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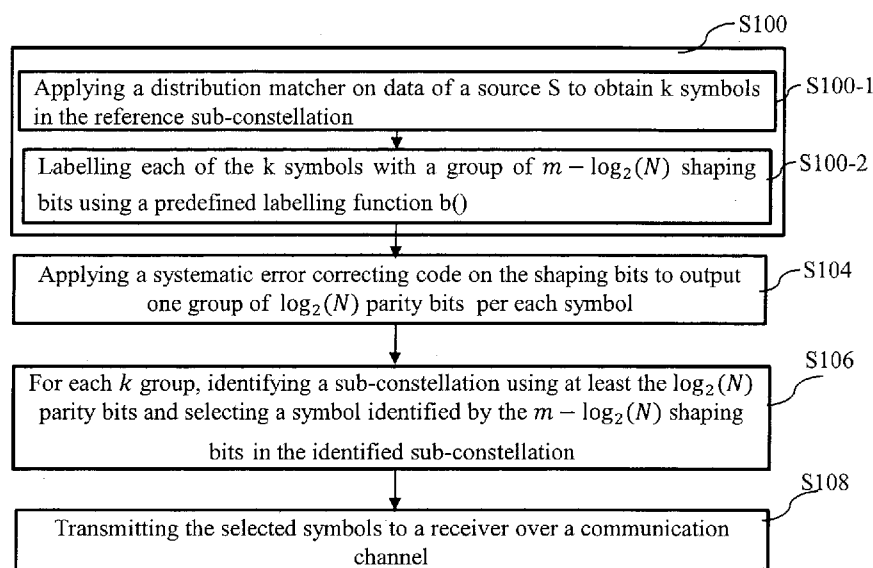


FIG. 6

(57) **Abstract:** A method, in a transmitter, is disclosed. The method is for transmitting data using a constellation with $M = 2^m$ symbols, divided in N sub-constellations, N and M being integers, where for any symbol in a reference sub-constellation, there is a symbol in each of the other sub-constellations with a same probability value. The method comprises: - obtaining from a source of data, k groups of $m - \log_2(N)$ shaping bits wherein each group of $m - \log_2(N)$ shaping bits identifies one symbol x_j in the reference sub-constellation, $j \in [1; k]$; - applying a systematic error correcting code on said k groups of $m - \log_2(N)$ shaping bits to output one group of $\log_2(N)$ parity bits per each symbol x_j ; - for each symbol x_j , identifying a sub-constellation using at least the group of $\log_2(N)$ parity bits and selecting a symbol identified by said $m - \log_2(N)$ shaping bits in said identified sub-constellation; and - transmitting each of said k selected symbols to a receiver over a communication channel.

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[DESCRIPTION]

[Title of Invention]

METHOD AND TRANSMITTER FOR TRANSMITTING DATA
USING CONSTELLATION

[Technical Field]

[0001]

At least one of the present embodiments generally relates to a method, in a transmitter, for transmitting data to a receiver over a communication channel. At least one embodiment relates to a transmitter configured to implement the method.

[Background Art]

[0002]

In a communication system, a transmitter is coupled to a receiver by way of a communication channel (e.g. an optical fiber). The transmitter usually comprises an encoder configured to encode the input data, e.g. a bitstream, into symbols belonging to a finite set, called a constellation. One dimensional ASK (English acronym of “Amplitude-Shift Keying”) and two dimensional QAM (English acronym of “Quadrature-Amplitude Keying”) are examples of such constellations. Here, one dimensional or two dimensional constellations mean that the symbols take value in $\mathbb{R}$ or in $\mathbb{R}^2$, respectively, $\mathbb{R}$ being the set of real numbers. These symbols are then transmitted over the communication channel to the receiver. The receiver comprises a decoder configured to decode the received symbols into output data.

[0003]

Communication systems in which uniformly distributed symbols are transmitted usually lead to an absence of a shaping gain. Therefore, in order to approach the channel capacity, it is known that the transmitter should process the input data to change the probability distribution of the transmitted symbols.

More precisely, the input data are processed so that the transmitted symbols have a non-uniform probability distribution that is adapted to the communication channel. This operation, called probabilistic shaping, can provide energy savings also known as shaping gain.

[0004]

In addition to shaping, the signal should be protected against errors with a so-called error-correcting code. Combining shaping and error-correcting code is complex.

[0005]

The document from Böcherer et al entitled “*Bandwidth Efficient and Rate-Matched Low-Density Parity-Check Coded Modulation*” and published in IEEE transactions on communications, vol. 63, no. 12, Dec. 2015 discloses a new coded modulation scheme that, at the transmitter, combines a distribution matcher for probabilistic shaping with a systematic error-correcting code. This method requires that the parity bit of the error-correcting code has an equiprobable distribution and is thus well-suited to the shaping of symmetric distributions as the symbols have the same probability to be positive or negative. However, it is not adapted to the shaping of non-symmetric distributions. In addition, this method is not compliant with distribution matchers that consider the sign bits as shaping bits and therefore change the conditional distribution of the sign bit which is no more independent of the value of the other bits.

[0006]

It is thus desirable to find a method for transmitting data that is adapted to non-symmetric distributions and that makes it possible to use distribution matchers which consider the sign bits as shaping bits.

[Summary of Invention]

[0007]

At least one of the present embodiments generally relates to a method, in a transmitter, for transmitting data using a constellation with $M = 2^m$ symbols, divided in N sub-constellations, N and M being integers, where for any symbol in a reference sub-constellation, there is a symbol in each of the other sub-constellations with a same probability value. The method comprises:

- obtaining from a source of data, k groups of $m - \log_2(N)$ shaping bits wherein each group of $m - \log_2(N)$ shaping bits identifies one symbol x_j in the reference sub-constellation, $j \in [1;k]$;
- applying a systematic error correcting code on said k groups of $m - \log_2(N)$ shaping bits to output one group of $\log_2(N)$ parity bits per each symbol x_j ;
- for each symbol x_j , identifying a sub-constellation using at least the group of $\log_2(N)$ parity bits and selecting a symbol identified by said $m - \log_2(N)$ shaping bits in said identified sub-constellation; and
- transmitting each of said k selected symbols to a receiver over a communication channel.

[0008]

This method is compliant with distribution matchers that consider the sign bits as shaping bits. In addition, it is also adapted to non-symmetric distributions.

[0009]

In one embodiment, obtaining from a source of data, k groups of $m - \log_2(N)$ shaping bits wherein each group of $m - \log_2(N)$ shaping bits identifies one symbol x_j in the reference sub-constellation, $j \in [1;k]$ comprises:

- applying a distribution matcher on said data of said source to obtain k symbols x_j in the reference sub-constellation ; and
- labelling each symbol with a group of $m - \log_2(N)$ shaping bits using a labelling function.

[0010]

In one embodiment, the labelling function is a natural labelling function.

[0011]

In one embodiment, the labelling function is a Gray labelling function.

[0012]

In one embodiment, wherein $N=2$, identifying, for each symbol x_j , a sub-constellation using at least the group of $\log_2(N)$ parity bits and selecting a symbol identified by said $m - \log_2(N)$ shaping bits in said identified sub-constellation comprises : selecting a shift value in the set $\{0; 2\}$ responsive to at least the group of $\log_2(N)$ parity bits and adding the selected shift value to the symbol x_j of the reference constellation to obtain the symbol to transmit.

[0013]

In one embodiment, selecting a shift value in the set $\{0; 2\}$ responsive to at least the group of $\log_2(N)$ parity bits comprises selecting a shift value responsive to double a sum modulo 2 of the group of $\log_2(N)$ parity bits and of the corresponding $m - \log_2(N)$ shaping bits.

[0014]

In one embodiment, the constellation is a M-ASK constellation.

[0015]

In one embodiment, wherein said source of data is an equiprobable source.

[0016]

At least one of the present embodiments generally relates to a transmitter configured to transmit data using a constellation with $M = 2^m$ symbols, divided in N sub-constellations, N and M being integers, where for any symbol in a reference sub-constellation, there is a symbol in each of the other sub-constellations with a same probability value. The transmitter comprises at least one processor configured to:

- obtain from a source of data, k groups of $m - \log_2(N)$ shaping bits wherein each group of $m - \log_2(N)$ shaping bits identifies one symbol x_j in the reference sub-constellation, $j \in [1; k]$;
- apply a systematic error correcting code on said k groups of $m - \log_2(N)$ shaping bits to output one group of $\log_2(N)$ parity bits per each symbol x_j ;
- for each symbol x_j , identify a sub-constellation using at least the group of $\log_2(N)$ parity bits and select a symbol identified by said $m - \log_2(N)$ shaping bits in said identified sub-constellation; and
- transmit each of said k selected symbols to a receiver over a communication channel.

[0017]

In one embodiment, to obtain from a source of data, k groups of $m - \log_2(N)$ shaping bits wherein each group of $m - \log_2(N)$ shaping bits identifies one symbol x_j in the reference sub-constellation, $j \in [1; k]$ comprises:

- to apply a distribution matcher on said data of said source to obtain k symbols x_j in the reference sub-constellation ; and
- to label each symbol with a group of $m - \log_2(N)$ shaping bits using a labelling function.

[0018]

In one embodiment, the labelling function is a natural labelling function.

[0019]

In one embodiment, the labelling function is a Gray labelling function.

[0020]

In one embodiment, wherein $N=2$, to identify, for symbol x_j , a sub-constellation using at least the group of $\log_2(N)$ parity bits and to select a symbol identified by said $m - \log_2(N)$ shaping bits in said identified sub-constellation comprises : to select a shift value in the set $\{0; 2\}$ responsive to

at least the group of $\log_2(N)$ parity bits and to add the selected shift value to the symbol x_j of the reference constellation to obtain the symbol to transmit.

[0021]

In one embodiment, to select a shift value in the set $\{0; 2\}$ responsive to at least the group of $\log_2(N)$ parity bits comprises to select a shift value responsive to double a sum modulo 2 of the group of $\log_2(N)$ parity bits and of the corresponding $m - \log_2(N)$ shaping bits.

[0022]

A computer program product is also disclosed that comprises program code instructions that can be loaded in a programmable device, the program code instructions causing implementation of the method according to any one of the disclosed embodiments when the program code instructions are run by the programmable device.

[0023]

A storage medium is also disclosed that stores a computer program comprising program code instructions, the program code instructions causing implementation of the method according to any one of the disclosed embodiments when the program code instructions are read from the storage medium and run by a programmable device.

[0024]

The characteristics of the invention will emerge more clearly from a reading of the following description of at least one example of embodiment, said description being produced with reference to the accompanying drawings.

[Brief Description of Drawings]

[0025]

[FIG. 1]

Fig. 1 illustrates schematically a communication system in which the present embodiments may be implemented.

[FIG. 2]

Fig. 2 depicts the symbols of an 8-ASK constellation.

[FIG. 3]

Fig. 3 depicts an example of a quantized target bit distribution of a 16-ASK constellation.

[FIG. 4]

Fig. 4 depicts two sub-constellations of the 16-ASK constellation and a natural labelling of the symbols according to an embodiment.

[FIG. 5]

Fig. 5 depicts an example of a quantized target bit distribution of an 8-ASK constellation.

[FIG. 6]

Fig. 6 depicts a method, in a transmitter, for transmitting binary data using a constellation with $M = 2^m$ symbols according to a specific embodiment.

[FIG. 7]

Fig. 7 depicts an example of a target distribution of a reference sub-constellation in the case of a 16-ASK constellation according to one embodiment.

[FIG. 8A]

Fig. 8A depicts a method, in a transmitter, for transmitting binary data using a 16-ASK constellation defined as a union of two sub-constellations according to a specific embodiment.

[FIG. 8B]

Fig. 8B depicts a method, in a transmitter, for transmitting binary data using a 16-ASK constellation defined as a union of two sub-constellations according to a specific embodiment.

[FIG. 9A]

Fig. 9A depicts a method, in a transmitter, for transmitting binary data using a 16-ASK constellation defined as a union of two sub-constellations according to a specific embodiment.

[FIG. 9B]

Fig. 9B depicts a method, in a transmitter, for transmitting binary data using a 16-ASK constellation defined as a union of two sub-constellations according to a specific embodiment.

[FIG. 10A]

Fig. 10A depicts for a reference sub-constellation of a 16-ASK constellation and the probabilities of the last bit level according to a specific embodiment.

[FIG. 10B]

Fig. 10B depicts for a reference sub-constellation of a 16-ASK constellation and the probabilities of the last bit level according to a specific embodiment.

[FIG. 11]

Fig.11 illustrates schematically an example of hardware architecture of a transmitter according to a specific embodiment.

[Description of Embodiments]

[0026]

Fig.1 illustrates schematically a communication system 1 in which the present embodiments may be implemented. The communication system 1 comprises a transmitter 10 and a receiver 14 that are coupled to one another by way of a communication channel 12. The transmitter 10 is fed with input data by at least one binary source S_0 and outputs symbols selected in a given alphabet $\mathcal{X}$ of symbols. In one embodiment, the binary source S_0 is equiprobable. The input data are for example bits of an audio/video bitstream. In an exemplary embodiment, the alphabet $\mathcal{X}$ is a M-ASK constellation,

where $M=2^m$ with M and m being integers. The symbols of a M -ASK constellations are defined as follows:

$$\mathcal{X} = \{-2^m + 1, \dots, -3, -1, +1, +3, \dots, +2^m - 1\}.$$

[0027]

Consequently, each symbol in this constellation can be represented by a sequence of $m = \log_2 M$ bits. Fig. 2 depicts the symbols of an 8-ASK constellation wherein the first symbol is -7 and the last one is 7. In the following, the various embodiments are described with reference to the ASK constellation. It will be appreciated, however, that the present embodiments are not restricted to the ASK constellation. As an example, it may also be used with a one dimensional constellation where the symbols have different values than the one specified in the above equation, such as the one obtained with geometric shaping (in this case geometric and probabilistic shaping would be combined).

[0028]

With reference to Fig. 1, let X be a discrete random variable representing the symbols at the input of the communication channel 12 with probability distribution $p(x_i) = p(X_i = x_i), x_i \in \mathcal{X}$. Let $p(y|x_i)$ be the channel distribution. e.g. with a Gaussian channel $p(y|x_i) \sim \mathcal{N}(x_i, \sigma^2)$, for all x_i . Let Y be a random variable representing the communication channel output. In the case of a Gaussian channel, Y is defined as follows: $Y = X + W$, where W is a Gaussian noise, e.g. $W \sim \mathcal{N}(0, \sigma^2)$.

[0029]

For the Gaussian channel, the signal-to-noise ratio (SNR) is defined as follows:

$$SNR = \frac{E[|X|^2]}{E[|W|^2]}$$

Given any communication channel, let $p^*(x)$ be the distribution of the input X that maximizes the mutual information (MI) for a given constellation

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$$p^*(x) = \arg \max_{p(x), E[|X|^2] \leq P} I(X; Y),$$

where P is the maximum average power. The quantity $\max_{E[|X|^2] \leq P} I(X; Y)$,

where the maximization is not only over the probability distribution but also over all possible inputs, is called the channel capacity. In the following, a discrete input is considered and optimization is only done over its distribution. The constellation (i.e., the set of positions of the elements of the discrete input) is not an optimization variable.

[0030]

$\widehat{p}^*(x)$ is defined as the set of quasi-optimal distributions, i.e.

$$p(x) \in \widehat{p}^*(x) \text{ if } I(X; Y) \geq \arg \max_{p(x), E[|X|^2] \leq P} I(X; Y) - \varepsilon,$$

where ε is a quantity whose magnitude depends on the requirements of the communication systems.

[0031]

The aim of probabilistic shaping is to process the input such that its probability distribution maximizes, or almost maximizes, the mutual information $I(X; Y)$. Said otherwise, the distribution of the input should be in $\widehat{p}^*(x)$.

[0032]

For the M-ASK constellation, $p(x)$ is often chosen as the MB distribution (English acronym of “Maxwell-Boltzmann distribution”). Indeed, in this case, the obtained performance is close to the one obtained with $p^*(x)$ (i.e. $p_{MB}(x) \in \widehat{p}^*(x)$ for ε small). The MB distribution can be quantized at the cost of negligible performance loss. As an example, a quantized distribution for a 16-ASK constellation as illustrated on Fig.3 exhibits quasi-optimal performance and thus can be used as a target shaping distribution.

[0033]

According to the present principles, the target shaping distribution is

quantized such that it can be expressed as the union of at least two sub-constellations where, for any symbol with a given probability value p_i in the first sub-constellation, there is a symbol in the other sub-constellation with the same probability value p_i . The first sub-constellation is called the reference sub-constellation and its distribution the reference distribution. On Fig. 3, the distribution of the reference sub-constellation is identified with bold lines.

[0034]

In one embodiment, the target shaping distribution is quantized such that two adjacent symbols have the same probability value. This is the case of the distribution illustrated on Fig.3. For the $M=16$ -ASK constellation, $\log_2(M) = 4$ bits are required for the labelling of the symbols. In one embodiment, the natural labelling of the symbols in this constellation is used and provided by the following table 1.

Symbols	-15	-13	-11	-9	-7	-5	-3	-1	1	3	5	7	9	11	13	15
Bit-level 1 (b_1)	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1
Bit level 2 (b_2)	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1
Bit level 3 (b_3)	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1
Bit level 4 (b_4)	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1

Table 1

[0035]

The bit level 4 is the sign bit and is used as a shaping bit. The first bit level b_1 which is the parity bit discriminates between the two sub-constellations as shown on Fig. 4. Indeed, the adjacent symbols with the same probability (according to Fig.3) have a different value for b_1 . The symbols of same probability values have the same remaining labelling bits (bit-level 2 to 4), e.g.

-15 and -13. Hence, the whole 16-ASK constellation $\mathcal{X}$ may be expressed as the union of a reference constellation $\mathcal{X}_r$ and a shifted version of this reference constellation. The reference sub-constellation $\mathcal{X}_r$ comprises the symbols in grey cells of table 1, i.e. $\{-15; -11; -7, -3, 1, 5, 9, 13\}$. The second sub-constellation comprises the other symbols. Said otherwise, $\mathcal{X} = \mathcal{X}_r \cup (\mathcal{X}_r + 2) = \cup_{a_i \in \alpha} \mathcal{X}_r + a_i$, where $\alpha = \{0, 2\}$. Moreover, a transmitted symbol belongs equiprobably to one of the two sub-constellations.

[0036]

In another embodiment, Gray labelling of the symbols in this constellation is used and provided by the following table 2.

Symbols	-15	-13	-11	-9	-7	-5	-3	-1	1	3	5	7	9	11	13	15
Bit-level 1 (b ₁)	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1	0
Bit level 2 (b ₂)	0	0	1	1	1	1	0	0	0	0	1	1	1	1	0	0
Bit level 3 (b ₃)	0	0	0	0	1	1	1	1	1	1	1	1	0	0	0	0
Bit level 4 (b ₄)	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1
S	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1

Table 2

[0037]

As in the case of natural labelling (Table 1), the whole 16-ASK constellation $\mathcal{X}$ may be expressed as the union of a reference constellation $\mathcal{X}_r$ and a shifted version of this reference constellation. The bit level 1 is used as the parity bit and enables to discriminate between the two sub-constellations. Indeed, the adjacent symbols with the same probability (according to Fig.3) have a different value for b₁. Therefore, as in the case of natural labelling, the bits b₂, b₃ and b₄ are used to label the symbols in $\mathcal{X}_r$.

[0038]

The reference sub-constellation $\mathcal{X}_r$ comprises the symbols in grey cells of the above table 2. The second sub-constellation comprises the other symbols. However, unlike with natural labelling, the rule to discriminate between the sub-constellations depends on the value of b_2 , b_3 and b_4 , more precisely on the value of a sum S . For each symbol, the sum S of its bit-levels is computed modulo 2. This sum S (last line of Table 2) is used in addition to the parity bit b_1 to discriminate between the two sub-constellations.

[0039]

In another embodiment, the target shaping distribution is quantized such that two symbols which are not necessarily adjacent have the same probability value. In this case, the sub-constellations are not “shifts” of each other. This is the case of the distribution of an 8-ASK constellation illustrated on Fig.5. On Fig.5, the symbols -3 and 5 have the same probability values but are not adjacent while the symbols -7 and -5 have the same probability value and are adjacent. On this figure, the distribution of the reference sub-constellation is identified with bold lines.

[0040]

For the $M=8$ -ASK constellation, $\log_2(M) = 3$ bits are required for the labelling. The labelling of the symbols in this constellation is provided by the following table 3.

Symbols	-7	-5	-3	-1	1	3	5	7
Bit level 1	0	1	0	0	1	0	1	1
Bit level 2	0	0	1	0	0	1	1	1
Bit level 3	0	0	0	1	1	1	0	1

Table 3

[0041]

The bit level 3 is the sign bit and is used as a shaping bit. The first bit level discriminates between the two sub-constellations. The symbols of same probability values have the same remaining labelling bits (bit-level 2 to 3). The reference sub-constellation $\mathcal{X}_r$ comprises the symbols in grey cells of table 1. The second sub-constellation comprises the other symbols.

[0042]

The method can be extended to cases with more than two sub-constellations, wherein for any symbol in the reference sub-constellation, there is a symbol in each of the other sub-constellations with a same probability value. Given N sub-constellations, N being an integer, $\log_2(N)$ bits are required to label and thus identify each of the N sub-constellations. Consequently, there should be $\log_2(N)$ parity bits for each symbol of the reference sub-constellation in order to identify a sub-constellation to which the symbol belongs.

[0043]

Fig. 6 depicts a method, in a transmitter, for transmitting data using a constellation with $M = 2^m$ symbols according to a specific embodiment.

[0044]

In a step S100, k groups of $m - \log_2(N)$ shaping bits wherein each group of $m - \log_2(N)$ shaping bits identifies one symbol in the reference sub-constellation $\mathcal{X}_r$ are obtained from a source of data S. In a specific embodiment, the source of data S is equiprobable.

[0045]

In an exemplary embodiment, the k groups of $m - \log_2(N)$ bits are obtained as disclosed on Fig.6 by using a distribution matcher in a step S100-1 to transform data of the source S into k symbols $\{x_1, x_2, \dots, x_k\}$, where each of the k symbols is in the reference sub-constellation $\mathcal{X}_r$. The constant composition distribution matcher disclosed in the document from Schulte et al

entitled “*Constant composition distribution matching*” published in IEEE Transactions on Information Theory 62(1), Nov. 2015, is an example of such a distribution matcher. Any other arbitrary types of distribution matchers may be used. The symbols in the reference sub-constellation $\mathcal{X}_r$ are approximately distributed according to the target distribution of the reference sub-constellation $\mathcal{X}_r$. An example of such a target distribution in the case where $N=2$ and the constellation is the 16-ASK constellation is depicted on Fig. 7.

[0046]

Each symbol $x_j \in \{x_1, x_2, \dots, x_k\}$, j being an integer in $[1;k]$, is labelled in a step S100-2 with a group $b(x_j)$ of $m - \log_2(N)$ bits called shaping bits, where $b(\cdot)$ is a labelling function, e.g. a natural labelling function or a Gray labeling function. The k groups of $m - \log_2(N)$ shaping bits $\{b(x_1), b(x_2), \dots, b(x_k)\}$ which thus corresponds to the k symbols $\{x_1, x_2, \dots, x_k\}$ are used as input to a systematic error correcting code P which outputs, in a step S104, one group of $\log_2(N)$ parity bits per each symbol x_j , x_j being in the reference constellation $\mathcal{X}_r$. An example of a systematic error correcting code is disclosed in section VII of the document from Böcherer et al entitled “*Bandwidth Efficient and Rate-Matched Low-Density Parity-Check Coded Modulation*”.

[0047]

In a step S106, each group of $\log_2(N)$ parity bits identifies a sub-constellation among the N sub-constellations and the symbol identified by said $m - \log_2(N)$ shaping bits in said identified sub-constellation is selected.

[0048]

In a step S108, the selected symbols are finally transmitted to a receiver over a communication channel.

[0049]

Fig. 8A depicts a method, in a transmitter, for transmitting data, in the specific case where $N=2$ and natural labelling is used.

[0050]

In the step S100, k groups of $m - 1$ shaping bits wherein each group of $m - 1$ shaping bits identifies one symbol in the reference sub-constellation $\mathcal{X}_r$ are obtained from a source of data S.

[0051]

In an exemplary embodiment, the k groups of $m - 1$ shaping bits are obtained as disclosed on Fig. 8A by using a distribution matcher in the step S100-1 to transform uniform data blocks of a source S into k symbols $\{x_1, x_2, \dots, x_k\}$, where x_i is in the reference sub-constellation $\mathcal{X}_r$. Any arbitrary types of distribution matchers may be used. The symbols in the reference sub-constellation $\mathcal{X}_r$ are approximately distributed according to the target distribution of the reference sub-constellation $\mathcal{X}_r$. An example of such a target distribution in the case where $N=2$ and the constellation is the 16-ASK constellation is depicted on Fig. 7. In this case, 3 shaping bits are obtained per symbol $x_j \in \{x_1, x_2, \dots, x_k\}$.

[0052]

Each symbol $x_j \in \{x_1, x_2, \dots, x_k\}$, j being an integer in $[1;k]$, is labelled in the step S100-2 using a natural labelling function with a group $b(x_j)$ of bits called shaping bits, namely 3 bits in case of a 16-ASK constellation. The k groups of shaping bits $\{b(x_1), b(x_2), \dots, b(x_k)\}$ corresponding to these symbols $\{x_1, x_2, \dots, x_k\}$ are used as input to a systematic error correcting code P which outputs, in the step S104, one parity bit b_1^j per each symbol x_j , x_j being in the reference constellation $\mathcal{X}_r$.

[0053]

In the step S106, each parity bit b_1^j determines a shift value α^j in the set $\alpha = \{0, 2\}$ for the symbol x_j of the reference sub-constellation. Thus, the parity bit b_1^j identifies in which sub-constellation the symbol to be transmitted should

be chosen. As an example, if the parity bit $b_1^j = 0$ then the symbol x_j is from the first sub-constellation while if the parity bit $b_1^j = 1$ then the symbol x_j is from the second sub-constellation. This is a convention and an opposite convention may be used, wherein if the parity bit $b_1^j = 0$ then the symbol x_j is from the second sub-constellation while if the parity bit $b_1^j = 1$ then the symbol x_j is from the first sub-constellation. The determined shift value is added to the symbol x_j of the reference sub-constellation.

[0054]

In the step S108, the selected symbols are finally transmitted to a receiver over a communication channel. Thus, in the case where $\alpha^j = 0$, the transmitted symbol is the symbol x_j the reference, and in the case where $\alpha^j = 2$, the symbol in the shifted sub-constellation is transmitted.

[0055]

Fig. 8B depicts a method, in a transmitter, for transmitting data, in the specific case where $N=2$ and Gray labelling is used.

[0056]

In the step S100, k groups of $m - 1$ shaping bits wherein each group of $m - 1$ shaping bits identifies one symbol in the reference sub-constellation $\mathcal{X}_r$ are obtained from a source of data S .

[0057]

In an exemplary embodiment, the k groups of $m - 1$ shaping bits are obtained as disclosed on Fig. 8B by using a distribution matcher in the step S100-1 to transform uniform data blocks of a source S into k symbols $\{x_1, x_2, \dots, x_k\}$, where x_i is in the reference sub-constellation $\mathcal{X}_r$. Any arbitrary types of distribution matchers may be used. The symbols in the reference sub-constellation $\mathcal{X}_r$ are approximately distributed according to the target distribution of the reference sub-constellation $\mathcal{X}_r$. An example of such a target

distribution in the case where $N=2$ and the constellation is the 16-ASK constellation is depicted on Fig. 7. In this case, 3 shaping bits are obtained per symbol $x_j \in \{x_1, x_2, \dots, x_k\}$.

[0058]

Each symbol $x_j \in \{x_1, x_2, \dots, x_k\}$, j being an integer in $[1;k]$, is labelled in the step S100-2 using a Gray labelling function with a group $b(x_j)$ of bits called shaping bits, namely 3 bits in case of a 16-ASK constellation. The k groups of shaping bits $\{b(x_1), b(x_2), \dots, b(x_k)\}$ corresponding to these symbols $\{x_1, x_2, \dots, x_k\}$ are used as input to a systematic error correcting code P which outputs, in the step S104, one parity bit b_1^j per each symbol x_j , x_j being in the reference constellation $\mathcal{X}_r$.

[0059]

In the step S106, for each parity bit b_1^j , a sum S_j of the parity bit b_1^j and of the associated shaping bits $b(x_j)$ is computed modulo 2, i.e. $S_j = \text{MOD}(\sum_{n=1}^m b_n^j, 2)$, where the shaping bits $b(x_j) = \{b_2^j, b_3^j, \dots, b_m^j\}$. Double the sum S_j is the shift value α^j in the set $\alpha = \{0, 2\}$ for the symbol x_j of the reference sub-constellation, i.e. $\alpha^j = 2 * S_j$. The determined shift value is added to the symbol x_j of the reference sub-constellation. Thus, in the case where $\alpha^j = 0$, the transmitted symbol is the symbol x_j the reference, and in the case where $\alpha^j = 2$, the symbol in the shifted sub-constellation is transmitted.

[0060]

In the step S108, the selected symbols are finally transmitted to a receiver over a communication channel.

[0061]

In the embodiments disclosed with respect to Figs 6, 8A and 8B, the parity bit is used to identify one sub-constellation among the sub-constellations whose union form the main constellation, e.g. a 16-ASK constellation.

Consequently, the sign bit is available for the shaping operation. Therefore, sign-bit shaping can be advantageously combined with systematic error-correcting code as depicted on Figs 9A and 9B.

[0062]

Fig. 9A depicts a method, in a transmitter, for transmitting binary data, in the specific case where a 16-ASK constellation is considered and $N=2$ according to another embodiment. In this embodiment, natural labelling is used.

[0063]

The target distribution depicted on Fig. 7 can be realized as shown on Fig. 9A.

[0064]

In the step S100, k groups of 3 shaping bits $b_2^j b_3^j b_4^j$ wherein each group identifies one symbol x_j in the reference sub-constellation $\mathcal{X}_r$ are obtained from a source of data S_0 . In one specific embodiment, the second and third bit levels in table 1, i.e. $b_2^j b_3^j$, are equiprobable and independent. Therefore, these two bits $b_2^j b_3^j$ are obtained from a binary source S_0 . The output of the source S_0 is used as input of four binary DMs, namely DM1, DM2, DM3 and DM4. These binary DMs output four sequences of bits identified as four binary non-equiprobable sources S_1, S_2, S_3 and S_4 . The probability of the last bit level, i.e. the sign bit b_4^j , is chosen based on the value of $b_2^j b_3^j$, i.e. $p(b_4^j | b_2^j b_3^j)$, and is independent of the value of b_1^j . Consequently, a switch selects a given non-equiprobable source (S_1, S_2, S_3 or S_4) based on the values of b_2^j and b_3^j . The different values for $p(b_4^j | b_2^j b_3^j)$ are depicted on Fig. 10A.

[0065]

On Fig. 10A, the parameters p_i represent the probabilities of the last bit level b_4^j conditioned on the values of b_2^j and b_3^j .

[0066]

In the specific case of a symmetric target distribution (in the case of a Gaussian channel), i.e. $p_1'=p_1$ and $p_2'=p_2$, , the number of non-equiprobable sources is divided by two and thus the switch selects a given non-equiprobable source (S_1 or S_2) based on the value of b_2^j , e.g. S_1 is selected in the case where $b_2^j = 0$ and S_2 is selected otherwise.

[0067]

Taking into account this symmetry, the shaping encoder is simplified with the number of binary sources being divided by two and bit flipping being used. This shaping method is disclosed in the patent application EP21305730.0 filed on June 1st, 2021.

[0068]

The k groups of shaping bits $\{b_2^j b_3^j b_4^j\}_{j \in [1;k]}$ corresponding to the symbols $\{x_1, x_2, \dots, x_k\}$ are used as input to a systematic error correcting code P which outputs, in the step S104, one parity bit b_1^j per each symbol x_j , x_j being in the reference constellation $\mathcal{X}_r$.

[0069]

In the step S106, each parity bit b_1^j identifies a sub-constellation among the N sub-constellations and the symbol identified by said $\{b_2^j b_3^j b_4^j\}$ shaping bits in said identified sub-constellation is selected.

[0070]

In the step S108, the selected symbols are finally transmitted to a receiver over a communication channel.

[0071]

Fig. 9B depicts a method, in a transmitter, for transmitting binary data, in the specific case where a 16-ASK constellation is considered and $N=2$ according to another embodiment. In this embodiment, Gray labelling is used.

[0072]

The target distribution depicted on Fig.7 can be realized as shown on Fig. 9B.

[0073]

In the step S100, k groups of 3 shaping bits $b_2^j b_3^j b_4^j$ wherein each group identifies one symbol x_j in the reference sub-constellation $\mathcal{X}_r$ are obtained from a source of data S_0 . In one specific embodiment, the second and fourth bit levels in table 2, i.e. $b_2^j b_4^j$, are equiprobable and independent. Therefore, these two bits $b_2^j b_4^j$ are obtained from a binary source S_0 . The output of the source S_0 is used as input of four binary DMs, namely DM1, DM2, DM3 and DM4. These binary DMs output four sequences of bits identified as four binary non-equiprobable sources S_1, S_2, S_3 and S_4 . The probability of the third bit level, i.e. the bit b_3^j , is chosen based on the values of b_2^j and b_4^j , i.e. $p(b_3^j | b_2^j b_4^j)$, and is independent of the value of b_1^j . Consequently, a switch selects a given non-equiprobable source (S_1, S_2, S_3 or S_4) based on the value of b_2^j and b_4^j . The different values for $p(b_3^j | b_2^j b_4^j)$ are depicted on Fig. 10B. On Fig. 10B, the parameters p_i represent the probabilities of the third bit level b_3^j conditioned on the values of b_2^j and b_4^j . In the specific case where $p_1' = p_1$ and $p_2' = p_2$, then $p(b_3^j | b_2^j b_4^j) = p(b_3^j | b_2^j)$. In this case, the number of non-equiprobable sources is divided by two and thus the switch selects a given non-equiprobable source (S_1 or S_2) based on the value of b_2^j , e.g. S_1 is selected in the case where $b_2^j = 0$ and S_2 is selected otherwise.

[0074]

The k groups of shaping bits $\{b_2^j b_3^j b_4^j\}_{j \in [1, k]}$ corresponding to the symbols $\{x_1, x_2, \dots, x_k\}$ are used as input to a systematic error correcting code P which outputs, in the step S104, one parity bit b_1^j per each symbol x_j , x_j being

in the reference constellation $\mathcal{X}_r$.

[0075]

In the step S106, for each parity bit b_1^j , a sum S_j of the parity bit b_1^j and of the associated shaping bits $b(x_j)$ is computed modulo 2, i.e. $S_j = \text{MOD} \sum_{n=1}^4 b_n^j, 2$. Double the sum S_j is the shift value α^j in the set $\alpha = \{0, 2\}$ for the symbol x_j of the reference sub-constellation, i.e. $\alpha^j = 2 * S_j$. The determined shift value is added to the symbol x_j of the reference sub-constellation obtained by mapping the shaping bits $\{b_2^j b_3^j b_4^j\}$ to a symbol x_j in the reference sub-constellation. Thus, in the case where $\alpha^j = 0$, the transmitted symbol is the symbol x_j the reference, and in the case where $\alpha^j = 2$, the symbol in the shifted sub-constellation is transmitted.

[0076]

In the step S108, the selected symbols are finally transmitted to a receiver over a communication channel.

[0077]

Fig. 11 illustrates schematically an example of hardware architecture of a transmitter 10 according to a specific embodiment.

[0078]

The transmitter 10 comprises, connected by a communication bus 110: a processor or CPU (acronym of “Central Processing Unit”) 101; a random access memory RAM 112; a read only memory ROM 113; a storage unit 114 such as an hard disk or such as a storage medium reader, e.g. a SD (acronym of “Secure Digital”) card reader; and at least one set of communication interfaces COM 115 enabling the transmitter 10 to transmit and receive data.

[0079]

The processor 111 is capable of executing instructions loaded into the RAM 112 from the ROM 113, from an external memory (such as an SD card),

from a storage medium (such as the HDD), or from a communication network. When the transmitter 10 is powered up, the processor 111 is capable of reading instructions from the RAM 112 and executing them. These instructions form a computer program causing the implementation, by the processor 111, of the methods described in relation to Figs. 6, 8 and 9.

[0080]

The methods described in relation to Figs. 6, 8 and 9 may be implemented in software form by the execution of the set of instructions by a programmable machine, for example a DSP (acronym of “Digital Signal Processor”), a microcontroller or a GPU (acronym of “Graphics Processing Unit”), or be implemented in hardware form by a machine or a dedicated component (chip or chipset), for example an FPGA (acronym of “Field-Programmable Gate Array”) or an ASIC (acronym of “Application-Specific Integrated Circuit”). In general, the transmitter 10 includes electronic circuitry adapted and configured for implementing the methods described in relation to Figs. 6, 8 and 9.

[CLAIMS]

[Claim 1]

A method, in a transmitter, for transmitting data using a constellation with $M = 2^m$ symbols, divided in N sub-constellations, N and M being integers, where for any symbol in a reference sub-constellation, there is a symbol in each of the other sub-constellations with a same probability value, comprising:

- obtaining from a source of data, k groups of $m - \log_2(N)$ shaping bits wherein each group of $m - \log_2(N)$ shaping bits identifies one symbol x_j in the reference sub-constellation, $j \in [1;k]$;
- applying a systematic error correcting code on said k groups of $m - \log_2(N)$ shaping bits to output one group of $\log_2(N)$ parity bits per each symbol x_j ;
- for each symbol x_j , identifying a sub-constellation using at least the group of $\log_2(N)$ parity bits and selecting a symbol identified by said $m - \log_2(N)$ shaping bits in said identified sub-constellation; and
- transmitting each of said k selected symbols to a receiver over a communication channel.

[Claim 2]

The method according to claim 1, wherein obtaining from a source of data, k groups of $m - \log_2(N)$ shaping bits wherein each group of $m - \log_2(N)$ shaping bits identifies one symbol x_j in the reference sub-constellation, $j \in [1;k]$ comprises:

- Applying a distribution matcher on said data of said source to obtain k symbols x_j in the reference sub-constellation ; and
- Labelling each symbol with a group of $m - \log_2(N)$ shaping bits using a labelling function.

[Claim 3]

The method according to claim 2, wherein the labelling function is a natural labelling function.

[Claim 4]

The method according to claim 2, wherein the labelling function is a Gray labelling function.

[Claim 5]

The method according to any one of claims 1 to 4, wherein $N=2$ and wherein for each symbol x_j , identifying a sub-constellation using at least the group of $\log_2(N)$ parity bits and selecting a symbol identified by said $m - \log_2(N)$ shaping bits in said identified sub-constellation comprises : selecting a shift value in the set $\{0; 2\}$ responsive to at least the group of $\log_2(N)$ parity bits and adding the selected shift value to the symbol x_j of the reference constellation to obtain the symbol to transmit.

[Claim 6]

The method according to claim 5, wherein selecting a shift value in the set $\{0; 2\}$ responsive to at least the group of $\log_2(N)$ parity bits comprises selecting a shift value responsive to double a sum modulo 2 of the group of $\log_2(N)$ parity bits and of the corresponding $m - \log_2(N)$ shaping bits.

[Claim 7]

The method according to any one of claims 1 to 6, wherein the constellation is an M-ASK constellation.

[Claim 8]

The method according to any one of claims 1 to 7, wherein said source of data is an equiprobable source.

[Claim 9]

A transmitter configured to transmit data using a constellation with $M = 2^m$ symbols, divided in N sub-constellations, N and M being integers, where for any symbol in a reference sub-constellation, there is a symbol in

each of the other sub-constellations with a same probability value, the transmitter comprises at least one processor configured to:

- obtain from a source of data, k groups of $m - \log_2(N)$ shaping bits wherein each group of $m - \log_2(N)$ shaping bits identifies one symbol x_j in the reference sub-constellation, $j \in [1; k]$;
- apply a systematic error correcting code on said k groups of $m - \log_2(N)$ shaping bits to output one group of $\log_2(N)$ parity bits per each symbol x_j ;
- for each symbol x_j , identify a sub-constellation using at least the group of $\log_2(N)$ parity bits and select a symbol identified by said $m - \log_2(N)$ shaping bits in said identified sub-constellation; and
- transmit each of said k selected symbols to a receiver over a communication channel.

[Claim 10]

The transmitter according to claim 9, wherein to obtain from a source of data, k groups of $m - \log_2(N)$ shaping bits wherein each group of $m - \log_2(N)$ shaping bits identifies one symbol x_j in the reference sub-constellation, $j \in [1; k]$ comprises:

- to apply a distribution matcher on said data of said source to obtain k symbols x_j in the reference sub-constellation ; and
- to label each symbol with a group of $m - \log_2(N)$ shaping bits using a labelling function.

[Claim 11]

The transmitter according to claim 10, wherein the labelling function is a natural labelling function.

[Claim 12]

The transmitter according to claim 10, wherein the labelling function is a Gray labelling function.

[Claim 13]

The transmitter according to any one of claims 9 to 12, wherein $N=2$ and wherein for each symbol x_j , to identify a sub-constellation using at least the group of $\log_2(N)$ parity bits and to select a symbol identified by said $m - \log_2(N)$ shaping bits in said identified sub-constellation comprises : to select a shift value in the set $\{0; 2\}$ responsive to at least the group of $\log_2(N)$ parity bits and to add the selected shift value to the symbol x_j of the reference constellation to obtain the symbol to transmit.

[Claim 14]

The transmitter according to claim 13, wherein to select a shift value in the set $\{0; 2\}$ responsive to at least the group of $\log_2(N)$ parity bits comprises to select a shift value responsive to double a sum modulo 2 of the group of $\log_2(N)$ parity bits and of the corresponding $m - \log_2(N)$ shaping bits.

[Claim 15]

A computer program product comprising program code instructions that can be loaded in a programmable device, the program code instructions causing implementation of the method according to any one of claims 1 to 8 when the program code instructions are run by the programmable device.

[Claim 16]

A storage medium storing a computer program comprising program code instructions, the program code instructions causing implementation of the method according to any one of claims 1 to 8 when the program code instructions are read from the storage medium and run by a programmable device.

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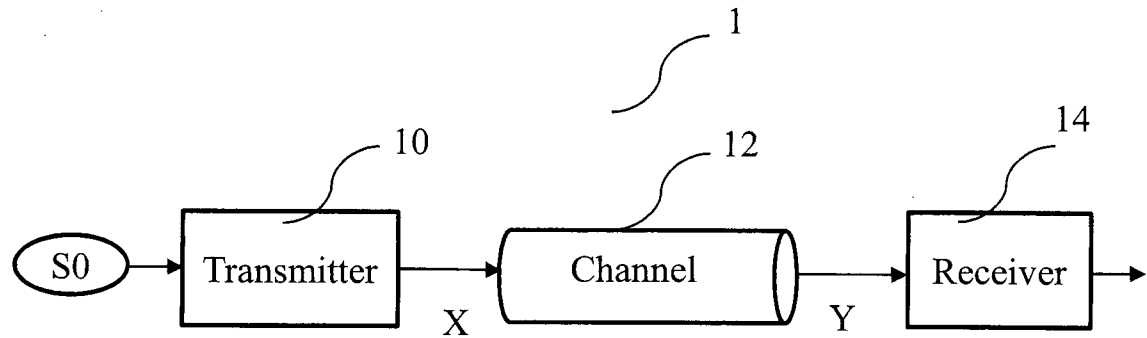


FIG. 1

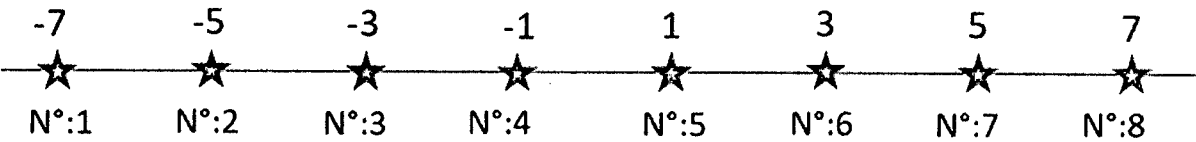


FIG. 2

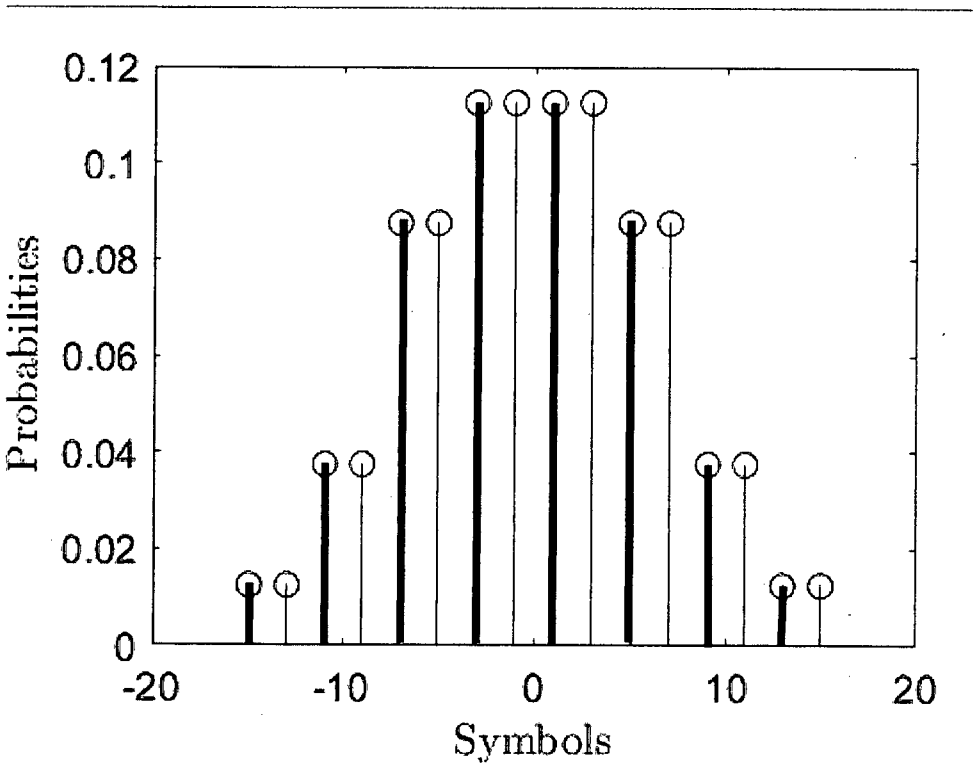


FIG. 3

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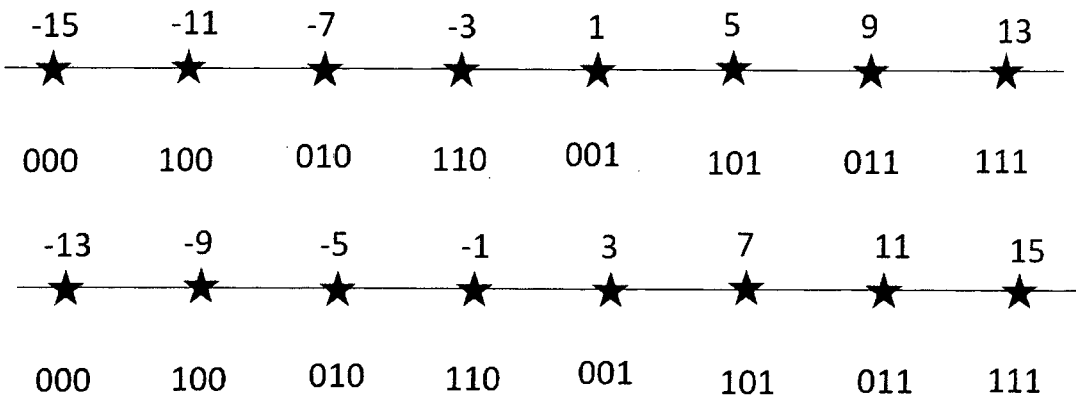


FIG. 4

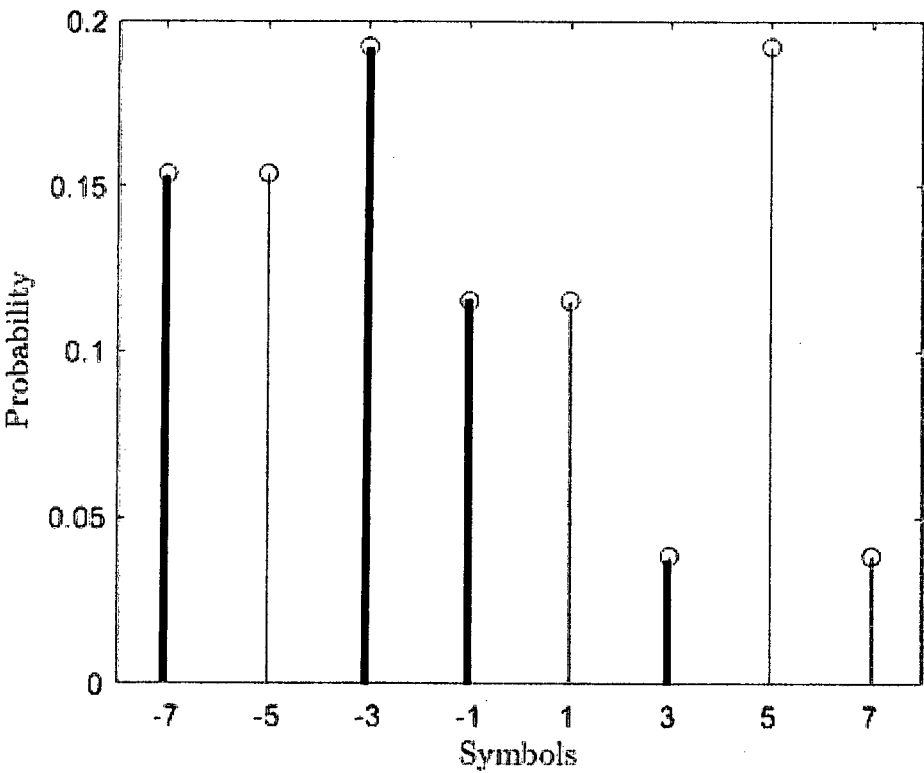


FIG. 5

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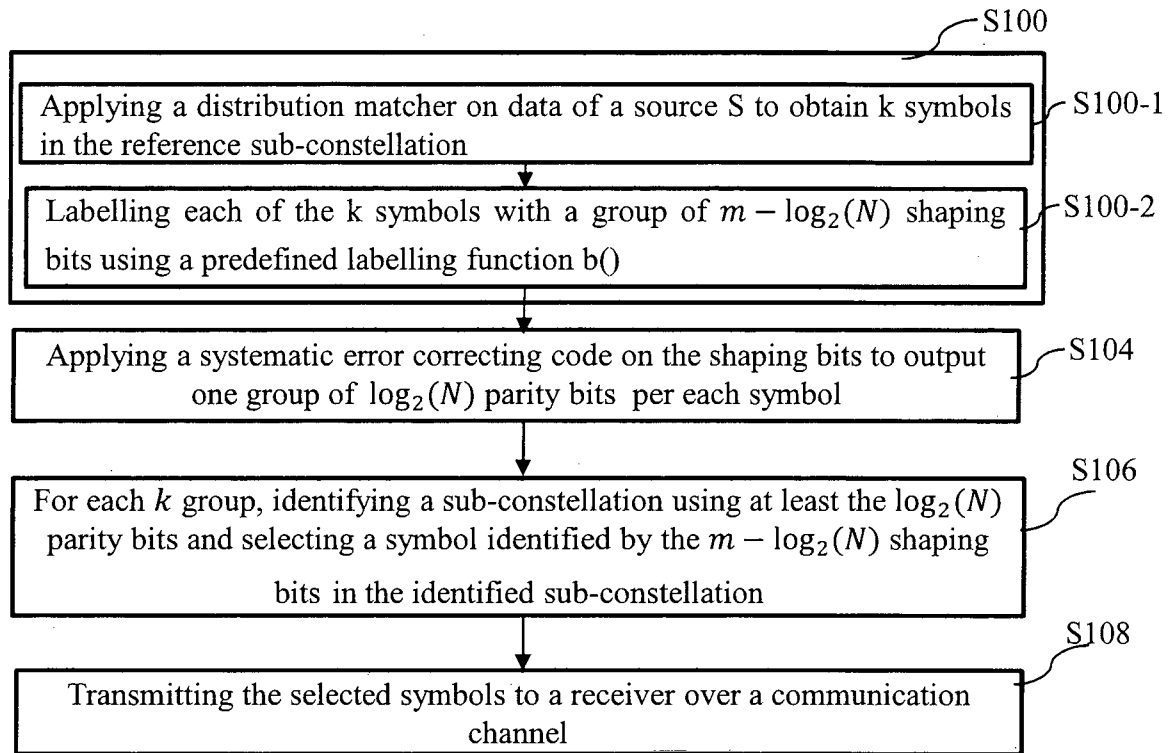


FIG. 6

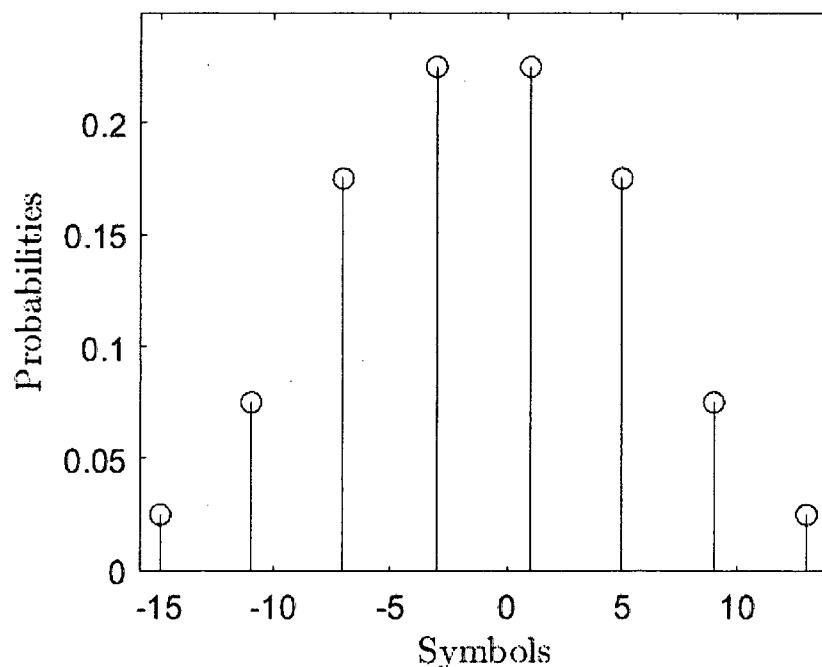


FIG. 7

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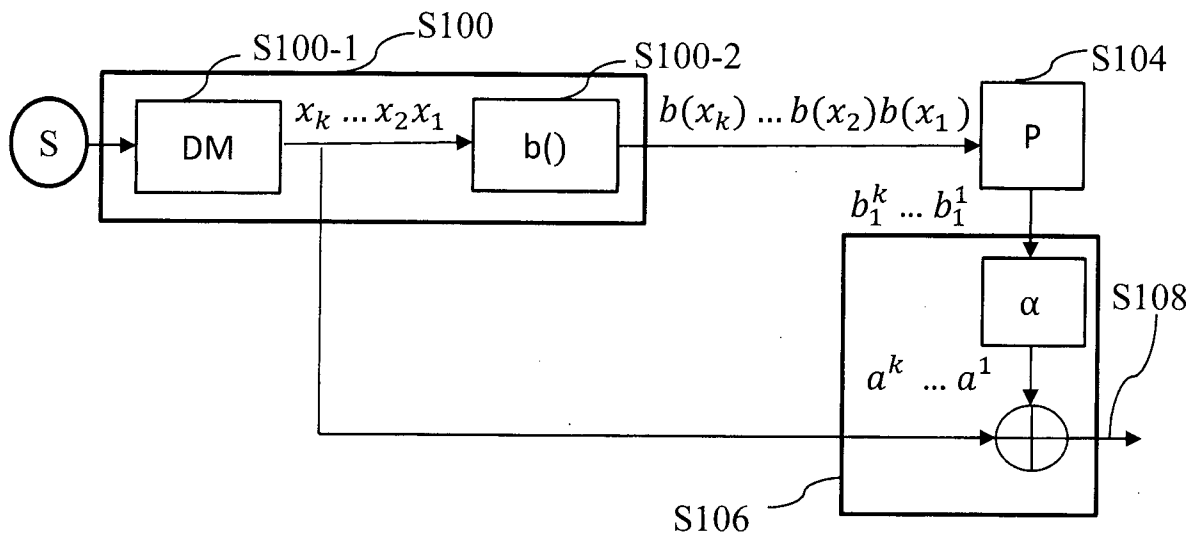


FIG. 8A

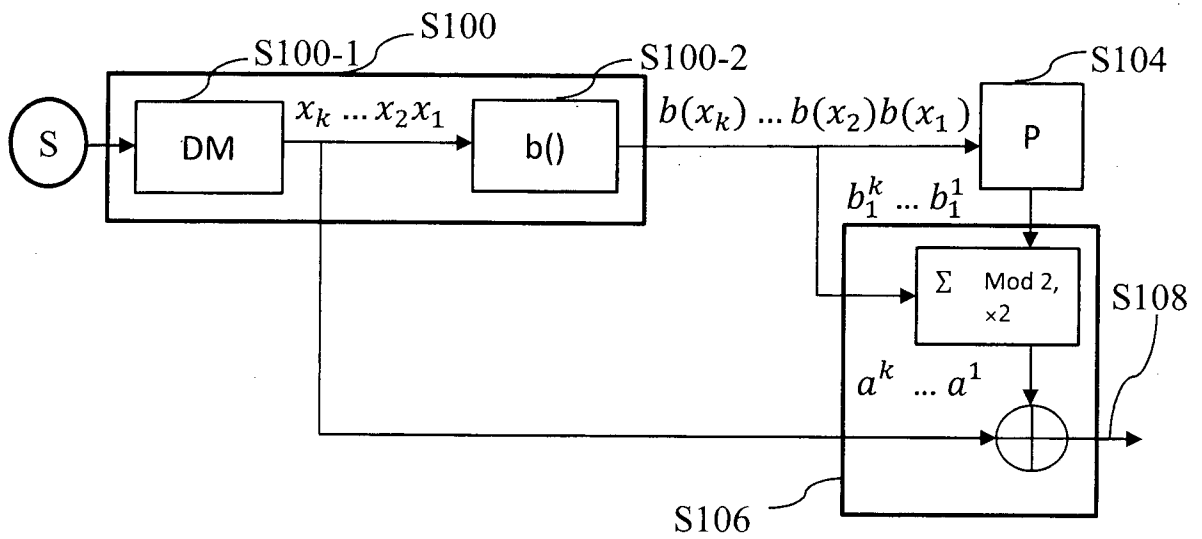


FIG. 8B

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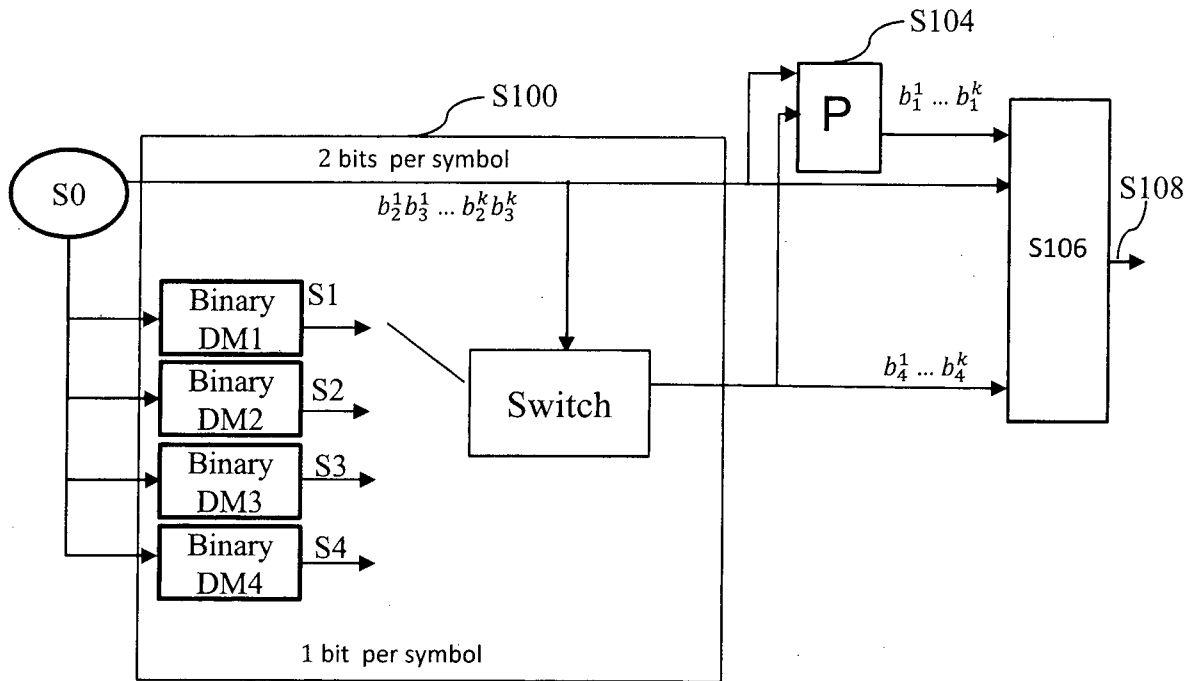


FIG. 9A

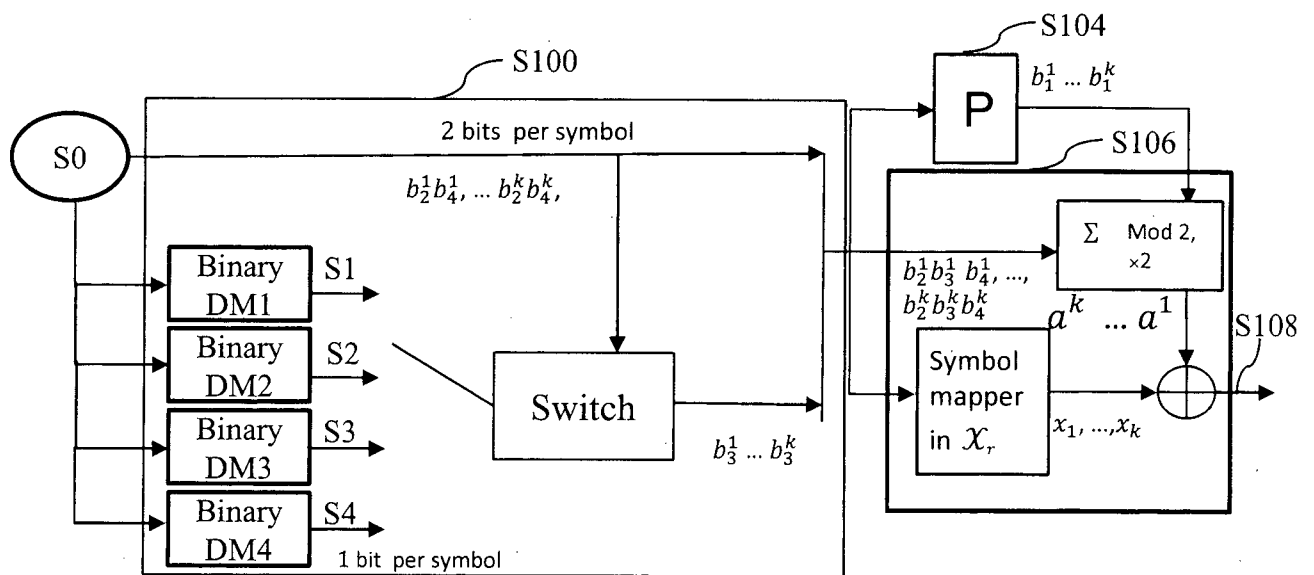


FIG. 9B

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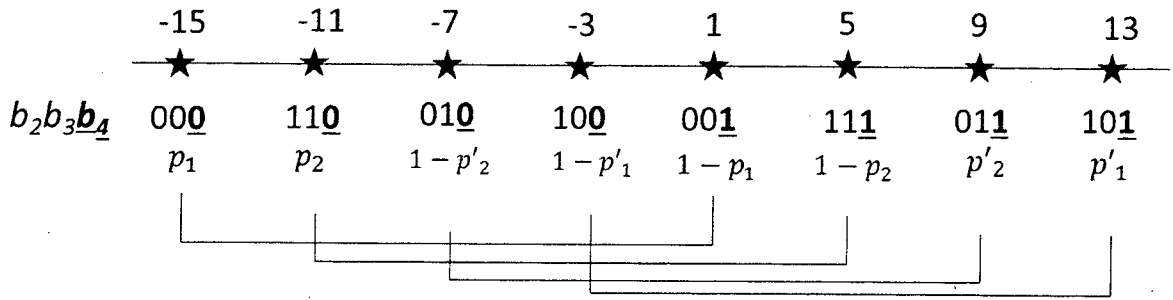


FIG. 10A

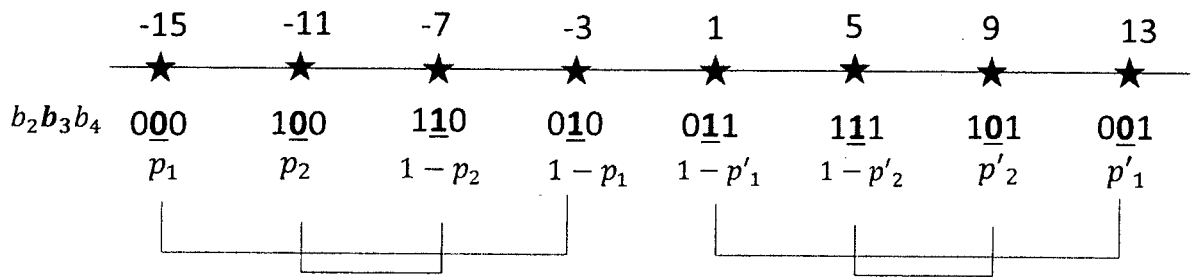


FIG. 10B

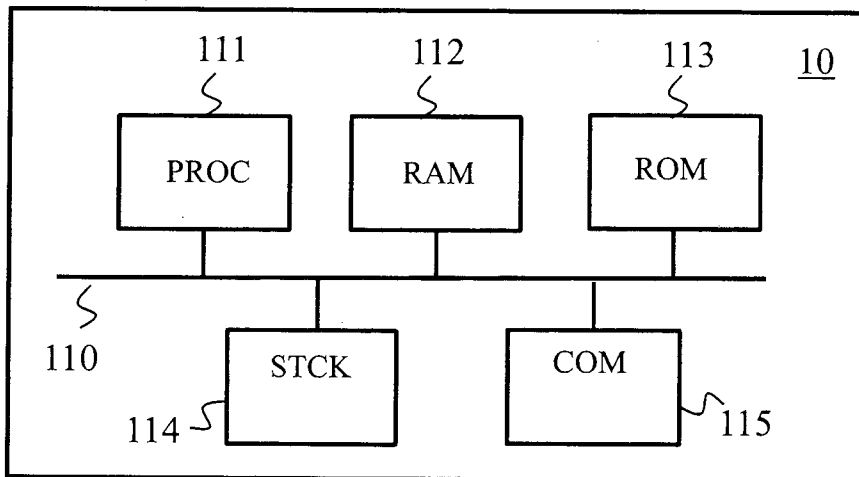


FIG. 11

INTERNATIONAL SEARCH REPORT

International application No

PCT/JP2022/033813

A. CLASSIFICATION OF SUBJECT MATTER**INV. H04L1/00****ADD.**

According to International Patent Classification (IPC) or to both national classification and IPC

B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)

H04L

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

Electronic data base consulted during the international search (name of data base and, where practicable, search terms used)

EPO-Internal, WPI Data**C. DOCUMENTS CONSIDERED TO BE RELEVANT**

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
X	FAYCAL AIT AOUDIA ET AL: "Joint Learning of Probabilistic and Geometric Shaping for Coded Modulation Systems", ARXIV.ORG, CORNELL UNIVERSITY LIBRARY, 201 OLIN LIBRARY CORNELL UNIVERSITY ITHACA, NY 14853, 10 April 2020 (2020-04-10), XP081641910, Sections I, II	1-16
A	EP 3 852 326 A1 (NOKIA TECHNOLOGIES OY [FI]) 21 July 2021 (2021-07-21) paragraphs [0041] - [0046]; figure 2 paragraphs [0053] - [0062]; figure 5 paragraphs [0076] - [0079]; figure 8	1-16



Further documents are listed in the continuation of Box C.



See patent family annex.

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"P" document published prior to the international filing date but later than the priority date claimed

"T" later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention

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"Y" document of particular relevance;; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art

"&" document member of the same patent family

Date of the actual completion of the international search

21 November 2022

Date of mailing of the international search report

29/11/2022

Name and mailing address of the ISA/

European Patent Office, P.B. 5818 Patentlaan 2

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Kreppel, Jan

INTERNATIONAL SEARCH REPORT

International application No
PCT/JP2022/033813

C(Continuation). DOCUMENTS CONSIDERED TO BE RELEVANT		
Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
A	US 2018/026725 A1 (CHO JOON HO [US]) 25 January 2018 (2018-01-25) paragraphs [0030] - [0036]; figures 2, 3A, 3B, 3C paragraphs [0082] - [0086]; figure 9 -----	1-16
A	WO 2019/034781 A1 (SONY CORP [JP]; SONY EUROPE LTD [GB]) 21 February 2019 (2019-02-21) paragraphs [0006] - [0011] paragraphs [0014] - [0041]; figures 1-5 -----	1-16

INTERNATIONAL SEARCH REPORT

Information on patent family members

International application No

PCT/JP2022/033813

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			EP 3852326 A1	21-07-2021
			US 2021218607 A1	15-07-2021

US 2018026725	A1	25-01-2018	NONE	

WO 2019034781	A1	21-02-2019	EP 3673594 A1	01-07-2020
			US 2020162193 A1	21-05-2020
			WO 2019034781 A1	21-02-2019
