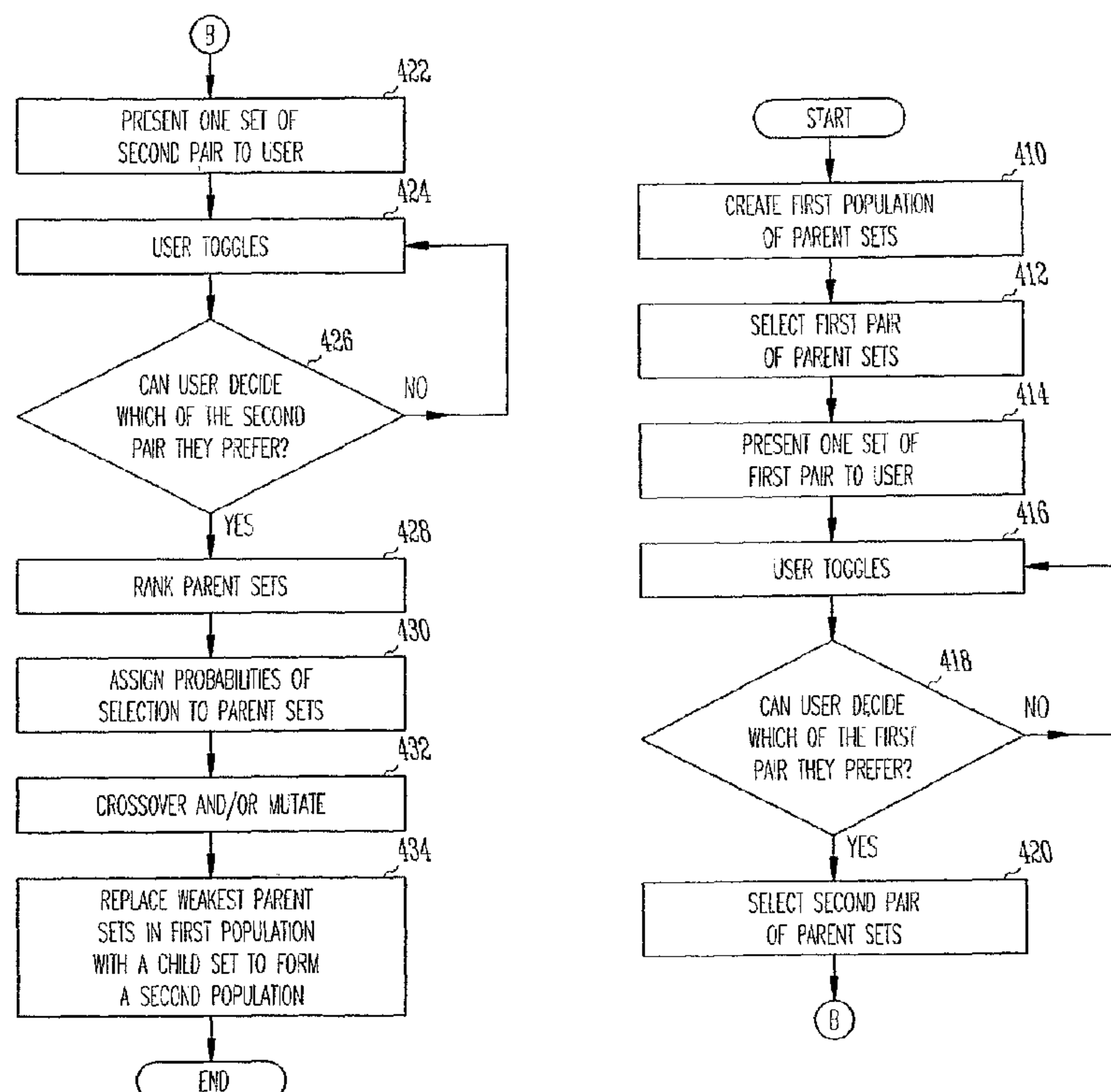




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(57) **Abrégé/Abstract:**

A field ready, unsupervised-use ready, method and apparatus for audio fitting a hearing aid is described in a hand held configuration having paired comparison (hearing selections) stored in and derivable from a memory therein. The paired comparisons are presented one at a time to a user and a preferred selection for each paired comparison is made by a select indicator after the user toggles back and forth between the selections for as many times necessary in determining their preferences. A genetic algorithm converges all the preferences upon a single solution. Crossover and mutation genetic algorithm operators operate on a linear range of indexes representative of parametric values of the pairs. A fully integrated hearing aid having all the above described features incorporated therein is also presented.

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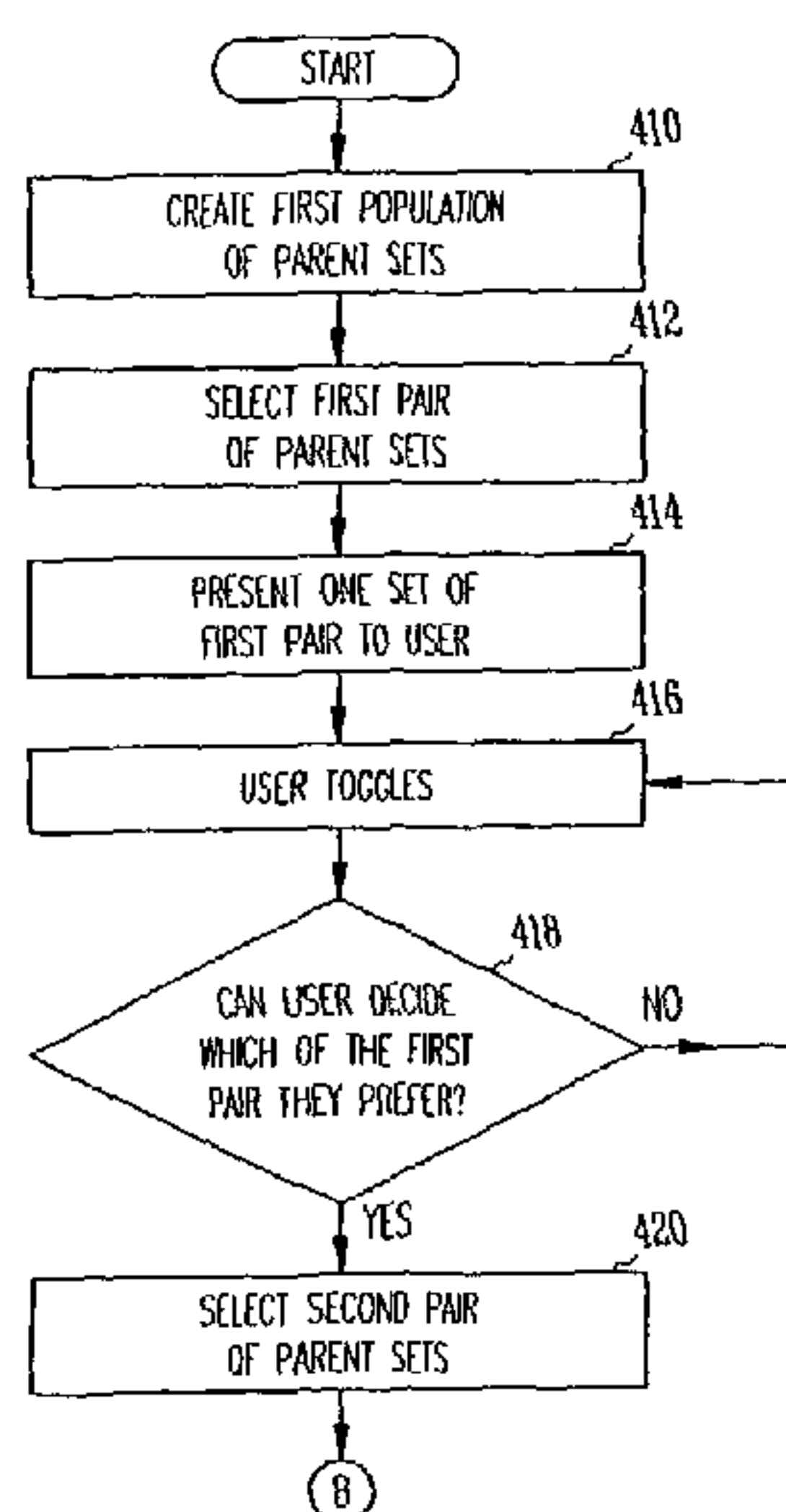
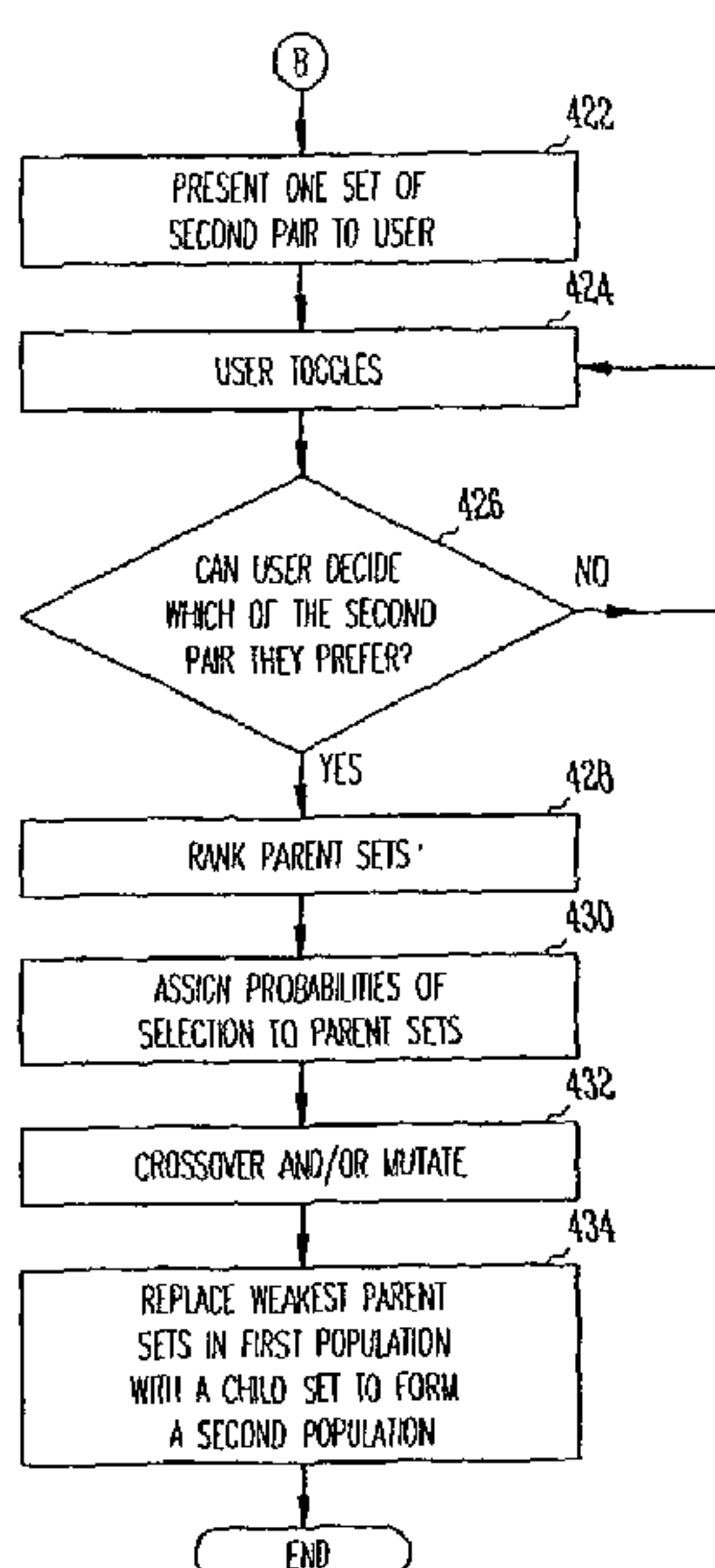
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(54) Title: HEARING AIDS AND METHODS AND APPARATUS FOR AUDIO FITTING THEREOF



(57) **Abstract:** A field ready, unsupervised-use ready, method and apparatus for audio fitting a hearing aid is described in a hand held configuration having paired comparison (hearing selections) stored in and derivable from a memory therein. The paired comparisons are presented one at a time to a user and a preferred selection for each paired comparison is made by a select indicator after the user toggles back and forth between the selections for as many times necessary in determining their preferences. A genetic algorithm converges all the preferences upon a single solution. Crossover and mutation genetic algorithm operators operate on a linear range of indexes representative of parametric values of the pairs. A fully integrated hearing aid having all the above described features incorporated therein is also presented.

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HEARING AIDS AND METHODS AND APPARATUS FOR AUDIO FITTING THEREOF

Field of the Invention

5 The present invention relates to hearing aids. In particular, it relates to methods and apparatus for efficaciously audio fitting them. More broadly, however, the present invention relates to perceptually tuning any system, such as hearing aids. Even more broadly, the present invention relates to genetic algorithms utilizing user input selection from paired comparisons for performing the tuning. Still even more
10 broadly, the present invention relates to genetic algorithm crossover and mutation operators for use in a genetic algorithm that neither operates directly on a parametric value nor a string of bits representing the parametric value.

Background of the Invention

15 Many fields encounter problems associated with perceptually tuning a system. For example, in perceptually tuning or “fitting” a hearing aid, antiquated methods subjected a single sensorineurally impaired user to many and various audio-related settings of their hearing aid and, often via technical support from an audiologist, individually determined the preferred settings for that single user. This
20 approach, however, has proven itself lacking in universal applicability.

 Thus, prescriptive fitting formulas have evolved whereby large numbers of users can become satisfactorily fit by adjusting the same hearing aid device. With the advent of programmable hearing aids, this approach has become especially more viable. This approach is, however, still too general because individual preferences
25 are often ignored. There currently exists no accepted selection strategy that provides a structured and efficient approach to incorporating individual preferences into hearing aid fittings.

 In one particular hearing aid fitting selection strategy, paired comparisons were used. In this strategy, users were presented with a choice between two actual
30 hearing aids from a large set of hearing aids and asked to compare them in an iterative round robin, double elimination tournament or modified simplex procedure

until one hearing aid “winner” having optimum frequency-gain characteristics was converged upon. These uses of paired comparisons, however, are extremely impractical in time and financial resources. Moreover, such strategy cannot easily find implementation in an unsupervised home setting by an actual hearing aid user.

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In a more recent, and very limited selection strategy, genetic algorithms were blended with user input to achieve a hearing aid fitting. As is known, and as its name implies, genetic algorithms, first introduced by John H. Holland, are a class of algorithms modeled upon living organisms’ ability to ensure their evolutionary success via natural selection. In natural selection, the fittest organisms survive while the weakest are killed off. The next generation of organisms (children) are, thus, offspring of the fittest previous generation (parents). The algorithms also provide for mutations as insurance against the development of a relatively unchanging population incapable of continued evolution.

10

In breeding children or offspring in a genetic algorithm, “crossover” operators are applied to parent genes. In essence, two parent bit strings (ones and zeroes, for example) from the algorithm are crossed at a crossover point and the children are given attributes of each parent. Mutation operators are also applied to a relatively smaller number of parent bit strings, typically by replacing ones with zeroes and vice versa. Both crossover and mutation closely model biological behavior where parent chromosomes line up and crossover thereby swapping portions of their genetic code or become mutated.

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The determination of which children are the results of which parents, how many children are produced, how many children survive, how long parents survive, how many mutations per children are created and other similar algorithm manipulations are functions of each particular genetic algorithm and vary, probably, as widely as the number of genetic algorithms in use.

25

In this particular hearing aid selection strategy using genetic algorithms, human subjects were asked to rank 20 hearing selections on a scale of 1 to 5. Then, through a series of genetic algorithm computations, a winning hearing selection was converged upon.

30

With absolute scaling approaches of this type, however, humans are generally not able to maintain the same response criteria over such a wide number of listening trials. For example, what a subject might record as a 2 for the first selection might not be the same 2 recorded for the twentieth selection. In other words, the scaling makes the comparison selection too complex. Moreover, and as with all hearing aid fitting selection strategies, this approach is unrealistic for hearing aid users to implement in their home in an unsupervised setting.

In a broader setting, genetic algorithms have also seen application in other perceptual tuning environments. For example, they have been used to (interactively with human subjects) tune simulated automobile wind noise to the subject's satisfaction and to successfully fit head-related transfer functions. These activities, like hearing aid fittings, take place in research settings and cannot, even if it were desirable, be readily performed in unsupervised field settings.

In a still broader setting, some genetic algorithm operators (crossover and mutation), have typically ineffectively evolved an organisms' population because of quickness, slowness, unstableness or some other poorly performing process in the operators. This is because the operators themselves typically operate directly on bit strings or directly on parameters having a wide, varied and non-linear range.

Accordingly, the art needs a better and more simple selection strategy for fitting or tuning hearing aids to individual users' preferred settings. Preferably, it needs an unsupervised field setting implementation. In a broader setting, the art needs better genetic algorithms for perceptually tuning a system having many interacting parameters. Still even more broadly, the art needs better genetic algorithm operators that serve to better evolve populations.

Summary of the Invention

The above-mentioned and other problems become solved by applying the apparatus, method and system principles and teachings associated with the hereinafter described hearing aids and audio fitting thereof. Even further, by applying the principles and teachings described for genetic algorithm operators,

better genetic algorithms can be applied to perceptually tuning any system, such as a radio, a hearing aid, a personal data or digital assistant device, etc.

5 In one embodiment, a field ready, unsupervised-use ready, method and apparatus for fitting a hearing aid is described in a hand held configuration having paired comparisons (hearing selections) stored in and derivable from a memory therein. The paired comparisons are presented one at a time to a user and a preferred selection for each paired comparison is made by a select indicator after the user toggles back and forth between the selections for as many times necessary in determining his or her preferences. A genetic algorithm converges all the
10 preferences upon a single solution. Crossover and mutation genetic algorithm operators operate on a linear range of indexes representative of parametric values of the pairs. A fully integrated hearing aid having all the above described features incorporated therein is also presented.

15 In still another embodiment, a genetic algorithm for perceptually tuning a system is presented that converges upon a solution set from a plurality of parent and child sets in first and second populations that were presented to a user in a paired comparison format.

20 In still other embodiments, crossover and mutation genetic algorithm operators are described that neither operate directly on a parametric value nor a string of bits representing the parametric value, but on a linear range of indexes representative of parametric values used by a parent from a population.

25 These and other embodiments, aspects, advantages, and features of the present invention will be set forth in part in the description that follows, and in part will become apparent to those skilled in the art by reference to the following description of the invention and referenced drawings or by practice of the invention. The aspects, advantages, and features of the invention are realized and attained by means of the instrumentation, procedures, and combinations particularly pointed out in the appended claims.

Brief Description of the Drawings

Figure 1A is a diagrammatic view of a perceptual tuning system in accordance with the teachings of the present invention showing a hearing aid user and apparatus useful in an audio fitting thereof;

5 Figure 1B is a diagrammatic view of a perceptual tuning system in accordance with the teachings of the present invention showing a hearing aid user and apparatus useful in an audio fitting thereof in a wireless embodiment;

Figure 2 is a block diagram in accordance with the teachings of the present invention for the system of Figure 1 (Figure 1A or Figure 1B);

10 Figure 3A is a diagrammatic view in accordance with the teachings of the present invention showing a first population comprised of a plurality of parent sets;

Figure 3B is a diagrammatic view in accordance with the teachings of the present invention showing a genetic algorithm crossover operator;

15 Figure 3C is a diagrammatic view in accordance with the teachings of the present invention showing a genetic algorithm mutation operator;

Figure 3D is a diagrammatic view in accordance with the teachings of the present invention showing a creation of a mutation set for the mutation operator of Figure 3C;

20 Figure 3E is a diagrammatic view in accordance with the teachings of the present invention showing a second population comprised of a plurality of parent and child sets;

Figure 4A is a first portion of a flow diagram in accordance with the teachings of the present invention showing paired comparisons presented to a user for selection thereof;

25 Figure 4B is a second portion of a flow diagram in accordance with the teachings of the present invention showing paired comparisons presented to a user for selection thereof; and

Figure 5 is a block diagram of an alternate embodiment of a perceptual tuning system in accordance with the teachings of the present invention.

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Detailed Description of the Preferred Embodiments

In the following detailed description of the preferred embodiments, reference is made to the accompanying drawings which form a part hereof, and in which is shown by way of illustration, specific embodiments in which the inventions may be practiced. These embodiments are described in sufficient detail to enable those skilled in the art to practice the invention, and it is to be understood that other embodiments may be utilized and that process, electrical or mechanical changes may be made without departing from the scope of the present invention.

With reference to Figure 1A, a perceptual tuning system of the present invention is shown generally as 10. The system, as presented in this figure and the remaining description, is in the context of fitting a hearing aid for a sensorineurally impaired user. It will be appreciated, however, that the system may and should be extended to various other environments, such as tuning a radio, a personal data assistant or any of a number of devices requiring such tuning. Thus, the present invention is not expressly limited to a hearing aid fitting unless so defined in the claims.

As illustrated, the system 10 has a user 12 outfitted with a hearing aid 14, an apparatus 16 in a hand held configuration for audio fitting the hearing aid via user selection of paired comparisons stored in and derivable therefrom and a communications link 18 in between. In one embodiment, as depicted by Figure 1B the communications link 18 is a wireless link and the necessary communications hardware are found in apparatus 16 and hearing aid 14 to support the wireless link. Apparatus 16 is a self-contained device ready for field use (e.g., home use) in an unsupervised setting.

It will be further appreciated that the system of Figure 1A (or Figure 1B) is shown as a left hearing aid configuration and one skilled in the art will be readily able to adapt the teachings herein and apply them without undue experimentation to right hearing aid embodiments and to systems having both left and right hearing aid embodiments. As such, the claims of the present invention are not to be construed as limited to a single, left hearing aid configuration.

It will be even further appreciated that hearing aids, although always having analog components, such as microphones and receivers, are generally referred to according to their primary mode of signal processing (analog processing or digital signal processing (DSP)) and can be of any type as described herein. The claims, therefore, are not to be construed as requiring a specific type of hearing aid.

Still further, although not shown, the present invention may find applicability in contexts in which an audiologist uses apparatus 16 to assist user 12 in fitting hearing aid 14.

With reference to Figure 2, the apparatus 16 and hearing aid 14 of system 10 are representatively shown in block diagram format and will be described first in terms of their electro-mechanical interconnections. Thereafter, and with simultaneous reference to other figures, the apparatus and hearing aid of system 10 will be described in functional detail. In the embodiment shown, apparatus 16 includes fully integrated user interface 20, processor 22 and power supply 23 for providing necessary voltage and currents to the user interface and processor. In an alternative embodiment, the apparatus 16 is separated into discrete components and/or discrete/integrated hybrids connected by appropriate communications links between the functional blocks with common or discrete internal or external power supplies.

User interface 20 may include volume switches 24, 26, respectively, for increasing (+) or decreasing (-) a volume of the apparatus 16 as appropriate. Select indicator 28 is used to indicate user preference between paired comparisons. Toggle device 30 allows the user to toggle back and forth between paired comparisons as often times as necessary before indicating their preference. The actual presentment of paired comparisons and indication of preference will be described in much more detail below.

The volume switches 24, 26, the select indicator 28 and toggle device 30 may be any of a variety of well known integrated or discrete switches, slides, buttons, etc. They preferably include electro-mechanical switches that send electrical signals in response to a mechanical manipulation thereof. They preferably

have appropriate size and shape to enable users to comfortably and intuitively manipulate them with very little manual dexterity.

In another embodiment, the toggle device 30 is not a mechanical device to be manipulated by a user but a software algorithm stored in processor memory that automatically toggles between paired comparisons according to a preferred timing schedule.

Visual indicators 32 of varying number, color and pattern are also preferably provided in the form of lights, such as light-emitting diodes (LED) to provide immediate visual feedback to the user upon manipulation of one of the user inputs.

Connected to the user interface 20 is processor 22 having a central processing unit 34, preferably a DSP with internal on-chip memory, read-only memory (ROM) 36 and flash memory 42 for use as a logging space of the user inputs from user interface 20.

ROM 36 preferably includes at least two algorithms. Hearing aid algorithms 38 and genetic algorithms 40.

In a fashion similar to that of the apparatus itself, it should be appreciated that processor 22 may be a fully integrated device or comprised of discrete components or a discrete/integrated hybrid and that all such embodiments are embraced herein.

The foregoing apparatus 16 is connected at one end of the communications link 18. At the other end is the hearing aid 14. In one embodiment, the communications link 18 is a set of wire(s). In an alternate embodiment, the link 18 is wireless. The link 18 in such embodiments includes, but is not limited to, any well known or hereinafter developed communications scheme, modulated or unmodulated technologies, including, but not limited to, wireless radio frequencies, infrared transmitter/receiver pairs, Bluetooth technologies, etc. In such embodiments, suitable hardware/software processing devices would be contained in the apparatus 16 and the hearing aid 14.

As shown, the hearing aid 14 contains an initial prescription setting 48, a microphone 44, a receiver 46 and a reset mechanism 50. It will be appreciated the

hearing aid also contains other mechanisms that are not shown but are well known to those skilled in the art, such as a power supply and a signal processor.

In one embodiment the apparatus 16 and hearing aid 14 are discrete components. In another embodiment, the entire contents of apparatus 16 and hearing aid 14 are fully integrated into one single hearing aid package 52.

Before describing the functional operation of the apparatus 16 together with hearing aid 14, or, alternatively, completely integrated hearing aid package 52, some words and nomenclature as used throughout this specification are presented. A “parameter” as used herein relates to a characteristic element of the system 10 that can take on a discrete value. In some embodiments, the discrete value is selected from one of a range of values. In one embodiment, for example, a parameter of Filter Length, L , (in # of filter taps) the discrete parametric value is 9. It is understood that the parameter L is not limited to a particular value of 9 and can be another number. The parameter L is capable of being any of the discrete values, including, but not limited to, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 13, 16, 20, 25, 32, 40, etc. In one embodiment, the filter length L may be as short as 1 (mere scaling of the input) and as long 256. The parameter L may be a discrete value taken from a range of countable numbers, for example, $\{3, 4, 5, 6, \dots, N \text{ or Infinity}\}$. The parameter L may also be a discrete value taken from an irregular set, such as $\{8, 10, 13, \dots, 32, 40\}$, for example. Other range types and ranges are possible, and the examples given here are not intended in a limited or exclusive sense. Typically what constrains the upper limit is the size of available memory, processing speed and the ability of a user to discern differences in that many filter taps. Some particular examples of parameters for perceptually tuning a hearing aid may be, but are not limited to, any of the following terms well known to research audiologists and audio processing engineers skilled in the art: gain, compression ratio, expansion ratio, frequency values, such as sampling and crossover frequencies, time constant, filter length, compression threshold, noise reduction, feedback cancellation, output limiting threshold, compression channel crossover frequencies, directional filter coefficients, constrained representations of large parameter groupings, and other known or hereinafter considered parameters. A “set” as used herein is one or more

parameters. A “population” is a plurality of sets. Capital letters A, B, C, D, . . . X, . . . etc., having subscripts or superscripts or both therewith will either be a particular parameter, such as A_1 or A'_1 , or a particular set, such as set A, set A', set B, set C, . . . set X, . . . etc. and will be understood from the context in which they are used. Numerous sets and sets of sets will be hereinafter presented. For clarity, they will often be presented in combination with reference to any of a variety of terms such as “parent,” “child,” “mutation,” or “summation.” These particular types of sets will also be understood from the following discussion.

With reference to Figure 3A, a population 320 is shown in tabular presentation 310 as a plurality of sets, set A, set B, set C, set D, . . . set X. Each set has, as defined, one or more parameters 1, 2, 3, . . . n (i.e., $n \geq 1$) wherein, for example, parameter 1 for set A is shown as A_1 while parameter 3 for set C is shown as C_3 etc. It will be appreciated that the depiction of a population in the foregoing manner is merely illustrative to enhance the reader's understanding of the present invention and does not require a physical creation of the population, nor is it required to be created in any particular format or groupings. As defined, it needs to be a plurality of sets.

With simultaneous reference to the many figures, a preferred embodiment of the present invention will be described that illustrates the methods for utilizing user selection between paired comparisons, and the genetic algorithms used to process the selections, in fitting hearing aids. At step 410 of Figure 4A, a population 320 is created. For clarity, since multiple populations are set forth hereinafter, this population will be a first population. The sets A, B, C, D, . . . X shown in population 320 will be referred to as parent sets. This first population is stored in any of the memories of the processor 22.

At step 412 a first pair of parent sets from the population 320 is selected for presentation to the user 12. This first pair can be any two sets of the parent sets of the first population and are preferably (but not necessarily) selected via the genetic algorithm to be described below. For example, the first pair consists of parent set A and parent set B. This step is invisible to the user and is performed very rapidly in processor 22.

At step 414, the first pair of parent sets is presented to the user. Presentation of the first pair of parent sets, it should be appreciated, means presentation of one parent set at a time, either parent set A or parent set B, for example. Presentation in the perceptual tuning environment of a hearing aid is accomplished via hearing aid 14. It will be further appreciated that since the parent sets of population 320 are comprised of one or more parameters, and since hearing aids have many parameters used to process sound, the user while being presented a pair of parent sets is actually being presented with a set of parameters through which they “hear” sounds. The user does not actually hear the parameters, they merely hear sounds in their hearing aid as processed via the parameter sets in parent set A or parent set B. Usually, hearing aids have appropriate and proprietary software to process sounds, such as hearing aid (H.A.) algorithm 38 stored in ROM 36 of apparatus 16.

In one actual experiment performed by the inventor of the present invention, parent sets were presented to a user in order to cancel feedback in the hearing aid. The sets were comprised of three parameters and two of the parameters were selected from the list consisting of Filter length, L , and time constant, α . Each of these parameters are summarized in the following table, Table 1.

Table 1: Exemplary Parametric Values Used in Experimental Testing

L, Filter Length (# of filter taps)	8	10	13	16	20	25	32	40
α , Time Constant ($\times 10^6$) (1/sec)	10	14	19	27	37	52	72	100

It should be appreciated that parameter Filter Length, L , for example, is one of any 8 discrete values (8, 10, 13, 16, 20, 25, 32, 40) arrived at via experimental data and is not to be considered limiting of the scope of the present invention.

Eventually, the user will need to determine which parent set they like better. Since a user can only “hear” one parent set at a time, either parent set A or B, for example, the user will need to toggle, at step 416, to the other parent set. Toggling is accomplished via depressing of toggle device 30.

To assist the user in determining which parent set they like better, they should perform a variety of tasks pertinent to the tuning. In the actual experiment, users were asked to “listen” to the parent sets in a variety of environments prone to feedback, such as placing their hand over their ear(s), listening to telephone dial tones, performing jaw movements, listening in the presence and/or absence of other background noises, and other similar activities.

At step 418, after performing such tasks, can the user decide which parent set of the first pair they prefer? If they cannot, they merely repeat steps 416 and 418 for as many times necessary until they can indicate a preference. If they can, the user indicates a preference by depressing select indicator 28 whereupon the result is logged in the logging space of flash memory 42. The logging space, for example, can be arranged in many ways. In a preferred embodiment, it can be arranged to record that parent set B was preferred over parent set A, such that an A or a B are recorded in a memory address pointing to the parameters from the parent sets that are actually part of parent sets A and B. Whether this type of logging is performed or another, they are to be embraced by this invention. All types of memory recording are well known write techniques.

At step 420, a second pair of parent sets from the first population is selected for presentment to the user. In continuing the example, parent set C and parent set D are selected via the genetic algorithm 40 stored in ROM 36.

One at a time, one of parent sets C or D is presented to the user at step 422 and the user toggles to the other of the parent sets at step 424. If the user cannot decide which of the parent sets of the second pair they prefer (step 426), they toggle back and forth between the second pair of parent sets.

Thereafter, the parent sets are ranked at step 428. A hierarchical ranking is determined for each parent set included in the presentation to the user. For example, parent sets A, B, C and D were presented to the user as first pair parent set A and B and second pair parent set C and D.

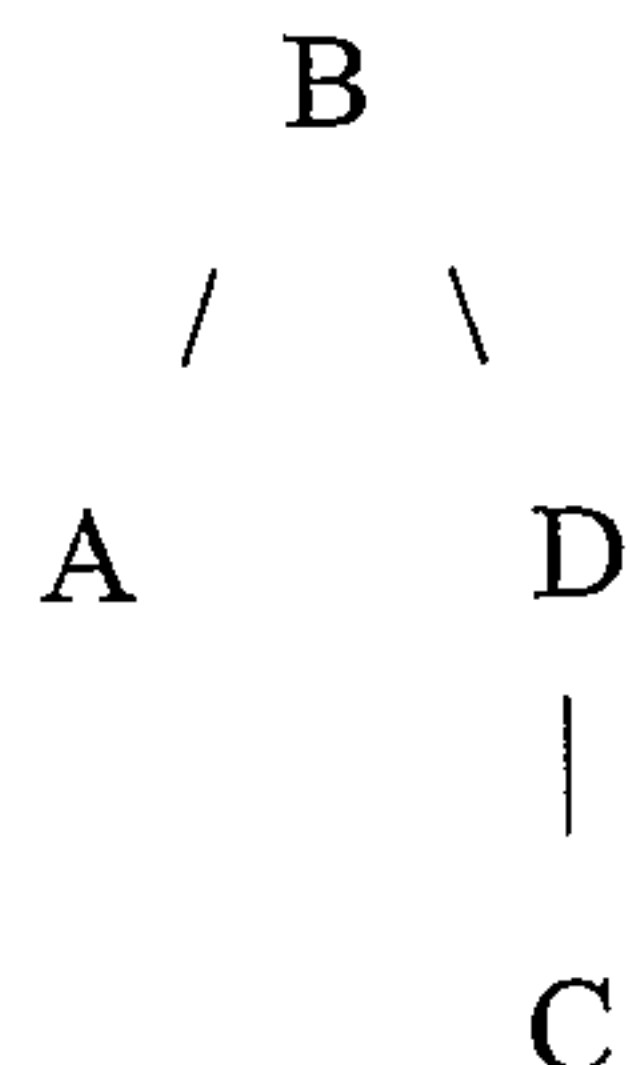
If the user preferred parent set B over A and parent set D over C, the ranking would be as follows: parent set B > parent set A; and parent set D > parent set C with the relationships between, at least the two preferred parent sets {B, D} and the

two non-preferred parent sets {A, C} being unknown. As such, it is likely that more than two iterations of presentment of pairs to the user would be performed. How many iterations depends upon how large the population is and what inferences can be made therefrom as will be shown in the continuing example. It should be appreciated that such description regarding how many pairs are presented is part of the work of the genetic algorithm 40 preferably stored in ROM 36 of apparatus 16. As such, no exact number of paired comparisons is required.

Intuitively, with fewer than four parent sets, fewer iterations are necessary. For example, if the population only consisted of two parent sets, only one pair of paired comparison need be presented before it is understood which parent set is preferred over all other sets and which set is preferred least amongst all other sets.

To continue, if parent set B and parent set D were presented to the user for paired comparison and the user indicated a preference for parent set B over D, we would also have: parent set B $\succ$ parent set D.

Or, graphically:



At this point, although parent set B and parent set C were never presented in direct comparison to one another, it can be inferred that parent set B $\succ$ parent set C. If you next presented parent set A and parent set D, and parent set D is indicated as preferred over parent set A, the genetic algorithm knows, and can more meaningfully receive a ranking (step 428): parent set B $\succ$ parent set D $\succ$ {A, C} where the relationship between parent set A and C is unknown. In a preferred embodiment, the ranks given are parent set B equal to number 1, parent set D equal to two, and parent sets A and C equal to 3.5 or $((3+4)/2)$ since they "tied." The advantage of the foregoing is that inconsistencies are avoided by not making comparisons when the dominance-equivalence relationship can be inferred from

previous responses (parent set B “dominates” C, parent set A is “equivalent” to C, for example).

With genetic algorithms, as in biology, the least fit genes do not survive. As such, the relationship between parent sets A and C is unnecessary to determine.

5 After ranking, probabilities of selection (as preferences are indicated via the select indicator 30) are assigned to the ranked parent sets at step 430.

In this example, the probabilities are presented in Table 2.

Table 2: Exemplary Probabilities of Selection of Parent Sets

	Parent Set (i)	Probability of Selection, p_i
10	A	0.19
	B	0.36
	C	0.19
	D	0.26

As will be noticed, the probabilities add up to equal one with higher probabilities assigned to those parent sets with higher ranks, i.e., those parent sets more likely to be selected by the user in a paired comparison over another parent set. Accordingly, parent set B has the highest probability while parent sets A and C have the lowest.

At step 434, the weakest, or least fit, parent sets of the first population will be replaced with child sets. In arriving at the child sets, it must first be determined which of the parent sets are the fittest so that the fittest survive while the weakest die. From the table, parent sets B and D are the fittest simply because they have the highest probabilities of selection while parent sets A and C are the weakest.

Once the two fittest parent sets are determined, genetic algorithm operators, either crossover and/or mutation at step 432 are applied to at least one parent set to produce child set(s). In one embodiment, the two fittest parent sets could be selected to produce child sets. In another embodiment to determine which parent sets will be used to produce a child set, two unique fittest sets of the parent sets are selected. This is done by associating each of the parent sets with intervals of numbers and, depending upon the comparison of intervals with the output of a

random number generator between zero and one (such as that provided by a uniform random number generator), selecting the two unique fittest parent sets.

For example, parent set A is associated with the interval of numbers $[0, p_A]$ or from Table 2, $[0, 0.19]$, parent set B the interval $(p_A, p_A + p_B]$ or $(0.19, 0.55]$, parent set C the interval $(p_A + p_B, p_A + p_B + p_C]$ or $(0.55, 0.74]$, and parent set D $(p_A + p_B + p_C, p_A + p_B + p_C + p_D]$ or $(0.74, 1.0]$. Next, in the actual experiment, a random number generated two outputs. A 0.95 followed by a 0.23. Thus, the two unique fittest parent sets are parent sets D and B (i.e, 0.95 is found in the range of the interval for parent set D $(0.74, 1.0]$ while 0.23 is found in the range of the interval for parent set B $(0.19, 0.55]$). Thus, parent sets B and D are the two unique fittest sets and will be used to produce child sets.

To illustrate both crossover and mutation, a table of indexes will be created from the exemplary parametric values from Table 1. In devising this table of indexes, however, only the filter length parameter will be used. It will be appreciated, though, that index tables for all parameters could be constructed. In this instance, parameter filter length, L, has 8 values (8, 10, 13, 16, 20, 25, 32 and 40) from Table 1. This parameter range reflects a wide range of values and it should be appreciated that it is non-linear. Then, an index is assigned for each value. Since there are eight values, eight indexes or indexes are assigned. In this case, indexes in a parent index range from 0 -7 were selected with 0 being the low parent index and 7 being the high parent index. The result is shown in Table 3.

Table3:Exemplary Table of Indexes for Filter Length, L, from Table 1.

Index	0 (Low)	1	2	3	4	5	6	7 (High)
L, Filter Length	8	10	13	16	20	25	32	40

Then, with reference to Figure 3B, the genetic algorithm crossover operator will be described as acting on the two fittest parent sets from the previous example (parent set B and D which are also the two unique fittest sets). In the figure, parent set B is comprised of a plurality of parameters 1 through n as shown by B_1 through B_n . In this example, n will equal 4. Likewise, for parent set D.

Parameter 1 for parent set B is a filter length of 16. Parameter 2 for parent set B is a filter length of 20. Parameter 3 for parent set B is a filter length of 10. Parameter 4 for parent set B is 32. Instead of showing parent set B as a set of parameter values, it is shown as a set of indexes. Thus, parent set B is shown as:

5

3	4	1	6
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where 3, 4, 1, and 6 are the parent indexes corresponding to the respective filter lengths 16, 20, 10, and 32. In a similar fashion, parent set D has parent indexes of 0, 6, 7, and 3.

10 In a first step for performing crossover, select a parent index position 100 and a child index position 102. In this embodiment, both positions are the same and correspond to the third index position (from the left) in both parent sets B and D (i.e., index 1 for parent set B and index 7 for parent set D) and the child index position 102 in both child sets B' and D'.

Then, create indexes in the child set B' by:

15 i) reproducing in child set B', to a left of the child index position, the parent indexes of one of the parent sets (parent set B) to the left of the parent index position (in this case indexes 3 and 4);

ii) reproducing in child set B' to a right of the child index position, the parent indexes of the other of the parent sets (parent set D) to the right of the parent index position (in this case index 3); and

20 iii) at the child index position, create any child index that is substantially equal to the low parent index (0), the high parent index (7) or any index in the range of indexes from the low parent index (0, from Table 3) to the high parent index (7, from Table 3). Likewise for child set D'.

25 In another embodiment, step iii) comprises, at the child index position, selecting the indexes from parent sets B and D (index 1 and index 7, respectively) and using a random number to select two new child indexes (one for each child set) in the range of between index 1 (low parent index) and index 7 (high parent index) that sum to the same value as the sum of the two parent set indexes, in this case, 1 + 7 = 8. For example, the two new child indexes for child sets B' and D'

30

respectively, which all sum to the value 8, include (1,7), (2,6), (3,5) (4,4), (5,3), (6,2) and (7,1).

For mutation, with reference to Figure 3C, begin with a parent set (parent set B). Again, the parent set is comprised of parameters being represented by parent indexes 3, 1, 6, and 3. Next, create a mutation set having a plurality of mutation indexes. In this example, they include -1, 0, 3, and 0.

Sum the mutation indexes and the parent indexes of the mutation and parent sets to form a summation set having a plurality of summation indexes. In this example, 2, 1, 9, 3 or (3+ -1), (1+0), (6 +3), (3+0).

Finally, reproduce the summation indexes in a child set. Since the summation indexes in this example had one index, the number 9, outside the range of the parent indexes from low parent index 0 to high parent index 7, the index 9 was rounded to the closest parent index in the range. In this example, the index 9 was rounded to 7 and the child set B' became child indexes 2, 1, 7, and 3.

In determining the mutation set, it is preferred to use a random number generator to come up with the mutation indexes. With reference to Figure 3D, it will be appreciated that the mutation indexes -1, 0, 3, and 0 were obtained by respectively rounding random numbers -0.94, 0.22, 3.49, and 0.18 to the nearest positive or negative integer.

In a preferred embodiment, the random numbers -0.94, 0.22, 3.49, and 0.18 were obtained from a normal distribution, $N(0, \sigma^2)$ for random variables having an average of 0 and a variance of distribution being equal to σ^2 where $\sigma = (\text{a system constant} \times \text{the number of indexes in the range of parent indexes})$. In this example, the system constant is 0.2 which was determined empirically by various run simulations of numbers while the number of indexes in the range of parent indexes 0-7 is eight (8): $\sigma = 0.2 \times 8 = 1.6$.

Mutation indexes could also be arrived at by various other random numbering schemes well known in the art. They could even be obtained without regard to random numbering. It is believed, however, that random numbers make the system more robust.

It should be appreciated that in the foregoing, the table of indexes is linear while the parametric values represented by the table of indexes is non-linear. In this manner, it has been observed that better evolution of populations occurs as compared to other evolution schemes that crossover and mutate directly on bit strings or directly on parameters having a wide, varied and non-linear range. Unlike those schemes where evolution is often too quick, too slow, too unstable or some other poorly performing process, the evolution of the present invention is stable and robust.

It should also be appreciated that use of the foregoing described operations for performing crossover and mutation, ultimately, allows mixing and matching of different parameter sets having different units and measuring schemes.

Thereafter, at step 434, the least fit or the weakest parent sets of the first population are replaced with child sets obtained from mutation, crossover or both. For example, in Figure 3E a second population 322 results, presented in tabular form 310, having weak parent sets A and C of the first population replaced with child sets B' and D' from the crossover operation of Figure 3B.

Thereafter, the steps beginning at step 410 of presenting paired comparisons to users begin again. It should be appreciated, however, that when comparisons are made now, they are made from the sets of the second population. As such, parent sets may be compared exclusively to other parent sets, child sets compared exclusively to other child sets, or a hybrid comparing child sets to parent sets.

As this process repeats itself, numerous population sets may be evolved that are many generations removed from the first population. The present invention is not limited to any particular number of population generations.

It should be further appreciated that as generations evolve (more populations are created), the relationships in the previous population are already known so that the only relationships that need to be determined are those between the child sets and the child sets with parent sets. As such, fewer comparisons are required with each next population. This results in less time being required for each next population.

How often mutation and crossover occur in relation to one another is a function of user preference. In one embodiment, more crossovers happen early on with more mutations happening later or vice versa. In another embodiment, crossovers and mutations occur together in the same exact number. In still another
5 embodiment, crossovers exceed mutations, or vice versa.

The process described above repeats itself for as many times as necessary to arrive at a converged upon solution set having the preferred set of parameters for fitting the hearing aid to the particular user. For example, it may be discovered that child set B' is the preferred set of all sets presented.

10 Consequently, it should be appreciated that users do not have to maintain consistent application of numbering scales, such as from 1 to 5, in their minds as they apply them to numerous various hearing solutions. They simply need to indicate a preference for one element of each pair (of hearing aid settings). This is as simple as depressing a select indicator on a hand held device after toggling back
15 and forth between the selections for as many times necessary in determining their preferences. A genetic algorithm does all the computation and kills off poor (weak) hearing solutions thereby quickly converging all the preferences upon a single solution. In the actual experiment, users made approximately 50 to 75 paired comparisons during about one hour of listening.

20 Moreover, the present embodiments now advantageously provide a solution whereby field ready (in home), unsupervised use ready hearing aids can be fit without need of any input other than the user's.

In another embodiment, the initial prescription setting 48 can be reset via mechanism 50 to update or replace the original prescription with the parameter(s)
25 of the converged upon solution set. In this manner, the hearing aid prescription can be modified according to individual preferences in the user's home environment. Preferably, reset mechanism 50 is a read/write device that can read the parameters of the solution set and write them over the parameters of the initial prescription setting.

30 With reference to Figure 5, another manner in which perceptual tuning in accordance with the present invention can be perceived is shown generally as 500.

In this diagram, the system 528 would be the hearing aid 14 of the previous example.

5 The population 518 is the same as population 320 before. The partial dominance model contains an entry for each possible pair, without respect to presentation order, from population 518 that can be presented to the user. For example, parent set A can be presented with parent sets B, C, D, . . . or X. Likewise, parent set B can be presented with parent sets C, D, . . . or X, etc. With 5 parent sets, 10 possible pairs result.

10 The parent sets are presented to the user as the block “select and present pairs” 524. Once presented, the user indicates his/her preference and the preference is logged at data collection 534 along with which two parent sets were presented and what parameters they were constructed from.

15 The user bases his/her preference upon the perception 532 of the pair (of parent sets) as they are observed in environment 530. As is implied by their names, perception is the act or result of perceiving as done by the user and environment is the surroundings in which the sounds are perceived.

20 The one or more parameters from which the parent sets are constructed are contained in block 526, set of n parameters, with n being one or more. Again, the parameters are a function of the system in which they are used and therefore interact diagrammatically with the system 528.

The hierarchical ranking of the parent sets happens with conversion to ranks 516.

At 514, a hypergeometric fitness function assigns the probabilities of selection based upon the conversion to ranks 516.

25 Based on this information, the genetic algorithm 512, decides which pairs, if any, from the population 518 become presented to the users at 524. Non-binary GA operators such as mutation and crossover previously described supply input to the genetic algorithm to form child sets. Thereafter, the genetic algorithm replaces parent sets of the population 518 with newly created child sets to form a second population comprised of parent sets and child sets. The genetic algorithm also 30 decides which sets from this second population get presented to the user at 524.

In further detail, the method of presenting pairs of parent sets and inferring ranks has four components. The first chooses which pair gets presented to the user. Then, the second draws all possible inferences based on the user's response and previous information. The third determines if another comparison is required. If
5 another response is not required, the fourth is invoked and generates ranks for all the members of the population.

The data collection can also include information about environment 530 that can be provided to the genetic algorithm to assist in its selection of pairs for presentment and, ultimately, upon its convergence upon a solution set that
10 perceptually tunes the system.

Finally, and representative of all embodiments herein, computer readable medium which can be accessed by a special or general purpose computer could be used to store information thereon, such as the genetic algorithm, the crossover operator, the mutation operator, the hypergeometric fitness function, the conversion
15 to ranks, the population(s), the partial dominance model, and/or the parameters and/or other methods described that give way to being read by a computer. By way of example, and not limitation, such computer readable media can comprise ROM, RAM, EEPROM, CDs or other optical disk storage devices, floppy disks or other magnetic disk storage devices, or any other media now known or hereinafter
20 invented which can be used to store the desired executable instructions or data fields of the exemplary information above. In a preferred embodiment, the stored information will be loaded into and for use in either the apparatus 16, the fully integrated hearing aid package 52 and/or the hearing aid 14. While these computer readable media are not shown in any figure, they are not required to be for they
25 represent technologies well known to those skilled in the art and their description is not any better understood by referencing a particular figure.

Conclusion

Hearing aids and methods and apparatus for efficaciously audio fitting them have been described. More broadly, however, the perceptual tuning of any system has been described that uses genetic algorithms that, in turn, utilize user input selection from paired comparisons. Such user input selection from paired comparisons in an audio fitting of a hearing aid, for example, relates to a user comparing two audio settings and selecting a preferred one. Still even more broadly, the present invention has been described in terms of improved genetic algorithm crossover and mutation operators for use in a genetic algorithm that neither operate directly on a parametric value nor a string of bits representing the parametric value.

The present invention has been particularly shown and described with respect to certain preferred embodiment(s). However, it will be readily apparent to those of ordinary skill in the art that a wide variety of alternate embodiments, adaptations or variations of the preferred embodiment(s), and/or equivalent embodiments may be made without departing from the intended scope of the present invention as set forth in the appended claims. Accordingly, the present invention is not limited except as by the appended claims.

WHAT IS CLAIMED IS:

1. An apparatus for fitting a hearing aid, comprising:
a memory having a first population stored therein, the first population comprising a plurality of parent sets;
a toggle device for toggling between a first pair of the plurality of parent sets;
a select indicator for selecting a preferred one set of the first pair; and
a communications link for interfacing with the hearing aid.
2. The apparatus according to claim 1, wherein each parent set of the plurality of parent sets comprises more than one parameter.
3. The apparatus according to claim 1, wherein the communications link is a wireless link.
4. The apparatus according to claim 1, further comprising a processor for ranking a hierarchy of the plurality of parent sets.
5. The apparatus according to claim 1, further comprising a processor for assigning a probability of selection by the select indicator to the plurality of parent sets.
6. The apparatus according to claim 1, wherein the plurality of parent sets comprises at least a first, second and third set, further comprising a genetic algorithm for deciding which of the first, second and third sets becomes the first pair.

7. The apparatus according to claim 1, further comprising a genetic algorithm operator for performing one of mutation and crossover on at least one set of the plurality of parent sets thereby forming a child set.
8. The apparatus according to claim 7, further comprising a genetic algorithm for replacing one of the plurality of parent sets in the first population with the child set thereby forming a second population.
9. The apparatus of claim 8, wherein the toggle device toggles between a second pair of sets selected from the second population.
10. The apparatus of claim 1, wherein the toggle device toggles between a plurality of pairs of the plurality of parent sets, further comprising a processor for converging the plurality of pairs to a single solution set.
11. A hearing aid fitted by the apparatus according to claim 1.
12. An apparatus for fitting a hearing aid, comprising:
 - a memory having a first population stored therein, the first population comprising a plurality of parent sets;
 - a toggle device for toggling between a plurality of pairs of the plurality of parent sets, each of the plurality of pairs having a first and second set;
 - a select indicator for selecting a preferred one of the first and second set in the each of the plurality of pairs;
 - a genetic algorithm operator for performing one of mutation and crossover on at least one set of the plurality of parent sets thereby producing a child set;
 - a genetic algorithm for replacing one of the plurality of parent sets in the first population with the child set thereby forming a second population wherein the toggle device toggles between another pair of sets, the another pair being selected from the second population;

a processor for converging the sets of the plurality of pairs and the another pair to a single solution set; and

a communications link for interfacing with the hearing aid.

13. The apparatus according to claim 12, wherein the processor ranks a hierarchy of the plurality of parent sets.

14. The apparatus according to claim 13, wherein the processor assigns a probability of selection by the select indicator to the sets of the plurality of pairs and the another pair.

15. The apparatus according to claim 14, wherein the genetic algorithm decides which of the plurality of parent sets becomes the first and second sets for each the plurality of pairs.

16. A hearing aid fitted by the apparatus according to claim 12.

17. A hearing aid, comprising:

a memory having a first population stored therein, the first population comprising a plurality of parent sets, each of the parent sets having at least one parameter;

a toggle device for toggling between a first pair of the plurality of parent sets; and

a select indicator for selecting a preferred one set of the first pair.

18. The hearing aid according to claim 17, further comprising an initial prescription setting and a reset mechanism for updating the initial prescription setting with one of the at least one parameters.
19. The hearing aid according to claim 17, wherein the toggle device is one of a software algorithm and mechanical mechanism.
20. The hearing aid according to claim 17, further comprising a processor for ranking a hierarchy of the plurality of parent sets.
21. The hearing aid according to claim 17, further comprising a processor for assigning a probability of selection by the select indicator to the plurality of parent sets.
22. The hearing aid according to claim 17, wherein the plurality of parent sets comprises at least a first, second and third set, further comprising a genetic algorithm for deciding which of the first, second and third sets becomes the first pair.
23. The hearing aid according to claim 17, further comprising a genetic algorithm operator for performing one of mutation and crossover on at least one set of the plurality of parent sets thereby forming a child set.
24. The hearing aid according to claim 23, further comprising a genetic algorithm for replacing one of the plurality of parent sets in the first population with the child set thereby forming a second population.

25. The hearing aid according to claim 24, wherein the toggle device toggles between a second pair of sets selected from the second population.
26. The hearing aid according to claim 17, wherein the toggle device toggles between a plurality of pairs of the plurality of parent sets, further comprising a processor for converging the plurality of pairs to a single solution set.
27. A method of fitting a hearing aid, comprising the steps:
preparing a first population of a plurality of parent sets;
presenting a first pair from the parent sets, the first pair comprising a first and second set and being presented with assistance of the hearing aid;
selecting a first preference between the first and second sets of the first pair;
operating on at least one set of the plurality of parent sets to obtain a child set, the child set being one of a mutation and crossover;
replacing one of the plurality of parent sets of the first population with the child set to form a second population;
presenting a second pair, the second pair comprising the child set and a third set, the third set being selected from the second population but not being the child set;
selecting a second preference between the child set and the third set of the second pair; and
converging on a solution set, the solution set being one of the first, second, third and child sets.
28. The method according to claim 27, further comprising the step of ranking a hierarchy of the plurality of parent sets.

29. The method according to claim 27, further comprising the step of assigning a probability of selection in one of the selecting steps to the first, second, third and child sets.
30. The method according to claim 27, further comprising the step of deciding which set of the plurality of parent sets becomes the first and second sets of the first pair.
31. A method of fitting a hearing aid, comprising the steps:
providing a hearing aid having an initial prescription;
preparing a population of a plurality of parent sets, each of the parent sets having at least one parent parameter;
presenting a first pair of sets from the parent sets, the first pair comprising a first and second set and being presented with assistance of the hearing aid;
selecting a first preference between the first and second sets of the first pair;
presenting a second pair of sets from the parent sets, the second pair comprising a third and fourth set;
selecting a second preference between the third and fourth sets of the second pair;
operating on one set of the plurality of parent sets to obtain a child set, the child set being one of a mutation and crossover of the one set, the child set having at least one child parameter;
replacing one of the plurality of parent sets of the first population with the child set to form a second population;
presenting a third pair of sets, the third pair comprising the child set and a fifth set, the fifth set being selected from the second population but not being the child set;
selecting a third preference between the child set and the fifth set;
converging on a solution set, the solution set being one of the first, second, third, fourth, fifth and child sets; and

updating the initial prescription with one of the at least one parent and child parameters.

32. A method of using a genetic algorithm in a system having a first population of a plurality of parent sets, comprising the steps;

presenting a first pair of sets from the parent sets, the first pair comprising a first and second set, the genetic algorithm selecting which of the parent sets becomes the first and second set;

indicating a preference to the genetic algorithm between the first and second sets of the first pair;

operating on at least one set of the plurality of parent sets with a genetic algorithm operator to obtain a child set, the child set being one of a mutation and crossover;

replacing one of the plurality of parent sets of the first population with the child set to form a second population;

presenting a second pair, the second pair comprising the child set and a third set, the third set being selected from the second population but not being the child set, the genetic algorithm selecting which set of the second population becomes the third set;

indicating a second preference to the genetic algorithm between the child set and the third set of the second pair; and

converging on a solution set, the solution set being one of the first, second, third and child sets.

33. A computer readable medium having executable instructions for performing the steps of claim 32.

34. A method of perceptually tuning a system using a genetic algorithm, comprising the steps:
- providing a system an initial setting;
 - preparing a population of a plurality of parent sets, each of the parent sets having at least one parent parameter;
 - presenting a first pair of sets from the parent sets, the first pair comprising a first and second set, the genetic algorithm selecting which of the plurality of parent sets becomes the first and second set;
 - indicating a first preference to the genetic algorithm between the first and second sets of the first pair;
 - presenting a second pair of sets from the parent sets, the second pair comprising a third and fourth set, the genetic algorithm selecting which of the plurality of parent sets becomes the third and fourth sets;
 - indicating a second preference to the genetic algorithm between the third and fourth sets of the second pair;
 - operating on one set of the plurality of parent sets with a genetic algorithm operator to obtain a child set, the child set being one of a mutation and crossover of the one set, the child set having at least one child parameter;
 - replacing one of the plurality of parent sets of the first population with the child set to form a second population;
 - presenting a third pair of sets, the third pair comprising the child set and a fifth set, the fifth set being selected from the second population but not being the child set, the genetic algorithm selecting which set of the second population becomes the fifth set;
 - indicating a third preference to the genetic algorithm between the child set and the fifth set;
 - converging on a solution set, the solution set being one of the first, second, third, fourth, fifth and child sets; and
 - updating the initial setting with one of the at least one parent and child parameters selected from the solution set.

35. A computer readable medium having executable instructions for performing the steps of claim 34.
36. A method of using a genetic algorithm crossover operator on at least a first and second parent set in a system population, each of the parent sets having a plurality of parent parameters, each the parent parameter being represented by a parent index wherein the parent indexes can be arranged in a range from a low the parent index to a high the parent index, comprising the steps:
- choosing a parent index position in the first and second parent sets with some of the parent indexes in each set of the first and second parent sets being to a left and right of the parent index position;
- creating a child set, the child set having a child index position, further comprising the steps,
- i) reproducing in the child set to a left of the child index position, the parent indexes of one of the first and second parent sets to the left of the parent index position;
- ii) reproducing in the child set to a right of the child index position, the parent indexes of the other of the first and second parent sets to the right of the parent index position; and
- iii) creating a child index at the child index position that is any value substantially equal to one of the low parent index, the high parent index and any the parent index in the range.
37. The method according to claim 36, wherein the range is linear.
38. A computer readable medium having executable instructions for performing the steps of claim 36.
39. A method of using a genetic algorithm mutation operator on at least one parent set in a system population, the one parent set having a plurality of

parent parameters, each the parent parameter being represented by a parent index wherein the parent indexes can be arranged in a range from a low the parent index to a high the parent index, comprising the steps:
creating a mutation set having a plurality of mutation indexes;
summing the mutation indexes and the parent indexes to form a summation set having a plurality of summation indexes; and
reproducing the mutation indexes in a child set.

40. The method according to claim 39, wherein the one of the mutation indexes is one of larger than the high parent index and smaller than the low parent index, wherein the step of reproducing the mutation indexes in the child set further comprises the step of rounding the one of the mutation indexes to one of the high parent index and the low parent index.
41. The method according to claim 39, wherein the step of creating the mutation set further comprises generating the mutation indexes by generating a plurality of random variables and rounding each the random variable to a closest integer.
42. The method according to claim 41, wherein the step of generating the plurality of random variables further comprises the step of creating a normal distribution for the random variables.
43. A computer readable medium having executable instructions for performing the steps of claim 39.

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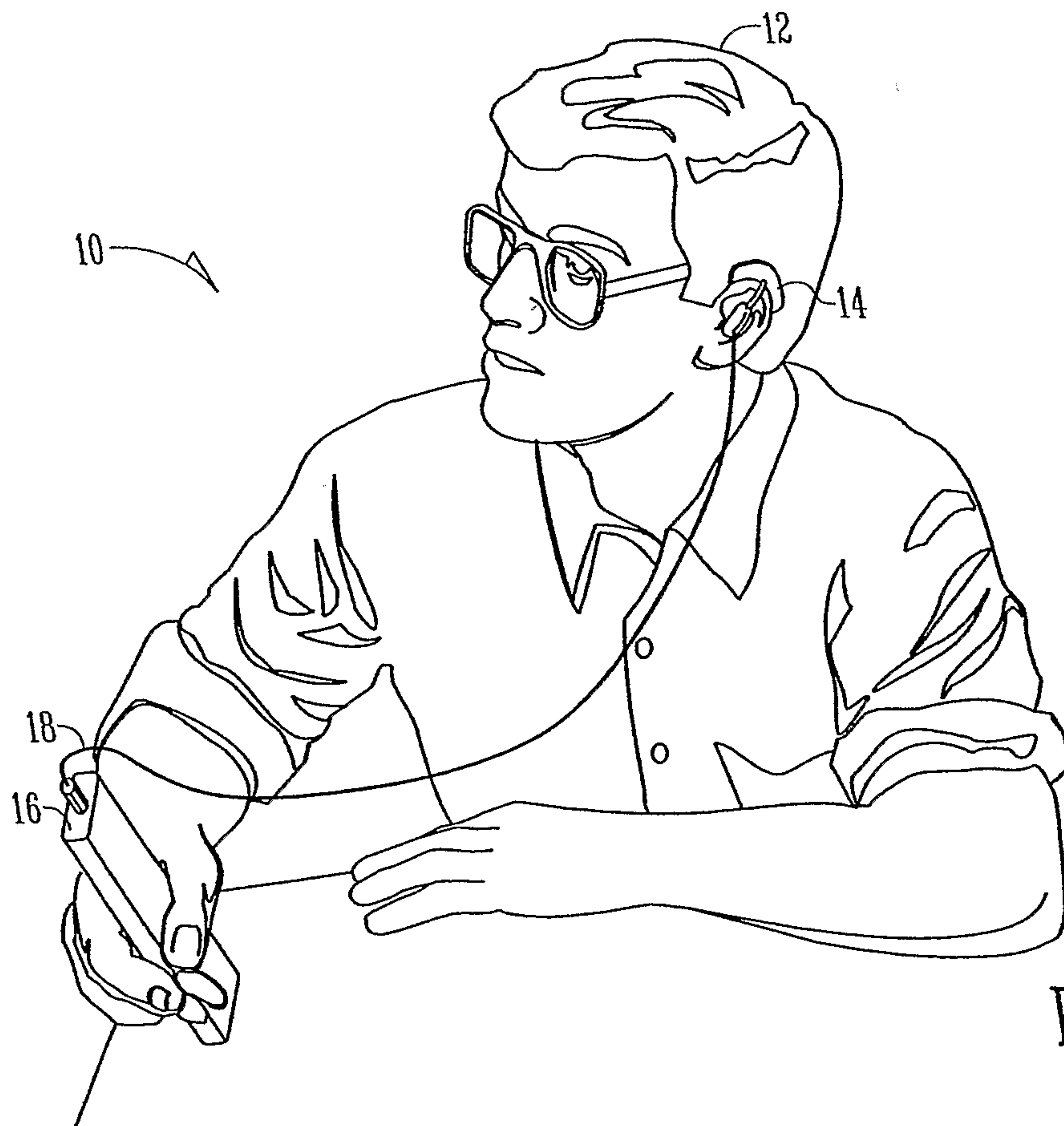


Fig. 1A

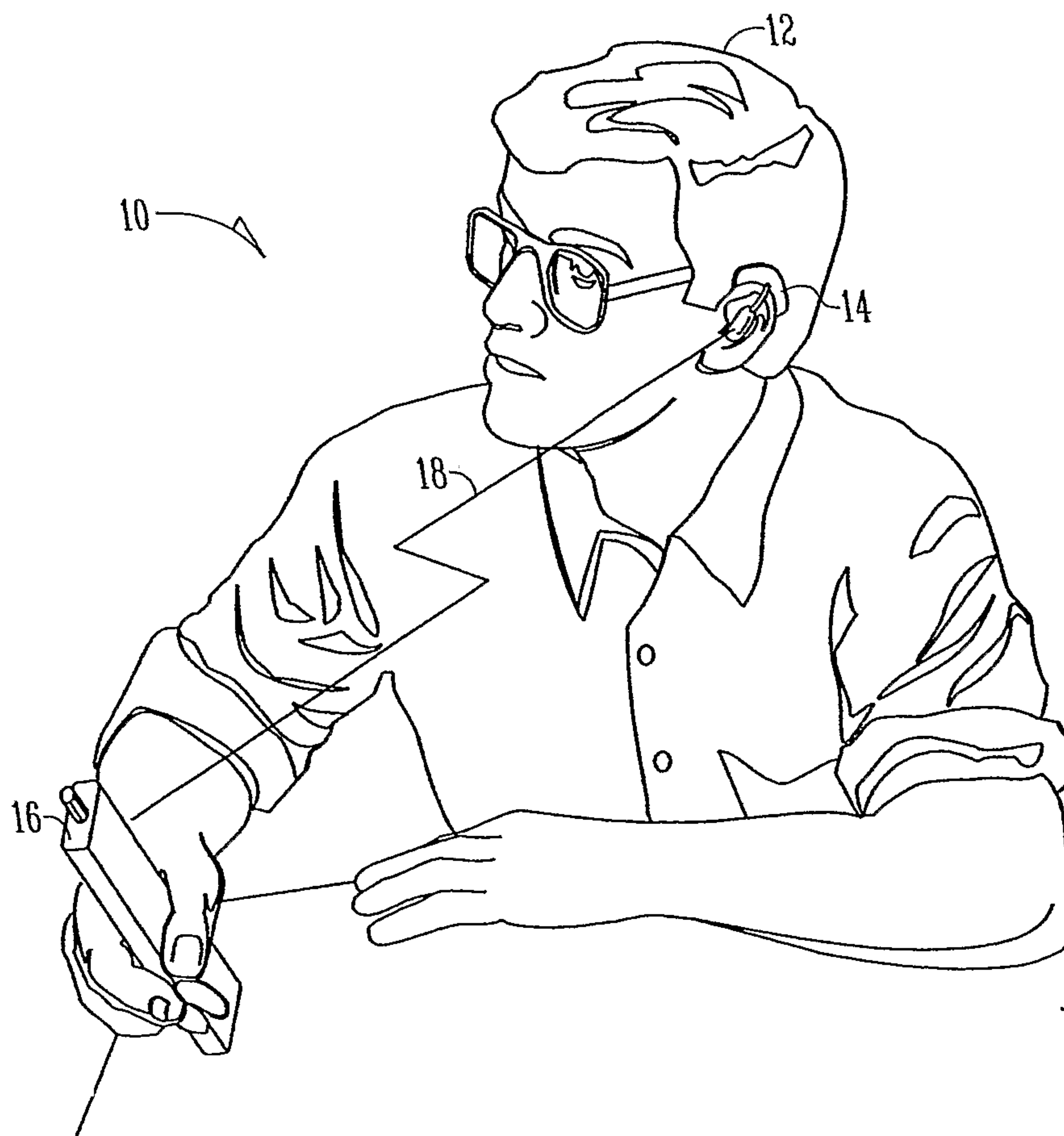


Fig. 1B

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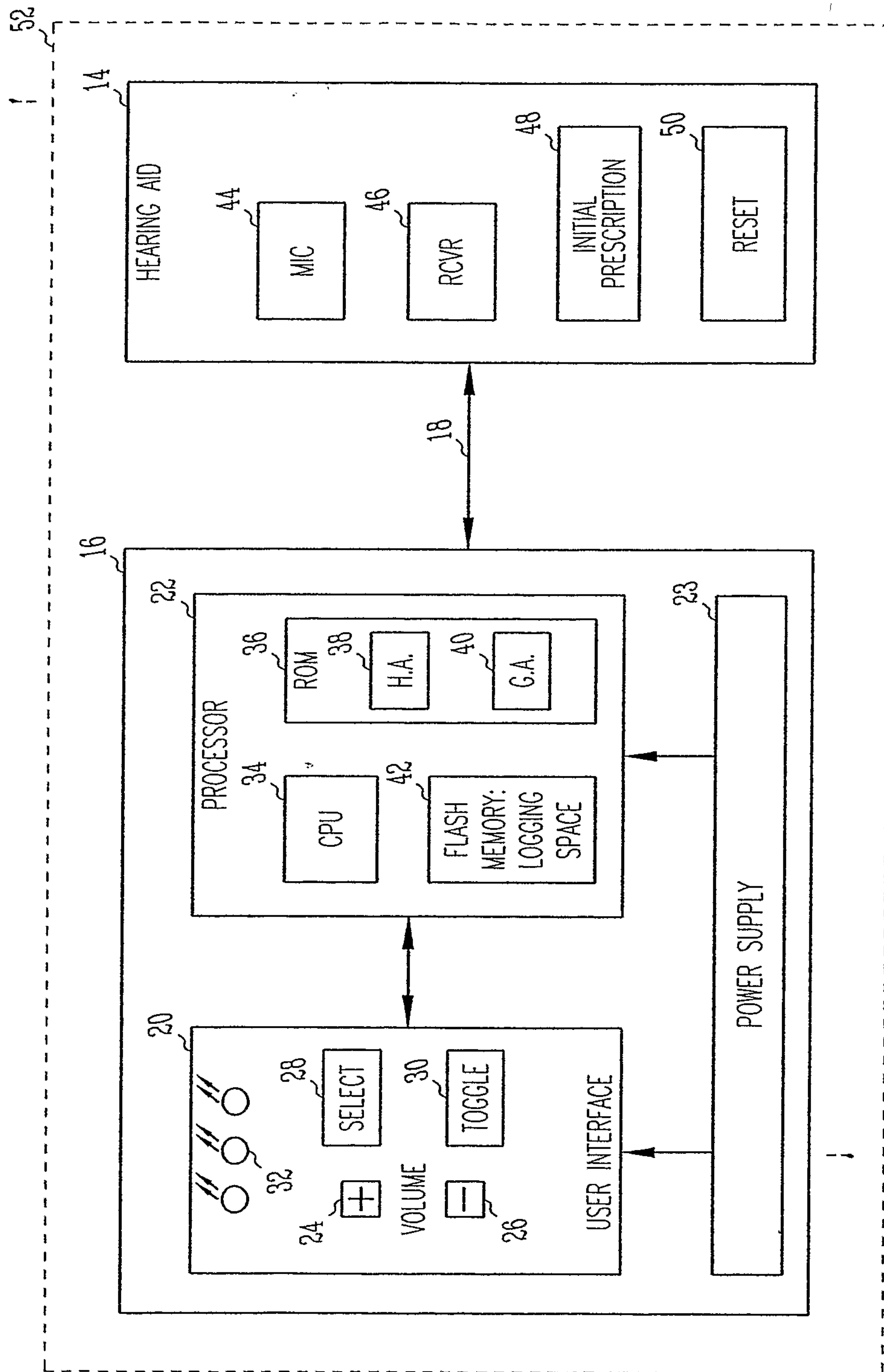


Fig. 2

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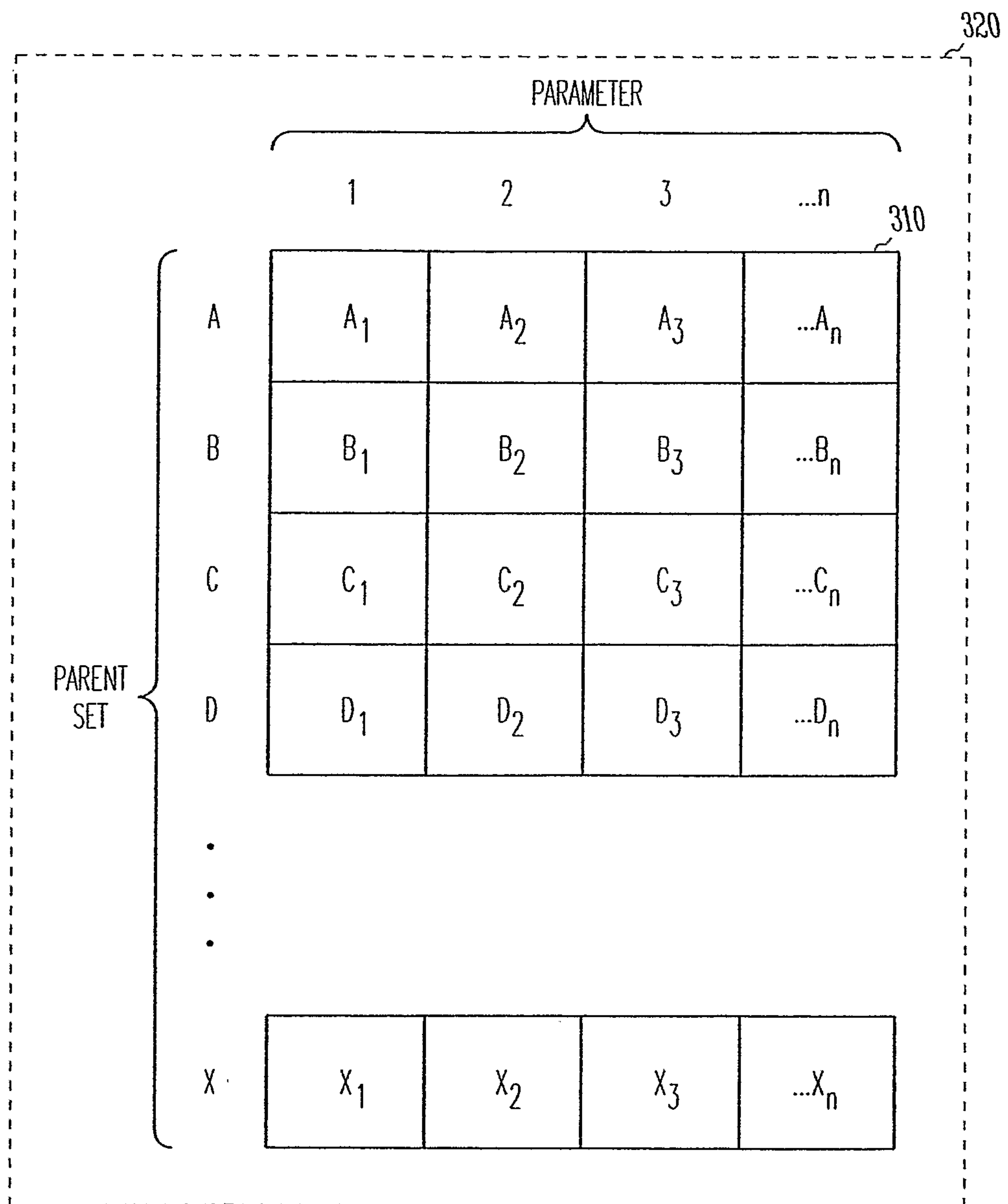


Fig.3A

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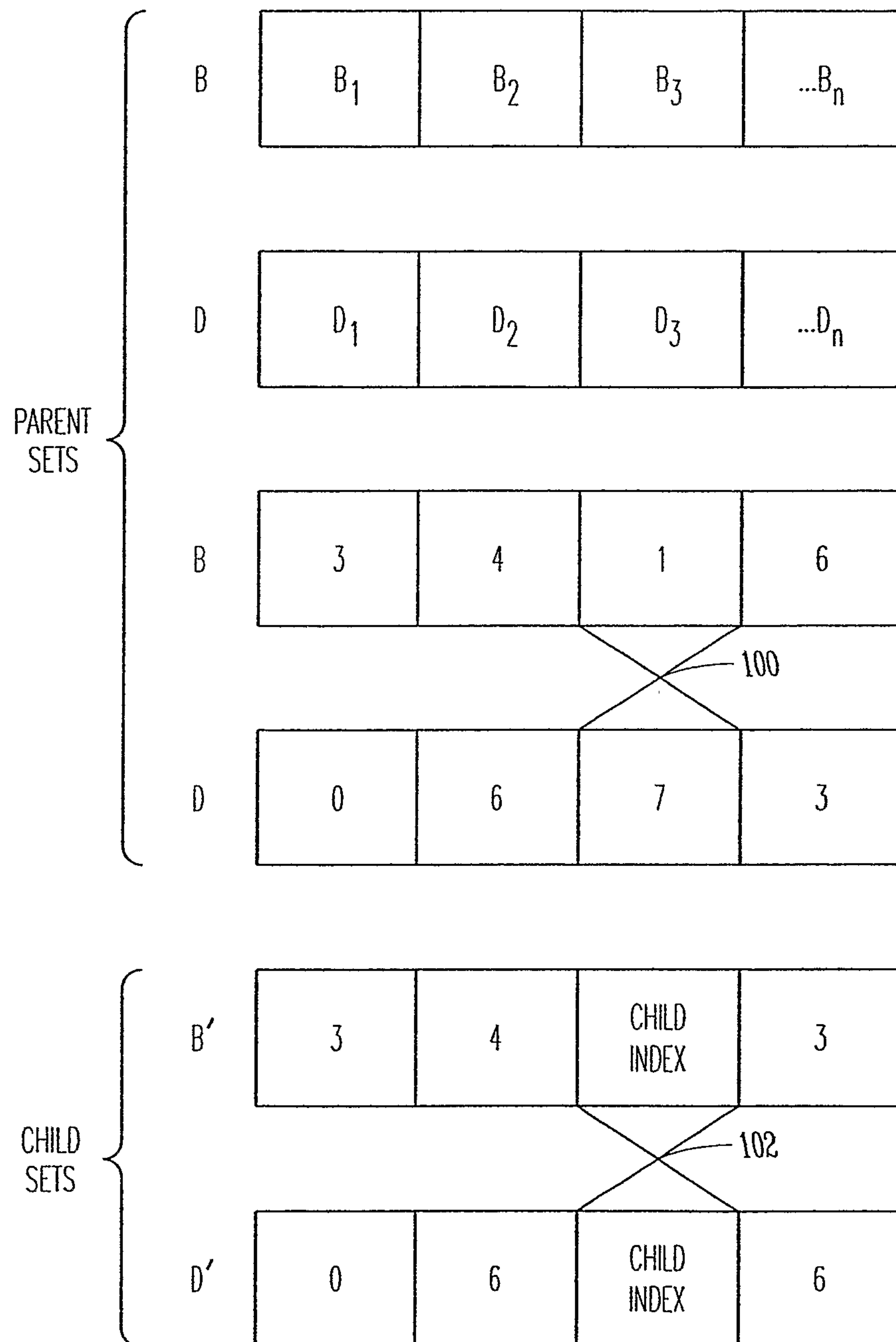


Fig.3B

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PARENT SET B	3	1	6	3
MUTATION SET	-1	0	3	0
SUMMATION SET	2	1	9	3
CHILD SET B'	2	1	7	3

Fig.3C

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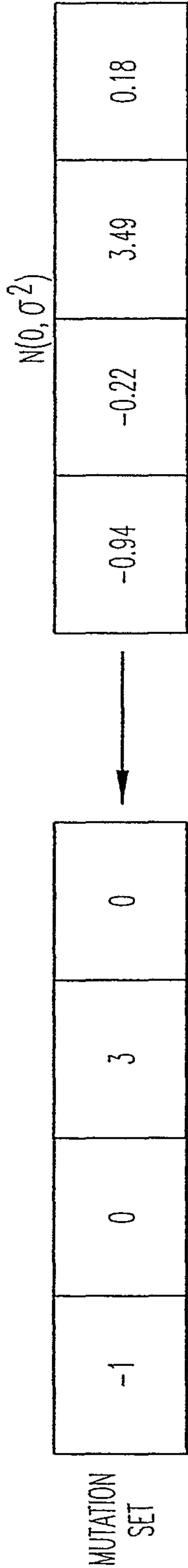


Fig.3D

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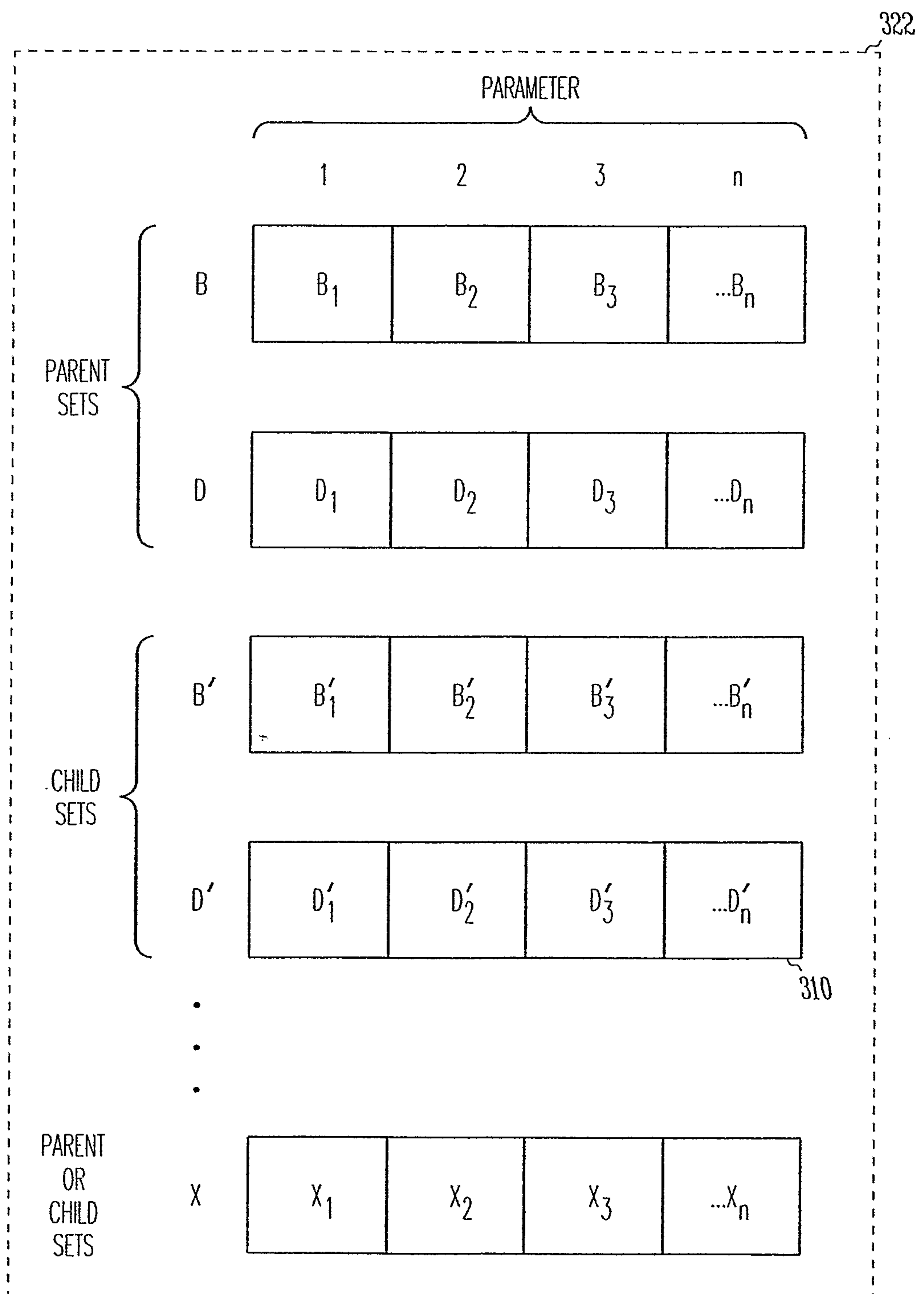


Fig.3E

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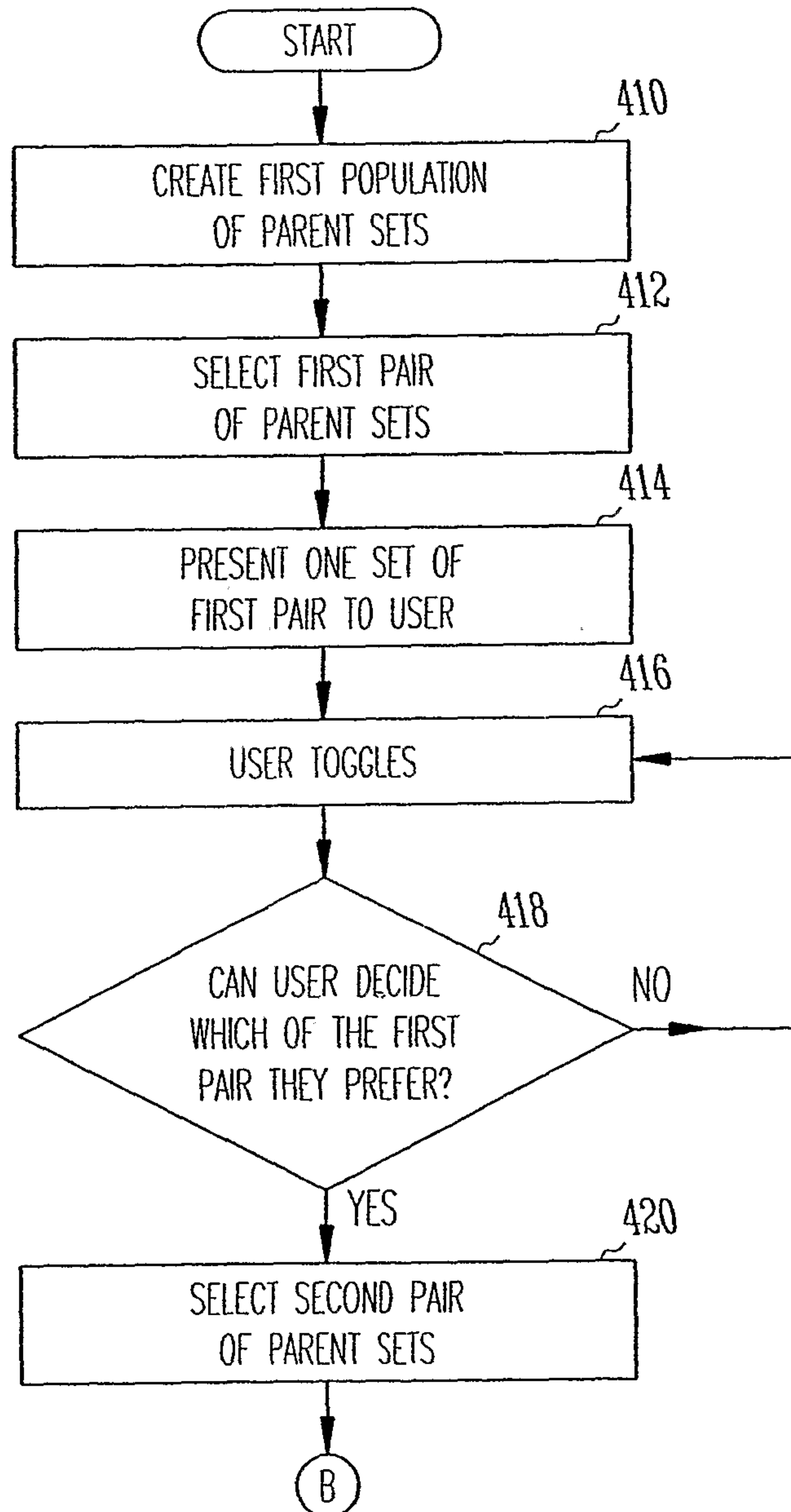


Fig. 4A

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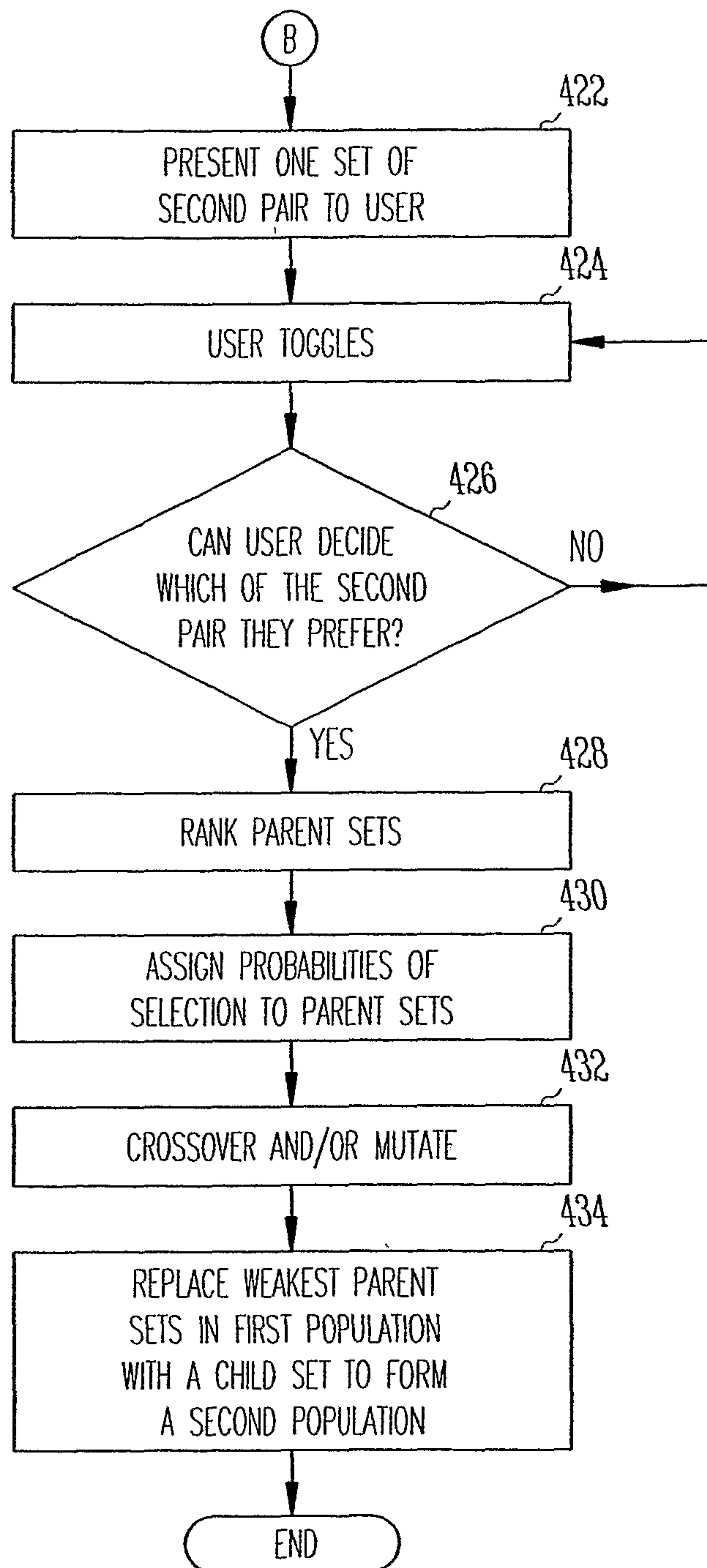


Fig. 4B

10/10

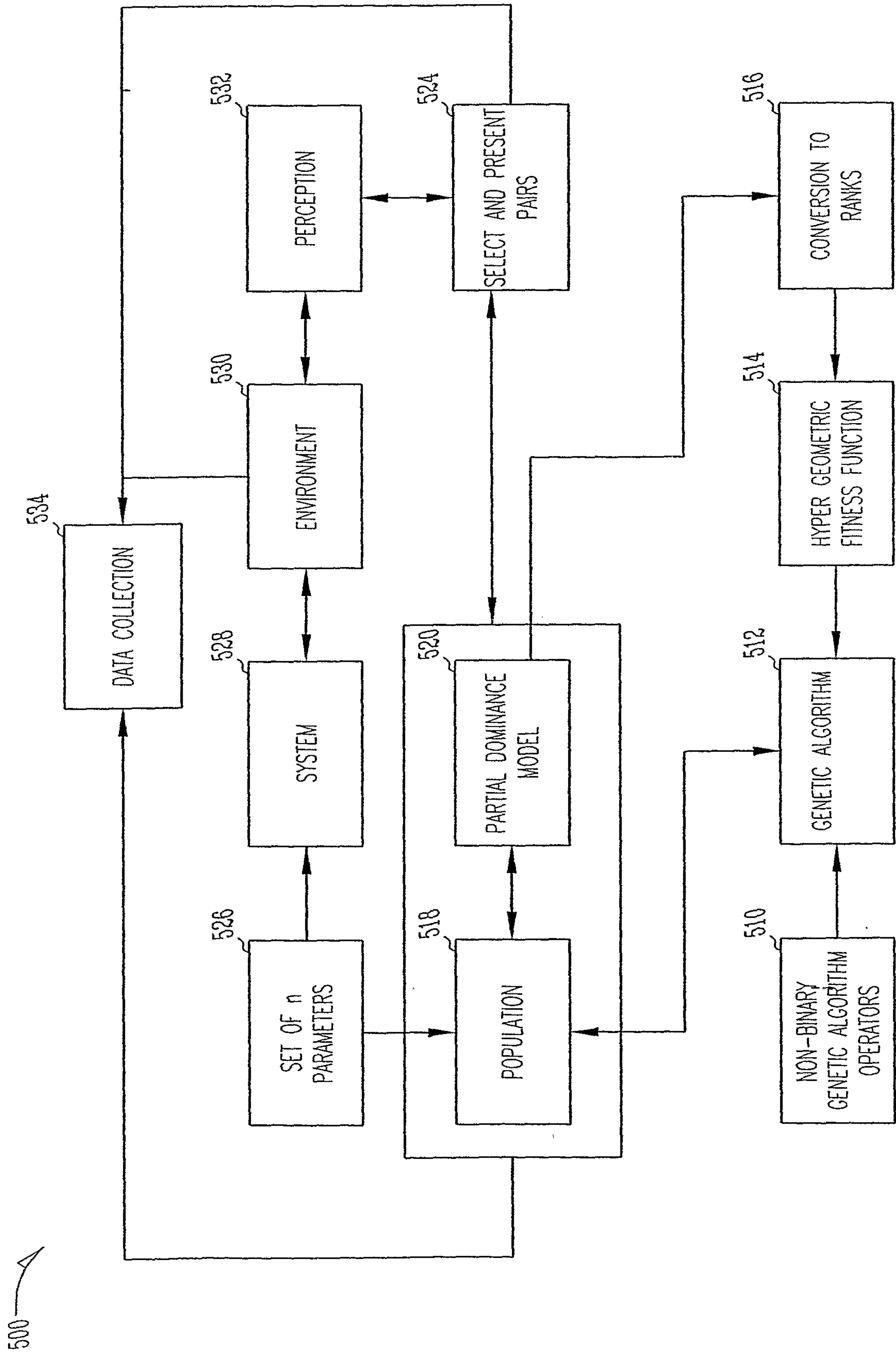


Fig. 5

