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(71) Applicant (for all designated States except US): **ARIEL-UNIVERSITY RESEARCH AND DEVELOPMENT COMPANY, LTD.** [IL/IL]; Building 3A, Kiryat Hamada Ariel University Center of Samaria, 40700 Ariel (IL).

(72) Inventors; and

(75) Inventors/Applicants (for US only): **BEN-MOSHE, Boaz** [IL/IL]; 18 Shalom Aleichem Street, 46703 Herzliya (IL).

**LEVI, Harel** [IL/IL]; 28 Bazel Street, 62744 Tel Aviv (IL).

(74) Agent: **GUR, Erez**; POB 1372, Weizman Street, 44113 Kfar Saba (IL).

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(54) Title: METHODS, DEVICES, AND USES FOR CALCULATING A POSITION USING A GLOBAL NAVIGATION SATELLITE SYSTEM

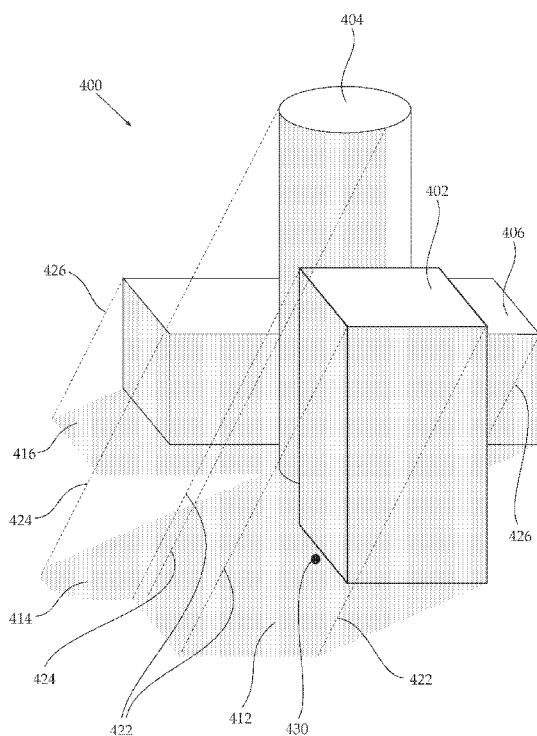


FIGURE 4

(57) Abstract: The invention, in some embodiments, relates to the field of global navigation satellite systems, and more particularly to the field of methods and devices for improving accuracy of position determination by receivers of global navigation satellite systems. Some embodiments of the invention relate to methods for generating a three-dimensional (3-D) representation of an urban area by a receiver of a global navigation satellite system using blocked lines of sight to satellites of the system. Additional embodiments of the invention relate to methods for transmitting a three-dimensional (3-D) representation of an urban area by a receiver of a global navigation satellite system for improving calculation of location by the global navigation satellite system receiver.



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## METHODS, DEVICES, AND USES FOR CALCULATING A POSITION USING A GLOBAL NAVIGATION SATELLITE SYSTEM

### RELATED APPLICATION

5           The present application gains priority from US Provisional Patent Application 61/426,541 filed 23 December 2010.

### FIELD AND BACKGROUND OF THE INVENTION

10           The invention, in some embodiments, relates to the field of global navigation satellite systems, and more particularly to the field of methods and devices for position determination by receivers of global navigation satellite systems.

          The invention, in some embodiments, relates to the field of urban mapping systems, and more particularly to the field of methods for generating a three-dimensional (3-D) representation of an urban area using a receiver of a global navigation satellite system.

15           Global Navigation Satellite Systems (GNSS) provide autonomous geo-spatial positioning, typically including global coverage. A global navigation satellite system allows an electronic receiver to determine its own position, namely longitude, latitude, and altitude, to within a few meters, using ephemeris data and time signals transmitted by radio from one or more satellites.

20           A GNSS receiver approximates its position by interpolating the signal from each navigation satellite, and specifically the precise coordinates of the satellite contained in the ephemeris data and the time stamps received from the satellite, into a pseudorange, indicating a region to which the signal from the satellite could travel in the specified time duration. Using at least four such pseudoranges and their associated satellite locations, the GNSS  
25           receiver computes its location by intersecting the pseudoranges to obtain a user position. The position is generally provided to a user as a position region, for example a position circle having a calculated center point indicating the most likely position of the receiver, and a radius that indicates an estimated error. Mathematically, four pseudoranges are sufficient to determine the position of the receiver with a reasonable error.

30           Disregarding topography and terrestrial objects on the Earth's surface, most global navigation satellite systems, such as GPS, GLONASS, and Galileo, have satellite coverage that ensures that a receiver on Earth has simultaneous lines of sight (LOS) to at least four satellites and can therefore accurately determine its position.

In most cases, a strong signal received by a GNSS receiver indicates the existence of a line of sight between the receiver and the satellite. Therefore, a GNSS device operating in an open area typically sorts captured signals according to their strengths, and uses the four strongest signals to calculate its location fairly accurately, typically with an error range within  
5 2-5 meters.

When the line of sight to a number of satellites is blocked, calculated position accuracy may decrease. For example, in many cities, such as downtown Manhattan, the tall buildings or other obstacles form an urban canyon where sky visibility is greatly limited. It is very common for a GNSS device operating in an area of this sort to be surrounded by  
10 obstacles which block the line of sight to most, if not all, otherwise available satellites. As mentioned above, at least four strong-enough signals, equivalent to four line-of-sight satellites, are required for accurate position determination. Therefore, a narrowly available sky which allows a GNSS receiver to have a line of sight to less than four satellites, leads to a skewed position computation, or, in the worst case, an inability of the receiver to compute its  
15 location. Moreover, objects such as building walls may reflect a signal from a satellite towards the receiver, leading to a mistaken pseudorange calculation.

As a result of the presence of tall buildings and other obstacles, a receiver in urban areas often provides a position circle with a large radius reflecting a greater error in a position calculation. Blocked lines of sight and signal reflections in an urban area may lead to  
20 estimated errors in position calculation of a few tens of meters, and in some instances even up to hundreds of meters. In some such cases the GNSS receiver is not able to calculate a position at all.

Several methods for determining whether a satellite has a line of sight (an "LOS satellite") or does not have a line of sight (an "NLOS satellite") to the receiver, have been  
25 developed, such as those described in U.S. Patent No. 7,577,445 and U.S. Patent Application Publication No. 2005/0124368.

In addition to methods for determining whether or not a satellite is in line of sight to a receiver, several methods for improving the accuracy of a position calculation in an urban area have been suggested. One such method is Map Matching, which is based on the  
30 assumption that the GNSS receiver is located inside a car, which drives at some estimated speed on top of a road with a known path. Thus, the location of the GNSS receiver can be limited by matching a road map of the terrain to the proposed position region, and thereby limiting the possible location of the GNSS receiver to areas of the proposed position region that correspond to roads.

Another such method is known as dead-reckoning. A dead-reckoning navigation system, calculates the current position by using a previously determined position, or fix, and advancing that position based upon known or estimated speeds over elapsed time, and course. In some systems, the vehicle is equipped with sensors that record the wheel rotation and steering direction which are available as position and speed input for the navigation system receiver. However, one of the disadvantages of dead-reckoning is that new values are calculated using previous values, and therefore errors and uncertainty regarding the calculated values will accumulate over time.

## 10 SUMMARY OF THE INVENTION

Some embodiments of the invention relate to methods for calculating a position of an object using a global navigation satellite system, by accounting for discrepancies between potential positions of the object within a region and the presence and/or absence of line of sight to at least one, preferably more than one, satellites. In some such embodiments, such discrepancies are identified with reference to a three-dimensional shading map of a region where the object is located.

Some embodiments of the invention relate to methods for mapping an urban area using a global navigation satellite system, by accounting for areas in which a satellite moves from having a line of sight (LOS) to a receiver to not having a line of sight (NLOS) to the receiver, as indicated by a satellite shading map of a region, and vice versa.

In accordance with some aspects of an embodiment of the teachings herein, there are provided methods and devices for calculating the position of a GNSS (Global Navigation Satellite System) receiver, including:

- receiving a plurality of signals from a first plurality of GNSS satellites;
- 25 calculating a region in which a GNSS receiver is located based on at least some of the received signals;
- for each satellite in a second plurality of GNSS satellites, classifying whether:
  - the satellite is a line-of-sight (LOS) satellite, having a line of sight to the GNSS receiver; or
  - 30 the satellite is a non-line-of-sight (NLOS) satellite, not having a line of sight to the GNSS receiver;
- obtaining at least one three-dimensional representation of an area including the region;

for each satellite in the second plurality of GNSS satellites, using the three-dimensional representation to define a three-dimensional shading representation including at least one illuminated subregion and at least one shaded subregion, such that a GNSS receiver located in the at least one illuminated subregion has a line of sight the satellite and a GNSS receiver located in the at least one shaded subregion does not have a line of sight to the satellite;

for each three-dimensional shading representation defining a shading surface which divides between the at least one illuminated subregion and the at least one shaded subregion, such that the at least one illuminated subregion is located above the shading surface and the at least one shaded subregion is located beneath the shading surface; and

for each satellite in the second plurality of GNSS satellites, eliminating from the region at least one subregion, thereby to identify a position in which the GNSS receiver is located, wherein:

if the satellite is a LOS satellite, eliminating from the region any portion which is located below the shading surface defined for the satellite; and

if the satellite is a NLOS satellite, eliminating from the region any portion which is located above the shading surface defined for the satellite.

In some embodiments, each satellite in the first plurality of GNSS satellites is located above the horizon relative to the GNSS receiver. In some embodiments, each satellite in the second plurality of GNSS satellites is located above the horizon relative to the GNSS receiver.

In some embodiments, the first plurality of GNSS satellites is included in the second plurality of GNSS satellites. In some such embodiments, the first plurality of GNSS satellites and the second plurality of GNSS satellites comprise the same plurality of GNSS satellites.

According to some embodiments, the calculating comprises using at least some strongest of the received signals to calculate the region in which the GNSS receiver is located. In some embodiments, the methods and devices also include, following the calculating and prior to the classifying, testing whether a radius of the region is greater than a predetermined threshold.

In some embodiments the classifying comprises using signal strength classification. In some embodiments, the area is larger than the region.

In some embodiments, the obtaining includes loading the three-dimensional representation into the GNSS receiver in the form of a software module. In some such

embodiments, the loading comprises repeatedly loading the three-dimensional representation into the GNSS receiver at a rate of at least once a day. In some such embodiments, the loading comprises loading the three-dimensional representation into the GNSS receiver prior to the receiving.

5 In some embodiments, the loading comprises loading the three-dimensional representation using at least one wireless communication method. In some such embodiments, the at least one wireless communication method comprises at least one of Wi-Fi, GSM, and Bluetooth®.

10 In some embodiments, at least one of the three-dimensional shading representation and a corresponding shading surface is defined substantially in real time. In some such embodiments, the defining is by the GNSS receiver. In some such embodiments, the at least one of the three-dimensional shading representation and a corresponding shading surface is defined by a server, external to the GNSS receiver, and is loaded from the server into the GNSS receiver using at least one wireless communication method. In some such  
15 embodiments, the at least one wireless communication method comprises at least one of Wi-Fi, GSM, and Bluetooth®.

In some embodiments, at least one of the three-dimensional shading representation and a corresponding shading surface is defined in advance of the classification of the second plurality of GNSS satellites, in a device external to the GNSS receiver. In some such  
20 embodiments, the at least one of the three-dimensional shading representation and a corresponding shading surface is loaded from the device external to the GNSS receiver into the GNSS receiver as a data module.

In some embodiment, the at least one of the three-dimensional shading representation and a corresponding shading surface is recalculated at a rate not slower than every 30 seconds  
25 based on changes to ephemeris data of the satellite. In some embodiment, the three-dimensional shading representation also includes at least one border subregion. In some such embodiments, the at least one border subregion lies along the shading surface corresponding to the three-dimensional shading representation.

In some embodiments, the eliminating includes defining a set of surface inequalities, each corresponding to a constraint defined by one of the shading surfaces and finding a  
30 solution to the set of surface inequalities, which solution comprises the identifying the position. In some such embodiments, the finding a solution comprises finding a solution which satisfies only some of the inequalities in the set of surface inequalities.

In some embodiments, the finding a solution comprises finding a solution which satisfies a maximal number of the inequalities in the set of surface inequalities. In some embodiments, the finding a solution includes assigning a confidence value to each inequality in the set of surface inequalities and finding a solution which maximizes the confidence of satisfied surface inequalities of the set of surface inequalities.

In accordance with some aspects of an embodiment of the teachings herein, there are provided methods and devices for creating a three-dimensional representation of terrestrial objects in an urban area, including:

obtaining a log file from at least one GNSS receiver, the log file containing information obtained in an urban area;

extracting from the log file a plurality data items, each data item including a timestamp, a position, and a signal strength captured from a GNSS satellite at the position and at the timestamp;

for each of the plurality of data items, classifying whether at the timestamp and at the location:

the satellite is a line-of-sight (LOS) satellite, having a line of sight to the GNSS receiver; or

the satellite is a non-line-of-sight (NLOS) satellite, not having a line of sight to the GNSS receiver;

using the classification to identify three-dimensional contours of terrestrial objects in the urban area.

In some embodiments, the information is obtained along a route taken by the at least one GNSS receiver in the urban area. In some embodiments, the using the classification includes finding locations in which there is a change in satellite status based on ones of the plurality of data items having consecutive timestamps, wherein the change in satellite status comprises one of a transition from the satellite being a LOS satellite to the satellite being a NLOS satellite and a transition from the satellite being a NLOS satellite to the satellite being a LOS satellite, defining the locations as contour edge points, and identifying the three-dimensional contours of the terrestrial objects such that two-dimensional contours of the terrestrial objects are bounded by the contour edge points.

In some embodiments, the finding comprises computing a distance function which corresponds to the number of satellites for which there is a change of satellite status at the locations. In some such embodiments, the computing a distance function comprises computing a weighted distance function, wherein the contribution to the distance function of



a change of satellite status for a satellite at a high angle with respect to the GNSS receiver is greater than the contribution of a change of satellite status for a satellite at a low angle with respect to the GNSS receiver.

In some embodiments, the defining comprises defining as the contour edge points specific ones of the locations for which the distance function is greater than a predetermined threshold. In some embodiments, the methods and devices also include, following the finding locations and prior to the defining the locations as contour edge points, eliminating ones of the locations for which there is a high probability of error.

In some embodiments, the two-dimensional contours comprise general polygons. In some embodiments, the two-dimensional contours include curved lines.

In some embodiments, the using the classification includes for each of the plurality of data items, defining a three-dimensional vector between the position and a position of the satellite based on ephemeris data of the satellite at the timestamp, labeling each vector of the three-dimensional vectors as a LOS vector if a satellite in a data item corresponding to the vector is classified as a LOS satellite, and as a NLOS vector if the satellite is classified as a NLOS satellite, defining the height of the three-dimensional contours to satisfy at least some of a plurality of constraints based on the plurality of three-dimensional vectors, wherein the height of the three-dimensional contours is defined to obstruct some of the three-dimensional vectors labeled as NLOS vectors, and not to obstruct some others of the three-dimensional vectors labeled as LOS vectors.

According to some embodiments, the defining height comprises defining the height to satisfy a maximal number of the plurality of constraints. In some embodiments, the defining height includes assigning a weight to each of the plurality of constraints and computing the height to maximize the weight of satisfied ones of the plurality of constraints. According to some embodiments, the classifying comprises using signal strength classification. In accordance with some aspects of an embodiment of the teachings herein, there are provided methods and devices for transmitting a three-dimensional representation of an area, to a GNSS receiver, for improving calculation, including:

at a fixed location, calculating a three-dimensional representation of an area;

receiving from a GNSS receiver an indication of a location of the GNSS receiver, the location being included in the area; and

transmitting at least a portion of the three-dimensional representation of the area from the fixed location to the GNSS receiver, the portion including a three-dimensional representation of the location.

In some embodiments, the calculating a three-dimensional representation comprises calculating a shading three-dimensional representation of the area. In some embodiments, the calculating comprises repeatedly calculating the three-dimensional representation of the area, at least once every 24 hours.

5 In some embodiments, the transmitting comprises using a wireless communication method to transmit the three-dimensional representation of the area. In some embodiments, the transmitting comprises transmitting the three-dimensional representation as a software module.

10 In some embodiments, the calculating comprises calculating the three-dimensional representation at a first rate and transmitting the three-dimensional representation at a second rate. In some such embodiments, the first rate is different from the second rate.

In some embodiments, the second rate is dependent on processing power restrictions of the GNSS receiver. In some embodiments, the second rate is dependent on a transmission bandwidth.

15 Aspects and embodiments of the invention are described in the specification hereinbelow and in the appended claims.

Unless otherwise defined, all technical and scientific terms used herein have the same meaning as commonly understood by one of ordinary skill in the art to which the invention  
20 pertains. In case of conflict, the specification, including definitions, will take precedence.

As used herein, the terms "comprising", "including", "having" and grammatical variants thereof are to be taken as specifying the stated features, integers, steps or components but do not preclude the addition of one or more additional features, integers, steps, components or groups thereof. These terms encompass the terms "consisting of" and  
25 "consisting essentially of".

As used herein, the indefinite articles "a" and "an" mean "at least one" or "one or more" unless the context clearly dictates otherwise.

Embodiments of methods and/or devices of the invention may involve performing or completing selected tasks manually, automatically, or a combination thereof. Some  
30 embodiments of the invention are implemented with the use of components that comprise hardware, software, firmware or combinations thereof. In some embodiments, some components are general-purpose components such as general purpose computers or oscilloscopes. In some embodiments, some components are dedicated or custom components such as circuits, integrated circuits or software.

For example, in some embodiments, some of an embodiment is implemented as a plurality of software instructions executed by a data processor, for example which is part of a general-purpose or custom computer. In some embodiments, the data processor or computer comprises volatile memory for storing instructions and/or data and/or a non-volatile storage, for example, a magnetic hard-disk and/or removable media, for storing instructions and/or data. In some embodiments, implementation includes a network connection. In some embodiments, implementation includes a user interface, generally comprising one or more of input devices (e.g., allowing input of commands and/or parameters) and output devices (e.g., allowing reporting parameters of operation and results.

#### BRIEF DESCRIPTION OF THE FIGURES

Some embodiments of the invention are described herein with reference to the accompanying figures. The description, together with the figures, makes apparent to a person having ordinary skill in the art how some embodiments of the invention may be practiced. The figures are for the purpose of illustrative discussion and no attempt is made to show structural details of an embodiment in more detail than is necessary for a fundamental understanding of the invention. For the sake of clarity, some objects depicted in the figures are not to scale.

In the Figures:

FIG. 1 is a pictorial illustration of an embodiment of a system for improving global navigation satellite system accuracy according to an embodiment of the teachings herein;

FIGS. 2A and 2B, when taken together, are a flow chart of an embodiment of a method for improving global navigation satellite system accuracy according to an embodiment of the teachings herein;

FIGS. 3A, 3B and 3C are schematic representations of an embodiment of a three-dimensional map of one urban area overlaid with shading maps associated with three satellites according to an embodiment of the teachings herein;

FIG. 4 is a schematic representation of an embodiment of a three-dimensional map of an urban area showing a shading map and the resulting shading surface according to an embodiment of the teachings herein;

FIG 5 is a pictorial illustration of a portion of a method for urban mapping according to an embodiment described herein; and

FIG. 6 is a flow chart of an embodiment of a method for generating a three-dimensional representation of an object.

DESCRIPTION OF SOME EMBODIMENTS OF THE INVENTION

The invention, in some embodiments, relates to the field of global navigation satellite systems, and more particularly to the field of methods and devices for improving accuracy of position determination by receivers of global navigation satellite systems. Some  
5 embodiments of the invention relate to methods for calculating the position of a GNSS (Global Navigation Satellite System) receiver, including:

receiving a plurality of signals from a first plurality of GNSS satellites;

calculating a region in which a GNSS receiver is located based on at least some of the received signals;

10 for each satellite in a second plurality of GNSS satellites, classifying whether:

the satellite is a line-of-sight (LOS) satellite, having a line of sight to the GNSS receiver; or

the satellite is a non-line-of-sight (NLOS) satellite, not having a line of sight to the GNSS receiver;

15 obtaining at least one three-dimensional representation of an area including the region;

for each satellite in the second plurality of GNSS satellites, using the three-dimensional representation to define a three-dimensional shading representation including at least one illuminated subregion and at least one shaded subregion, such  
20 that a GNSS receiver located in the at least one illuminated subregion has a line of sight the satellite and a GNSS receiver located in the at least one shaded subregion does not have a line of sight to the satellite;

for each three-dimensional shading representation defining a shading surface which divides between the at least one illuminated subregion and the at least one shaded  
25 subregion, such that the at least one illuminated subregion is located above the shading surface and the at least one shaded subregion is located beneath the shading surface; and

for each satellite in the second plurality of GNSS satellites, eliminating from the region at least one subregion, thereby to identify a position in which the GNSS  
30 receiver is located, wherein:

if the satellite is a LOS satellite, eliminating from the region any portion which is located below the shading surface defined for the satellite; and

if the satellite is a NLOS satellite, eliminating from the region any portion which is located above the shading surface defined for the satellite.

Some embodiments of the invention relate to devices or calculating the position of a GNSS (Global Navigation Satellite System) receiver, including:

a signal receiver configured to receive a plurality of signals from a first plurality of GNSS satellites;

a region-calculating module configured to calculate a region in which a GNSS receiver is located based on at least some of the received signals;

a satellite classification module, configured to, for each satellite in a second plurality of GNSS satellites, classify whether:

the satellite is a line-of-sight (LOS) satellite, having a line of sight to the GNSS receiver; or

the satellite is a non-line-of-sight (NLOS) satellite, not having a line of sight to the GNSS receiver;

a shading representation defining module configured to obtain at least one three-dimensional representation of an area including the region and for each satellite in the second plurality of GNSS satellites, to use the three-dimensional representation to define a three-dimensional shading representation including at least one illuminated subregion and at least one shaded subregion, such that a GNSS receiver located in the at least one illuminated subregion has a line of sight the satellite and a GNSS receiver located in the at least one shaded subregion does not have a line of sight to the satellite;

a shading surface calculating module configured to define, for each three-dimensional shading representation, a shading surface which divides between the at least one illuminated subregion and the at least one shaded subregion, such that the at least one illuminated subregion is located above the shading surface and the at least one shaded subregion is located beneath the shading surface; and

a subregion eliminating module configured for each satellite in the second plurality of GNSS satellites, to eliminate from the region at least one subregion, thereby to identify a position in which the GNSS receiver is located, wherein:

if the satellite is a LOS satellite, eliminating from the region any portion which is located below the shading surface defined for the satellite; and

if the satellite is a NLOS satellite, eliminating from the region any portion which is located above the shading surface defined for the satellite.

Some embodiments of the invention relate to methods for generating a three-dimensional (3-D) representation of an urban area by a receiver of a global navigation satellite system using blocked lines of sight to satellites of the system.

Some embodiments of the invention relate to methods for creating a three-dimensional representation of terrestrial objects in an urban area, including obtaining a log file from at least one GNSS receiver, the log file containing information obtained in an urban area, extracting from the log file a plurality data items, each data item including a timestamp, a position, and a signal strength captured from a GNSS satellite at the position and at the timestamp, for each of the plurality of data items, classifying whether at the timestamp and at the location, the satellite is a line-of-sight (LOS) satellite, having a line of sight to the GNSS receiver or the satellite is a non-line-of-sight (NLOS) satellite, not having a line of sight to the GNSS receiver, using the classification to identify three-dimensional contours of terrestrial objects in the urban area.

Some embodiments of the invention relate to devices for device for creating a three-dimensional representation of terrestrial objects in an urban area, including a data obtaining module configured to obtain a log file from at least one GNSS receiver, the log file containing information obtained in an urban area, a data extractor configured to extract from the log file a plurality data items, each data item including a timestamp, a position, and a signal strength captured from a GNSS satellite at the position and at the timestamp, a classification module, configured to, for each of the plurality of data items, classify whether at the timestamp and at the location, the satellite is a line-of-sight (LOS) satellite, having a line of sight to the GNSS receiver or the satellite is a non-line-of-sight (NLOS) satellite, not having a line of sight to the GNSS receiver, a contour identification module configured to use the classification to identify three-dimensional contours of terrestrial objects in the urban area.

Some embodiments of the invention relate to methods for transmitting a three-dimensional (3-D) representation of an urban area by a receiver of a global navigation satellite system for improving calculation of location by the global navigation satellite system receiver.

Some embodiments of the invention relate to methods for transmitting a three-dimensional representation of an area, to a GNSS receiver, for improving calculation, including at a fixed location, calculating a three-dimensional representation of an area, receiving from a GNSS receiver an indication of a location of the GNSS receiver, the location being included in the area, and transmitting at least a portion of the three-dimensional

representation of the area from the fixed location to the GNSS receiver, the portion including a three-dimensional representation of the location.

The principles, uses and implementations of the teachings herein may be better understood with reference to the accompanying description and figures. Upon perusal of the description and figures present herein, one skilled in the art is able to implement the invention without undue effort or experimentation.

Before explaining at least one embodiment of the invention in detail, it is to be understood that the invention is not limited in its applications to the details of construction and the arrangement of the components and/or methods set forth in the following description and/or illustrated in the drawings and/or the Examples. The invention can be implemented with other embodiments and can be practiced or carried out in various ways. It is also understood that the phraseology and terminology employed herein is for descriptive purpose and should not be regarded as limiting.

As discussed in the introduction, blocked line of sight between a receiver of a global navigation satellite system and one or more satellites, due to terrestrial objects, for example city buildings and other objects in an urban area, may be a source of errors in position calculation for GNSS receivers.

Reference is now made to Figure 1, which is a pictorial illustration of a system for improving global navigation satellite system accuracy according to an embodiment of the teachings herein. As seen in Figure 1, a receiver **10** of a global navigation satellite system is located in an urban area which includes several tall buildings, indicated by reference numerals **12** and **14**. A plurality of satellites of a global navigation satellite system, indicated by reference numerals **16**, **18**, and **20**, are seen orbiting the Earth **22**.

As seen in Figure 1, the satellites **16** are below the horizon with respect to receiver **10**, and therefore invisible to receiver **10**. Receiver **10** may be able to receive signals from satellites **18** and **20**, which are in a visible range with respect to the receiver **10**. That being said, each satellite **18** and **20** in the visible range can be classified as a line of sight (LOS) satellite or a non line of sight (NLOS) satellite, depending on whether the receiver has an unblocked line of sight with that satellite.

As seen in Figure 1, satellite **20** is a LOS satellite, having an unblocked line of sight to receiver **10**. Satellites **18** are NLOS satellites, because the respective lines of sight between the satellites **18** and the receiver **10** are blocked by buildings **12** and/or **14**.

The signal strength received from a LOS satellite such as **20** is typically no less than 3dB from the maximum signal strength, and is dependent on factors such as weather

conditions and the location of a receiver such as receiver **10** on the face of Earth. Signals transmitted by NLOS satellites such as satellites **18** may be received indirectly by receiver **10** through reflections from various surfaces in an urban area. The signal strength received from an NLOS satellite is typically less than 6dB below the maximum signal strength.

5 Typically, location calculations which are based on signals received from NLOS satellites such as satellites **18**, or that take into consideration signals from NLOS satellites, are error prone. This is due to the fact that such signals are received through reflections off one or more objects surrounding the receiver **10**, such as the walls of a building **12**. As a result, the pseudorange determined by receiver **10** using a signal received from an NLOS  
10 satellite **18** is different from the true pseudorange that corresponds to the distance to that satellite **18**.

As known in the art, the receiver **10** can calculate which of the visible satellites **18** and **20** is a LOS satellite and which is a NLOS satellite, for example as described in U.S. Patent No. 7,577,445 and U.S. Patent Application Publication No. 2005/0124368. According  
15 to some embodiments of the teachings herein, the knowledge that satellites **18** are NLOS satellites and/or that satellite **20** is an LOS satellite, is used to improve the accuracy of the position calculation by receiver **10**, since this requires that receiver **10** be in a position where it has a direct line of sight to satellite **20**, and at the same time where it does not have a direct line of sight to any of satellites **18**. When a receiver **10** is found, for example, in an urban  
20 region, this may greatly limit the range of possible locations where receiver **10** may be located, and in some embodiments herein is employed to improve the accuracy of the location calculated by receiver **10**, as described hereinbelow.

Reference is now made to Figures 2A and 2B, which when taken together, are a flow  
25 chart of a method for improving global navigation satellite system accuracy according to an embodiment of the teachings herein.

As seen in Figure 2A, a GNSS receiver, such as GNSS receiver **10** of Figure 1, receives signals from a plurality of satellites, as indicated by reference numeral **200**, and uses these signals to calculate a preliminary position circle, as indicated by reference numeral **202**. The calculation of the preliminary position circle may be carried out using any suitable  
30 method, for example as known in the art, for example by using the four strongest received signals.

As seen in reference numeral **204**, if the calculated preliminary position circle is sufficiently accurate, that is to say if the radius of the calculated preliminary position circle is not greater than a pre-determined threshold, for example, five meters, the calculated



preliminary position circle is reported to the user, using methods known in the art, as indicated by reference numeral **206**. In some embodiments, the reported position circle is stored as the last known position of the GNSS receiver, as indicated by reference numeral **208**.

5           Returning to reference numeral **204**, if the calculated preliminary position circle is not accurate enough, for example, its radius is greater than a pre-determined threshold, the GNSS receiver checks whether or not a signal was received from all the satellites that are expected to be visible within the preliminary position circle (equivalent to satellites **18** and **20** depicted in Figure 1), as indicated by reference numeral **210**. If there is one or more satellites from  
10       which the receiver expected to receive a signal when in the preliminary position circle, and such a signal was not received, the GNSS receiver classifies the one or more satellites as NLOS satellites, as indicated by reference numeral **212**.

          As seen at reference numeral **214**, regardless of the existence of satellites from which the GNSS receiver expected to receive a signal and did not receive such a signal, the GNSS  
15       receiver proceeds to classify at least one, and preferably each one, of the satellites from which it did receive a signal as a LOS satellite or as a NLOS satellite, typically using methods known in the art such as signal strength, or methods described in U.S. Patent No. 7,577,445 and U.S. Patent Application Publication No. 2005/0124368.

          For example, when using a signal strength method, a received signal which is stronger  
20       than a threshold, such as a threshold between 3 dB and 6 dB from the maximum, corresponds to a LOS satellite, while a signal which is weaker than the threshold, e.g., less than 9 dB corresponds to a NLOS satellite. In some embodiments, the threshold is a fixed threshold. In some embodiments, the threshold varies dynamically, for example between 3dB and 6dB, according to the angle of the satellite, the location of the receiver on earth, and adaptive  
25       criteria.

          Turning to reference numeral **216**, it is seen that the GNSS receiver receives a three-dimensional representation, such as a map, of the terrestrial objects in a general region in which the receiver is located. For example, the three-dimensional representation may include a representation of buildings, bridges, and tunnels, in an urban area where the receiver is  
30       located.

          In some embodiments, the three-dimensional representation is a representation of a large area, for example an area of 10,000 square meters. In some embodiments, the area is that of a county, a city or a substantial portion of a city (e.g., a city center, a neighborhood, a commercial zone) in which the GNSS receiver is located. In some embodiments, the three-

dimensional representation is a representation of a smaller area, such as the preliminary position circle calculated at reference numeral **202** or a neighborhood in which the preliminary position circle is located.

5 In some embodiments, the three-dimensional representation is loaded to a memory unit of the GNSS receiver in the form of a software module. In some embodiments, the three-dimensional representation is loaded to the GNSS receiver approximately in real-time, following computation of the preliminary position circle, for example by using wireless communication methods known in the art, such as Wi-Fi, GSM, or Bluetooth®.

10 In some embodiments, three-dimensional representations may be loaded into the GNSS receiver in advance of using the GNSS receiver. Such preloading of the GNSS receiver may be carried out by the user, for example by loading three-dimensional representations of areas or regions that the user expects to visit. In some such embodiments, when a preliminary position circle is calculated by the GNSS receiver, as described hereinabove at reference numeral **202**, the required three-dimensional representation of the  
15 area is already loaded into the GNSS receiver.

As seen at reference numeral **218**, for at least some, preferably each satellite in the visible range with respect to the GNSS receiver at the preliminary position circle, and regardless of a signal actually being received from each such satellite, the GNSS receiver obtains a shading map associated with the satellite.

20 In some embodiments, the shading map is based on the three-dimensional representation of the area, and is defined by a three-dimensional shading surface. In some such embodiments, the subregion under the surface is a shaded subregion, that is a subregion in which there is no line of sight to the satellite, and the subregion over the surface is an illuminated subregion, that is a subregion in which there is a line of sight to the satellite. An  
25 example of a shading map and a corresponding shading surface is shown in Figure 4 and is described in detail hereinbelow with reference thereto.

Typically, the shading map and corresponding shading surface are dependent on the exact position of the satellite, and is therefore dependent on the time of day in which it is obtained. Due to this, the shading map and shading surface are typically valid only for  
30 approximately 30 seconds, after which time they must be updated to compensate for the movement of the satellite relative to the earth surface and to the change in the satellite's ephemeris data.

In some embodiments, the calculation of a shading map and the corresponding shading surface is performed for an immediate area at which the GNSS receiver is located,

and which includes the preliminary position circle calculated by the receiver at reference numeral **202**. In some embodiments such calculation is performed for a larger area such as an entire city in which the receiver is located.

In some embodiments the calculation of an updated shading map and the corresponding shading surface is performed substantially in real time by the GNSS receiver and updated frequently, such as more frequently than every 30 seconds, more frequently than every 20 seconds, more frequently than every 10 seconds, more frequently than every 5 seconds and even more frequently than every one second. In some embodiments, the calculation is as frequent as ten times per second.

In some embodiments the calculation of a shading map and the corresponding shading surface is performed externally to the receiver, and the results, in the form of shading maps and shading surfaces, are loaded to the GNSS receiver, typically as data modules, each time the shading map and shading surface is refreshed. In some such embodiments the shading map and shading surface is updated frequently, such as more frequently than every 30 seconds, more frequently than every 20 seconds, more frequently than every 10 seconds, more frequently than every 5 seconds and even more frequently than every one second. In some embodiments, the updating is as frequent as ten times per second.

In some embodiments shading map and shading surface calculations are performed substantially in real time externally to a receiver, for example by a server, which imparts the results, in the form of shading maps and shading surfaces, to the GNSS receiver using any suitable wireless communication method, such as Wi-Fi, GSM, or Bluetooth®. In some such embodiments an updated shading map and shading surface are imparted to the GNSS receiver frequently, such as more frequently than every 30 seconds, more frequently than every 20 seconds, more frequently than every 10 seconds, more frequently than every 5 seconds and even more frequently than every one second. In some embodiments, the imparting is as frequent as ten times per second.

In some embodiments, shading maps and shading surfaces are calculated externally to the GNSS receiver, for example by a server, at a first rate but are imparted to and obtained by the receiver at a second rate. In some embodiments, the second rate is dependent on the GNSS receiver, for example on the processing power of the GNSS receiver, and on the bandwidth available to wirelessly transfer the shading maps and shading surfaces to one or more GNSS receivers.

In some embodiments, shading maps and shading surfaces are calculated externally to the GNSS receiver, for example by a server, for a large geographical area such as a whole

city, but the shading maps and shading surfaces actually imparted to and/or obtained by the GNSS receiver are of a smaller geographical area.

In some embodiments the shading maps define, in addition to illuminated subregions and shaded subregions, also border subregions. Such border subregions typically lay along the surface defined by the shading surfaces, and represent areas in which it is not clear whether a GNSS receiver would or would not have a line of sight to the satellite.

In accordance with an embodiment of the teachings herein, and as described in further detail at reference numerals **220-236**, the GNSS receiver compares the shading maps obtained for each satellite to the classification of that satellite as a LOS satellite or a NLOS satellite. On the basis of such comparison, the GNSS receiver may eliminate from the preliminary position circle areas for which the shading map of a given satellite does not agree with the LOS or NLOS classification of that satellite with respect to the receiver.

For example, the GNSS receiver is unlikely to be found in a subregion which is shaded in a shading map associated with a satellite that was classified by the receiver as being a LOS satellite and such a subregion may therefore be eliminated from the preliminary position circle. Similarly, the receiver is unlikely to be found in a subregion which is illuminated in a shading map associated with another satellite which the receiver classified as being a NLOS satellite, and hence such a subregion may be eliminated from the preliminary position circle. Elimination of all unlikely subregions from the preliminary position circle provides a new position region, which usually has an improved accuracy.

Specifically, the comparison of the shading maps and the classification of the satellites is carried out using mathematical tools. As seen at reference numeral **220**, a shading surface inequality is defined for each satellite. For each satellite classified as a LOS satellite, the inequality is defined such that it demands that the receiver be placed above the shading surface, that is, in the illuminated subregion. Conversely, for each satellite classified as a NLOS satellite, the inequality demands that the receiver be placed beneath the shading surface, that is, in the shaded subregion.

According to some embodiments, it is possible to assign a confidence value to each inequality, the confidence value indicating how certain one is of the classification of the satellite as LOS or NLOS. In such a case, the inequalities associated with satellites that are clearly LOS, such as satellites from which a very strong signal is received, and the inequalities associated with satellites that are clearly NLOS, such as satellites from which no signal was received, would be assigned a high confidence value. Conversely, the inequalities associated with satellites for which the classification as LOS or NLOS is unclear, would be

assigned a low confidence value. It is appreciated that the assignment of confidence values to the inequalities, though it may further increase the accuracy of the resulting position circle defined by the GNSS receiver, is not necessary for the GNSS receiver to provide a sufficiently accurate result.

5           As seen at reference numeral **226**, the shading surface inequalities corresponding to each of the satellites classified as LOS and NLOS satellites are considered together, as a system of inequalities for which a solution is being sought.

A solution for the inequality system is then obtained, for example using linear programming, as indicated by reference numeral **228**.

10           In some embodiments, if there is no solution that satisfies all the inequalities, the appropriate solution is one that satisfies the highest number of shading inequalities in the inequality system.

In some embodiments, in which confidence values are assigned to the inequalities, the solution is one that maximizes the confidence of the satisfied inequalities.

15           As seen at reference numeral **230**, the GNSS receiver checks how many solutions to the inequality system are found. If, practically speaking, a single solution is found for the inequality system, the GNSS receiver defines a position circle corresponding to the area represented by that solution, as indicated by reference numeral **232**, and reports this position circle to the user, using methods known in the art, as indicated by reference numeral **206**. In  
20 some embodiments, the reported position circle is stored as the last known position of the GNSS receiver, as indicated by reference numeral **208**.

If multiple sufficiently-acceptable solutions are found for the inequality system, for example, multiple maximal values were found, at reference numeral **230**, the GNSS receiver uses additional methods and/or additional data to further increase the position accuracy and to  
25 determine which of the areas which are represented by those solutions is the most likely position of the GNSS receiver, as indicated by reference numeral **234**.

According to some embodiments, the GNSS receiver applies map matching to the areas represented by the multiple solutions, and uses the map matching result as the area at which the GNSS receiver is most likely to be positioned. In such embodiments, any suitable  
30 map matching method may be used, for example a map matching method known in the art.

According to some embodiments the GNSS receiver applies dead-reckoning to the areas represented by the multiple solutions, and uses the dead-reckoning result as the area at which the GNSS receiver is most likely to be positioned. In such embodiments, any suitable dead-reckoning method may be used, for example a dead-reckoning method known in the art.

As seen at reference numeral **236**, the GNSS receiver defines a position circle based on the area which was determined at reference numeral **234** to be the most likely position of the GNSS receiver. The receiver then reports the position circle to the user, using methods known in the art, as indicated by reference numeral **206**. In some embodiments, the reported position circle is stored as the last known position of the GNSS receiver, as indicated by reference numeral **208**.

It is appreciated that the method of the teachings herein can be used regardless of the altitude, or elevation, of the GNSS receiver above the ground, and without the need to know whether or not the GNSS receiver is located at or above ground level. This is due to the fact that the system of inequalities defines a three-dimensional polygon, which has a height dimension, and therefore a solution that satisfies the inequalities may be anywhere in the height dimension of the polygon, including above the ground.

Additionally, because each shading surface used to define the system of inequalities is defined in three dimensions, and does not only define illuminated areas and shaded areas within a plane at a specific height, there is no need to know the altitude of the GNSS receiver prior to application of the shading surfaces.

Reference is now made to Figures 3A, 3B, and 3C, which are schematic representations of a three-dimensional map of one urban area **300** overlaid with shading maps associated with three satellites according to an embodiment of the teachings herein.

As seen in Figures 3A, 3B, and 3C, the urban area **300** includes a plurality of above-ground constructions, such as buildings **302**, which are similar to buildings **12** and **14** of Figure 1. As seen, the three-dimensional representation of the urban area **300** is identical in all of Figures 3A, 3B, and 3C, while the shading map **304** of Figure 3A, shading map **306** of Figure 3B, and shading map **308** of Figure 3C, differ. Each of Figures 3A, 3B, and 3C, corresponds to a different one of satellites **S1**, **S2**, and **S3**, (not shown), and the shading maps **304**, **306**, and **308** are each dependent on the azimuth position of the associated satellites **S1**, **S2**, and **S3**, which dependency causes the differences in the shading patterns. The shading maps **304**, **306**, and **308** may be generated using any suitable shading algorithm, such as that provided by the OpenGL and OpenGL ES-2 graphics libraries.

The shadowed regions in shading maps **304**, **306**, and **308**, represent regions of the urban area at which a GNSS receiver would have no line of sight to the associated satellite, for example because the line of sight is blocked by buildings **302**, while the illuminated regions represent regions at which a GNSS receiver would have a line of sight to the satellite. Stated otherwise, when a GNSS receiver, such as receiver **10** of Figure 1, is located in a

shadowed region, such as any of circles **310**, the satellite is a NLOS satellite, such as satellites **18** of Figure 1. Conversely, when such a GNSS receiver is located in an illuminated region, such as any of diamonds **312**, the satellite is a LOS satellite, such as satellite **20** of Figure 1.

5 As seen in Figures 3A, 3B, and 3C, each figure is marked with positions **P1**, **P2**, and **P3**. From Figures 3A, 3B, and 3C, when taken together, the line of sight to satellites **S1**, **S2**, and **S3** can be concluded.

Specifically, **P1** is in line of sight to all three satellites **S1**, **S2**, and **S3**, since it is in an illuminated region in all three shading maps **304**, **306**, and **308**. **P2** is in light of sight to  
 10 satellites **S1** and **S2**, and is not in line of sight to satellite **S3**, since it is in the illuminated regions in shading maps **304** and **306**, and is in the shaded region in shading map **308**. **P3** is in light of sight to satellites **S1**, and is not in line of sight to satellites **S2** and **S3**, since it is in the illuminated regions in shading map **304**, and is in the shaded region in shading maps **306** and **308**.

15 By classifying each of **S1**, **S2** and **S3** as a LOS or NLOS satellite (for example according to received signal strength) by a receiver situated in an *a priori* unknown position in the vicinity of positions **P1**, **P2**, and **P3**, and by comparing the results of such a classification to the calculated lines of sight as described above, the receiver can consider each of the positions as more probable or less probable as the actual position of the receiver,  
 20 thereby improving the accuracy of the position calculation.

For example, in the context of Figure 1, satellites **18** were classified as NLOS satellites, while satellite **20** was classified as a LOS satellite. Considering a situation in which **S1** corresponds to satellite **20** of Figure 1, and **S2** and **S3** correspond to satellites **18** of Figure 1, it is clear that the receiver must be in a position at which it has a line of sight to **S1** and  
 25 does not have lines of sight to **S2** and **S3**. From consideration of the combination of shading maps **304**, **306**, and **308**, it can be deduced that the GNSS receiver must be located at **P3**, where it has a line of sight only to **S1**, and does not have a line of sight to **S2** and **S3**. Thus, the location identified by the GNSS receiver, which initially included all of positions **P1**, **P2**, and **P3** may be reduced to include only the limited vicinity around **P3**, thereby providing the  
 30 user with a more accurate position calculation.

Reference is now made to Figure 4, which is a schematic representation of an embodiment of a three-dimensional map of an urban area showing a shading map and the resulting shading surface according to an embodiment of the teachings herein.

As seen in Figure 4, an urban area **400** includes buildings **402**, **404**, and **406**. As seen, each of buildings **402**, **404** and **406** defines a respective shaded region **412**, **414**, and **416** relative to a GNSS satellite **S4** (not shown). As can be seen each of the shaded regions **412**, **414**, and **416** is defined by one or more planes, the outlines of which are indicated by the dashed lines **422**, **424**, and **426**, respectively.

When a GNSS receiver is located in a shaded area with respect to the satellite, in which there is no line of sight with the satellite, it is in fact located under one or more of the planes. For example, a GNSS receiver located at the point indicated by reference numeral **430** is located beneath the surface defined by dashed lines **422**, and is therefore in the shaded region **412** caused by building **402**. A shading inequality corresponding to the shading surface of **S4**, as described hereinabove with reference to Figure 2, would demand that the GNSS receiver be beneath the shading surface for satellite **S4**, as seen in Figure 4.

#### Three-dimensional mapping of an urban area

In some embodiments, the teachings of the invention are used to generate a three-dimensional representation of an urban area. Generally, a three-dimensional representation is generated as a result of an inverse process of the method described hereinabove with reference to Figures 1-4.

As known, most GNSS receivers maintain a log file containing information regarding the GNSS receiver's route and the captured satellite signals along that route. Specifically, one can extract from the log file, for each location along the route of the GNSS receiver, the signal strength for each signal received at that location. In some embodiments, the possibility to track down signals is utilized for generating a three-dimensional model of the buildings in an urban area, as described herein.

In general, given a GNSS receiver's log file which includes information, from which triplets of time, position, and signal strength to each traceable satellite can be extracted. Each traceable satellite at each given position along the route can be classified as a LOS satellite or a NLOS satellite, as described hereinabove in reference to Figure 2. A three-dimensional vector can then be defined from the GNSS receiver, when placed at a specific location, toward each traceable satellite, where the vectors can be divided into those directed towards LOS satellites and those directed towards NLOS satellites. In order to generate a three-dimensional representation of the urban area along the route recorded by the GNSS receiver, one must construct the surface such that all the vectors directed to NLOS satellites would be



blocked by terrestrial objects, and all the vectors directed to LOS satellites would not be blocked by any objects.

Reference is now made to Figure 5, which is a pictorial illustration of a portion of a method for urban mapping according to an embodiment described herein.

5 As seen in Figure 5, a GNSS receiver is located at a specific point **P1** in an urban area **500**. From reviewing a log file of the GNSS receiver, it can be concluded that the receiver was located at P1 at a specific time of day, for example, 4:00pm, and the ephemeris data for each of the satellites from which a signal was captured can be obtained. From the listing of signal strengths in the log file, and using methods known in the art, each of the satellites from  
10 which a signal was captured by the GNSS receiver may be classified as a LOS satellite or as a NLOS satellite.

According to an embodiment of the teachings herein, for each satellite, a three-dimensional vector is defined from point **P1** toward the satellite, based on the ephemeris data obtained for that satellite. In Figure 5, all the vectors that are directed to LOS satellites are  
15 indicated using one line type, such as a solid line shown in vectors **502**, and all the vectors that are directed to NLOS satellites are indicated using another line type, such as a dashed line shown in vectors **504**. The vectors **502** and **504** define a set of constraints on the location of buildings in the urban area **500**, since such buildings must not obstruct any of vectors **502**, and should obstruct all of vectors **504**. One example of compliance with the constraints  
20 imposed by vectors **502** and **504** is shown in Figure 5, as buildings **506**.

It is appreciated that the process described hereinabove with respect to **P1** is repeated for multiple points, preferably as many as possible, along the route taken by at least one, but preferably many, GNSS receivers, thereby providing a large set of constraints to be met, thereby enabling fairly accurate mapping of the buildings and satellite obstructions located in  
25 the mapped area.

In some embodiments only vectors to LOS satellites are used as described herein for mapping. In some embodiments only vectors to NLOS satellites are used as described herein for mapping. That said, in preferred embodiments vectors to both LOS and NLOS satellites are used as described herein for mapping.

30 Reference is now made to Figure 6, which is a flow chart of an embodiment of a method for mapping an urban area using a global navigation satellite system according to an embodiment of the teachings herein.

As seen at reference numeral **600**, log files are obtained from at least one, but preferably multiple GNSS receiver. As known in the art, such log files include information

from which one could extract time stamps and GNSS satellite identifications and signal strengths for each captured signal along a route taken by the GNSS receiver.

Multiple triplets are extracted from each log file, each triplet including a timestamp, the position at which the GNSS receiver was at that time, and signal strength captured from a specific satellite at that position at that time, as seen at reference numeral **602**. It is appreciated that triplets including the same time and position, and differing in the signal data reflect signals received from different GNSS satellites at one location at a given point in time.

Subsequently, for each triplet, the satellite is classified as being a LOS satellite or a NLOS satellite with respect to the GNSS receiver at that point at that time, as seen at reference numeral **604**. In some embodiments, the satellite is classified based on the strength of signal captured from that satellite. Alternately, the satellite may be classified using any classification method known in the art, such as those described in U.S. Patent No. 7,577,445 and U.S. Patent Application Publication No. 2005/0124368. In some embodiments, not all triplets are used. In some embodiments, fewer than all triplets are used. For example, in some embodiments no triplets corresponding to NLOS satellites are used while in some embodiments, no triplets corresponding to LOS satellites are used.

As seen at reference numeral **606**, for each pair of time consecutive samples obtained from a given GNSS receiver, a distance function is computed. A specific time sample includes all the triplets contained in the given GNSS receiver's log file which have the specified timestamp.

It is appreciated that in the context of the teachings herein the term "time consecutive samples" relates to any pair of samples separated by a relatively short time duration, and not necessarily to two samples taken immediately one after the other without any other sample taken between them.

According to some embodiments, the distance function is computed based on the change in the LOS/NLOS satellite between two consecutive timestamps. That is, if a given satellite was a LOS satellite at the first timestamp, and was a NLOS satellite at the second timestamp, that satellite would contribute to the distance function. Similarly, if a given satellite was a NLOS satellite at the first timestamp, and was a LOS satellite at the second timestamp, that satellite would contribute to the distance function. If the status of the satellite did not change between the two timestamps, it would not contribute to the distance function.

In some embodiments the contribution to the distance function is a weighted contribution, where satellites at a high angle with respect to the GNSS receiver have a greater

contribution to the distance function than satellites at a low angle with respect to the GNSS receiver.

As seen in reference numeral **608**, if the computed distance function is greater a pre-determined threshold value, a point which is extrapolated from the two time consecutive samples is defined as an edge point, as indicated by reference numeral **610**.

In some embodiments, the point is extrapolated based on the sample timestamps and on the velocity of the GNSS receiver. In some embodiments, the point is the average of the positions in the two time consecutive samples. In some such embodiments, the point is a weighted average of the positions in the two time consecutive samples.

It is appreciated that edge-points tend to appear at the edges and corners of obstructions such as building, and can therefore be used to identify the contours of the buildings or obstructions in an urban area.

Typically, multiple edge points are identified, such as edge points identified using multiple different pairs of time consecutive samples and/or data obtained from several GNSS receivers. In some embodiments, some edge points which are likely to be erroneous, such as those having a potential high position error are filtered out of the set of edge points used for further computation.

Once the set of edge points is defined the planar, two-dimensional contours, of obstructions in the urban area are computed, as indicated at reference numeral **612**. The two-dimensional contours are computed to be bounded by, or enclosed by, the previously identified edge points. In some embodiments, the contours are general polygons. In some embodiments, the contours are constrained shapes including curved lines.

Following computation of the two-dimensional contours of the obstructions, a height value must be determined for each contour. For this purpose, for each triplet included in each of the GNSS receiver's log files (although in some embodiments fewer than all triplets are used), a three-dimensional vector is calculated, as seen at reference numeral **614**. The three-dimensional vector for a given triplet virtually connects the position of the GNSS receiver with the position of the satellite, based on the ephemeris data of the satellite at the given timestamp. As seen at reference numeral **616**, each vector is labeled according to the LOS/NLOS status of the satellite for the corresponding triplet.

It is appreciated that as described hereinabove with reference to Figure 5, each of the vectors defines a constraint on the height of the buildings in the urban area, since the buildings must obstruct the NLOS vectors and must not obstruct the LOS vectors. Therefore, as seen at reference numeral **618**, the height of each of the two-dimensional contours

computed at reference numeral **612** is computed to be a height for which a maximal number of vector constraints is satisfied.

According to some embodiments, the vector constraints are weighted, such that vectors with higher ray angles are given a greater weight than vectors with lower ray angles, and such that the height is computed to maximize the weight of the satisfied constraints.

In some embodiments, a GNSS receiver is positioned at at least one well-defined location in an urban area for which it is desired to generate a three-dimensional representation. The exact location of the GNSS receiver is typically identified using any suitable method, such as a surveying map. Preferably the GNSS receiver is positioned at the well-defined location for a relatively long period time, such as several hours.

For each point in time during the period of time, the receiver identifies which visible satellites are LOS satellites and which are NLOS satellites, for example, according to signal strength, as known in the art. If a satellite is classified as a NLOS satellite, it is concluded that a terrestrial object, for example a building or a bridge, is obstructing the line of sight between the receiver and that satellite.

By considering the combination of the azimuth direction of blocked and unblocked lines of sight to the visible satellites from the well-defined location during the period of time, and particularly, considering the locations of transition from unblocked line of sight to blocked line of sight, and vice versa, the three-dimensional outlines of terrestrial objects are calculated to generate a three-dimensional representation of the vicinity of the location at which the receiver was placed.

It is appreciated that if this process is repeated in multiple well defined locations, a general three-dimensional representation for an urban area may be obtained by combining the three-dimensional representations generated for the vicinity of each of the locations at which the receiver was placed.

It is appreciated that certain features of the invention, which are, for clarity, described in the context of separate embodiments, may also be provided in combination in a single embodiment. Conversely, various features of the invention, which are, for brevity, described in the context of a single embodiment, may also be provided separately or in any suitable subcombination or as suitable in any other described embodiment of the invention. Certain features described in the context of various embodiments are not to be considered essential features of those embodiments, unless the embodiment is inoperative without those elements.

Although the invention has been described in conjunction with specific embodiments thereof, it is evident that many alternatives, modifications and variations will be apparent to those skilled in the art. Accordingly, it is intended to embrace all such alternatives, modifications and variations that fall within the scope of the appended claims.

- 5        Citation or identification of any reference in this application shall not be construed as an admission that such reference is available as prior art to the invention.

Section headings are used herein to ease understanding of the specification and should not be construed as necessarily limiting.

CLAIMS:

1. A method for calculating the position of a GNSS (Global Navigation Satellite System) receiver, comprising:

receiving a plurality of signals from a first plurality of GNSS satellites;

calculating a region in which a GNSS receiver is located based on at least some of said received signals;

for each satellite in a second plurality of GNSS satellites, classifying whether:

said satellite is a line-of-sight (LOS) satellite, having a line of sight to said GNSS receiver; or

said satellite is a non-line-of-sight (NLOS) satellite, not having a line of sight to said GNSS receiver;

obtaining at least one three-dimensional representation of an area including said region;

for each satellite in said second plurality of GNSS satellites, using said at least one three-dimensional representation to define a three-dimensional shading representation including at least one illuminated subregion and at least one shaded subregion, such that a GNSS receiver located in said at least one illuminated subregion has a line of sight said satellite and a GNSS receiver located in said at least one shaded subregion does not have a line of sight to said satellite;

for each said three-dimensional shading representation defining a shading surface which divides between said at least one illuminated subregion and said at least one shaded subregion, such that said at least one illuminated subregion is located above said shading surface and said at least one shaded subregion is located beneath said shading surface; and

for each satellite in said second plurality of GNSS satellites, eliminating from said region at least one subregion, thereby to identify a position in which said GNSS receiver is located, wherein:

if said satellite is a LOS satellite, eliminating from said region any portion which is located beneath said shading surface defined for said satellite; and

if said satellite is a NLOS satellite, eliminating from said region any portion which is located above said shading surface defined for said satellite.

2. A method according claim 1 and wherein each satellite in said first plurality of GNSS satellites is located above the horizon relative to said GNSS receiver.

3. A method according to any of the preceding claims and wherein each satellite in said second plurality of GNSS satellites is located above the horizon relative to said GNSS receiver.
4. A method according any of the preceding claims and wherein said first plurality of GNSS satellites is included in said second plurality of GNSS satellites.
5. A method according to any of the preceding claims and wherein said first plurality of GNSS satellites and said second plurality of GNSS satellites comprise the same plurality of GNSS satellites.
6. A method according to any of the preceding claims and wherein said calculating comprises using at least some strongest of said received signals to calculate said region in which said GNSS receiver is located.
7. A method according to any of the preceding claims and also comprising, following said calculating and prior to said classifying, testing whether a radius of said region is greater than a predetermined threshold.
8. A method according to any of the preceding claims and wherein said classifying comprises using signal strength classification.
9. A method according to any of the preceding claims, and wherein said obtaining at least one three-dimensional representation comprises obtaining at least one three-dimensional representation of an area which is larger than said region.
10. A method according to any of the preceding claims and wherein said obtaining comprises loading said at least one three-dimensional representation into said GNSS receiver in the form of a software module.
11. A method according to claim 10 and wherein said loading comprises repeatedly loading said at least one three-dimensional representation into said GNSS receiver at a rate of at least once a day.

12. A method according to any of claims 10-11 and wherein said loading comprises loading said at least one three-dimensional representation using at least one wireless communication method.
13. A method according to any of the preceding claims and wherein at least one of said defining a three-dimensional shading representation and said defining a shading surface is carried out substantially in real time.
14. A method according to claim 13 and wherein said defining is by said GNSS receiver.
15. A method according to claim 13 and wherein at least one of said defining a three-dimensional shading representation and said defining a shading surface is carried out by a server, external to said GNSS receiver, and at least one of said three-dimensional shading representation and said shading surface is loaded from said server into said GNSS receiver using at least one wireless communication method.
16. A method according to any of the preceding claims and wherein at least one of said defining a three-dimensional shading representation and said defining a shading surface is in advance of said classification of said second plurality of GNSS satellites, in a device external to said GNSS receiver.
17. A method according to claim 16 and wherein at least one of said defining a three-dimensional shading representation and said defining a shading surface comprises loading at least one of said three-dimensional shading representation and said shading surface from said device external to said GNSS receiver into said GNSS receiver as a data module.
18. A method according to any of the preceding claims, and wherein at least one of said defining a three-dimensional shading representation and said defining a shading surface comprises recalculating at least one of said three-dimensional shading representation and said shading surface at a rate not slower than every 30 seconds based on changes to ephemeris data of said satellite.



19. A method according to any of the preceding claims and wherein said defining a three-dimensional shading representation includes defining at least one border subregion.
20. A method according to claim 19 and wherein said defining at least one border subregion comprises defining said at least one border subregion to lay along said shading surface corresponding to said three-dimensional shading representation.
21. A method according to any of the preceding claims and wherein said eliminating comprises:
  - defining a set of surface inequalities, each corresponding to a constraint defined by one of said shading surfaces; and
  - finding a solution to said set of surface inequalities, which solution comprises said identifying said position.
22. A method according to claim 21 and wherein said finding a solution comprises finding a solution which satisfies only some of the inequalities in said set of surface inequalities.
23. A method according to claim 22 and wherein said finding a solution comprises finding a solution which satisfies a maximal number of the inequalities in said set of surface inequalities.
24. A method according to claim 22 and wherein said finding a solution comprises:
  - assigning a confidence value to each inequality in said set of surface inequalities; and
  - finding a solution which maximizes the confidence of satisfied surface inequalities of said set of surface inequalities.
25. A device for calculating the position of a GNSS (Global Navigation Satellite System) receiver, comprising:
  - a signal receiver configured to receive a plurality of signals from a first plurality of GNSS satellites;
  - a region-calculating module configured to calculate a region in which a GNSS receiver is located based on at least some of said received signals;
  - a satellite classification module, configured to, for each satellite in a second plurality of GNSS satellites, classify whether:

said satellite is a line-of-sight (LOS) satellite, having a line of sight to said GNSS receiver; or

said satellite is a non-line-of-sight (NLOS) satellite, not having a line of sight to said GNSS receiver;

a shading representation defining module configured to obtain at least one three-dimensional representation of an area including said region and, for each satellite in said second plurality of GNSS satellites, to use said at least one three-dimensional representation to define a three-dimensional shading representation including at least one illuminated subregion and at least one shaded subregion, such that a GNSS receiver located in said at least one illuminated subregion has a line of sight said satellite and a GNSS receiver located in said at least one shaded subregion does not have a line of sight to said satellite;

a shading surface calculating module configured to define, for each three-dimensional shading representation, a shading surface which divides between said at least one illuminated subregion and said at least one shaded subregion, such that said at least one illuminated subregion is located above said shading surface and said at least one shaded subregion is located beneath said shading surface; and

a subregion eliminating module configured, for each satellite in said second plurality of GNSS satellites, to eliminate from said region at least one subregion, thereby to identify a position in which said GNSS receiver is located, wherein:

if said satellite is a LOS satellite, eliminating from said region any portion which is located beneath said shading surface defined for said satellite; and

if said satellite is a NLOS satellite, eliminating from said region any portion which is located above said shading surface defined for said satellite.

26. A device according claim 25 and wherein each satellite in said first plurality of GNSS satellites is located above the horizon relative to said GNSS receiver.

27. A device according to any of claims 25-26 and wherein each satellite in said second plurality of GNSS satellites is located above the horizon relative to said GNSS receiver.

28. A device according any of claims 25-27 and wherein said first plurality of GNSS satellites is included in said second plurality of GNSS satellites.

29. A device according to any of claims 25-28 and wherein said first plurality of GNSS satellites and said second plurality of GNSS satellites comprise the same plurality of GNSS satellites.
30. A device according to any of 25-29 claims and wherein said region-calculating module is configured to use at least some strongest of said received signals to calculate said region in which said GNSS receiver is located.
31. A device according to any of claims 25-30 and also comprising a region testing module, configured to test whether a radius of said region is greater than a predetermined threshold.
32. A device according to any of claims 25-31 and wherein said satellite classification module is configured to use signal strength classification.
33. A device according to any of claims 25-32, and wherein said area is larger than said region.
34. A device according to any of claims 25-33 and wherein said shading representation defining module is configured to obtain said at least one three-dimensional representation by loading said three-dimensional representation into said GNSS receiver in the form of a software module.
35. A device according to claim 34 and wherein said shading representation defining module is configured to repeatedly load said at least one three-dimensional representation into said GNSS receiver at a rate of at least once a day.
36. A device according to any of claims 34-35 and wherein said shading representation defining module is configured to load said at least one three-dimensional representation using at least one wireless communication method.
37. A device according to any of claims 25-36 and wherein at least one of said three-dimensional shading representation and said shading surface is defined substantially in real time.

38. A device according to claim 37 and wherein said shading representation defining module is configured to define said at least one of said three-dimensional shading representation and said shading surface.

39. A device according to claim 37 and also comprising a server, external to said GNSS receiver, said server being configured to define said at least one of said three-dimensional shading representation and said shading surface and to load said at least one of said three-dimensional shading representation and said shading surface into said GNSS receiver using at least one wireless communication method.

40. A device according to any of claims 25-39 and also comprising a shading defining device external to said GNSS receiver, configured to define at least one of said three-dimensional shading representation and said shading surface in advance of said classification of said second plurality of GNSS satellites.

41. A device according to claim 40 and wherein said shading defining device is configured to load said at least one of said three-dimensional shading representation and said shading surface into said GNSS receiver as a data module.

42. A device according to any of claims 25-41, and wherein shading representation defining module is configured to recalculate at least one of said three-dimensional shading representation and said shading surface at a rate not slower than every 30 seconds based on changes to ephemeris data of said satellite.

43. A device according to any of claims 25-42 and wherein said shading representation defining module is also configured to define at least one border subregion.

44. A device according to claim 43 and wherein said at least one border subregion lies along said shading surface corresponding to said three-dimensional shading representation.

45. A device according to any of claims 25-44 and wherein said subregion eliminating module comprises:

an inequality defining module configured to define a set of surface inequalities, each corresponding to a constraint defined by one of said shading surfaces; and

a solution finding module configured to find a solution to said set of surface inequalities, which solution comprises said identifying said position.

46. A device according to claim 45 and wherein said solution finding module is configured to find a solution which satisfies only some of the inequalities in said set of surface inequalities.

47. A device according to claim 46 and wherein said solution finding module is configured to find a solution which satisfies a maximal number of the inequalities in said set of surface inequalities.

48. A device according to claim 46 and wherein said solution finding module is configured to find a solution by assigning a confidence value to each inequality in said set of surface inequalities and finding a solution which maximizes the confidence of satisfied surface inequalities of said set of surface inequalities.

49. A method for creating a three-dimensional representation of terrestrial objects in an urban area, comprising:

obtaining a log file from at least one GNSS receiver, said log file containing information obtained in an urban area;

extracting from said log file a plurality data items, each data item including a timestamp, a position, and a signal strength captured from a GNSS satellite at said position and at said timestamp;

for each of said plurality of data items, classifying whether at said timestamp and at said position:

said satellite is a line-of-sight (LOS) satellite, having a line of sight to said GNSS receiver; or

said satellite is a non-line-of-sight (NLOS) satellite, not having a line of sight to said GNSS receiver; and

using said classification to identify three-dimensional contours of terrestrial objects in said urban area.

50. A method according to claim 49 and wherein said information is obtained along a route taken by said at least one GNSS receiver in said urban area.

51. A method according to any of claims 49-50 and wherein said using said classification comprises:

finding locations in which there is a change in satellite status based on ones of said plurality of data items having consecutive timestamps, wherein said change in satellite status comprises one of a transition from said satellite being a LOS satellite to said satellite being a NLOS satellite and a transition from said satellite being a NLOS satellite to said satellite being a LOS satellite;

defining said locations as contour edge points; and

identifying said three-dimensional contours of said terrestrial objects such that two-dimensional contours of said terrestrial objects are bounded by said contour edge points.

52. A method according to claim 51 and wherein said finding comprises computing a distance function which corresponds to the number of satellites for which there is a change of satellite status at said locations.

53. A method according to claim 52 and wherein said computing a distance function comprises computing a weighted distance function, wherein the contribution to said weighted distance function of a change of satellite status for a satellite at a high angle with respect to said GNSS receiver is greater than the contribution of a change of satellite status for a satellite at a low angle with respect to said GNSS receiver.

54. A method according to either of claims 52 and 53 and wherein said defining comprises defining as said contour edge points ones of said locations for which said distance function is greater than a predetermined threshold.

55. A method according to any of claims 51-54 and also comprising, following said finding locations and prior to said defining said locations as contour edge points, eliminating ones of said locations for which there is a high probability of error.

56. A method according to any of claims 51-55 and wherein said two-dimensional contours comprise general polygons.

57. A method according to any of claims 51-56 and wherein said two-dimensional contours include curved lines.

58. A method according to any of claims 49-57 and wherein said using said classification comprises:

for each of said plurality of data items, defining a three-dimensional vector between said position and a position of said satellite based on ephemeris data of said satellite at said timestamp;

labeling each vector of said three-dimensional vectors as a LOS vector if said satellite in said data item corresponding to said vector is classified as a LOS satellite, and as a NLOS vector if said satellite is classified as a NLOS satellite; and

defining the height of said three-dimensional contours to satisfy at least some of a plurality of constraints based on said plurality of three-dimensional vectors, wherein said height of said three-dimensional contours is defined to obstruct some of said three-dimensional vectors labeled as NLOS vectors, and not to obstruct some others of said three-dimensional vectors labeled as LOS vectors.

59. A method according to claim 58 and wherein said defining said height comprises defining said height to satisfy a maximal number of said plurality of constraints.

60. A method according to claim 58 and wherein said defining said height comprises:

assigning a weight to each of said plurality of constraints; and

computing said height to maximize the weight of satisfied ones of said plurality of constraints.

61. A method according to any of claims 49-60 and wherein said classifying comprises using signal strength classification.

62. A device for creating a three-dimensional representation of terrestrial objects in an urban area, comprising:

a data obtaining module configured to obtain a log file from at least one GNSS receiver, said log file containing information obtained in an urban area;

a data extractor configured to extract from said log file a plurality data items, each data item including a timestamp, a position, and a signal strength captured from a GNSS satellite at said position and at said timestamp;

a classification module, configured to, for each of said plurality of data items, classify whether at said timestamp and at said position:

said satellite is a line-of-sight (LOS) satellite, having a line of sight to said GNSS receiver; or

said satellite is a non-line-of-sight (NLOS) satellite, not having a line of sight to said GNSS receiver; and

a contour identification module configured to use said classification to identify three-dimensional contours of terrestrial objects in said urban area.

63. A device according to claim 62 and wherein said data obtaining module is configured to obtain information captured along a route taken by said at least one GNSS receiver in said urban area.

64. A device according to any of claims 62-63 and wherein said contour identification module comprises:

a location finding module configured to find locations in which there is a change in satellite status based on ones of said plurality of data items having consecutive timestamps, wherein said change in satellite status comprises one of a transition from said satellite being a LOS satellite to said satellite being a NLOS satellite and a transition from said satellite being a NLOS satellite to said satellite being a LOS satellite and to define said locations as contour edge points; and

a two-dimensional contour identification module configured to identify said three-dimensional contours of said terrestrial objects such that two-dimensional contours of said terrestrial objects are bounded by said contour edge points.

65. A device according to claim 64 and wherein said location finding module is configured to compute a distance function which corresponds to the number of satellites for which there is a change of satellite status at said locations.

66. A device according to claim 65 and wherein said location finding module is configured to compute a weighted distance function, wherein the contribution to said weighted distance



function of a change of satellite status for a satellite at a high angle with respect to said GNSS receiver is greater than the contribution of a change of satellite status for a satellite at a low angle with respect to said GNSS receiver.

67. A device according to either of claims 65 and 66 and wherein said location finding module is configured to define as said contour edge points ones of said locations for which said distance function is greater than a predetermined threshold.

68. A device according to any of claims 64-67 and wherein said location finding module is also configured to eliminate ones of said locations for which there is a high probability of error.

69. A device according to any of claims 64-68 and wherein said two-dimensional contours comprise general polygons.

70. A device according to any of claims 64-69 and wherein said two-dimensional contours include curved lines.

71. A device according to any of claims 62-70 and wherein said contour identification module comprises:

- a vector defining module configured, for each of said plurality of data items, to define a three-dimensional vector between said position and a position of said satellite based on ephemeris data of said satellite at said timestamp;

- a vector labeling module configured to label each vector of said three-dimensional vectors as a LOS vector if said satellite in said data item corresponding to said vector is classified as a LOS satellite, and as a NLOS vector if said satellite is classified as a NLOS satellite; and

- a height defining module configured to define the height of said three-dimensional contours to satisfy at least some of a plurality of constraints based on said plurality of three-dimensional vectors, wherein said height of said three-dimensional contours is defined to obstruct some of said three-dimensional vectors labeled as NLOS vectors, and not to obstruct some others of said three-dimensional vectors labeled as LOS vectors.

72. A device according to claim 71 and wherein said height defining module is configured to define said height to satisfy a maximal number of said plurality of constraints.

73. A device according to claim 71 and wherein said height defining module is configured to assign a weight to each of said plurality of constraints and to compute said height to maximize the weight of satisfied ones of said plurality of constraints.

74. A device according to any of claims 62-73 and wherein said classification module is configured to use signal strength classification.

75. A method for transmitting a three-dimensional representation of an area, to a GNSS receiver, for improving calculation, comprising:

at a fixed location, calculating a three-dimensional representation of an area;  
receiving from a GNSS receiver an indication of a location of the GNSS receiver, said location being included in said area; and  
transmitting at least a portion of said three-dimensional representation of said area from said fixed location to said GNSS receiver, said portion including a three-dimensional representation of said location.

76. A method according to claim 75 and wherein said calculating a three-dimensional representation comprises calculating a shading three-dimensional representation of said area.

77. A method according to any of claims 75-76 and wherein said calculating comprises repeatedly calculating said three-dimensional representation of said area, at least once every 24 hours.

78. A method according to any of claims 75-77 and wherein said transmitting comprises using a wireless communication method to transmit said three-dimensional representation of said area.

79. A method according to any of claims 75-78 and wherein said transmitting comprises transmitting said three-dimensional representation as a software module.

80. A method according to any of claims 75-79 and wherein said calculating comprises calculating said three-dimensional representation at a first rate and transmitting said three-dimensional representation at a second rate.

81. A method according to claim 80 and wherein said first rate is different from said second rate.

82. A method according to either of claims 80 and 81 and wherein said second rate is dependent on a processing power restrictions of said GNSS receiver.

83. A method according to any of claims 80-82 and wherein said second rate is dependent on a transmission bandwidth.

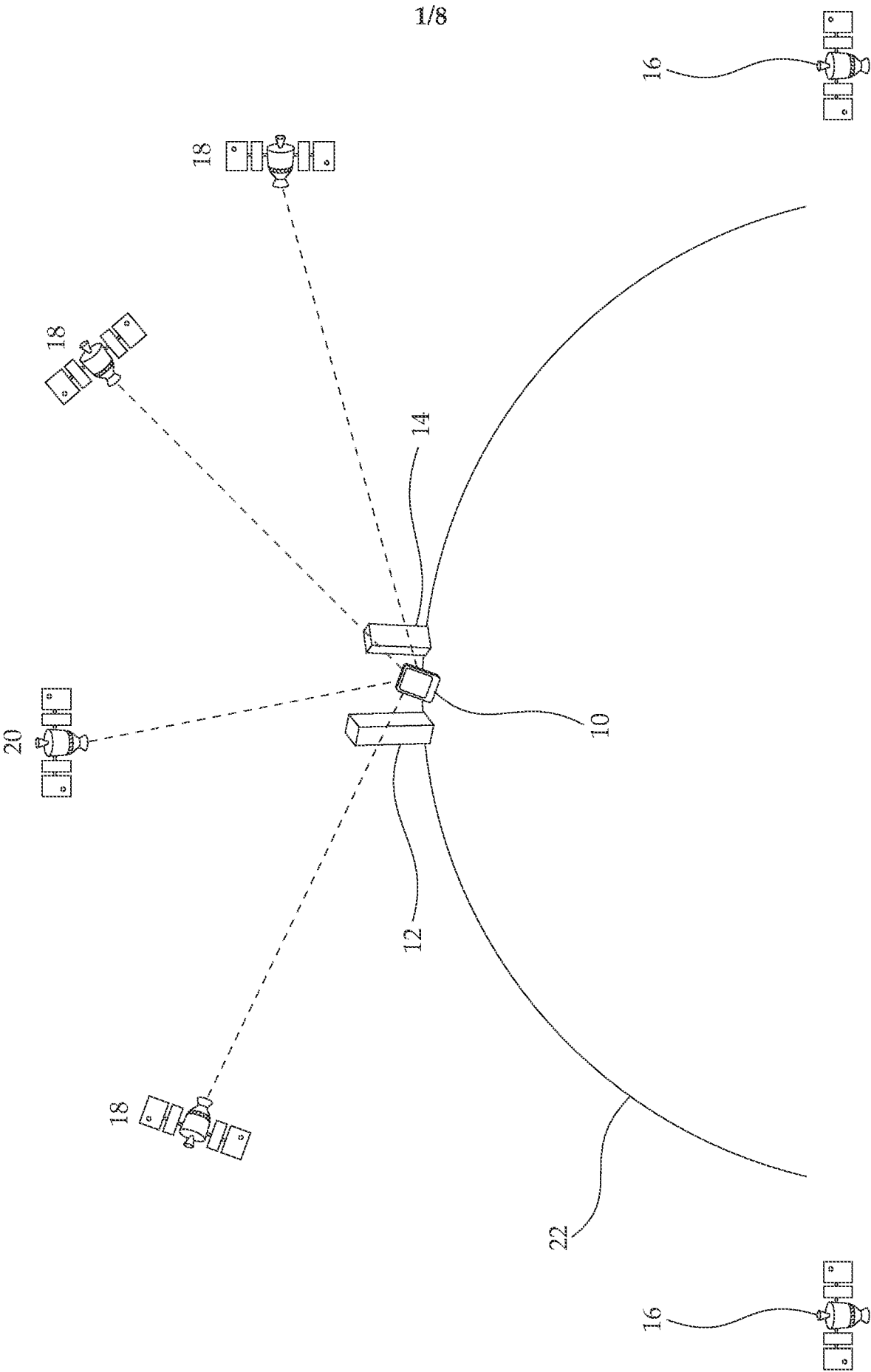


FIGURE 1

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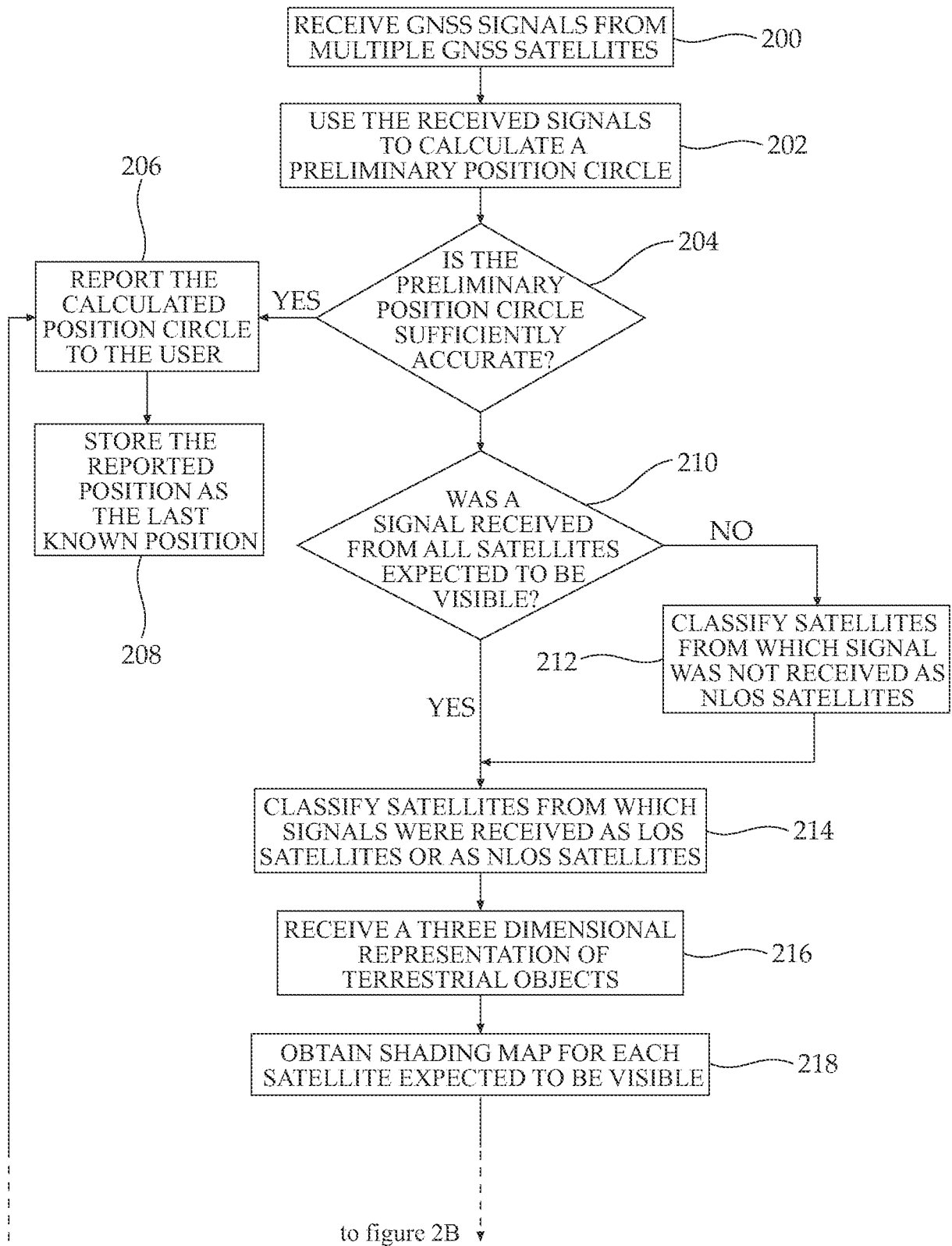


FIGURE 2A

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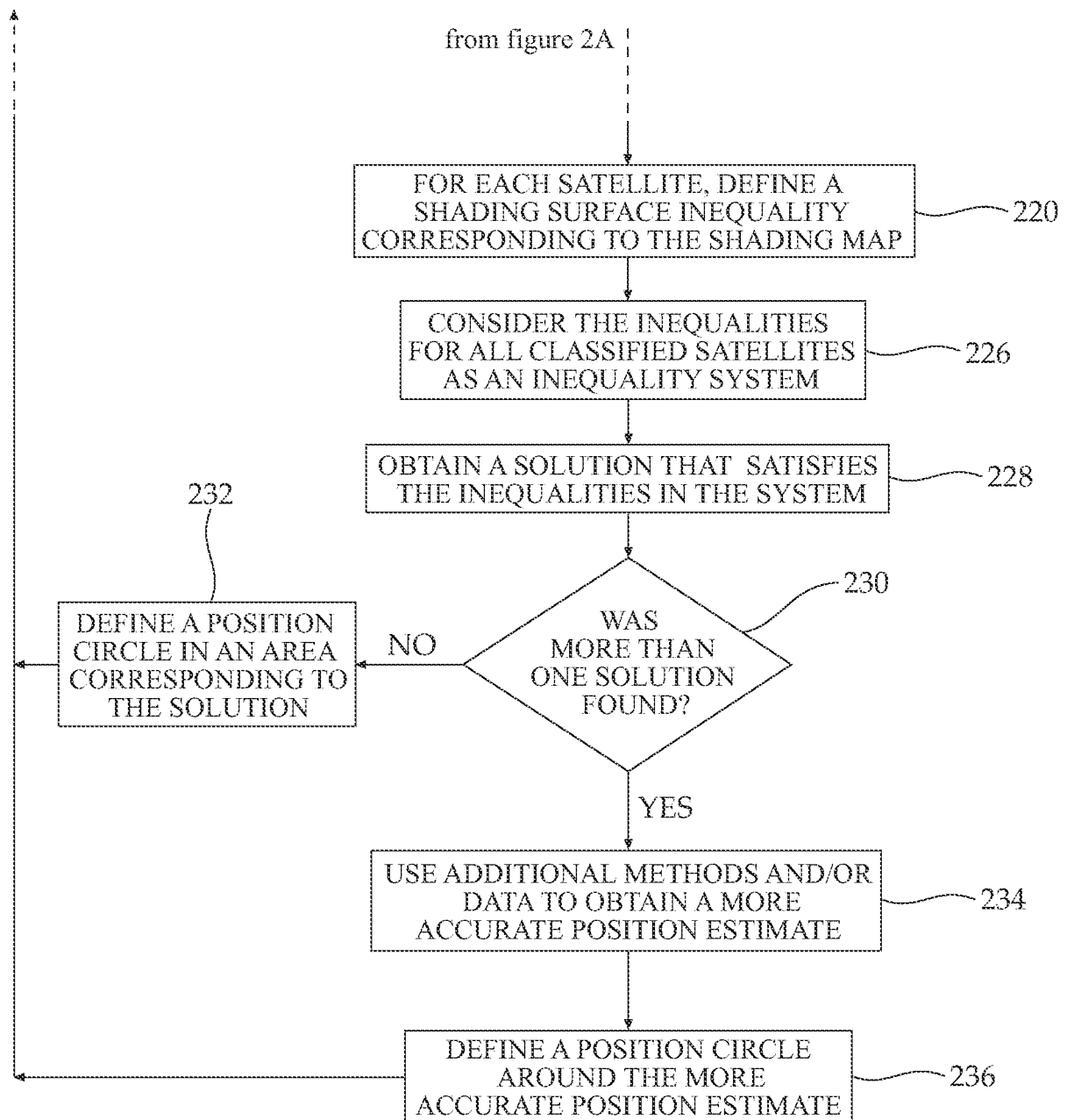
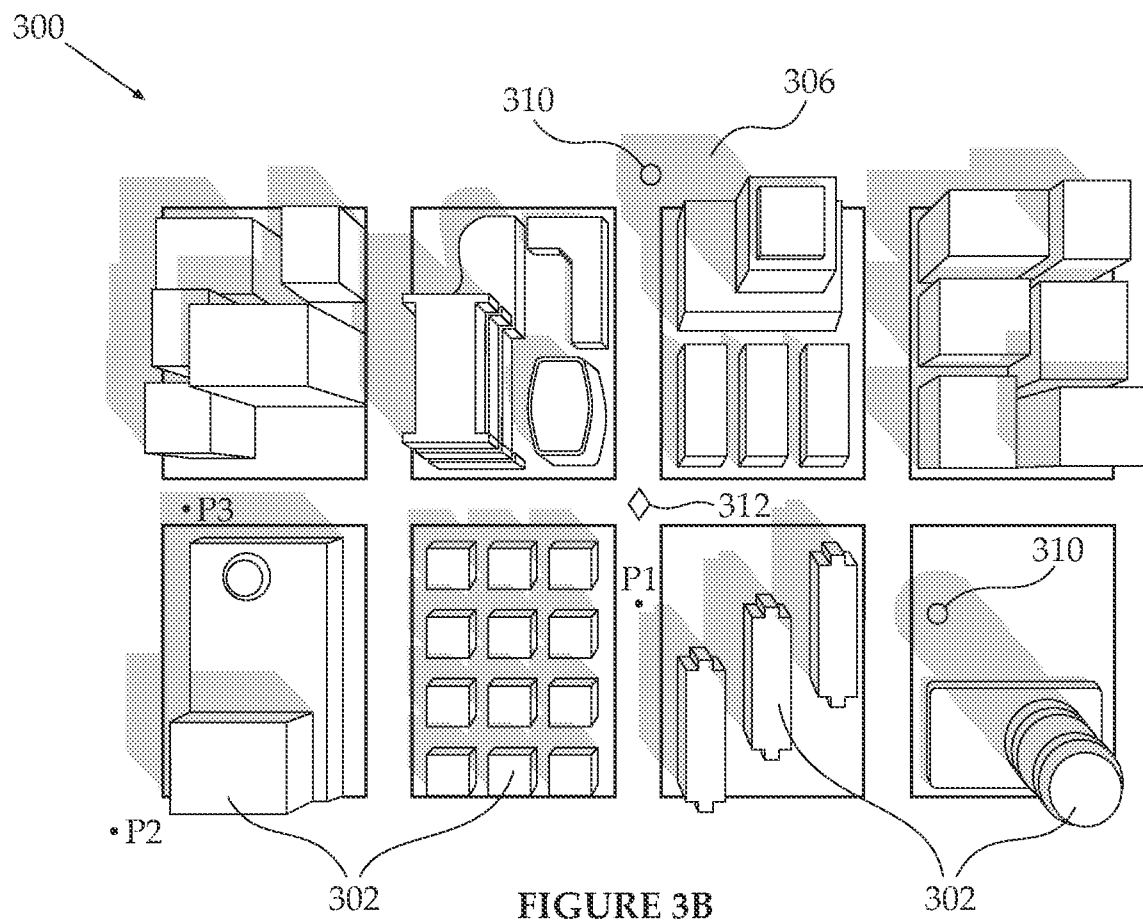
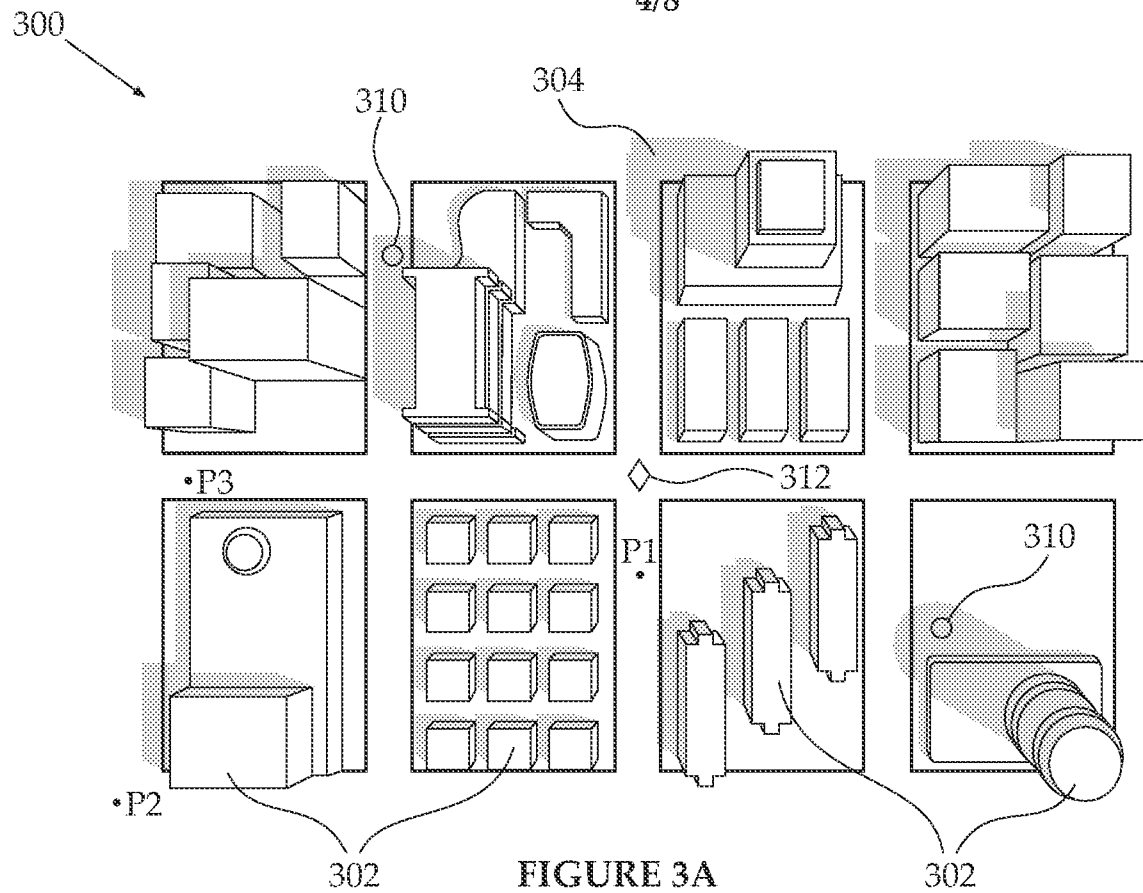


FIGURE 2B

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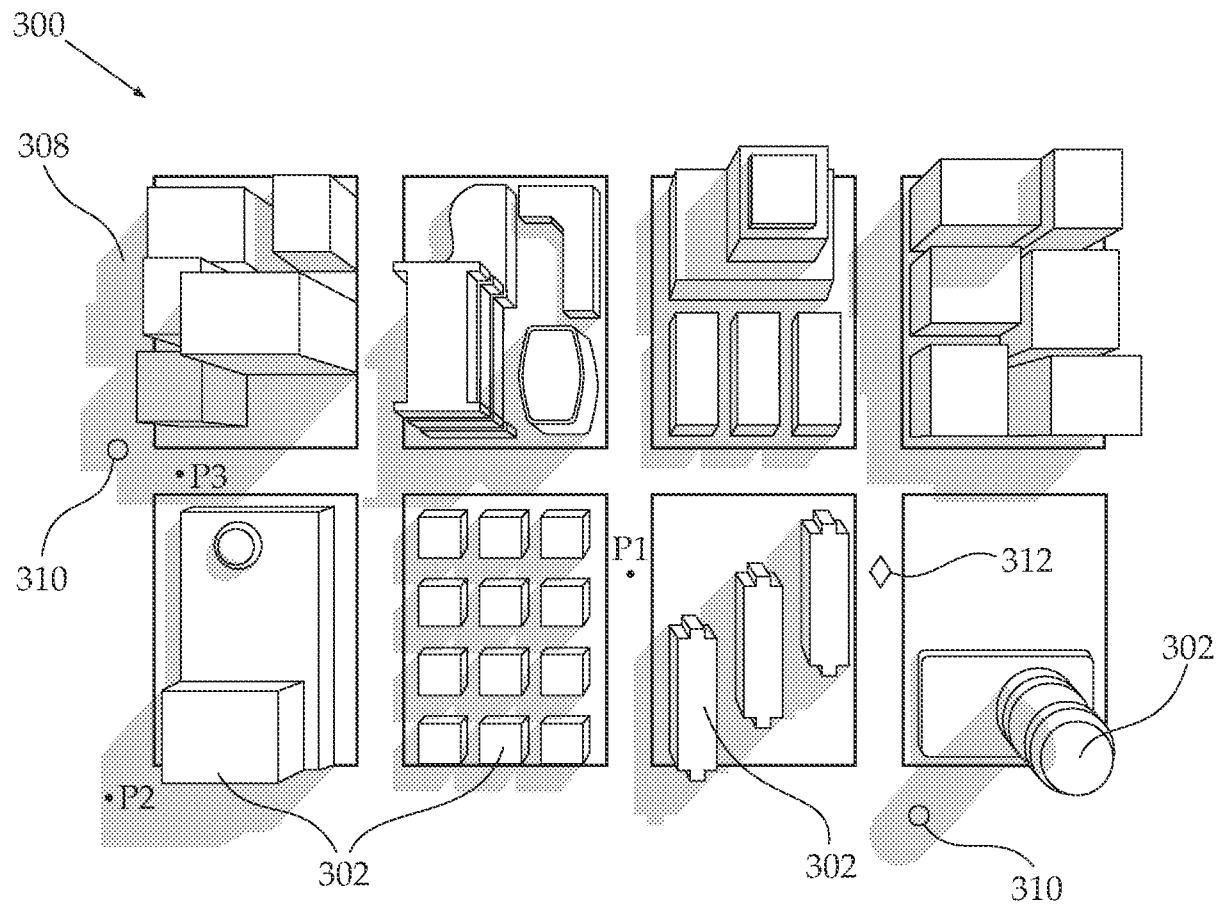


FIGURE 3C



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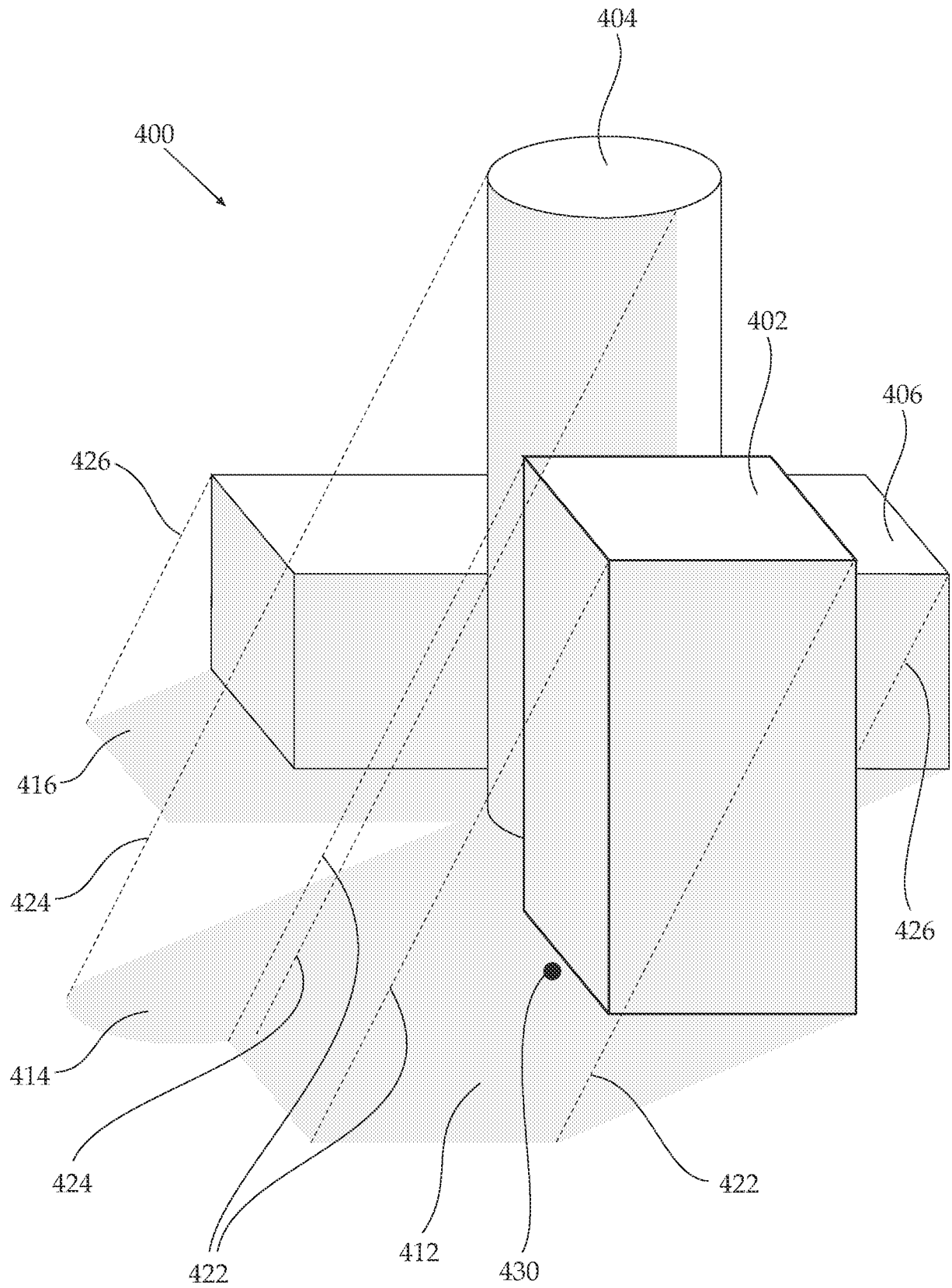


FIGURE 4

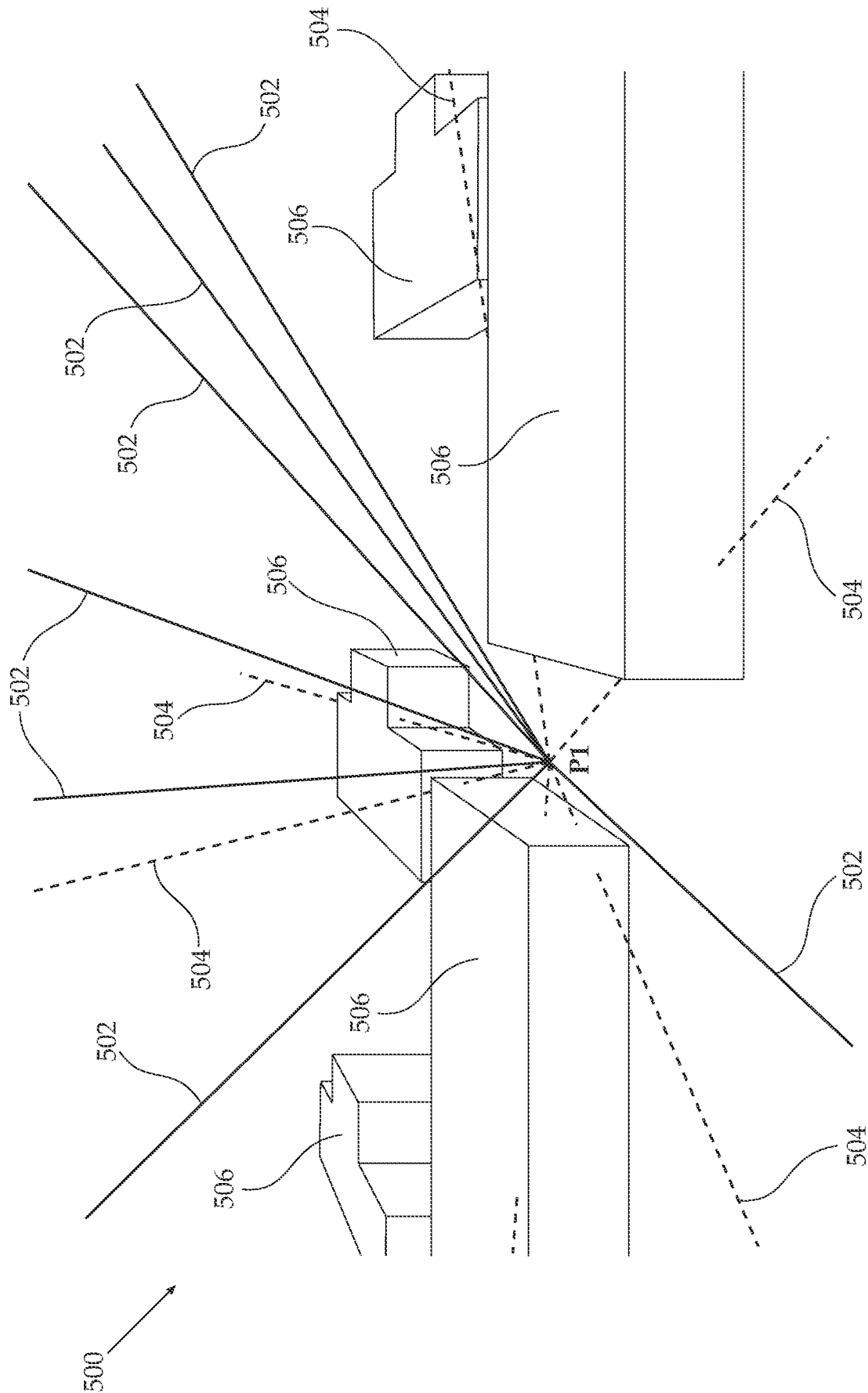


FIGURE 5

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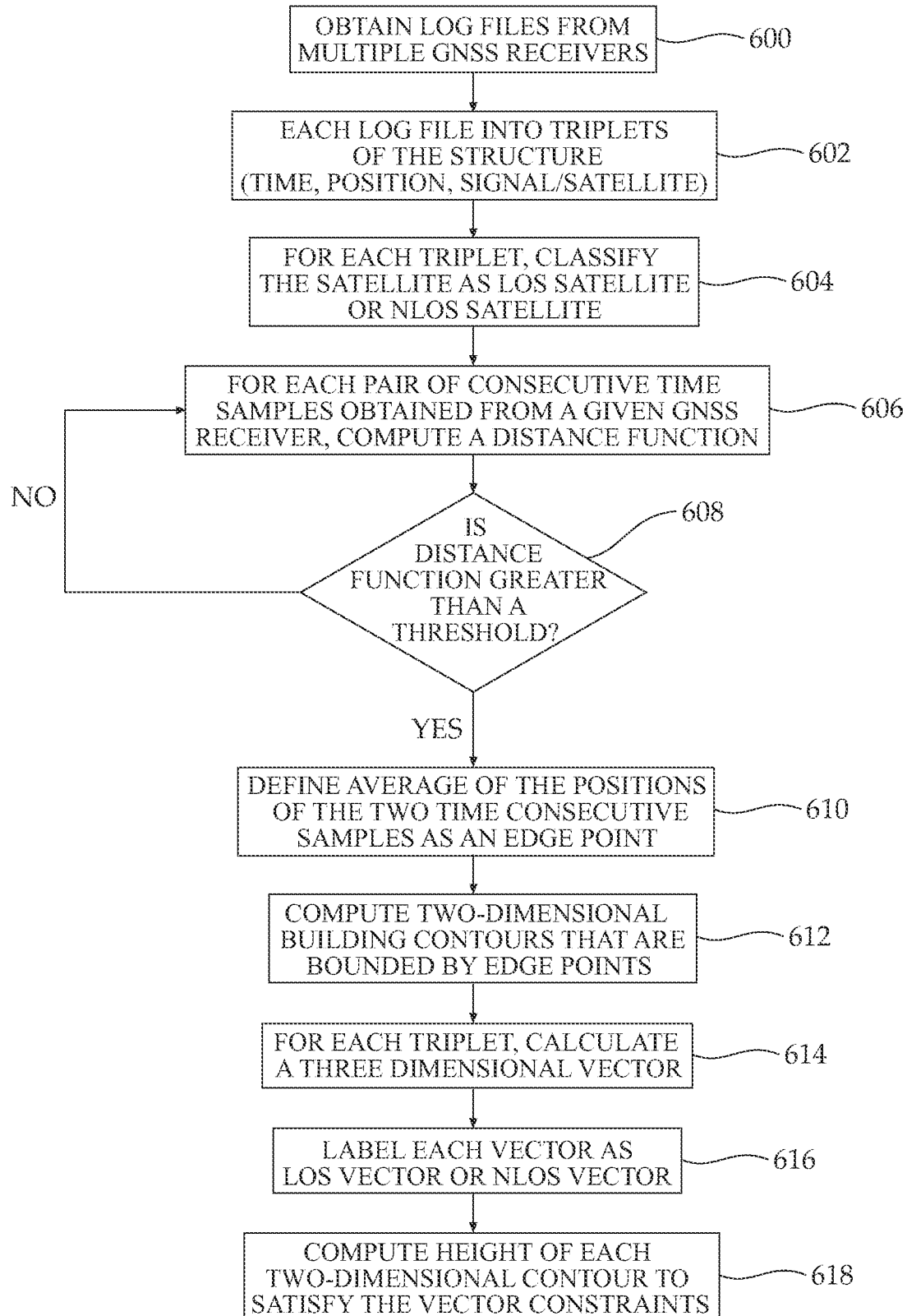


FIGURE 6