

(12) **United States Patent**  
**Jain et al.**

(10) **Patent No.:** **US 11,066,917 B2**  
(45) **Date of Patent:** **Jul. 20, 2021**

(54) **EARTH-BORING TOOL RATE OF PENETRATION AND WEAR PREDICTION SYSTEM AND RELATED METHODS**

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(\*) Notice: Subject to any disclaimer, the term of this  
patent is extended or adjusted under 35  
U.S.C. 154(b) by 565 days.

(21) Appl. No.: **15/976,330**

(22) Filed: **May 10, 2018**

(65) **Prior Publication Data**  
US 2019/0345809 A1 Nov. 14, 2019

(51) **Int. Cl.**  
**E21B 44/00** (2006.01)  
**E21B 44/02** (2006.01)  
(Continued)

(52) **U.S. Cl.**  
CPC ..... **E21B 44/02** (2013.01); **E21B 21/08**  
(2013.01); **E21B 45/00** (2013.01); **E21B 47/26**  
(2020.05);  
(Continued)

(58) **Field of Classification Search**  
CPC . E21B 7/00; E21B 44/02; E21B 47/26; E21B  
21/08; E21B 49/003; E21B 45/00;  
(Continued)

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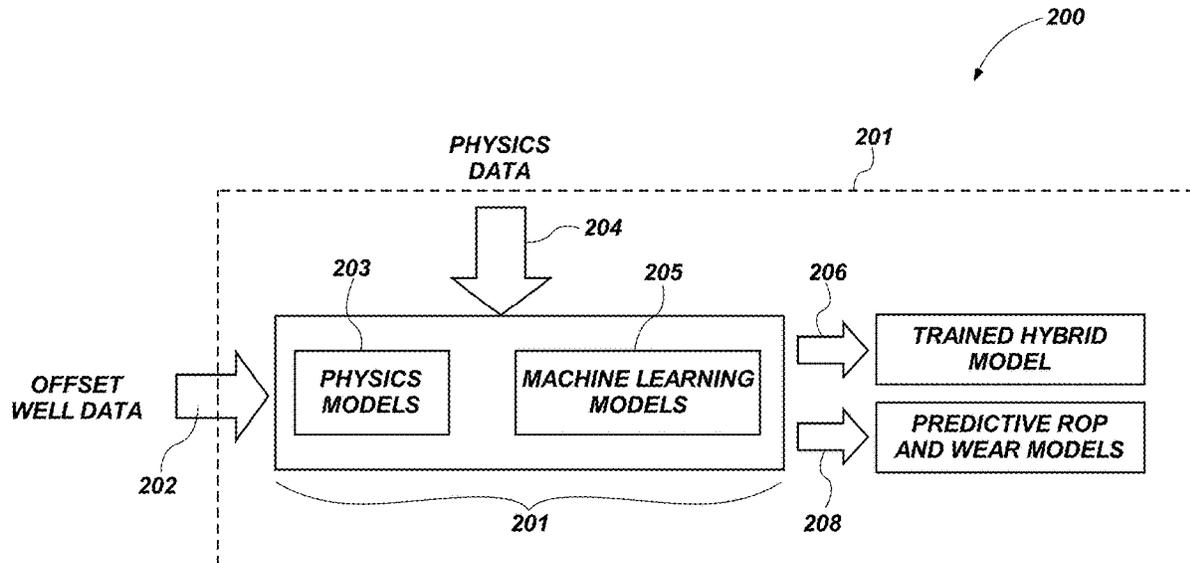
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(57) **ABSTRACT**

An earth-boring tool system that includes a drilling assembly for drilling a wellbore and a surface control unit. The surface control unit includes a prediction system that is configured to train a hybrid physics and machine-learning model based on input data, provide, via the hybrid model, a predictive model representing a rate of penetration of an earth-boring tool and wear of the earth-boring tool during a planned drilling operation, provide one or more recommendations of drilling parameters based on the predictive model, utilize the one or more recommendations in a drilling operation, receive real-time data from the drilling operation, retrain the hybrid model based on a combination of the input data and the real-time data, and provide, via the retrained model, an updated predictive model of a rate of penetration of an earth-boring tool and wear of the earth-boring tool during a remainder of the planned drilling operation.

**20 Claims, 10 Drawing Sheets**



- (51) **Int. Cl.**  
*E21B 21/08* (2006.01)  
*E21B 49/00* (2006.01)  
*E21B 45/00* (2006.01)  
*E21B 47/26* (2012.01)
- (52) **U.S. Cl.**  
 CPC ..... *E21B 49/003* (2013.01); *E21B 2200/22*  
 (2020.05)
- (58) **Field of Classification Search**  
 CPC ..... *E21B 2200/22*; *E21B 44/005*; *E21B 7/06*;  
*E21B 10/00*; *E21B 21/06*; *E21B 41/00*;  
*E21B 44/00*; *E21B 47/00*; *E21B 47/022*;  
*E21B 49/00*; *E21B 49/08*; *G01V 1/44*;  
*G01V 1/30*; *G01V 1/306*; *G06F 3/1454*;  
*G06F 30/20*; *G06F 17/18*; *G06F 17/5009*;  
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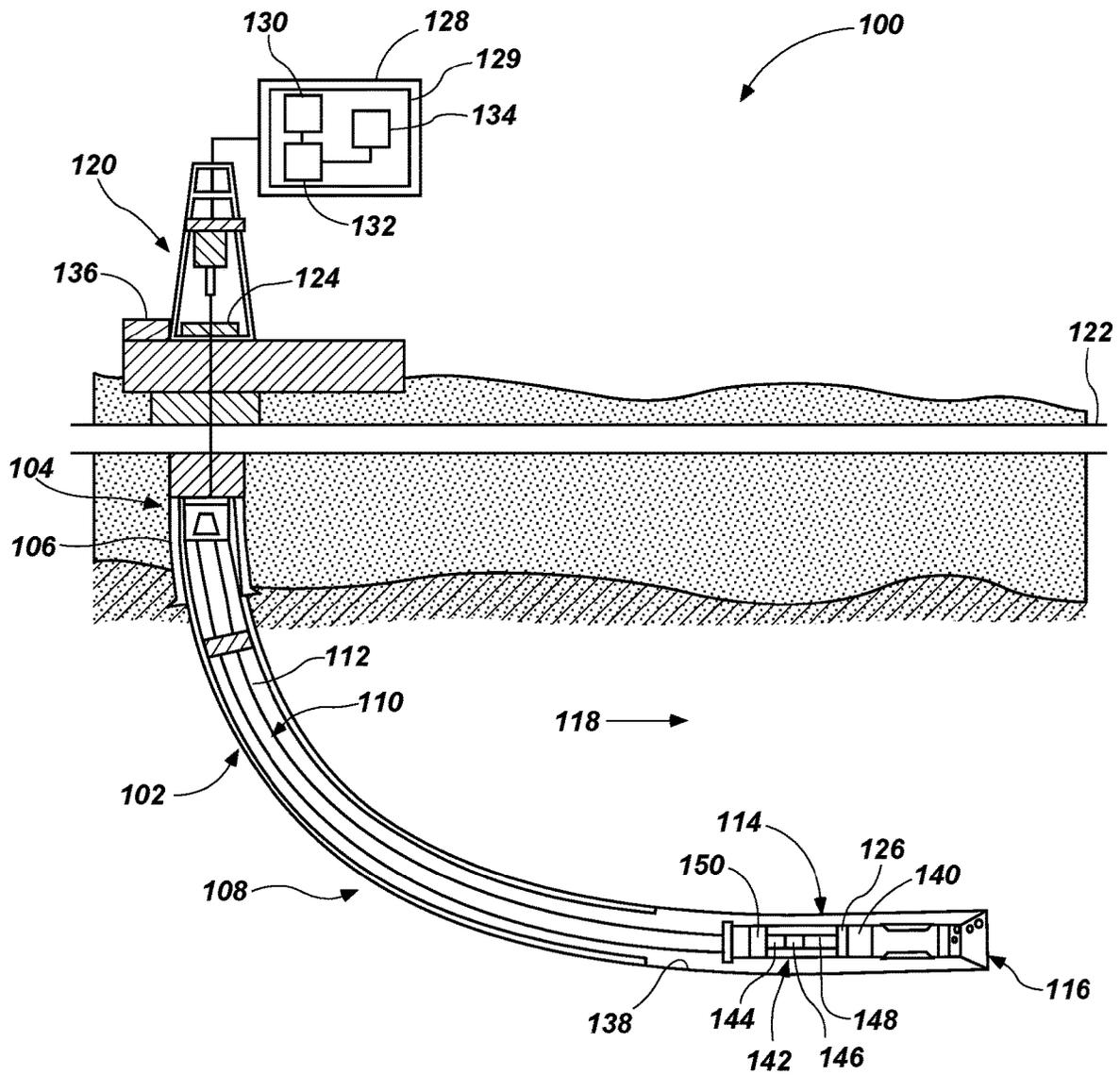


FIG. 1

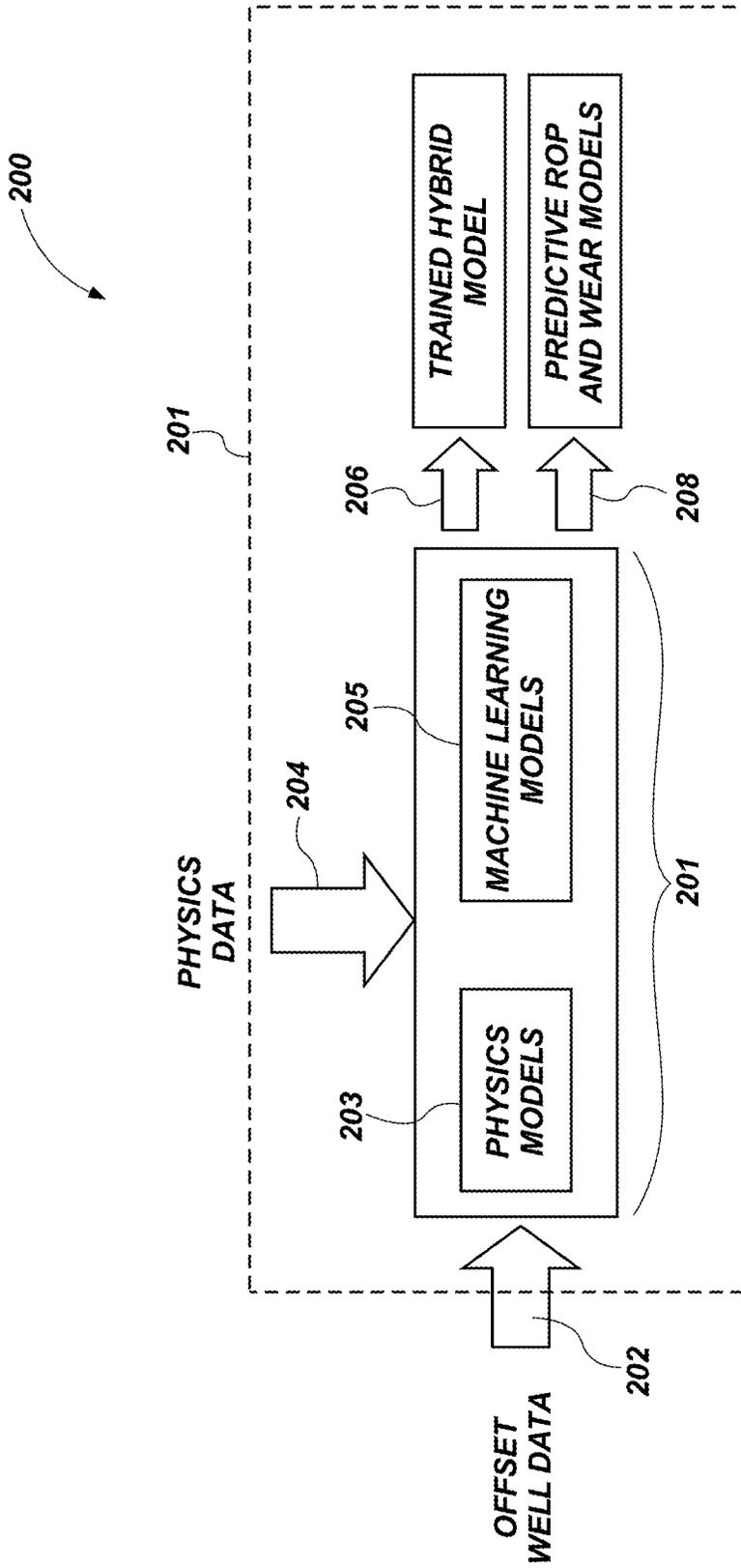


FIG. 2

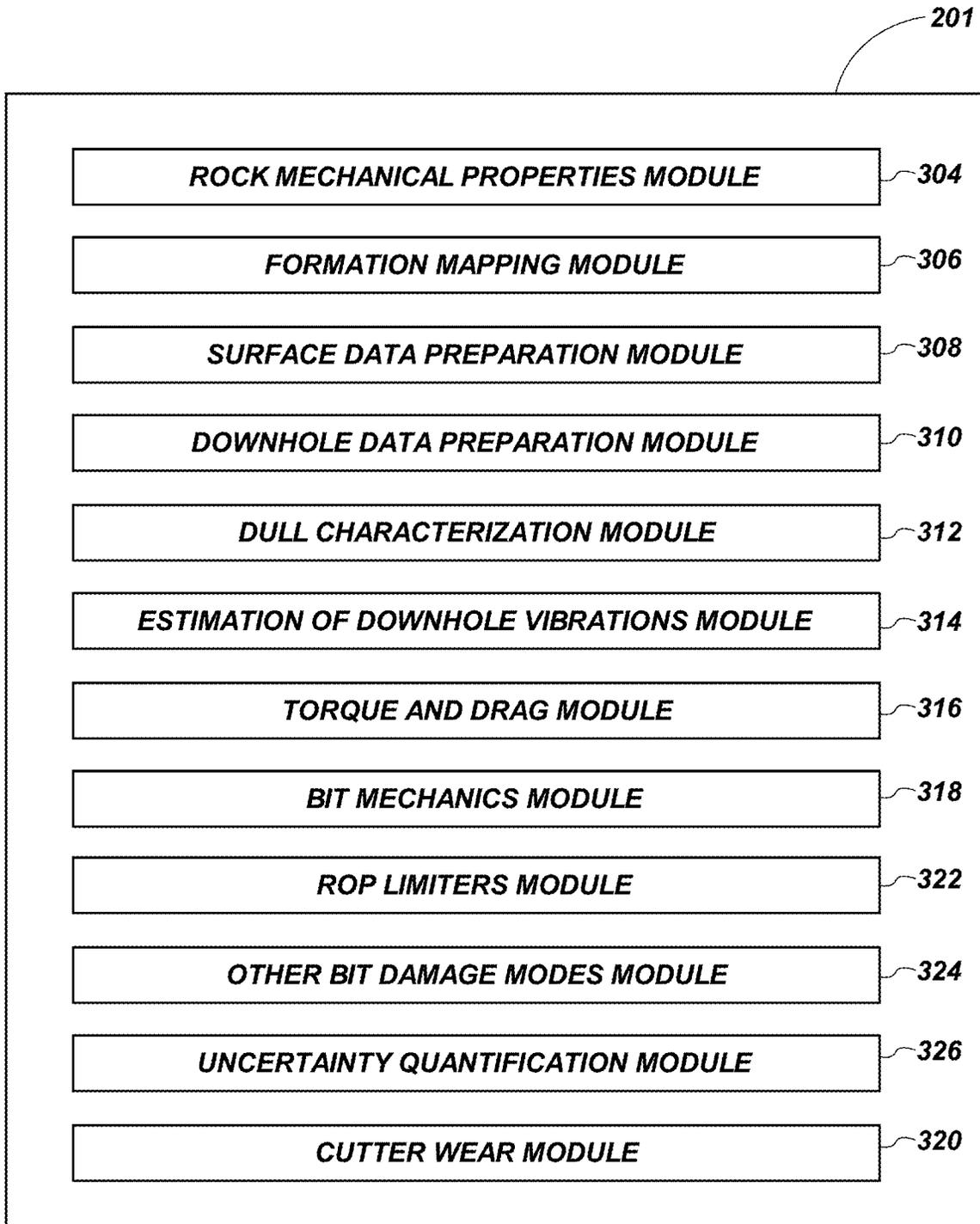


FIG. 3A

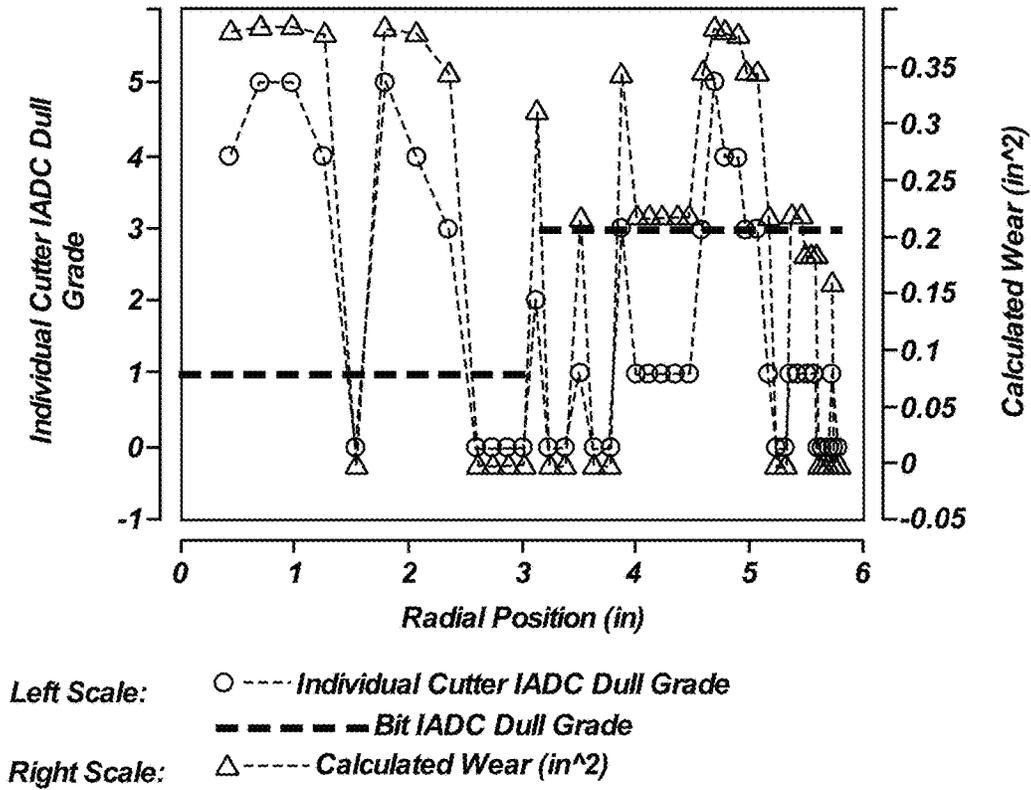


FIG. 3B

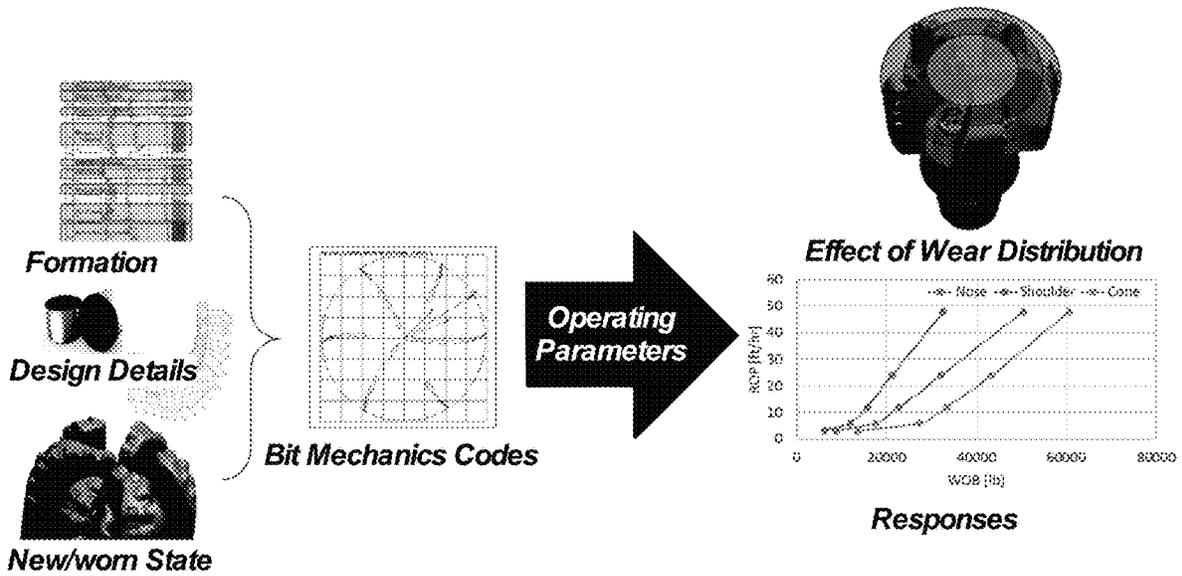


FIG. 3C

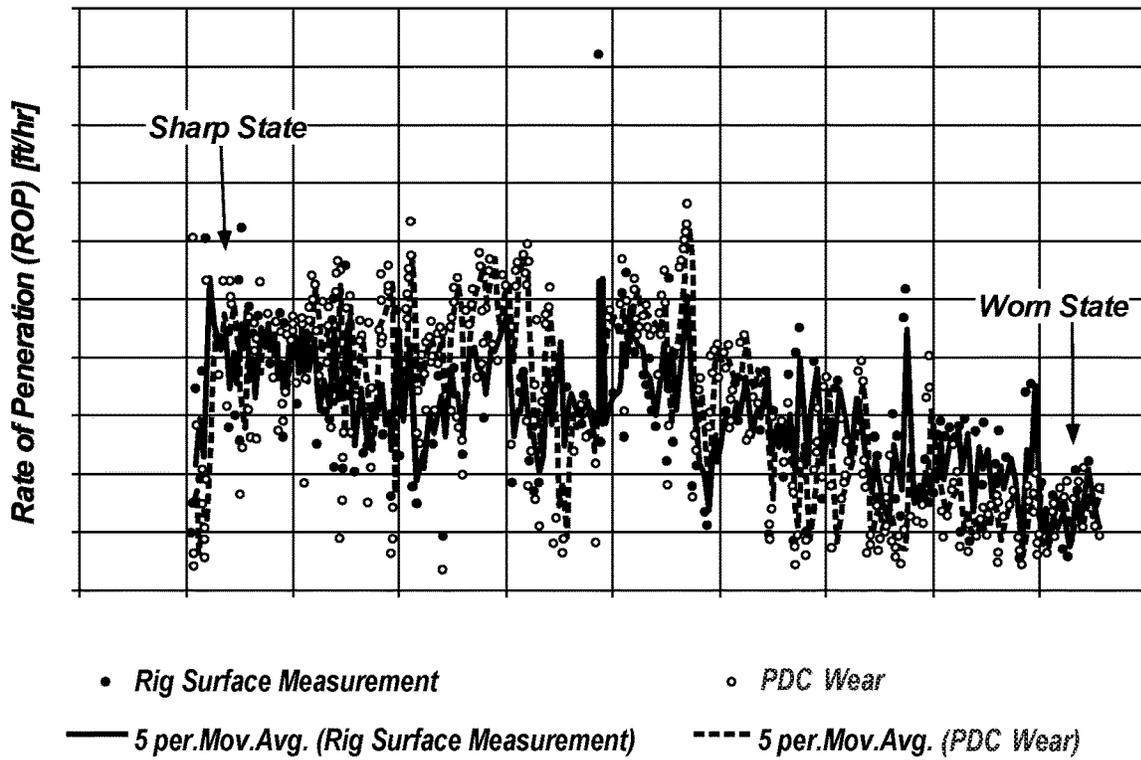


FIG. 3D

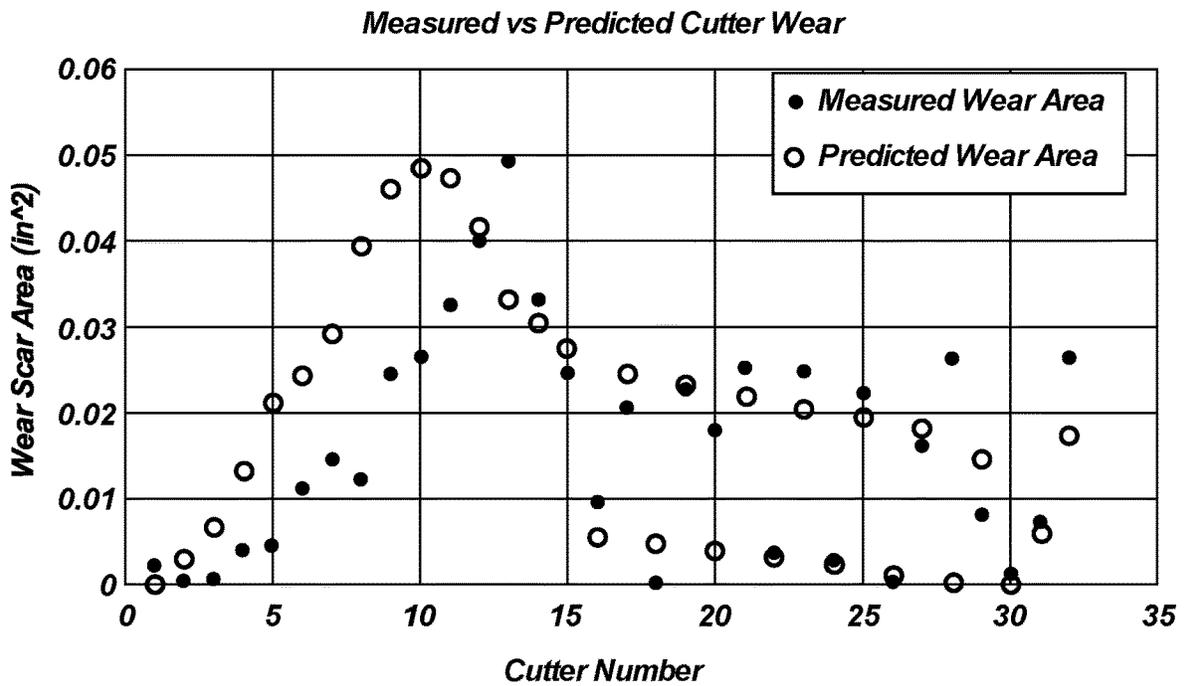


FIG. 3E

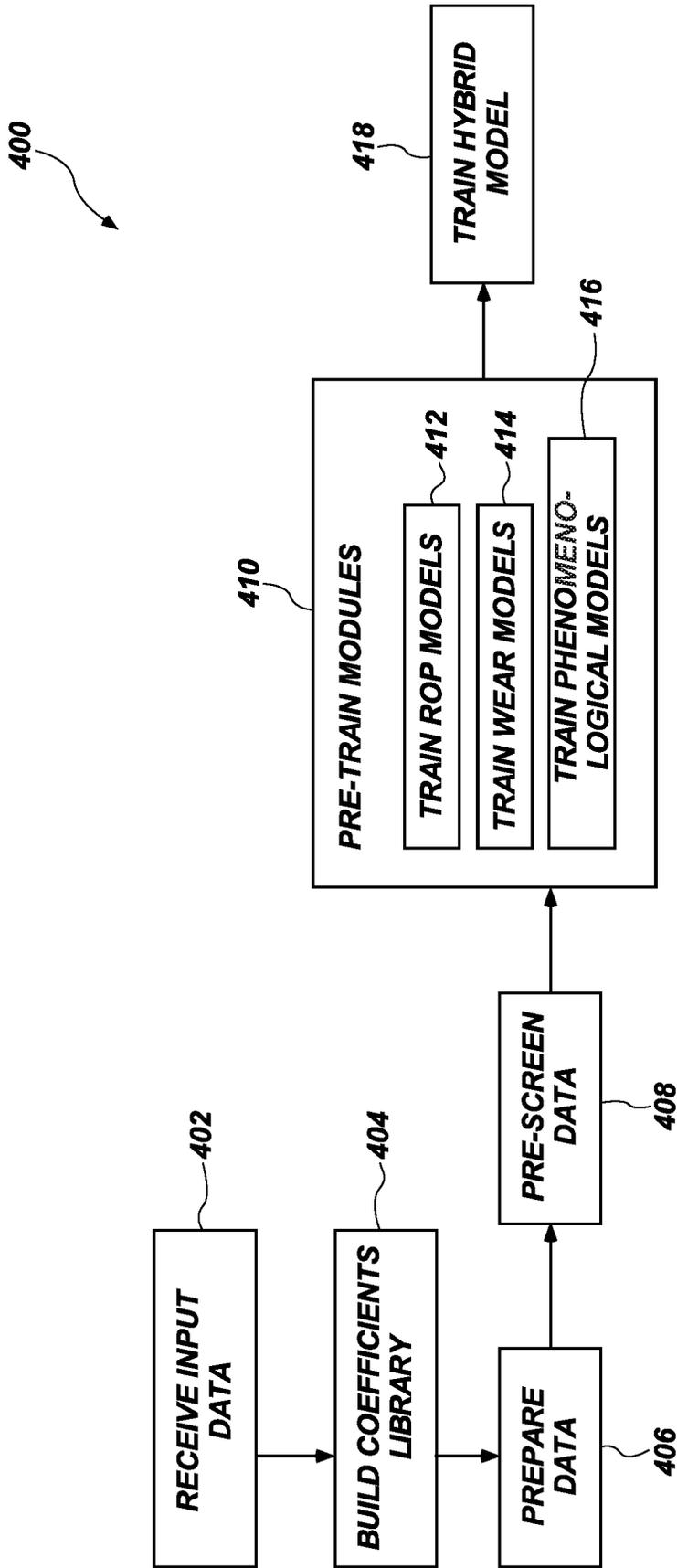


FIG. 4A

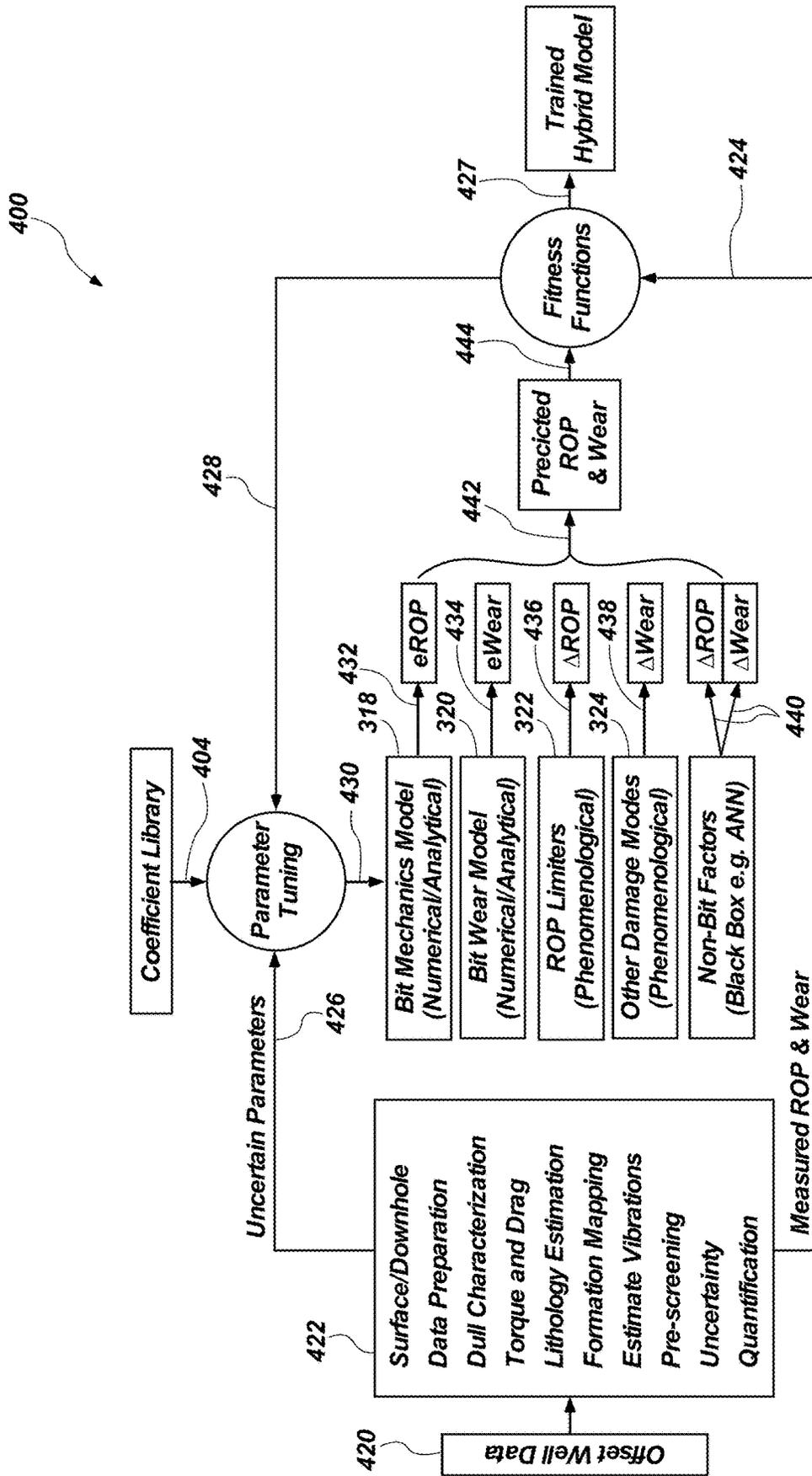


FIG. 4B

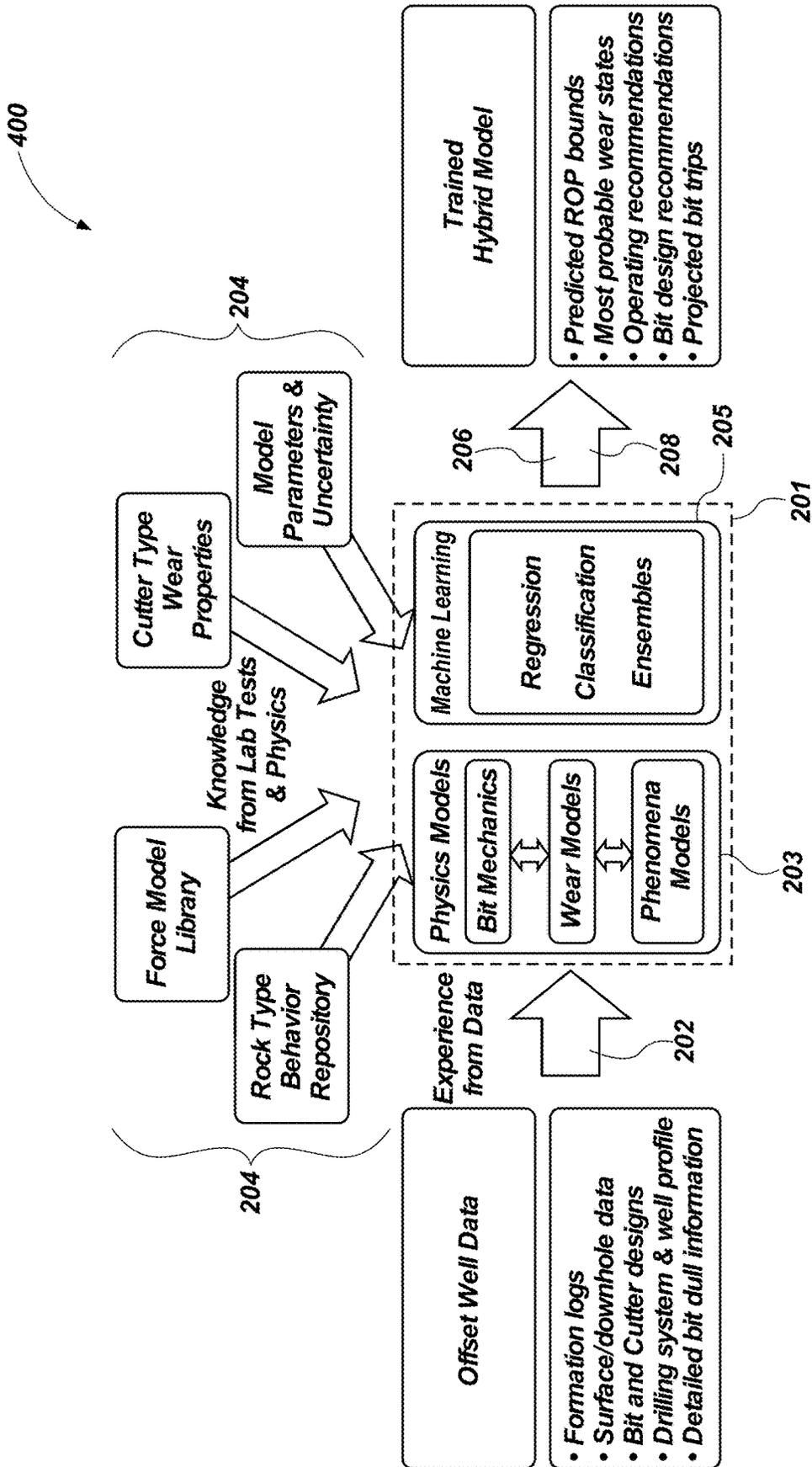


FIG. 4C

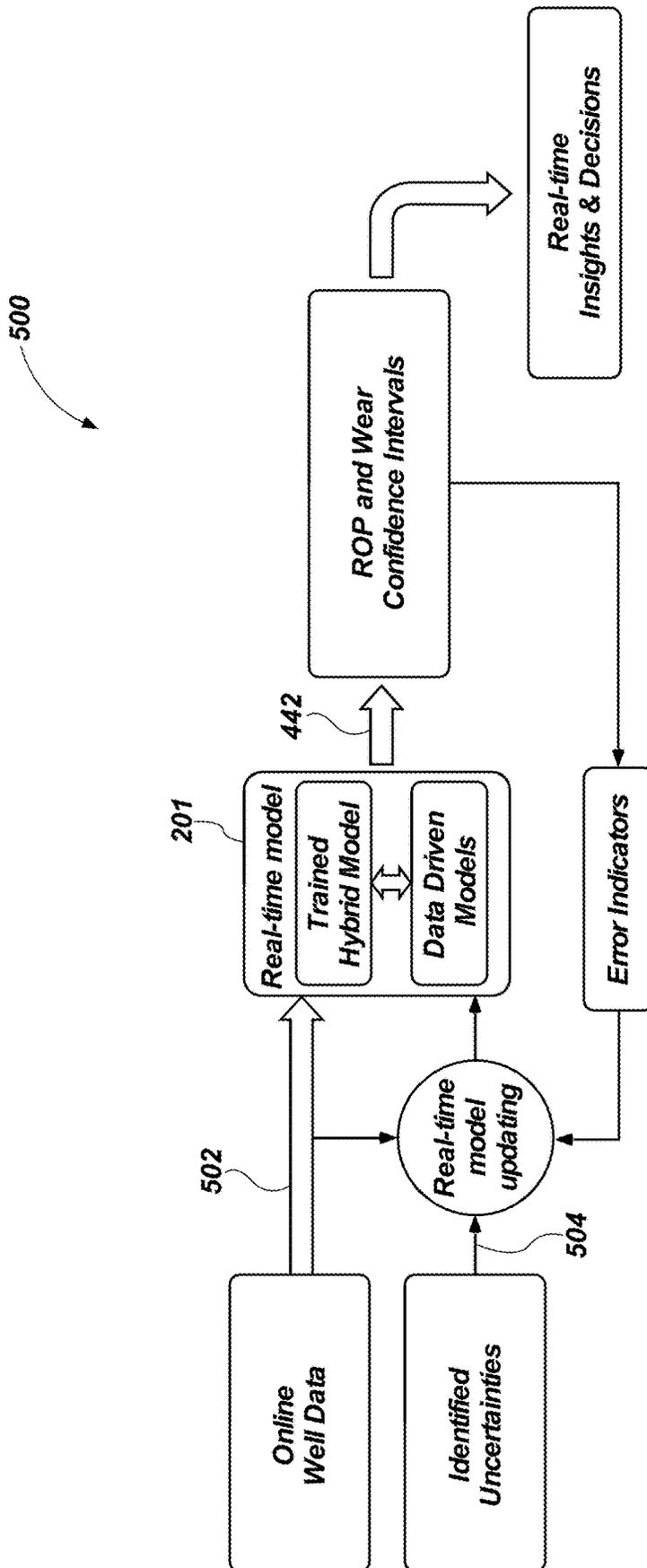


FIG. 5

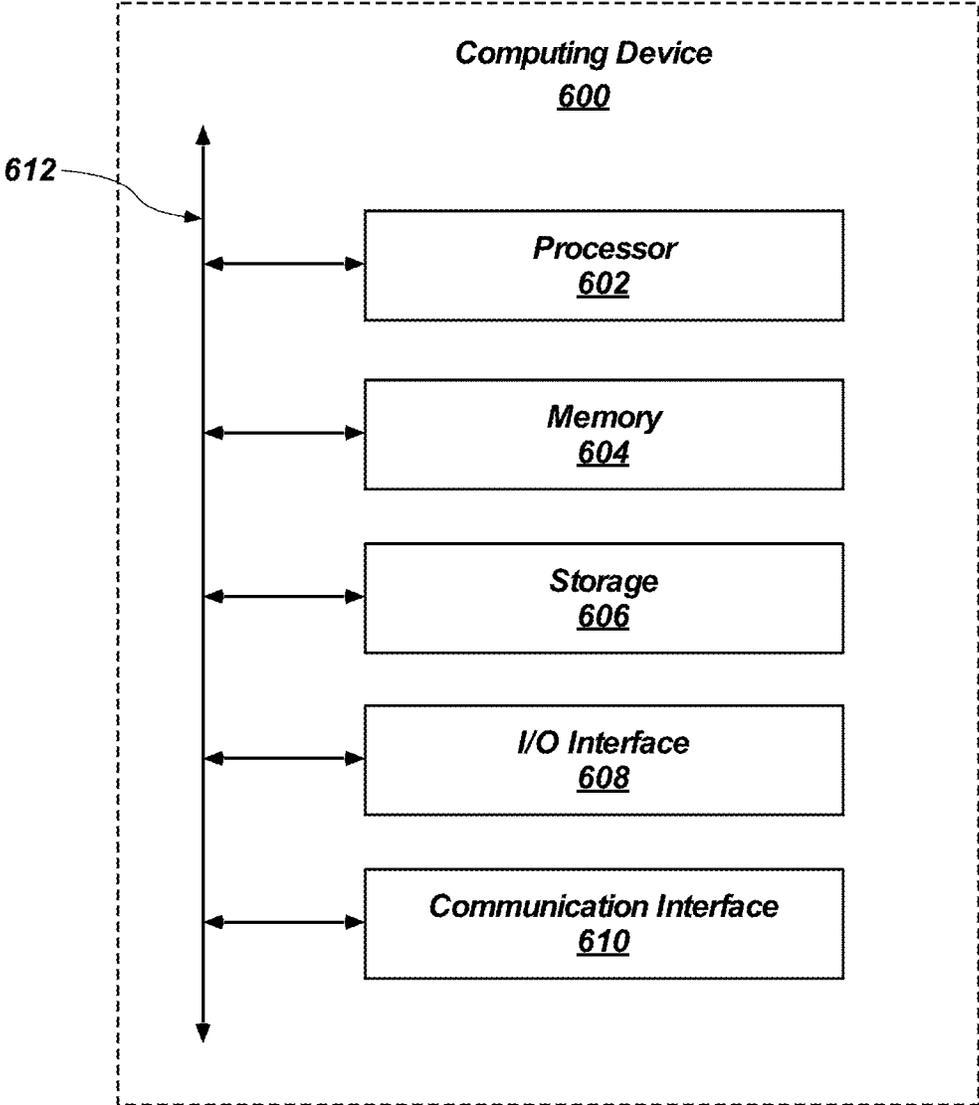


FIG. 6

# EARTH-BORING TOOL RATE OF PENETRATION AND WEAR PREDICTION SYSTEM AND RELATED METHODS

## TECHNICAL FIELD

This disclosure relates generally to earth-boring tool rate of penetration and wear prediction systems and methods of using such systems.

## BACKGROUND

Oil wells (wellbores) are usually drilled with a drill string. The drill string includes a tubular member having a drilling assembly that includes a single drill bit at its bottom end. The drilling assembly may also include devices and sensors that provide information pertaining to a variety of parameters relating to the drilling operations (“drilling parameters”), behavior of the drilling assembly (“drilling assembly parameters”) and parameters relating to the formations penetrated by the wellbore (“formation parameters”). A drill bit and/or reamer attached to the bottom end of the drilling assembly is rotated by rotating the drill string from the drilling rig and/or by a drilling motor (also referred to as a “mud motor”) in the bottom hole assembly (“BHA”) to remove formation material to drill the wellbore.

Conventional methods of predicting and optimizing bit performance utilize physics-based models during pre-well planning. While the physics models can describe the fundamental mechanics and can predict laboratory performance, the physics models lack sufficient calibration to predict field-specific behavior accurately. Moreover, unknown factors and uncertainties that are not conventionally included in the physics models introduce errors to any predictions. Moreover, the most comprehensive and accurate conventional physics models are too slow for real-time predictions.

Conventional data analytics and machine-learning models, on the other hand, have the ability to handle uncertainties and produce results fast enough for real-time predictions. However, training the machine-learning models requires a relatively large amount of data from offset wells. This results in any predictions being useful only in later wells. Moreover, introductions of new variables, new designs, new conditions, etc., that were previously unseen in the offset data, which is common in oilfield drilling, render predictions inaccurate.

## BRIEF SUMMARY

Some embodiments of the present disclosure include a method of providing predictive models of rates of penetration and wear of an earth-boring tool during a planned drilling operation. The method may include receiving input data and training a hybrid physics and machine-learning model with the input data by building a coefficient library of drilling parameters of a planned drilling operation. Building the coefficient library may include determining initial predictions of the drilling parameters of the planned drilling operation based on physics data within the input data and determining relative influences and rankings of the drilling parameters the planned drilling operation based on the physics data. The method may further include providing, via the hybrid physics and machine-learning model, a predictive model representing a rate of penetration of an earth-boring tool and wear of the earth-boring tool during the planned drilling operation.

In additional embodiments, the present disclosure includes an earth-boring tool system. The earth-boring tool system may include a drilling assembly for drilling a wellbore and a surface control unit operably coupled to the drilling assembly. The surface control unit may include a prediction system that includes at least one processor and at least one non-transitory computer-readable storage medium storing instructions thereon that, when executed by the at least one processor, cause the prediction system to: pre-train a plurality of modules individually within a hybrid physics and machine-learning model; train the plurality of modules together to develop the hybrid physics and machine-learning model based on input data; provide, via the hybrid physics and machine-learning model, a predictive model representing a rate of penetration of an earth-boring tool and wear of the earth-boring tool during a planned drilling operation, provide one or more recommendations of drilling parameters based on the predictive model, utilize the one or more recommendations in a drilling operation, receive real-time data from the drilling operation, retrain the hybrid physics and machine-learning model based on a combination of the input data and the real-time data; provide, via the retrained hybrid physics and machine-learning model, an updated predictive model of a rate of penetration of the earth-boring tool and wear of the earth-boring tool during a remainder of the planned drilling operation.

Some embodiments of the present disclosure include a method of providing predictive models of rates of penetration and wear of an earth-boring tool during a planned drilling operation. The method may include receiving real-time data from a drilling operation at a trained hybrid physics and machine-learning model, analyzing the real-time data via the hybrid physics and machine-learning model, providing, via the hybrid physics and machine-learning model and based at least partially on the analysis, a predictive model representing a rate of penetration of an earth-boring tool and wear of the earth-boring tool throughout at least part of a remainder of the drilling operation, providing one or more recommendations of drilling parameters based on the predictive model, and operating at least a portion of the drilling operation using the one or more recommendations of drilling parameters.

## BRIEF DESCRIPTION OF THE DRAWINGS

For a detailed understanding of the present disclosure, reference should be made to the following detailed description, taken in conjunction with the accompanying drawings, in which like elements have generally been designated with like numerals, and wherein:

FIG. 1 is a schematic diagram of a wellbore system comprising a drill string that includes an earth-boring tool according to one or more embodiments of the present disclosure;

FIG. 2 shows example processes of a prediction system via a schematic-flow diagram according to one or more embodiments of the present disclosure;

FIG. 3A is a schematic representation of various modules included within a hybrid physics and machine-learning model according to one or more embodiments of the present disclosure;

FIG. 3B shows a plot that demonstrates dull state characterization that may be obtained via one or more modules of the hybrid model according to one or more embodiments of the present disclosure;

FIG. 3C shows a schematic representation of a process by which a hybrid model may utilize a bit mechanics module to

determine and/or calculate in-situ rock strength, resulting cutting forces to be experienced on earth-boring tool, and ROP of the earth-boring tool in new and worn states;

FIGS. 3D and 3E show comparisons of measured and predicted values of ROP and wear according to one or more embodiments of the present disclosure;

FIG. 4A shows example processes of a prediction system utilized in pre-well planning via a schematic-flow diagram according to one or more embodiments of the present disclosure;

FIG. 4B shows an additional simplified sequence-flow that the prediction system utilizes to train the hybrid model, which is utilized in pre-well planning, according to one or more embodiments of the present disclosure;

FIG. 4C shows an additional representation of the sequence-flow of FIG. 4A that the prediction system utilizes to train the hybrid model and/or generate one or more rate of penetration and wear predictive models for given earth-boring tools and planned drilling operations during pre-well planning, according to one or more embodiments of the present disclosure;

FIG. 5 shows additional example processes of the prediction system including real-time re-training and usage of the hybrid model via a schematic-flow diagram; and

FIG. 6 is schematic diagram of a surface control unit of an embodiment of an earth-boring tool monitoring system of the present disclosure.

#### DETAILED DESCRIPTION

The illustrations presented herein are not actual views of any drilling system, earth-boring tool monitoring system, or any component thereof, but are merely idealized representations, which are employed to describe embodiments of the present invention.

As used herein, the terms “bit” and “earth-boring tool” each mean and include earth-boring tools for forming, enlarging, or forming and enlarging a borehole. Non-limiting examples of bits include fixed-cutter (drag) bits, fixed-cutter coring bits, fixed-cutter eccentric bits, fixed-cutter bi-center bits, fixed-cutter reamers, expandable reamers with blades bearing fixed cutters, and hybrid bits including both fixed cutters and rotatable cutting structures (roller cones).

As used herein, the singular forms following “a,” “an,” and “the” are intended to include the plural forms as well, unless the context clearly indicates otherwise.

As used herein, the term “may” with respect to a material, structure, feature, or method act indicates that such is contemplated for use in implementation of an embodiment of the disclosure, and such term is used in preference to the more restrictive term “is” so as to avoid any implication that other compatible materials, structures, features, and methods usable in combination therewith should or must be excluded.

As used herein, any relational term, such as “first,” “second,” etc., is used for clarity and convenience in understanding the disclosure and accompanying drawings, and does not connote or depend on any specific preference or order, except where the context clearly indicates otherwise. For example, these terms may refer to an orientation of elements of an earth-boring tool when disposed within a borehole in a conventional manner. Furthermore, these terms may refer to an orientation of elements of an earth-boring tool when disposed as illustrated in the drawings.

As used herein, the term “substantially” in reference to a given parameter, property, or condition means and includes to a degree that one skilled in the art would understand that the given parameter, property, or condition is met with a

small degree of variance, such as within acceptable manufacturing tolerances. By way of example, depending on the particular parameter, property, or condition that is substantially met, the parameter, property, or condition may be at least 90.0% met, at least 95.0% met, at least 99.0% met, or even at least 99.9% met.

As used herein, the term “about” used in reference to a given parameter is inclusive of the stated value and has the meaning dictated by the context (e.g., it includes the degree of error associated with measurement of the given parameter, as well as variations resulting from manufacturing tolerances, etc.).

Some embodiments of the present disclosure include a bit rate of penetration and wear prediction system (hereinafter “prediction system”) for drilling optimization during pre-well planning as well as real-time drilling. The prediction system combines strengths of physics-based models with strengths of machine-learning models to form a hybrid physics and machine-learning model, which provides predictive rates of penetration and wear models for earth-boring tools and planned drilling operations. In particular, the prediction system integrates data (e.g., knowledge and understanding) obtained from theory and laboratory testing from the physics-based models into a hybrid machine-learning framework that utilizes field experience captured using data analytics. As a result, the predictions system provides a fast and accurate hybrid model that requires relatively minimal offset data and which has the ability to account for introductions of new variables, conditions, and uncertainties.

In some embodiments, the hybrid model includes one or more physics models, which include drill bit mechanics simulation models (“mechanics models”). The mechanics models include detailed three-dimensional geometry descriptions, rock failure models, cutter wear progression models, cutter fracture criteria, and other phenomena that affect wear and rate of penetration of an earth-boring tool. As will be appreciated by one of ordinary skill in the art, the foregoing models may be developed over a relatively long period of time (e.g., several years) based on theory and laboratory experimentation. The prediction system may identify coefficients used in the foregoing models (i.e., the analytical and numerical models) that may not be precisely known for a given field application. Additionally, the prediction system may determine the dependence of these coefficients on cutter type, rock formation, and other environmental factors. Then, the prediction system may determine (e.g., establish) initial estimates, upper and lower bounds, and relative rankings of the coefficients in various scenarios. The prediction system feeds the foregoing information to the machine-learning models of the hybrid models that conduct model training based on input data from offset wells. The machine-learning models of the hybrid models also determine (e.g., capture) influence of unaccounted influencing factors in complementary black-box models. Such factors may include measured parameters such as bottom-hole-assemblies, wellbore profiles, vibrations, drilling crew, and rig, as well as unmeasured parameters such as wellbore quality.

Additionally, some embodiments of the present disclosure include a hybrid model that, in comparison to conventional prediction systems, provides more accurate predictions with effective treatment of uncertainties. Moreover, the hybrid system requires less offset well data to provide accurate predictive models and can account for new variables. The hybrid system provides predictive models fast enough to enable real-time decision during drilling operations. Like-

wise, the predictive models generated by the hybrid model follow fundamental drilling principles and laws of physics.

FIG. 1 is a schematic diagram of an example of a drilling system 100 that may utilize the apparatuses and methods disclosed herein for drilling boreholes. FIG. 1 shows a borehole 102 that includes an upper section 104 with a casing 106 installed therein and a lower section 108 that is being drilled with a drill string 110. The drill string 110 may include a tubular member 112 that carries a drilling assembly 114 at its bottom end. The tubular member 112 may be made up by joining drill pipe sections or it may be a string of coiled tubing. A drill bit 116 may be attached to the bottom end of the drilling assembly 114 for drilling the borehole 102 of a selected diameter in a formation 118.

The drill string 110 may extend to a rig 120 at the surface 122. The rig 120 shown is a land rig 120 for ease of explanation. However, the apparatuses and methods disclosed may also be used with an offshore rig 120 that is used for drilling boreholes under water. A rotary table 124 or a top drive may be coupled to the drill string 110 and may be utilized to rotate the drill string 110 and to rotate the drilling assembly 114, and thus the drill bit 116, to drill the borehole 102. A drilling motor 126 may be provided in the drilling assembly 114 to rotate the drill bit 116. The drilling motor 126 may be used alone to rotate the drill bit 116 or to superimpose the rotation of the drill bit 116 by the drill string 110. The rig 120 may also include conventional equipment, such as a mechanism to add additional sections to the tubular member 112 as the borehole 102 is drilled. A surface control unit 128, which may be a computer-based unit, may be placed at the surface 122 for receiving and processing downhole data transmitted by sensors 140 in the drill bit 116 and sensors 140 in the drilling assembly 114, and for controlling selected operations of the various devices and sensors 140 in the drilling assembly 114. The sensors 140 may include one or more of sensors 140 that determine acceleration, weight on bit, torque, pressure, cutting element positions, rate of penetration, inclination, azimuth, formation lithology, etc.

In some embodiments, the surface control unit 128 may include an earth-boring tool rate of penetration (“ROP”) and wear prediction system 129 (referred to hereinafter as “prediction system 129”). The prediction system 129 may include a processor 130 and a data storage device 132 (or a computer-readable medium) for storing data, algorithms, and computer programs 134. The data storage device 132 may be any suitable device, including, but not limited to, a read-only memory (ROM), a random-access memory (RAM), a flash memory, a magnetic tape, a hard disk, and an optical disc. Additionally, the surface control unit 128 may further include one or more devices for presenting output to an operator of the drilling assembly 114, including, but not limited to, a graphics engine, a display (e.g., a display screen), one or more output drivers (e.g., display drivers), one or more audio speakers, and one or more audio drivers. In certain embodiments, the surface control unit 128 is configured to provide graphical data to a display for presentation to an operator. The graphical data may be representative of one or more graphical user interfaces and/or any other graphical content as may serve a particular implementation. As is described in greater detail in regard to FIGS. 2-4C, the prediction system 129 may generate predictive ROP and wear models based on offset well data and physics data and utilizing physics model and machine-learning techniques. Furthermore, although the prediction system 129 is described herein as being part of the surface control unit 128, the disclosure is not so limited; rather, as will be

understood by one of ordinary skill in the art, the prediction system 129 may be discrete from the surface control unit 128 and may be disposed anywhere within the drilling assembly 114 or may be remote to the drilling assembly 114. The surface control unit 128 and the prediction system 129 are described in greater detail below with reference to FIG. 5.

During drilling, a drilling fluid from a source 136 thereof may be pumped under pressure through the tubular member 112, which discharges at the bottom of the drill bit 116 and returns to the surface 122 via an annular space (also referred as the “annulus”) between the drill string 110 and an inside sidewall 138 of the borehole 102.

The drilling assembly 114 may further include one or more downhole sensors 140 (collectively designated by numeral 140). The sensors 140 may include any number and type of sensors 140, including, but not limited to, sensors generally known as the measurement-while-drilling (MWD) sensors or the logging-while-drilling (LWD) sensors, and sensors 140 that provide information relating to the behavior of the drilling assembly 114, such as drill bit rotation (revolutions per minute or “RPM”), tool face, pressure, vibration, whirl, bending, and stick-slip. The drilling assembly 114 may further include a controller unit 142 that controls the operation of one or more devices and sensors 140 in the drilling assembly 114. For example, the controller unit 142 may be disposed within the drill bit 116 (e.g., within a shank and/or crown of a bit body of the drill bit 116). In some embodiments, the controller unit 142 may include, among other things, circuits to process the signals from sensor 140, a processor 144 (such as a microprocessor) to process the digitized signals, a data storage device 146 (such as a solid-state-memory), and a computer program 148. The processor 144 may process the digitized signals, and control downhole devices and sensors 140, and communicate data information with the surface control unit 128 and the earth-boring tool wear prediction system 129 via a two-way telemetry unit 150.

FIG. 2 shows example processes 200 of the prediction system 129 via a schematic-flow diagram. For instance, FIG. 2 shows one or more embodiments of a simplified sequence-flow that the prediction system 129 utilizes to train a hybrid model 201 and to provide a predictive ROP and wear model related to earth-boring tools and drilling operations. As used herein, the phrase a “ROP and wear model” may refer to predicted (e.g., estimated) values of rates of penetration and predicted wear states and amounts for a given earth-boring tool during at least a portion of a planned drilling operation or at any point within the planned drilling operation. As will be appreciated by one of ordinary skill in the art, the values indicated in the ROP and wear model may be determined within confidence intervals. Moreover, as described herein, any values determined and/or predicted by the prediction system 129 may be presented within confidence intervals.

In some embodiments, the prediction system 129 may include a hybrid physics and machine-learning model 201 (hereinafter “hybrid model 201”). For example, the hybrid model 201 may include one or more physics models 203 and one or more machine-learning models 205. Furthermore, as is described in greater detail below, the prediction system 129 utilizes the hybrid model 201 to generate one or more ROP and wear predictive models for given earth-boring tools and planned drilling operations.

In some embodiments, the process 200 of generating one or more ROP and wear predictive models for a given earth-boring tool and planned drilling operation may include the hybrid model 201 receiving input data, as shown in act 202 of FIG. 2. In one or more embodiments, the input data

may include historical offset well data. For example, the input data may include historical data including one or more of formation logs, well architecture and design data, surface and downhole data, bit and cutter design data, drilling system details data, and bit dull data.

Additionally, the hybrid model **201** receives physics data, as shown in act **204** of FIG. **2**. In some embodiments, the physics data may include, for example, one or more force model libraries, rock type behavior repositories, cutter type wear properties, and model parameters and uncertainties. Additionally, the physics data may include three-dimensional geometry descriptions, rock failure models, cutter wear progression models, cutter fracture criteria, and any other phenomena that affect wear and ROP of earth-boring tools. In one or more embodiments, the physics data may include pre-developed physics models that are based on historical data and/or theory and laboratory experimentation.

Upon receiving the offset well data and the physics data, the hybrid model **201** analyzes and processes the input data with the hybrid model **201** (i.e., the one or more physics models **203** and the one or more machine-learning models **205** (i.e., techniques)) to train the hybrid model **201**, as will be understood in the art, and to provide predictive ROP and wear models for given earth-boring tools and drilling operations, as shown in acts **206** and **208**, respectively. Additionally, via the analysis and the trained hybrid model **201**, the hybrid model **201** may provide predictions (e.g., simulations, models, values, etc.) related to drilling parameters such as, (e.g., drilling operations that involve) for example, build-up-rates, turn rates, lateral ROP, unconfined compressive strength, walk rate, dog leg severity, confined compressive strength, contact forces, rib forces, bending moments, WOB, pressures, inclinations, azimuth, borehole trajectories, hole qualities, drilling torque, drilling vibrations, cutter damage (e.g., breakage, chipping, cracking, spalling, etc.), bit trip, gage and bit body wear, etc. In further embodiments, the hybrid model **201** may provide predictions (e.g., simulations, models, values, etc.) related to lithology parameters such as, (e.g., drilling operations that involve) for example, rock types, rock strengths, grain/clast sizes, mineralogy, fabric, chemical properties, compositions, porosity, permeability, and/or texture of a subterranean formation to be drilled. As used herein, the term “drilling parameters” may refer to any of the drilling parameters and lithology parameters described herein. Furthermore, “drilling operations” may refer to any operations that involve (e.g., would be benefited by information related to) any of the above drilling parameter and/or lithology parameters. The training and operations of the hybrid model **201** are described in greater detail below in regard to FIGS. **3A-5**.

FIG. **3A** is a schematic representation of the hybrid model **201** according to one or more embodiments of the present disclosure. As shown, in some embodiments, the hybrid model **201** may, between the physics models **203** and the machine-learning models **205**, include a plurality of modules (e.g., sub-systems and/or models designed to perform particular analyses and operations for the hybrid model **201**). In some embodiments, the plurality of modules may form a part of one or more of the physics models **203** and the machine-learning models **205** of the hybrid model **201**. For example, a given module may be wholly part of (i.e., operated within) either the physics models **203** or the machine-learning models **205**, or the given module may operate within both the physics models **203** and the machine-learning models **205**. Additionally, in some embodiments, a given module may be operated within one of the physics models **203** and the machine-learning models

**205** but may be dependent on data determined by the other of the physics models **203** and the machine-learning models **205**. For example, the given modules may be informed (e.g., taught) by the other of the physics models **203** and the machine-learning models **205**, as will be understood in the art. In other embodiments, one or more of the plurality of modules may be separate and distinct from the physics models **203** and/or the machine-learning models **205** of the hybrid model **201**, and the physics models **203** and/or the machine-learning models **205** may operate in conjunction with the one or more of the plurality of modules to predict one or more drilling parameters of a drilling operation to assist in generating the predictive ROP and wear model for a given earth-boring tool and a planned drilling operation.

In one or more embodiments, the hybrid model **201** may include a rock mechanical properties module **304**, a formation-mapping module **306**, surface data preparation module **308**, a downhole data preparation module **310**, a dull characterization module **312**, an estimation of downhole vibrations module **314**, a torque and drag module **316**, a bit mechanics module **318**, a cutter wear module **320**, a ROP limiters module **322**, an other bit damage modes module **324**, and an uncertainty quantification module **326**. Each of the foregoing modules is described in greater detail below. Furthermore, as will be appreciated by one of ordinary skill in the art, the hybrid model **201** may include any number of additional modules related to analyzing and processing data for estimating drilling parameters, wear states, lithology parameters, and/or drilling behaviors.

With the rock mechanical properties module **304**, the hybrid model **201** may generate predictive models related to component lithology, unified lithology, and rock mechanical properties. For instance, the rock mechanical properties module **304** may utilize the physics models **203** and/or machine-learning models **205** of the hybrid model **201** to generate predictive models related to component lithology, unified lithology, and rock mechanical properties based on formation logs such as gamma ray data, acoustics data, density data, photoelectric absorption data, and neutron porosity data. In some embodiments, the predictive models generated by the rock mechanical properties module **304** provide prediction data related to lithology, properties such as UCS and friction angle, drillability analysis such as abrasivity, interfacial severity, and bit balling index.

Utilizing the formation-mapping module **306**, the hybrid model **201** may utilize the physics models **203** and/or machine-learning models **205** of the hybrid model **201** to generate predictive models related to formation properties for a planned well based on offset well formation logs. For instance, the hybrid model **201** may utilize the formation-mapping module **306** to generate predictive models related to formation properties in situations where formation logs are not available for a given formation of a planned drilling operation during model training (discussed below) or during pre-well planning predictions. Additionally, the hybrid model **201** may utilize the formation-mapping module **306** to use seismic measurement data to account for faults in earth formations. Moreover, the hybrid model **201** may utilize the formation-mapping module **306** in real-time (e.g., the real-time hybrid model discussed in greater detail in regard to FIG. **5**) to update and correct predicted formation logs based on real-time measured data such as, for example, formation logs or drilling responses.

Using the surface data preparation module **308**, the hybrid model **201** may clean surface data of the offset well data of the input data. For instance, the hybrid model **201** may detect and correct (or remove) corrupt or inaccurate records

from the surface data and may identify incomplete, incorrect, inaccurate, or irrelevant parts of the surface data and then replace, modify, or delete the coarse data (e.g., dirty data). In some embodiments, the hybrid model **201** may identify missing data or data that is not physically valid and may utilize known in-filling methods to complete missing data where necessary. For example, the hybrid model **201** may clean the surface data in any manner known in the art. Additionally, via the surface data preparation module **308**, the hybrid model **201** may prepare the surface data in a format for data analysis by the hybrid model **201**. For instance, the hybrid model **201** may prepare the surface data in a format such as, for example, comma separated values (CSV), text, XML, etc. For example, the hybrid model **201** may prepare the surface data in one or more formats that the hybrid model **201** can recognize and read. Moreover, via the surface data preparation module **308**, the hybrid model **201** may calculate variances and other statistics such as, for example, means, medians, modes, deviations, moving averages, etc., related to a quality of the surface data.

Via the downhole data preparation module **310**, the hybrid model **201** processes available downhole data from the offset well data of the input data and may link the downhole data to time (e.g., time during a drilling procedure represented in the offset well data) and depth references. Additionally, the hybrid model **201** may clean the downhole data. For instance, the hybrid model **201** may detect and correct (or remove) corrupt or inaccurate records from the downhole data and may identify incomplete, incorrect, inaccurate, or irrelevant parts of the downhole data and then may replace, modify, or delete the coarse data (e.g., dirty data). For example, the hybrid model **201** may clean the downhole data in any manner known in the art. Additionally, via the downhole data preparation module **310**, the hybrid model **201** may prepare the downhole data in a format for data analysis by the hybrid model **201**. Moreover, via the surface data preparation module **308**, the hybrid model **201** may calculate variances and other statistics related to a quality of the downhole data.

Utilizing the dull characterization module **312**, the hybrid model **201** may process (e.g., analyze) relatively high-resolution (e.g., micron resolutions) scans of bit dulls to characterize amounts of wear on individual cutters, blades, roller cones, or any other portions of an earth-boring tool or drilling assembly and wear scar geometry features for use within wear models. Additionally, via the dull characterization module **312**, the hybrid model **201** may process (e.g., analyze) images (e.g., photographs) and/or dull grades to estimate an amount of wear on individual cutters, blades, roller cones, or any other portions of an earth-boring tool or drilling assembly and wear scar geometry features.

With continued reference to the dull characterization module **312**, FIG. 3B shows a plot that demonstrates dull state characterization that may be determined by cutter level dull grading, laser scans, or high-resolution optical scans of an earth-boring tool (e.g., bit) utilizing the methods (e.g., the dull characterization module **312**) described herein. For instance, the plot provides details such as wear area, volume lost, etc., for each cutter of the earth-boring tool. Compared to the conventional bit level International Association of Drilling Contractors (IADC) dull grading, the cutter level dull grading achieved in the present disclosure is more accurate and more detailed. As is apparent from the example below, the bit dull grade for cutters in the inner part of the earth-boring tool determined via the conventional methods has significant error.

With the estimation of downhole vibrations module **314**, the hybrid model **201** may, in an absence of downhole measurements, estimate downhole parameters from surface measurements (e.g., surface data). For instance, via the estimation of downhole vibrations module **314**, the hybrid model **201** may estimate stick/slip, backward whirl, axial vibrations, etc.

The hybrid model **201** may utilize the torque and drag module **316** to predict (e.g., estimate) axial and torsional friction to be experienced by an earth-boring tool during a planned drill operation. Additionally, the hybrid model **201** may utilize the torque and drag module **316** to predict (e.g., estimate) downhole WOB (or torque) when surface WOB (or torque) measurement are available. For instance, the hybrid model **201** may utilize data, such as, surface data, data related to a well profile, a wellbore quality, adjustable kick off and stabilizers in the bottom-hole-assembly, mud type, flow rates of hydraulic fluids, string rotations per minutes, buckling, and/or vibrations to predict axial and torsional friction to be experienced by an earth-boring tool during a planned drill operation.

In some embodiments, the bit mechanics module **318** may include a numerical model (e.g., a bit mechanics model) that includes a three-dimensional bit design of a given earth-boring tool (e.g., an earth-boring tool to be used in a drilling operation and analyzed during pre-well planning), cutter geometries of the earth-boring tool, detailed dull state characterization, rock properties of a formation, and bottom hole geometry of a well bore. The hybrid model **201** may use the bit mechanics module **318** to determine and/or calculate in-situ rock strength, resulting cutting forces to be experienced on earth-boring tool, and ROP of the earth-boring tool in new and worn states.

With continued reference to the bit mechanics module **318**, FIG. 3C shows a schematic representation of a process by which hybrid model **201** may use the bit mechanics module **318** to determine and/or calculate in-situ rock strength, resulting cutting forces to be experienced on earth-boring tool, and ROP of the earth-boring tool in new and worn states. As shown in FIG. 3C, a same amount of total wear areas distributed on different regions of an earth-boring tool may contribute differently to ROP. For instance, in the example illustrated in FIG. 3C, a cone region of an earth-boring tool is shown to contribute most significantly to ROP, followed by a nose region of the earth-boring tool and the shoulder region of the earth-boring tool.

In one or more embodiments, the cutter wear module **320** may include a numerical model (e.g., a bit wear model) for non-linear wear progression on an earth-boring tool. The numerical model for non-linear wear progression of the cutter wear module **320** may be dependent on the determined cutting forces (e.g., force calculations) from the bit mechanics module **318**. Additionally, the cutter wear module **320** may utilize temperature information (e.g., temperature calculations) from a heat transfer model; and the numerical model for non-linear wear progression of the cutter wear module **320** may be dependent on the temperature calculations. The hybrid model **201** may use the cutter wear module **320** to determine and/or calculate non-linear wear on cutters, blades, roller cones, or any other portions of an earth-boring tool during a planned drilling operation.

With continued reference to the cutter wear module **320** and the bit mechanics module **318**, FIGS. 3D and 3E show comparisons of measured and predicted values of ROP and wear (e.g., earth-boring tool wear). The predicted values are determined with a sub-model of the hybrid model (e.g., the numerical models) in which the physics model of the hybrid

model **201** utilizes tuned coefficients (described below in regard to FIG. 4A). The example shown in FIGS. 3D and 3E is representative of a partially trained hybrid model during an iterative training process.

The hybrid model **201** may utilize the ROP limiters module **322** to determine effects of ROP limiters, which are not included in the bit mechanics module **318**, on ROP of an earth-boring tool within a formation during a planned drilling operation. For example, the hybrid model **201** may utilize the ROP limiters module **322** to determine effects of mud (e.g., oil-based mud, solids content of mud, mud weights, mud viscosity, etc.), vibrations, rate sensitivity in drilling, bit balling, etc., on ROP of an earth-boring tool during a planned drilling operation.

Using the other bit damage modes module **324**, the hybrid model **201** may predict (e.g., estimate) bit damage on an earth-boring tool from sources other than smooth wear. For example, using the other bit damage modes module **324**, the hybrid model **201** may predict gross cracking on the earth-boring tool due to overloads from impacts or formation transitions, damage accumulation due to repeated impacts and/or fretting, and fatigue damage due to fluctuating loads. Additionally, via the other bit damage modes module **324**, the hybrid model **201** may predict effects of earth-boring tool (e.g., bit) and/or cutter design features on damage to the earth-boring tool that are not accounted for with the bit mechanics module **318** and the cutter wear module **320**.

The hybrid model **201** may use the uncertainty quantification module **326** to identify amounts of uncertainty in the predictions and/or generated predictive models of the hybrid model **201**. For example, the hybrid model **201** may use the uncertainty quantification module **326** to determine variances of known parameters, error bounds for calculated parameters, and confidence intervals and/or probabilities for a predictions and/or predictive model. Additionally, the hybrid model **201** may use the uncertainty quantification module **326** to identify parameters that are not accounted for in any predictive models generated by the hybrid model **201** and to identify effects that are not accounted for and/or explained by any predictive models generated by the hybrid model **201**. Moreover, the hybrid model **201** may use the uncertainty quantification module **326** to perform performance quality checks on input and output data. Likewise, the hybrid model **201** may use the uncertainty quantification module **326** to identify parameters that need to be updated during a real-time application (e.g., updated with real-time data from a real-time drilling operation (discussed in greater detail in regard to FIG. 5)).

FIG. 4A shows example processes **400** of the prediction system **129** via a schematic-flow diagram. For instance, FIG. 4A shows one or more embodiments of a simplified sequence-flow that the prediction system **129** utilizes to train the hybrid model **201** and/or generate one or more ROP and wear predictive models for given earth-boring tools and planned drilling operations. FIG. 4B shows an additional simplified sequence-flow that the prediction system **129** utilizes to train the hybrid model **201**. FIG. 4C shows another representation of the sequence-flow that the prediction system **129** utilizes to train the hybrid model **201** and/or generate one or more ROP and wear predictive models for given earth-boring tools and planned drilling operations.

Referring to FIGS. 4A, 4B, and 4C together, as shown in act **402** of FIG. 4A, as discussed above, the hybrid model **201** receives input data, as shown in act **402** of FIG. 4A. In some embodiments, the input data may include offset well data and physics data (e.g., data from laboratory tests and physics models **203**). As mentioned above, the offset well data may include one or more of formation logs, well architecture and design, surface and downhole data, bit and cutter design information, drilling system details, and bit

dull information, while the physics data may include data from rock-type behavior repositories, from force model libraries, related to cutter type wear properties, and from model parameters and uncertainties.

Based on the input data, the hybrid model **201** builds a coefficients library utilized with the models to be predicted and/or generated by the hybrid model **201**, as shown in act **404** of FIG. 4A. In some embodiments, the hybrid model **201** builds the coefficients library based primarily on laboratory data and physics (e.g., the physics data). For example, the hybrid model **201** may build the coefficients library in order to account for known information (e.g., parameters determined and known by the physics models **203** and experimentation) within the hybrid model **201** (i.e., model) by constraining behavior of free parameters within the hybrid model **201**. In some embodiments, the known information may be acquired from historic laboratory tests, new laboratory tests, internal/external literature on wear tests, drilling tests, cutting tests, rock hardness tests, rock abrasivity tests, etc. Moreover, by and/or while building the coefficients library, the hybrid model **201** determines dependency of the coefficients on cutter types, cutter geometries, cutter materials, rock types, lithology parameters, environments, etc. Furthermore, by and/or while building the coefficients library, the hybrid model **201** determines relative rankings and influences of coefficients for different cutters, rocks, environments, etc., (e.g., drilling parameters) of a planned drilling operation. Likewise, by and/or while building the coefficients library, the hybrid model **201** determines initial predications (e.g., values) and upper and lower bounds for all the determined coefficients of the coefficients library. The hybrid model **201** may utilize any of the plurality of modules described in regard to FIGS. 3A-3E to build the coefficients library.

Below are some examples of determining coefficients of the coefficients library. As will be appreciated by one of ordinary skill in the art, measured responses in field data (e.g., input data) and the hybrid model **201** may be expressed as:

$$Y^F = Y^F(X^C); Y^M = Y^F(X^C, C)$$

where the field responses,  $Y^F$  (e.g., ROP, wear state) are dependent on controlled variables,  $X^C$  (WOB, RPM, etc.) and the behavior is governed by the field (i.e., natural science and/or physics). The model  $Y^M$  aims to capture the same behavior with physical and data influenced laws that contain modeling constants,  $C$  ( $C_0, C_1, m, A_1, A_2, \dots$ ). As will be appreciated by one of ordinary skill in the art, there can be errors involved in measurement and computation that are not accounted for here.

The foregoing algorithm involves decomposing the modeling constants  $C$  into rock, bit (e.g., cutting and/or rubbing elements), and environment dependent quantities from laboratory and physics data (e.g., knowledge). The method includes isolating the dependencies where possible but may include combining the dependencies in some situations. For example, some constants could be rock and environment dependent.

The following is a non-limiting example of a wear model: Wear of an elemental strip of height  $Z$  is given as:

$$DZ = F(T)ABRDL$$

$$F(T) = C_0 \text{EXP} \left[ \frac{C_1(T + 273)}{3273} \right]$$

where  $DZ$  is incremental wear,  $ABR$  is abrasivity of rock,  $DL$  is incremental distance slid, and  $F(T)$  is a temperature

dependent function of cutter hardness ( $C_o$  and  $C_1$  are coefficients). The temperature evolution is governed by:

$$\bar{T}_w - T_f = q_1 f = \frac{\alpha K_f F_n V}{A_w} f$$

$$f(WFA, h) = C_1 \times h^{C_2} \times WFA^{C_3} \dots + C_4 \text{EXP}(-h)$$

where  $T_w$  is wear flat temperature,  $T_f$  is fluid temperature,  $F_n$  is normal force on the wear flat,  $V$  is the cutting speed,  $A_w$  (or WFA) is an area of wear flat,  $h$  is convection heat transfer coefficient, and  $C_1$ - $C_4$  and  $\alpha$  are constants.

Likewise, as another non-limiting example, within a force model, the hybrid model **201** may determine dependencies of coefficients (e.g., worn state coefficients to predict wear flat pressure). For instance, influence of a dependency of a coefficient may be relatively quantified from laboratory tests and physics data (e.g., knowledge). Additionally, the relative influence of dependency may be determined under various conditions (e.g., rock type under various fluid conditions). Furthermore, initial estimates (e.g., guesses) may be provided to the hybrid model when determining the coefficients library. For instance, the hybrid model **201** may develop initial estimates, bounds, relative influence/ranking, dependencies, interactions, and other constraints on behavior of the coefficients (i.e., free parameters) based on laboratory tests, literature, and physics (i.e., physics data). As will be appreciated by one of ordinary skill in the art, developing the initial estimates, bounds, relative influence/ranking, dependencies, interactions, and other constraints on behavior of the coefficients (i.e., free parameters) based on physics data enhances prediction accuracy and reduces required amounts of offset well data for training the hybrid model **201**.

Upon determining and/or building the coefficients library, the hybrid model **201** prepares the input data for data analysis by the hybrid model **201**, as shown in act **406** of FIG. **4A**. For instance, the hybrid model **201** may clean all available surface data and downhole data from the offset well data of the input data. As a non-limiting example, the hybrid model **201** may detect and correct (or remove) corrupt or inaccurate records from the surface data and downhole data and may identify incomplete, incorrect, inaccurate, or irrelevant parts of the surface data and downhole data and then replace, modify, or delete the coarse data (e.g., dirty data). For example, the hybrid model **201** may clean the surface data and downhole data in any manner known in the art. Additionally, the hybrid model **201** may prepare the surface data and downhole data in a format for data analysis by the hybrid model **201**. Moreover, the hybrid model **201** may calculate variances and other statistics related to a quality of the surface data and downhole data. In some embodiments, the hybrid model **201** may use one or more of the surface data preparation module **308** and the downhole data preparation module to prepare the surface data and the downhole data.

Additionally, preparing the input data for data analysis by the hybrid model **201** may include characterizing dull states of an earth-boring tool and/or portions of an earth-boring tool. For example, the hybrid model **201** may process (e.g., analyze) relatively high-resolution scans of bit dulls to characterize amounts of wear on individual cutters, blades, roller cones, etc., and wear scar geometry features. Additionally, the hybrid model **201** may process (e.g., analyze) images (e.g., photographs) and/or dull grades to estimate an amount of wear on individual cutters, blades, roller cones, or any other portions of an earth-boring tool and wear scar

geometry features. For instance, the hybrid model **201** may use the dull characterization module **312** to characterize the dull states of an earth-boring tool and/or portions of an earth-boring tool.

Moreover, preparing the input data for data analysis by the hybrid model **201** may include predicting (e.g., estimating) rock mechanical properties. For example, the hybrid model **201** may generate predictive models related to component lithology, unified lithology, and rock mechanical properties. For instance, hybrid model **201** may generate predictive models related to component lithology, unified lithology, and rock mechanical properties based on formation logs such as gamma ray data, acoustics data, density data, photoelectric absorption data, and neutron porosity data. In some embodiments, the hybrid model **201** may use the rock mechanical properties module **304** to predict rock mechanical properties. Additionally, the hybrid model **201** may use the formation-mapping module **306** to map a current well and/or well plan. Moreover, the hybrid model **201** may use the estimation of downhole vibrations module **314** to estimate downhole vibrations. As will be understood in the art, all of or portions of the above-determine predicted values and predictive models may be added to the input data for further analysis by the hybrid model **201**.

After preparing the input data for data analysis, the hybrid model **201** pre-screens the prepared input data, as shown in act **408** of FIG. **4A**. In some embodiments, pre-screening the prepared input data may include performing high-level analytics to identify major effects and factors that affect ROP and damage/wear of earth-boring tools and/or drilling assemblies. In some embodiments, the high-level analytics may include high-level descriptive, predictive, diagnostic, and prescriptive analytics, which are known in the art. As a non-limiting example, pre-screening the prepared input data may include determining which non-earth-boring tool (e.g., non-bit) related factors are affecting ROP and damage/wear of earth-boring tools. For instance, pre-screening the prepared input data may relate to operating practices and may include determining how well recommended procedures are followed by an operator or an automatic drilling. Additionally, pre-screening the prepared input data may include determining a quality of making drill pipe connections (e.g., duration, damage to threads), a quality of restarting drilling operations after a connection, etc. As another non-limiting example, pre-screening the prepared input data may include determining whether earth-boring tool effects (e.g., bit effects) are affecting ROP and damage/wear of the earth-boring tool. As yet another non-limiting example, pre-screening the prepared input data may include determining whether wear is a dominant damage mode.

Upon pre-screening the prepared input data, the hybrid model **201** pre-trains the individual modules of the hybrid model **201**, as shown in act **410** of FIG. **4A**. In some embodiments, pre-training the individual modules may include training a hybrid bit mechanics module **318** (e.g., ROP model), as shown in act **412** of FIG. **4A**. In one or more embodiments, the hybrid model **201** trains the hybrid bit mechanics module **318** with the offset field data. Additionally, the hybrid model **201** trains the bit mechanics module **318** by predicting the ROP of a given earth-boring tool within a planned drilling operation at the beginning of the drilling operation (e.g., run) in a sharp state using a design and/or bit metrology pre-drilling operation (e.g., pre-run), and the hybrid model **201** trains the hybrid bit mechanics module **318** by predicting the ROP at an end of the drilling operation in a worn state using metrology of a dull bit (e.g., earth-boring tool). By predicting the ROP at the beginning

of a drilling operation and at the end of the drilling operation, the hybrid model **201** predicts sharp state force model coefficients and at least some worn state force model coefficients. As will be understood by one of ordinary skill in the art, multiple solutions may be possible.

In one or more embodiments, pre-training the individual modules may include training the hybrid bit mechanics module **318** and the cutter wear module **320** (e.g., wear models) of the physics models **203** of the hybrid model **201**, as shown in act **414** of FIG. **4A**. In some embodiments, the hybrid model **201** trains the bit mechanics module **318** and cutter wear module **320** by predicting wear states of an earth-boring tool and the ROP of the earth-boring tool during an end of a drilling operation (e.g., run). The hybrid model **201** may compare a predicted dull to final field (e.g., real) dull metrology data. The foregoing may demonstrate the effects of formation abrasiveness, cutter wear resistance, and bit design/cutter redundancy. Additionally, based on the foregoing, the hybrid model **201** may predict coefficients for a worn state force model and a wear progression model. As will be understood by one of ordinary skill in the art, multiple solutions may be possible.

In some embodiments, pre-training the individual modules may include optionally training phenomenological models for ROP and wear of the physics models **203**, as shown in act **416**. The phenomenological models may include measured responses (e.g., mechanical specific energy and/or ROP) and wear progression (e.g., Archard's Model). Additionally, the phenomenological models may be earth-boring tool company diagnostic and may be utilized in an ensemble (e.g., combination of machine-learning models **205** (i.e., techniques)). Beyond what is described herein, any of the modules and/or models described herein may be trained via any of the methods described in U.S. Pat. No. 8,417,495 to Dashevskiy, the disclosure of which is incorporated in its entirety by reference herein.

In some embodiments, pre-training the individual modules may include predicting (e.g., estimating) the contributions of effects that not included in the bit mechanics and wear models (e.g., bit mechanics module **318**, cutter wear module **320**, etc.). For instance, pre-training the individual modules may include predicting the contributions of the ROP limiters module **322**, other bit damage modes module **324**, and other factors, such as, for example, rig parameters (e.g., type, drilling parameters, and bottom-hole-assembly parameters). The foregoing modules may account for incremental effects in ROP and wear/damage on the earth-boring tool.

Upon training the individual modules, the hybrid model **201** may train the hybrid model **201**, as shown in act **418** of FIG. **4A**. FIG. **4B** shows a schematic diagram representing an example of how the hybrid model **201** is trained and how the physics models **203** and the machine-learning models **205** within the hybrid model **201** interact. For example, as show in FIG. **4B**, and as discussed above, the hybrid model **201** may receive input data, as show in act **420** of FIG. **4B**. Additionally, the input data may include any of the input data described above in regard to FIGS. **2-4A**. Furthermore, as shown in act **422**, the hybrid model **201** may analyze the input data with the machine-learning models **205** of the hybrid model **201** and within a plurality of the modules described above in regard to FIGS. **3A-3E**. For example, the hybrid model **201** may analyze the input data via one or more of the surface data preparation module **308**, the downhole data preparation module **310**, the dull characterization module **312**, the estimation of downhole vibrations module **314**, the torque and drag module **316**, the rock mechanical

properties (i.e., lithology estimation) module **304**, the formation-mapping module **306**, and the uncertainty quantification module **326**. Additionally, the hybrid model **201** may analyze the input via any of the methods described above in regard to FIG. **2** and in regard to the above-listed modules.

As noted above, the hybrid model **201** may analyze the input data utilizing the machine-learning models **205** of the hybrid model **201**. For instance, the hybrid model **201** may analyze the input data utilizing one or more of regression models (e.g., a set of statistical processes for estimating the relationships among variables), classification models, and/or phenomena models. Additionally, the machine-learning models **205** may include a quadratic regression analysis, a logistic regression analysis, a support vector machine, a Gaussian process regression, ensemble models, or any other regression analysis. Furthermore, in yet further embodiments, the machine-learning models **205** may include decision tree learning, regression trees, boosted trees, gradient boosted tree, multilayer perceptron, one-vs-rest, Naïve Bayes, k-nearest neighbor, association rule learning, a neural network, deep learning, pattern recognition, or any other type of machine-learning. In yet further embodiments, the analysis may include a multivariate interpolation analysis.

In some embodiments, the hybrid model **201** may also perform the pre-screening analysis described above in regard to act **408** of FIG. **4A** on the input data.

Upon analyzing the input data via the above-described modules and machine-learning models **205**, the hybrid model **201** processes any data related to measured and/or determined drilling parameters (e.g., ROP and wear parameters) with fitness functions, as shown in act **424** of FIG. **4B** and processes uncertain parameters, described above in regard to uncertainty quantification module **326** and FIG. **3A**, via a parameter tuning process, as shown in act **426** of FIG. **4B**.

Processing the data related to measured and/or determined drilling parameters (e.g., ROP and wear parameters) with fitness functions (e.g., error or objective functions) may include applying one or more fitness functions to the data to prediction errors in (i.e., differences between) reference solutions (e.g., measured values of parameters being predicted) and model predicted values. For example, applying one or more fitness functions to the data quantifies how well the hybrid model **201** is able to predict reality. In other words, the fitness functions determine prediction error (i.e., the difference between measured values and model predicted values). In some embodiments, the fitness functions may compare error at each depth or time increment (pointwise) of a drilling operation, compare smoothed (e.g., moving average filter) values, compare shapes of the measured and predicted curves (e.g., correlation functions), and/or use statistical measures such as k-test to determine error. Error may be calculated as an average, a mean square error, an average correlation coefficient, a performance index, a least squared error, etc.

The data related to measured and/or determined drilling parameters (referred to herein as "measured data") may also be utilized to at least partially train the hybrid model **201**, as shown in act **427** of FIG. **4B**. In other words, for a given set of input values (e.g., parameters), the hybrid model **201** is expected (e.g., trained) to produce the same output values (e.g., measured and/or determined drilling parameters). For example, the hybrid model **201** may be trained via any of the methods described in U.S. Pat. No. 8,417,495 to Dashevskiy, the disclosure of which is incorporated in its entirety by reference herein.

In some embodiments, in addition to training the hybrid model **201** at least partially with the measured data, as noted above, the hybrid model **201** may identify parameters in the measured data (e.g., offset well data, etc.), which are not known with enough certainty and subjects the identified parameters to a parameter tuning process, as shown in act **428** of FIG. **4B** and as mentioned above in regard to act **426** of FIG. **4B**. For example, if the error determined via the fitness functions is greater than a tolerance (or improvement in the error in successive iterations is greater than a tolerance), the hybrid model **201** utilizes an algorithm to adjust (e.g., tune) the coefficients in the hybrid model **201** within the constraints identified by the coefficient library and modules described above. For example, for parameters within the data for which values are not known with relatively high level of certainty (i.e., for parameters with errors greater than a given tolerance), the hybrid model **201** may subject the data to parameter tuning process. In other words, the hybrid model **201** may identify parameters having the greatest uncertainty and may subject only those identified parameters to the parameter tuning process. Having a smaller number of free parameters alleviates problems with overfitting and improves accuracy. Acts **424**, **426**, and **428** of FIG. **4B** result in one or more sets of tuned coefficient values for the coefficients library of the trained hybrid model **201**.

Upon tuning the coefficient library, the uncertain parameters, and the measured data via the parameter tuning process, the hybrid model **201** provides the tuned data (e.g., tuned coefficient values) to one or more of the modules within the physics models **203** and the machine-learning models **205** of the hybrid model **201**, as shown in act **430** of FIG. **4B**. In particular, the hybrid model **201** provides the tuned data (e.g., tuned coefficient values) to the bit mechanics module **318**, the cutter wear module **320**, the ROP limiters module **322**, of the other bit damage modes module **324** of the physics models **203**. Additionally, the hybrid model **201** provides the tuned data (e.g., tuned coefficient values) to one or more black-box machine-learning models and/or neural networks for an analysis of non-earth-boring tool factors (i.e., non-bit factors).

The bit mechanics module **318** may utilize the tuned data (e.g., tuned coefficient values) via any of the manners described above in regard to FIGS. **3A-3E** to make predictions. For instance, the hybrid model **201** may use the bit mechanics module **318** and the tuned data to determine and/or calculate in-situ rock strength, resulting cutting forces on earth-boring tool, and ROP in new and worn states of the earth-boring tool. As a non-limiting example, the hybrid model **201** may use the bit mechanics module **318** to predict (e.g., estimate) an ROP in new and worn states of the earth-boring tool, as shown in act **432** of FIG. **4B**.

The cutter wear module **320** (referred to as “bit wear model”) may utilize the tuned data (e.g., tuned coefficient values) via any of the manners described above in regard to FIGS. **3A-3E** to make predictions. For example, the hybrid model **201** may use the cutter wear module **320** and the tuned data to predict (e.g., estimate) non-linear wear on cutters, blades, roller cones, or any other portion of an earth-boring tool during a planned drilling operation, as shown in act **434** of FIG. **4B**.

The ROP limiters module **322** may analyze utilize the tuned data (e.g., tuned coefficient values) via any of the manners described above in regard to FIGS. **3A-3E** to make predictions. For instance, the hybrid model **201** may use the ROP limiters module **322** and the tuned data to predict (e.g., estimate) the effects of ROP limiters on the ROP of an earth-boring tool during a planned drilling operation. As a

non-limiting example, the hybrid model **201** may use the ROP limiters module **322** to predict a change in ROP of the earth-boring tool due to the ROP limiters during a planned drilling operation, as shown in act **436** of FIG. **4B**.

The other bit damage modes module **324** may utilize the tuned data (e.g., tuned coefficient values) via any of the manners described above in regard to FIGS. **3A-3E** to make predictions. For example, the hybrid model **201** may use the other bit damage modes module **324** and the tuned data to predict (e.g., estimate) earth-boring tool (e.g., bit) damage from sources other than smooth wear. As a non-limiting example, the hybrid model **201** may use the other bit damage modes module **324** to predict a change in wear (e.g., a change in wear states) of an earth-boring tool during a planned drilling operation or during portions of a planned drilling operation, as shown in act **438** of FIG. **4B**.

Additionally, the hybrid model **201** may analyze and/or utilize the tuned data with one or more black-box machine-learning models and/or neural networks to predict changes in ROP and changes in wear due to the influence of unaccounted factors, as shown in act **440** of FIG. **4B**. For example, the hybrid model **201** may analyze the tuned data with one or more black-box machine-learning models and/or neural networks to predict changes in ROP and changes in wear due to measured parameters such as bottom-hole assemblies, wellbore profile, vibrations, drilling crew, and rig, as well as unmeasured parameters such as wellbore quality. In view of the foregoing, because portions of the tuned data may have been analyzed via one or more machine-learning techniques as described above in regard to act **422** prior to being analyzed by the physics model **203**, the machine-learning models **205** of the hybrid model **201** may inform (e.g., teach) the physics models **203** of hybrid model **201** about reality (i.e., based on real measured input data). Likewise, because portions of the input data originate from physics models, the physics models **203** of the hybrid model **201** inform (e.g., teach) the machine-learning models **205** about physics.

Based on the predicted values of ROP and wear of an earth-boring tool determined in acts **432-440**, the hybrid model **201** may predict and generate overall ROP and wear models (the predictive ROP and wear models) for an earth-boring tool during a drilling operation, as shown in act **442** of FIG. **4B**. Additionally, in some embodiments, the hybrid model **201** may process the predictive ROP and wear models via one or more fitness functions, as shown in act **444** of FIG. **4B**. For instance, the hybrid model **201** may process the predictive ROP and wear models via any of the fitness functions described above and via any of the manners described above in regard to act **424** of FIG. **4B**.

Furthermore, the output values of the predictive ROP and wear models (e.g., the values output after applying the fitness functions) may be utilized to train the hybrid model **201** (i.e., hybrid model **201**) for a given earth-boring tool and/or planned drilling operation (e.g., planned well). For example, as will be understood in the art, for a given set of input values (e.g., parameters) of an earth-boring tool and/or planned drilling operation, the hybrid model **201** (i.e., hybrid model **201**) is expected to produce the same output values (i.e., predictive ROP and wear models) as is produced via the machine-learning models **205** and physics models **203** described in acts **422-444** of FIG. **4B**. In particular, the hybrid model **201** is trained to produce the values for a given set of input values (e.g., parameters) of an earth-boring tool and/or planned drilling operation that correspond to the values provided by the machine-learning models **205** and physics models **203** described in acts **422-444** of FIG. **4B** by

iterating the training process for a large number of input value sets. After a sufficient number of iterations, the hybrid model **201** becomes a trained hybrid model **201**. The trained hybrid model **201** may then be utilized to simulate or predict (e.g., estimate) ROP and wear models for a given set of input values (e.g., parameters) of an earth-boring tool and/or planned drilling operation. Furthermore, the hybrid model **201** may then be utilized to determine variance between the ROP and wear models generated by the machine-learning models **205** and physics models **203** described in acts **422-444** of FIG. **4B** and the ROP and wear models generated by trained hybrid model **201**. As will be understood in the art, the trained hybrid model **201** may include a “pre-well” trained hybrid model **201** at this point, because the trained hybrid model **201** has not been trained on real-time data.

FIG. **5** shows additional example processes **500** of the prediction system **129** via a schematic-flow diagram. For instance, FIG. **5** shows one or more embodiments of a simplified sequence-flow that the prediction system **129** utilizes to validate and retrain the hybrid model **201** based on real-time data and provide real-time predictive ROP and wear models. As shown in act **502** of FIG. **5**, the hybrid model **201** may receive online well data (i.e., real-time well data) related to a current wellbore operation (e.g., drilling operation). As used herein, the term “real-time” when used in reference to data and/or predictive models may refer data and/or predictive models that are available and/or generated within seconds, minutes, or hours of the events indicated in the real-time data occurring. In one or more embodiments, the real-time well data may be obtained via one or more sensors (e.g., sensors **140** (FIG. **1**)) throughout the drilling assembly **114** (FIG. **1**). For example, in some embodiments, the real-time data may be obtained via any of the sensors and/or manners described in U.S. Pat. No. 8,100,196, to Pastusek et al., filed Feb. 6, 2009, U.S. Pat. No. 7,849,934, to Pastusek et al., filed Feb. 16, 2007, and U.S. Pat. No. 7,604,072, to Pastusek et al., filed Jun. 7, 2005, the disclosures of which are incorporated in their entireties by this reference herein.

Additionally, the hybrid model **201** may receive uncertain parameters and identify new uncertain parameters based on what real-time (e.g., online) well data is available and the well data’s quality, as shown in act **504**. For example, the hybrid model **201** may receive any of the uncertain parameters described above in regard to act **426** of FIG. **4B**. Moreover, the hybrid model **201** may analyze the online well data and the uncertain parameters via any of the manners described above in regard to FIG. **4B**. Furthermore, the hybrid model **201** may retrain (e.g., validate) the hybrid model **201** via any of the training methods described above in regard to FIG. **4B** in order to generate a real-time hybrid model **201** (e.g., retrained hybrid model **201**, updated hybrid model **201**) based on the pre-well hybrid model **201** and the acquired real-time data. In other words, utilizing the online well data, the hybrid model **201** may enhance the pre-well hybrid model **201**. As a result, the real-time hybrid model **201** may generate (e.g., determine) real-time predictive ROP and wear models for a given earth-boring tool and drilling operation. Moreover, as will be understood, the real-time hybrid model **201** may be continuously refined and updated by continually feeding the real-time hybrid model **201** real-time data and retraining the hybrid model **201**.

Based on the real-time predictive ROP and wear models generated by the hybrid model **201**, the hybrid model **201** may provide recommendations for drilling parameters, which may lead to real-time drilling parameters optimization. Additionally, based on the real-time predictive ROP

and wear models generated by the hybrid model **201**, the hybrid model **201** determine and provide an expected earth-boring tool life, most probable wear states, predicted ROP bounds, optimized trip plans, optimized trajectories, etc. Additionally, more accurate predictive ROP and wear models will result in better earth-boring tool and drilling parameters selections, which will result in higher quality boreholes and better success rates of achieving well plans. Moreover, better earth-boring tool and drilling parameters may maximize ROP and optimize directional objectives during a drilling operation.

Furthermore, as will be understood by one of ordinary skill in the art, the prediction system **129** described herein may be advantageous over conventional methods of predicting earth-boring tool operations. For example, the prediction system **129** of the present disclosure may provide a relatively fast and accurate predictive model that requires minimal offset well data. Additionally, the prediction system **129** of the present disclosure may be capable of accounting for introductions of new input variables and/or conditions as well as uncertainties.

Moreover, information provided via the real-time predictive ROP and wear models may be utilized to optimize PDC bit design and drilling parameters of an earth-boring tool for performance in a dull state and to extend ROP in a dull state. As a result, the prediction system **129** of the present disclosure may reduce invisible lost time and non-productive time, which may lead to cost savings and more efficient drilling operations.

FIG. **6** is a block diagram of a surface control unit **128** and/or prediction system **129** according to one or more embodiments of the present disclosure. As shown in FIG. **6**, in some embodiments, the surface control unit **128** and/or prediction system **129** may include an earth-boring tool monitoring system **600** (e.g., computing device). One will appreciate that one or more computing devices may implement the earth-boring tool monitoring system **600**. The earth-boring tool monitoring system **600** can comprise a processor **602**, a memory **604**, a storage device **606**, an I/O interface **608**, and a communication interface **610**, which may be communicatively coupled by way of a communication infrastructure **612**. While an exemplary computing device is shown in FIG. **6**, the components illustrated in FIG. **6** are not intended to be limiting. Additional or alternative components may be used in other embodiments. Furthermore, in certain embodiments, the computing device **600** can include fewer components than those shown in FIG. **6**. Components of the computing device **600** shown in FIG. **6** will now be described in additional detail.

In one or more embodiments, the processor **602** includes hardware for executing instructions, such as those making up a computer program. As an example and not by way of limitation, to execute instructions, the processor **602** may retrieve (or fetch) the instructions from an internal register, an internal cache, the memory **604**, or the storage device **606** and decode and execute them. In one or more embodiments, the processor **602** may include one or more internal caches for data, instructions, or addresses. As an example and not by way of limitation, the processor **602** may include one or more instruction caches, one or more data caches, and one or more translation lookaside buffers (TLBs). Instructions in the instruction caches may be copies of instructions in the memory **604** or the storage device **606**.

The memory **604** may be used for storing data, metadata, and programs for execution by the processor(s). The memory **604** may include one or more of volatile and non-volatile memories, such as Random Access Memory

(“RAM”), Read-Only Memory (“ROM”), a solid state disk (“SSD”), Flash memory, Phase Change Memory (“PCM”), or other types of data storage. The memory **604** may be internal or distributed memory.

The storage device **606** includes storage for storing data or instructions. As an example and not by way of limitation, storage device **606** can comprise a non-transitory storage medium described above. The storage device **606** may include a hard disk drive (HDD), a floppy disk drive, flash memory, an optical disc, a magneto-optical disc, magnetic tape, or a Universal Serial Bus (USB) drive or a combination of two or more of these. The storage device **606** may include removable or non-removable (or fixed) media, where appropriate. The storage device **606** may be internal or external to the computing device **600**. In one or more embodiments, the storage device **606** is non-volatile, solid-state memory. In other embodiments, the storage device **606** includes read-only memory (ROM). Where appropriate, this ROM may be mask programmed ROM, programmable ROM (PROM), erasable PROM (EPROM), electrically erasable PROM (EEPROM), electrically alterable ROM (EAROM), or flash memory or a combination of two or more of these.

The I/O interface **608** allows a user to provide input to, receive output from, and otherwise transfer data to and receive data from computing device **600**. The I/O interface **608** may include a mouse, a keypad or a keyboard, a touch screen, a camera, an optical scanner, network interface, modem, other known I/O devices or a combination of such I/O interfaces. The I/O interface **608** may include one or more devices for presenting output to a user, including, but not limited to, a graphics engine, a display (e.g., a display screen), one or more output drivers (e.g., display drivers), one or more audio speakers, and one or more audio drivers. In certain embodiments, the I/O interface **608** is configured to provide graphical data to a display for presentation to a user. The graphical data may be representative of one or more graphical user interfaces and/or any other graphical content as may serve a particular implementation.

The communication interface **610** can include hardware, software, or both. In any event, the communication interface **610** can provide one or more interfaces for communication (such as, for example, packet-based communication) between the computing device **600** and one or more other computing devices or networks. As an example and not by way of limitation, the communication interface **610** may include a network interface controller (NIC) or network adapter for communicating with an Ethernet or other wire-based network or a wireless NIC (WNIC) or wireless adapter for communicating with a wireless network, such as a WI-FI.

Additionally or alternatively, the communication interface **610** may facilitate communications with an ad hoc network, a personal area network (PAN), a local area network (LAN), a wide area network (WAN), a metropolitan area network (MAN), or one or more portions of the Internet or a combination of two or more of these. One or more portions of one or more of these networks may be wired or wireless. As an example, the communication interface **610** may facilitate communications with a wireless PAN (WPAN) (such as, for example, a BLUETOOTH® WPAN), a WI-FI network, a WI-MAX network, a cellular telephone network (such as, for example, a Global System for Mobile Communications (GSM) network), or other suitable wireless network or a combination thereof.

Additionally, the communication interface **610** may facilitate communications various communication protocols. Examples of communication protocols that may be used

include, but are not limited to, data transmission media, communications devices, Transmission Control Protocol (“TCP”), Internet Protocol (“IP”), File Transfer Protocol (“FTP”), Telnet, Hypertext Transfer Protocol (“HTTP”), Hypertext Transfer Protocol Secure (“HTTPS”), Session Initiation Protocol (“SIP”), Simple Object Access Protocol (“SOAP”), Extensible Mark-up Language (“XML”) and variations thereof, Simple Mail Transfer Protocol (“SMTP”), Real-Time Transport Protocol (“RTP”), User Datagram Protocol (“UDP”), Global System for Mobile Communications (“GSM”) technologies, Code Division Multiple Access (“CDMA”) technologies, Time Division Multiple Access (“TDMA”) technologies, Short Message Service (“SMS”), Multimedia Message Service (“MMS”), radio frequency (“RF”) signaling technologies, Long Term Evolution (“LTE”) technologies, wireless communication technologies, in-band and out-of-band signaling technologies, and other suitable communications networks and technologies.

The communication infrastructure **612** may include hardware, software, or both that couples components of the computing device **600** to each other. As an example and not by way of limitation, the communication infrastructure **612** may include an Accelerated Graphics Port (AGP) or other graphics bus, an Enhanced Industry Standard Architecture (EISA) bus, a front-side bus (FSB), a HYPERTRANSPORT™ (HT) interconnect, an Industry Standard Architecture (ISA) bus, an INFINIBAND™ interconnect, a low-pin-count (LPC) bus, a memory bus, a Micro Channel Architecture (MCA) bus, a Peripheral Component Interconnect (PCI) bus, a PCI-Express (PCIe) bus, a serial advanced technology attachment (SATA) bus, a Video Electronics Standards Association local (VLB) bus, or another suitable bus or a combination thereof.

The embodiments of the disclosure described above and illustrated in the accompanying drawings do not limit the scope of the disclosure, which is encompassed by the scope of the appended claims and their legal equivalents. Any equivalent embodiments are within the scope of this disclosure. Indeed, various modifications of the disclosure, in addition to those shown and described herein, such as alternative useful combinations of the elements described, will become apparent to those skilled in the art from the description. Such modifications and embodiments also fall within the scope of the appended claims and equivalents.

What is claimed is:

1. A method, comprising:

receiving input data;

training a hybrid physics and machine-learning model with the input data by building a coefficient library of drilling parameters of a planned drilling operation, comprising:

determining initial predictions of the drilling parameters of the planned drilling operation based on physics data within the input data; and

determining relative influences and rankings of the drilling parameters of the planned drilling operation based on the physics data; and

providing, via the hybrid physics and machine-learning model, a predictive model representing a rate of penetration of an earth-boring tool and wear of the earth-boring tool during the planned drilling operation.

2. The method of claim 1, further comprising providing one or more recommendations of the drilling parameters based on the predictive model.

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3. The method claim 2, further comprising drilling a borehole based at least partially on the one or more recommendations of drilling parameters.

4. The method of claim 1, further comprising:  
 receiving real-time data from a drilling operation;  
 retraining the hybrid physics and machine-learning model based on a combination of the input data and the real-time data; and  
 providing, via the retrained hybrid physics and machine-learning model, an updated predictive model of a rate of penetration of the earth-boring tool and wear of the earth-boring tool during a remainder of the planned drilling operation.

5. The method of claim 4, further comprising providing one or more updated recommendations of drilling parameters based on the updated predictive model.

6. The method claim 1, wherein training a hybrid physics and machine-learning model comprises:  
 identifying drilling parameters having the greatest uncertainties; and  
 subjecting the drilling parameters to a parameter tuning process.

7. The method of claim 1, wherein providing a predictive model representing wear of the earth-boring tool comprises utilizing wear state characterization at a cutter level to predict wear of the earth-boring tool.

8. The method of claim 1, wherein the input data comprises offset well data and the physics data.

9. The method of claim 8, wherein the offset well data comprises one or more of formation logs, well architecture and design, surface and downhole data, bit and cutter design information, drilling system details, or bit dull information.

10. The method of claim 8, wherein the physics data comprises one or more of drill bit mechanics simulation models, three-dimensional geometry descriptions of earth-boring tools or formations, rock failure models, cutter-wear progression models, or cutter fracture criteria.

11. The method of claim 1, further comprising training a plurality of individual modules within the hybrid model.

12. The method of claim 11, wherein training the plurality of individual modules within the hybrid model comprises training at least a bit mechanics module, a cutter wear module, and a rate-of-penetration limiters module.

13. An earth-boring tool system, comprising:  
 a drilling assembly for drilling a wellbore; and  
 a surface control unit operably coupled to the drilling assembly, the surface control unit comprising a prediction system, comprising:  
 at least one processor; and  
 at least one non-transitory computer-readable storage medium storing instructions thereon that, when executed by the at least one processor, cause the prediction system to:  
 pre-train a plurality of modules individually within a hybrid physics and machine-learning model;  
 train the plurality of modules together to develop the hybrid physics and machine-learning model based on input data;  
 provide, via the hybrid physics and machine-learning model, a predictive model representing a rate of penetration of an earth-boring tool and wear of the earth-boring tool during a planned drilling operation;

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provide one or more recommendations of drilling parameters based on the predictive model;  
 utilize the one or more recommendations in a drilling operation;  
 receive real-time data from the drilling operation;  
 retrain the hybrid physics and machine-learning model based on a combination of the input data and the real-time data; and  
 provide, via the retrained hybrid physics and machine-learning model, an updated predictive model of a rate of penetration of the earth-boring tool and wear of the earth-boring tool during a remainder of the planned drilling operation.

14. The earth-boring tool system of claim 13, further comprising instructions that, when executed by the at least one processor, cause the prediction system to provide one or more updated recommendations of drilling parameters based on the updated predictive model.

15. The earth-boring tool system of claim 13, wherein providing a predictive model comprises analyzing the input data with one or more of physics models or machine-learning models of the hybrid physics and machine-learning model.

16. The earth-boring tool system of claim 15, wherein the machine-learning models are selected from a list consisting of a regression analysis, a classification analysis, a neural network, or an ensemble of machine-learning models.

17. A method, comprising:  
 receiving real-time data from a drilling operation at a trained hybrid physics and machine-learning model;  
 analyzing the real-time data via the hybrid physics and machine-learning model;  
 providing, via the hybrid physics and machine-learning model and based at least partially on the analysis, a predictive model representing a rate of penetration of an earth-boring tool and wear of the earth-boring tool throughout at least part of a remainder of the drilling operation;  
 providing one or more recommendations of drilling parameters based on the predictive model; and  
 operating at least a portion of the drilling operation using the one or more recommendations of drilling parameters.

18. The method of claim 17, wherein the drilling operation comprises an operation that involves at least one of a build-up-rate, a turn rate, a lateral ROP, an unconfined compressive strength, a walk rate, a dog leg severity, a WOB, a confined compressive strength, a contact force, a rib force, a bending moment, a pressure, an inclination, an azimuth, a borehole trajectory, a drilling torque, drilling vibrations, or a hole quality.

19. The method of claim 17, wherein analyzing the real-time data comprises analyzing the real-time data with one or more of physics models or machine-learning models of the hybrid physics and machine-learning model.

20. The method of claim 17, further comprising continuously retraining the hybrid physics and machine-learning model with real-time data throughout a duration of the drilling operation.