Title: SYSTEM AND METHODS FOR POSITIONING A MANIPULATOR ARM BY CLUTCHING WITHIN A NULL-PERPENDICULAR SPACE CONCURRENT WITH NULL-SPACE MOVEMENT

Abstract: Devices, systems, and methods for positioning an end effector or remote center of a manipulator arm by floating a first set of joints within a null-perpendicular joint velocity sub-space and providing a desired state or movement of a proximal portion of a manipulator arm concurrent with end effector positioning by driving a second set of joints within a null-space orthogonal to the null-perpendicular space. Methods include floating a first set of joints within a null-perpendicular space to allow manual positioning of one or both of a remote center or end effector position within a work space and driving a second set of joints according to an auxiliary movement calculated within a null-space according to a desired state or movement of the manipulator arm during the floating of the joints. Various configurations for devices and systems utilizing such methods are provided herein.
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SYSTEM AND METHODS FOR POSITIONING A MANIPULATOR ARM BY CLUTCHING WITHIN A NULL-PERPENDICULAR SPACE CONCURRENT WITH NULL-SPACE MOVEMENT

CROSS-REFERNCES TO RELATED APPLICATIONS

[0001] This application is a Non-Provisional of and claims the benefit of priority from U.S. Provisional Patent Application No. 61/799,920 filed on March 15, 2013 and entitled "Systems and Methods for Positioning a Manipulator Arm by Clutching within a Null-Perpendicular Space Concurrent with Null-Space Movement" (Attorney Docket No. ISRG03900PROV/US), the full disclosure of which is incorporated herein by reference.


BACKGROUND OF THE INVENTION

[0003] The present invention generally provides improved surgical and/or robotic devices, systems, and methods.

[0004] Minimally invasive medical techniques are aimed at reducing the amount of tissue which is damaged during diagnostic or surgical procedures, thereby reducing patient recovery time, discomfort, and deleterious side effects. Millions of "open" or traditional surgeries are performed each year in the United States; many of these surgeries can potentially be
performed in a minimally invasive manner. However, only a relatively small number of surgeries currently use minimally invasive techniques due to limitations in surgical instruments, and techniques, and the additional surgical training required to master them.

[0005] Minimally invasive telesurgical systems for use in surgery are being developed to increase a surgeon's dexterity as well as to allow a surgeon to operate on a patient from a remote location. Telesurgery is a general term for surgical systems where the surgeon uses some form of remote control, e.g., a servomechanism, or the like, to manipulate surgical instrument movements rather than directly holding and moving the instruments by hand. In such a telesurgery system, the surgeon is provided with an image of the surgical site at the remote location. While viewing typically a three-dimensional image of the surgical site on a suitable viewer or display, the surgeon performs the surgical procedures on the patient by manipulating master control input devices, which in turn control the motion of robotic instruments. The robotic surgical instruments can be inserted through small, minimally invasive surgical apertures to treat tissues at surgical sites within the patient, often the trauma associated with accessing for open surgery. These robotic systems can move the working ends of the surgical instruments with sufficient dexterity to perform quite intricate surgical tasks, often by pivoting shafts of the instruments at the minimally invasive aperture, sliding of the shaft axially through the aperture, rotating of the shaft within the aperture, and/or the like.

[0006] The servomechanism used for telesurgery will often accept input from two master controllers (one for each of the surgeon's hands) and may include two or more robotic arms or manipulators. Mapping of the hand movements to the image of the robotic instruments displayed by the image capture device can help provide the surgeon with accurate control over the instruments associated with each hand. In many surgical robotic systems, one or more additional robotic manipulator arms are included for moving an endoscope or other image capture device, additional surgical instruments, or the like.

[0007] A variety of structural arrangements can be used to support the surgical instrument at the surgical site during robotic surgery. The driven linkage or "slave" is often called a robotic surgical manipulator, and exemplary linkage arrangements for use as a robotic surgical manipulator during minimally invasive robotic surgery are described in U.S. Patent Nos. 6,758,843; 6,246,200; and 5,800,423, the full disclosures of which are incorporated herein by reference. These linkages often make use of a parallelogram arrangement to hold an instrument having a shaft. Such a manipulator structure can constrain movement of the instrument so that the instrument shaft pivots about a remote center of spherical rotation.
positioned in space along the length of the rigid shaft. By aligning this center of rotation with the incision point to the internal surgical site (for example, with a trocar or cannula at an abdominal wall during laparoscopic surgery), an end effector of the surgical instrument can be positioned safely by moving the proximal end of the shaft using the manipulator linkage without imposing potentially dangerous forces against the abdominal wall. Alternative manipulator structures are described, for example, in U.S. Patent Nos. 6,702,805; 6,676,669; 5,855,583; 5,808,665; 5,445,166; and 5,184,601, the full disclosures of which are incorporated herein by reference.

[0008] While the new robotic surgical systems and devices have proven highly effective and advantageous, still further improvements would be desirable. For example, a manipulator arm may include additional redundant joints to provide increased movements or configurations under certain conditions. When moving surgical instruments within a minimally invasive surgical site, however, these joints may exhibit a significant amount of movement outside the patient, often more movement than needed or expected, particularly when pivoting instruments about minimally invasive apertures through large angular ranges. Alternative manipulator structures have been proposed which employ software control over a highly configurable kinematic manipulator joint set to restrain pivotal motion to the insertion site while inhibiting inadvertent manipulator/ manipulator contact outside the patient (or the like). These highly configurable "software center" surgical manipulator systems may provide significant advantages, but may also present challenges. In particular, the mechanically constrained remote-center linkages may have safety advantages in some conditions. Additionally, the wide range of configurations of the numerous joints often included in these manipulators may result in the manipulators being difficult to manually set-up in a configuration that is desirable for a particular procedure. Nonetheless, as the range of surgeries being performed using telesurgical systems continues to expand, there is an increasing demand for expanding the available configurations and the range of motion of the instruments within the patient. Unfortunately, both of these changes can increase the challenges associated with the motion of the manipulators outside the body, and can also increase the importance of avoiding excessive movement of the manipulators arm for certain tasks.

[0009] For these and other reasons, it would be advantageous to provide improved devices, systems, and methods for surgery, robotic surgery, and other robotic applications, and it would be particularly beneficial if these improved technologies provided the ability to provide more consistent and predictable movement of the manipulator arm during set-up or
positioning of the manipulator. It would be further desirable to provide such improvements while increasing the range of motion of the instruments for at least some tasks and without significantly increasing the size, mechanical complexity, or costs of these systems, and while maintaining or improving their dexterity.

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BRIEF SUMMARY OF THE INVENTION

[0010] The present invention generally provides improved robotic and/or surgical devices, systems, and methods. In many embodiments, the invention will employ highly configurable surgical robotic manipulators. These manipulators, for example, may have more degrees of freedom of movement than the associated surgical end effectors have within a surgical workspace. A robotic surgical system in accordance with the present invention typically includes a manipulator arm supporting a robotic surgical instrument and a processor to calculate coordinated joint movements for manipulating an end effector of the instrument. The joints of the robotic manipulators supporting the end effectors allow the manipulator to move throughout a range of different configurations for a given end effector position and/or a given pivot point location. In one aspect, the invention provides improved movement of the manipulator arm by floating one or more joints within a null-perpendicular space to allow a distal portion of the manipulator arm to be repositioned, such as the distal end effector and/or remote center, while one or more joints are driven within a null-space to effect various other tasks or desired movements, such as collision avoidance or driving the arm toward a desired pose.

[0011] In one aspect, the robotic surgical system may utilize one or more clutch modes in which one or more joints are allowed to float along one or more axes (e.g. one or more degrees-of-freedom) within a joint velocity sub-space that results in movement of a distal portion of the manipulator, such as an end effector or distal end effector or a remote center about which an instrument shaft of the end effector pivots adjacent a minimally invasive aperture during surgery. This joint velocity sub-space is referred to as a null-perpendicular space, which is orthogonal to a null-space in which movement of the joints results in no change in state of the end effector and/or remote center. Since the manipulator arm is highly configurable, often including redundant joints such that a range of configurations and joints states are available for a given state of the end effector or remote center, movement of distal portion, such as an end effector, during set-up may result in undesirable movement of proximal portions of the manipulator arm resulting in poorly conditioned configurations or collisions between the manipulator arm and adjacent arms or personnel. For example, when
inserting or positioning the tool tip or distal end effector of the manipulator within a cannula at the minimally invasive aperture before surgery, referred to herein as "docking," movement of the tool tip or end effector may results in undesirable movement of the more proximal portions of the manipulator arm. Thus, in one aspect, the invention provides improved movement of the manipulator by floating of one or more joints within the null-perpendicular space so that a user or patient side assistance can manually backdrive or reposition the end effector and/or the remote center during surgery, while movement of one or more other joints of the manipulator are driven within a null-space so as to provide improved movement of proximal portions of the manipulator arm by effecting various other tasks, such as collision avoidance, movement toward a desired pose, or movement according to various algorithms using the null space (the null-space moving with the end effector or remote center). This aspect simplifies set-up of the manipulator arm by allowing the patient-side assistant to "dock" the end effector within the cannula to prepare for surgery without driving or manipulating each other joint of the manipulator arm. This aspect is particularly useful in highly configurable manipulator arms, especially manipulator arms having redundant joints and manipulator arms utilizing a Jacobian based controller in which the primary calculations of the one or more joints are based on velocities rather than positions. These features may be utilized as a clutch feature or clutch mode (e.g. null-perpendicular float clutch) separately or in combination with various other clutching modes or any of the movements described herein. In addition, various aspects of the feature described above may be incorporated into one or more of the movements or modes described herein.

[0012] In some embodiments, a manipulator arm may include additional redundant joints that allow for various types of movements within a null-space, such as an auxiliary movement to avoid collisions, move toward a desired pose or to improve conditioning of the joints. In some embodiments, rather than relying on robotic devices that are mechanically constrained to pivot a tool about a fixed point in space, or robotic devices having passive joints which passively pivot about the tissues of a minimally invasive aperture, the present invention may calculate a motion that includes pivoting a link of the manipulator linkage about an aperture site. The degrees of freedom of the robotic linkages supporting the end effectors can allow the linkage to move throughout a range of configurations for a given end effector position, and the systems may drive the linkages to configurations which inhibit collisions involving one or more moving robotic structures. Set-up of highly flexible robotic linkages can be facilitated by processors which drive one or more joints of the linkage while the linkage is being manually positioned. Joint state sensors may be used to sense the
manual backdriving movement of the floating joints for use in subsequent calculated joint movements.

[0013] In some embodiments, the invention allows for floating of a first set of joints to allow a patient-side assistant to manually backdrive the end effector or a remote center about which the end effector pivots to a desired position (e.g., location or alignment), while a second set of joints are driven to move the manipulator arm according to a desired state or movement. This aspect is accomplished by driving the first set of joints to float within a null-perpendicular space, while the second set of joints are driven within a null-space to effect one or more auxiliary tasks, such as collision avoidance, pose preference or other desired movements. The system senses movement of the floating joints during manual moving of the joints so as to determine the null-space in which the auxiliary movement of the second set of joints is calculated. It should be noted that the manipulator arm need not be mechanically "locked" to a set of constraints, if used, but rather a set of constraints can be utilized to direct movement of one or more joints of the manipulator arm when moving within the null-space.

[0014] In general, manually backdriving "floating joints" results in movement of various other joints in response and may result in undesirable movement of one or more joints, such as a collision between the manipulator arm and an adjacent arm or personnel, excessive movement, or movement toward an undesirable or a poorly conditioned pose. Manually backdriving a portion of the manipulator arm may utilize the same joints as used in manipulation of the end effector or may include various other selected joints or sets of joints. To provide improved movement of the manipulator arms, the redundant degrees of freedom may be used to determine a movement of the manipulator arm within a null-space concurrent with floating of the end effector or remote center. This may be accomplished by calculating joint movement of the plurality of the joints that "float" a first set of joints within a null-perpendicular space (i.e. joint velocity sub-space which results in movement of the end effector and/or remote center) and drive a second set of joints within a null space (i.e. joint velocity sub-space which maintains the position of the end effector and/or remote center, the null-space being orthogonal to the null-perpendicular space). Driving the second set of joints within the null-space allows for a repeatable and/or a desirable pattern of movement of the manipulator arm during position according to various algorithms in order to provide a desirable movement of a portion of the manipulator arm proximal the distal end effector during manual backdriving movement of the end effector. Typically, these features are included in a clutch mode to allow set-up or docking of the end effector before surgery or repositioning during surgery.
In one aspect, the movement of a manipulator arm having redundant degrees of freedom utilizes primary calculations based on joint velocities, such as by using a Jacobian based controller. As described herein, "floating" of the joints can generally be described as driving the joints so as to zero out the torques of the motors associated with movement of the joints (e.g. the controller memory may be continually reset to be equal to the input values so that the differences between the measured position and velocity and the commanded position and velocity are zero). It should be understood, however, that despite zeroing of the torques that would result in movement of the joint, various controller functions may still apply torques to the floating joints, such as may be used for friction compensation, gravity compensation, or the like, and such functions may remain unaltered during floating of the joints. As described herein, "servoing" the joints can generally be described as driving the joints with torques needed to maintain the desired state (e.g. position, alignment, etc.) so as to keep a portion of the manipulator, such as the distal end effector, "locked" in the desired state, without requiring any mechanical locking of any particular joint.

In many embodiments, first and second modules of the processor will be used differently in different control modes, such as a clutch mode, as described above and a tissue manipulator mode in which movement of the end effector according to a desired tissue manipulator movement is commanded by a surgeon. The tissue manipulator mode will often comprise a master/slave mode. The effective degrees of freedom of a particular joint may differ in the clutch mode as compared to the tissue manipulation mode. For example, a manipulator assembly providing the end effector with six or more mechanical degrees of freedom could be constrained so as to allow the end effector to be moved in space solely about a pivotal rotation center located where no joint is present. Alternatively, such an end effector might be translatable along an arbitrary plane skewed at an angle relative to every linkage and joint axis of the manipulator linkage assembly.

The manipulator assembly will often comprise a surgical tool or instrument having a shaft extending between a mounting interface and the end effector. The processor in a first mode may be configured to derive the desired movement of the end effector within an internal surgical space so that the shaft passes through a minimally invasive aperture site.

Such a master/slave controller may, for example, comprise a velocity controller using an Jacobian pseudo-inverse matrix, which will often comprise a portion of the first module, or alternatively an augmented Jacobian. A second module may be used in the second or clutch mode, and may employ a projection of a clutch matrix with the inverse Jacobian matrix so as to provide combinations of joint velocities that are allowed in the clutch mode. The
processor in the clutch mode may float a first set of joints within a joint velocity sub-space to allow manual articulation or movement of a first portion of the manipulator (e.g. end effector or associated remote center) to a desired position, while driving a second set of joints according to one or more null-space algorithms to provide a desired movement of another portion of the manipulator (e.g. a proximal portion between the proximal base and distal end effector) according to various null-space algorithms. In some embodiments, an orientation of the end effector (or some other structure of the manipulator) may be orientationally constrained by driving of the driven clutch joints while that structure is manually translated by backdriving to a new location.

[0018] In one aspect of the present invention, a redundant degrees of freedom (RDOF) surgical robotic system with manipulate input is provided. The RDOF surgical robotic system comprises a manipulator assembly, one or more user input devices, and a processor with a controller. A manipulator arm of the assembly has a plurality of joints providing sufficient degrees of freedom that allow a range of joint states for a given end effector state. In response to receiving a tissue manipulation command to move the end effector with a desired movement, the system calculates end effector displacing movement of the joints by calculating joint velocities within a null-perpendicular-space of the Jacobian orthogonal to the null-space, and drives the joints according to the calculated movement to effect the desired end effector movement. To provide increased range of motion for the various other types of movements described above, the system may include a revolute proximal most joint that affects the pitch of a distal instrument shaft of the manipulator and/or a distal revolute joint coupling an instrument to a proximal portion of the manipulator arm that effects a pivotal movement of the instrument shaft. In some embodiments, one or both of these joints may also be utilized in any of the clutch modes described herein.

[0019] In another aspect of the invention, the manipulator is configured to move such that an intermediate portion of the instrument shaft pivots about a remote center. Between the manipulator and the instrument, there are a plurality of driven joints providing sufficient degrees of freedom to allow a range of joint states for an end effector position when the intermediate portion of the instrument shaft passes through an access site. A processor having a controller couples the input device to the manipulator. Typically, in the tissue manipulator mode, in response to receiving a manipulation command to effect a desired end effector's movement, the system calculates end effector displacing movement of the joints, comprising calculating joint velocities within a null-perpendicular-space of the Jacobian orthogonal to the null-space, and drives the joints according to the calculated movement to
effect the desired end effector movement in which the instrument shaft pivots about the remote center. In a clutch mode, the processor determines movements of one or more joints to float the first set of joints to allow a patient-side assistant to move an intermediate portion of the instrument within the access site and maintains the desired remote center location about which the shaft pivots. It is appreciated that this is but one of many variations of the clutch mode in accordance with the principles of the present invention and the clutch made may configured to float one or both of the tool tip or distal end effector and a remote center about which the end effector pivots while various other joints are maintained at a desired state. In addition, it is appreciated that various clutch modes may be concurrently used in order to effect various other tasks as needed.

[0020] In some embodiments, a first joint from the first set of joints of the manipulator is a revolute joint coupling the manipulator arm to the base. The desired state of the end effector may include a desired position, velocity or acceleration of the end effector. In yet another aspect of the present invention, a surgical robotic manipulator with a proximal revolute joint and a distal parallelogram linkage is provided, the pivotal axis of the revolute joint substantially intersecting with the axis of the instrument shaft of the end effector, preferably at a remote center if applicable. The system further includes a processor having a controller coupling the input to the manipulator arm and configured to calculate a movement of the plurality of joints in response to a user input command. The system may include a clutch mode in which a first set of joints of the plurality of joints float within a null-perpendicular space to allow a patient-side assistant to move the end effector or a remote center about which the end effector moves to a desired position for surgery while one or more joints of a second set of joints are driven within a null-space according to one or more algorithms to effect various tasks, such as collision avoidance, pose preference, or to improve conditioning of the manipulator arm. In any of the embodiments described herein, each of the first and second set of joints may include one or more joints and the first and second joints may include one or more joints in common or may be entirely different sets of joints.

[0021] A further understanding of the nature and advantages of the present invention will become apparent by reference to the remaining portions of the specification and drawings. It is to be understood, however, that each of the figures is provided for the purpose of illustration only and is not intended as a definition of the limits of the scope of the invention. Furthermore, it is appreciated than any of the features in any of the described embodiments could be modified and combined with any of various other features described herein or known to one of skill in the art and still remain within the spirit and scope of the invention.
BRIEF DESCRIPTION OF THE DRAWINGS

[0022] FIG. 1A is an overhead view of a robotic surgical system in accordance with embodiments of the present invention, the robotic surgical system having a surgical station with a plurality of robotic manipulators for robotically moving surgical instruments having surgical end effectors at an internal surgical site within a patient.

[0023] FIG. 1B diagrammatically illustrates the robotic surgical system of FIG. 1A.

[0024] FIG. 2 is a perspective view illustrating a master surgeon console or workstation for inputting surgical procedure commands in the surgical system of FIG. 1A, the console including a processor for generating manipulator command signals in response to the input commands.

[0025] FIG. 3 is a perspective view of the electronics cart of FIG. 1A.

[0026] FIG. 4 is a perspective view of a patient side cart having four manipulator arms.

[0027] FIGS. 5A-5D show an exemplary manipulator arm.

[0028] FIGS. 6A-6B show an exemplary manipulator arm in the pitch forward configuration and pitch back configurations, respectively.

[0029] FIG. 6C shows a graphical representation of the range of motion of the surgical instrument end effector of an exemplary manipulator arm, including a cone of silence or conical tool access limit zone in each of the pitch forward and pitch back configurations.

[0030] FIG. 7A shows exemplary manipulator arms having a proximal revolute joint that revolves the manipulator arm about an axis of a proximal revolute joint.

[0031] FIG. 7B shows an exemplary manipulator arm and the associated range of motion and cone of silence, the exemplary manipulator arm having a proximal revolute joint that revolves the manipulator arm around an axis of a proximal revolute joint the movement of which can be used to mitigate the depicted cone of silence.

[0032] FIGS. 8A-8B show an exemplary manipulator arms having a revolute joint near the distal instrument holder.

[0033] FIG. 9A schematically illustrates a highly flexible manipulator assembly having a clutch input switch so as to facilitate manual positioning of a surgical tool adjacent a minimally invasive aperture while a processor configures the manipulator joint in response to the manual backdriving movement.
FIGS. 9 B and 9 C schematically illustrate reconfiguring of the joints of the manipulator assembly within a range of alternative joint configurations during manual backdriving movement of the arm.

FIGS. 10A-10C show sequential views of an exemplary manipulator arm having a revolute joint near a distal instrument holder as the joint is moved throughout its range of joint movement.

FIGS. 11A-11B show the revolved profile of an exemplary manipulator arm having a distal revolute joint when the angular displacement of the joint is 0° versus an angular displacement of 90°, respectively.

FIGS. 12A-12C show exemplary manipulator arms having a proximal joint that translates a proximal joint supporting the manipulator arm about a curved path.

FIGS. 13A-13B graphically represent the relationship between the null-space and the null-perpendicular-space of the Jacobian of an exemplary manipulator assembly.

FIGS. 14 graphically illustrates subspaces of the joint velocity space in a manipulator arm having a software remote center.

FIG. 15 schematically illustrates a method in accordance with many embodiments.

FIG. 16 illustrate example methods in accordance with many embodiments.

DETAILED DESCRIPTION OF THE INVENTION

The present invention generally provides improved surgical and robotic devices, systems, and methods. The invention is particularly advantageous for use with surgical robotic systems in which a plurality of surgical tools or instruments may be mounted on and moved by an associated plurality of robotic manipulators during a surgical procedure. The robotic systems will often comprise telerobotic, telesurgical, and/or telepresence systems that include processors configured as master-slave controllers. By providing robotic systems employing processors appropriately configured to move manipulator assemblies with articulated linkages having relatively large numbers of degrees of freedom, the motion of the linkages can be tailored for work through a minimally invasive access site. The large number of degrees of freedom allows a system operator, or an assistant, to reconfigure the linkages of the manipulator assemblies while maintaining the desired end effector state, optionally in preparation for surgery and/or while another use maneuvers the end effector during a surgical procedure. While aspects of the invention are generally described manipulators having
redundant degrees of freedom, it is appreciated that aspects may apply also to non-redundant manipulators or a redundant arm approaching a singularity.

[0043] The robotic manipulator assemblies described herein will often include a robotic manipulator and a tool mounted thereon (the tool often comprising a surgical instrument in surgical versions), although the term "robotic assembly" will also encompass the manipulator without the tool mounted thereon. The term "tool" encompasses both general or industrial robotic tools and specialized robotic surgical instruments, with these later structures often including an end effector which is suitable for manipulation of tissue, treatment of tissue, imaging of tissue, or the like. The tool/manipulator interface will often be a quick disconnect tool holder or coupling, allowing rapid removal and replacement of the tool with an alternate tool. The manipulator assembly will often have a base which is fixed in space during at least a portion of a robotic procedure, and the manipulator assembly may include a number of degrees of freedom between the base and an end effector of the tool. Actuation of the end effector (such as opening or closing of the jaws of a gripping device, energizing an electrosurgical paddle, or the like) will often be separate from, and in addition to, these manipulator assembly degrees of freedom.

[0044] The end effector will typically move in the workspace with between two and six degrees of freedom. As used herein, the term "position" encompasses both location and orientation. Hence, a change in a position of an end effector (for example) may involve a translation of the end effector from a first location to a second location, a rotation of the end effector from a first orientation to a second orientation, or a combination of both. When used for minimally invasive robotic surgery, movement of the manipulator assembly may be controlled by a processor of the system so that a shaft or intermediate portion of the tool or instrument is constrained to a safe motion through a minimally invasive surgical access site or other aperture. Such motion may include, for example, axial insertion of the shaft through the aperture site into a surgical workspace, rotation of the shaft about its axis, and pivotal motion of the shaft about a pivot point adjacent the access site.

[0045] Many of the exemplary manipulator assemblies described herein have more degrees of freedom than are needed to position and move an end effector within a surgical site. For example, a surgical end effector that can be positioned with six degrees of freedom at an internal surgical site through a minimally invasive aperture and may in some embodiments have nine degrees of freedom (six end effector degrees of freedom - three for location, and three for orientation—plus three degrees of freedom to comply with the access site constraints), but will often have ten or more degrees of freedom. Highly configurable
manipulator assemblies having more degrees of freedom than are needed for a given end effector position can be described as having or providing sufficient degrees of freedom to allow a range of joint states for an end effector position in a workspace. For example, for a given end effector position, the manipulator assembly may occupy (and be driven between) any of a range of alternative manipulator linkage positions. Similarly, for a given end effector velocity vector, the manipulator assembly may have a range of differing joint movement speeds for the various joints of the manipulator assembly within the null-space of the Jacobian.

[0046] The invention provides robotic linkage structures which are particularly well suited for surgical (and other) applications in which a wide range of motion is desired, and for which a limited dedicated volume is available due to the presence of other robotic linkages, surgical personnel and equipment, and the like. The large range of motion and reduced volume needed for each robotic linkage may also provide greater flexibility between the location of the robotic support structure and the surgical or other workspace, thereby facilitating and speeding up setup.

[0047] The term "state" of a joint or the like will often herein refer to the control variables associated with the joint. For example, the state of an angular joint can refer to the angle defined by that joint within its range of motion, and/or to the angular velocity of the joint. Similarly, the state of an axial or prismatic joint may refer to the joint's axial position, and/or to its axial velocity. While many of the controllers described herein comprise velocity controllers, they often also have some position control aspects. Alternative embodiments may rely primarily or entirely on position controllers, acceleration controllers, or the like. Many aspects of control system that can be used in such devices are more fully described in U.S. Patent No. 6,699,177, the full disclosure of which is incorporated herein by reference. Hence, so long as the movements described are based on the associated calculations, the calculations of movements of the joints and movements of an end effector described herein may be performed using a position control algorithm, a velocity control algorithm, a combination of both, and/or the like.

[0048] In many embodiments, the tool of an exemplary manipulator arm pivots about a pivot point adjacent a minimally invasive aperture. In some embodiments, the system may utilize a hardware remote center, such as the remote center kinematics described in U.S. Patent No. 6,786,896, the entire contents of which are incorporated herein in its entirety. Such systems may utilize a double parallelogram linkage which constrains the movement of the linkages such that the shaft of the instrument supported by the manipulator pivots about a
remote center point. Alternative mechanically constrained remote center linkage systems are
known and/or may be developed in the future. Surprisingly, work in connection with various
aspects of the invention indicates that remote center linkage systems may benefit from highly
configurable kinematic architectures. In particular when a surgical robotic system has a
linkage that allows pivotal motion about two axes intersecting at or near a minimally invasive
surgical access site, the spherical pivotal motion may encompass the full extent of a desired
range of motion within the patient, but may still suffer from avoidable deficiencies (such as
being poorly conditioned, being susceptible to arm-to-arm or arm-to-patient contact outside
the patient, and/or the like). At first, adding one or more additional degrees of freedom that
are also mechanically constrained to pivotal motion at or near the access site may appear to
offer few or any improvements in the range of motion. Nonetheless, such joints can provide
significant advantages by allowing the overall system to be configured in or driven toward a
collision-inhibiting pose, by further extending the range of motion for other surgical
procedures, and the like. In other embodiments, the system may utilize software to achieve a
remote center, such as described in U.S. Patent Application No. 8,004,229, the entire contents
of which are incorporated herein by reference. In a system having a software remote center,
the processor calculates movement of the joints so as to pivot an intermediate portion of the
instrument shaft about a pivot point determined, as opposed to a mechanical constraint. By
having the capability to compute software pivot points, different modes characterized by the
compliance or stiffness of the system can be selectively implemented. More particularly,
different system modes over a range of pivot points/centers (e.g., moveable pivot points,
passive pivot points, fixed/rigid pivot point, soft pivot points) can be implemented as desired.

[0049] Despite the many advantages of a robotic surgical system having multiple highly
configurable manipulators, since the manipulators include a relatively large number of joints
and links between the base and instrument, manual positioning of the links can be
challenging and complicated. Even when the manipulator structure is balanced so as to avoid
gravitational effects, attempting to align each of the joints in an appropriate arrangement or to
reconfigure the manipulator as desired can be difficult, time consuming, and may involve
significant training and/or skill. The challenges can be even greater when the links of the
manipulator are not balanced about the joints, such that positioning such a highly
configurable structures in an appropriate configuration before or during surgery can be a
struggle due to the manipulator arm length and the passive and limp design in many surgical
systems.
These issues can be addressed by allowing a user, such as a physician's assistant, to quickly and easily reconfigure the manipulator arm by floating one or more joints within a clutch mode. Repositioning a manipulator arm having floating joints, however, may present certain challenges. While the large number of redundant joints may provide increased range of motion for certain tasks, the additional joints in the manipulator arm may cause various movements of the arm to be overly complex during positioning or reconfiguration, such that the movements appear unpredictable or the amount of overall movements causes various other clinical concerns. To improve the movement of the manipulator arm, in many embodiments, the system drives a second set of joints within a null-space according to one or more null-space algorithms concurrent with floating the first set of joints so as to provide improved manipulator arm movement during manual positioning of the end effector by a user in the clutch mode. Examples of null-space movements that may be used in any of the clutch modes described herein are described in U.S. Provisional Application No. 61/654,755 filed June 1, 2012, entitled "Manipulator Arm-to-Patient Collision Avoidance Using a Null-Space;" and U.S. Provisional Application No. 61/654,773 filed June 1, 2012, entitled "System and Methods for Avoiding Collisions Between Manipulator Arms Using a Null-Space," the disclosures of which are incorporated herein by reference in their entireties.

In the following description, various embodiments of the present invention will be described. For purposes of explanation, specific configurations and details are set forth in order to provide a thorough understanding of the embodiments. However, it will also be apparent to one skilled in the art that the present invention may be practiced without the specific details. Furthermore, well-known features may be omitted or simplified in order not to obscure the embodiment being described.

Referring now to the drawings, in which like reference numerals represent like parts throughout the several views, FIG. 1A is an overhead view illustration of a Minimally Invasive Robotic Surgical (MIRS) system 10, in accordance with many embodiments, for use in performing a minimally invasive diagnostic or surgical procedure on a Patient 12 who is lying down on an Operating table 14. The system can include a Surgeon's Console 16 for use by a Surgeon 18 during the procedure. One or more Assistants 20 may also participate in the procedure. The MIRS system 10 can further include a Patient Side Cart 22 (surgical robot) and an Electronics Cart 24. The Patient Side Cart 22 can manipulate at least one removably coupled tool assembly 26 (hereinafter simply referred to as a "tool") through a minimally invasive incision in the body of the Patient 12 while the Surgeon 18 views the surgical site through the Console 16. An image of the surgical site can be obtained by an endoscope 28,
such as a stereoscopic endoscope, which can be manipulated by the Patient Side Cart 22 so as to orient the endoscope 28. The Electronics Cart 24 can be used to process the images of the surgical site for subsequent display to the Surgeon 18 through the Surgeon's Console 16. The number of surgical tools 26 used at one time will generally depend on the diagnostic or surgical procedure and the space constraints within the operating room among other factors. If it is necessary to change one or more of the tools 26 being used during a procedure, an Assistant 20 may remove the tool 26 from the Patient Side Cart 22, and replace it with another tool 26 from a tray 30 in the operating room.

[0053] FIG. 1B diagrammatically illustrates a robotic surgery system 50 (such as MIRS system 10 of FIG. 1A). As discussed above, a Surgeon's Console 52 (such as Surgeon's Console 16 in FIG. 1A) can be used by a Surgeon to control a Patient Side Cart (Surgical Robot) 54 (such as Patent Side Cart 22 in FIG. 1A) during a minimally invasive procedure. The Patient Side Cart 54 can use an imaging device, such as a stereoscopic endoscope, to capture images of the procedure site and output the captured images to an Electronics Cart 56 (such as the Electronics Cart 24 in FIG. 1A). As discussed above, the Electronics Cart 56 can process the captured images in a variety of ways prior to any subsequent display. For example, the Electronics Cart 56 can overlay the captured images with a virtual control interface prior to displaying the combined images to the Surgeon via the Surgeon's Console 52. The Patient Side Cart 54 can output the captured images for processing outside the Electronics Cart 56. For example, the Patient Side Cart 54 can output the captured images to a processor 58, which can be used to process the captured images. The images can also be processed by a combination the Electronics Cart 56 and the processor 58, which can be coupled together so as to process the captured images jointly, sequentially, and/or combinations thereof. One or more separate displays 60 can also be coupled with the processor 58 and/or the Electronics Cart 56 for local and/or remote display of images, such as images of the procedure site, or other related images.

[0054] FIG. 2 is a perspective view of the Surgeon's Console 16. The Surgeon's Console 16 includes a left eye display 32 and a right eye display 34 for presenting the Surgeon 18 with a coordinated stereo view of the surgical site that enables depth perception. The Console 16 further includes one or more input control devices 36, which in turn cause the Patient Side Cart 22 (shown in FIG. 1A) to manipulate one or more tools. The input control devices 36 can provide the same degrees of freedom as their associated tools 26 (shown in FIG. 1A) so as to provide the Surgeon with telepresence, or the perception that the input control devices 36 are integral with the tools 26 so that the Surgeon has a strong sense
of directly controlling the tools 26. To this end, position, force, and tactile feedback sensors
(not shown) may be employed to transmit position, force, and tactile sensations from the
tools 26 back to the Surgeon's hands through the input control devices 36.

[0055] The Surgeon's Console 16 is usually located in the same room as the patient so that
the Surgeon may directly monitor the procedure, be physically present if necessary, and
speak to an Assistant directly rather than over the telephone or other communication medium.
However, the Surgeon can be located in a different room, a completely different building, or
other remote location from the Patient allowing for remote surgical procedures.

[0056] FIG. 3 is a perspective view of the Electronics Cart 24. The Electronics Cart 24 can
be coupled with the endoscope 28 and can include a processor to process captured images for
subsequent display, such as to a Surgeon on the Surgeon's Console, or on another suitable
display located locally and/or remotely. For example, where a stereoscopic endoscope is
used, the Electronics Cart 24 can process the captured images so as to present the Surgeon
with coordinated stereo images of the surgical site. Such coordination can include alignment
between the opposing images and can include adjusting the stereo working distance of the
stereoscopic endoscope. As another example, image processing can include the use of
previously determined camera calibration parameters so as to compensate for imaging errors
of the image capture device, such as optical aberrations.

[0057] FIG. 4 shows a Patient Side Cart 22 having a plurality of manipulator arms, each
supporting a surgical instrument or tool 26 at a distal end of the manipulator arm. The Patient
Side Cart 22 shown includes four manipulator arms 100 which can be used to support either a
surgical tool 26 or an imaging device 28, such as a stereoscopic endoscope used for the
capture of images of the site of the procedure. Manipulation is provided by the robotic
manipulator arms 100 having a number of robotic joints. The imaging device 28 and the
surgical tools 26 can be positioned and manipulated through incisions in the patient so that a
kinematic remote center is maintained at the incision so as to minimize the size of the
incision. Images of the surgical site can include images of the distal ends of the surgical
instruments or tools 26 when they are positioned within the field-of-view of the imaging
device 28.

[0058] Regarding surgical tool 26, a variety of alternative robotic surgical tools or
instruments of different types and differing end effectors may be used, with the instruments
of at least some of the manipulators being removed and replaced during a surgical procedure.
Several of these end effectors, including DeBakey Forceps, microforceps, Potts scissors, and
clip applier include first and second end effector elements which pivot relative to each other so as to define a pair of end effector jaws. Other end effectors, including scalpel and electrosurgical probe have a single end effector element. For instruments having end effector jaws, the jaws will often be actuated by squeezing the grip members of handle. Single end effector instruments may also be actuated by gripping of the grip members, for example, so as to energize an electrosurgical probe.

[0059] The elongate shaft of instrument 26 allow the end effectors and the distal end of the shaft to be inserted distally into a surgical worksite through a minimally invasive aperture, often through an abdominal wall or the like. The surgical worksite may be insufflated, and movement of the end effectors within the patient will often be effected, at least in part, by pivoting of the instrument 26 about the location at which the shaft passes through the minimally invasive aperture. In other words, manipulators 100 will move the proximal housing of the instrument outside the patient so that shaft extends through a minimally invasive aperture location so as to help provide a desired movement of end effector. Hence, manipulators 100 will often undergo significant movement outside patient P during a surgical procedure.

[0060] Exemplary manipulator arms in accordance with many embodiments of the present invention can be understood with reference to FIGS. 5A-13C. As described above, a manipulator arm generally supports a distal instrument or surgical tool and effects movements of the instrument relative to a base. As a number of different instruments having differing end effectors may be sequentially mounted on each manipulator during a surgical procedure (typically with the help of a surgical assistant), a distal instrument holder will preferably allow rapid removal and replacement of the mounted instrument or tool. As can be understood with reference to FIG. 4, manipulators are proximally mounted to a base of the patient side cart. Typically, the manipulator arm includes a plurality of linkages and associated joints extending between the base and the distal instrument holder. In one aspect, an exemplary manipulator includes a plurality of joints having redundant degrees of freedom such that the joints of the manipulator arm can be driven into a range of differing configurations for a given end effector position. This may be the case for any of the embodiments of manipulator arms disclosed herein.

[0061] In many embodiments, such as shown for example in FIG. 5A, an exemplary manipulator arm includes a proximal revolute joint J1 that rotates about a first joint axis so as to revolve the manipulator arm distal of the joint about the joint axis. In some embodiments, revolute joint J1 is mounted directly to the base, while in other embodiments, joint J1 may be
mounted to one or more movable linkages or joints. The joints of the manipulator, in combination, have redundant degrees of freedom such that the joints of the manipulator arm can be driven into a range of differing configurations for a given end effector position. For example, the manipulator arm of FIGS. 5A-5D may be maneuvered into differing configurations while the distal member 511 (such as a cannula through which the tool 512 or instrument shaft extends) supported within the instrument holder 510 maintains a particular state and may include a given position or velocity of the end effector. Distal member 511 is typically a cannula through which the tool shaft 512 extends, and the instrument holder 510 is typically a carriage (shown as a brick-like structure that translates on a spar) to which the instrument attaches before extending through the cannula 511 into the body of the patient through the minimally invasive aperture.

[0062] Describing the individual links of manipulator arm 500 of FIGS. 5A-5D along with the axes of rotation of the joints connecting the links as illustrated in FIG. 5A-5D, a first link 504 extends distally from a pivotal joint J2 which pivots about its joint axis and is coupled to revolute joint J1 which rotates about its joint axis. Many of the remainder of the joints can be identified by their associated rotational axes, as shown in FIG. 5A. For example, a distal end of first link 504 is coupled to a proximal end of a second link 506 at a pivotal joint J3 that pivots about its pivotal axis, and a proximal end of a third link 508 is coupled to the distal end of the second link 506 at a pivotal joint J4 that pivots about its axis, as shown. The distal end of the third link 508 is coupled to instrument holder 510 at pivotal joint J5. Typically, the pivotal axes of each of joints J2, J3, J4, and J5 are substantially parallel and the linkages appear "stacked" when positioned next to one another, as shown in FIG. 5D, so as to provide a reduced width w of the manipulator arm and improve patient clearance during maneuvering of the manipulator assembly. In many embodiments, the instrument holder also includes additional joints, such as a prismatic joint J6 that facilitates axial movement of instrument 306 through the minimally invasive aperture and facilitates attachment of the instrument holder to a cannula through which the instrument is slidably inserted.

[0063] The distal member or cannula 511 through which the tool 512 extends may include additional degrees of freedom distal of instrument holder 510. Actuation of the degrees of freedom of the instrument will often be driven by motors of the manipulator, and alternative embodiments may separate the instrument from the supporting manipulator structure at a quickly detachable instrument holder/instrument interface so that one or more joints shown here as being on the instrument are instead on the interface, or vice versa. In some embodiments, cannula 511 includes a rotational joint J8 (not shown) near or proximal of the
insertion point of the end effector or the pivot point PP, which generally is disposed at the site of a minimally invasive aperture. A distal wrist of the instrument allows pivotal motion of an end effector of surgical tool 512 about instrument joints axes of one or more joints at the instrument wrist. An angle between end effector jaw elements may be controlled independently of the end effector location and orientation.

[0064] The range of motion of an exemplary manipulator assembly can be appreciated by referring to FIGS. 6A-6C. During a surgical procedure, an exemplary manipulator arm can be maneuvered into a pitch forward configuration, as shown in FIG. 6A, or into a pitch back configuration, as shown in FIG. 6B, as needed to access particular patient tissues within a surgical workspace. A typical manipulator assembly includes an end effector that can pitch forwards and backwards about an axis by at least ± 60 degrees, preferably by about ± 75 degrees, and can also yaw about an axis by ± 80 degrees. Although this aspect allows for increased maneuverability of the end effector with the assembly, there may be configurations in which movement of the end effector may be limited, particularly when the manipulator arm is in the full pitch forward or full pitch back configuration as in FIGS. 6A and 6B. In one embodiment, the manipulator arm has a Range of Motion (ROM) of (± 75 degrees) for the outer pitch, and (±300 degrees) for the outer yaw joints, respectively. In some embodiments, the ROM may be increased for the outer pitch to provide a ROM larger than (± 90 degrees) in which case the "cone of silence" could be made to disappear entirely, although generally the inner sphere associated with insertion limitations would remain. It is appreciated that various embodiments may be configured to have increased or decreased ROM, that the above noted ROMs are provided for illustrative purposes, and further that the invention is not limited to the ROMs described herein.

[0065] FIG. 6C graphically represents the overall range of motion and workspace of the tool tip of the exemplary manipulator of FIGS. 5A-5B. Although the workspace is shown as hemisphere, it may also be represented as a sphere depending on the range of motion and configuration of one or more revolute joints of the manipulator, such as joint J1. As shown, the hemisphere in FIG. 6C includes a central, small spherical void as well as two conical voids. The voids represent the areas in which movement of the end effector may be impossible due to mechanical constraints or unfeasible due to extremely high joint velocities that make movement of the end effector difficult or slow. For these reasons, the conical void are referred to as the "cone of silence." In some embodiments, the manipulator arm may reach a singularity at a point within the cone. Since movement of the manipulator within or near the cone of silence may be impaired, it can be difficult to move the manipulator arm...
away from the cone of silence without manually backdriving one or more links of the manipulator to reconfigure the linkages and joints of the manipulator, which often requires an alternative operating mode and delays the surgical procedure.

[0066] Movement of the instrument shaft into or near these conical portions typically occurs when the angle between distal linkages in the manipulator is relatively small. Such configurations can be avoided by reconfiguring the manipulator to increase the angles between linkages (so that the linkages are moved into a more orthogonal position relative to each other). For example, in the configurations shown in FIGS. 6A and 6B, when the angle between the distal most link and the instrument holder (angle \( \theta \)) becomes relatively small movement of the manipulator may become more difficult. Depending on the range of joint movements in the remaining joints in various embodiments, when the angle between certain linkages decreases, movement of the manipulator may be inhibited and in some cases, the manipulator arm may no longer be redundant. A manipulator configuration in which the instrument shaft nears these conical portions, or in which the angles between linkages are relatively low is said to be "poorly conditioned" such that maneuverability and dexterity of the manipulator arm is limited. It is desirable that the manipulator be "well conditioned" so as to maintain dexterity and range of movement.

[0067] While the embodiments of the manipulator described above may be utilized in the present invention, some embodiments may include additional joints, which may also be used to improve dexterity and the conditioning of the manipulator arm. For example, an exemplary manipulator may include a revolute joint and/or linkage proximal of joint J1 which can be used to revolve the manipulator arm of FIG. 5A, and its associated cone of silence, about an axis of the revolute joint so as to reduce or eliminate the cone of silence. In another embodiment, the exemplary manipulator may also include a distal pivotal joint that pivots the instrument holder about an axis substantially perpendicular to joint J5, thereby offsetting the end effector so as to further reduce the cone of silence and improve the range of movement of the surgical tool. In still another embodiment, a proximal joint of the manipulator arm, such as J1, may be movably mounted on the base, so as to move or shift the cone of silence as needed and improve the range of motion of the manipulator end effector during manual positioning of the end effector in the clutch mode. The use and advantages of such additional joints can be understood by referring to FIGS. 7A-13C, which illustrate examples of such joints, which may each be used independent of one another or used in combination, in any of the exemplary manipulator arms described herein.
FIGS. 7A-7B illustrate an additional redundant joint for use with exemplary manipulator arms - a first joint coupling a proximal portion of the manipulator arm to the base. The first joint is a proximal revolute joint \( J_1' \) that revolves the manipulator arm about a joint axis of joint \( J_1' \). The proximal revolute \( J_1' \) includes a link 501 that offsets joint \( J_1 \) from the proximal revolute \( J_1' \) by a pre-determined distance or angle. The link 501 can be a curved linkage, as shown in FIG. 7A, or a linear or angled linkage, as shown in FIG. 7B. Typically, the joint axis of the joint \( J_1' \) is aligned with the remote center RC or insertion point of the end effector, as shown in each of FIG. 7A. In an exemplary embodiment, the joint axis of joint \( J_1' \) passes through the remote center, as does each other revolute joint axis in the manipulator arm, to prevent motion at the body wall and can therefore be moved during surgery. The axis of joint \( J_1' \) is coupled to a proximal portion of the arm so it can be used to change the position and orientation of the back of the arm. In general, redundant axes, such as this, allow the instrument tip to follow the surgeon's commands while simultaneously avoiding collisions with other arms or patient anatomy and can also be used in the various clutch modes to provide such movement during manual positioning or docking of the end effector during set-up. In one aspect, the proximal revolute \( J_1' \) is used solely to change the mounting angle of the manipulator with respect to the floor. This angle is important in order to 1) avoid collisions with external patient anatomy and 2) reach anatomy inside the body. Typically, the angle \( \alpha \) between the proximal link of the manipulator attached to the proximal revolute joint \( J_1' \) and the axis of the proximal revolute is about 15 degrees.

FIG. 7B illustrates the relationship of the proximal revolute joint \( J_1' \) and its associated joint axis and the cone of silence in an exemplary manipulator arm. The joint axis of the proximal revolute joint \( J_1' \) may pass through the cone of silence or may be completely outside of the cone of silence. By revolving the manipulator arm about the axis of the proximal revolute \( J_1' \), the cone of silence can be reduced (in an embodiment where the joint \( J_1' \) axis passes through the cone of silence), or can be effectively eliminated (in an embodiment where the proximal revolute joint axis extends completely outside the cone of silence). The distance and angle of the link 501 determines the position of the joint \( J_1' \) axis relative to the cone of silence.

FIGS. 8A-8B illustrates another type of redundant joint for use with exemplary manipulator arms, a distal revolute joint \( J_7 \) coupling the instrument holder 510 to a distal link of the manipulator arm 508. The distal revolute joint \( J_7 \) allows the system to laterally pivot or twist the instrument holder 510 about the joint axis, which typically passes through the remote center or insertion point. Ideally, the revolute joint is located distally on the arm and
is therefore particularly well suited to moving the orientation of the insertion axis. The addition of this redundant axis allows the manipulator to assume multiple positions for any single instrument tip position. In general, redundant axes, such as this, allow the instrument tip to follow the surgeon's commands while simultaneously avoiding collisions with other arms or patient anatomy. Because the distal revolute joint J7 has the ability to move the insertion axis closer to the yaw axis, it is able to increase the range of motion when the manipulator arm is in a pitch back position. The relationship between the axis of the distal revolute joint J7, the yaw axis of J1 and the insertion axis of end effector is shown in FIG. 8B. FIGS. IOA-I0C show the sequential movement of joint J7 and how movement of joint J7 shifts the insertion axis of end effector from side to side.

[0071] Referring now to FIG. 9A, another alternative manipulator assembly 520 includes a manipulator linkage arm 522 for removably supporting a surgical tool 524. A clutch input 516 comprises an input button which can be actuated by a hand engaging a link 518 of the manipulator that is to be disposed adjacent to access site 514 during surgery. This allows the hand to both actuate the input and help maneuver the manipulator into the appropriate position for surgery. In some embodiments, additional clutch inputs may be mounted on various other links so as to allow manual articulation of a link on which the clutch input is disposed. In many embodiments, the link 518 on which clutch input 516 is coupled to a shaft of a removable tool by an axial insertion joint. In one aspect, the system is configured such that the hand which actuates the clutch input 516 may also reposition the manipulator in the clutch mode without assistance from another hand. In another aspect, repositioning of the manipulator may be facilitated by having a user position both a first hand on the manipulator link 518 adjacent clutch input 516 and a second hand at a distance from the clutch input, particularly when reorienting the link to a desired axial insertion angle. In certain embodiments, while clutch input 516 is actuated by the hand, the system processor will float the first set of joints of manipulator 520 to allow manual backdriving movement of link 518 to a desired position, while the second set of joints is driven in a null-space to provide a desired movement of the proximal portion of the manipulator without otherwise interfering with manual positioning of link 518.

[0072] If the clutched degrees of freedom of the slave manipulator linkage coincide with one or more joint degrees of freedom (that is, if some joints are locked and some joints are free to move in the clutch mode), then clutching is direct: one simply turns off the controller for those joints that are free to move. However, it will often be advantageous to clutch joints in a dependent way, where motion of one joint is linked by the controller to motion of at least
one other joint so that they can be manually articulated together as a single degree of
freedom. This may be achieved by driving at least one joint of a robotic manipulator
assembly in response to external articulation of at least one other joint. The controller can
effect this motion, which will often be different than any degree of freedom of the mechanical
system, by defining any desired arbitrary linear combination of joints that can be treated as a
single degree of freedom that the operator may manipulate, optionally while some or all of
the other mechanical degrees of freedom remain locked. This general concept includes port
clutching, instrument clutching, elbow clutching (in which an intermediate elbow is allowed
to move, for example, from an upward oriented apex configuration around to a laterally
oriented apex configuration while a state of the end effector is maintained), and other
clutching modes.

[0073] Various clutching modes and clutching behaviors may be included in any of the
manipulators described herein, including for example in nonredundant hardware center arms,
hardware center arms having redundant degrees of freedom and software center arms. In one
aspect, the various clutching modes and clutching behaviors may be used separately, while in
other aspect, any of the various clutch modes or clutch features may be used in combination
with one another. For example, the manipulator system may include an arm-clutch mode and
a port-clutch mode. These clutch modes allow a user to perform various tasks while effecting
various other tasks or desired movements. For example, the arm-clutch mode may allow a
user, such as the patient-side assistant, to back-drive the arm into a desired state and the port-
clutch mode may allow a user to move a port through which the instrument extends. These
modes may be combined so as to allow a patient-side assistant to back-drive the arm to a
desired state while concurrently moving the port through which the instrument extends. In
some embodiments, upon exiting the various clutch modes or features, a "following" state
commences from the new arm state provided by the clutch mode(s) or clutch feature(s).
Thus, a clutch mode may be a combination of various clutching modes or clutching features
or behaviors, a variety of which are set forth in detail below.

[0074] Referring now to Figs. 9A and 9B, manipulator assembly 502 may be reconfigured
by the processor for any of a variety of differing reasons. In one aspect, a joint 526 may be
driven from a downward oriented apex configuration to an upward oriented apex
configuration so as to inhibit collisions with an adjacent arm, equipment, or personnel or to
enhance a range of motion of the end effector 508. Some, but not all, of these changes in
configuration of the manipulator assembly may be in response to external forces applied to
the manipulator assembly, with the processor often driving a different joint of the
manipulator than that which is being acted upon by the external force. For example, a manipulator arm movements may be effected in response to physiological movement of the patient such as patient breathing or the like or in response to repositioning of the patient, such as by reorienting a surgical table, and the like. In another aspect, the processor may reconfigure the manipulator assembly in response to calculations performed by the processor. In either aspect, the processor may vary from a simple master-slave controller so as to drive manipulator assembly in response to a signal so as to provide a preferred manipulator assembly configuration. Such configuring of the manipulator assembly may occur during master-slave end effector movements, during manual or other repositioning of the manipulator assembly, and/or at least partly at a different time, such as after releasing a clutch input. In many clutch modes, such movement is effected concurrently or simultaneously with floating of one or more joints (or alternatively one or both of the end effector and remote center) within the null-perpendicular space.

[0075] In one aspect, the null-space movement of the arm may be calculated in accordance with a set of constraints to effect movement along a desired path in a first mode, while floating one or more joints (which may include floating of one or both of the end effector and remote center) within the null-perpendicular space as described above. This allows at least a portion of the manipulator arm to move according to a desired movement, such as to improve conditioning of the arm, while another portion of the manipulator arm, such as a set-up joint, end effector, or remote center location, is moved by the user to a desired position.

[0076] One advantage of the distal revolute joint $J^7$ is that it may be used to reduce the patient clearance cone, which is the swept volume of the distal portion of the manipulator arm proximal of the insertion point that must clear the patient to avoid collision between the patient and the instrument holder or distal linkages of the manipulator arm. FIG. 11A illustrates the patient clearance cone of the proximal portion of the manipulator arm while the angular displacement of the distal revolute joint remains at 0°. FIG. 11B illustrates the reduced patient clearance cone of the proximal portion of the manipulator arm while the distal revolute joint is shown having an angular displacement of 90° about its axis. Thus, in procedures having minimal patient clearance near the insertion point, use of the joint $J^7$ in accordance with the present invention may provide additional clearance while maintaining the remote center location or the position of the end effector as desired.

[0077] FIGS. 12A-12C illustrate another type of redundant joint for use with exemplary manipulator arms, a proximal joint that translates or revolves the manipulator arm about an axis. In many embodiments, this proximal translatable joint translates a proximal joint of the
manipulator, such as joint J1 or J1', along a path so as to reduce or eliminate the cone of silence by shifting or rotating the range of motion of the manipulator arm to provide for better conditioning and improved maneuverability of the manipulator arm. The translatable joint may include a circular path, such as shown in joint J1" in FIGS. 12A-12D, or may include a semi-circular or arcuate path, such as shown in FIGS. 13A-13C. Generally, the joint revolves the manipulator arm about an axis of the translatable joint that intersects with the remote center RC about which the shaft of the tool 512 extending through cannula 511 pivots. Although in the embodiment shown in FIGS. 12A-12C, the axis of J1" is a vertical axis, although in some embodiments, the axis of J1" may be horizontal or various angles of inclination.

[0078] In certain embodiments, the manipulator arm 500 may include any or all of a proximal or distal revolute joint, a proximal translatable joint and a parallelogram configuration of the distal linkages. Use of any or all of these features provide additional redundant degrees of freedom and provide a desired movement of the manipulator arm concurrent with manually backdriving the distal end effector or remote center so as to provide for a better "conditioned" manipulator assembly by increasing the angles between linkages thereby improving the dexterity and motion of the manipulator during re-positioning and upon exiting of the clutch mode. The increased flexibility of this exemplary manipulator can also be used to optimize the kinematics of the manipulator linkage so as to avoid joint limits, singularities, and the like.

[0079] In certain embodiments, the joint movements of the manipulator are controlled by driving one or more joints with a controller using motors of the system, the joints being driven according to coordinated and joint movements calculated by a processor of the controller. Mathematically, the controller may perform at least some of the calculations of the joint commands using vectors and/or matrices, some of which may have elements corresponding to configurations or velocities of the joints. The range of alternative joint configurations available to the processor may be conceptualized as a joint velocity sub-space. The joint velocity sub-space may, for example, have as many dimensions as the manipulator has degrees of freedom, and a particular configuration of the manipulator may represent a particular point in the joint velocity sub-space, with each coordinate corresponding to a joint state of an associated joint of the manipulator.

[0080] In an exemplary embodiment, the system includes a controller in which a commanded position and velocity of a feature in the work-space, denoted here as its Cartesian space, are inputs. The feature may be any feature on or off the manipulator, which
can be used as a control frame to be articulated using control inputs. An example of a feature on the manipulator, used in many examples described herein, would be the tool-tip. Another example of a feature on the manipulator would be a physical feature which is not on the tool-tip, but is a part of the manipulator, such as a pin or a painted pattern. An example of a feature off the manipulator would be a reference point in empty space which is exactly a certain distance and angle away from the tool-tip. Another example of a feature off the manipulator would be a target tissue whose position relative to the manipulator can be established. In all these cases, the end effector is associated with an imaginary control frame which is to be articulated using control inputs. However, in the following, the "end effector" and the "tool tip" are used synonymously. Although generally, there is no closed form relationship which maps a desired Cartesian space end effector position to an equivalent joint-space position, there is generally a closed form relationship between the Cartesian space end effector and joint-space velocities. The kinematic Jacobian is the matrix of partial derivatives of Cartesian space position elements of the end effector with respect to joint space position elements. In this way, the kinematic Jacobian captures the kinematic relationship between the end effector and the joints. In other words, the kinematic Jacobian captures the effect of joint motion on the end effector. The kinematic Jacobian (J) can be used to map joint-space velocities (dq/dt) to Cartesian space end effector velocities (dx/dt) using the relationship below:

\[ \frac{dx}{dt} = J \frac{dq}{dt} \]

[0081] Thus, even when there is no closed-form mapping between input and output positions, mappings of the velocities can iteratively be used, such as in a Jacobian-based controller to implement a movement of the manipulator from a commanded user input, however a variety of implementations can be used. Although many embodiments include a Jacobian-based controller, some implementations may use a variety of controllers that may be configured to access the Jacobian of the manipulator arm to provide any of the features described herein.

[0082] One such implementation is described in simplified terms below. The commanded joint position is used to calculate the Jacobian (J). During each time step (At) a Cartesian space velocity (dx/dt) is calculated to perform the desired move (dx_{dei}/dt) and to correct for built up deviation (Δχ) from the desired Cartesian space position. This Cartesian space velocity is then converted into a joint-space velocity (dq/dt) using the pseudo-inverse of the
The resulting joint-space commanded velocity is then integrated to produce joint-space commanded position (q). These relationships are listed below:

\[
\frac{dx}{dt} = \frac{dx_{\text{des}}}{dt} + k \Delta x \quad (1)
\]

\[
\frac{dq}{dt} = J^\# \frac{dx}{dt} \quad (2)
\]

\[
q_i = q_{i,j} + \frac{dq}{dt} \cdot At \quad (3)
\]

The pseudo-inverse of the Jacobian (J) directly maps the desired end effector motion (and, in some cases, a remote center of pivotal tool motion) into the joint velocity space. If the manipulator being used has more useful joint axes than end effector degrees of freedom (e.g. up to six), then the manipulator is said to be redundant. For example, when a remote center of tool motion is in use, the manipulator should have an additional 3 joint axes for the 3 degrees of freedom associated with location of the remote center. A redundant manipulator's Jacobian includes a "null-space" having a dimension of at least one. In this context, the "null-space" of the Jacobian (N(J)) is the space of joint velocities which instantaneously achieves no end effector motion (and when a remote center is used, no movement of the pivotal point location); and "null-motion" is the combination, trajectory or path of joint positions which also produces no instantaneous movement of the end effector and/or location of the remote center. Incorporating or injecting the calculated null-space velocities into the control system of the manipulator to achieve a desired reconfiguration of the manipulator changes above equation (2) to the following:

\[
\frac{dq}{dt} = \frac{dq_{\text{perp}}}{dt} + \frac{dq_{\text{null}}}{dt} \quad (4)
\]

\[
\frac{dq_{\text{perp}}}{dt} = J^\# \frac{dx}{dt} \quad (5)
\]

\[
\frac{dq_{\text{null}}}{dt} = (1 - J^\# J) z = V_n V_n^T z = V_n a \quad (6)
\]

The joint velocity according to Equation (4) has two components: the first being the null-perpendicular-space component, the "purest" joint velocity (shortest vector length) which produces the desired end effector motion (and when the remote center is used, the desired remote center motion); and the second being the null-space component. Equations (2) and (5) show that without a null-space component, the same equation is achieved. Equation (6) starts with a traditional form for the null-space component on the left, and on the far right side, shows the form used in an exemplary system, wherein (V_n) is the set of orthonormal basis vectors for the null-space, and (a) are the coefficients for blending those basis vectors. In some embodiments, a is determined by control parameters, variables or settings, such as by use of knobs or other control means, to shape or control the motion within the null-space as desired.
FIG. 13A graphically illustrates the relationship between the null-space of the Jacobian and the null-perpendicular-space of the Jacobian. FIG. 13A shows a two-dimensional schematic showing the null-space along the horizontal axis, and the null-perpendicular-space along the vertical axis, the two axes being orthogonal to one another. The diagonal vector represents the sum of a velocity vector in the null-space and a velocity vector in the null-perpendicular-space, which is representative of Equation (4) above.

FIG. 13B graphically illustrates the relationship between the null-space and the null-motion manifold within a four-dimensional joint space, shown as the "null-motion manifold." Each arrow (q1, q2, q3, and q4) representing a principal joint axis. The closed curve represents a null-motion manifold which is a set of joint-space positions which instantaneously achieves the same end effector position. For a given point A on the curve, since the null-space is a space of joint velocities which instantaneously produce no movement of the end effector, the null-space direction (p+A) is parallel to the tangent of the null-motion manifold at point A.

In manipulator arms having distal instruments that pivot about a remote center as determined by the hardware configuration, the manipulator arms typically include manipulator joints and set-up joints, the manipulator joints allowing commanded movement of the manipulator arm within a range of configuration and set-up joints. An example of a set-up joints include one or more revolute or pivotal joints attaching the manipulator arm to a proximal base movement of which may pivot or revolve the remote center within a range of movement of the set-up joints. In one aspect, the set-up joints are used to position the manipulator arm into a desired configuration prior to surgery (or to allow various desired movement during surgery), while the manipulator joints allow the surgeon to manipulate the arm and associated end effector to perform surgery. The set-up joints are not required to be fully motorized or drivable and may include joints that are manually adjusted during set-up, although the set-up joints may include fully drivable joints that are driven according to various algorithms. The various clutching features may include manipulator joints, set-up joints or both.

In certain embodiments, when the manipulator is in an arm-clutch mode, substantially all manipulator joints are allowed to float. It is appreciated, however, that when a joint is allowed to "float" torques may still be applied to compensate for gravity to allow the manipulator arm to be driven or manually backdriven to the desired state. When the manipulator is in the port-clutch mode, the manipulator set-up joints are allowed to float so that the remote center is released while torques remain applied to the manipulator joints (e.g.
remain "servoed") so as to maintain the end effector at a controlled position (e.g. fixed position and/or orientation) while allowing the location of the port to be adjusted as desired. In a manipulator arm having a hardware remote center and non-redundant joints, when both the arm-clutch and port-clutch features are activated simultaneously, all the manipulator joints and manipulator set-up joints are released (e.g. allowed to "float").

[0089] In manipulators having manipulator joints with redundant degrees of freedom and a hardware remote center, the manipulator arm has a null-space of one or more dimensions (DIM = n, where n ≥ 1). In some such manipulator arms, the set-up joints may include joints that are not fully motorized, such that the joint velocities discussed herein do not include the set-up joints. In addition to the clutching features described above, such manipulator arms may include various other clutch modes or features that utilize the redundant degrees of freedom of the manipulator joints. For example, some manipulators may include a null-clutch or null-float mode in which the manipulator joints are allowed to float along a null-space of the joints while maintaining a desired state of the tool tip and/or distal end effector. This allows the user or patient side assistant to reconfigure the manipulator arm proximal of the distal end effector, such as by driving one or more joints, or allows one for one or more various other tasks, such as collision avoidance.

[0090] In one aspect, a manipulator system in accordance with the present invention may include null-perpendicular clutch or null-perpendicular float that allows the end effector to float, while the movement of the joints within the null-space is controlled by any variety of null-space algorithms. This aspect allows the user or a patient-side assistant to backdrive (e.g. manually articulate) the end effector while various other features or algorithms relating to null-space movement are enacted (e.g. collision avoidance, commanded reconfiguration, tracking along a desired path within the null-space, emphasizing movement to control or increase range of movement of one or more joints, or any other movement pertaining to the null-space). Examples of such movements are described in further detail in the following applications: U.S. Provisional Application No. 61/654,755 filed June 1, 2012, entitled "Manipulator Arm-to-Patent Collision Avoidance Using a Null-Space;" U.S. Provisional Application No. 61/654,764 filed June 1, 2012, entitled "Commanded Reconfiguration of a Surgical Manipulator Using the Null-Space;" U.S. Provisional Application No. 61/654,773 filed June 1, 2012, entitled "Systems and Methods for Avoiding Collisions Between Manipulator Arms Using a Null-Space;" each of which the entire contents are incorporated herein in their entirety for all purposes.
In manipulators having joints with redundant degrees of freedom where the location of the remote center is determined by software, the joints of the manipulator need not be classified as set-up joints versus manipulator joints. For example, in a manipulator arm having a hardware remote center, a minimum of three kinematic set-up joints degrees of freedom are required for positioning the remote center within a three-dimensional space and six kinematic manipulator degrees of freedom are required for positioning and orienting the end effector in three-dimensional space. Additional joint degrees of freedom provide redundancies in either the set-up or manipulator kinematics. In a manipulator arm having a remote center determined by software, as opposed to a hardware remote center, the locating of the remote center and the positioning and orienting of the end effector may collectively be performed by the manipulator joints such that movement of the joints may contribute to both the set-up and manipulator kinematics without the use of distinct set-up joints and manipulator joints. Thus, to position each of the remote center and end effector within a three-dimensional space, at least nine kinematic degrees of freedom are needed in a general non-redundant software center manipulator arm. Additional joints beyond these result in redundancies in either the end effector, the remote center, or both. Further understanding of the joint space of such manipulators can be gained by referring to Figure 14 discussed below.

FIG. 14 graphically illustrates various sub-spaces of the n-dimensional joint velocity space of an example manipulator arm having a software remote center within the null-space (N) and the null-perpendicular space ($N^\perp$) being orthogonal to the null-space associated movement of the remote center (RC) and end effector (EE) and numbers of dimensions shown ($DIM = n$). The various subspaces illustrated are as follows:

- **Subspace A** ($N^\perp$(RC)) is the null-perpendicular-space of the remote center, which is the subspace of joint velocities that result in motion of the remote center. Since the location of the remote center requires within the three-dimensional space requires three degrees-of-freedom, this subspace is three-dimensional.

- **Subspace B** ($N$(RC)) is the null-space of the remote center, which is the subspace of joint velocities that result in no instantaneous motion of the remote center. This subspace is orthogonal to subspace A such that subspace B is ($n - 3$) dimensional, where $n$ is the dimension of the full joint velocity space (e.g. the total number of joints).

- **Subspace C** ($N^\perp$(EE)) is the null-perpendicular-space of the end effector, which is the subspace of joint velocities that result in motion of the end effector. Since positioning and
orienting the end effector requires three degrees-of-freedom for positions and three degrees-of-freedom for orientations, this subspace is six-dimensional.

[0096] Subspace D \( (N(EE)) \) is the null-space of the end effector, which is the subspace of joint velocities that result in no instantaneous motion of the end effector. This subspace is orthogonal to subspace C such that it is \( (n - 6) \) dimensional.

[0097] Subspace E is the union or direct sum of subspace A and subspace C: \( N^\perp (RC + EE) \): The subspace of joint velocities which result in motion of either the remote center, the end effector, or both. From the definitions of Subspace (A) and Subspace (C), this subspace is nine-dimensional.

[0098] Subspace F \( (N(RC + EE)) \) is the intersection of subspace B and subspace D, which is the subspace of joint velocities that results in no instantaneous motion of either the remote center or the end effector. This subspace is orthogonal to subspace E such that it is \( (n - 9) \) dimensional.

[0099] The subspaces of a manipulator arm having a software remote center can be utilized by various other clutch modes, including but not limited to an arm-clutch mode, port-clutch mode, arm null-clutch mode, port null-clutch mode, arm null-perpendicular clutch mode, port null-perpendicular clutch mode, arm-port-null-perpendicular clutch mode, and arm-port-null-clutch mode, any mode described herein, or various combinations thereof. Certain clutch mode features are discussed in further detail below in reference to the examples subspaces illustrated in Figure 14.

[0100] In one aspect, in order to make any of the port clutch behaviors clinically acceptable, the kinematics is likely to be set up with the distal end effector position and orientation defined relative to the remote center rather than the manipulator base. In such a case, when a port clutch is activated, and the remote center is floated and backdriven, presumably following a body wall, the end effector follows the backdriven port as well. This is in contrast to the case in which the kinematics of the end effector is defined relative to the base, in which case clutching the port would keep the end effector undesirably stationary.

Using the former relative kinematic definition, the motion of the end effector relative to the entry at the body wall is minimized, which is desirable since the end effector may be interacting with anatomy.

[0101] In one aspect, the invention provides an arm-clutch mode or feature. The arm-clutch feature maintains a state of the remote center (e.g. the remote center is servoed) to
allow the end effector to be repositioned by a user (e.g. patient-side assistant) by backdriving one or more joints, such as by manually articulating the end effector. The arm-clutch feature may be used by itself or concurrently with various other clutch features, such as the port-clutch feature described below. Typically, when the arm-clutch feature is used by itself, the Jacobian based controller is "servoing" within subspace A and floating along subspace B.

[0102] In another aspect, the invention provides an port-clutch mode or feature. The port-clutch features allowing the remote center to be repositioned by a user by backdriving one or more joints, such as by manual backdriving movement by a patient-side assistant. When the remote center is being repositioned, holding the end effector fixed in space is possible by servoing within the subspace C. However, a clinician would intuitively expect that the end effector doesn't move relative to the remote center. So when the port-clutch feature is used by itself, the Jacobian based controller is floating the joints between the base of the manipulator to the remote center, and servoing the joints from the remote center to the end effector.

[0103] The various clutch modes or features described herein may be utilized concurrently or simultaneously, including the arm-clutch and port-clutch features. In certain embodiments, simultaneously effecting the arm-clutch and port-clutch features floats all joints of the manipulator arm. An alternative means of implementing this feature is an arm-port-null-perpendicular-clutch described below.

[0104] In another aspect, the invention provides a null-clutch mode or feature. The null-clutch feature keeps both the remote center and the end effector servoed, while allowing the manipulator joints to be repositioned by a user by backdriving one or more joints. In many embodiments, when this feature is used, the Jacobian based controller is servoing the joints within subspace E and floats the joints along subspace F.

[0105] In yet another aspect, the invention provides an arm-null-perpendicular-clutch mode or feature. The arm-null-perpendicular-clutch feature provides a desired behavior by (a) floating the end effector, (b) servoing the remote center, and (c) allowing the null-space algorithms to drive the joints. This is achieved by servoing along subspace A; floating along the subspace within subspace E which is orthogonal to subspace A; and allowing the null-space algorithms to drive along subspace F.

[0106] In another aspect, the invention provides a port-null-perpendicular-clutch mode or feature. The port-null-perpendicular-clutch feature provides the desired behavior by (a) servoing the end effector, (b) floating the remote center, and (c) allowing the null-space
algorithms to drive the joints. This behavior is achieved by servoing the joints along subspace C; floating the joints along the subspace within subspace E which is orthogonal to subspace C; and allowing the null-space algorithms to drive along subspace F.

[0107] In yet another aspect, the invention provides an arm-port-null-perpendicular-clutch mode or feature. The arm-port-null-perpendicular-clutch features provides the desired behavior by (a) floating the end effector, (b) floating the remote center, and (c) allowing the null-space algorithms to drive the joints. This behavior is achieved by floating the joints along subspace E; and allowing the null-space algorithms to drive along subspace F.

[0108] FIGS. 15-16 illustrate methods of reconfiguring a manipulator assembly of a robotic surgical system in accordance with many embodiments of the present invention. FIG. 15 shows a simplified schematic of the required blocks need to implement the general algorithms to control the patient side cart joint states, in relation to the equations discussed above. According to the method of FIG. 15, the system: calculates the forward kinematics of the manipulator arm; then calculates \( \frac{dx}{dt} \) using Equation (1), calculates \( \frac{dq_{pr}}{dt} \) using Equation (5), then calculates \( \frac{dq_{nix}}{dt} \) from \( z \), which may depend on \( \frac{dq_{pr}}{dt} \) and the Jacobian using Equation (6). From the calculated \( \frac{dq_{pr}}{dt} \) and \( \frac{dq_{nix}}{dt} \), the system then calculates \( \frac{dq}{dt} \) and \( q \) using Equations (4) and (3), respectively, thereby providing the movement by which the controller can effect the desired movement of the manipulator while maintaining the desired state of the end effector and/or location of the remote center during floating of the first set of joints and manual backdriving movement by the user.

[0109] FIG. 16 shows a block diagram of an example method for use in a robotic system. In the clutch mode depicted, the robotic system floats a first set of joints of the manipulator arm associated with a position or orientation of an end effector or remote center, senses a manual backdriving movement of the end effector or remote center during floating of the first set of joints, calculates a movement of a second set of joints associated with movement of a proximal portion of the manipulator arm within a null-space according to a desired state or movement, and drives the joints according to the calculated movements during floating of the joints to provide the desired state or movement of the manipulator arm concurrent with manual backdriving movement of the end effector or remote center. It can be appreciated that this method may include various aspects or features of any of the embodiments described herein.

[0110] While the exemplary embodiments have been described in some detail for clarity of understanding and by way of example, a variety of adaptations, modifications, and changes
will be obvious to those of skill in the art. Hence, the scope of the present invention is limited solely by the appended claims.
WHAT IS CLAIMED IS:

1. A robotic method comprising:
   providing a manipulator arm including a movable distal end effector, a
   proximal portion coupled to a base, and a plurality of joints between the end effector and the
   base, the plurality of joints having sufficient degrees of freedom to allow a range of differing
   joint states for a given end effector state in a surgical work space;
   floating a first set of joints of the plurality of joints within a null-perpendicular
   space of a Jacobian, the first set of joints associated with a position of the end effector within
   the work space, wherein the null-perpendicular space is a joint velocity space in which
   movement of the first set of joints results in movement of the end effector;
   sensing a manual backdriving movement of the end effector to a desired
   position within the work space;
   calculating an auxiliary movement of a second set of joints of the plurality of
   joints to effect a desired movement of a proximal portion of the manipulator arm, wherein
   calculating the auxiliary movement comprises calculating joint velocities of the second set of
   joints within a null-space of the Jacobian, the null-space being orthogonal to the null-
   perpendicular space; and
   driving the second set of joints according to the calculated auxiliary movement
   concurrent with floating of the first set of joints.

2. The robotic method of claim 1, wherein the desired position of the end
   effector comprises a position and/or alignment of the end effector within the work space so as
   to allow for insertion of the distal end effector through a cannula or positioning of the end
   effector adjacent a minimally invasive aperture.

3. The robotic method of claim 1, wherein the desired state or movement
   of the proximal portion of the manipulator arm is any or all of a desired position, velocity,
   configuration, pose, reconfiguration movement, or collision avoidance movement of the
   manipulator arm within the work space.

4. The robotic method of claim 3, wherein the desired state or movement
   of the proximal portion of the manipulator arm comprises a state or movement of a portion of
   the manipulator arm proximal the distal end effector.
5. The robotic method of claim 1, wherein each of the first and second set of joints includes one or more joints.

6. The robotic method of claim 1, wherein the first and second set of joints includes one or more joints in common.

7. The robotic method of claim 1, wherein floating of the first set of joints, calculating the auxiliary movement, and driving the joints according to the auxiliary movement occurs within a first clutch mode of a processor determining movement of the joints, the processor further having a tissue manipulation mode, the method further comprising:
   receiving a tissue manipulation command from a user input to move the end effector to effect a desired tissue manipulation;
   calculating a manipulation movement of the plurality of joints in response to the tissue manipulation command so as to move the manipulator with the desired movement.

8. The robotic method of claim 7, wherein when in the tissue manipulation mode, the method further comprises:
   calculating an auxiliary movement of a subset of joints of the plurality of joints to effect a desired state or movement of the manipulator arm during tissue manipulation, wherein calculating the auxiliary movement comprises calculating joint velocities of the subset of joints within the null-space; and
   driving the subset of joints according to the calculated auxiliary movement and manipulation movement so as to move the end effector according to the commanded manipulation movement concurrent with the desired movement of the manipulator arm.

9. The robotic method of claim 1, wherein the manipulator arm is configured to support a tool having an intermediate portion with the intermediate portion extending along an insertion axis distally of the proximal portion and the end effector is at a distal end of the intermediate portion, wherein at least some of the joints mechanically constrain movement of the tool relative to the base such that the tool of the manipulator arm pivots about a remote center disposed along the insertion axis to facilitate movement of the end effector at a work site accessed through a minimally invasive aperture.
10. The robotic method of claim 9, wherein a portion of the manipulator arm adjacent the end effector is mechanically constrained relative to the base such that an instrument shaft of the end effector pivots about a remote center when the constrained portion moves.

11. The robotic method of claim 9, wherein a first joint of the plurality of joints couples the proximal portion to the base, the first joint comprising a revolute joint that supports the distal portion of the manipulator arm such that joint movement of the revolute joint pivots the distal portion of the manipulator arm about a pivotal axis of the revolute joint, wherein the pivotal axis extends from the revolute joint and through the remote center so that the insertion axis of the manipulator arm moves along a distally tapered cone oriented towards the remote center.

12. The robotic method of claim 11, wherein the second set of joints includes the first joint.

13. A robotic method comprising:

   providing a manipulator arm including a movable distal end effector, a proximal portion coupled to a base, and a plurality of joints between the end effector and the base, the plurality of joints having sufficient degrees of freedom to allow a range of differing joint states for a given end effector state within a surgical work space, wherein the end effector comprises an instrument shaft that pivots about a remote center adjacent a minimally invasive aperture within the work space during a surgical procedure;

   floating a first set of joints of the plurality of joints within a null-perpendicular space of a Jacobian, wherein the null-perpendicular space is a joint velocity space in which movement of the first set of joints results in movement of the distal end effector within the work space;

   driving the plurality of joints so as to maintain the remote center at a controlled position in the work space;

   sensing a manual backdriving movement of the distal end effector to a desired position within the work space;

   calculating an auxiliary movement of a second set of the plurality of joints to effect a desired movement of the manipulator arm, wherein calculating the auxiliary movement comprises calculating joint velocities of the second set of joints within a null-
space of the Jacobian, the null-space being orthogonal to the null-perpendicular space,
wherein the null-space is a joint velocity space in which joint movement maintains the state
of the end effector; and

driving the second set of joints according to the calculated auxiliary movement
concurrent with maintaining the position of the remote center and the desired movement of
the manipulator arm.

14. The robotic method of claim 13, wherein the first and second set of
joints include one or more joints in common.

15. The robotic method of claim 13, wherein the controlled position
comprises a fixed location within the work space.

16. A robotic method comprising:

- providing a manipulator arm including a movable distal end effector, a
proximal portion coupled to a base, and a plurality of joints between the end effector and the
base, the plurality of joints having sufficient degrees of freedom to allow a range of differing
joint states for a given end effector state, wherein the distal end effector comprises an
instrument shaft that pivots about a remote center adjacent a minimally invasive aperture
within a surgical work space during a surgical procedure;

- floating a first set of the plurality of joints within a null-perpendicular space of
a Jacobian, wherein the null-perpendicular space is a joint velocity sub-space in which
movement of the joints results in movement of the remote center within the work space;

- driving the plurality of joints so as to maintain a controlled position of the end
effector within the work space;

- sensing a manual backdriving movement of the remote center to a desired
location within the work space;

- calculating an auxiliary movement of a second set of the plurality of joints to
effect a desired movement of the manipulator arm, wherein calculating the auxiliary
movement comprises calculating joint velocities of the second set of joints within a null-
space of the Jacobian, the null-space being orthogonal to the null-perpendicular space,
wherein the null-space is a joint velocity space in which joint movement maintains a state of
the distal end effector; and
driving the second set of joints according to the calculated auxiliary movement during floating of the first set of joints concurrent with maintaining the controlled position of the end effector and the desired movement of the manipulator arm.

17. The robotic method of claim 16, wherein the first and second set of joints include one or more joints in common.

18. The robotic method of claim 17, wherein the controlled position comprises a fixed position or alignment of the end effector relative to the remote center.

19. The robotic method of claim 17, wherein the controlled position comprises a fixed position or alignment of the end effector within the work space.

20. A robotic method comprising:

   providing a manipulator arm including a movable distal end effector, a proximal portion coupled to a base, and a plurality of joints between the end effector and the base, the plurality of joints having sufficient degrees of freedom to allow a range of differing joint states for a given end effector state within a surgical work space, wherein the end effector comprises an instrument shaft that pivots about a remote center adjacent a minimally invasive aperture within the work space during a surgical procedure;

   floating a first set of joints of the plurality of joints within a null-perpendicular space of a Jacobian, wherein the null-perpendicular space is a joint velocity sub-space in which joint movement results in movement of both a position of the distal end effector and a location of the remote center within the work space;

   sensing manual backdriving movement of the end effector to a desired position within the work space and movement of the remote center to a desired location within the work space;

   calculating an auxiliary movement of a second set of joints of the plurality of joints to effect a desired state or movement of the manipulator arm, wherein calculating the auxiliary movement comprises calculating joint velocities of the second set of joints within a null-space of the Jacobian, the null-space being orthogonal to the null-perpendicular space, wherein the null-space is a joint velocity sub-space in which movement of the second set of joints maintains a state of the end effector and the remote center; and

   driving the second set of joints according to the calculated auxiliary movement while floating the first set of joints so as to allow manual backdriving movement of both the
distal end effector and remote center to a desired position and location, respectively, within
the work space concurrent with the desired state or movement of the manipulator arm.

21. A robotic system comprising:
   a manipulator arm configured for robotically moving a distal end effector
   relative to a proximal base, the manipulator arm having a plurality of joints between the end
   effector and a proximal portion coupled to the base, the plurality of joints having sufficient
   degrees of freedom to allow a range of differing joint states for a given end effector state
   within a surgical work space, wherein the end effector comprises an instrument shaft that
   pivots about a remote center adjacent a minimally invasive aperture within the work space
   during a surgical procedure;
   an input for receiving a manipulation command to effect a desired tissue
   manipulation movement of the end effector; and
   a processor coupling the input to the manipulator arm, comprising a
   manipulation mode and a clutch mode,
   the processor in the manipulation mode configured to calculate joint
   movements to provide the desired end effector movement in response to the manipulation
   command,
   the processor in the clutch mode configured to:
   float a first set of joints of the plurality of joints within a null-
   perpendicular space of a Jacobian to allow manual backdriving movement of the end
   effector to a desired position within the work space, wherein the null-perpendicular
   space is a joint velocity sub-space in which movement of the joints results in
   movement of the end effector;
   calculate an auxiliary movement of a second set of joints of the
   plurality of joints to effect a desired movement of the manipulator arm, wherein
   calculating the auxiliary movement comprises calculating joint velocities of the
   second set of joints within a null-space of the Jacobian, the null-space being
   orthogonal to the null-perpendicular space; and
   drive the second set of joints according to the calculated auxiliary
   movement concurrent with floating of the first set of joints.

22. The robotic system of claim 21, wherein in the clutch mode, the
processor is configured to float the first set of joints concurrent with calculating the auxiliary
movement and driving the second set of joints according to the calculated auxiliary
movement.

23. The robotic system of claim 21, wherein the desired position of the end
effector comprises a position and/or alignment of the end effector within the work space so as
to allow insertion of the distal end effector through a cannula or positioning of the end
effector adjacent a minimally invasive aperture.

24. The robotic system of claim 21, wherein the desired state or movement
of the manipulator arm is any or all of a desired position, velocity, configuration, pose,
reconfiguration movement, or collision avoidance movement of the manipulator arm within
the work space.

25. The robotic system of claim 21, wherein the manipulator is configured
such that each of the first and second set of joints includes one or more joints.

26. The robotic system of claim 21, wherein the manipulator is configured
such that the first and second set of joints includes one or more joints in common.

27. The robotic system of claim 21, wherein a first joint of the plurality of
joints that couples the proximal portion to the base is a revolute joint that supports the joints
of the manipulator arm such that joint movement of the revolute joint pivots one or more
joints of the manipulator arm about a pivotal axis of the revolute joint, the pivotal axis
extending from the revolute joint through a shaft of the end effector.

28. The robotic system of claim 21, wherein one or both of the first and
second set of joints includes the first joint.

29. The robotic system of claim 21, wherein the joints of the manipulator
comprise remote center joints configured to mechanically constrain movement of a distal
portion of the manipulator arm to pivot about a remote center pivot point along an insertion
axis adjacent a minimally invasive aperture and wherein the processor is further configured to
drive the joints to maintain the intermediate portion at the pivot point.

30. A robotic system comprising:
a manipulator arm configured for robotically moving a distal end effector
relative to a proximal base, the manipulator arm having a plurality of joints between the end
effector and a proximal portion coupled to the base, the plurality of joints having sufficient
degrees of freedom to allow a range of differing joint states for a given end effector state
within a surgical work space, wherein the end effector comprises an instrument shaft that
pivots about a remote center adjacent a minimally invasive aperture within the work space
during a surgical procedure;

an input for receiving a manipulation command to effect a desired
manipulation movement of the end effector; and

a processor coupling the input to the manipulator arm, the processor
configured to with a manipulation mode and a clutch mode,
the processor in the manipulation mode configured to calculate movement of
the joints in response to the command so as to move the end effector with the desired
manipulation movement, and

the processor in the clutch mode configured to:

float a first set of joints of the plurality of joints within a null-
perpendicular space of a Jacobian to allow manual backdriving movement of the end
effector and/or an associated remote center about which the end effector pivots,

wherein the null-perpendicular space is a joint velocity sub-space in which movement
of the first set of joints results in movement of the end effector and/or the remote
center within the work space;

calculate an auxiliary movement of a second set of joints of the
plurality of joints to effect a desired movement of the manipulator arm, wherein
calculating the auxiliary movement comprises calculating joint velocities of the
second set of joints within a null-space of the Jacobian, the null-space being
orthogonal to the null-perpendicular space, wherein the null-space is a joint velocity
sub-space in which joint movement maintains the state of the end effector and/or
associated remote center; and

drive the second set of joints according to the calculated auxiliary
movement concurrent with the desired movement of the end effector and/or
associated remote center.

31. The robotic system of claim 30, wherein the processor in the clutch
mode is configured such that the null-perpendicular space is a joint velocity sub-space in
which movement of the joints results in movement of the distal end effector within the work
space, and

wherein the processor is further configured to calculate movement of the
plurality of joints in the clutch mode so as to maintain the remote center at a controlled
position.

32. The robotic system of claim 30, wherein the processor in the clutch
mode is configured such that the null-perpendicular space is a joint velocity sub-space in
which movement of the joints results in movement of the remote center within the work
space, and

wherein the processor is further configured to calculate movement of the
plurality of joints in the clutch mode so as to maintain the end effector at a controlled position
concurrent with floating the first set of joints to allow movement of the remote center and the
desired movement of the manipulator arm.

33. The robotic system of claim 32, wherein the controlled position of the
remote center comprises a fixed position or alignment of the end effector relative the remote
center.

34. The robotic system of claim 32, wherein the controlled position of the
remote center comprises a fixed position or alignment of the end effector within the work
space.

35. The robotic system of claim 30, wherein the processor in the clutch
mode is configured such that the null-perpendicular space is a joint velocity sub-space in
which joint movement results in movement of both a position of the distal end effector and a
location of the remote center within the work space, and

the processor in the clutch mode is further configured to drive the second set
of joints according to the calculated auxiliary movement while floating the first set of joints
so as to allow manual backdriving movement of both the distal end effector and remote
center to a desired position and location, respectively, within the work space concurrent with
providing the desired state or movement of the manipulator arm.
\[ \dot{\mathbf{q}} = \dot{q}_\perp + \dot{q}_N \]

FIG. 13A
MULTI-DIM JOINT SPACE

FIG. 13B

q_1

q_2

q_3

q_4

qd_{null} \cdot dt

Null-Space Direction

Null-Motion Manifold
Calculate forward kinematics

Calculate $\dot{x}$ using EQUATION (1)

Calculate $\dot{q}$ perp using EQUATION (5)

Calculate $\dot{q}$ and $q$ using EQUATIONS (4) and (3)

Calculate JACOBIAN

Calculate $\dot{q}$ null using EQUATION (6)

FIG. 15
Floating a first set of joints of the manipulator arm associated with a position or orientation of a tool tip or remote center

Sensing a manual movement of the end effector or remote center during floating of the first set of joints

Calculating a movement of a second set of joints associated with movement of a proximal portion of the manipulator arm within a null-space according to a desired state or movement

Driving the joints according to the calculated movements while floating of the joints to provide the desired state or movement of the manipulator arm concurrent with manual movement of the tool tip or remote center

FIG. 16
**INTERNATIONAL SEARCH REPORT**

International application No
PCT/US2014/031082

A. CLASSIFICATION OF SUBJECT MATTER

INV. A61B19/00 B25J9/16 B25J18/00

ADD.

According to International Patent Classification (IPC) or to both national classification and IPC

B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)

A61B B25J

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

Electronic data base consulted during the international search (name of data base and, where practicable, search terms used)

EPO-Internal , WPI Data

C. DOCUMENTS CONSIDERED TO BE RELEVANT

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<th>Citation of document, with indication, where appropriate, of the relevant passages</th>
<th>Relevant to claim No.</th>
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Further documents are listed in the continuation of Box C. See patent family annex.

* Special categories of cited documents:
  
  "A" document defining the general state of the art which is not considered to be of particular relevance
  
  "E" earlier application or patent but published on or after the international filing date
  
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  "YA" document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art
  
  "S" document member of the same patent family

Date of the actual completion of the international search
24 June 2014

Date of mailing of the international search report
01/07/2014

Name and mailing address of the ISA/

European Patent Office, P.B. 5818 Patentlaan 2
NL-2280 HV Rijswijk
Tel. (+31-70) 340-2040,
Fax: (+31-70) 340-3016

Authorized officer

Schnurbusch, Daniel
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<th>Relevant to claim No.</th>
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### INTERNATIONAL SEARCH REPORT

#### Box No. II Observations where certain claims were found unsearchable (Continuation of item 2 of first sheet)

This international search report has not been established in respect of certain claims under Article 17(2)(a) for the following reasons:

1. **Claims Nos.: 1-20**
   - because they relate to subject matter not required to be searched by this Authority, namely:
     - see **FURTHER INFORMATION sheet** PCT/ISA/21 10

2. **Claims Nos.:**
   - because they relate to parts of the international application that do not comply with the prescribed requirements to such an extent that no meaningful international search can be carried out, specifically:

3. **Claims Nos.:**
   - because they are dependent claims and are not drafted in accordance with the second and third sentences of Rule 6.4(a).

#### Box No. III Observations where unity of invention is lacking (Continuation of item 3 of first sheet)

This International Searching Authority found multiple inventions in this international application, as follows:

1. **[ ]** As all required additional search fees were timely paid by the applicant, this international search report covers all searchable claims.

2. **[ ]** As all searchable claims could be searched without effort justifying an additional fees, this Authority did not invite payment of additional fees.

3. **[ ]** As only some of the required additional search fees were timely paid by the applicant, this international search report covers only those claims for which fees were paid, specifically claims Nos.:

4. **[ ]** No required additional search fees were timely paid by the applicant. Consequently, this international search report is restricted to the invention first mentioned in the claims; it is covered by claims Nos.:

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**Remark on Protest**

- **[ ]** The additional search fees were accompanied by the applicant’s protest and, where applicable, the payment of a protest fee.
- **[ ]** The additional search fees were accompanied by the applicant’s protest but the applicable protest fee was not paid within the time limit specified in the invitation.
- **[ ]** No protest accompanied the payment of additional search fees.
Method claims 1-20 define a method for treatment of the human or animal body by surgery practiced on the human or animal body, because "[...] providing a manipulator arm including a movable distal end effector [...] to allow a range of differing joint states for a given end effector state in a surgical work space [...] floating a first set of joints [...] associated with a position of the end effector within the work space [...] which results in movement of the end effector [...]" (claims 1, 13, 16 and 20) is seen as a surgical step performed on a patient, because the end effector, being situated at a surgical site, receives commands to be moved and therefore manipulate tissue. Therefore no search has been performed for the subject-matter of this claim and the corresponding dependent claims (see Article 17 (2) PCT and Rule 39.1.(iv) PCT) and no written opinion is required for the subject-matter of these method claims (see Rule 43bis.1 and Rule 67.1 (iv) PCT).
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