No. 652,231.

M. I. PUPIN.

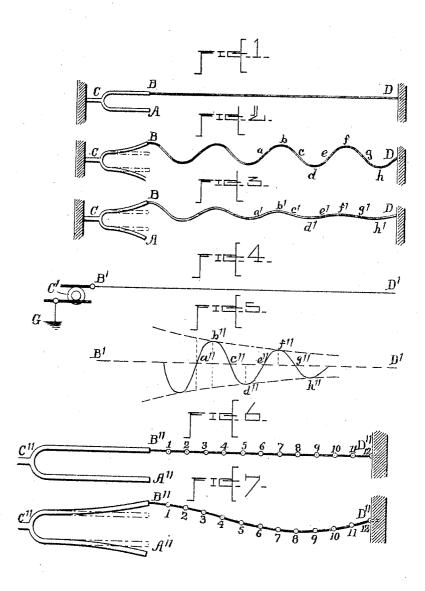
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ART OF REDUCING ATTENUATION OF ELECTRICAL WAVES.

(Application filed May 28, 1900.)

(No Model.)

2 Sheets-Sheet 1.



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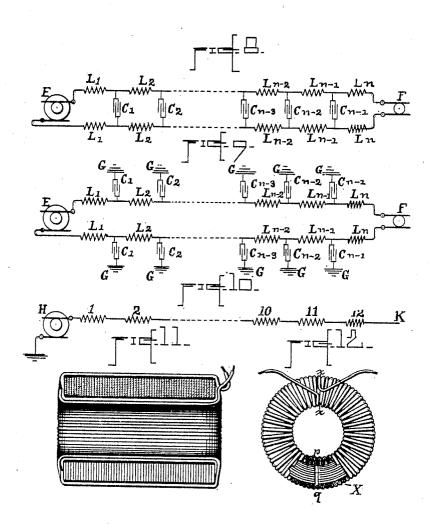
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United States Patent Office.

MICHAEL IDVORSKY PUPIN, OF YONKERS, NEW YORK.

ART OF REDUCING ATTENUATION OF ELECTRICAL WAVES.

SPECIFICATION forming part of Letters Patent No. 652,231, dated June 19, 1900.

Original application filed December 14, 1899, Serial No. 740,238. Divided and this application filed May 28, 1900. Serial No. 18,305. (No model.)

To all whom it may concern.

Be it known that I, MICHAEL IDVORSKY Pupin, a citizen of the United States of America, and a resident of Yonkers, county of Westchester, and State of New York, have invented certain new and useful Improvements in the Art of Reducing Attenuation of Electrical Waves, of which the following is a specification.

My invention consists in an improvement in the construction and installation of conductors for the transmission of electrical energy by means of electrical waves, whereby by decreasing the current necessary to transmit 15 the amount of energy required the attenuation of such waves is reduced, and therefore the efficiency of transmission is increased.

Electrical conductors—say a given length of copper wire—possess ohmic resistance, self-20 inductance, and electrostatic capacity. A variable electrical current in such a conductor is accompanied by three distinct kinds of reactions-viz., the resistance reaction, selfinductance reaction, and the displacement of 25 electrostatic reaction. In overcoming these relations the impressed electromotive force does three kinds of work, which appear, respectively, as, first, heat generated in the conductor and as energy which is stored in 30 the medium surrounding the conductor in the form of, second, magnetic and, third, electrostatic energy. The laws governing these three reactions govern the flow of variable currents in wire conductors. A mathe-35 matical discussion of the laws of flow of variable currents in long wire conductors was first given by Prof. William Thomson, now Lord Kelvin, in 1855. His theory was considerably extended by the late Prof. G. Kirch-40 hoff in 1857. Since that time the subject has been very extensively studied by many investigators, particularly in connection with the modern developments in telegraphy, telephony, and long-distance transmission of 45 power by alternating currents. I have also

been engaged for several years in experimental and mathematical researches of this subject, some of the results of which were given in a paper read before the American 50 Institute of Electrical Engineers on March 22,

1899. This paper, which is entitled "Propa-

gation of Long Electrical Waves," is published in Vol. XV of the transactions of that society, and frequent references will be made to it in

the course of this application.

In the accompanying drawings, which form a part of this specification, Figure 1 is a diagram illustrating a tuning-fork and a string to be vibrated thereby. Fig. 2 is a diagram illustrating the waves set up in this string 60 when it is executing forced vibrations in air under the action of the tuning-fork. Fig. 3 is a diagram illustrating the same apparatus with the string executing forced vibrations in a medium which offers appreciable resist- 65 ance to the vibrations of the string. Fig. 4 is a diagram illustrating an electrical generator of alternating currents and a conductor leading therefrom, the system being grounded at one end only. Fig. 5 is a diagram of 70 an electrical wave propagated along the conductor of Fig. 4 when the generator impresses a simple harmonic electromotive force upon the conductor. Fig. 6 is a diagram of a vibrating system similar to that of Fig. 1, but 75 with a string which is loaded by weights distributed uniformly along its length. Fig. 7 is a diagram illustrating the waves set up in this string when executing forced vibrations under the action of the tuning-fork in a me- 80 dium which offers appreciable resistance to the vibration of the string. Fig. 8 is a diagram illustrating what is here called a "reactance-conductor" of the first type. Fig. 9 is a diagram of a modified reactance-conduc- 85 tor of the first type. Fig. 10 is a diagram of a slow-speed conductor of the second type, called also in this specification a "reactanceconductor." Figs. 11 and 12 are details of apparatus. Fig. 11 is a sectional view of a 90 transformer having an iron core made up of thin plates. Fig. 12 is the end view of the same transformer.

The main results of the theory of the propagation of electrical waves in long wire con- 95 ductors should be stated here briefly for the purpose of placing the claims of this application in their true light. A mechanical analogy will add much to the clearness of this state-

In diagram of Fig. 1, A B C is a tuning-fork which is rigidly fixed at its neck C. To the

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free extremity of prong B is attached a heavy flexible string B D. This string is supposed to be under a certain tension, and one of its terminals is fixed at D. Its position of equi-5 librium is represented by the full line B D. Suppose now that the tuning fork is made to vibrate steadily by an electromagnet or otherwise. The string will vibrate with it, the vibrations of the string being forced vibrato tions—that is, vibrations which follow the period of the tuning-fork. Two principal forms of vibration will be described here briefly. The form of stationary waves is rep-resented in diagram of Fig. 2. This form is 15 obtained when the internal and external frictional resistances are negligibly small. The waves travel with undiminished amplitude. Hence the direct wave coming from the tuning-fork and the reflected wave coming from 20 the fixed point D will have the same amplitude, and therefore by their interference stationary waves will be formed with fixed nodes at a c e g D and ventral segments at b d f h. When, however, internal and ex-25 ternal frictional resistances are not negligibly small, then a progressive attenuated system of waves is formed, which is illustrated in diagram of Fig. 3. The amplitude of the wave is continually diminished in its prog-30 ress from B to D on account of the frictional resistance. After its reflection at D the returning wave, having a smaller amplitude than the oncoming wave, cannot form by interference with it a system of stationary 35 waves. The string therefore does not present to an observer a definite wave form, as in the case of stationary waves. Its appearance is continually changing. If, however, we observe the string by means of a rotating 40 mirror or by properly-timed electrical sparks we shall see the string as represented by curve a' b' c' d' e' f' in Fig. 3. It is a wave curve with continually-diminishing amplitude due to attenuation. Assuming that the 45 frictional-resistance reactions are proportional to the velocity, the attenuation ratio (the ratio of amplitudes of two successive half-waves) will be a constant quantity. velocity of propagation which fixes the wave 50 length for a given frequency and the attenuation ratio are the most characteristic constants of the curve. Both of these depend on the density of the string, its tension, frictional resistance, and frequency. For instance, the 55 greater the tension, other things being equal, the greater will be the velocity of propagation, and hence the longer the wave length for a given frequency. That which is of particular importance is the attenuation ratio 60 and its relation to the density of the string. By substituting strings of greater and greater density we can diminish the attenuation to anything we please in spite of the presence of the frictional resistance, and, vice versa, 65 by making the string lighter and lighter we can increase the attenuation. In other words,

mits wave energy more efficiently than a light This important physical fact has a direct bearing upon the fundamental physical 70 principles on which this application rests. It is therefore important to formulate a clear physical view of it. The energy which the string receives from the tuning-fork and then transmits toward D exists partly as kinetic en- 75 ergy or energy of motion of the string's mass and partly as potential energy or energy of deformation of the string. The process of propagation of a wave consists in the successive transformation of the kinetic part of the total 80 energy into potential energy, and vice versa. During this transformation a part of the energy is lost as heat on account of the frictional reactions. These reactions are supposed to be proportional to the velocity, so 85 that the rate of loss due to these reactions will be proportional to the square of the velocity. Consider now the kinetic energy of an element of the string. It is proportional to the product of mass into the square of its 90 velocity. Making the mass n^2 times as large we shall be able to store up in the element the same amount of kinetic energy with only 1-nth of the velocity; but since the rate of dissipation into heat due to frictional resist- 95 ances is proportional to the square of velocity, it follows that in the second case the element of the string transmits the same amount of energy with only 1-nth part of the loss. In other words, the heat loss is in- 100 versely proportional to the density of the The physical fact that dense strings transmit energy more efficiently than light ones is therefore reduced to the fundamental principle that dense strings require a smaller 105 velocity in order to store up a given amount of kinetic energy, and smaller velocity means a smaller dissipation into heat and therefore a smaller attenuation of the wave. The denser the string the more nearly will its vibration 110 approach the form of stationary waves.

The vibration of the string just considered is a perfect analogy to the propagation of electrical waves along wire conductor B' D', Fig. 4, one end, B', of which is connected to 115 generator C' of simple harmonic electromotive force, the other pole of the generator being grounded at C. The existence of this analogy is due to the physical fact that the three reactions which accompany the vibra- 120 tion of a string-viz., the acceleration reaction, the tensional reaction, and the frictional reaction-follow the same laws as the three reactions which accompany the flow of a variable current in a long wire conductor-viz., 125 the ohmic-resistance reaction, inductance reaction, and the capacity reaction—that is to say, the ohmic resistance, the inductance, and the reciprocal of the capacity of the conductor, all per unit length, correspond, re- 130 spectively, to the coefficient of friction, the density, and the tension of the string.

in a resisting medium a dense string trans- In Fig. 5 the line B' D' represents the wire conductor B' D' of-Fig. 4. The ordinates of

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the curve $a^{\prime\prime}$ $b^{\prime\prime}$ $c^{\prime\prime}$ $d^{\prime\prime}$ $e^{\prime\prime}$ $f^{\prime\prime}$ represent the instantaneous values of the current at the various points of the conductor. This current curve is of the same form as the curve of the 5 string illustrated in Fig. 3. The magnetic energy of the current corresponds to the kinetic energy of the vibrating string, and just as a dense string transmits mechanical energy more efficiently than does a light string 10 so a wire of large inductance per unit length will, under otherwise the same conditions, transmit energy in the form of electrical waves more efficiently than a wire with small inductance per unit length, for a wire of large in-15 ductance can store up a given quantity of magnetic energy with a smaller current than is necessary with a wire of small inductance. When the process of storing up magnetic energy is accompanied by small currents, the heat losses will be smaller than when this process is accompanied by large currents, and smaller heat losses mean smaller attenuation, and therefore a higher efficiency. A few numerical examples about to be discussed 25 will illustrate this accurately and fully. Before discussing the examples I shall give two definitions. On page 122 of the paper on "Propagation of Long Electrical Waves" mathematical expressions are given for the 30 most important constants, to which the names of "wave-length constant" and "attenuation constant" are assigned in this application. The mathematical expressions for these constants, which are represented by symbols 35 α and β , respectively, are as follows:

$$\alpha = \sqrt{\frac{1}{2} p \operatorname{C} \{ \sqrt{p^2 \operatorname{L}^2 + \operatorname{R}^2 + p \operatorname{L} \}}},$$

$$\beta = \sqrt{\frac{1}{2} p \operatorname{C} \{ \sqrt{p^2 \operatorname{L}^2 + \operatorname{R}^2 - p \operatorname{L} \}}},$$

40 where

L = inductance of the wire per mile.

C = capacity of the wire per mile.

R = ohmic resistance of the wire per mile.

$$p = \frac{2\pi}{T}.$$

T = period of the impressed electromotive

The physical significance of these two constants can be stated in a simple manner. Let

 λ = wave length.

55

$$\lambda = \frac{2 \pi}{\alpha}.$$

Hence the name "wave-length constant," which is applied to it in this specification. 60 Again, let a wave of amplitude U start from point B', Fig. 4. By the time it reaches a point at a distance s from B'' its amplitude will be $Ue^{-\beta s}$, where e is the base of Naperian logarithms. The constant β measures the 65 attenuation—hence the name "attenuation

this specification the "attenuation factor," because it is the factor by which the initial amplitude has to be multiplied to get the am- 70 plitude at a point at a distance s from the source. I shall consider now two distinct numerical examples for the purpose of showing how these constants influence the transmission of electrical energy over long wire con- 75

Underground cables for telephonic communication in New York city are now constructed which have the following values per

$$L = 0$$
, (very nearly.)
 $C = 5 \times 10^{-8}$ farads.

R = 20 ohms.

The formula for α and β reduces this case to ⁸⁵

$$\alpha = \sqrt{\frac{1}{2} p C R}.$$

$$\beta = \sqrt{\frac{1}{2} p C R}.$$

$$p = 2 \pi \times 3,000 = 1,900$$
, (roughly.)

90

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I select the frequency of three thousand p. p. s., because this is according to all authorities far beyond the highest frequency which occurs in the telephonic transmission of speech. I shall show that even for this high frequency the attenuation can be much reduced by adding inductance to the cable. We get for this frequency

$$\alpha = .0974.$$
 $\beta = .0974.$

The wave length $\lambda = \frac{2 \pi}{\alpha} = 64$ miles in round 105

The attenuation over a distance of two hundred and fifty miles (approximately equal to the distance between New York and Boston) is obtained as follows: Let U be the initial 110 amplitude or amplitude of current in New York. Then the current in Boston will be

$$U e^{-250\beta} = U e^{-24}$$
.

This means that practically no current what-ever reaches Boston. The ohmic resistance wipes out completely the wave energy, even before the wave has progressed half-way between New York and Boston. Even if it were possible to substitute a heavier wire, so as to 120 make R equal five ohms, we should have current in Boston equal current in New York multiplied by e^{-12} , it being assumed that the capacity is not increased. Under such conditions telephonic communication between New 125 York and Boston would be impossible even over this heavy wire cable. The same is true even if we assume that the highest important frequency in telephony is much less than three thousand p. p. s. Let us see now how the 130 twenty-ohms-per-mile cable will act, if we suppose that by some means its inductance per constant" which is assigned to it in this application. The expression $e^{-\beta s}$ is called in would be about ten times the inductance per

mile of the long-distance telephone-wire between New York and Chicago. The wave length and the attenuation constant of such a cable would be approximately

> $\lambda = 6.66$ miles, $\beta = .01$ miles,

and current in Boston equal current in New York multiplied by $e^{-2.5}$. Under these con-10 ditions telephonic communication over such a cable would be practicable even over a distance of one thousand miles. These numerical examples show clearly the enormous beneficial effects of inductance. Section I of my 15 paper cited above gives a résumé of the existing mathematical theory bearing upon this subject and calls particular attention to the importance of inductance in long conductors. I was the first to verify this theory by ex-20 periments, and these experiments are described in the first part of Section III of the paper cited above. These experiments were not only the first experiments on record on long electrical waves, but they also form a 25 part of the experimental investigations by means of which the invention disclosed in this application was first reduced to practice by me. The theories so far discussed recommend strongly the employment of line conductors 30 of high inductance for long-distance transmission of power by electrical waves, but they do not tell us the way of constructing lines which will have this very desirable property. The additional theory necessary for any ad-35 vance in this direction was first worked out by me. Part of my investigations in this direction was published in Sections II and III of the paper cited above. Figs. 8 and 9 of the drawings which accompany this specifi-40 cation are copies of Figs. 4 and 5 of that paper. Referring now to Fig. 8, E is an alternator, and F is a receiving apparatus—say a telephone-receiver. L_1 L_2 to L_n are small coils without iron wound on wooden spools, 45 each coil having an inductance of approximately .0125 henry and a resistance of 2.5 ohms. These coils are connected in series, forming a continuous line which connects the alternator E to the receiving instrument F. 50 In the actual apparatus, part of which is shown in Fig. 11 of said paper, there were four hundred coils. C₁ C₂ to C_{n-1} are small condensers connecting opposite points of the line. Perferring parts for the same condensers. the line. Referring now to Fig. 9, the condensers C_1 to C_{n-1} are shown as connecting the points between the consecutive coils to the ground G. The capacity of each condenser was approximately .025 microfarad. The mathematical theory of the flow of an 60 alternating current in such a conductor, which I have called a "reactance conductor," is given in Section II of the paper cited above. It is, so far as I know, entirely new. Its principal object was to find an answer to the 65 question in how far such a conductor resembles an ordinary telephone-line with uniformly-distributed inductance, capacity,

and resistance. The answer which this theory gives is perfectly definite. The answer given in the paper is that up to a frequency 70 of one thousand p. p. s. such a line represents very nearly an ordinary telephone-line having per mile an inductance of .005 henry, a resistance of one ohm, and a capacity of .01 microfarad; but even for a frequency of 75 three thousand five hundred p. p. s. a slowspeed conductor represents, if not very nearly, still quite approximately, an ordinary line with uniformly-distributed inductance, resistance, and capacity, the approximation being quite within the limits of my errors of observation, (between one and two per cent.,) and this is true with a much higher degree of accuracy for lower frequencies, therefore quite accurately for all frequencies which are 85 of any importance in the telephonic transmission of speech. A high-potential or highinductance line has not only the advantage of small attenuation, but also another advantage of the greatest importance in telephony, 90 and that is very small distortion in the sense that all frequencies which are present in the human voice are attenuated in very nearly the same degree. It is therefore a distortionless line. I have evolved the following general rule: If n be the number of coils per wave length, then for that wave length the slow-speed conductor will represent an ordinary telephone-line with the accuracy of the formula

Sin. $\frac{\pi}{n} = \frac{\pi}{n}$..

Thus, for instance, when n=16

$$\frac{\pi}{16} = .196.$$

100

Sin.
$$\frac{\pi}{16} = .196 - .00122 + .$$

Hence sin. $\frac{\pi}{16}$ differs from $\frac{\pi}{16}$ by about two-

thirds of one per cent. of the value of $\frac{\pi}{16}$. This

rule was found by me theoretically and verified experimentally by experiments described in Section III of paper cited above. A conductor constructed in the manner just described was called by me a "slow-speed conductor," because the velocity of propagation along such a conductor is smaller than along 120 ordinary lines. Another technical term should be explained now. Much convenience of expression is derived from an introduction of what I call the "angular distance" between two points on a line conduc-tor. Thus we can say that two points at a linear distance of a wave length have an angular distance of 2π . With this understanding it follows that two points at a linear distance of $\frac{\lambda}{n}$, where λ equals wave length, will 130

have an angular distance of $\frac{2 \pi}{n}$. The rule given above can now be stated as follows: A 652,231

ã

slow-speed conductor resembles an ordinary line conductor with a degree of approximation measured by the ratio of the sine of half the angular distance covered by a coil to half 5 the angular distance itself. It is now an easy matter to pass on to a second type or slowspeed conductor which is better adapted to commercial use for the purpose of diminishing the attenuation of electrical waves. 10 second type of slow-speed conductor is called here a "reactance-conductor." Referring to Fig. 10, H is the transmitting and K the receiving end of a long electrical conductor 1, 2, to 10, 11, 12 K. At points 1, 2, to 10, 11, 15 12 introduce equal coils in series with the line and let the distance between any two This equality successive coils be the same. of coils and distances is not absolutely necessary, but preferable. We have now an-20 other type of slow-speed conductor. slow-speed conductor, which I shall refer to as the "second type" or simply reactanceconductor, differs from those of the first type described in that it has in place of the lumped 25 capacity distributed capacity only, and also it has in addition to the lumped inductance and lumped resistance evenly-distributed inductance and resistance. This slow-speed conductor of the second type is evidently 30 much less of a departure from an ordinary line conductor than the slow-speed conductor of the first type. It is therefore a reasonable inference that the slow-speed conductor of the second type will operate like an ordinary 35 line under the same conditions under which the slow-speed conductor of the first type so operates, and that is when the value of half the angular distance between two consecutive coils is approximately equal to its sine. This 40 rule is the foundation upon which the invention described in this application rests. careful research of this matter was made by me and the truth of the rule just given as applied to slow-speed conductors of the sec-45 and type has been completely verified. The results of this research, which will be published in the near future, will be explained in language devoid of mathematical symbols. the object being to explain in as simple a man-50 ner as is possible the action of a reactanceconductor. I shall employ again the analogy of a vibrating string. In Fig. 6, A" B" C" is a tuning-fork rigidly fixed at its neck C'. The full line B" D" represents a heavy flexi-55 ble inextensible string which is under tension and fixed at D". The circles, equally distributed over the string B" D", represent equal masses attached to the string. Let now the tuning-fork vibrate with a suitable 60 period, so as to develop in the beaded string a vibration the wave length of which is equal to or greater than the distance B" D", somewhat as shown in Fig. 7. The vibration of the beaded string (represented in Fig. 7) will 65 then to within an accuracy of a fraction of one per cent. be the same as that of a uniform

resistance, and mass which the beaded string has. The mechanical vibration in such a string is a perfect analogy to the electrical 70 vibration in an electrical conductor represented in Fig. 10. In this diagram the alternator H is supposed to develop approximately a simple harmonic electromotive force. One pole of the alternator is grounded at G and the 75 other pole is connected to a wire conductor. At equal distances 1 2 to 10 11 12 are inserted in series with the line twelve equal coils. Suppose now that the electromotive force impressed by the alternator develops in the con- 80 ductor an electrical vibration three-fourths the wave length of which covers the distance or a greater distance. Then the law of flow of the current in this conductor will be the same as the law of distribution of velocity in the 85 beaded string of Figs. 6 and 7. This mechanical analogy, besides being instructive, offers also an inexpensive method of studying the flow of current in long wire conductors. A few experiments with beaded strings 90 excited by tuning-forks will convince one soon of the soundness of the physical basis on which rests the invention described in this application. A reactance-conductor is a long electrical wire conductor having pref- 95 erably reactance sources in series at preferably equal intervals. Such a conductor, just like the reactance-conductor of the first type, is equivalent to a uniform wire conductor of the same inductance, capacity, and resist- 100 ance per unit length when the angular distance between two successive coils is such that one-half of this distance is approximately equal to its sine. Such a conductor will therefore possess low attenuation and 105 inappreciable distortion if its reactance per unit length is large in comparison with its resistance. This condition can be readily fulfilled in conductors of this kind. the interpolated reactance sources consist of 110 simple coils, they should be made preferably without iron cores, so as to avoid as much as possible hysteresis and Foucault - current losses and current distortion. This can be done in nearly every case without making 115 the coils too bulky or too high in ohmic resistance. If for any special reasons coils of small dimensions per unit inductance are required, then iron or preferably the finestthat is, springiest—quality of steel should be 120 employed and the magnetization kept down as much as possible. For telephony the angular distance between any two successive coils should sufficiently satisfy the rule given above for the highest frequency, which is of 125 importance in the telephonic transmission of speech. I shall now show how the rules explained

so far in this specification can be applied in practice by working out two particular cases, 130 giving all the instructions which I believe are necessary to those skilled in the art.

one per cent. be the same as that of a uniform | (a) Suppose that it is required to transmit string of the same length, tension, frictional | speech telephonically over a distance of three

thousand miles of wire stretched upon poles. The total attenuation factor over that distance should be about the same as that over the best New York-Chicago circuits of the 5 American Bell Telephone Company, which is (leakage not included) about e^{-15} for the highest frequency of importance in speech namely, about fifteen hundred p. p. s. It is proposed to state first the conditions which 10 will give an attenuation factor of $e^{-1.5}$ with a length of three thousand miles. Let

> β = the attenuation constant. l = distance = 3,000 miles.

15 $e^{-3,000\beta}$ = the attenuation factor = $e^{-1.5}$.

Then

30

 $3,000 \beta = 1.5.$

20 Assume that a copper wire of four ohms per mile resistance is used and that the additional resistance introduced by the inductance-coils is .6 ohms per mile. The total resistance per mile will then be 4.6 ohms. When the re25 actance per mile is sufficiently great in comparison to the resistance, we have the following simplified formula for the attenuation constant:

$$\beta = \frac{\mathrm{R}}{2} \sqrt{\frac{\mathrm{C}}{\mathrm{L}}}.$$

Observe that β is independent of the frequency and that therefore the reactance-conductor is distortionless. The capacity C for 35 a wire of 4 ohms per mile is .01 microfarads, the wire being hung as the long-distance airlines of the American Bell Telephone Company are hung. The inductance of the wire can be neglected, and I shall consider L as 40 due solely to the inductance of the inductance-coils. The value of the inductance which will satisfy the assumed conditions can be calculated from the formula just given, as

3,000
$$\beta$$
 = 3,000 $\frac{4.6}{2} \frac{1}{10^3} \sqrt{\frac{.01}{L}} = 1.5$.

$$L = .2$$
 henry.

50 Having calculated the inductance per mile, the next step is to calculate the wave length for the highest frequency to be considered—namely, fifteen hundred p. p. s.

55
$$\lambda = \frac{2 \pi}{\alpha} = \frac{2 \pi}{p \sqrt{\text{L C}}} = \frac{10^3}{1,500 \sqrt{.2 \times .01}} =$$

15 miles, approximately.

A sufficiently-high degree of approximation to a uniform telephone-line will be obtained 60 if we use fifteen coils per wave length of the highest frequency. This is one coil per mile. The inductance of each coil will be L equals .2 henry. Its resistance should be six-tenths of an ohm. To wind such a coil, using no 65 iron, take about sixteen hundred feet of wire of two ohms per mile and wind it into a coil of five inches internal diameter and twelve

inches in length. The line just described has a comparatively-high inductance. It is therefore a high-potential line. Transmitter-coils 70 of a larger transformation ratio than those employed at present will be found more suitable for working over lines of high reactance.

To take another case, suppose it be required to transmit speech telephonically over a submarine cable two thousand miles long. In this case inductance-coils of small volume are preferable on account of considerations of mechanical construction. To secure high inductance with small volume, steel or iron 8c cores should be used to avoid excessive ohmic resistance. Coils having iron cores are a source of three kinds of losses—viz., those due to Faucault currents, hysteresis, and ohmic resistance. Each one of these losses has 85 to be very small if the coil is to be efficient. I have found that this can be accomplished at any rate when it is required to transmit only small quantities of energy. If the core is finely subdivided, Foucault currents are 90 negligible, especially for exceptionally-weak magnetizations, such as will be employed in the case before us. It will now be shown that hysteresis also can be made negligibly small. Let the wire have a resistance of five 95 ohms per mile. According to present cable construction the capacity per mile with wires of such size is very nearly three-tenths microfarad. Introduce inductance-coils at proper distances, so as to make the inductance threetenths henry per mile, and suppose that these coils add one ohm per mile, thus increasing the ohmic resistance to six ohms per mile. The wave length for a frequency of fifteen hundred p. p. s. will be

> $\lambda = 2$ miles, approximately. $2,000 \ \beta = 6.$ $e^{-2,000\beta} = e^{-6}$.

Hence

105

011

To secure a close approximation to the rule above given, it will be necessary to introduce sixteen coils per wave length or eight coils The inductance of each coil will 115 per mile. then be .0375 henry. The resistance of each coil will be .0125 ohms. Employing cores of iron or well-annealed steel, coils of this inductance can be readily made which will be small enough to go within the sheathing of a 120 submarine cable as these are constructed today and at the same time show negligiblysmall Foucault-current and hysteresis losses.

In Fig. 11 X' is a ring-shaped disk. Its internal diameter is 2.5 centimeters and its ex- 125 ternal diameter is 6.5 centimeters. Its thickness is .002 centimeters, or about .005 inches. It has a narrow slit p. q. A core is built up by piling together a sufficient number of such disks to give the required length, which 13c we will assume is ten centimeters. In Fig. 11 a transverse section of such a core is represented. Wind this core with two layers of wire having 8.5 ohms resistance per mile.

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Let each layer have forty-eight turns. The length of the wire will be eighty feet, and its ohmic resistance will therefore be a little more than .125 ohms. Eight coils per mile 5 will therefore add one ohm per mile to the resistance, making the total resistance six ohms per mile. To calculate the inductance, the permeability of the iron must be known. In telephony the maximum value of the current at the sending-station is generally less than .0001 amperes, or .00001 units of current in the centimeter gram second system. The magnetomotive force of the magnetic circuit is for this value of the magnetizing-current:

$$M = 4 \pi s C = 4 \pi \times 96 \times 10^{-5}$$
.

The intensity II of the magnetizing force will be

$$\frac{\mathbf{M}}{l} = \mathbf{H},$$

where l is the mean length of the magnetic circuit equal to ten centimeters—roughly. Hence

$$H = \frac{4 \pi \times 96}{10^6} = .0012.$$

For excessively-feeble magnetizing forces of this kind the magnetic permeability μ of first-class iron is about 180. (See Ewing on Mag-30 netic Induction in Iron and other Metals, p. 119, especially Sec. 87.) The intensity of magnetic induction will be $B=180\times.0012=.22$ lines of induction persquare centimeter. At this excessively-low induction there is no hysteresis (see Ewing, cited above, Sec. 89, especially top of page 128, and Sec. 180.) The inductance of the coil can now be easily calculated. The formula is

$$L = \frac{4 \pi s^2 q \mu}{l \times 10^9},$$

where

40

15

25

s = number of turns = 96.

 $q = \text{cross-section of core in cm.} \square = 20.$

 $\mu = \text{permeability} = 180.$

Hence

$$L = .042$$
 henry.

50 The diameter of the coil when finished will be less than 2.5 inches and its length 4.25 inches. Such a coil can be placed conveniently within the sheathing of a submarine cable. Its diameter can very easily be restuded by increasing its length.

It should be observed here as a warning that unless inductance-coils with iron cores are constructed in such a way as to keep downthe magnetization, hysteresis, Foucault-60 current losses, and distortion of current by the varying value of the magnetic permeability at each cycle of magnetization will work disastrously. The limit of magnetization permissible will not, however, be passed-65 even if the magnetizing-current is thirty times as large as is assumed above—that is,

three milliamperes—(See Ewing, Sec. 87,) a strength of current which is capable of operating telegraphic apparatus. It should also 70 be observed that the iron core represented in Figs. 11 and 12 can be made by winding very fine iron wire, the plane of the windings being perpendicular to the axis of the cylindrical tube which constitutes the core. The 75 advantage of this core is that it still further reduces the Foucault-current losses and also prevents magnetic creeping. (See Ewing, end of Sec. 89.) The cross-section of the wire core would have to be made larger than 80 that of the plate-core to allow for the more imperfect filling up of the available space by the substance of the wire.

The invention has been explained with reference to telegraphy and telephony; but it is 85 also applicable to the transmission of power

by alternating currents.

It is to be understood that only the simplest and most direct manner of increasing the reactance of the line has been shown—viz., by 90 introducing simple coils. There are, however, various other ways known in the art of producing the same effect. For instance, we may have each reactance-coil provided with a secondary winding and place a condenser in 95 circuit with this secondary. By properly adjusting the capacity of the condenser the effective inductance and the effective resistance of the reactance-coil can be increased or diminished within somewhat wide limits; but 100 the simplicity and uniformity attainable with the simple coils makes it, in my opinion, the best method. In all of these arrangements the reactance of the line per unit length is increased by introducing reactance at various 105 points along the line, referred to in the claim as reactance sources. The particular means of increasing the reactance is not important, the fundamental idea of the invention being to transmit energy with small current by ad- 110 justing the reactance of the line, thereby diminishing heat losses and resulting attenuation. The equivalence between a reactanceconductor of the second type and its corresponding uniform conductor holds true with 115 respect to free vibrations also. It holds true also for periodic unidirectional impulses, because, since each unidirectional electrical impulse employed in ordinary telegraphy and cabling can be represented by a convergent 120 series of simple harmonic impulses which are harmonically related to each other, it follows that a reactance-conductor will act, like its corresponding uniform conductor for ordinary methods of telegraphy, by unidirectional 125 electrical impulses if the reactance-conductor satisfies the rule given above for a frequency the period of which is sufficiently small in comparison to the time of duration of the unidirectional impulse. Their ratio should 130 equal twenty-five or more.

even if the magnetizing-current is thirty times as large as is assumed above—that is, the magnetizing-current can be as high as

a given frequency and all frequencies smaller than this given frequency and have specified that sixteen coils per wave length corresponding to that given frequency should be used; but such a close resemblance between the two is in many cases not required, so that a considerably-smaller number than sixteen coils per wave length may be employed. all cases, however, the construction and the 10 distribution of the reactance-coils will be governed by the character of the variable electromotive force which is to be impressed upon the line and the form of the resultant current-wave and by the amount of attenuation 15 with which it is proposed to work in a way which can be easily deduced from the rule

given above. It will be seen from the foregoing description that the method of diminishing the at-20 tenuation of electrical waves transmitted over a conductor consists in distributing along the conductor reactance sources of sufficient strength and making the reactance sources sufficient in number relatively to the . 25 wave length to secure the attenuation constant and the degree of approximation of the resulting non-uniform conductor (consisting of the uniform conductor and the distributed reactance sources) to a uniform conductor, as 30 the requirements of the particular problem necessitate. The conductor will then act with respect to the electrical waves within the proper limits of periodicity-that is, for the shortest waves to be considered and all 35 longer waves as a uniform conductor having the same resistance, inductance, and capacity per unit length. It will of course be noted that the character of the waves to be transmitted as defined by the periodicities con-40 tained in it is the controlling factor determining the distribution of the inductance

It will be seen from the foregoing statement that this invention applies to "electrical wave transmission" and involves the construction of a "wave-conductor." If the length of the conductor relatively to the wave length of the current transmitted is sufficiently great to permit the development of 50 the wave phenomenon, then there is wave transmission; but if the conductor is too short for this there is mere ordinary direct trans-The distinction is that if there is no perceptible development of waves there is 55 no perceptible attenuation, and therefore the invention does not apply. The term "waveconductor" is intended to indicate a conductor which forms a part of a system of conductors over which electrical energy is transmit-60 ted by electrical wave transmission. The use of these terms in the claim is intended to bring out the distinction here stated. It will be noted that I have herein described

a method of modifying a conductor of uniformly-distributed capacity, resistance, and 65 reactance in such manner as to diminish its attenuation constant by increasing its effective inductance without affecting seriously its character as a uniform conductor with respect to the waves to be transmitted. This I 70 accomplish by distributing along the uniform conductor reactance sources at periodically-recurring points, the distance between the points being determined by the considerations heretofore presented. There results from this 75 method a non-uniform wave-conductor consisting of a uniform wave-conductor having reactance sources distributed at periodicallyrecurring points along its length in such manner that the resulting wave-conductor is 80 equivalent, within proper limits, to the corresponding uniform conductor from which it is produced, except that it has increased effective inductance. It will of course be understood from the foregoing discussion that the 85 distance between the reactance sources is determined by the wave length to be transmitted or the wave lengths which constitute the components of a complex wave to be transmitted and by the required degree of approxi- 90 mation to a corresponding uniform conductor with respect to distortion and attenuation of the waves to be transmitted.

The apparatus is not claimed herein.

This case is filed as a divisional application 95 of my former application entitled "Improvements in the art of reducing attenuation of electrical waves and apparatus therefor," filed December 14, 1899, Serial No. 740,238, pursuant to a requirement by the Patent Office that 100 the said application be divided, so as to separate apparatus and method claims.

It will be obvious that many changes can be made without departing from the spirit of my invention. Therefore, without limiting 105 myself to the precise details shown,

What I claim as new, and desire to secure by Letters Patent of the United States, is—
The method of diminishing the attenuation constant of a uniform wave-conductor which consists in increasing the inductance of the conductor sufficiently to secure the required diminution of the attenuation constant, by distributing along it inductance sources at periodically-recurring points, the distance between consecutive points being such as to preserve approximately its character as a uniform conductor with respect to the waves to be transmitted, substantially as described.

Signed at New York city, New York, this 120 26th day of May, 1900.

MICHAEL IDVORSKY PUPIN.

Witnesses:

THOMAS EWING, Jr., SAMUEL W. BALCH.