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[54]	CONTOURED ULTRASONIC DELAY LINE	
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[51]	Int. Cl	H03h 9/26, H03h 9/30
[58]	Field of Se	arch 333/30 R, 30 M, 72;
-		310/8.1, 8.3, 8.5, 8.6
[56]		References Cited

**UNITED STATES PATENTS** 

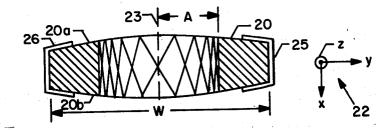
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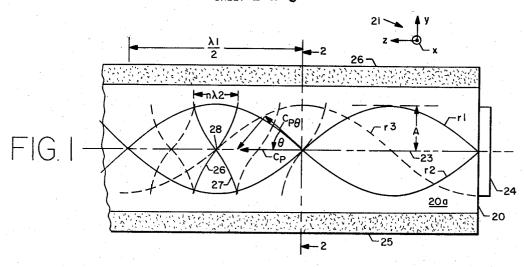
## [57] ABSTRACT

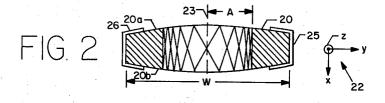
A delay line comprising a strip of ultrasonic solid material having a pair of elongated and generally convex major surfaces to form a contoured cross section. Acoustic wave propagation between the major surfaces is confined to a region which extends a distance A in both directions from the center of the strip along the width or transverse dimension, where A is less than one-half of the width and is a function of the acoustical wavelength.

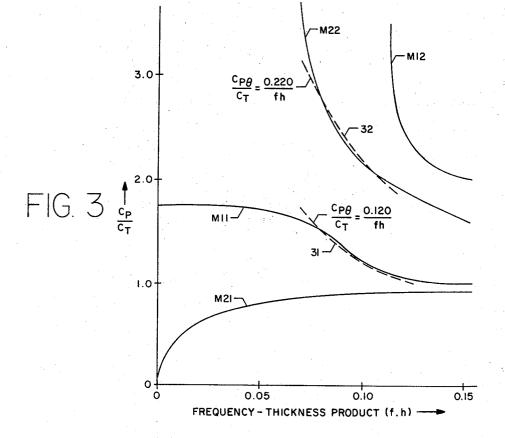
# 8 Claims, 10 Drawing Figures



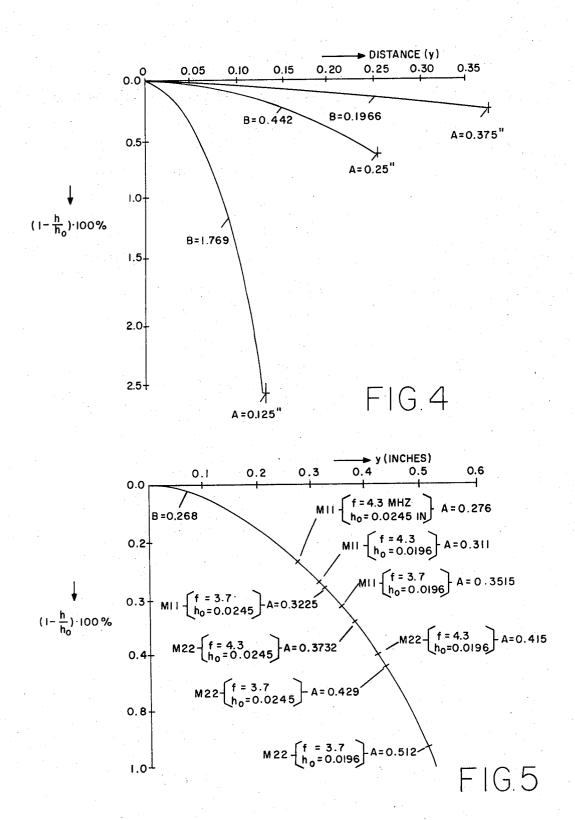
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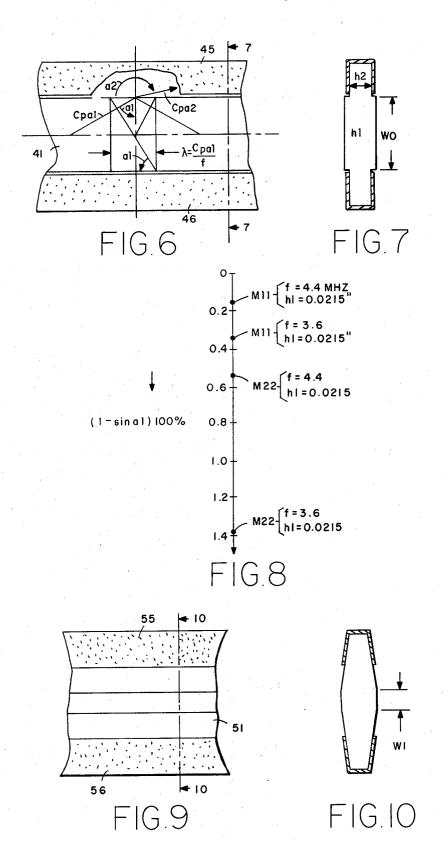






# SHEET 2 OF 3





### CONTOURED ULTRASONIC DELAY LINE

#### **BACKGROUND OF THE INVENTION**

#### A. Field of the Invention

This invention relates to delay devices and in particular to solid ultrasonic delay lines.

Ultrasonic delay lines are generally operable to provide either a nondispersive or a dispersive delay of continuous wave or pulse type signals. The terms dispersive 10 and nondispersive refer to the delay versus frequency characteristic of a delay line. If delay changes with frequency, the line is said to be dispersive. On the other hand, if the delay is constant, or nearly so, for all frequencies, the line is termed nondispersive.

#### B. Prior Art

The propagation of continuous waves in solid plates is described in chapter 5 of the reference book chanical Waveguides" by Martin Redwood, Pergamon Press, 1960. This description is based upon the premise 20 ters denote like elements of structure; and that in a uniform thickness sheet of infinite width there is no variation of acoustical particle displacement in the width of y direction. A close approximation of actual performance to this theory has been realized by the application of absorbing tape to the edges of a finite 25 width metallic strip (e.g., aluminum or aluminum alloy) such that there are no edge reflections which interfere with wave propagation in the central (untaped) portion of the strip. Such a delay line is described by T.R. Meeker in an article entitled "Dispersive Ultra- 30 sonic Delay Lines Using the First Longitudinal Mode in a Strip," IRE Transactions, Volume UE-7, No. 2, June, 1960. A disadvantage of this strip design is that in accordance with diffraction theory, there is appreciable beam spreading in the width or y direction such that a 35 7-7 of FIG. 6; large amount of acoustic energy is absorbed by the tape, thereby resulting in relatively high acoustic losses.

Acoustic delay lines or waveguides of various cross sections, such as circles, rectangles and elipses, not employing absorbing means along the length thereof, have been studied as exemplified by Chapter 6 of the aforementioned Redwood reference. Dispersive delay lines have also been made of wire as evidenced by the article of J.E. May entitled "Wire Type Dispersive Ultrasonic 45 Delay Lines," IRE Transactions, Volume UE-7, No. 2, June, 1960. While these delay lines do not suffer the loss due to absorbing tape, other problems have been encountered. For example, the very small area of the piezoelectric transducers on wire type dispersive lines 50 have limited their use to relatively low frequencies. In addition, the interference of unwanted modes of propagation have prevented smooth transmission over a wide band of frequencies.

## BRIEF SUMMARY OF THE INVENTION

An object of the present invention is to provide a novel and improved acoustic delay line.

Another object is to provide a novel and improved delay line in which there is negligible beam spreading loss

Yet another object is to provide a novel and improved acoustic delay line of high efficiency in which unwanted modes of wave propagation are suppressed. 65

Briefly, an acoustic delay line embodying the present invention is comprised of a strip of ultrasonic transmis-

sion material having a pair of elongated and convex major surfaces to form a contoured cross section with a width W many times greater than the thickness h. When a beam of acoustic waves is applied to the strip, 5 the wave propagation between the major surfaces is confined to a region which extends a distance A in both directions from the center of a strip along the width dimension. A is less than one half of the width and is a function of the acoustical frequency and phase velocity of the acoustic waves. Since the phase velocity characteristics of the undesired modes differ from those of the desired mode, the parameter A is generally larger for the unwanted or spurious propagation modes. By properly positioning the inside edge of the absorbing tape, 15 it is possible to suppress the unwanted modes of propagation.

#### BRIEF DESCRIPTION OF THE DRAWING

In the accompanying drawings like reference charac-

FIG. 1 is a plan view of a portion of an acoustic delay line embodying the present invention;

FIG. 2 is a cross sectional view taken along the lines 2-2 of the FIG. 1 delay line;

FIG. 3 is a plot of the ratio of phase velocity to transverse velocity versus the frequency and thickness product for an aluminum strip delay line;

FIG. 4 is a graph showing exemplary contours for delay lines embodying the present invention;

FIG. 5 is a plot of another exemplary contour for a delay line embodying the present invention;

FIG. 6 is a plan view of a portion of a contoured delay line which is a further embodiment of the invention;

FIG. 7 is a cross sectional view taken along the lines

FIG. 8 is a line graph illustrating the boundaries of wave propagation for different longitudinal modes;

FIG. 9 is a plan view of a portion of another contoured delay line embodiment of the invention; and FIG. 10 is a cross sectional view of the FIG. 9 embodiment.

## DESCRIPTION OF PREFERRED EMBODIMENT

Referring now to FIGS. 1 and 2 there is shown a portion of a contoured delay line 20 embodying the present invention. The length, width and heighth of the line 20 extend in the z, y and x directions, respectively, which directions are depicted at 21 and 22 in FIGS. 1 and 2, respectively. The width W (FIG. 2) is many times greater than the maximum height along the x direction. Although the line 20 may consist of any ultrasonic transmission material, it preferably takes the form of an elongated thin strip of aluminum or aluminum alloy. The total length of the strip is a function of delay required in any desired application. Preferably, the line thickness is tapered throughout the length of the strip so as to enhance the frequency range over which linear dispersive operation occurs.

Conventional piezoelectric ceramic transducers in the form of rectangular bars are bonded to the end faces of the strip, only one of which is shown at 24 in FIG. 1. These transducers are poled in the thickness direction, electroded, and soldered to the line with the poling direction parallel to the length of the strip so as to produce and respond to vibrations in a thicknesslongitudinal-mode. Accordingly, when one of the transducers is excited by an alternating voltage applied to the electroded areas of the major surfaces thereof, a thickness-longitudinal-mode of vibration is induced therein. This vibration in turn produces an elastic wave motion in the strip which propagates down the line. When the propagated energy reaches the transducer at the opposite end, a thickness-longitudinal-mode of vibration is induced therein and converted by the transducer to electrical energy. As will be clear to those skilled in the art, the electrical and physical connections at each of the ends of the line are similar and therefore either transducer can be used as the input or output, i.e., the line is completely reciprocal.

In accordance with the present invention, the strip thickness is given a contour in which the maximum thickness occurs at the center of the strip. In the embodiment illustrated in FIGS. 1 and 2, the contour takes the form of a convex continuous shape in which the maximum thickness occurs at the center line 23 of the strip. Due to the contour, the elastic wave propagation in the z direction is confined to an area which extends a distance A on either side of the center line 23. As best seen in FIG. 2, the reflection angle of an elastic wave between the contoured major surfaces 20a and 20b is maximum at or near the center line 23 and becomes gradually smaller until at a distance A it becomes zero and reverses itself. That is, the contouring of the major surfaces tends to set up points of reflection at a distance A on either side of the center line 23 so that the propagation of an elastic wave is confined to 30 pressed as follows: this region.

As will become apparent thereinafter, the distance A turns out to be smaller for wave propagation in the first longitudinal mode M11 than for propagation in the undesired modes M12, M21 and M22. As a result, the placement of the edges of a pair of absorber tapes 25 and 26 can be chosen so as to suppress wave propagation in the undesired modes.

In the discussion which follows, it is assumed that the x, y and z coordinate axes are superimposed upon the 40 strip 20 so that the center line 23 becomes the x - z plane. Using a ray method of analysis, assume that two rays,  $r_1$  and  $r_2$ , shown in FIG. 1, are symmetrical about the center line 23. These rays travel in three dimensions as follows: (a) move in the x direction by alternate reflection between the major surfaces x00 and x00 of the strip in a manner shown in FIG. 2; (b) progress from side to side of the strip (x00 direction) as shown in both FIGS. 1 and 2; and (x00 have an overall resultant propagation along the length of the strip (x20 direction).

The lateral or y position of each ray at any instant of time can be expressed as a sine function of the distance along the strip length or z direction as follows:

$$y = A \sin \beta z$$

where  $\beta = 2\pi/\lambda 1$ ,  $\lambda 1$  is the wavelength of the sine wave along z and A is the amplitude of the sine function and distance to extremity of a particular mode of acoustic propagation from the centerline 23 or x - z plane.

The phase velocity directed along the sine curve of FIG. 1 and parallel to the y-z plane of the strip is designated  $C_{p\theta}$ . The phase velocity directed along the strip length (z-axis) is designated  $C_p$ .  $C_p$  also represents the phase velocity of the acoustic wave propagation along the strip.

As the phase front 26 of the ray  $r_1$  moves along the sine curve, the longitudinal phase velocity  $C_p$  is larger than the tangential phase velocity  $C_{p\theta}$  along the sine curve and is related to it in the following way:

$$C_{p\theta} = C_p \cos \theta$$

(2)

where  $\theta$  is the angle of the phase velocity vector,  $C_{p\theta}$ , relative to the z-axis.

A necessary condition for single-mode propagation in a wave guide of any sort is that the phase velocity  $C_p$  be uniform over the entire cross sectional area of the guide. It is hence necessary that the phase velocity along a third ray,  $r_3$ , be the same as  $C_p$ . However, since for  $r_3$  at the line 2-2,  $\theta=0$ ,  $C_{p\theta}=C_p$ , so that the condition is fulfilled. In other words, for constant  $C_p$ ,  $C_{p\theta}$  must be a cosine function of  $\theta$  in accordance with equation (2).

By inspection of the  $C_{p\theta}$  and  $C_p$  vector diagram in FIG. 1,  $\tan \theta = dy/dz$ . The first derivative of equation (1) with respect to z is  $\beta A \cos \beta z$ . From equation (1)  $\sin \beta z = y/A$ . Accordingly,  $\tan \theta$  can be expressed as follows:

$$\tan \theta = dy/dz = \beta \quad \sqrt{A^2 - y^2} = \beta A \quad \sqrt{1 - y^2/A^2}$$
(3)

From equation (3) it is evident that  $\cos \theta$  can be expressed as follows:

$$\cos \theta = \sqrt{\beta^2 (A^2 - y^2) + 1} \tag{4}$$

Substituting equation (4) into equation (2), the ratio  $\overline{C_p/C_{p\theta}}$  can be expressed as follows:

$$\overline{C_p/C_{p\theta}} = \sqrt{\beta^2 (A^2 - y^2) + 1}$$
(5)

The mode of propagation described herein is assumed to be symmetrical about the x - z plane as well as about the y - z plane. Referring to FIG. 1, this requires that the phase fronts 26 and 27, which intersect at the center line 23 at point 28, be in phase with each other. This requires at  $y = \pm A$  that the phase fronts 26 and 27 be separated by  $n \lambda 2$ , where n is any positive integer and  $\lambda 2 = C_p/f$  and f is the acoustic frequency.

The analytic formula for the phase front (26 or 27) may be obtained in the following manner. Since, for any value of y, the phase front must be orthogonal to the direction of a ray, the slope of the phase front must be the negative inverse of the slope of the ray. Since the slope of the ray is given by equation (3), the curve zl for the phase front is given by

$$dzl = -\beta \quad \sqrt{A^2 - y^2 \, dy} \tag{6}$$

Integrating both sides of equation (6);

$$zl = -\beta [y/2 \quad \sqrt{A^2 - y^2} + A^2/2 \sin^{-1} y/A]$$
(7)

Assuming that the origin of the coordinate axes 21 coincides with the point 28 in FIG. 1 so that the phase fronts 26 and 27 are symmetrical about the x - y plane

and setting y = to A in equation (7), the following expression can be written for zl

$$zl = -\beta[\pi A^2/4] = n\lambda 2/2$$

Ignoring the minus sign and setting n=1 for the first mode,  $\beta$  can be expressed as follows:

$$\beta = 2\lambda 2/\pi_A 2$$

Substituting  $\beta = 2\pi/\lambda 1$  into equation (9),  $\lambda 1$  is given by

$$\lambda 1 = \pi^2 A^2 / \lambda 2$$

(10)

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The phase velocity of the first and second longitudinal acoustic modes in a strip of uniform thickness, h, and a radian frequency, w, has been shown in the aforementioned Meeker reference to be obtainable from a solution of the following frequency equation:

$$\frac{\tan\left[\frac{wh}{2C_{t}}\left(1-\frac{C_{t}^{2}}{C_{p}^{2}}\right)^{\frac{1}{2}}\right]}{\tan\left[\frac{wh}{2C_{d}}\left(1-\frac{C_{d}^{2}}{\overline{C_{p}^{2}}}\right)^{\frac{1}{2}}\right]} = \frac{1}{\left(2-\frac{C_{d}^{2}}{C_{p}^{2}}\right)^{\frac{1}{2}}} = \frac{1}{\left(1-\frac{\beta^{2}A^{2}}{2}\right)} = \frac{1}{\left(1-\frac$$

In FIG. 3 the curves designated M11 and M12 are plotted solutions for the first and second longitudinal (symmetric modes) M11 and M12. Also plotted in FIG. 3 are curves representing the first and second asymmetric modes M21 and M22. These modes are described and the frequency equations given in Chapter 5 of the aforementioned Redwood reference. The curves in FIG. 3 are plotted for Poisson's ratio  $\rho = 0.355$ , and transverse velocity  $C_t = 0.1215$  in/ $\mu$ scc.

If  $C_p$  in FIG. 3 and in equation (11) is replaced by  $C_{p\theta}$ , the dependence of  $C_{p\theta}$  on thickness for any fre- 50 quency can be found. Also in FIG. 3 it can be seen that in the frequency-thickness product range of interest (0.072 - 0.105), the curves for the M11 and M22 modes can be closely approximated by the dashed hyperbolic curves 31 and 32, respectively. These approxi-55 mate hyperbolic curves for the M11 and M22 modes may be expressed in equations (12) and (13) respectively, as follows:

$$C_{iji}/C_i = 0.1200/fh$$

(12)

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 $C_{un}/C_{t} = 0.220/fh$ 

Utilizing either equation (12) or equation (13) and allowing the thickness at y=A to be  $h_A$ , the ratio of h to  $h_A$  can be given by:

$$h/h_A \cong \overline{C}_p/\overline{C}_{p\theta} = 1/\cos\theta = \sec\theta = \sqrt{\beta^2 (A^2 - y^2) + 1}$$

When the thickness h has its maximum value of  $h_0$  at y=0, equation (14) can be rewritten as follows:

$$h_0/h_A = \sec \theta_{max} = \sqrt{\beta^2 A^2 + 1}$$
 (15)

The thickness h at any value of y can be related to the center thickness  $h_0$  as follows:

$$h/h_0 = h/h_A \cdot h_A/h_0 = \sec \theta/\sec \theta_{max} = \frac{\sqrt{\beta^2(A^2 - y^2) + 1/\beta^2 A^2 + 1}}{\sqrt{\beta^2(A^2 - y^2) + 1/\beta^2 A^2 + 1}}$$

$$\sqrt{\beta^2(A^2-y^2)+1/\beta^2A^2+1}$$

(16)

Both A and  $\beta$  are fractions such that  $\beta^2$  A<sup>2</sup> is much less than 1 so that terms including  $A^4$  and/or  $\beta^4$  can be neglected. As a result, the radical expression of

$$\sqrt{\beta^2 A^2 + 1}$$

can be simplified as follows:

$$\sqrt{\beta^2 A^2 + 1} \cong \sqrt{1 + \beta^2 A^2 + \beta^4 A^4 / 4} = 1 + \beta^2 A^2 / 2$$

A still further approximation of equation (17) can be made as follows:

$$\frac{1}{1 + \frac{\beta^2 A^2}{2}} = \frac{\left(1 - \frac{\beta^2 A^2}{2}\right)}{\left(1 + \frac{\beta^2 A^2}{2}\right)\left(1 - \frac{\beta^2 A^2}{2}\right)}$$
$$= \frac{1 - \frac{\beta^2 A^2}{2}}{1 - \frac{\beta^4 A^4}{2}} \cong 1 - \frac{\beta^2 A^2}{2}$$

Utilizing equations (17) and (18), equation (16) can be rewritten as follows:

$$h/h_0 \cong (\beta^2 A^2/2 - \beta^2 y^2/2 + 1) (1 - \beta^2 A^2/2)$$
(19)

Multiplying out the two terms on the right hand side of equation (19) and neglecting terms including  $\beta^4$  and/or A<sup>4</sup>, equation (19) can be written as follows:

$$h/h_0 \cong 1 - \beta^2 y^2/2 \tag{20}$$

The percentage reduction from the center thickness  $h_0$  is found from equation (20) to be:

$$(1 - h/h_0) \cdot 100\% = \beta^2 y^2 / 2 \cdot 100\%$$

Equations (20) and (21) basically describe a parabolic function such that the contour is approximately parabolic in shape and independent of the distance A. The percent reduction from the center thickness as given by equation (21) is plotted in FIG. 4 for a frequency-thickness product of 0.085 MHz inches (the frequency being equal to 4 MHz.) for values of A= 0.125, 0.250 and 0.375 inches and corresponding val7

ues of  $\beta = 1.769$ , 0.442 and 0.1966, respectively. The points on these curves can be calculated as follows. First,  $C_p$  is calculated from equation (12) by employing a measured value of the transverse velocity  $C_t = 0.1215$ inches/microseconds. Next, the value of  $\beta$  is calculated from equation (9) with the value of  $\lambda 2$  being equal to  $C_p/f$  or 0.0434. Then, equation (21) can be employed to calculate different values of the quantity  $(1-h/h_0)$ 100 percent for different values of y. Having once selected a value of  $\beta$ , and thus established a desired contour (e.g., one similar to one of the three curves in FIG. 4) at a midband frequency, it is, of course, desirable to find the values of A at the extremes of the frequency range of interest. The value of A for each new wavelength or frequency is then computed directly from 15 equation (9).

With reference again to FIG. 3, two additional or spurious modes M21 and M22 exist in the range of interest. The first asymmetric mode M21 has a positive slope in this range and, hence, is subject to the normal beam spreading loss occurring in a flat or uncontoured delay line strip. However, the reasoning developed above for the M11 mode applies equally to the M22 mode except that the latter mode is asymmetric about the cener y - z plane. In addition, this mode is closely approximated by the inverse relationship given in equation (13).

In FIG. 5 there is plotted a contour for  $\beta = 0.268$ , utilizing equation (21). It is assumed that this contour is to be employed for all sections of a tapered delay line strip, the extreme thicknesses of which are:  $h_0 = 0.0245$ and 0.0196 inches. The values of A have been calculated and plotted on the contour for frequency values of 4.3 and 3.7 MHz. for both thickness values in both the M11 and M22 modes, utilizing equations (9), (12) and (13). By inspection, it can be seen that all the points representing the A values of the spurious mode M22 lie further from the center line than all the points representing the A values of the desired mode M11. It is therefore possible, by positioning the inside edge of the absorbing tapes 25 and 26 (FIGS. 1 and 2) to cover the extremities of the undesired spurious mode (while not covering the extremities of the desired mode). to selectively absorb out the unwanted acoustic wave 45 propagation in the M22 mode. For the example given, the edge of the absorbing tape 25 or 26 should be placed at a distance of about 0.36 inches from the center of the strip for both of the delay line sections.

When different thicknesses are employed to accomplish a more linear delay change over a wider frequency bandwidth, it is possible to change the lateral position of the absorbing tape for different thicknesses of the strip so as to more effectively separate the wanted from the unwanted signals. That is, the edge of the absorbing tape need not be at the same distance from the center line of the strip for different thicknesses thereof.

The foregoing analysis is heuristic in nature and is not presented as a rigorous treatment of three dimensional wave motions. Experimental results, however, have agreed closely with results predicted from the graphs. Improvements in the continuous wave loss at center frequency of a 4 MHz., 2,500 micro-second aluminum strip dispersive delay line have been as much as 10 decibels as compared to an uncontoured delay line strip of similar design.

The contouring of a delay line strip may be accomplished by etching in from the edges of the strip by lay-

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ing a loosely coiled delay line strip in an empty tank and filling the tank with the etchant at a slow linear rate up to the center line of the strip. The coil is turned over and the operation repeated for the other edge. In using this technique, the transverse taper produced in one example was 0.0003 inches at plus or minus 0.375 inches from the center of the strip.

It has been further discovered that a workable contour can be achieved by rolling 1.75 inch wide and 0.05 inch thick aluminum strip stock through a two high rolling mill which is set for 40 to 50 percent reduction in thickness of the strip and which has a roll diameter of four inches and an axial roll length of six inches. The contour thus achieved can then be measured and plotted to produce a graph similar to that shown in FIG. 5. The values of  $\beta$  and A can then be calculated for the frequency range of interest.

In other embodiments of the invention, the contour need not be continuous by may have discontinuities. Thus, the delay line strip portion shown in FIG. 6 has a transverse stepped contour such that the central portion of width Wo has a thickness h1 and the two edge sections have a thickness h2 which is smaller than h1. The two edge sections are also covered with absorbing tape 45 and 46.

If a ray of an acoustic wave traveling at a phase velocity  $C_{pa1}$  in the strips strikes the step at an angle of incident a1, it may continue to travel in the edge section at a refracted angle a2 and phase velocity  $C_{pa2}$  or be totally reflected into the central portion at the angle a1. Snell's Law applies in this case as follows:

$$\sin a_1 / \sin a_2 = C_{pa_1} / C_{pa_2}$$
(22)

In addition, the phase velocities  $C_{pa1}$  and  $C_{pa2}$  are related to the frequency and thicknesses h1 and h2 in accordance with FIG. 3. The angle a1 beyond which total reflection occurs is found by setting  $\sin a2 = 1$ . Also, if the inverse relationships shown in FIG. 3 are assumed, the thickness ratio in terms of a1 is given as follows:

$$\sin a 1 = C_{pa_1}/C_{pa_2} = h2/h1$$
(23)

In FIG. 8 the percentage thickness reduction,  $(1-\sin aI)$  100 percent is plotted on a line graph for two frequencies (3.6 and 4.4 MHz.) for both the M11 and M22 modes with h1 = 0.0215 inches. Thus, by controlling the thickness ratio h2/h1 (as for example, a reduction of 0.45 percent), the acoustic wave propagation in the desired M11 mode may be guided into the central portion of the strip while the suprious M22 mode wave propagation can be made to excape into the edge sections and be absorbed by the tape.

In FIGS. 9 and 10 there is illustrated a portion of another delay line strip 51 having a further discontinuous type contour embodying the present invention. In this contour, the edges of the strip are reduced with a linear taper leaving a flat width W1 in the center of the strip. This type of contour also includes the case where the width of the flat section W1 is reduced to zero. It should be evident that other contours having curvatures somewhat different from the embodiment shown in FIGS. 1, 2, 6, 7, 9 and 10 may be employed so long as the center thickness is larger than the thickness at the edges of the strip.

What is claimed is:

- 1. A delay line comprising
- a strip of ultrasonic transmission material having a pair of elongated and generally convex major surfaces to form a contoured cross section with a 5 width W many times greater than the thickness h;
- means for applying a beam of acoustic waves to said strip whereby acoustic wave propagation between the major surfaces is confined to a region which ex- 10 contour is generally continuous. tends a distance A in both directions from the center of the strip along the width dimension, where A < W/2.
- 2. A delay line as set forth in claim 1 wherein said beam applying means includes a transducer poled in 15 the longitudinal mode affixed to one end thereof and means for applying electrical signals to said transducer.
- 3. A delay line as set forth in claim 2 and further including
  - absorbing tape means wrapped around the minor sur- 20 faces of said strip and extending inwardly along said major surfaces toward the center of the strip a distance less than W/2 - A.
  - 4. A delay line as set forth in claim 2 wherein A is a function of both the acoustical wave- 25

- length and the acoustical phase velocity such that its values throughout the frequency band of interest are smaller for the longitudinal mode M11 than for the mode M22; and
- wherein the edges of said absorbing tape means are positioned so as to absorb acoustical wave propagation in the M22 mode and to allow acoustical wave propagation in the M11 mode.
- 5. A delay line as set forth in claim 4 wherein said
  - 6. A delay line as set forth in claim 4 wherein said contour includes a central section having a uniform thickness h1 and a pair of edge sections each of thickness h2; and
  - wherein the edges of said absorbing tape means are positioned along the edge sections.
    - 7. A delay line as set forth in claim 4
    - wherein said contour has a central position of uniform thickness and width W1, where W1<W, and a pair of tapered edge sections.
    - 8. A delay line as set forth in claim 4
    - wherein said contour includes a pair of tapered sections which have their maximum thickness at the center of the strip.

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