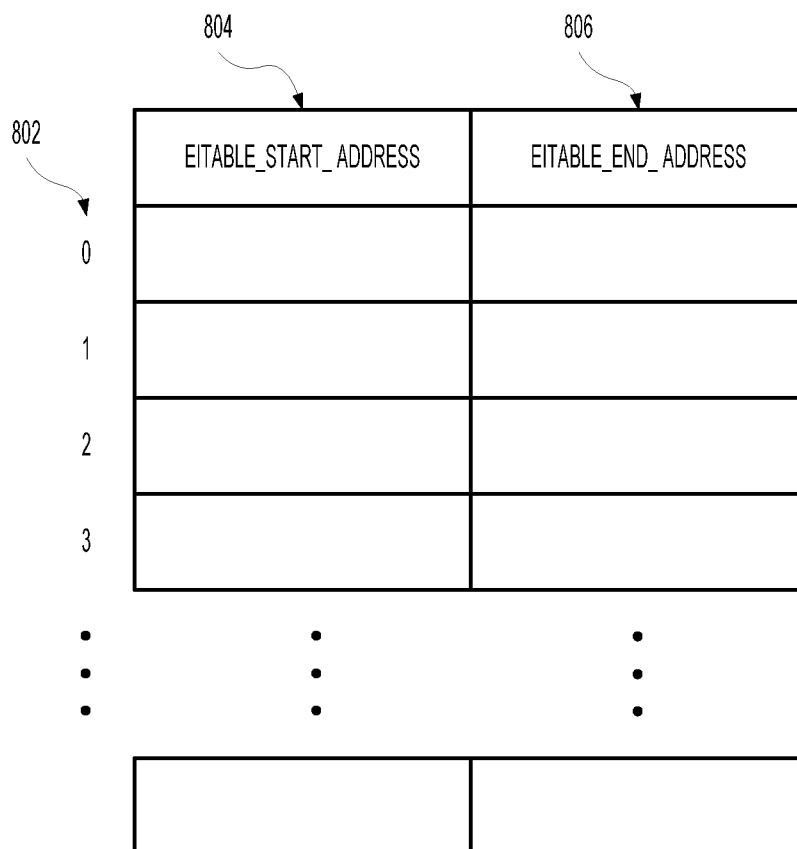
512

	704	706	708
702	PTABLE_START_OFFSET	ETABLE_START_OFFSET	NUM_ETABLE_ENTRIES
0			
1			
2			
3			
⋮	⋮	⋮	⋮
⋮	⋮	⋮	⋮
⋮	⋮	⋮	⋮
bMax-2			

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FIG. 8

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FIG. 9

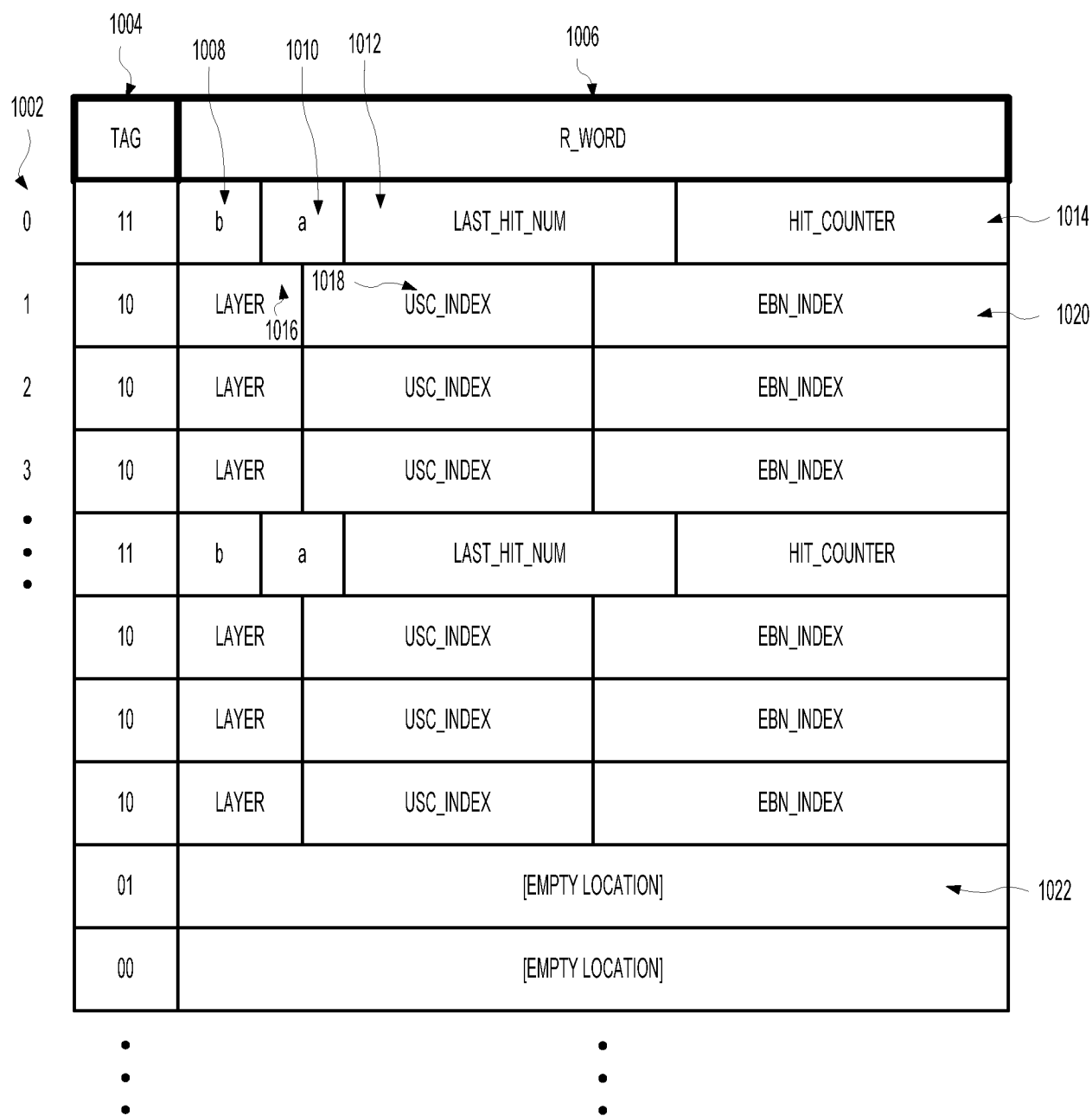
518

	904	906
902	BLOCK_COLUMN	B_INDEX
0		
1		
2		
3		
•	•	•
•	•	•
•	•	•

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FIG. 10

522



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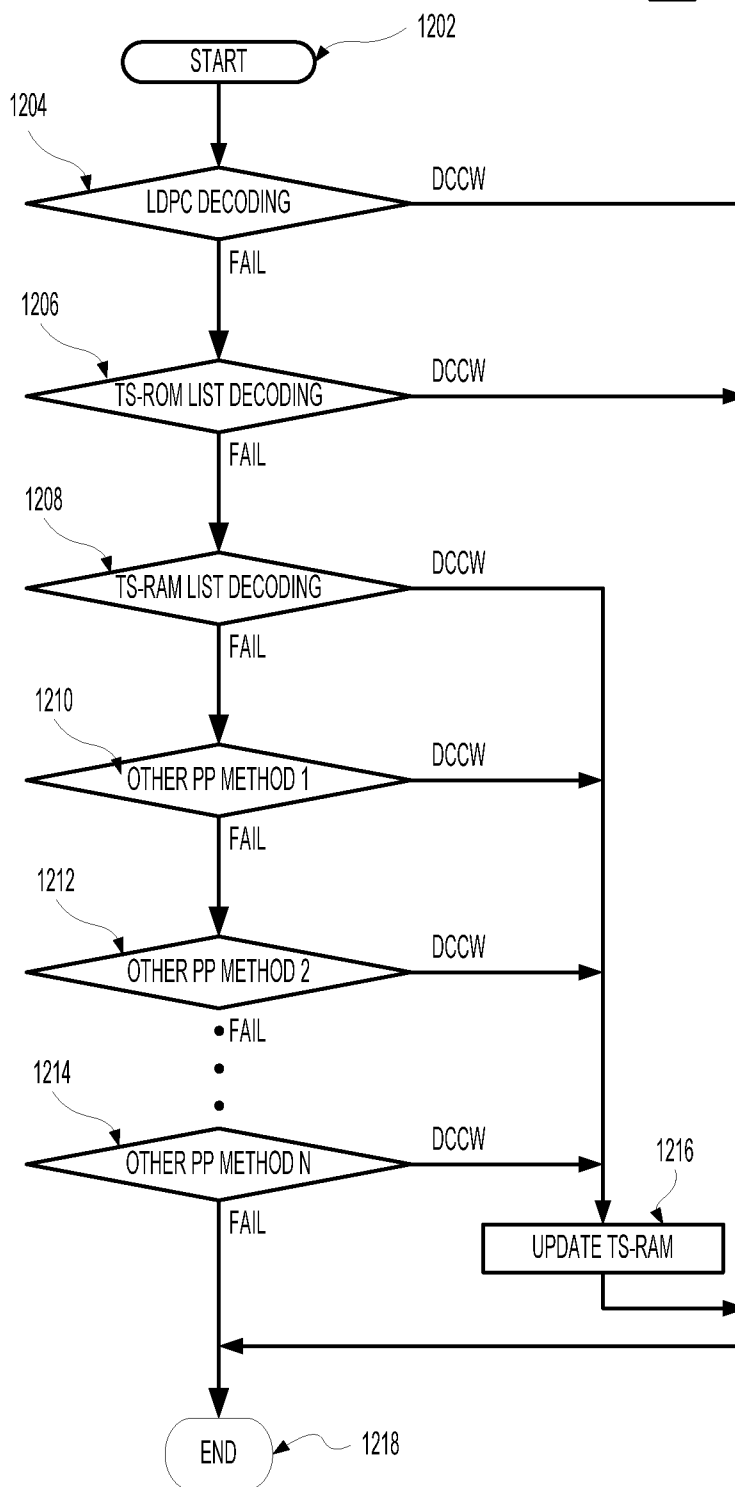
FIG. 11

524



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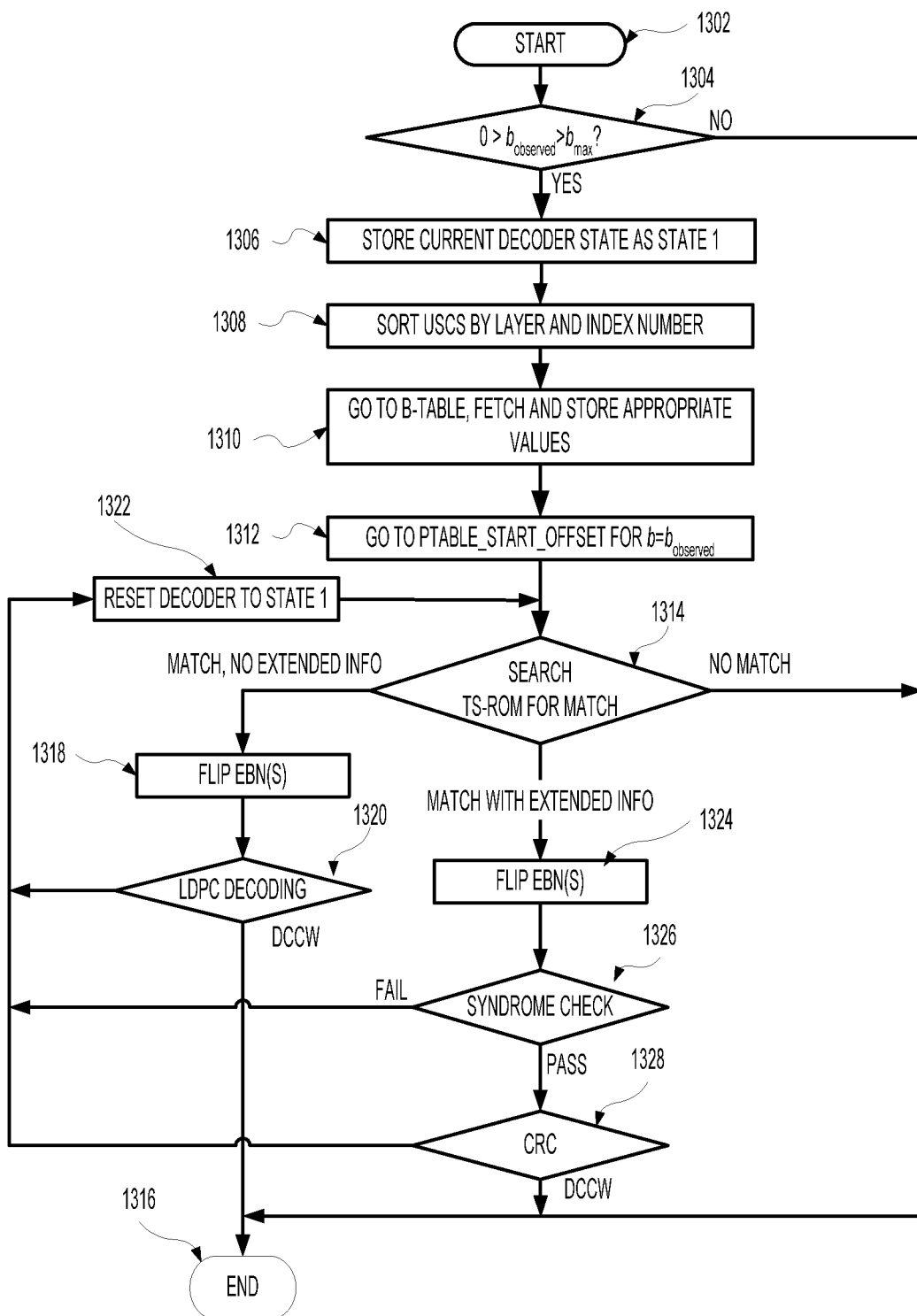
FIG. 12

1200

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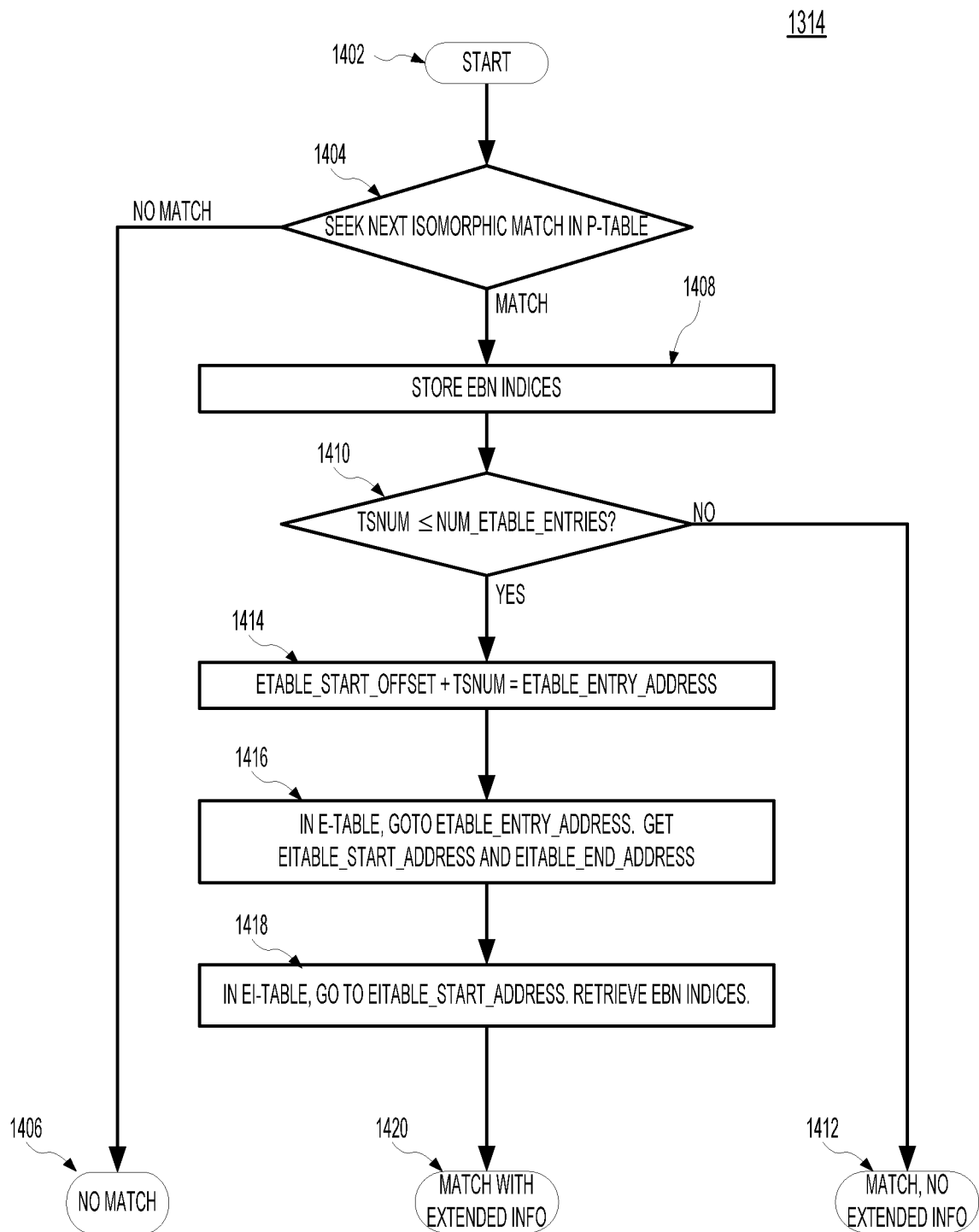
FIG. 13

1206



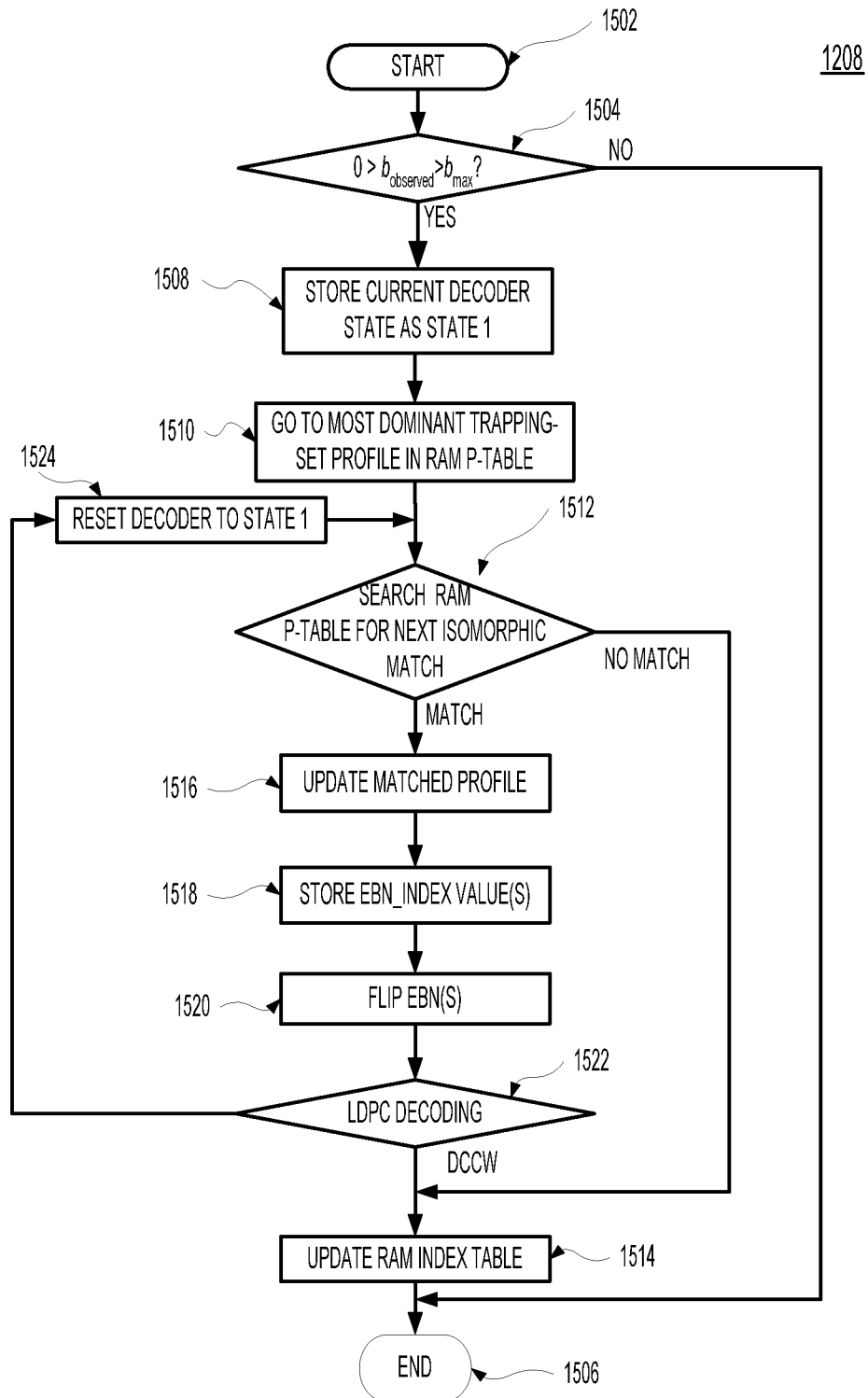
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FIG. 14



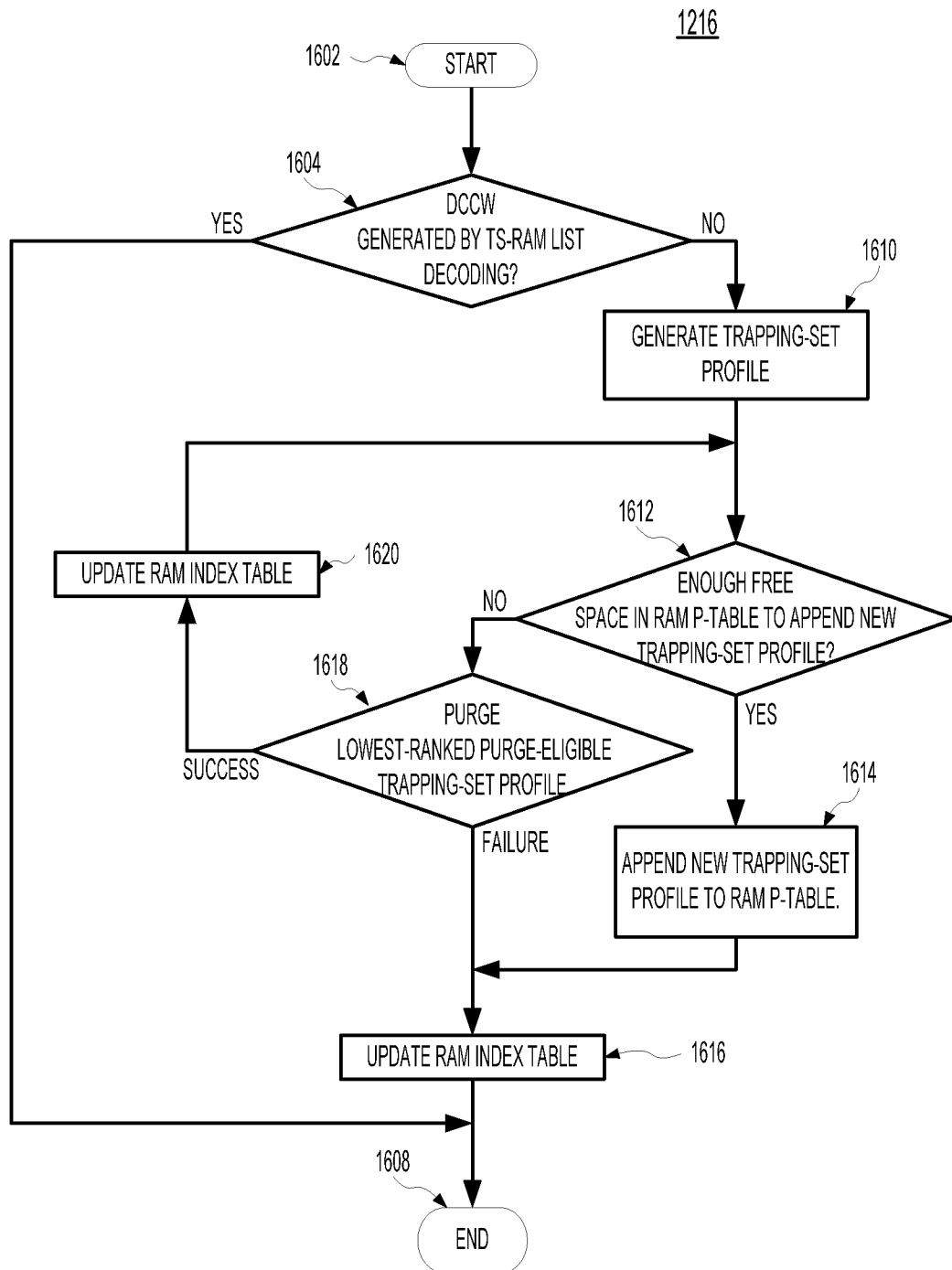
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FIG. 15



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FIG. 16



INTERNATIONAL SEARCH REPORT

International application No.

PCT/US 08/86523

A. CLASSIFICATION OF SUBJECT MATTER

IPC(8) - H03M 13/00 (2009.01)

USPC - 714/758

According to International Patent Classification (IPC) or to both national classification and IPC

B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)

USPC: 714/758

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched
USPC: 714/746, 758, 759, 763, 769; 711/100, 104, 154

Electronic data base consulted during the international search (name of data base and, where practicable, search terms used)

PubWEST(USPT,PGPB,EPAB,JPAB); DialogPRO; WIPO, EPO, CITESEER, Google patents, Google scholar

Search Terms Used: decoding, decoder, encoded data, index table, RAM, random access memory, trapping set, "near codeword", near-codeword, stopping set, closest codeword, uncorrectable error, correct codeword, LDPC etc.

C. DOCUMENTS CONSIDERED TO BE RELEVANT

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
Y	US 2007/0011573 A1 (FARJADRAD et al.) 11 January 2007 (11.01.2007) entire document especially abstract, para [0004]-[0008], para [0020]-[0021], para [0023]-[0024], para [0028].	1-20
Y	US 2008/0163032 A1 (LASTRAS-MONTANO) 03 July 2008 (03.07.2008) entire document especially Figs 9-11, abstract, para [0008]-[0012], para [0041], para [0047]-[0053], para [0061], para [0187].	1-20
A	US 2008/0126910 A1 (VENKATESAN et al.) 29 May 2008 (29.05.2008) entire document	1-20

☐ Further documents are listed in the continuation of Box C.

* Special categories of cited documents:

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"O" document referring to an oral disclosure, use, exhibition or other means

"P" document published prior to the international filing date but later than the priority date claimed

"T" later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention

"X" document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step when the document is taken alone

"Y" document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art

"&" document member of the same patent family

Date of the actual completion of the international search

02 February 2009 (02.02.2009)

Date of mailing of the international search report

12 FEB 2009

Name and mailing address of the ISA/US

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Facsimile No. 571-273-3201

Authorized officer:

Lee W. Young

PCT Helpdesk: 571-272-4300

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