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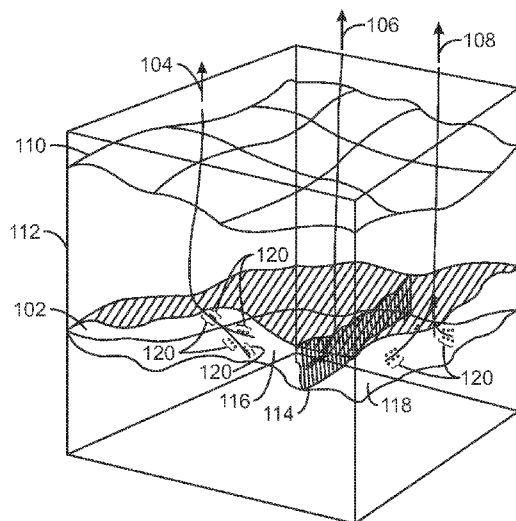
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(54) Title: METHODS AND SYSTEMS FOR MACHINE-LEARNING BASED SIMULATION OF FLOW



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FIG. 1

(57) Abstract: There is provided a method for modeling a hydrocarbon reservoir that includes generating a reservoir model comprising a plurality of sub regions. At least one of the sub regions is simulated using a training simulation to obtain a set of training parameters comprising state variables and boundary conditions of the at least one sub region. A machine learning algorithm is used to approximate, based on the set of training parameters, an inverse operator of a matrix equation that provides a solution to fluid flow through a porous media. The hydrocarbon reservoir can be simulated using the inverse operator approximated for the at least one sub region. The method also includes generating a data representation of a physical hydrocarbon reservoir can be generated in a non-transitory, computer-readable, medium based, at least in part, on the results of the simulation.



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**METHODS AND SYSTEMS FOR MACHINE-LEARNING BASED SIMULATION
OF FLOW**

CROSS-REFERENCE TO RELATED APPLICATIONS

5 **[0001]** This application claims the benefit of U.S. Provisional Patent Application 61/368,939 filed July 29, 2010 entitled METHODS AND SYSTEMS FOR MACHINE-LEARNING BASED SIMULATION OF FLOW, the entirety of which is incorporated by reference herein.

10 **[0002]** This application is related to, and claims the benefit of, the following U.S. Provisional Patent Applications, the entireties of which are incorporated by reference herein: No. 61/368,921, filed July 29, 2010 entitled METHODS AND SYSTEMS FOR MACHINE-LEARNING BASED SIMULATION OF FLOW; No. 61/368,923, filed July 29, 2010 entitled METHODS AND SYSTEMS FOR MACHINE-LEARNING BASED SIMULATION OF FLOW; and No. 61/368,930, filed July 29, 2010 entitled METHODS
15 AND SYSTEMS FOR MACHINE-LEARNING BASED SIMULATION OF FLOW.

FIELD OF THE INVENTION

[0003] Exemplary embodiments of the present techniques relate to a method and system that provides machine-learning techniques to aid in simulations of flow in porous media.

BACKGROUND

20 **[0004]** This section is intended to introduce various aspects of the art, which may be associated with exemplary embodiments of the present techniques. This discussion is believed to assist in providing a framework to facilitate a better understanding of particular aspects of the present techniques. Accordingly, it should be understood that this section should be read in this light, and not necessarily as admissions of prior art.

25 **[0005]** Hydrocarbons are widely used for fuels and chemical feedstocks. Hydrocarbons are generally found in subsurface rock formations that are generally termed reservoirs. Removing hydrocarbons from the reservoirs depends on numerous physical properties of the rock formations, such as the permeability of the rock containing the hydrocarbons, the ability of the hydrocarbons to flow through the rock formations, and the proportion of hydrocarbons
30 present, among others.

[0006] Often, mathematical models termed “reservoir simulation models” are used to simulate hydrocarbon reservoirs for locating hydrocarbons and optimizing the production of

the hydrocarbons. A reservoir simulator models the flow of a multiphase fluid through a heterogeneous porous media, using an iterative, time-stepping process where a particular hydrocarbon production strategy is optimized. Most reservoir simulation models assume linear potential flow. Darcy's law may be used to describe the linear relationship between potential gradients and flow velocity. In some regions of the reservoir, non-Darcy flow models such as Forchheimer flow, which describe a non-linear relationship between potential gradient and fluid velocity, may be used. In general, however, these models were developed assuming single-phase flow. Therefore, reservoir simulators have extended those models to multiphase flow assuming that each phase may be handled separately and or coupled via capillary pressure effects.

[0007] Once the governing equations are defined, equations on a simulation grid are discretized. State variables are then updated through time according to the boundary conditions. The accuracy of the solution depends on the assumptions inherent in the discretization method and the grid on which it is applied. For example, a simple two-point flux approximation (TPFA) in conjunction with a finite difference approach assumes that the fluid velocity is a function of potentials of only two points. This is valid if the grid is orthogonal and permeability is isotropic in the region in question. If permeability is not isotropic and/or the grid is not orthogonal, this TPFA is incorrect and the fluid velocity will be inaccurate. Alternative multi-point flux approximations (MPFA) or different discretization methods, such as Finite Element Methods, have been applied to address this problem. Such methods currently suffer from their inability to resolve the problem on complex geometries in a computationally efficient manner.

[0008] Properties for reservoir simulation models, such as permeability or porosity, are often highly heterogeneous across a reservoir. The variation may be at all length scales from the smallest to the largest scales that can be comparable to the reservoir size. Disregarding the heterogeneity can often lead to inaccurate results. However, computer simulations that use a very fine grid discretization to capture the heterogeneity are computationally very expensive.

[0009] Accordingly, the simulation grid is often relatively coarse. As a consequence, each grid cell represents a large volume (e.g. 100 meters to kilometers on each side of a 3D grid cell). However, physical properties such as rock permeability vary quite significantly over that volume. Most modern simulators start with a fine grid representation of the data and use some version of flow-based scale-up to calculate an effective permeability over the

coarse grid volume. However, relative permeability, which is a function of saturation, may change dramatically over the volume of the coarse grid when simulated using a fine grid model. This is handled by both scaling up the absolute permeability and assuming that relative permeability scales uniformly in the volume of the coarse grid cell, or by the use of dynamic pseudo functions for each coarse grid cell block. As currently used, pseudo functions do not provide the reusability and flexibility needed to attain their full potential. For example, a change in boundary conditions (moving a well) requires regeneration of the pseudo functions.

5 [0010] In some cases, a dual permeability simulation model may be used to improve scale-up accuracy. Dual permeability simulation models use methods conceptually similar to the use of pseudo functions in order to generate two-level effective permeabilities and matrix-fracture transfer functions. Furthermore, effects such as hysteresis, where relative permeability is not only a function of saturation, but also direction in which saturation is changing, are treated as special cases. In other words, a property such as phase permeability is a scale and time dependent property that is difficult to scale-up accurately and with a simple model.

[0011] A method of using a neural network to determine an optimal placement of wells in a reservoir is described in “Applying Soft Computing Methods to Improve the Computational Tractability of a Subsurface Simulation–Optimization Problem,” by Virginia M. Johnson & Leah L. Rogers, 29 JOURNAL OF PETROLEUM SCIENCE AND ENGINEERING 2001.153–175 (2001). Using a standard industry reservoir simulator, a knowledge base of 550 simulations sampling different combinations of 25 potential injection locations was created. Neural networks were trained from a representative sample of simulations, which forms a re-useable knowledge base of information for addressing many different management questions. Artificial neural networks (ANNs) were trained to predict peak injection volumes and volumes of produced oil and gas at three and seven years after the commencement of injection. The rapid estimates of these quantities provided by the ANNs were fed into net profit calculations, which in turn were used by a genetic algorithm (GA) to evaluate the effectiveness of different well-field scenarios.

25 [0012] Methods of using different types of neural networks as proxies to a reservoir simulation are described in “Use of Neuro-Simulation techniques as proxies to reservoir simulator: Application in production history matching,” by Paulo Camargo Silva, et al., JOURNAL OF PETROLEUM SCIENCE AND ENGINEERING 57 273–280 (2007). In this article,

different types of Neural Networks were used as proxies to a reservoir simulator. The Neural Networks were applied in a study of production history matching for a synthetic case and a real case. A reservoir simulator was used to generate training sets for the Neural Networks. And for these cases, the authors were able to reproduce the narrowly modeled behavior response via the ANN.

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- [0013] Methods to provide an improved and faster history matching with a nonlinear proxy are described in “Improved and More-Rapid History Matching with a nonlinear Proxy and Global Optimization,” by A. S. Cullick, et al., SPE 101933, SOCIETY OF PETROLEUM ENGINEERS (2008). A comprehensive, nonlinear proxy neural network is trained with a relatively small set of numerical simulations that were defined through a design of experiments (DOE). The neural network is used to characterize parameter sensitivities to reservoir parameters and to generate solution sets of the parameters that match history. The solution sets generated by the neural network can be validated with the simulator or used as initial solutions for a full optimization.
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- [0014] Additional background information can be found in “Smooth Function Approximation Using Neural Networks,” by Silvia Ferrari & Robert F. Stengel, IEEE TRANSACTIONS ON NEURAL NETWORKS, VOL. 16, No. 1 (2005); and “Introducing Predictive Analytics: Opportunities,” by Paul Stone, SPE 106865, Society of Petroleum Engineers (2007). None of the techniques described above provide a fast and accurate method of using a machine learning techniques to compute a machine learning based solution surrogate for performing a reservoir simulation.
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SUMMARY

- [0015] Exemplary embodiments of the present invention provide techniques for using machine learning to model a hydrocarbon reservoir. An exemplary embodiment provides a method for modeling a hydrocarbon reservoir that includes generating a reservoir model that has a plurality of sub regions. The method also includes simulating at least one sub region of the plurality of sub regions using a training simulation to obtain a set of training parameters comprising state variables and boundary conditions of the at least one sub region. A machine learning algorithm can be used to approximate, based on the set of training parameters, an inverse operator of a matrix equation that provides a solution to fluid flow through a porous media. The hydrocarbon reservoir can be simulated using the inverse operator approximated for the at least one sub region. The method also includes generating a data representation of a
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physical hydrocarbon reservoir in a non-transitory, computer-readable, medium based, at least in part, on the results of the simulation.

[0016] In some embodiments, simulating at least one sub region of the plurality of sub regions using the training simulation includes specifying a set of physical, geometrical, or numerical parameters of the at least one sub-region, wherein the set of physical, geometrical, or numerical parameters includes at least one of rock porosity, phase permeability, and geological characteristics. The method may also include storing the inverse operator approximated for the at least one sub region and physical, geometrical, or numerical parameters corresponding to the at least one sub region to a database of surrogate solutions for use in subsequent reservoir simulations. The inverse operator approximated for the at least one sub region can be re-used for a second sub region based on a comparison of a set of physical, geometrical, or numerical parameters corresponding to the at least one sub region and a new set of physical, geometrical, or numerical parameters that characterize the second sub region.

[0017] In some embodiments, using the machine learning algorithm to approximate the inverse operator includes training a neural net using the training parameters, wherein the boundary conditions are used as input to the neural net and the state variables are used as the desired output. Simulating the at least one sub region using the training simulation can include specifying a set of boundary condition types for each boundary of the sub region and generating a fine-gridded computational mesh of the at least one sub region. Simulating the at least one sub region using the training simulation can also include specifying a set of boundary condition values based, at least in part, on physical characteristics of the reservoir.

[0018] Another exemplary embodiment provides a method for producing a hydrocarbon from a hydrocarbon reservoir that includes generating a reservoir model that has a plurality of sub regions. The method includes simulating at least one sub region of the plurality of sub regions using a training simulation to obtain a set of training parameters comprising state variables and boundary conditions of the at least one sub region. A machine learning algorithm can be used to approximate, based on the set of training parameters, an inverse operator of a matrix equation that provides a solution to fluid flow through a porous media. The hydrocarbon reservoir can be simulated using the inverse operator approximated for the at least one sub region. The method also includes producing a hydrocarbon from the hydrocarbon reservoir based, at least in part, upon the results of the simulation.

[0019] In some embodiments, producing the hydrocarbon includes drilling one or more

wells to the hydrocarbon reservoir, wherein the wells include production wells, injection wells, or both. Producing the hydrocarbon can also include setting production rates from the hydrocarbon reservoir.

[0020] Another exemplary embodiment provides a system for modelling reservoir properties that includes a processor and a non-transitory machine readable medium comprising code configured to direct the processor to generate a reservoir model that has a plurality of sub regions. The machine readable medium can also includes code configured to direct the processor to simulate at least one sub region of the plurality of sub regions using a training simulation to obtain a set of training parameters comprising state variables and boundary conditions of the at least one sub region. The machine readable medium can also include code configured to direct the processor to use a machine learning algorithm to approximate, based on the set of training parameters, an inverse operator of a matrix equation that provides a solution to fluid flow through a porous media. The machine readable medium can also includes code configured to direct the processor to simulate the reservoir using the inverse operator approximated for the at least one sub region. The machine readable medium can also include code configured to direct the processor to generate a data representation of a physical hydrocarbon reservoir in a non-transitory, computer-readable, medium based, at least in part, on the results of the simulation.

[0021] In some embodiments, the machine readable medium includes code configured to direct the processor to receive a set of physical, geometrical, or numerical parameters of the at least one sub-region used for simulating the at least one sub region using the training simulation, wherein the set of physical, geometrical, or numerical parameters includes at least one of rock porosity, phase permeability, and geological characteristics. The machine readable medium can also include code configured to direct the processor to store the inverse operator approximated for the at least one sub region and physical, geometrical, or numerical parameters corresponding to the at least one sub region to a database of surrogate solutions for use in subsequent reservoir simulations. The machine readable medium can also include code configured to direct the processor to re-use the inverse operator approximated for the at least one sub region for a second sub region based on a comparison of a set of physical, geometrical, or numerical parameters corresponding to the at least on sub region and a new set of physical, geometrical, or numerical parameters that characterize the second sub region.

[0022] In some embodiments, the system includes a neural net, wherein the machine readable medium includes code configured to direct the processor to train the neural net using

the training parameters, wherein the boundary conditions are used as input to the neural net and the state variables are used as the desired output. The machine readable medium can also include code configured to direct the processor to receive a set of boundary condition types for each boundary of the sub region and generate a fine-gridded computational mesh of the sub region for simulating the at least one sub region using the training simulation. The machine readable medium can also include code configured to direct the processor to receive a set of boundary condition values for simulating the at least one sub region using the training simulation, wherein the set of boundary condition values is based, at least in part, on physical characteristics of the reservoir.

10 [0023] Another exemplary embodiment provides a non-transitory, computer readable medium that includes code configured to direct a processor to create a simulation model of a hydrocarbon reservoir, wherein the simulation model includes a plurality of sub regions. The computer readable medium also includes code configured to direct a processor to simulate at least one sub region of the plurality of sub regions using a training simulation to obtain a set of training parameters comprising state variables and boundary conditions of the at least one sub region. The computer readable medium also includes code configured to direct a processor to use a machine learning algorithm to approximate, based on the set of training parameters, an inverse operator of a matrix equation that provides a solution to fluid flow through a porous media. The computer readable medium also includes code configured to direct a processor to simulate the hydrocarbon reservoir using the inverse operator approximated for the at least one sub region. The computer readable medium also includes code configured to direct a processor to generate a data representation of a physical hydrocarbon reservoir in a non-transitory, computer-readable, medium based, at least in part, on the results of the simulation.

25 [0024] In some embodiments, the computer readable medium includes code configured to store the inverse operator approximated for the at least one sub region and physical, geometrical, or numerical parameters corresponding to the at least one sub region to a database of surrogate solutions for use in simulating another sub-region in the simulation model or a different simulation model. The computer readable medium can also include code configured to direct a processor to generate a neural net and train the neural net using the training parameters. The computer readable medium can also include code configured to direct a processor to determine a set of boundary condition types for each boundary of the sub

region, and generate a fine-gridded computational mesh of the sub region for use in the full-physics simulation of the sub region.

BRIEF DESCRIPTION OF THE DRAWINGS

5 [0025] The advantages of the present techniques are better understood by referring to the following detailed description and the attached drawings, in which:

[0026] Fig. 1 is a schematic view of a reservoir, in accordance with an exemplary embodiment of the present techniques;

10 [0027] Fig. 2 is a top view of a reservoir showing a planar projection of a computational mesh over the reservoir, in accordance with an exemplary embodiment of the present techniques;

[0028] Fig. 3 is a process flow diagram of a workflow for modelling a reservoir, in accordance with an exemplary embodiment of the present techniques;

[0029] Fig. 4 is a schematic view of an exemplary neural net, in accordance with an exemplary embodiment of the present techniques;

15 [0030] Fig. 5 is a schematic view of a reservoir simulation model, in accordance with an exemplary embodiment of the present techniques.

[0031] Fig. 6 is a process flow diagram of a method for computing the solution surrogate for each sub region of a reservoir model, in accordance with an exemplary embodiment of the current invention;

20 [0032] Fig. 7 is a one-dimensional model of a coarse grid cell, in accordance with an exemplary embodiment of the present techniques;

[0033] Fig. 8 is a two dimensional coarse grid cell, in accordance with an exemplary embodiment of the present techniques;

25 [0034] Fig. 9 is a process flow diagram of a method of performing a reservoir simulation using the coarse scale approximation of the phase permeability, in accordance with an exemplary embodiment of the present techniques;

[0035] Fig. 10 is a two-dimensional view of a reservoir model showing a planar projection of a computational mesh, in accordance with an exemplary embodiment of the present techniques;

30 [0036] Fig. 11 is a process flow diagram of a method of performing a reservoir

simulation using a constitutive relationship between pressure and flow, in accordance with an exemplary embodiment of the present techniques;

[0037] Fig. 12 is a schematic view of a coarse grid model of a reservoir, in accordance with an exemplary embodiment of the present techniques;

5 [0038] Fig. 13 is a process flow diagram of a method for modeling fluid flow in a reservoir, in accordance with an exemplary embodiment of the present techniques;

[0039] Fig. 14 is a schematic view of a one dimensional medium through which a porous flow may be simulated using machine learning;

[0040] Fig. 15 is a response diagram of the medium shown in Fig. 14;

10 [0041] Fig. 16 is a graph of test data comparing a finite difference simulation of the sub region shown in Fig. 14 with a machine learning based solution surrogate simulation;

[0042] Fig. 17 is a fine mesh simulation model used to develop a training set for training a neural net solution surrogate to porous media flow;

15 [0043] Fig. 18 is model of the central sub region shown in the fine mesh simulation model Fig. 17;

[0044] Fig. 19 is a graph of the concentration at boundary segment C4 of Fig. 18 at varying time steps; and

[0045] Fig. 20 is a block diagram of an exemplary cluster computing system that may be used in exemplary embodiments of the present techniques.

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DETAILED DESCRIPTION

[0046] In the following detailed description section, the specific embodiments of the present techniques are described in connection with preferred embodiments. However, to the extent that the following description is specific to a particular embodiment or a particular use of the present techniques, this is intended to be for exemplary purposes only and simply provides a description of the exemplary embodiments. Accordingly, the present techniques are not limited to the specific embodiments described below, but rather, such techniques include all alternatives, modifications, and equivalents falling within the true spirit and scope of the appended claims.

25 [0047] At the outset, and for ease of reference, certain terms used in this application and their meanings as used in this context are set forth. To the extent a term used herein is not

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defined below, it should be given the broadest definition persons in the pertinent art have given that term as reflected in at least one printed publication or issued patent. Further, the present techniques are not limited by the usage of the terms shown below, as all equivalents, synonyms, new developments, and terms or techniques that serve the same or a similar purpose are considered to be within the scope of the present claims.

[0048] "Coarsening" refers to reducing the number of cells in simulation models by making the cells larger, for example, representing a larger space in a reservoir. Coarsening is often used to lower the computational costs by decreasing the number of cells in a reservoir model prior to generating or running simulation models.

[0049] "Computer-readable medium" or "non-transitory, computer-readable medium," as used herein, refers to any non-transitory storage and/or transmission medium that participates in providing instructions to a processor for execution. Such a medium may include, but is not limited to, non-volatile media and volatile media. Non-volatile media includes, for example, NVRAM, or magnetic or optical disks. Volatile media includes dynamic memory, such as main memory. Common forms of computer-readable media include, for example, a floppy disk, a flexible disk, a hard disk, an array of hard disks, a magnetic tape, or any other magnetic medium, magneto-optical medium, a CD-ROM, a holographic medium, any other optical medium, a RAM, a PROM, and EPROM, a FLASH-EPROM, a solid state medium like a memory card, any other memory chip or cartridge, or any other tangible medium from which a computer can read data or instructions.

[0050] As used herein, "to display" or "displaying" includes a direct act that causes displaying of a graphical representation of a physical object, as well as any indirect act that facilitates displaying a graphical representation of a physical object. Indirect acts include providing a website through which a user is enabled to affect a display, hyperlinking to such a website, or cooperating or partnering with an entity who performs such direct or indirect acts. Thus, a first party may operate alone or in cooperation with a third party vendor to enable the information to be generated on a display device. The display device may include any device suitable for displaying the reference image, such as without limitation a virtual reality display, a 3-D display, a CRT monitor, a LCD monitor, a plasma device, a flat panel device, or printer.

[0051] "Exemplary" is used exclusively herein to mean "serving as an example, instance, or illustration." Any embodiment described herein as "exemplary" is not to be construed as preferred or advantageous over other embodiments.

[0052] “Flow simulation” is defined as a numerical method of simulating the transport of mass (typically fluids, such as oil, water and gas) or energy through a physical system using a simulation model. The physical system may include a three-dimensional reservoir model, fluid properties, and the number and locations of wells. Flow simulations may use or provide
5 a way to evaluate a strategy (often called a well-management strategy) for controlling injection and production rates. These strategies can be used to maintain reservoir pressure by replacing produced fluids with injected fluids (for example, water and/or gas). When a flow simulation correctly recreates a past reservoir performance, it is said to be “history matched,” and a higher degree of confidence is placed in its ability to predict the future fluid behavior in
10 the reservoir.

[0053] “Permeability” is the capacity of a rock to transmit fluids through the interconnected pore spaces of the rock. Permeability may be measured using Darcy's Law: $Q = (k \Delta P A) / (\mu L)$, wherein Q = flow rate (cm^3/s), ΔP = pressure drop (atm) across a cylinder having a length L (cm) and a cross-sectional area A (cm^2), μ = fluid viscosity (cp), and k =
15 permeability (Darcy). The customary unit of measurement for permeability is the millidarcy. The term “relatively permeable” is defined, with respect to formations or portions thereof, as an average permeability of 10 millidarcy or more (for example, 10 or 100 millidarcy).

[0054] “Pore volume” or “porosity” is defined as the ratio of the volume of pore space to the total bulk volume of the material expressed in percent. Porosity is a measure of the
20 reservoir rock's storage capacity for fluids. Porosity is preferably determined from cores, sonic logs, density logs, neutron logs or resistivity logs. Total or absolute porosity includes all the pore spaces, whereas effective porosity includes only the interconnected pores and corresponds to the pore volume available for depletion.

[0055] A “reservoir” or “reservoir formation” is defined as a pay zone (for example,
25 hydrocarbon producing zones) that include sandstone, limestone, chalk, coal and some types of shale. Pay zones can vary in thickness from less than one foot (0.3048 m) to hundreds of feet (hundreds of m). The permeability of the reservoir formation provides the potential for production.

[0056] “Reservoir properties” and “reservoir property values” are defined as quantities
30 representing physical attributes of rocks containing reservoir fluids. The term “reservoir properties” as used in this application includes both measurable and descriptive attributes. Examples of measurable reservoir property values include porosity, permeability, water saturation, and fracture density. Examples of descriptive reservoir property values include

facies, lithology (for example, sandstone or carbonate), and environment-of-deposition (EOD). Reservoir properties may be populated into a reservoir framework to generate a reservoir model.

[0057] “Reservoir simulation model” refers to a specific mathematical representation of a
5 real hydrocarbon reservoir, which may be considered to be a particular type of geologic model. Reservoir simulation models are used to conduct numerical experiments (reservoir simulations) regarding past performance in order to verify that our understanding of the reservoir properties is correct and future performance of the field with the goal of determining the most profitable operating strategy. An engineer managing a hydrocarbon
10 reservoir may create many different reservoir simulation models, possibly with varying degrees of complexity, in order to quantify the past performance of the reservoir and predict its future performance.

[0058] “Transmissibility” refers to the volumetric flow rate between two points at unit viscosity for a given pressure-drop. Transmissibility is a useful measure of connectivity.
15 Transmissibility between any two compartments in a reservoir (fault blocks or geologic zones), or between the well and the reservoir (or particular geologic zones), or between injectors and producers, can all be useful for characterizing connectivity in the reservoir.

[0059] “Well” or “wellbore” includes cased, cased and cemented, or open-hole wellbores, and may be any type of well, including, but not limited to, a producing well, an experimental
20 well, an exploratory well, and the like. Wellbores may be vertical, horizontal, any angle between vertical and horizontal, deviated or non-deviated, and combinations thereof, for example a vertical well with a non-vertical component. Wellbores are typically drilled and then completed by positioning a casing string within the wellbore. Conventionally, a casing string is cemented to the well face by circulating cement into the annulus defined between the
25 outer surface of the casing string and the wellbore face. The casing string, once embedded in cement within the well, is then perforated to allow fluid communication between the inside and outside of the tubulars across intervals of interest. The perforations allow for the flow of treating chemicals (or substances) from the inside of the casing string into the surrounding formations in order to stimulate the production or injection of fluids. Later, the perforations
30 are used to receive the flow of hydrocarbons from the formations so that they may be delivered through the casing string to the surface, or to allow the continued injection of fluids for reservoir management or disposal purposes.

Overview

[0060] Exemplary embodiments of the present invention provide techniques for using machine learning algorithms to generate solution surrogates for use in simulating a fluid flow in a reservoir such as a hydrocarbon reservoir. A simulation model may be segmented into a plurality of sub regions or coarse cells. Sets of training data may be obtained for a sub region
5 by performing a full- physics simulation of the sub region. The training set may be used to compute the surrogate solution for the sub region through a machine learning algorithm such as a neural net. In some exemplary embodiments, the surrogate solution method may be an approximation of the inverse operator of a matrix equation for the fluid flow through a porous media. In some exemplary embodiments, the surrogate solution may be a formulation of
10 Darcy's law, and supervised machine learning may be used to generate a coarse scale approximation of the phase permeability of a coarse grid cell. In some exemplary embodiments, the surrogate solution may be a constitutive relationship that approximates the flow response at a flux interface of a coarse cell or sub region. Furthermore, a reservoir simulation may include a combination of different types of surrogate solution methods for
15 different regions of space or time. The surrogate solution computed for a sub region or coarse cell may be represented in some form that may be stored in a database for re-use in subsequent reservoir simulations.

[0061] Fig. 1 is a schematic view 100 of a reservoir 102, in accordance with an exemplary embodiment of the present techniques. The reservoir 102, such as an oil or natural
20 gas reservoir, can be a subsurface formation that may be accessed by drilling wells 104, 106, and 108 from the surface 110 through layers of overburden 112. The wells 104, 106, and 108 may be deviated, such as being directionally drilled to follow the reservoir 102. Further, the wells can be branched to increase the amount of hydrocarbon that may be drained from the reservoir, as shown for wells 104 and 108. The wells 104, 106, and 108, can have numerous
25 areas with perforations 120 (indicated as dots next to the wells) to allow hydrocarbons to flow from the reservoir 102 into the wells 104, 106, and 108 for removal to the surface. The reservoir 102 may have one or more faults 114 dividing areas, for example regions 116 and 118, which may either restrict or enhance the flow of hydrocarbons. A simulation model, or simulator, of the reservoir 102 is likely to find that the greatest changes occur in the vicinity
30 of the wells 104, 106, and 108, and other reservoir features, such as the fault 114. Accordingly, it would be useful to keep fine structure in the vicinity of each of these features.

[0062] Fig. 2 is a top view of a reservoir showing a planar projection of a computational mesh 200 over the reservoir, in accordance with an exemplary embodiment of the present

techniques. Although the computational mesh 200 is shown as a two dimensional grid of computational cells (or blocks) 202 to simplify the explanation of the problem, it should be understood that the actual computational mesh 200 can be a three dimension matrix of computational cells 202 that encompasses the reservoir. Further, the computational cells 202 may be of any size or shape, resulting in an unstructured grid. Generally, a computational cell 202 is a single two or three dimensional location within a simulation model that represents a physical location in a reservoir. Computational cell 202 may be represented by a functional relationship, or “solution surrogate,” generated by a machine learning technique, such as a neural net, probability tree, support vector machine, radial basis functions, and the like. Computational cells 202 may interact with adjacent computational cells 202, for example, by having flux properties assigned to a shared border with the adjacent computational cells 202. The flux properties may include heat or mass transfer driven by a difference in temperature or pressure between the adjacent computational cells 202.

[0063] The computational mesh 200 can be coarsened in areas that may have less significant changes, for example, by combining computational cells 202 that are not in proximity to a well or other reservoir feature. Similarly, as shown in Fig. 2, the computational mesh 200 may retain a fine mesh structure in the vicinity of wells or other reservoir features, such as the first well 204, or other reservoir features, for example, a second well 206, a third well 208, a fault 210, or any other features that may show larger changes than other areas. The computational mesh 200 may be used to model a reservoir as discussed further with respect to Fig. 3.

Workflow for Modelling a Reservoir

[0064] Fig. 3 is a process flow diagram of a workflow 300 for modelling a reservoir, in accordance with an exemplary embodiment of the present techniques. Although the discretization (coarsening) and the level of implicitness (which state variables, such as pressure or saturation, are treated implicitly or explicitly in the formulation) of the solution process varies, simulation models may perform in a similar fashion as workflow 300. A simulation model can begin at block 302 by parsing user input data. The input data may include the problem formulation, a geologic model that is discretized into grid blocks with physical properties defined at each grid block, including rock properties (such as permeability) and fluid properties (such as transmissibility). At block 304, boundary conditions for the simulation may be calculated, for example, from the governing equations.

[0065] At block 306, a linear solver may use a Jacobian matrix to generate an

approximate solution for the simulation. Additionally, the approximate solution may be computed using a solution surrogate generated according to the machine learning techniques discussed herein. At block 308, physical properties are calculated from the approximate solution. At block 310, the calculated properties are compared to either previously calculated
5 properties or to measured properties to determine whether a desired accuracy has been reached. In an exemplary embodiment, the determination is made by identifying that the calculated properties have not significantly changed since the last iteration (which may indicate convergence). For example, convergence may be indicated if the currently
10 calculated properties are within 0.01%, 0.1%, 1 %, 10 %, or more of the previously calculated properties. In other embodiments, the determination may be determining if the calculated properties are sufficiently close to measured properties, for example, within 0.01%, 0.1%, 1 %, 10 %, or more. If the desired accuracy is not reached, process flow returns to block 306 to perform another iteration of the linear solver.

[0066] If at block 310, the desired accuracy has been reached, process flow proceeds to
15 block 312, at which results are generated and the time is incremented by a desired time step. The results may be stored in a data structure on a tangible, machine readable medium, such as a database, for later presentation, or the results may be immediately displayed or printed after generation. The time step may be, for example, a day, a week, a month, a year, 5 years, 10 years or more, depending, at least in part, on the desired length of time for the simulation. At
20 block 314, the new time is compared to the length desired for the simulation. If the simulation has reached the desired length of time, the simulation ends at block 316. If the time has not reached the desired length, flow returns to block 304 to continue with the next increment. The simulation time frame may be a month, a year, five years, a decade, two decades, five decades, or a century or more, depending on the desired use of the simulation
25 results.

Computing an Approximate Solution

[0067] The techniques described below use the concept of supervised machine learning to generate the approximate solution at block 306 of method 300. Computing the approximate solution at block 306 may involve determining a different solution surrogate for each of the
30 coarse cells or sub regions involved in the simulation. Various machine-learning techniques may be used to generate the solution surrogate. The machine learning algorithm may operate on data set, D, represented by the formula shown in Eqn. 1.

$$D: \{\tilde{x}_i, \tilde{y}_i, i=1 \dots n\}$$

Eqn. 1

[0068] In the above equation, “x” represents a set of known input vectors, “y” represents a set of corresponding real-valued outputs, and “n” represents the total number of samples. The machine learning algorithm may be used to determine, using this limited information, the dependence shown in Eqn. 2.

$$\tilde{y} = M(\tilde{x}, \tilde{w})$$

Eqn. 2

[0069] In the above equation, “w” represents model parameters that describe the functional relationship between the input vectors, x, and output vectors, y. The dependence may be generated by finding values for the model parameters, w, that provide a suitable approximation of the output vectors, y, when compared to a training set, which represents a set of desired outputs values.

[0070] Fig. 4 is a schematic view of an exemplary neural net 400 that may be used in embodiments of the present techniques. The neural net 400 may include a network of nodes 402. The neural net 400 may include an input layer 404, an output layer 406 and one or more hidden layers 408. Each node 402 in a layer may be connected to the nodes 402 of a preceding layer by a connection 410 characterized by a weighting value, w. The value computed for any given node may be a function of the values at each connected node in the preceding layer modified by the weighting values, w. For example, the node labeled “h₁” may be computed by the formula shown in Eqn. 3.

$$h_1 = f(w_1 i_1 + w_2 i_2 + w_3 i_3 + w_4 i_4)$$

Eqn. 3

[0071] A training set including a set of inputs 412 and a set of desired outputs 414 may be used to train the neural net 400, e.g., to set the values of the weights. A set of inputs 412 may be fed into the input layer 404 of the neural net 400. Node values may then be computed for each node in the hidden layer 408. If the neural net includes more than one hidden layer 408, node values are successively computed for each subsequent hidden layer 408. Node values are then computed for the output layer 406 to generate a set of outputs 416 of the neural net. The set of outputs 416 may be compared to a desired output set 414 to determine a measure of the deviation, sometimes referred to as an “objective function” or “cost function,” between the set of computed outputs 416 and the desired output set 414. The desired output set 414 may be generated by a full-physics simulation of the system under consideration or based on measured characteristics of the system. The objective function

computed for one iteration of the neural net computation may be used to alter the weighting values applied to each of the node connections 410 for the next iteration of the neural net computation. The neural net may be iteratively computed and the calculation of the objective function repeated until the objective function is below an acceptable threshold. After the last
 5 iteration of the neural net, the weight values correspond to an approximation of the response function of the system under consideration. The weight values may be extracted and used as a solution surrogate for a sub-region, as discussed with respect to Fig. 5, below.

[0072] It will be appreciated that the exemplary neural net described herein is used to introduce concepts of machine learning. In actual practice, the neural net may be any suitable
 10 neural net, including any number of hidden layers 408 and any number of nodes 402 per layer, as well as any other proper topology of neuron connections. Further, it will be appreciated that embodiments may include other supervised machine learning techniques, such as probabilistic trees, support vector machines, radial basis functions, and other machine learning techniques.

15 Approximating the Inverse Operator

[0073] In an exemplary embodiment, the solution surrogate may be an approximation of the inverse operator of a matrix equation that relates the fluid flow through a porous media with the boundary conditions of the corresponding grid cell. When discretized on a numerical grid, the set of partial differential equations constructed for the implicit solution of
 20 fluid flow through a porous media with boundary conditions at a given time-step takes the general form of a matrix equation as shown in Eqn. 4.

$$A_{ij}x_i = b_i \quad \text{Eqn. 4}$$

[0074] The structure of the matrix equation is determined by the type of boundary conditions, which may be a mixture of Neumann and Dirichlet boundary conditions. The
 25 values of the boundary conditions determine the values of b_i . In the above formula, 'x' is a vector of unknowns, which may be propagated over time, for example, state variables such as pressure and compositions at a grid cell. The matrix operator, A, depends on properties of the system. A solution of the unknown state variables, x, can be computed according to the formula shown in Eqn. 5.

$$30 \quad x = A^{-1}b \quad \text{Eqn. 5}$$

In an exemplary embodiment, the action of the inverse operator, A^{-1} , is approximated over an appropriate sub-region of the reservoir simulation model via machine learning methods in

order to facilitate fast online use of the approximation as a solution surrogate during reservoir modeling.

[0075] Fig. 5 is a schematic view of a reservoir simulation model, in accordance with an exemplary embodiment of the present techniques. The reservoir simulation model 500 may be divided into any suitable number of sub regions 502. The equations that describe the evolution of state variables such as pressure and composition for each sub region 502 may be represented by a matrix structure characterized by a set of physical, geometrical, or numerical parameters based on the geological characteristics of the matrix structure, such as rock porosity, phase permeability, and the like. A first region may include an injector well 504, and an n^{th} region may include a producer well 506. Each region 502 may be characterized by a set of boundary conditions. Pressure boundaries may be of a Dirichlet boundary type that defines the pressure at the boundary between two regions 502 such as the boundary 508. Flux boundaries may be of a Neumann boundary type that describes the phase flow rate at the boundary between two regions such as depicted on boundary 510.

[0076] To compute the matrix equation solution for the sub region 502, the sub region's boundaries may be partitioned into representative sets by type, for example, flux boundaries and pressure boundaries. For each set of boundary condition types, a set of boundary condition values may be specified that mimic the variety of potentially realistic boundary conditions. The matrix element values of each sub region 502 are determined by physical parameters of the system such as rock porosity, phase permeability, and the like. A training simulation may then be used to generate the training set, $\{b_s, x_s\}$, $s = 1 \dots S$, where the boundary conditions, b_s , may be used as the input 412 to the neural net and, the state variables, x_s , may be used as the desired output 416 (Fig. 4). The resulting training set may be stored to a database along with the physical, geometrical, or numerical parameters used by the training simulation to generate the training set. As used herein, the training simulation refers to a numerically and computationally accurate reservoir simulation with enough resolution to capture all desired physical processes. In other words, the training simulation can be a high resolution, highly accurate reservoir simulation that is based on Finite Element Analysis, Finite Difference Analysis, among other mathematical simulation techniques. In embodiments, the training simulation may be a finely meshed, full physics reservoir simulation.

[0077] The dependence, $x_i = A_{ij}^{-1} b_j$, can be approximated for the sub region 502 by a

machine learning method such as a neural net, $x_i = [A_{ij}^{-1}]_{NN} b_i$, with n inputs and m outputs. In exemplary embodiments, the B and X sets are *a priori* bounded, where $b_i \in B \subset R^n$ and $x_i \in X \subset R^m$ and $m \leq n$. Further, the training set, $\{b_s, x_s\}, s=1 \dots S$, contains a good distribution within the desired parameter space, and S is large, for example, $S > 3 \times n \times m$. In some embodiments, the set of boundary conditions, b_i , uniquely determines the solution, x_i . In some embodiments, a non-unique scenario may be identified during the training phase. For example, the problem may be reduced or approximated by a similar problem with a unique solution or the set of boundary conditions may reveal that they are not good candidates for this approach. If a neural net is properly trained (to small error), it will compute the unique solution for every new or old region. Practical remedies to prevent non-unique solutions are either to split the region in smaller parts, or consider inputs both from the current and previous time steps. Sometimes using additional inputs (such as state integrals) may work. In general the ambiguity is inherited from the inverse operator approximation process, which may not have a guaranteed unique solution. The matrix equation solution computed for each sub region 502 may then be used as the solution surrogate for computing the approximate solution at block 306 of method 300 (Fig. 3). Furthermore, the solution surrogate and the associated physical, geometrical, or numerical parameters may be stored to a database to be re-used in subsequent reservoir simulations.

[0078] Fig. 6 is a process flow diagram of a method 600 for looking up and using an existing trained surrogate model or computing a new solution surrogate for each sub region 102 of a reservoir model, as needed, in accordance with an exemplary embodiment of the current invention. The method 600 starts at block 602, wherein the database of solution surrogates is searched to identify a solution surrogate that represents a suitable approximation of the sub region 502 (Fig. 5), based on a comparison of the physical, geometrical, or numerical parameters of the sub region and the solution surrogate. Examples of parameters that may serve as lookup keys for sub-regions and their surrogate model solutions include, but are not limited to row sum or column sum vectors, diagonal vectors, L1, L2, LN norms of these vectors, and so on. Physical parameters describing the sub-region may also serve as useful lookup keys. Examples of physical parameters that may serve as lookup keys include, but are not limited to, average permeability, porosity, or mobility of the sub-region or vectors of distributions of these physical variables. Examples of numerical parameters that may serve as lookup keys include, but are not limited to, time step size and geometrical descriptions of the regions, among others.

[0079] At block 602, a determination is made regarding whether a solution surrogate representing a suitable approximation of the sub region 502 exists in the database. If a suitable approximation is identified, the process flow may advance to block 606, wherein the solution surrogate obtained from the database is used to generate the state variables, x_i , of the sub region 502. If a suitable approximation is not identified, the process flow may advance to block 608.

[0080] At block 608, a determination is made regarding whether the sub region 502 is a candidate to be modeled by the machine learning method described above. Such regions may be identified by any combination of computational, analytical and interpretive methods such as seismic pattern recognition and expert analysis of the geological structure, rock properties, or experience in applying such methods. The sub region 502 may be a candidate to be modeled by the machine learning method if the heterogeneity of the rock porosity and permeability may be accurately described using a few parameters and the sub regions flow response to different boundary conditions can be captured by the solution surrogate as determined during the training period. Examples of such parameters include, but are not limited to, average permeability, porosity, or mobility of the sub-region or vectors of distributions of these physical variables. If the sub region 502 is not a candidate to be modeled by the machine learning method, the process flow may advance to block 610, and machine learning techniques for computing the solution surrogate of the sub region 502 are not used for the particular sub region 502 under consideration.

[0081] If, at block 608, it is determined that the sub region 502 is a candidate to be modeled by the machine learning method, the process flow may advance to block 612. At block 612, the boundary of the sub region may be partitioned into a plurality of boundary element types. For the sub-region 102 under consideration, the region's boundary may be partitioned into an appropriate set of boundary elements that will represent the variety of anticipated boundary element types this region is likely to encounter as part of a reservoir simulation model. For example, the boundary element types may include a combination of pressure boundaries 508 and flux boundaries 510, as discussed in relation to Fig. 5.

[0082] At block 614, the boundary condition types may be specified. For example, boundary condition types may include Neumann boundaries, Dirichlet boundaries, as well as other boundary types, and combinations thereof.

[0083] At block 616, boundary condition values may be specified for each of the boundary elements. The boundary condition values may include any suitable sampling of the

boundary parameter space. In some embodiments, the boundary condition values may be specified based on known conditions of an actual reservoir. For example, the boundary condition values for the flux boundaries 108 may be based on a known fluid production rate of the producer well 506 or a known fluid injection rate at the injector well 504. The
 5 boundary condition values for the flux boundaries 108 may also be based on the physical characteristics of the reservoir, for example, well casings, fault lines, and the like.

[0084] At block 618, a training simulation may be used to generate the training set 416, $\{b_s, x_s\}, s = 1 \dots S$. Input to the training simulation may include, the boundary condition values determined at block 616 and the physical, geometrical, or numerical parameters of the
 10 sub region determined at block 608. The training simulation may include, for example, finite element analysis of the sub region 502 using a fine mesh model of the sub region 502. The training set 416 generated by the training simulation may then be used to compute the solution surrogate, using the machine learning techniques described above.

[0085] At block 620, the solution surrogate may be stored to a database of solution
 15 surrogates. Each solution surrogate in the database may be paired with the corresponding physical, geometrical, or numerical parameters used to generate the training set 416. In this way, the solution surrogate may be reused for future reservoir simulations based on a degree of similarity between the physical, geometrical, or numerical parameters used to the generate the solution surrogate and the physical, geometrical, or numerical parameters of subsequent
 20 sub regions 102 used for future reservoir simulations. The method 600 may be repeated for each sub region 502 included in the reservoir simulation.

[0086] During block 306 of the method 300 for modeling the reservoir, the matrix equation solution generated at block 620, or retrieved from the database at block 606, may be used to generate the state variables of the sub region 502 during the computation of the
 25 approximate solution (block 306 of method 300). Generation of the state variable may be accomplished by using the solution surrogate and a different set of boundary conditions from the original boundary conditions used to generate the solution surrogate. For example, boundary conditions for one sub region 502 may be based on the state variables previously computed for an adjacent sub region 502.

[0087] In some exemplary embodiments, the training and exploitation of the Neural net allows apparently non-similar sub-regions to contribute to each other's teachings. This may occur if, for example, the matrix equation derived by a discretized form of the reservoir simulation yields, for some boundary elements, a similar form as that from another region

with different physical properties. This may be possible because the abstraction imposed by this approach will allow homogenization of different physical properties in the discretized form of the matrix equation.

Computing a Coarse Scale Approximation

5 [0088] In some embodiments, a reservoir simulation may be performed by dividing the reservoir model into a plurality of coarse grid cells. The state variables for each coarse grid cell may be computed using a formulation of Darcy's Law. Supervised machine learning may be used to generate a coarse scale approximation of the phase permeability of the coarse grid cell, which may be used during the computation of the approximate solution at block 306
10 of method 300. Computing the approximate solution at block 306 may involve determining a different coarse scale approximation of the phase permeability for each of the coarse grid cells or cell faces involved in the simulation.

[0089] The multi-phase extension of Darcy's law, yields the formula shown in Eqn. 6.

$$\bar{v}_v = -\frac{1}{\mu_v} \bar{K}_v \nabla P_v \quad \text{Eqn. 6}$$

15 In the above equation, $\bar{K}_v$ is phase permeability which contains both the absolute and relative phase permeability, μ_v is the phase viscosity, and the pressure gradient, ∇P_v , may include saturation dependent capillary pressure and gravity force. Thus, the phase velocity, $\bar{v}_v$, is a function of potential gradient and phase permeability, which is itself a function of phase saturation and scale lengths.

20 [0090] Fig. 7 is a one-dimensional model of a coarse grid cell 700, in accordance with an exemplary embodiment of the present techniques. The coarse grid cell shown in Fig. 7 includes a cluster of three fine grid cells 702, each of which may be characterized by a fine grid permeability 704. The line 706 represents actual phase saturation across the three fine grid cells 702. The actual phase saturation may be discretized for each fine grid cells 702, as
25 shown by lines 708, which represents the discretized scalar saturation of phase in each of the fine grid cells 702. The boundary conditions of the coarse cell may include an input phase velocity 710 and output phase velocity 712. The coarse scale approximation of the phase permeability for the coarse grid cell 700 may be characterized as a function of the fine grid permeability of each of the fine grid cells. The fine grid permeability of each of the fine grid
30 cells is a function of saturation and, therefore, time. For example, the coarse scale

approximation of the phase permeability of the coarse grid cell 700 at the end of the fine grid time steps may be a function of the phase permeability history of the fine grid cells 702, as represented by the formula shown in Eqn. 7.

$$k_{v, effective}(t^n) = f[k_{v,1}(S_{v,1}(t^n), k_{v,2}(S_{v,2}(t^n), k_{v,3}(S_{v,3}(t^n), k_{v,1}(S_{v,1}(t^{n-1}), k_{v,2}(S_{v,2}(t^{n-1}), k_{v,3}(S_{v,3}(t^{n-1}), \dots, scale_length_param] \quad \text{Eqn. 7}$$

- 5 **[0091]** In the above formula, $K_{v, effective}(t^n)$ equals the coarse scale approximation of the coarse grid cell 700 at a time step, n. The term $K_{v,i}$ equals the discretized phase permeability at each fine grid cell, and the term $S_{v,i}$ equals the phase saturation at each fine grid cell. For two-dimensional or three-dimensional models, the effective phase permeability can be written as a tensor as shown in Eqn. 8.

$$10 \quad \begin{pmatrix} \mathbf{v}_{v,x} \\ \mathbf{v}_{v,y} \end{pmatrix} = -\frac{1}{\mu_v} \begin{pmatrix} \mathbf{k}k_{v,xx} & \mathbf{k}k_{v,xy} \\ \mathbf{k}k_{v,yx} & \mathbf{k}k_{v,yy} \end{pmatrix} \begin{pmatrix} \nabla P_{v,x} \\ \nabla P_{v,y} \end{pmatrix} \quad \text{Eqn. 8}$$

- [0092]** Fig. 8 is a two dimensional coarse grid cell, in accordance with an exemplary embodiment of the present techniques. The coarse grid cell shown in Fig. 8 includes a three-by-three matrix of nine fine grid cells. Each of the fine grid cells may be associated with a discretized phase permeability. The fine scale phase velocity at the cell interface is represented as, $V_{v,i}$. As indicated by the formula shown in Eqn. 9, the effective phase permeability tensor for the coarse cell may be a function of any of the model parameters of the fine grid, for example, the phase permeability, phase saturation, phase velocity, and the like.

$$15 \quad k_{v, effective}(t) = f[k_{v,i}, S_{v,i}, V_{v,i}, \dots, model\ parameters,] \quad \text{Eqn. 9}$$

- 20 Machine learning algorithms such as neural nets may be used to provide the effective permeability, k, on a specified coarse grid element given the boundary phase velocity. In such an embodiment, $k_{v, effective}$ is the output and $k_{v,i}, S_{v,i}, V_{v,i}$, and model parameters are input.

- [0093]** The saturation and velocity parameters in the independent variable list may be for all fluid phases. In some embodiments, global information may be used to generate a more realistic set of boundary conditions for the training, in which case model parameters in the equation above will include physical parameters for fine grid cells outside the boundary of the coarse grid cell 700. To increase the likelihood that the effective permeability may be re-used for multiple coarse grid cells, the parameter space should not be too large. The sampling of the parameter space can be chosen to enable sufficient coverage of the parameter

space while increasing the probability that the effective permeability may be re-used for multiple coarse grid elements. Using the technique described above, effects such as hysteresis may be considered naturally as an extension of phase permeability scale up rather than a special physical process.

5 [0094] Fig. 9 is a process flow diagram of a method 900 of performing a reservoir simulation using the coarse scale approximation of the phase permeability, in accordance with an exemplary embodiment of the present techniques. The method 900 may begin at block 902, wherein the reservoir model may be divided into a plurality of coarse grid cells 700 based on parameters such as heterogeneity and coarse scale fluid properties, for example,
10 phase permeability, phase saturation, and the like.

[0095] At block 904, one of the coarse grid cells 700 generated at block 902 may be used to identify a matching coarse grid cell model in a database of previously processed coarse grid cells. Identifying the matching coarse grid cell model may include comparing the model training parameters of the present coarse grid cell 700 with the training parameters stored for
15 each of the previously processed coarse grid cells to identify an existing model that more closely resembles the current model. As described above for the approximation of an inverse operator, metrics to compare and search for models may include mathematical parameters such as vectors of permeabilities, derived values of these parameters such as norms of the vectors, and model parameters such as those describing discretization and time stepping. For
20 these examples, standard parameter distance metrics such as Euclidian distance may be used.

[0096] At block 906, a determination is made regarding whether a matching coarse grid cell model for the present coarse grid cell 700 has been identified. If a matching model has been identified, the process flow may advance to block 908. At block 908, the coarse scale approximation of the phase permeability associated with the previously computed coarse grid
25 cell may be obtained from the database. The coarse scale approximation of the phase permeability obtained from the database may be used during the reservoir simulation to compute the state variables for the coarse grid cell 700.

[0097] If a matching model has not been identified at block 906, the process flow may advance to block 910. At block 910, a fine grid model is generated for the coarse grid cell.
30 The coarse grid cell may be divided into a suitable number of fine grid cells 702. For each of the fine grid cells 702, a suitable set of boundary conditions that cover current and expected variations and physical, geometrical, or numerical parameters such as phase permeability may be specified.

[0098] At block 912, the fine grid training simulations may be performed over the coarse grid cell 700. The fine grid training simulations may be performed using a numerically and computationally accurate reservoir simulation with enough resolution to capture all desired physical processes, as described above in relation to Fig. 5. In this manner, a variety of simulated boundary conditions may be obtained. The simulated boundary conditions computed for the coarse grid cell 700 may be used to train the neural net to obtain the approximate phase permeability of the coarse grid cell 700. As described above, $k_{v, \text{effective}}$, is the output and $k_{v,i}$, $S_{v,i}$, $V_{v,i}$, and model parameters are input. Techniques such as over-sampling may be used to provide more realistic boundary conditions. The training may be performed for both steady state and dynamic conditions, with potentially any combination of physical effects such as capillary pressure and gravity.

[0099] At block 914, the approximate phase permeability of the coarse grid cell 700 may be stored to a database for re-use in subsequent reservoir simulations. Additionally, the model training parameters used to compute the approximate phase permeability may be stored to the database in association with the approximate phase permeability for use in determining whether the approximate phase permeability can be used for a given coarse grid cell encountered in a subsequent reservoir simulation.

[00100] The techniques discussed above provide for scale-up from the traditional geological model scale to reservoir simulation scale. In some embodiments, the present techniques can be applied to scale-up from the laboratory relative permeability measurements made on core.

Approximating a Constitutive Relationship

[00101] Fig. 10 is a two-dimensional view of a reservoir model showing a planar projection of a computational mesh, in accordance with an exemplary embodiment of the present techniques. The reservoir model may include an irregular, coarse mesh 1000, which may be a mesh of an actual physical space to be modeled. The coarse mesh 1000 may include irregular shaped coarse grid cells 1002. For example, the coarse mesh may include various geographical features such as an eroded region 1003. Each coarse grid cell 1002 may be further subdivided into a fine mesh 1004 that includes a plurality of fine grid cells 1006. Additionally, the coarse mesh 1000 of the actual physical space may be mapped to a reference mesh 1008. The reference mesh 1008 may be an orthogonal mesh that includes a plurality of rectangular coarse grid cells 1010, wherein each of the irregular shaped coarse

grid cells 1002 may be mapped to a corresponding rectangular coarse grid cell 1010 of the reference mesh 1008. Each coarse grid cell 1012 may be associated with a corresponding potential, or pressure. The boundary between two coarse grid cells may be associated with a corresponding flux and may be referred to as flux interface 1012.

5 **[00102]** In some embodiments, supervised machine learning may be used to generate a constitutive relationship between the flow response at the flux interface 1012 and the pressure difference, or potential drop, between each of the coarse grid cells 1010 surrounding the flux interface 1012. Further, the constitutive relationship may account for the difference in geometry between the rectangular coarse grid cells 1040 of the reference mesh 1030 and the
10 irregular coarse grid cells 1010 of the irregular mesh 1000. In this way, the constitutive relationship computed for the coarse grid cells 1010 of the reference mesh 1008 may be reused in future reservoir simulations wherein the shape of the coarse grid cells varies from the original cell shape on which the training was based.

[00103] The potential drop between two coarse grid cells 1010, $\Delta\Phi_{1-2}$, may be written as
15 a function of the fluxes on the flux interface 1012 between two coarse grid cells 1010, $F_1...F_7$, as represented by the formula shown in Eqn. 10.

$$\Delta\Phi_{1-2} = f\left(F_1, \dots, F_7, \dots, geometry, \overline{K}_v(S_v(t)), params\right) \quad \text{Eqn. 10}$$

Conversely, the flux at each flux interface 1012 may be written as a function of potential in the coarse grid cells 1010 surrounding the flux interface 1012, as represented by the formula
20 shown in Eqn. 11.

$$F_7 = f\left(\Phi_1, \dots, \Phi_8, \dots, geometry, \overline{K}_v(S_v(t)), params\right) \quad \text{Eqn. 11}$$

[00104] In the above formulas, F_i corresponds with a flux at a flux interface 1012 between two coarse grid cells 1004. The term Φ_i corresponds with the potential at one of the coarse grid cells 1010. The term “*geometry*” is a value that corresponds with the geometry of the
25 irregular coarse grid cell 1002. The geometry may be parameterized using geometrical parameters such as grid cell height, width, depth, curvature on a side, and so on. The term “ $\overline{K}_v(S_v(t))$ ” represents the phase permeability of the support region defined by the coarse grid cell, which is a function of the phase saturation at time step, t . The term “*params*” represents additional parameters that describe the system such as fluid properties.

30 **[00105]** The constitutive relationship between flux and pressure for each coarse grid cell 1010 may be computed using machine learning techniques, for example, using a neural net

such as the neural net described in relation to Fig. 4. For example, in accordance with Eqn. 11, the input to the machine learning method such as the neural net may be Φ_i , *geometry*, $\overline{K}_v(S_v(t))$, and *params* and the output may be the flux, F , on the boundary of the cell. Depending on the characteristics of the coarse grid cell 1010, the constitutive relationship
 5 between flux and pressure will generally not correspond with Darcy's Law. However, the constitutive relationship should degenerate to Darcy's law for simple discretization, isotropic effective properties, and orthogonal grids.

[00106] Fig. 11 is a process flow diagram of a method 1100 of performing a reservoir simulation using a constitutive relationship between pressure and flow, in accordance with an
 10 exemplary embodiment of the present techniques. The method 1100 may begin at block 1102, wherein a coarse grid simulation model for a reservoir is generated and parameterized by the terms in Eqn. 11, such as, Φ_i , *geometry*, $\overline{K}_v(S_v(t))$, and *params*. The resulting simulation model may include a coarse mesh 1000 with a plurality of irregular shaped coarse grid cells 1002 (Fig. 10). A set of descriptive parameters such as phase permeability and cell
 15 geometry may be specified for each coarse grid cell 1002.

[00107] At block 1104, a flux interface 1012 is selected and a database of previously computed constitutive relationships may be searched to identify an existing constitutive relationship that may be used to compute the flow response for the flux interface 1012 (Fig. 10). Identifying the constitutive relationship may include comparing the parameters of the
 20 coarse grid cells 1012 surrounding the flux interface 1012 with the parameters of previously generated coarse grid cells 1012 to identify an existing model that closely resembles the current model. As described above for the approximation of an inverse operator, metrics to compare and search for models may include mathematical parameters such as vectors of permeabilities, geometry, permeability distribution of the surrounding coarse grid cells 1010
 25 or derived values of these parameters such as norms of the vectors, and model parameters such as those describing discretization and time stepping. For these examples, standard parameter distance metrics such as Euclidian distance may be used.

[00108] At block 1106, a determination is made regarding whether a suitable approximation of the current flux interface 1012 model exists in the database of previously
 30 computed constitutive relationships. If a suitable approximation does exist, the process flow may advance to block 1108, wherein the previously computed constitutive relationship may be used for the selected flux interface 1012 during the reservoir simulation. During the

simulation, the conservation laws, such as conservation of mass, momentum, angular momentum, energy, and the like, will be enforced across the flux interface 1012 between the coarse grid cells 1010.

[00109] If, at block 1106, a suitable approximation does not exist for the flux interface
5 1012, a new constitutive relationship may be computed for the selected flux boundary 1012 and the process flow may advance to block 1110. At block 1110, a fine mesh model may be generated for each of the coarse mesh cells 1010 surrounding the flux interface 1012. The fine mesh model may include a plurality of fine grid cells 1004 for each of the coarse grid cells 1010 surrounding the selected flux boundary 1012. As indicated by block 1112, block
10 1110 may be repeated for coarse grids of different scales (cell sizes) to increase the reusability of the resulting constitutive relationship computed for the flux boundary 1012. In this way, the constitutive relationship may be used to represent phenomena at different physical scales encountered for different simulation executions.

[00110] At block 1114, a fine scale simulation may be performed for each coarse grid cell
15 1004 using a training simulation, which may be a numerically and computationally accurate reservoir simulation with enough resolution to capture all desired physical processes, as described above in relation to Fig. 5. The fine scale simulation provides a set of boundary conditions and initial conditions, which may be used as the training set for training the neural net 400 (Fig 4). For example, the input 412 of the neural net 400 may include the potential at
20 each coarse grid cell 1006 as well as other parameters specified in Eqn. 11. The desired output 414 of the neural net 400 may include the flux at each interface between the coarse grid cells 1006. In some embodiments, over-sampling and other techniques are used to provide more realistic boundary conditions. The training may be performed for both steady state and dynamic conditions, with potentially any combination of physical effects such as
25 capillary pressure and gravity, thus allowing for model reuse.

[00111] As indicated by block 1116, block 1114 may be repeated for coarse mesh cells
1004 of different primary shape types. The constitutive relationships derived for each different primary shape type may remain valid under mild geometrical deformation, which may be applied to construct a coarse grid model of a specific reservoir, and thus, will be
30 reusable for different reservoirs.

[00112] At block 1118, the constitutive relationship between fluid flux and potential gradients for the selected flux interface 1012 may be extracted from the trained neural net

400. In some embodiments, the constitutive relationship used for training may be that of the fine grid solution after it has been averaged or smoothed.

[00113] At block 1120, fine grid simulations computed for each of the different mesh scales generated at block 1114 and 1116 may be evaluated to determine an uncertainty estimate for the coarse grid constitutive relationship. This may be done through numerical experiment using a variety of different fine scale parameter distributions. The uncertainty estimate is a measure of the accuracy of the constitutive relationships computed at different coarse scales. The uncertainty estimate may be used to determine an estimated level of geologic feature detail that will provide suitable accuracy during the generation of the training set used to train the neural net.

[00114] At block 1122, a determination may be made regarding which groups of parameters are more amendable to constitutive modeling and which groups of parameters are more amenable to full-scale simulation. Parameters that depend on material or geometrical parameters will tend to be more amenable to constitutive modeling, while parameters that are process dependant will tend to be more amenable to full-scale simulation. This determination may be made a-priori as well as by evaluating the sensitivity of the trained neural net 400 to small changes in material parameters and boundary conditions.

[00115] At block 1124, the constitutive relationship and the model training parameters used to generate the constitutive relationship may be stored to a database for future use in subsequent reservoir simulations. The model training parameters may include the coarse grid geometry, phase permeability tensor as a function of capillary pressure tables, and characteristics of the coarse grid model including the time dependent parameters.

Integration of Machine Learning Based Approximations

[00116] Fig. 12 is a schematic view of a coarse grid model 1200 of a reservoir, in accordance with an exemplary embodiment of the present techniques. In some exemplary embodiments, the techniques for computing a machine learning based solution surrogate for a reservoir sub region described above may be combined during reservoir simulation. The coarse grid model 1200 may include a plurality of sub regions 1202, each of which may be characterized according to different physical, geometrical, or numerical parameters, for example, different rock porosity, phase permeability, and the like. A first sub region 1202 may include an injector well 1204, and an nth sub region may include a producer well 1206. The injector well 1204 and producer well 1206 may be surrounded by near-well regions 1208

and 1210, both of which may be modeled separately. Each sub region 1202 may be approximated with a different solution surrogate computed using one of the techniques described above. For example, some sub regions 1202 may be approximated with an inverse operator, A^{-1} , as described in relation to Figs. 5 and 6. Some sub regions 1202 may be approximated with a coarse scale relative permeability operator as described in relation to Fig. 7-9. Some sub regions 1202 may be approximated with a surrogate constitutive relationship between flux and pressure, as described in relation to Figs. 10 and 11. Each of the sub regions 1202, the near well regions 1208 and 1210, the injector well 1204, and the producer well 1206 may be referred to as “elemental regions.” Between each elemental region is an interface 1212. A solution of the reservoir model 1200 may be computed by computing the flow response for each elemental region individually, based on the solution surrogate available or suitable for each elemental region 1202. The flow response characteristics may be computed for each elemental region in order from the injector well 1204 to the producer well 1206. The boundary conditions for each elemental region may be determined based on the flux at the interface 1212 determined for the previously computed sub region 102.

[00117] Fig. 13 is a process flow diagram of a method 1300 for modeling fluid flow in a reservoir, in accordance with an exemplary embodiment of the present techniques. The method 1300 may begin at block 1302, wherein the coarse grid model 1200 (Fig. 12) may be identified and parameterized. Identifying and parameterizing the coarse grid simulation model 1200 may include dividing the reservoir model into a plurality of sub regions 1202 based on parameters such as heterogeneity and coarse scale fluid properties, for example, phase permeability, phase saturation, and the like. The reservoir model 1202 may be divided into sub regions 1202 such that each sub region 1202 exhibits a relatively consistent rock texture that may be properly modeled via machine learning methods. The sub-regions 1202 may be more amenable to machine learning based modeling techniques if the heterogeneity of porosity and permeability of the sub-region 102 may be well described by just a few parameters and the flow response of the sub region 1202 to different boundary conditions may be properly captured by the surrogate model. Such sub region 1202 may be identified by any combination of computational, analytical and interpretive methods such as seismic pattern recognition and expert analysis.

[00118] At block 1304, a sub region 1202 may be selected and used to search database of existing solution surrogates. Identifying the matching solution surrogate for the sub region

1202 may include comparing the model parameters of the selected sub region 502 (Fig. 5) with the model parameters stored for each of the previously generated solution surrogates to identify an existing solution surrogate whose model parameters closely resemble the selected sub region 502.

5 [00119] At block 1306, a determination is made regarding whether a matching solution surrogate for the present sub region 1202 has been identified. If a matching solution surrogate has been identified, the process flow may advance to block 1308. At block 1308, the identified solution surrogate may be obtained from the database. The solution surrogate obtained from the database may be used during the reservoir simulation to compute the flow
10 response at the interface 1212 between the current sub region 1202 and the next sub region 1202. During simulation, the applicable conservation laws, such as conservation of mass, momentum, angular momentum, energy, and the like, will be enforced across the flux interface 1212 between the sub regions 1202.

[00120] If a matching model has not been identified at block 1306, the process flow may
15 advance to block 1310, wherein a solution surrogate may be computed for the sub region 1202, using a machine learning method such as the neural net 400 (Fig. 4). The training set used to train the training neural net 400 may be computed by running a training simulation, which may be a numerically and computationally accurate reservoir simulation with enough resolution to capture all desired physical processes including the fluid flow over the sub
20 region 1202. The training set may then be used to compute the solution surrogate, as described above in relation to Figs. 5-11. In some exemplary embodiments, a plurality of training sets may be generated by running a plurality of full-physics reservoir simulations using a variety of boundary conditions that are likely to be encountered in subsequent reservoir simulations in which the resulting solution surrogate will be used. In some
25 embodiments, the training set may be computed by another surrogate model. The resulting training sets may be used to train the neural net multiple times, and a least squares algorithm may be applied to the multiple neural net solutions to compute the surrogate solution.

[00121] At block 1312 the solution surrogate may be used to compute the state variables such as fluid properties or fluid flow at the interfaces 1212 of the sub region 1202. For
30 example, given an initial set of state variables at the interface 1212, the solution surrogate provides the change in the state variables at the interface 1212 at the end of a given time-step. The flow at the interface 1212 may be governed by any suitable model for pressure and flow

change across a boundary, such as the inverse matrix operator, A^{-1} , Darcy's Law, or a machine learning based constitutive relationship.

[00122] At block 1314, the model parameters for the sub region 1302 and the resulting solution surrogate may be stored to the database for use in subsequent reservoir simulations.

5 The process flow described above may be repeated for each sub region 1202. To reduce the parameter space used to develop the training sets for the machine learning algorithm, a reduced set of parameters to describe the simulation system may be identified by methods such as principle component analysis (PCA) or proper orthogonal decomposition (POD). The use of PCA or POD may reveal that full systems with distinct and unique looking
10 parameter sets are indistinguishable in a reduced system and may therefore be excluded as extraneous.

Experimental results – One Dimensional Diffusion

[00123] Fig. 14 is a schematic view of a one dimensional medium 1400 through which a porous flow may be simulated using machine learning. The medium 1400 may include outer
15 sub regions 1402 with a diffusion coefficient of one. The medium 1400 may also include a central sub region 1404 over which the diffusion coefficient varies between a very high diffusion coefficient, for example 10, and a very low diffusion coefficient, for example 0.1. The diffusion coefficient may be randomly specified at 100 discrete intervals along the central sub region 1404. The diffusion coefficient across the medium 1400 is shown in the
20 corresponding graph 1406, wherein the x-axis 1408 represents the distance along the medium and the y-axis 1410 represents the diffusion coefficient.

[00124] Diffusion in the medium 1400 is caused by a non-stationary boundary condition at a left boundary 1412, where a concentration is specified as a sine function with amplitude of 1.0. The right bound 1414 remains closed (no-flow). The exact frequency of boundary
25 condition oscillations was excluded from system parameters to force the model to describe any unknown variations without memorizing a frequency "hint." The goal of the present experiment was to relate the concentration at a left bound 1416 of the central sub region 1404 with the concentration at a right bound 1418 of the central sub region 1404 using a neural net.

[00125] Fig. 15 is a response diagram of the medium shown in Fig. 14. The response
30 diagram shows the point-to-point dependence between the concentration at the left bound 1416 of the central sub region 1404 with concentration at the right bound 1418 of the central sub region 1404 generated by a finite difference simulation. The data represented by the

response diagram may be used as a training set for training a neural network. The inputs to the neural network are the concentrations at the left bound 1416 and the right bound 1418 of the central sub region 1404 at some number of previous time-steps. The system has one external parameter, which is the fraction of low diffusion coefficient cells compared to high diffusion coefficient cells. The system also includes embedded sequences of concentrations from the left bound 1416 and right bound 1418 of the central sub region 1404. The desired output of the neural network is the value of concentration at the right bound 1418 of the central sub region 1404 at the next time step. Modeled in this way, a random sub region can be extracted from the finite difference simulation scheme and replaced with a neural net that exchanges information with the rest of the system at each time step.

[00126] Fig. 16 is a graph 1600 of test data comparing a finite element simulation of the sub region shown in Fig. 14 with a machine learning based solution surrogate simulation as described in relation to Figs. 14 and 15. The y-axis 1602 represents the concentrations at the right bound 1418 of the central sub region 1404. The x-axis 1604 represents the time step. The test data includes twenty trajectories representing concentrations at the right bound 1418 of the central sub region 1404 as a function of time step for twenty different central sub region 1404 compositions. The composition of the central sub region was varied for each trajectory by randomly varying the fraction of low diffusion coefficient cells to high diffusion coefficient cells. The neural net solution surrogate included three layers of nonlinear neurons, and three previous time steps were included as input to the neural net. Solid lines 1608 represent finite element simulated data. Dashed lines 1610 represent machine-learning based solution surrogate simulated data. As shown in Fig. 16, the neural net solution surrogate provided as average precision equal to the deviation between samples.

Experimental results – Two Dimensional Transport

[00127] Fig. 17 is a fine mesh simulation model 1700 used to develop a training set for training a neural net solution surrogate to porous media flow. The fine mesh simulation model 1700 includes a central sub region 1708, which represents a region of shale. The middle shale region contains non-transparent barriers 1710, creating a complicated fine grain flow. Steady state flow was established between a single injector well 1702 and each of a number of single producer wells 1704 positioned at varying locations labeled “1” to “13.” A tracer (not shown) was introduced at the injector well with sinusoidal time dependence. The main liquid flow from the injector well 1702 to any one of the producer wells 1704 is stationary. The injector well 1702 starts to pump the tracer substance, which follows pressure

gradients and flow. The distribution of the tracer concentration is observed as a function of time and the X and Y spatial coordinates.

- 5 **[00128]** The goal of the present experiment was to approximate the flow response of the central sub region 1708 by means of a machine-learning model. Forty reservoir simulations were carried out, with different parameters settings such as the shale length fraction, the shale spacing fractions in X and Y directions, shale region extent, and coordinates of each of the producer wells 1704. Additionally, the location of the producer well 1704 was changed to yield a different flow pattern and hence a different set of flow boundary conditions along the two sides of the central sub region 1708.
- 10 **[00129]** The first trial task of each simulation was to approximate the complete fluid flow in the fine mesh simulation model 1700 as indicated by the tracer concentration as a function of time and the X and Y coordinates. The goal is to create a neural net model with fewer neuron weight parameters compared to the total number of values in the tabular numerical solution of the simulation. It was found that results from a neural net model with 500 weight
- 15 parameters corresponding to a compression ratio of 1:1000 provided enough accuracy to be visually similar to the results from the full simulation. A neural net with 500 nodes provided significant compression of the surrogate model compared to the full simulation model. Next, the boundary of the central sub region 1708 was split into four segments 1802, as shown in Fig. 18.
- 20 **[00130]** In a slightly different setting all data from the first half of a simulation (plus a complete injector history) were used for training, with the aim of projecting the solution to the second half. This simulation demonstrated accuracy during 10%-20% at the beginning of second half time, and then degraded. It is worth noting that the training time was a couple of hours on a standard PC. This is of the same order as the cost of running the simulations.
- 25 **[00131]** Fig. 18 is model of the central sub region shown in the fine mesh simulation model of Fig. 17. As shown in Fig. 18, the boundary of the central sub region 1708 was split into four segments 1802. Each boundary segment 1802 corresponds with a spatially averaged concentration over the length of the boundary segment 1802. The goal was to predict the concentration at one of the boundary segments 1802 as a function of the delayed
- 30 concentration sequences at all four boundary segments 1802 under varied system state parameters, such as shale length fraction, the shale spacing fractions in X and Y directions, shale region extent, and coordinates of the producer well 1704. The concentration at the

boundary segment 1802 labeled “C4” can be represented by the formula shown in Eqn. 12:

$$C4(t) = F(C1(t-1),...C1(t-n), C2(t-1)...C2(t-n), C3(t-1),...C3(t-n), X, Y, \text{Parameters}) \text{ Eqn. 12}$$

[00132] As shown in the above formula, the concentration at boundary segment C4 at time
 5 step, t, is a function of the concentration at boundary segments C1, C2, and C3 at previous
 time steps, t-1 to t-n, the X and Y coordinates of the producer well 1704, and the system state
 parameters.

[00133] A neural network was trained using training sets computed by all but one of the
 previous simulations. The latter simulation was used as a control simulation to evaluate the
 10 performance of the trained neural network. After training the neural net, the solution
 surrogate provided by the neural net was used to predict the concentration at the C4 boundary
 segment and compared to the control simulation.

[00134] Fig. 19 is a graph of the concentration at boundary segment C4 if
 Fig. 18 at varying time steps. Specifically, the graph shows the actual concentration as
 15 computed by the control simulation overlaid on top of the concentration as computed by the
 solution surrogate provided by the trained neural net. The graph 19 shows close correlation
 between the full-physics simulation and the machine-learning based solution surrogate.

Exemplary Cluster Computing System

[00135] Fig. 20 is a block diagram of an exemplary cluster computing system 2000 that
 20 may be used in exemplary embodiments of the present techniques. The cluster computing
 system 2000 illustrated has four computing units 2002, each of which may perform
 calculations for part of the simulation model. However, one of ordinary skill in the art will
 recognize that the present techniques are not limited to this configuration, as any number of
 computing configurations may be selected. For example, a small simulation model may be
 25 run on a single computing unit 2002, such as a workstation, while a large simulation model
 may be run on a cluster computing system 2000 having 10, 100, 1000, or even more
 computing units 2002. In an exemplary embodiment, each of the computing units 2002 will
 run the simulation for a single subdomain or group of computational cells. However,
 allocation of the computing units 2002 may be performed in any number of ways. For
 30 example, multiple sub regions may be allocated to a single computing unit 2002 or multiple
 computing units 2002 may be assigned to a single sub region, depending on the
 computational load on each computing unit 2002.

[00136] The cluster computing system 2000 may be accessed from one or more client systems 2004 over a network 2006, for example, through a high speed network interface 2008. The network 2006 may include a local area network (LAN), a wide area network (WAN), the Internet, or any combinations thereof. Each of the client systems 2004 may have
5 non-transitory, computer readable memory 2010 for the storage of operating code and programs, including random access memory (RAM) and read only memory (ROM). The operating code and programs may include the code used to implement all or any portions of the methods discussed herein. Further, the non-transitory computer readable media may hold a data representation of a physical hydrocarbon reservoir, for example, a reservoir model as
10 shown in Figs. 5, 10, and 12. The client systems 2004 can also have other non-transitory, computer readable media, such as storage systems 2012. The storage systems 2012 may include one or more hard drives, one or more optical drives, one or more flash drives, any combinations of these units, or any other suitable storage device. The storage systems 2012 may be used for the storage of code, models, data, and other information used for
15 implementing the methods described herein. For example, the data storage system may hold a plurality of solution surrogates that have been computed for previously encountered sub regions and may be re-used in subsequent reservoir simulations.

[00137] The high speed network interface 2008 may be coupled to one or more communications busses in the cluster computing system 2000, such as a communications bus
20 2014. The communication bus 2014 may be used to communicate instructions and data from the high speed network interface 2008 to a cluster storage system 2016 and to each of the computing units 2002 in the cluster computing system 2000. The communications bus 2014 may also be used for communications among computing units 2002 and the storage array 2016. In addition to the communications bus 2014 a high speed bus 2018 can be present to
25 increase the communications rate between the computing units 2002 and/or the cluster storage system 2016.

[00138] The cluster storage system 2016 can have one or more tangible, computer readable media devices, such as storage arrays 2020 for the storage of data, visual representations, results, code, or other information, for example, concerning the
30 implementation of and results from the methods of Fig. 23. The storage arrays 2020 may include any combinations of hard drives, optical drives, flash drives, holographic storage arrays, or any other suitable devices.

[00139] Each of the computing units 2002 can have a processor 2022 and associated local

tangible, computer readable media, such as memory 2024 and storage 2026. The processor 2022 may include a single processing core, multiple processing cores, a GPU, or any combinations thereof. The memory 2024 may include ROM and/or RAM used to store code, for example, used to direct the processor 2022 to implement the method illustrated in Fig. 23.

- 5 The storage 2026 may include one or more hard drives, one or more optical drives, one or more flash drives, or any combinations thereof. The storage 2026 may be used to provide storage for intermediate results, data, images, or code associated with operations, including code used to implement the methods of Figs. 3, 6, 9, 11, and 13.

- [00140] The present techniques are not limited to the architecture or unit configuration illustrated in Fig. 20. For example, any suitable processor-based device may be utilized for implementing all or a portion of embodiments of the present techniques, including without limitation personal computers, networks personal computers, laptop computers, computer workstations, GPUs, mobile devices, and multi-processor servers or workstations with (or without) shared memory. Moreover, embodiments may be implemented on application specific integrated circuits (ASICs) or very large scale integrated (VLSI) circuits. In fact, persons of ordinary skill in the art may utilize any number of suitable structures capable of executing logical operations according to the embodiments.

- [00141] While the present techniques may be susceptible to various modifications and alternative forms, the exemplary embodiments discussed above have been shown only by way of example. However, it should again be understood that the present techniques are not intended to be limited to the particular embodiments disclosed herein. Indeed, the present techniques include all alternatives, modifications, and equivalents falling within the true spirit and scope of the appended claims.

CLAIMS

What is claimed is:

1. A method for modeling a hydrocarbon reservoir, comprising:
generating a reservoir model comprising a plurality of sub regions;
5 simulating at least one sub region of the plurality of sub regions using a training
simulation to obtain a set of training parameters comprising state variables and
boundary conditions of the at least one sub region;
using a machine learning algorithm to approximate, based on the set of training
parameters, an inverse operator of a matrix equation that provides a solution to
10 fluid flow through a porous media;
simulating the hydrocarbon reservoir using the inverse operator approximated for the
at least one sub region; and
generating a data representation of a physical hydrocarbon reservoir in a non-
transitory, computer-readable, medium based, at least in part, on the results of
15 the simulation.
2. The method of claim 1, wherein simulating at least one sub region of the plurality of
sub regions using the training simulation comprises specifying a set of physical, geometrical,
or numerical parameters of the at least one sub-region, wherein the set of physical,
geometrical, or numerical parameters comprises at least one of rock porosity, phase
20 permeability, and geological characteristics.
3. The method of claim 1, comprising storing the inverse operator approximated for the
at least one sub region and physical, geometrical, or numerical parameters corresponding to
the at least one sub region to a database of surrogate solutions for use in subsequent reservoir
simulations.
- 25 4. The method of claim 1, wherein the inverse operator approximated for the at least one
sub region is re-used for a second sub region based on a comparison of a set of physical,
geometrical, or numerical parameters corresponding to the at least on sub region and a new
set of physical, geometrical, or numerical parameters that characterize the second sub region.
5. The method of claim 1, wherein using the machine learning algorithm to approximate
30 the inverse operator comprises training a neural net using the training parameters, wherein the

boundary conditions are used as input to the neural net and the state variables are used as the desired output.

6. The method of claim 1, wherein simulating the at least one sub region using the training simulation comprises specifying a set of boundary condition types for each boundary
5 of the sub region and generating a fine-gridded computational mesh of the at least one sub region.

7. The method of claim 1, wherein simulating the at least one sub region using the training simulation comprises specifying a set of boundary condition values based, at least in part, on physical characteristics of the reservoir.

10 8. A method for producing a hydrocarbon from a hydrocarbon reservoir, comprising:
generating a reservoir model comprising a plurality of sub regions;
simulating at least one sub region of the plurality of sub regions using a training
simulation to obtain a set of training parameters comprising state variables and
boundary conditions of the at least one sub region;
15 using a machine learning algorithm to approximate, based on the set of training
parameters, an inverse operator of a matrix equation that provides a solution to
fluid flow through a porous media;
simulating the hydrocarbon reservoir using the inverse operator approximated for the
at least one sub region; and
20 producing a hydrocarbon from the hydrocarbon reservoir based, at least in part, upon
the results of the simulation.

9. The method of claim 8, wherein producing the hydrocarbon comprises:
drilling one or more wells to the hydrocarbon reservoir, wherein the wells comprise
production wells, injection wells, or both;
25 setting production rates from the hydrocarbon reservoir; or
any combinations thereof.

10. A system for modelling reservoir properties, comprising:
a processor;
a non-transitory machine readable medium comprising code configured to direct the
30 processor to:

generate a reservoir model comprising a plurality of sub regions;

simulate at least one sub region of the plurality of sub regions using a training simulation to obtain a set of training parameters comprising state variables and boundary conditions of the at least one sub region;

5 use a machine learning algorithm to approximate, based on the set of training parameters, an inverse operator of a matrix equation that provides a solution to fluid flow through a porous media;

simulate the reservoir using the inverse operator approximated for the at least one sub region; and

10 generate a data representation of a physical hydrocarbon reservoir in a non-transitory, computer-readable, medium based, at least in part, on the results of the simulation.

11. The system for claim 10, wherein the machine readable medium comprises code configured to direct the processor to receive a set of physical, geometrical, or numerical parameters of the at least one sub-region used for simulating the at least one sub region using the training simulation, wherein the set of physical, geometrical, or numerical parameters comprises at least one of rock porosity, phase permeability, and geological characteristics.

12. The system for claim 10, wherein the machine readable medium comprises code configured to direct the processor to store the inverse operator approximated for the at least one sub region and physical, geometrical, or numerical parameters corresponding to the at least one sub region to a database of surrogate solutions for use in subsequent reservoir simulations.

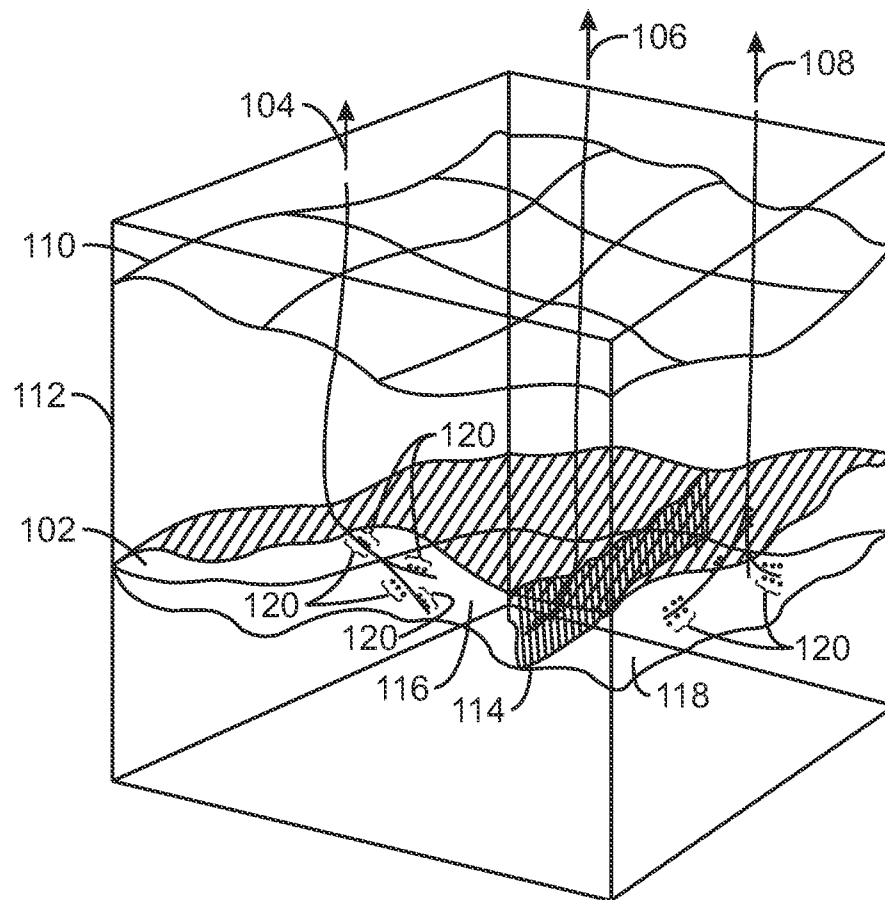
13. The system for claim 10, wherein the machine readable medium comprises code configured to direct the processor to re-use the inverse operator approximated for the at least one sub region for a second sub region based on a comparison of a set of physical, geometrical, or numerical parameters corresponding to the at least one sub region and a new set of physical, geometrical, or numerical parameters that characterize the second sub region.

14. The system of claim 10, comprising a neural net, wherein the machine readable
medium comprises code configured to direct the processor to train the neural net using the
30 training parameters, wherein the boundary conditions are used as input to the neural net and
the state variables are used as the desired output.

15. The system of claim 10, wherein the machine readable medium comprises code configured to direct the processor to receive a set of boundary condition types for each boundary of the sub region and generate a fine-gridded computational mesh of the sub region for simulating the at least one sub region using the training simulation.
- 5 16. The system of claim 10, wherein the machine readable medium comprises code configured to direct the processor to receive a set of boundary condition values for simulating the at least one sub region using the training simulation, wherein the set of boundary condition values is based, at least in part, on physical characteristics of the reservoir.
- 10 17. A non-transitory, computer readable medium comprising code configured to direct a processor to:
- create a simulation model of a hydrocarbon reservoir, wherein the simulation model comprises a plurality of sub regions;
 - simulate at least one sub region of the plurality of sub regions using a training simulation to obtain a set of training parameters comprising state variables and boundary conditions of the at least one sub region;
 - 15 use a machine learning algorithm to approximate, based on the set of training parameters, an inverse operator of a matrix equation that provides a solution to fluid flow through a porous media;
 - simulate the hydrocarbon reservoir using the inverse operator approximated for the at least one sub region; and
 - 20 generate a data representation of a physical hydrocarbon reservoir in a non-transitory, computer-readable, medium based, at least in part, on the results of the simulation.
18. The non-transitory, computer readable medium of claim 17 comprising code configured to store the inverse operator approximated for the at least one sub region and physical, geometrical, or numerical parameters corresponding to the at least one sub region to a database of surrogate solutions for use in simulating another sub-region in the simulation model or a different simulation model.
- 25 19. The non-transitory, computer readable medium of claim 17 comprising code configured to direct the processor to generate a neural net and train the neural net using the training parameters.
- 30

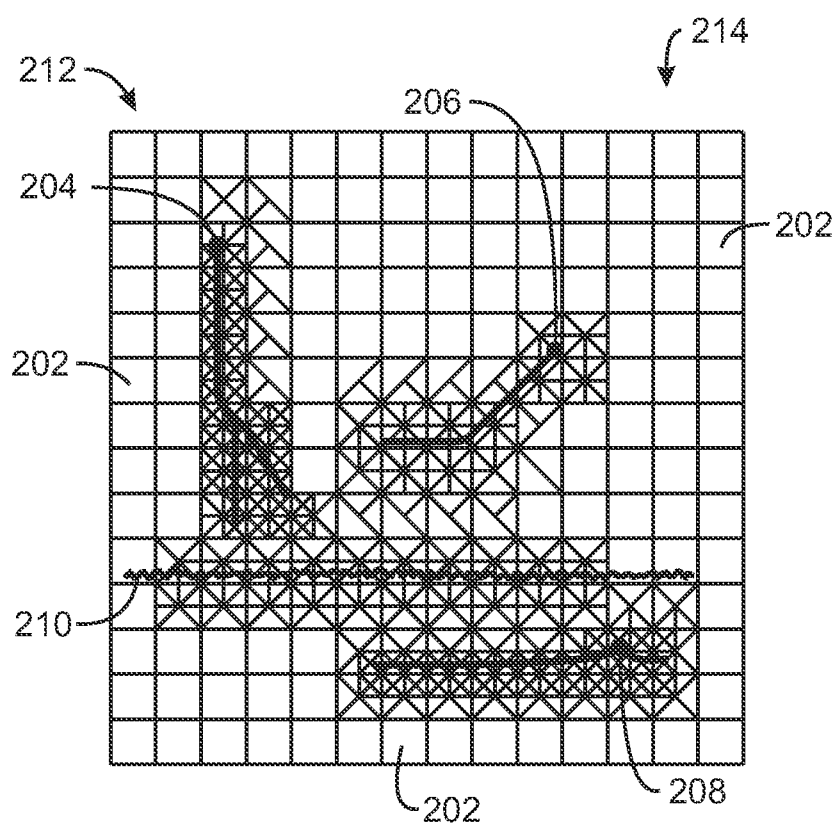
20. The non-transitory, computer readable medium of claim 17 comprising code configured to direct the processor to determine a set of boundary condition types for each boundary of the sub region, and generate a fine-gridded computational mesh of the sub region for use in the full-physics simulation of the sub region.

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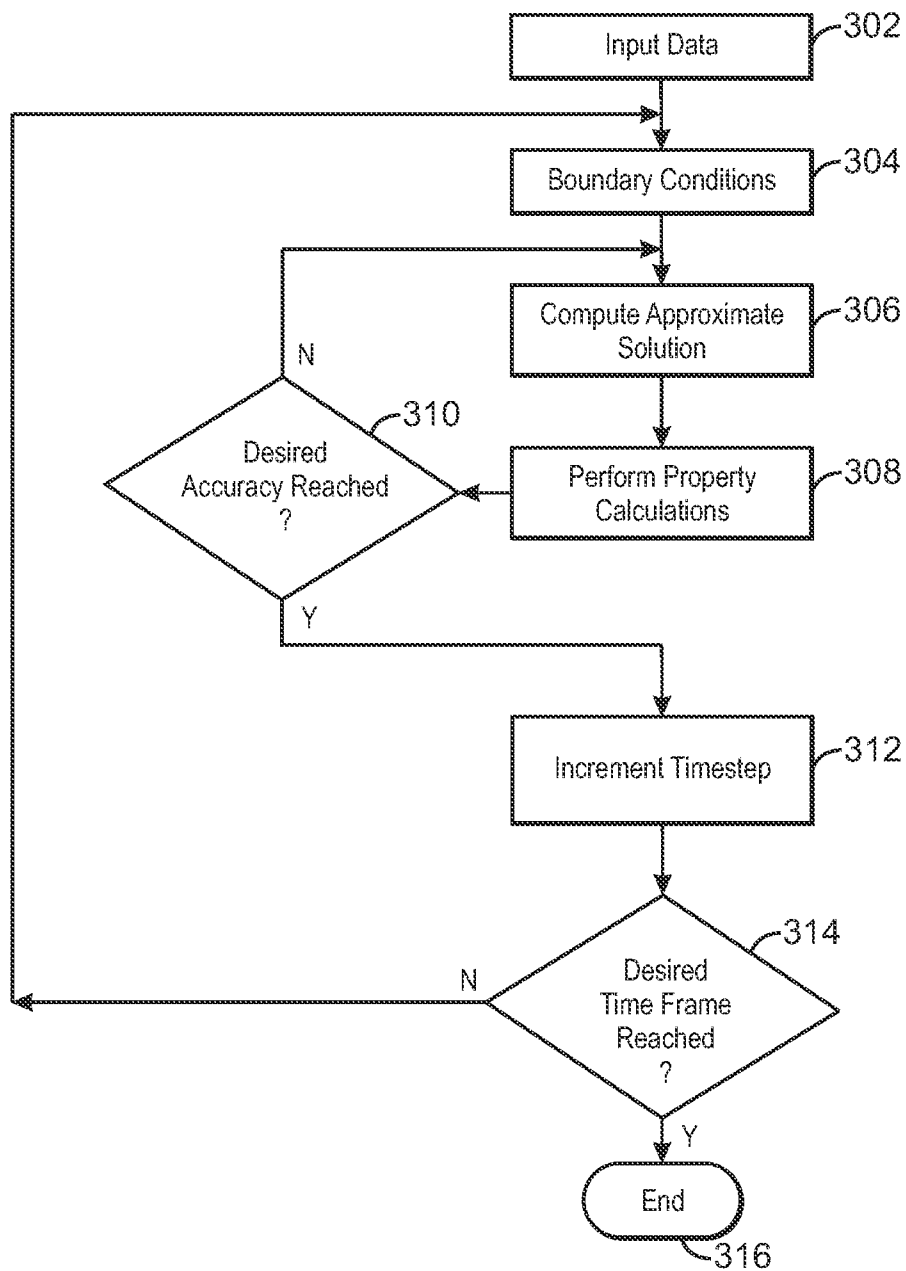
100
FIG. 1

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200
FIG. 2

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300
FIG. 3

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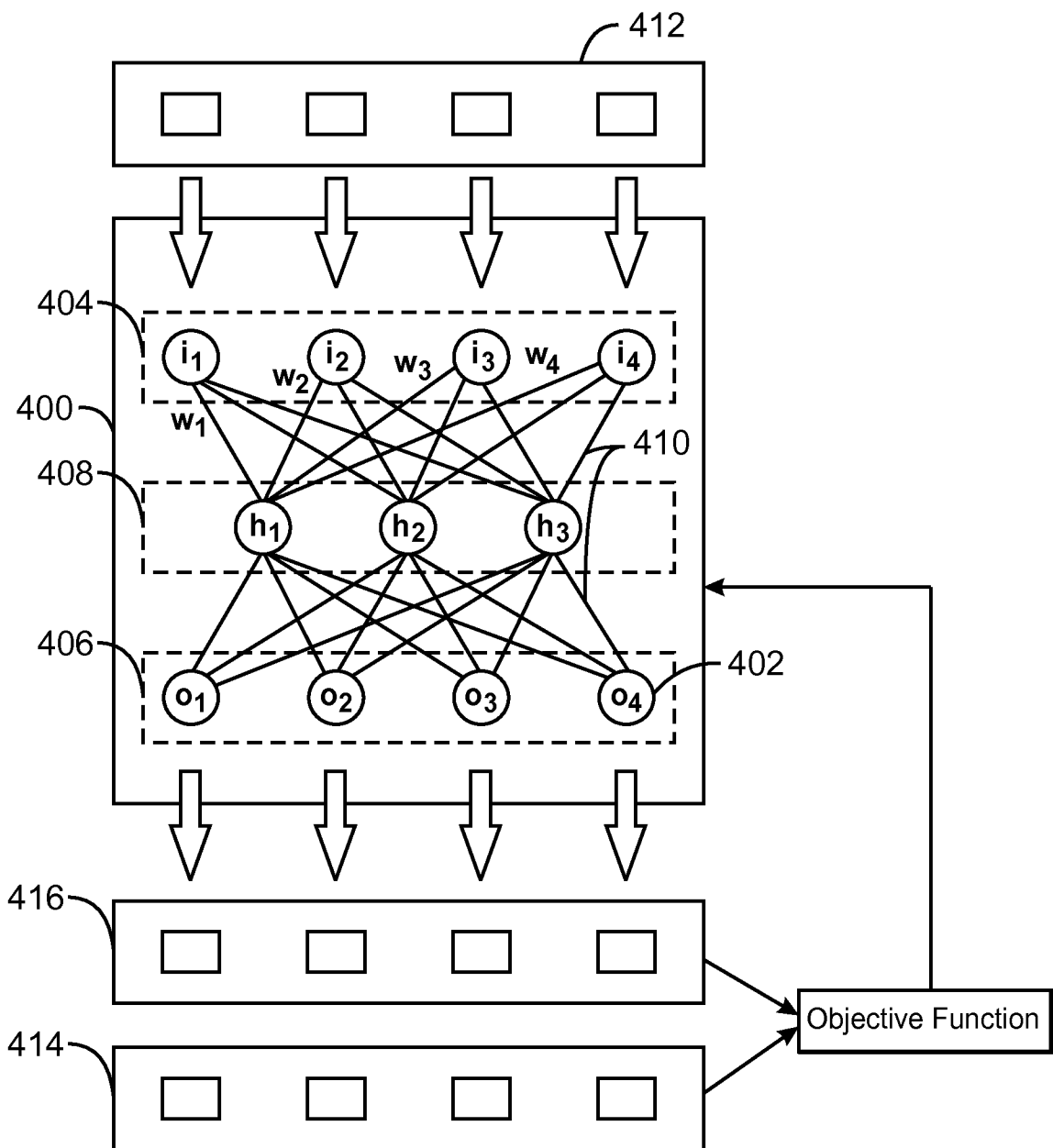
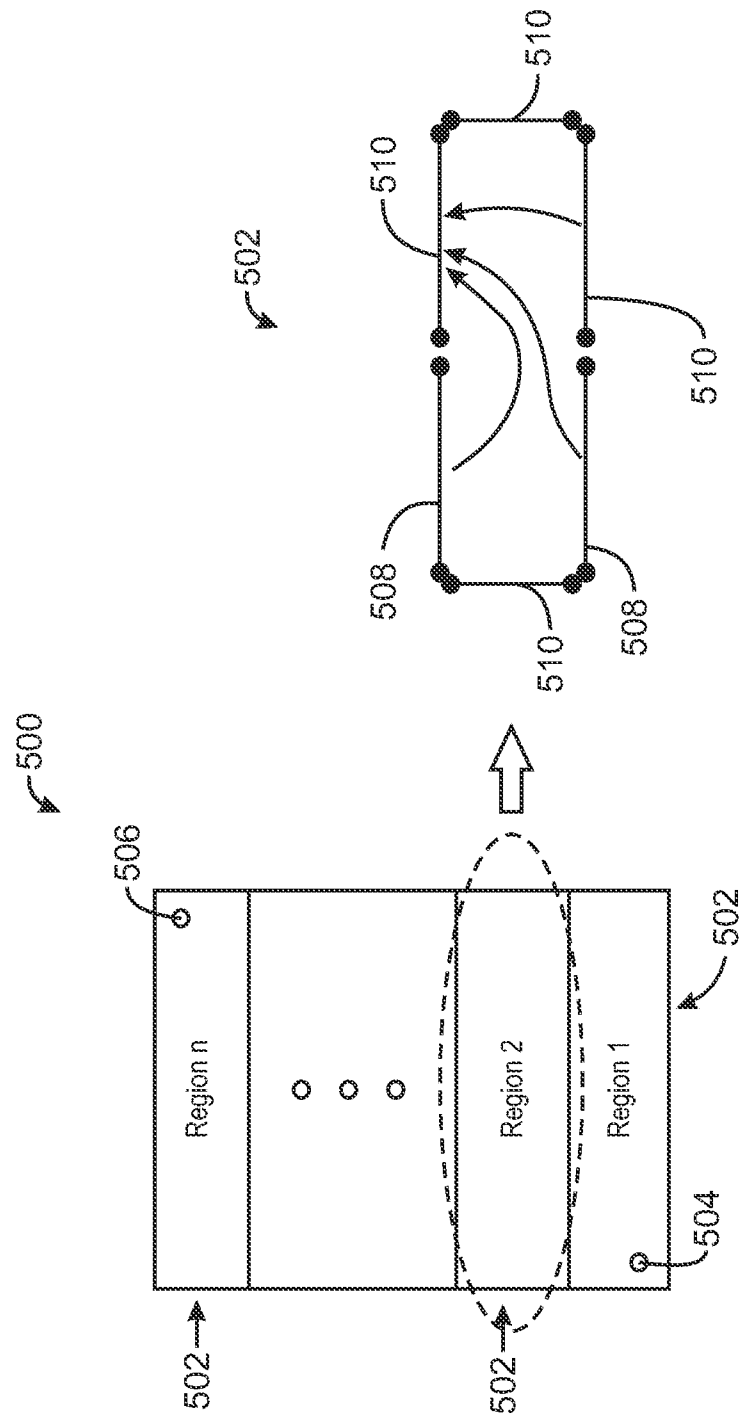


FIG. 4

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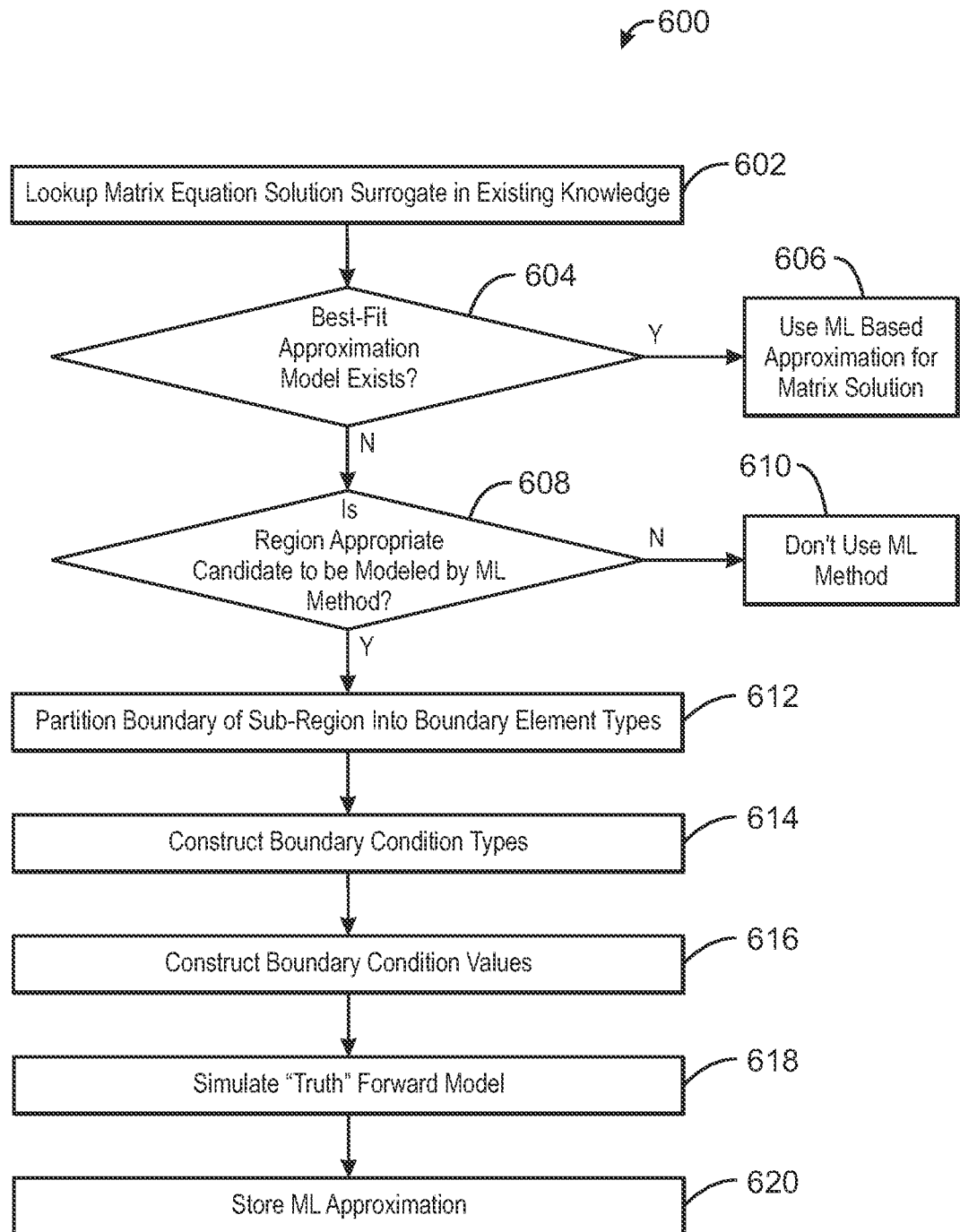


FIG. 6

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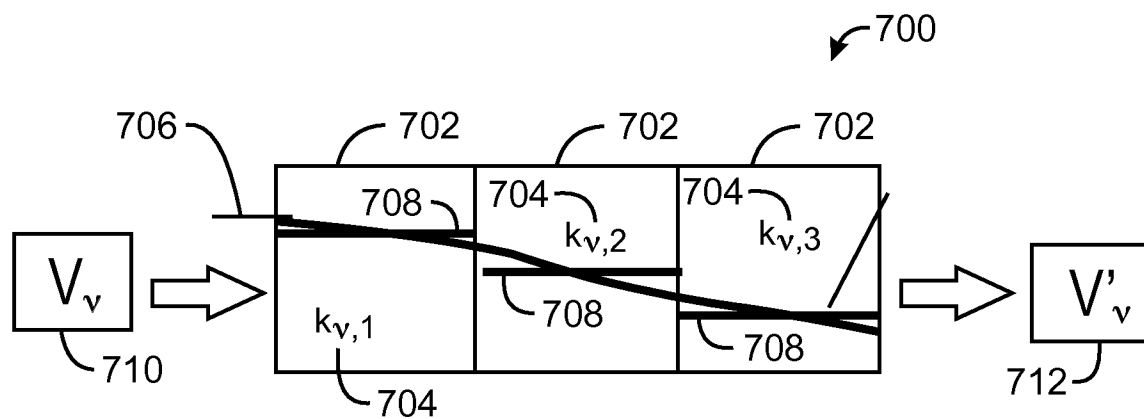


FIG. 7

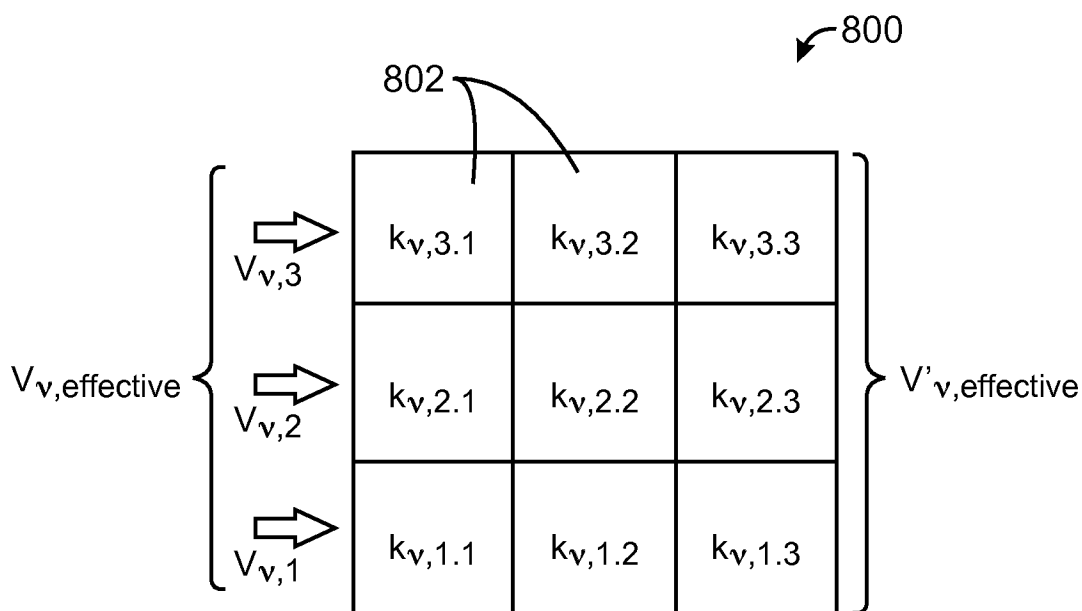


FIG. 8

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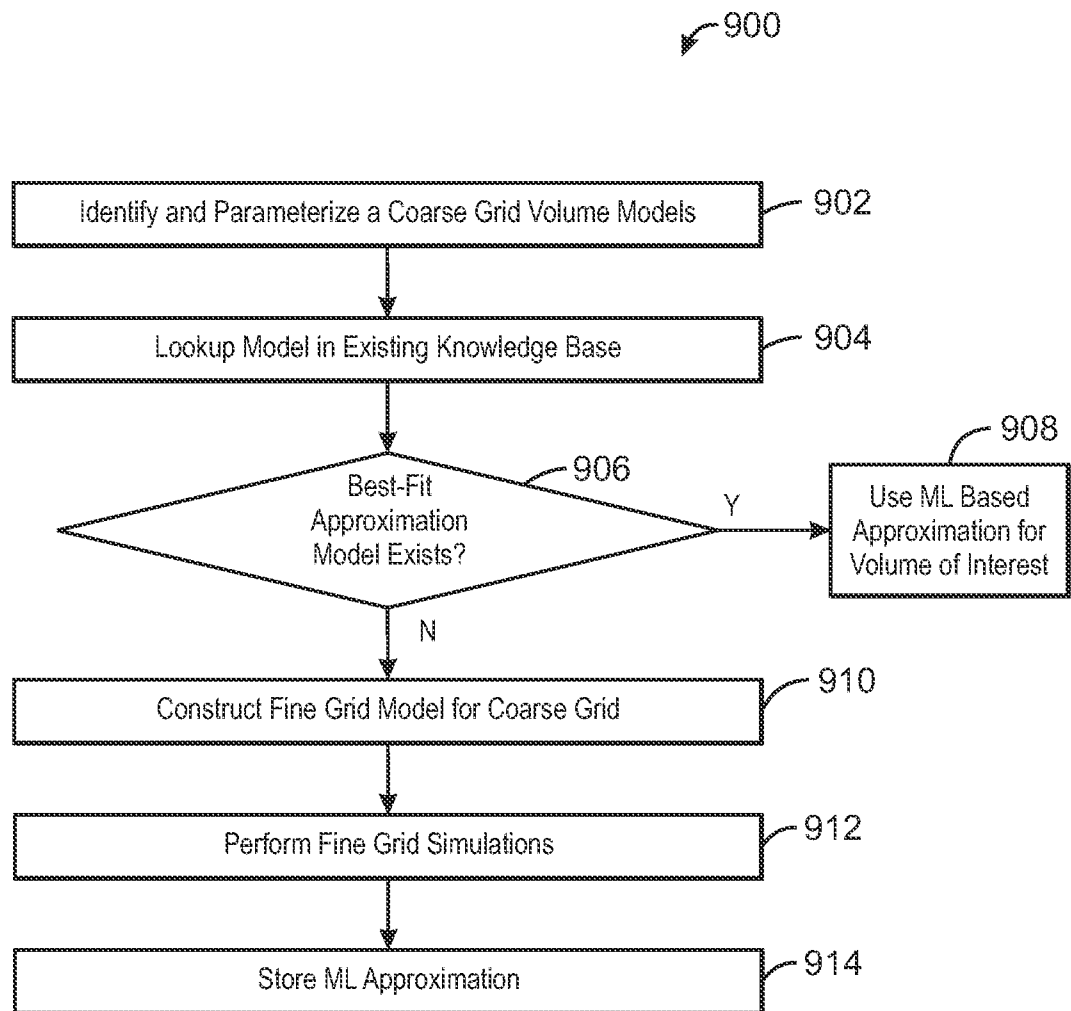


FIG. 9

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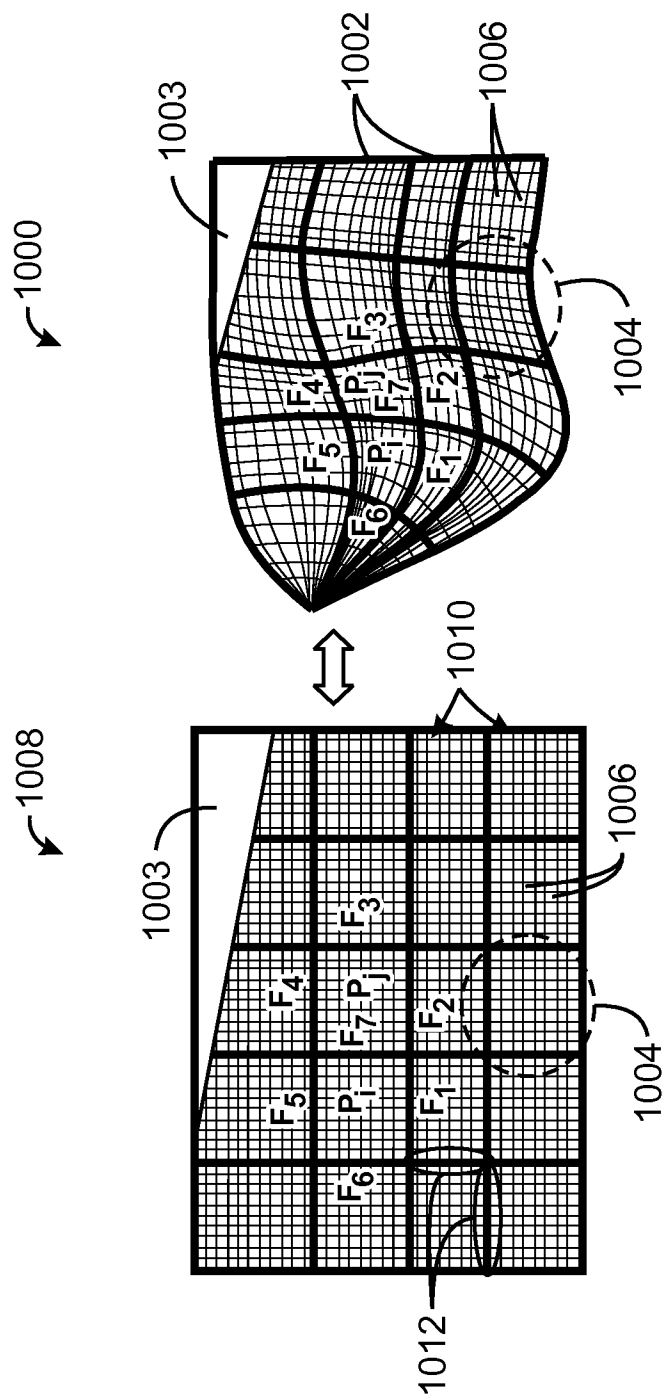


FIG. 10

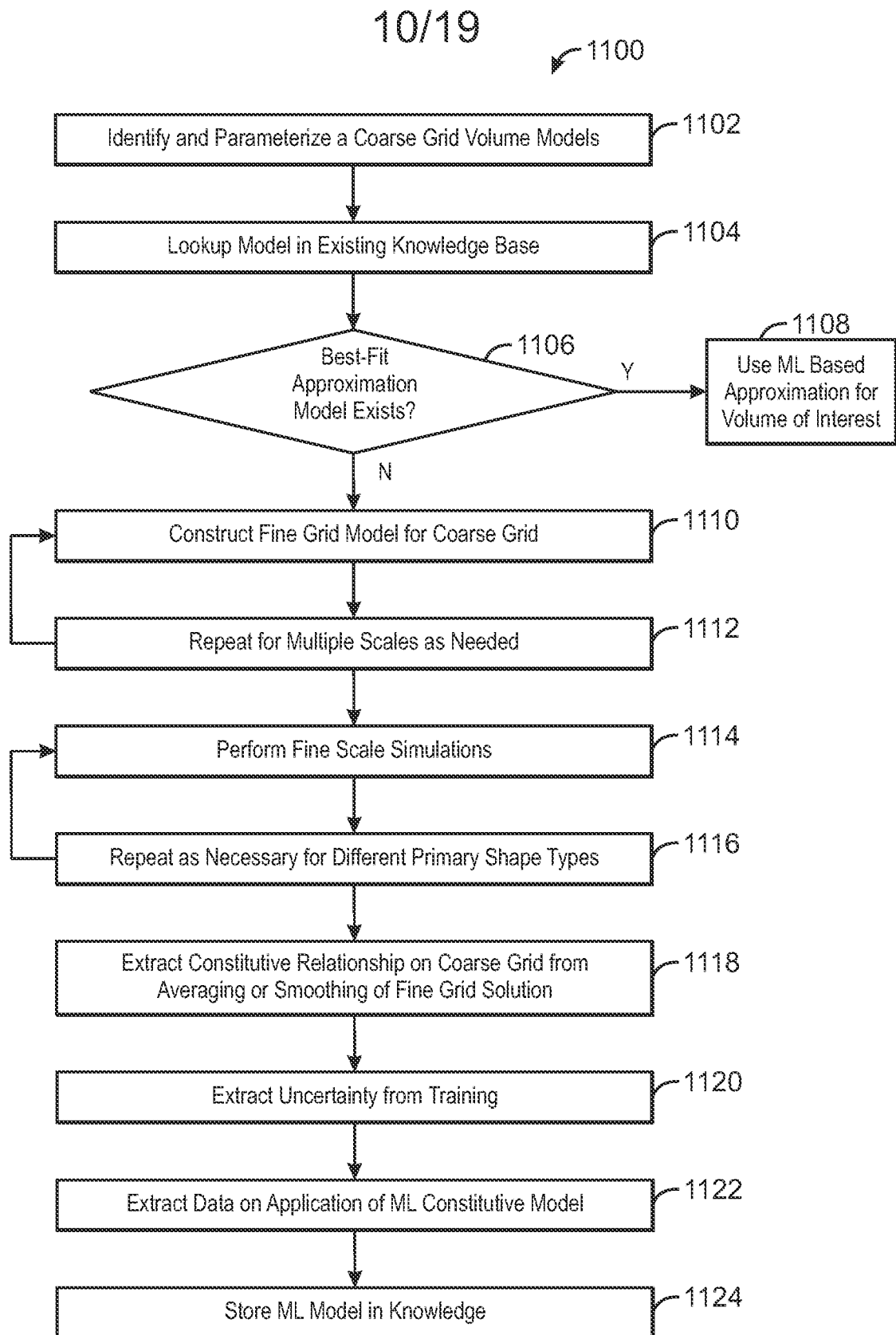


FIG. 11

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1300

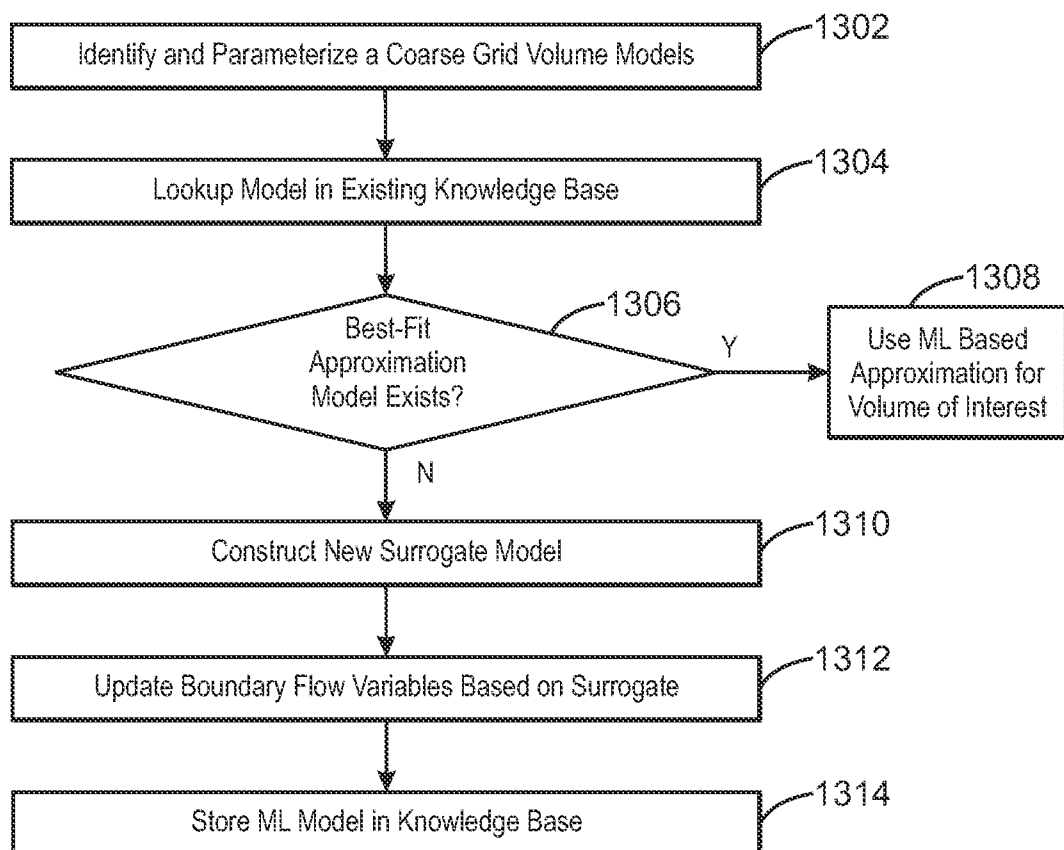


FIG. 13

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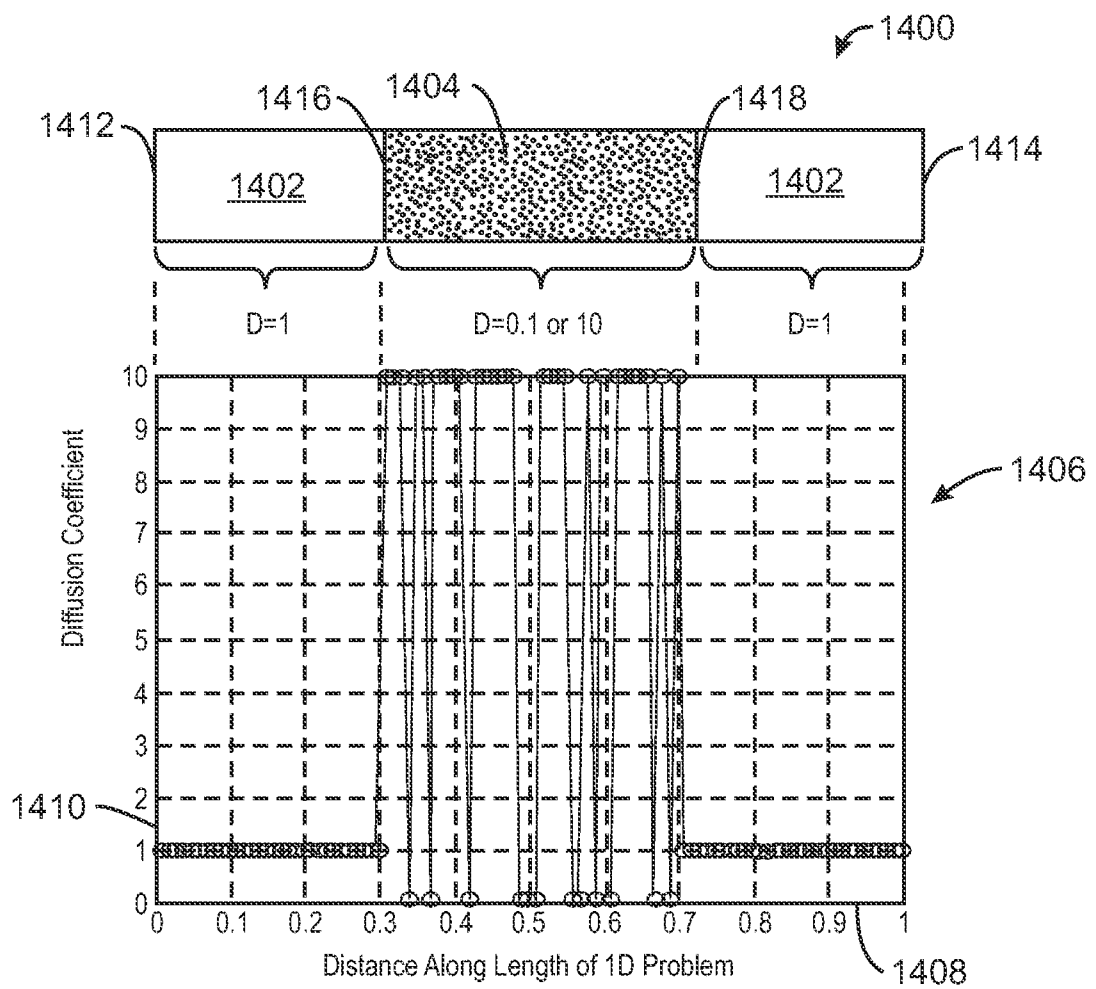


FIG. 14

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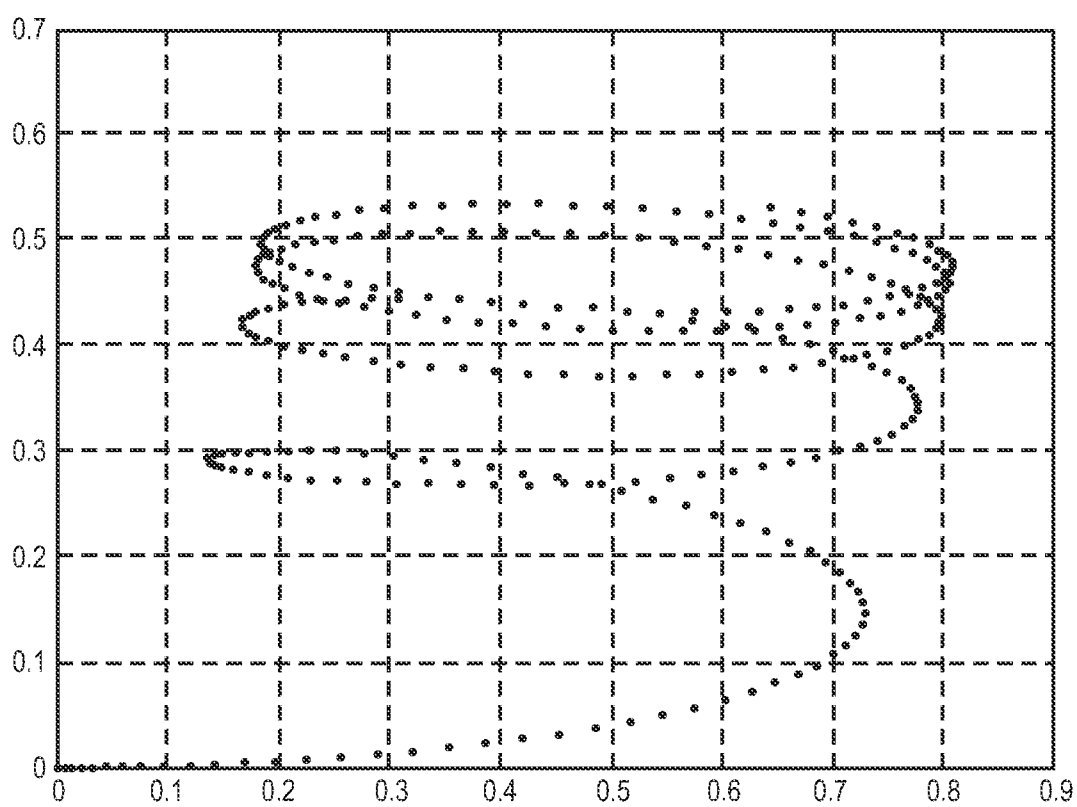


FIG. 15

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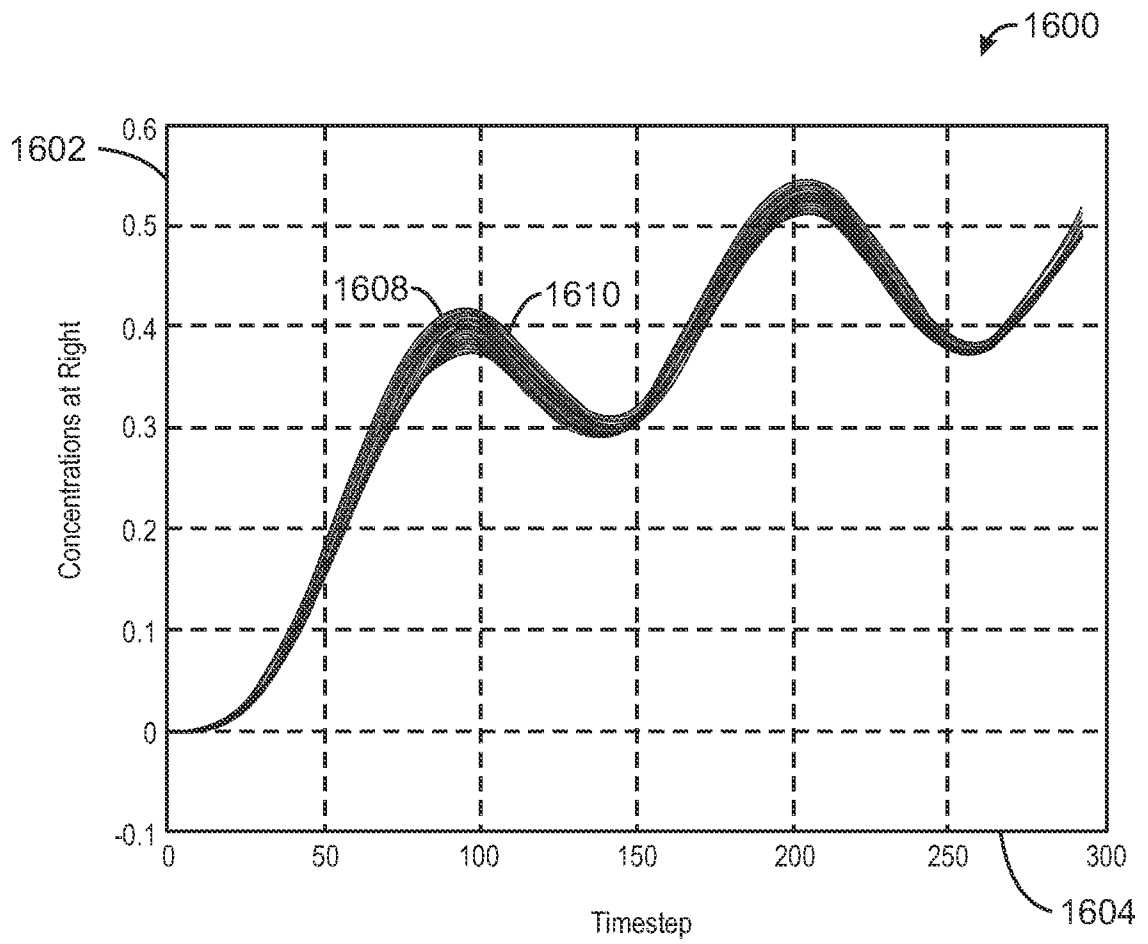


FIG. 16

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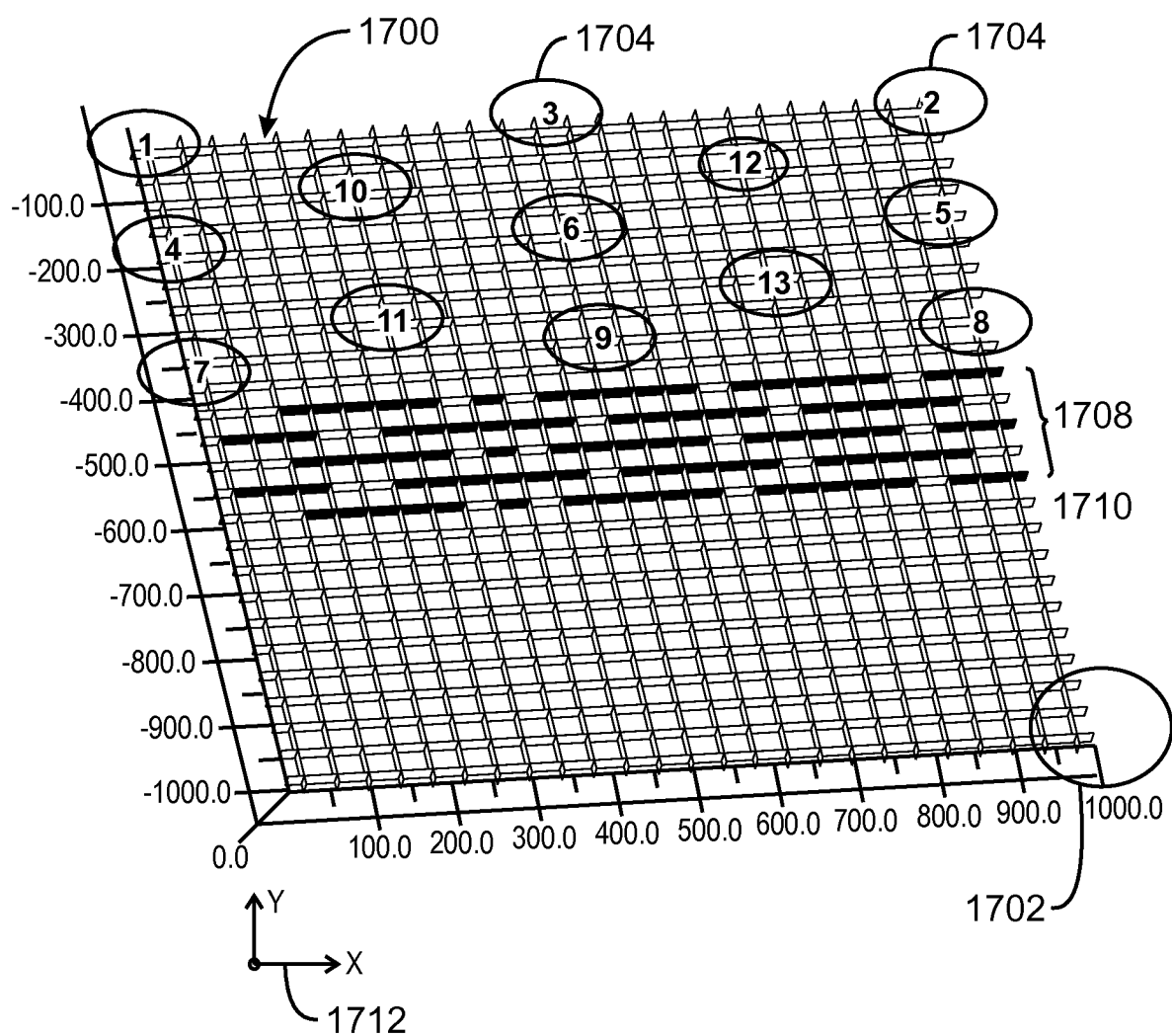


FIG. 17

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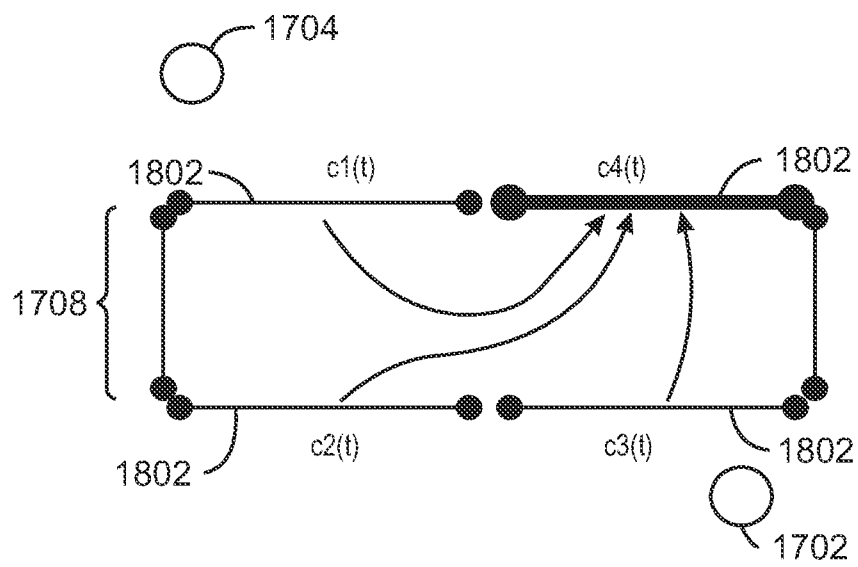


FIG. 18

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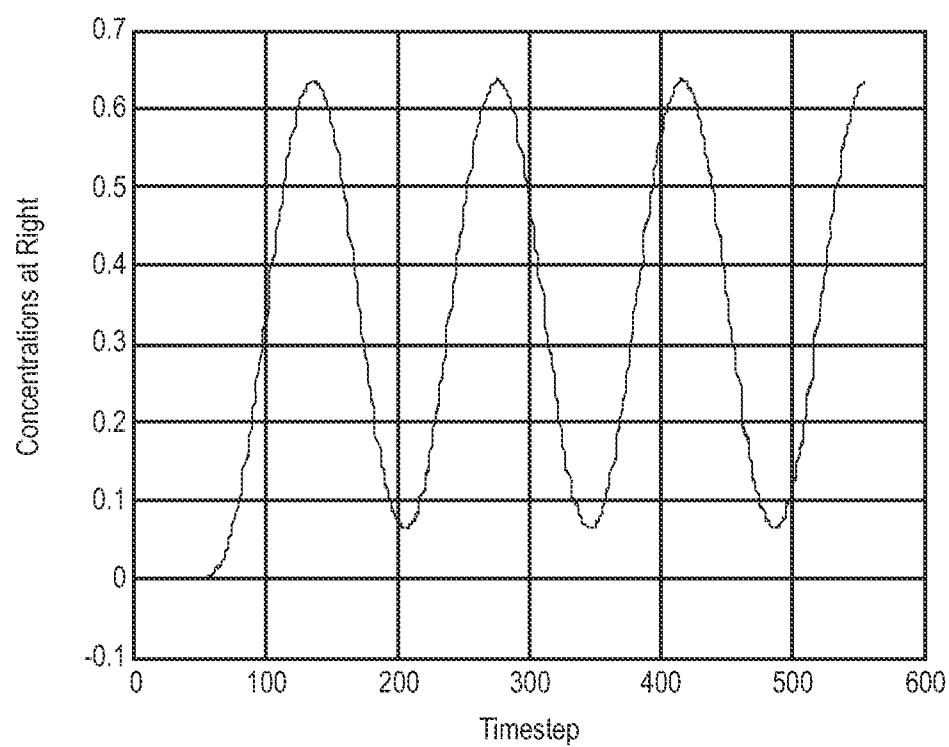


FIG. 19

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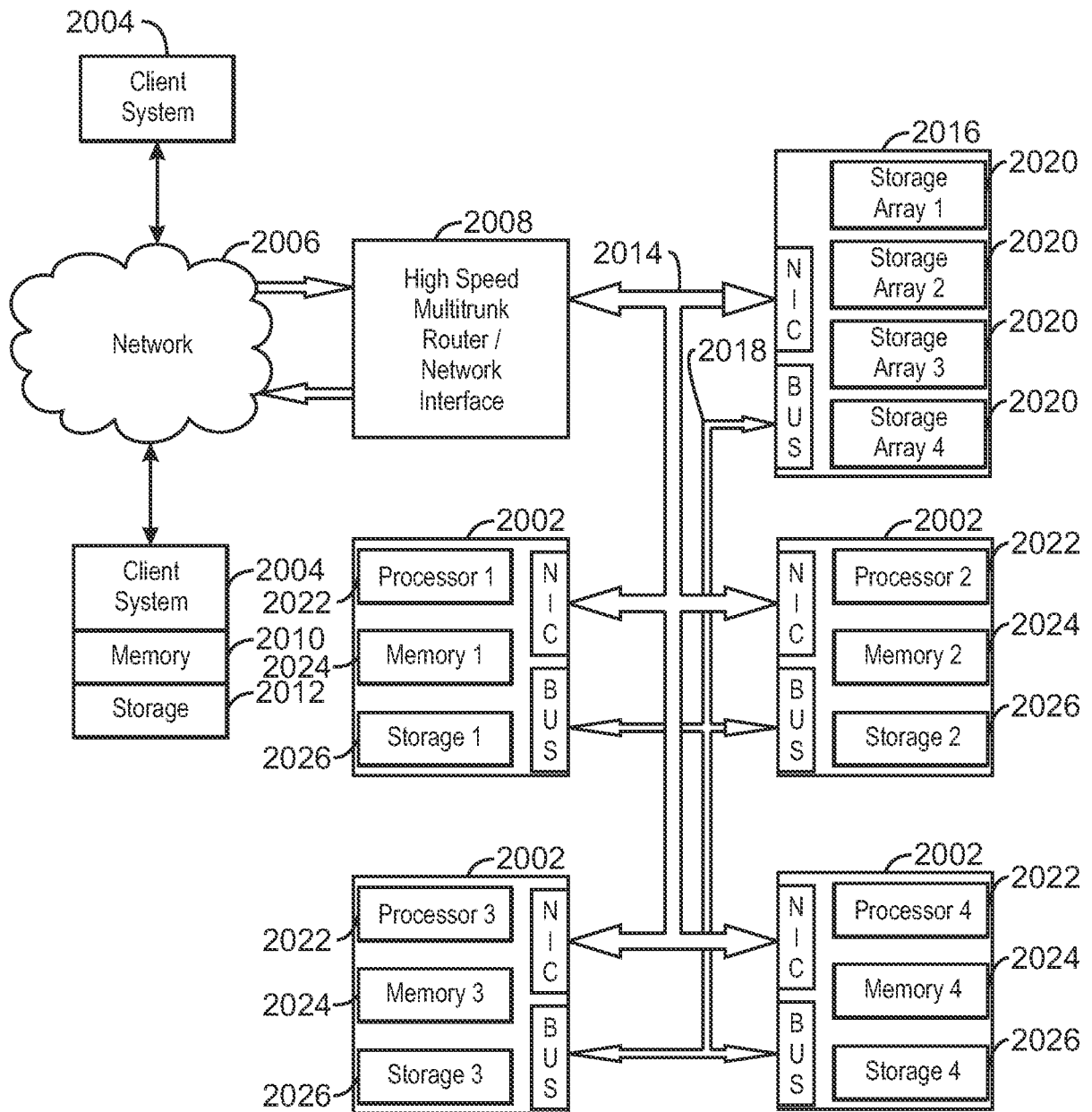


FIG. 20

INTERNATIONAL SEARCH REPORT

International application No.

PCT/US 11/37177

A. CLASSIFICATION OF SUBJECT MATTER

IPC(8) - G06G 7/48 (2011.01)

USPC - 703/10

According to International Patent Classification (IPC) or to both national classification and IPC

B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)

USPC: 703/10

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

USPC: 703/1, 6, 10; 706/12, 15, 16, 44, 920 (keyword limited; terms below)

Electronic data base consulted during the international search (name of data base and, where practicable, search terms used)

PubWEST (USPT, PGPB, EPAB, JPAB); Google Scholar; Google Patents

Keywords: hydrocarbon; reservoir; simulation; neural training; inverse operator; matrix; porosity; permeability; sub-region; mesh

C. DOCUMENTS CONSIDERED TO BE RELEVANT

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
Y	US 2010/0138196 A1 (HUI et al.) 03 June 2010 (03.06.2010) entire document, especially Abstract; para [0008], [0014], [0016], [0017], [0019], [0033], [0035]-[0037], [0039], [0043], [0045]-[0047], [0052]-[0054], [0059], [0062]	1 - 20
Y	US 7,596,480 B2 (FUNG et al.) 29 September 2009 (29.09.2009) entire document, especially Abstract; col. 3, ln 39-62; col. 6, ln 42 to col. 7, ln 5	1 - 20
A	US 2009/0125239 A1 (NIEMEYER et al.) 14 May 2009 (14.05.2009) entire document	1 - 20
A	JANSEN, et al. "Model-Based Control of Multiphase Flow in Subsurface Oil Reservoirs". In Journal of Process Control. Published March, 2008 [online]. [retrieved on 2011.08.25]. Retrieved from the Internet <URL: http://www.citg.tudelft.nl/fileadmin/Faculteit/CiTG/Over_de_faculteit/Afdelingen/Afdeling_Geotechnologie/secties/sectie_Petroleum_Engineering/research/Smart_fields/publications/2008/doc/JansenBosgraAndVanDenHof2008_JPC_Manuscript.pdf > entire document	1 - 20
A	US 2002/0013687 A1 (ORTOLEVA) 31 January 2002 (31.01.2002) entire document	1 - 20
A	SAUNDERS, et al. "Fluid flow monitoring in oil fields using downhole measurements of electrokinetic potential". In Geophysics, vol. 73, no. 5, pages E165-E180. Published September, 2008 [online]. [retrieved on 2011.08.25]. Retrieved from the Internet <URL: http://www3.imperial.ac.uk/pls/portallive/docs/1/55809696.PDF > entire document	1 - 20
	- Please see continuation sheet -	

☒ Further documents are listed in the continuation of Box C.

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"A" document defining the general state of the art which is not considered to be of particular relevance

"E" earlier application or patent but published on or after the international filing date

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"O" document referring to an oral disclosure, use, exhibition or other means

"P" document published prior to the international filing date but later than the priority date claimed

"T" later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention

"X" document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step when the document is taken alone

"Y" document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art

"&" document member of the same patent family

Date of the actual completion of the international search

25 August 2011 (25.08.2011)

Date of mailing of the international search report

06 SEP 2011

Name and mailing address of the ISA/US

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PCT Helpdesk: 571-272-4300

PCT OSP: 571-272-7774

INTERNATIONAL SEARCH REPORT

International application No.

PCT/US 11/37177

C (Continuation). DOCUMENTS CONSIDERED TO BE RELEVANT		
Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
A	GHARBI et al., "An Artificial Neural Network for the Prediction of Immiscible Flood Performance". In Energy & Fuels, vol. 9, no. 5, pages 894-900. Published July 5, 1995 [online]. [retrieved on 2011.08.25]. Retrieved from the Internet <URL: http://chentserver.uwaterloo.ca/aekamel/che720/my_papers/NN_homo.pdf > entire document	1 - 20