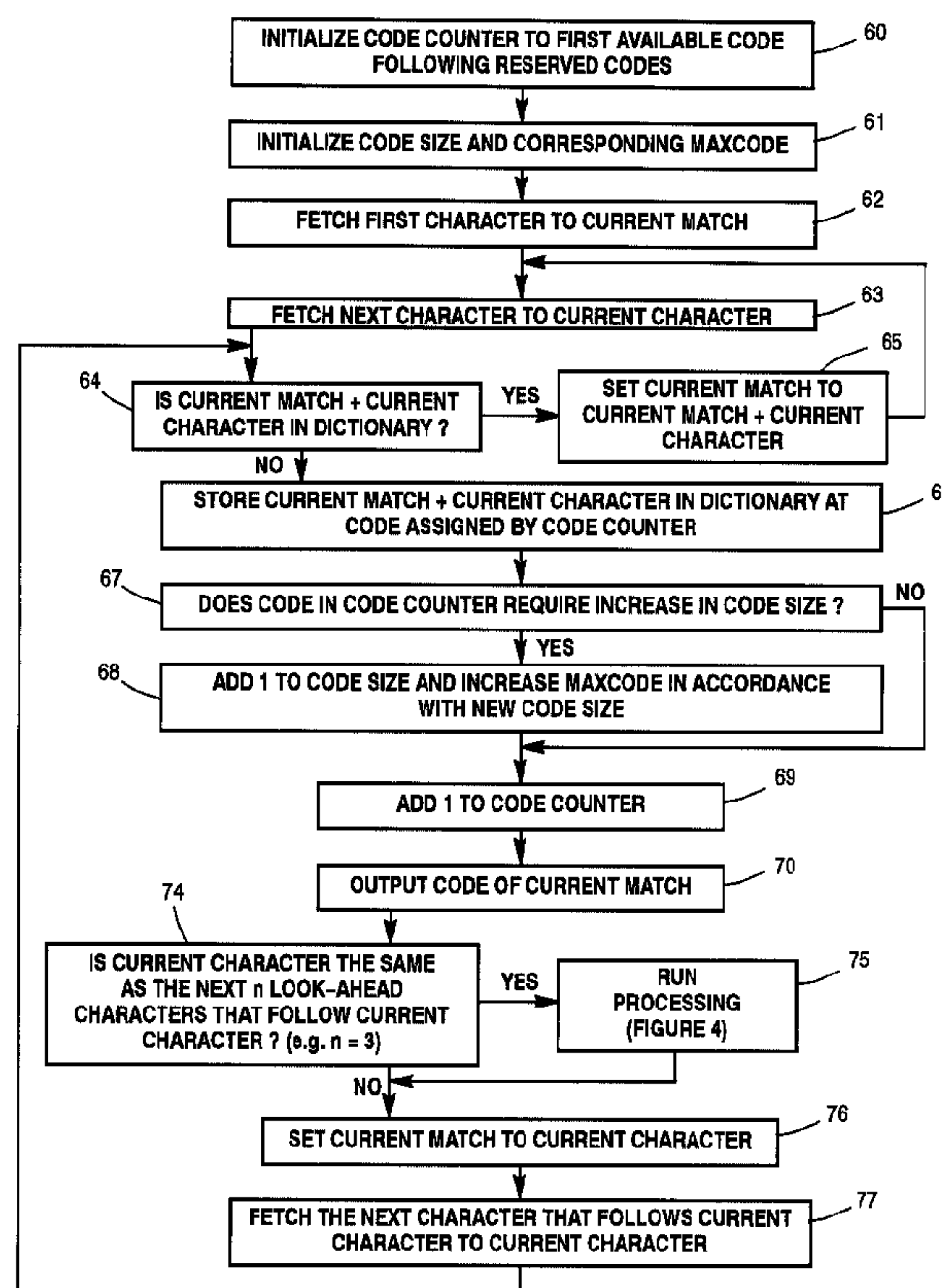




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(54) Titre : APPAREIL ET PROCEDE DE COMPRESSION DE DONNEES LZW INTEGRANT LE CODAGE / DECODAGE
PAR LONGUEUR DE PLAGE
(54) Title: LZW DATA COMPRESSION/DECOMPRESSION APPARATUS AND METHOD WITH EMBEDDED RUN-
LENGTH ENCODING/DECODING



(57) Abrégé/Abstract:

In an LZW data compressor, the occurrence of a character run in the input character stream is determined and the run count is added to the existing code in the compressor code counter to generate a compressor code output representative of the run count. The LZW data decompressor subtracts the existing code in the decompressor code counter from the received compressed code



(57) **Abrégé(suite)/Abstract(continued):**

to recover the run count. In accordance with a further feature, large length runs are processed by reducing the run count to less than the system maximum code by subtracting a selected predetermined constant from the run count. The reduced run count is outputted by the compressor preceded by a reserved code representative of the selected predetermined constant. In response to the received reserved code and the reduced count that follows, the decompressor adds the selected predetermined constant corresponding to the received reserved code to the received reduced count to recover the original run count.

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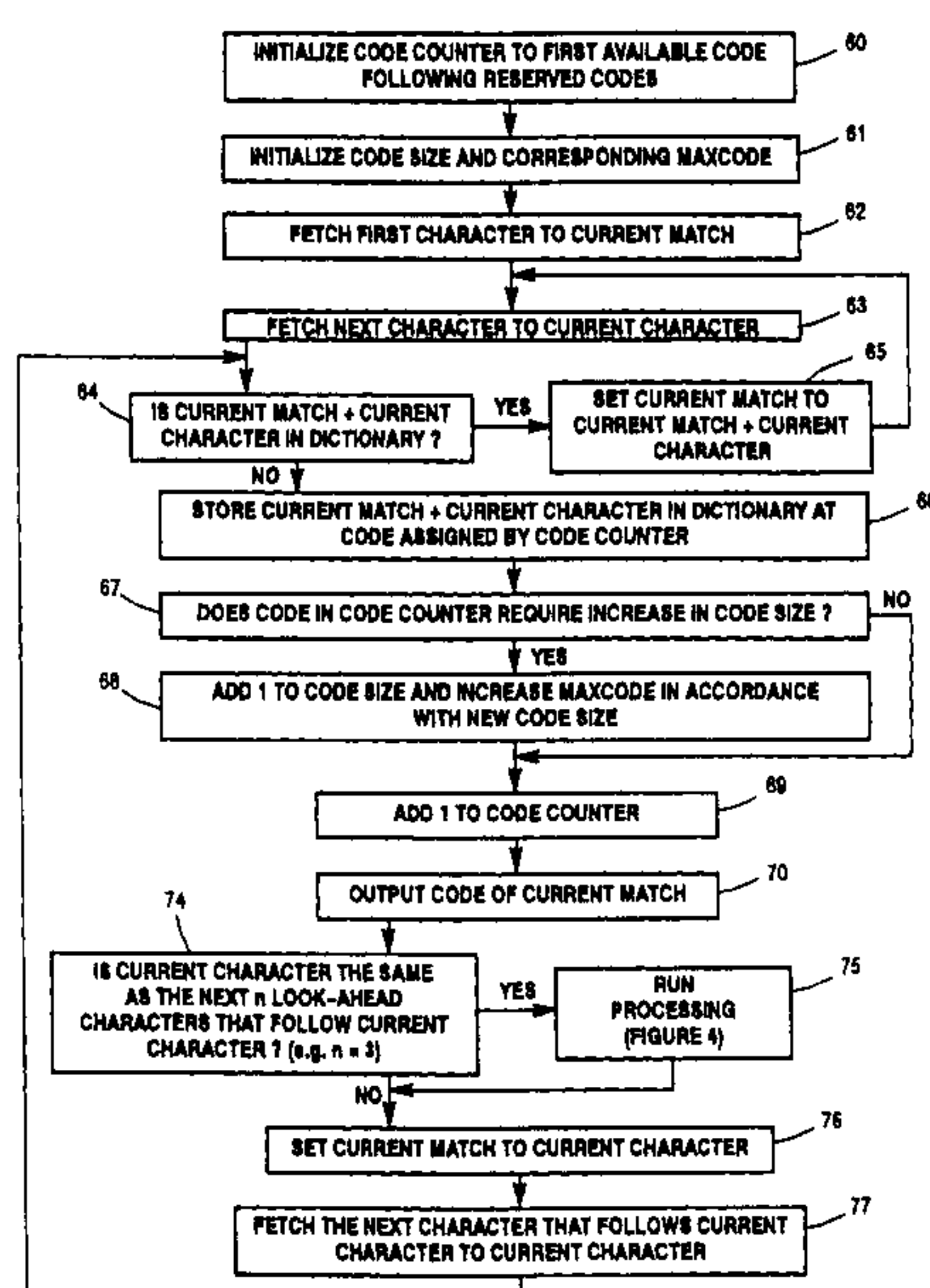
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(54) Title: LZW DATA COMPRESSION/DECOMPRESSION APPARATUS AND METHOD WITH EMBEDDED RUN-LENGTH ENCODING/DECODING



(57) Abstract: In an LZW data compressor, the occurrence of a character run in the input character stream is determined and the run count is added to the existing code in the compressor code counter to generate a compressor code output representative of the run count. The LZW data decompressor subtracts the existing code in the decompressor code counter from the received compressed code to recover the run count. In accordance with a further feature, large length runs are processed by reducing the run count to less than the system maximum code by subtracting a selected predetermined constant from the run count. The reduced run count is outputted by the compressor preceded by a reserved code representative of the selected predetermined constant. In response to the received reserved code and the reduced count that follows, the decompressor adds the selected predetermined constant corresponding to the received reserved code to the received reduced count to recover the original run count.

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1 **LZW DATA COMPRESSION/DECOMPRESSION APPARATUS AND METHOD**
 WITH EMBEDDED RUN-LENGTH ENCODING/DECODING

BACKGROUND OF THE INVENTION

5 1. **Field of the Invention**

 The invention relates to LZW data compression and decompression systems particularly with respect to including run-length encoding and decoding within the LZW compression and decompression processing,
10 respectively.

 2. **Description of the Prior Art**

 Professors Abraham Lempel and Jacob Ziv provided the theoretical basis for LZ data compression and decompression systems that are in present day widespread
15 usage. Two of their seminal papers appear in the IEEE Transactions on Information Theory, IT-23-3, May 1977, pp. 337-343 and in the IEEE Transactions on Information Theory, IT-24-5, September 1978, pp. 530-536. A
20 ubiquitously used data compression and decompression system known as LZW, adopted as the standard for V.42 bis modem compression and decompression, is described in U.S. Patent 4,558,302 by Welch, issued December 10, 1985. LZW has been adopted as the compression and decompression
25 standard used in the GIF and TIFF image communication protocols.

30

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1 Another type of data compression and
decompression, denoted as run-length encoding (RLE),
compresses a repeating character run by providing a
compressed code indicating the character and the length
5 of the run. RLE is thus effective in encoding long
strings of the same character. For example, RLE is
effective in compressing a long sequence of blanks that
may be included at the beginning of a data file. RLE
is also effective in image compression where an image
10 contains a long run of consecutive pixels having the
same value, such as in the sky portion of a land-sky
image.

 In the prior art, run-length encoding has been
combined with LZ systems as exemplified in the following
15 U.S. patents: patent 4,929,946 by O'Brien et al., issued
May 29, 1990; patent 4,971,407 by Hoffman, issued November
20, 1990; patent 4,988,998 by O'Brien, issued January
29, 1991; patent 5,247,638 by O'Brien et al., issued
September 21, 1993; patent 5,389,922 by Seroussi et al.,
20 issued February 14, 1995; and patent 5,861,827 by Welch
et al., issued January 19, 1999.

 In some prior art systems, run-length encoding
has been combined with an LZ system by applying the data
to a run-length encoder and then applying the run-length
25 encoded data to the LZ based system. In such an
architecture, a run-length encoder is utilized at the
front end of the compressor and a run-length decoder
is utilized at the output end of the decompressor. Such
a system suffers from the disadvantages of increased
30 equipment, expense, control overhead and processing time.
Patents 4,971,407 and 4,988,998 exemplify such a system.

 In the LZW based system of patent 5,389,922,
certain output codes from the compressor are suppressed
in the presence of a run of repeating input data
35 characters. A special run enhancement engine is utilized
at the input to the decompressor to regenerate the missing
codes.

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1 In the compressor of the system of patent
5,861,827, when a partial string W and a character C
are found, a new string is stored with C as an extension
character on the string PW where P was the string conveyed
5 in the last transmitted output compressed code. With
this compression algorithm, a run of characters is encoded
in two compressed codes regardless of its length. The
decompressor of this system uses a special unrecognized
code process to maintain synchronism with the compressor.

10 In the system of patent 4,929,946 a run is
indicated by transmitting one of a predetermined set
of reserved reference values followed by a repeat count
for the run. The reserved reference values are defined
so that the number of bits in the repeat count that
15 follows the reserved reference value is reduced. The
requirement of the use of the reserved reference value
in the compressed stream for every run that is detected
tends to reduce the compression. Additionally, the system
is apparently limited to processing relatively small
20 length runs. Patent 5,247,638 provides descriptions
similar to those of patent 4,929,946.

 Another data compression system involving the
encoding of data character runs is disclosed in said
U.S. Patent 6,166,665, issued December 26, 2000. In the compressor
25 of this patent application, runs are processed by
successively looking ahead into the input to determine
if contiguous numerically increasing segments exist in
the run.

 Yet another data compression system involving
30 the encoding of data character runs is disclosed in said
U.S. Patent 6,137,428, issued October 24, 2000. In the compressor
of this patent application, runs are processed by
mathematically determining, from the length of the run,
the respective output codes corresponding to the
35 contiguous numerically increasing segments that exist
in the run.

 It is an object of the present invention to embed

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1 run-length encoding and decoding in an LZW data
compression and decompression system where a provision
is included that does not require the transmission of
a special reserved code to inform the decompressor of
5 the existence of the run. It is a further object of
the present invention to provide for the processing of
very large length runs.

SUMMARY OF THE INVENTION

10 The present invention enhances the well-known
LZW data compression/decompression system by determining
when a run of input data characters occurs and by
combining the run character count with the existing code
value from the compressor code counter to generate a
15 compressor output representative of the run count. The
decompressor utilizes the existing code value in the
decompressor code counter to recover the run count from
the compressor output. In a further feature of the
present invention, very large length runs are processed
20 by reducing the run count by a selected predetermined
process and outputting the reduced run count preceded
by a reserved code representative of the selected
predetermined process. In response to the received
reserved code, the decompressor applies the predetermined
25 process corresponding to the received reserved code to
recover the original run count by increasing the received
reduced count in accordance with the predetermined
process.

30 BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 is a schematic block diagram of a data
compressor for compressing data in accordance with the
present invention.

35 Figure 2 is a chart providing details of the
Count Reduction Table of Figure 1.

Figure 3 is a control flow chart illustrating
the operations executed by the compressor of Figure 1

- 5 -

1 so as to perform data compression in accordance with
the present invention.

Figure 4 is a control flow chart illustrating
the run processing logic utilized in the flow chart of
5 Figure 3 so as to perform data compression in accordance
with the features of the present invention.

Figure 5 is a schematic block diagram of a data
decompressor embodied in accordance with the present
invention for recovering data compressed by the compressor
10 of Figure 1.

Figure 6 is a chart providing details of the
Count Increase Table of Figure 5.

Figure 7 is a control flow chart illustrating
the operations executed by the decompressor of Figure
15 5 so as to perform data decompression in accordance with
the present invention.

Figure 8 is a control flow chart illustrating
the run processing logic utilized in the flow chart of
Figure 7 so as to perform data decompression in accordance
20 with the features of the present invention.

Figure 9 is a chart exemplifying the operations
of the compressor of Figure 1 in accordance with the
control flow charts of Figures 3 and 4.

Figure 10 is a chart exemplifying the operations
25 of the decompressor of Figure 5 in accordance with the
control flow charts of Figures 7 and 8.

DESCRIPTION OF THE PREFERRED EMBODIMENT

Referring to Figure 1, a data compressor 10 is
30 illustrated that compresses a stream of input data
characters applied at an input 11 into a stream of
corresponding compressed codes at an output 12. The
compressor 10 includes working registers denoted as a
Current Character register 13, a Current Match register
35 14, a Code Size register 15, a Look-Ahead Buffer 16,
a Count register 17, a Maxcode register 20, a Character
Temp register 21 and a Reserved Code register 22. The

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1 compressor 10 further includes a Code Counter 23 for
sequentially generating code values that are used to
process run and non-run characters in accordance with
the present invention in a manner to be described.

5 The compressor 10 further includes look-ahead
comparison logic 24 that performs comparisons between
a character in the Current Character register 13 and
characters in the Look-Ahead Buffer 16 to determine if
a run is about to commence in a manner to be further
10 described. The compressor 10 further includes a Count
Reduction Table 25 for use in run processing in accordance
with the present invention. The Count Reduction Table
25 provides a Limit 26 in a manner to be explained.
Details of the Count Reduction Table 25 and Limit 26
15 will be described below with respect to Figure 2.

 The compressor 10 further includes count reduction
logic 27 for reducing the count value in the register
17 pursuant to the Count Reduction Table 25 in a manner
to be described in accordance with the present invention.
20 Further included in the compressor 10 is control 30 for
controlling the operations of the compressor 10 in
accordance with the operational flow charts of Figures
3 and 4 in a manner to be described.

 Also included is a Dictionary 35 for storing
25 character strings in cooperation with the compressor
10 in a manner to be described. Data is communicated
between the compressor 10 and the Dictionary 35 via a
bi-directional data bus 36 under control of a control
bus 37.

30 Further included is an Input Character Buffer
40 that buffers the input data character stream received
at the input 11. The individual input data characters
are applied from the Input Character Buffer 40 via a
bus 41 to the Current Character register 13, the Current
35 Match register 14 and the Look-Ahead Buffer 16 in
accordance with operations to be described. The
compressor 10 controls acquiring input data characters

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1 from the Input Character Buffer 40 via a control bus 42.

Briefly, the operation of the compressor 10 is as follows. Input data characters are fetched from the Input Character Buffer 40 and conventional LZW data
5 compression is performed thereon providing a compressed code stream at the output 12. In a well-known manner the Code Counter 23 is progressively incremented to assign code values to extended strings that are stored in the Dictionary 35. The compressor 10 is described herein
10 in terms of a variable length code as is well understood in the art. When the count in the Code Counter 23 attains a maximum count as stored in the Maxcode register 20, the Code Size in the register 15 is incremented. The LZW compression algorithm is described in detail in said
15 patent 4,558,302.

Using the Look-Ahead Buffer 16 and the look-ahead comparison logic 24, consecutive input characters are examined and if n (e.g. n=3) look-ahead characters are the same as the character in the Current Character
20 register 13, the LZW process diverts to run-length encoding to process the character run. The number of characters in the run are counted using the Current Character register 13, the Count register 17 and the Character Temp register 21. If the run count in the
25 Count register 17 is less than or equal to the difference between the maximum code in the Maxcode register 20 and the extant code in the Code Counter 23, the sum of the run count in the Count register 17 and the extant code in the Code Counter 23 is output. Otherwise, if the
30 run count is less than the system maximum code, a first Reserved Code is output followed by the run count using the system maximum code size. If the run count is greater than or equal to the system maximum code, the count is reduced by a selected predetermined process so that the
35 reduced count is less than the system maximum code. A further Reserved Code that corresponds to the selected predetermined process is output followed by the reduced

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1 count.

The embodiment described herein is, for purposes of explanation, illustrated in an ASCII implementation. The ASCII environment utilizes an 8 bit character size supporting an alphabet of 256 characters. In a variable length code implementation, the Code Size may begin with 9 bits and sequentially increase to 10, 11, 12, etc., bits at codes 512, 1024, 2048, etc., respectively. Typically in such systems, a maximum Code Size of 12 bits is utilized with a maximum system code of 4096.

In such an ASCII implementation, the set of Reserved Codes are conveniently larger than the largest character value and, as will be explained, conveniently begin at Reserved Code 257. In the embodiment to be described, five Reserved Codes are utilized ending at Reserved Code 261. Thus, in the ASCII implementation, the first available code from the Code Counter 23 for representing multiple character strings begins with code 262. It is appreciated that embodiments could also be predicated on a fixed length code output of, for example, 12 bits, as is well known.

Referring to Figure 2, details of the Count Reduction Table 25 and Limit 26 of Figure 1 are illustrated. The Count Reduction Table 25 defines a plurality of selectable predetermined processes so that a run count value may be reduced in a predetermined manner to a value less than the system maximum code. The Count Reduction Table 25 also defines Reserved Codes corresponding to the respective processes. Each of lines 50-53 of the Table 25 defines one of the processes. For purposes of specificity, the system maximum code is 2^{12} or 4096. The process 50, for example, is selected for count values that are greater than or equal to 2^{12} but less than 2×2^{12} . As seen in the Reduced Count column of the Table for process 50, run counts in this range are reduced by 2^{12} . The Reserved Code for the process 50 is 258. For convenience, the decimal value of the

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1 upper limit for each count range is given in the so
denoted column of the Table. For the parameters utilized,
it is appreciated that the largest run count to be
processed by the system is limited to runs of less than
5 20480 characters. It is furthermore appreciated that
this Limit is increased by merely adding further lines
to the Table.

The Count Reduction Table 25 is established for
use in an ASCII environment where the characters are
10 represented in 8 bits and have character values in the
range of 0-255. The Reserved Codes are selected as
257-261. The first available code for representing
multiple character strings is therefore 262. For purposes
of specificity, the system maximum code size is 12 bits
15 providing a system maximum code of 4096. Run counts
that are less than the system maximum code may, in a
manner to be later explained, be processed in a manner
that is represented by the Reserved Code value of 257.
The first line of Table 25 denotes this relationship.

20 With continued reference to Figure 1, the
conventional LZW processing utilizes the Current Character
register 13, the Current Match register 14, the Code
Size register 15, the Code Counter 23 and the Dictionary
35. The run processing in accordance with the present
25 invention also utilizes the Code Counter 23 as well as
the Look-Ahead Buffer 16, the Count register 17, the
Maxcode register 20, the Character Temp register 21,
the Reserved Code register 22, the look-ahead comparison
logic 24, the Count Reduction Table 25, the Limit 26
30 and the count reduction logic 27. The control flow charts
of Figures 3 and 4 illustrate the detailed operations
to be executed by the compressor 10. The control 30
is considered as containing appropriate circuitry such
as state machines to control execution of the operations.
35 Referring to Figure 3, with continued reference
to Figure 1, at a block 60, the Code Counter 23 is
initialized to the first available code following the

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1 Reserved Codes that are indicated in the Reserved Code
set of the Count Reduction Table 25 of Figure 2. Thus,
in the illustrated embodiment, the Code Counter 23 is
set to 262. At a block 61, the Code Size register 15
5 is initialized to the beginning Code Size, for example,
9 bits in the ASCII embodiment. Additionally, the Maxcode
register 20 is set to the corresponding maximum code
for the Code Size. As appreciated, the maximum code
in 9 bits is 511. The Reserved Codes indicated in the
10 block 60 and the Maxcode indicated in the block 61 are
utilized in the run processing in accordance with the
present invention in a manner to be described.

At a block 62, the first input character is
fetched into the Current Match register 14 and, at a
15 block 63, the next following character is fetched into
the Current Character register 13. The value in the
Current Match register 14 together with the next character
in the Current Character register 13 comprise a two
character string as is well appreciated in the art (e.g.
20 see patent 4,558,302).

Processing continues at a block 64 wherein the
Dictionary 35 is searched to determine if the string
comprising the Current Match concatenated by the Current
Character is in the Dictionary. Dictionary searching
25 procedures are well known in the art for performing the
function of the block 64 (e.g. see patent 4,558,302 and
patent 5,861,827).

If at the block 64 the string is found in the
Dictionary 35, the YES branch from the block 64 is taken
30 to a block 65. At block 65, the contents of the Current
Match register 14 is updated to contain an indication
of the string that was found. As is well known in the
art, a string has a code associated therewith and,
generally, the string code of the currently matched string
35 is set into the Current Match register 14. Details of
specific implementations for the function of the block
65 are well known (e.g. see patent 4,558,302 and patent

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1 5,861,827). After updating the Current Match register
14 with the currently matched string, control returns
to the block 63 to fetch the next input data character
to the Current Character register 13. In this manner,
5 the loop formed by the blocks 63-65 compares the input
data character stream with the strings stored in the
Dictionary 35 to find the longest match therewith.

In the block 64, when the concatenation of the
currently matched string with the next character fetched
10 at the block 63 results in an extended string that is
not in the Dictionary 35, the NO branch from the block
64 is taken to a block 66. At the block 66 this extended
string that was not found in the Dictionary 35 is entered
therein and the extant code of the Code Counter 23 is
15 assigned to this stored extended string. Details of
specific implementations for the function of the block
66 are well known (e.g. see patent 4,558,302).

Processing proceeds to a block 67 wherein the
code in the Code Counter 23 is tested to determine if
20 an increase in the Code Size is required. If so,
processing continues to a block 68 whereat the Code Size
register 15 is incremented by 1. If an increase in Code
Size is required, the value in the Maxcode register 20
is also increased in accordance with the new Code Size.
25 The value Maxcode is increased to the maximum code that
will be supported by the new Code size bits. For example,
a Code Size of 10 bits has a Maxcode of $(2^{10}-1)=1023$.
The value in the Maxcode register 20 is utilized in the
run processing of the present invention in a manner to
30 be discussed with respect to Figure 4. If an increase
in Code Size is not required at the block 67, the block
68 is by-passed to continue processing at a block 69.
At block 69, the Code Counter 23 is incremented by 1.

Processing continues at a block 70 whereat the
35 code of the Current Match is output as part of the
compressed code stream provided at the compressor output
12. The code of the Current Match is provided by the

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1 Current Match register 14. When Current Match is a
multiple character string, the code of the string resides
in the Current Match register 14 and was the longest
match found in the Dictionary 35 as described above with
5 respect to the block 64. It is appreciated that the
Current Match that is output at the block 70 can also
be a single character. The output code in this case
is the value of the character. Implementation details
of the functionality of block 70 are well known in the
10 art (e.g. see patent 4,558,302 and patent 5,861,827).

Processing continues at a block 74 whereat the
Current Character in the register 13 is tested against
the next n look-ahead characters that follow Current
Character to determine if they are the same. This process
15 is performed by the logic 24 utilizing the appropriate
characters fetched into the Look-Ahead Buffer 16. For
example, n may be set equal to 3 for convenience.

At the block 74, the Current Character is compared
to the next n look-ahead characters that follow Current
20 Character to determine if a run of the same character
is about to commence. If the Current Character is the
same as the next n look-ahead characters, the YES branch
of the block 74 is taken to a run processing block 75.
The details of the run processing block 75 are illustrated
25 in Figure 4.

If one of the n look-ahead characters does not
match Current Character, the NO branch of the block 74
is taken to continue the conventional LZW data compression
processing.

30 Accordingly, processing continues at a block
76 whereat the Current Match register 14 is set to the
character in the Current Character register 13.
Thereafter, at a block 77, the next input data character
that follows the present Current Character is fetched
35 to the Current Character register 13. It is appreciated
that, at the block 76, the Current Match register 14
is set to the input data character that resulted in a

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1 mismatch in the previous processing. Implementation
details for the functionality of blocks 76 and 77 are
well known in the art (e.g. see patent 4,558,302 and
patent 5,861,827). Control then returns to the block
5 64 to begin a new LZW data compression cycle with the
Current Match code that now resides in the Current Match
register 14 and the Current Character that now resides
in the Current Character register 13.

It is appreciated that aside from the blocks
10 74 and 75, the reference to Maxcode in the blocks 61
and 68 and the reference to Reserved Codes in the block
60, the remainder of Figure 3 depicts standard LZW data
compression processing. Thus, any known implementation
of LZW data compression can be utilized in implementing
15 the LZW data compression aspects of the present invention.

Referring to Figure 4, with continued reference
to Figures 1-3, the details of the run processing of
the block 75 of Figure 3 are illustrated. The run
processing begins at a block 80 whereat the character
20 in the Current Character register 13 is provided at the
output 12 of the compressor 10. At a block 81, the Count
in the Count register 17 is set to 0. Processing
continues with a block 82 whereat the Current Character
in the register 13 is saved to the Character Temp register
25 21. Thereafter, at a block 83, the next character that
follows Current Character is fetched to the Current
Character register 13.

At a block 84, the fetched character in the
Current Character register 13 is compared to the preceding
30 character in the Character Temp register 21 to determine
equality therebetween. If Current Character is equal
to Character Temp, the character run is continuing and
the YES branch from the block 84 is taken. If, however,
Current Character is not equal to Character Temp, the
35 character run has ended with the mismatching character
residing in the Current Character register 13. When,
at the block 84, the end of the character run is

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1 indicated, the NO branch is taken therefrom.

The YES branch from the block 84 enters a block 85 whereat the Count in the Count register 17 is tested to determine if the Count, when incremented by 1, would
5 remain less than the Limit 26 established by the Count reduction process. The Limit 26 was discussed above with respect to Figure 2 and in the described implementation is equal to 20480 characters. It is appreciated that this Limit is implementation specific
10 and can be significantly greater merely by adding further lines to the Count Reduction Table 25 as discussed above with respect to Figure 2.

If Count+1 is less than the Limit at the block 85, processing continues with a block 86 whereat the
15 Count in the Count register 17 is incremented by 1. Thus, the run count in the Count register 17 is incremented to count the run character just fetched at the block 83 which matches the character in the Character Temp register 21 at the block 84. Processing then loops
20 back to the block 82 to continue counting the characters of the run.

The blocks 81-86 provide logic for counting the characters of the run. Other logic arrangements may be utilized to the same effect in performing this
25 function.

If the run has ended at the block 84 or if the next Count will be greater than the Limit at the block 85, the respective NO branches proceed to a block 90. At the block 90 a test is made to determine if the Count
30 in the Count register 17 is less than or equal to Maxcode minus the code in the Code Counter 23. The test of the block 90 is performed to determine if sufficient counts remain in the Code Counter 23 at the current Code Size to accommodate the Count of the run characters established
35 by the blocks 81-86. If so, the Count of the run characters can be transmitted to the decompressor without using any special reserved code to signal the decompressor

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1 that run information is about to be received.

Accordingly, the YES branch from the block 90 is taken to a block 91 whereat the Count in the Count register 17 is added to the code from the Code Counter
5 23 with the resulting value set into the Count register 17. Processing then proceeds to a block 92 whereat the Count in the Count register 17 is provided at the output 12 of the compressor 10.

Processing then returns to the block 76 of Figure
10 3 to re-enter the LZW processing loop.

If, at the block 90, the Count is greater than Maxcode minus the code in the Code Counter, the NO branch from the block 90 is taken to a block 93. The block 93 is the entrance to processing used when the Count
15 of the run characters is too large to be accommodated by the processing of the blocks 91 and 92. The processing that follows the block 93 uses procedures delineated in the Count Reduction Table 25 as discussed above with respect to Figure 2. In the processing entered from
20 the block 93, the compressor 10 signals the occurrence of a run by outputting one of the Reserved Codes delineated in the Table 25.

Accordingly, at the block 93, the Count is tested to determine if it is less than the system maximum code.
25 If so, processing proceeds to a block 94 at which the Reserved Code register 22 is set to the first Reserved Code value. As observed in the first line of the Table 25 of Figure 2, the first Reserved Code of the illustrated embodiment is 257.

30 At a block 95, the first Reserved Code value now in the Reserved Code register 22 is provided to the output 12 of the compressor 10. Thereafter, at a block 96, the Count from the Count register 17 is provided to the output 12 of the compressor 10. The compressor
35 10 outputs this count value using the system maximum Code Size. As discussed above, the maximum Code Size for the disclosed embodiment is 12 bits. Other bit and

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1 Code Sizes may also be utilized in practicing the invention to the same effect. Processing from the block 96 returns to the block 76 of Figure 3 to re-enter the LZW processing loop.

5 When, at the block 93, the Count is not less than the system maximum code, processing enters a block 97 followed by a block 98. At the blocks 97 and 98, a predetermined process is selected, as discussed above with respect to Figure 2, from the processes 50-53 in
10 accordance with the value of the Count in the Count register 17. Thus at the block 97, with reference to Figure 2, the Count in the Count register 17 is reduced by the predetermined process that is selected so that the reduced Count is less than the system maximum code.
15 This reduced Count is then set into the Count register 17. For example, if the count before reduction is greater than or equal to 3×2^{12} and less than 4×2^{12} , the process 52 is selected wherein the Count in the Count register 17 is reduced by 3×2^{12} .

20 At the block 98, the Reserved Code register 22 is set to a Reserved Code value that corresponds to the selected predetermined process. Thus, when the predetermined process 52 is selected, the Reserved Code register 22 is set to 260.

25 Processing then continues with the blocks 95 and 96 whereat the Reserved Code from the Reserved Code register 22 and the Count from the Count register 17 are output to signal the occurrence of the run processed in the blocks 97 and 98 and to convey the run count
30 therefor. Processing then returns to the block 76 of Figure 3 to re-enter the LZW data processing loop.

It is appreciated from the processing of the blocks 93-98 that very large runs can be accommodated by the system of the present invention. The specific
35 embodiment illustrated can accommodate 20479 run characters utilizing the predetermined process 53.

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1 Referring to Figure 5, with continued reference
to Figure 1, a data decompressor 110 is illustrated that
decompresses a stream of compressed codes applied at
an input 111 into a recovered stream of data characters
5 at an output 112. It is appreciated that the compressed
code stream from the output 12 of the compressor 10
(Figure 1), if applied to the input 111 of the
decompressor 110, results in the recovery, at the output
112 of the decompressor 110, of the original input data
10 character stream applied to the input 11 of the
compressor 10.

The decompressor 110 includes working registers
denoted as a Current Code register 113, a Previous Code
register 114, a Code Size register 115 and a Count
15 register 117. The decompressor 110 further includes
a Code Counter 123 for sequentially generating code values
that are used to process incoming compressed codes in
a manner to be described. It is appreciated that the
Code Counter 123 will maintain a lock-step relationship
20 with the Code Counter 23 of the compressor 10 of Figure 1
as will be appreciated from the descriptions to follow.

The decompressor 110 also includes a Count
Increase Table 125 utilized in processing incoming
compressed codes representative of data character runs.
25 Details of the Count Increase Table 125 will be described
with respect to Figure 6. Also included is count increase
logic 127 utilized together with the Count Increase Table
125 for restoring incoming reduced count values to
appropriate run count values. The count increase logic
30 127 and Count Increase Table 125 reverses the count
reduction effected by the Count Reduction Logic 27 and
Count Reduction Table 25 of the compressor 10 of Figure 1.

Further included in the decompressor 110 is
control 130 for controlling the operations of the
35 decompressor 110 in accordance with the operational flow
charts of Figures 7 and 8 in a manner to be described.

A Dictionary 135 is included for storing data

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1 character strings corresponding to received compressed
code inputs. In the operation of the decompressor 110,
the contents of the Dictionary 135 are maintained
identical to the contents of the Dictionary 35 of the
5 compressor 10 of Figure 1. The Dictionary 135 is coupled
to the decompressor 110 via a bi-directional data bus
136 and a control bus 137.

Included with the decompressor 110 is an Input
Code Buffer 140 that buffers the input compressed codes
10 received at the input 111. The individual input codes
are applied from the Input Code Buffer 140, via a bus
141, to the Current Code register 113 in accordance with
operations to be described. The decompressor 110 controls
acquiring input codes from the Input Code Buffer 140
15 via a control bus 142.

Briefly, the operation of the decompressor 110
is as follows. A code fetched to the Current Code
register 113 is examined to determine if it greater than
the extant code of the Code Counter 123. If so, the
20 input code represents a run count which is recovered
by subtracting the extant code in the Code Counter 123
from the received input code. If the input Current Code
is equal to a Reserved Code, the next following code
is fetched which is a run count. The received run count
25 value is processed in accordance with the value of the
particular Reserved Code. In both instances where the
input data represents a character run, the character
is obtained from the Previous Code register 114 and the
run count is obtained in a manner to be further described.

30 If the input Current Code is less than or equal
to the extant code of the Code Counter 123, standard
LZW data decompression is performed to recover the data
character string corresponding to the input Current Code.
Extended strings are stored in the Dictionary 135 in
35 a manner well understood in the art of LZW data
decompression.

Referring to Figure 6, with continued reference

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1 to Figure 5, details of the Count Increase Table 125
are illustrated. As indicated in lines 150-153, the
run count is recovered from an input code received by
the decompressor 110 by adding the illustrated values
5 to the received code in accordance with the respective
received Reserved Code as depicted. Specifically, lines
150-153 of the Table 125 indicate that in response to
receiving Reserved Codes 258-261, respectively, the Count
is increased by 2^{12} ; 2×2^{12} ; 3×2^{12} or 4×2^{12} , respectively.
10 In response to the Reserved Code 257, the received count
is used directly without increase as will be further
explained. The first line of Table 125 depicts this
relationship.

The control flow charts of Figures 7 and 8
15 illustrate the detailed operations to be executed by
the decompressor 110. The control 130 is considered
as containing appropriate circuitry such as state machines
to control execution of the operations.

Referring to Figure 7, with continued reference
20 to Figures 5 and 6, at a block 160 the Code Counter 123
is initialized in the same manner as described above
with respect to the block 60 of Figure 3. At a block
161, the Code Size register 115 is initialized to the
beginning Code Size as explained above with respect to
25 the block 61 of Figure 3.

At a block 162, the first or the next input
compressed code is fetched to the Current Code register
113. If control proceeds from block 161 to block 162,
the code that is fetched will be the first code. If
30 control enters block 162 via the illustrated return path
from run processing, the code that is fetched will be
the next code rather than the first code.

At a block 163, the decompressor 110 provides,
at its output 112, the string of data characters
35 corresponding to the compressed code fetched into the
Current Code register 113. Data character string recovery
from an input compressed code using the Dictionary 135

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1 is well known in the art of LZW data decompression.
Numerous specific implementations are well known for
the function of the block 163 (e.g. see patent 4,558,302).

It is appreciated that the code fetched to the
5 Current Code register 113 may represent either a single
character string or a multi-character string. As is
well known, such strings are distinguished from one
another by the value of the code. Generally, multi-
character strings are represented by codes that are
10 greater than or equal to the first available code
discussed above with respect to the block 160. Codes
for single character strings generally have values equal
to, or representative of, the single character and
therefore have values less than the first available code.

15 At a block 164, the code in the Current Code
register 113 is transferred to the Previous Code register
114. At a block 165, the next input compressed code
is fetched to the Current Code register 113.

At a block 166, the code in the Current Code
20 register 113 is tested to determine if it is equal to
a Reserved Code. In the illustrated embodiment, the
reserved codes are 257-261 as denoted in the Count
Increase Table 125 of Figure 6. If Current Code is not
equal to a Reserved Code, the NO branch from the block
25 166 is taken to a block 167. At the block 167, the code
in the Current Code register 113 is tested to determine
if it greater than the extant code in the Code Counter
123. If Current Code is not greater than Code Counter,
the NO branch from block 167 is taken to a block 169.

30 If, however, the Current Code is equal to a
Reserved Code, the YES branch from the block 166 is taken
to a run processing block 168. Similarly, if Current
Code is greater than Code Counter, the YES branch from
the block 167 is taken to the run processing block 168.
35 Details of the decompression run processing will be
described with respect to Figure 8. After the code or
codes for a run have been processed and the run has been

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1 recovered, control returns to block 162.

At a block 169, the code in the Current Code register 113 is tested to determine if it is less than or equal to the extant code of the Code Counter 123.

5 (Only "less than" testing is used because of the previous testing of blocks 166 and 167). If Current Code is less than Code Counter, the YES branch from block 169 is taken to a sequence of blocks 180-185. If Current Code is equal to Code Counter, the NO branch from the block 169
10 is taken to a sequence of blocks 190 and 191. It is appreciated that the blocks 180-185 represent well-known normal LZW data decompression processing and that the blocks 190 and 191 represent well-known exception case LZW data decompression processing (e.g. see patent
15 4,558,302).

At the block 180, the data character string corresponding to the code in the Current Code register 113 is provided by the decompressor 110 at the output 112 thereof.

20 At the block 181, the Dictionary 135 is updated by storing an extended string comprising the string corresponding to the code in the Previous Code register 114 extended by the first character of the string corresponding to the code in the Current Code register
25 123. This stored extended string is assigned the string code value of the extant code of the Code Counter 123. In conventional LZW implementations, the code in the Previous Code register 114, together with the extension character, is stored in Dictionary 135 at a location
30 designated by the code assigned by the Code Counter 123.

At blocks 182-184, the Code Counter 123 is advanced by 1 and a Code Size increment is effected if required. If a Code Size increase is not required, the test of block 182 results in by-passing the Code Size
35 incrementation block 183. The Code Size register 115 is utilized in this process. The incrementation of the Code Counter 123 to the next code is performed at the

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1 block 184.

At the block 185, the code in the Current Code register 113 is transferred to the Previous Code register 114. In conventional LZW data decompression, the Previous Code set into the Previous Code register 114 at the block 185 is utilized in the following LZW data decompression cycle in the dictionary updating function of block 181. In the run processing of the present invention, this Previous Code is utilized to define the run character in a manner to be explained with respect to Figure 8. Control from the block 185 is returned to the block 165.

If LZW exception case processing is required, the NO branch from the block 169 is taken to the block 190 whereat the string corresponding to the code in the Previous Code register 114 is extended by the first character of this string and is provided at the output 112 of the decompressor 110. At the block 191, this extended string of the block 190 is stored in the Dictionary 135 with an assigned code of the code in the Code Counter 123. Control then continues with the block 182 as previously described.

The blocks 160-165, 169, 180-185 and 190-191 of Figure 7 comprise the processing performed by a conventional LZW data decompressor. Numerous implementations are known for performing the functions of these blocks (e.g. see patent 4,558,302).

The blocks 166-168 comprise decompression run processing in accordance with the present invention embedded in a conventional LZW decompressor.

It is appreciated in Figure 7 that the conventional LZW processing of blocks 180-185 and 190-191 return processing to the block 165 to fetch the next code to the Current Code register 113. In distinction to this, the run processing of block 168 returns processing to the block 162. This is to effectively re-initialize the Previous Code register 114 at block 164 after a run has been processed so that the

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1 decompressor 110 continues to remain synchronized with
the output from the compressor 10.

Referring to Figure 8, with continued reference
to Figures 5-7, details of the run processing block 168
5 of Figure 7 are illustrated. If, as discussed above
with respect to blocks 166 and 167 of Figure 7, the code
in the Current Code register 113 is not equal to a
Reserved Code but is greater than the extant code in
the Code Counter 123, control transfers from the block
10 167 of Figure 7 to a block 200 of Figure 8. At the block
200, the extant code in the Code Counter 123 is subtracted
from the code in the Current Code register 113 and the
result is set into the Count register 117. At a block
201, the decompressor 110 repeatedly provides, at its
15 output 112, the character residing in the Previous Code
register 114 a number of times equal to the number in
the Count register 117. In this manner, the decompressor
110 recovers the data character run that was compressed
by the compressor 10. Control then returns to block
20 162 of Figure 7.

If the input code in the Current Code register
113 is equal to a Reserved Code indicated in the Count
Increase Table 125 of Figure 6, control transfers from
the block 166 of Figure 7 to a block 202 of Figure 8.
25 At the block 202, the next input code is fetched to the
Count register 117 using the system maximum Code Size.
At a block 203, a test is executed to determine if the
Current Code is equal to the first Reserved Code value.
For the described embodiment, the first Reserved Code,
30 as indicated in Figure 6, is 257. If at the block 203,
Current Code is equal to the first Reserved Code, control
transfers to the block 201 and the associated data
character run is recovered as previously described.

If, however, at the block 203, the Current Code
35 is not equal to the first Reserved Code, control transfers
to a block 204 whereat the Count in the Count register
117 is increased by the selected predetermined process

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1 corresponding to the further Reserved Code value in the
Current Code register 113. As previously described,
the Count Increase Table 125, as detailed in Figure 6,
illustrates the specific predetermined processes 150-153
5 corresponding to the Reserved Codes 258-261, respectively.
Depending on the Reserved Code that is received, the
Count is increased as illustrated. Thereafter, processing
continues with the block 201, as previously described,
to recover the associated data character run.

10 It is appreciated, as previously described, that
for the illustrated embodiment, a run of 20479 characters
can be accommodated. Longer runs can be accommodated
by the decompressor 110 simply by adding further lines
to the Count Increase Table 125 of Figure 6. Of course,
15 corresponding further lines would be added to the Count
Reduction Table 25 of Figure 2 as previously explained.

It is appreciated that the functionality of the
blocks 200, 203 and 204 of Figure 8 is performed by the
count increase logic 127 of Figure 5 using the Count
20 register 117, the Code Counter 123 and the Count Increase
Table 125 of Figure 5.

In all of the run processing described above,
it is appreciated that the run character is transmitted
at compressor block 80 of Figure 4 and, at the
25 decompressor, conveniently resides in the Previous Code
register 114 as the result of the processing of block
185 of Figure 7.

With continued reference to Figures 2, 4, 6,
7 and 8, it is appreciated that whatever the run
30 processing that is applied by the compressor (Figures
2 and 4), it is reversed by the decompressor run
processing (Figures 6 and 8) so that the original run
input data is recovered.

The compressor processing of blocks 90-92 of
35 Figure 4 is reversed by blocks 167, 200 and 201 of Figures
7 and 8. In this aspect of the invention, the Count
of the run is transmitted by the processing of blocks

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1 91 and 92. The sum of the run count and the extant code
of the compressor code counter is output at block 92
and at block 200 of the decompressor processing, the
extant value of the decompressor code counter is
5 subtracted from the received code to recover the run
count. The decompressor recognizes this character run
condition by detecting, at block 167, that the received
code is greater than the extant code of the decompressor
code counter. Using this processing of the present
10 invention, it is not necessary to transmit a Reserved
Code from the compressor to the decompressor to signal
the existence of the run.

The compressor processing of blocks 93-96 of
Figure 4 is reversed by decompressor blocks 166 and
15 201-203 of Figures 7 and 8. In this case, the first
Reserved Code value is utilized to signal the decompressor
of the particular processing. The Reserved Code value
of 257 is utilized in the above-described embodiment.
In this processing, the run count is transmitted by the
20 compressor following this first Reserved Code. The
decompressor, after receiving this first Reserved Code,
utilizes the received run count to recover the character
run.

The compressor run processing of blocks 93, 97,
25 98, 95 and 96 of Figure 4 is reversed by the decompressor
processing of blocks 166 and 201-204. In the compressor
processing of blocks 97 and 98, the run count is reduced
by a selected predetermined process so that Count is
less than the system maximum code and a Reserved Code
30 is utilized that corresponds to the selected predetermined
process. The decompressor processing recognizes the
Reserved Code and, by utilizing the inverse of the
selected predetermined process, increases the received
count to the original run count value so as to recover
35 the original character run. The compressor predetermined
processes 50-53 of Figure 2 correspond, respectively,
to the decompressor predetermined processes 150-153 of

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1 Figure 6. It is observed that the decompressor
predetermined processes of Figure 6 are the inverses
of the compressor predetermined processes of Figure 2.

The above described embodiments of the invention
5 are illustrated in terms of variable code length. It
is appreciated that the above embodiments may also be
utilized in a fixed code length environment with some
readily apparent modifications. For example, a fixed
code length embodiment may utilize a fixed code size
10 of 12 bits. In this configuration, the maximum system
code would be 4096.

In a fixed code length embodiment, the Code Size
registers 15 and 115 of Figures 1 and 5 would not be
utilized. Similarly, the Code Size initialization, test
15 and incrementation of blocks 61, 67 and 68 of Figure
3, as well as corresponding blocks 161, 182 and 183 of
Figure 7 would not be required. In such an embodiment,
Maxcode would be fixed and would be equal to the fixed
system maximum code, e.g. 4096. The logic of Figures
20 3, 4, 7 and 8 would then remain the same except that
the system maximum code and the system maximum code size
would be the fixed values as discussed.

Referring to Figure 9, with continued reference
to Figures 1-4, an example of the operation of the
25 compressor 10 in accordance with the flow charts of
Figures 3 and 4, is illustrated. At the top of the
Figure, an input data character stream is shown where
sequential characters are identified by character sequence
numbers. This is done to facilitate following the
30 progress of the characters through the steps of the
example. It is appreciated that the sequence numbers
are shown for purposes of character identification and
do not appear in the actual data character stream.

The example is largely self-explanatory, with
35 the actions performed delineated in the left-hand column
and the blocks of Figures 3 and 4 that participate in
the actions designated in the right-hand column. It

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1 is noted that the run of the character "a" is 47
characters long and the run of the character "c" is 15000
characters long.

5 In actions 1-8, standard LZW data compression
is performed on the input data characters through the
character "a(5)". Several LZW compression cycles are
performed and in each cycle, as noted in the right-hand
column, the block 74 is traversed to test for a character
run. With the block 74 positioned in the processing
10 as illustrated in Figure 3, all strings that exist in
the Dictionary 35 will be matched in the block 64 of
Figure 3 prior to invoking run processing at the block
74. Therefore, the LZW processing is taking precedence
over the run processing.

15 In action 8, block 74 of Figure 3 recognizes
that the Current Character "a(5)" is the same as the
next n look-ahead characters as observed in the input
data character stream at the top of the Figure. Control
then proceeds to the block 75 for run processing. It
20 is appreciated that even though the illustrated run of
the character "a" begins with "a(4)", the character "a(4)"
was absorbed into the LZW processing at action 6.

In action 9, the character "a(5)" is output
pursuant to the block 80 of Figure 4 and the run counting
25 begins with character "a(6)". The loop comprised of
the blocks 82-86 of Figure 4 counts the characters and
at action 12 the mismatching character "c(1)" is fetched
stopping the count at 45 as illustrated. In action 12,
the block 90 of Figure 4 determines that the count of
30 45 in the Count register 17 of Figure 1 is less than
the difference between Maxcode and the code of 266 in
the Code Counter 23.

In action 13, blocks 91 and 92 of Figure 4 add
the code counter value of 266 with the count value of
35 45 to provide a Count of 311 which is output. Control
then returns to block 76 of Figure 3 to resume the LZW
processing wherein the next character "c(2)" is fetched

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1 and the Dictionary is updated as illustrated.

In actions 14-18, the 15000 character run of the data character "c" is processed. In action 18, the blocks 90 and 93 of Figure 4 direct the processing to the blocks 97 and 98 thereof. In action 19, the count of 14998 is reduced to a count of 2710 by utilizing the process 52 of Figure 2. The corresponding Reserved Code of 260 is set into the Reserved Code register 22 of Figure 1 as illustrated. This code is then output at the block 95 of Figure 4, as illustrated in action 19, followed by the reduced count of 2710 at action 20. The block 96 of Figure 4 depicts the outputting of the Count.

In actions 20-22, processing returns to LZW data compression at the block 76 of Figure 3.

15 More detailed descriptions of the actions of Figure 9 relative to the blocks of Figures 3 and 4 are readily apparent and will not be provided for brevity.

Referring to Figure 10, with continued reference to Figures 5, 6, 7 and 8, an example of the operation of the decompressor 110 in accordance with the flow charts of Figures 7 and 8 is illustrated. The format of Figure 10 is generally similar to that of Figure 9 and descriptions given above with respect to Figure 9 are applicable. The input compressed code stream at the top of Figure 10 is the compressor output illustrated in Figure 9. It is observed that the output of Figure 10 is the recovered data character stream illustrated at the top of Figure 9.

In actions 1-5, conventional LZW decompression is performed recovering the original data character stream through character "a(5)". It is noted that LZW exception case processing is performed at action 4 where the received Current Code is equal to the decompressor Code Counter (NO branch of block 169 of Figure 7).

35 At action 6, the run of the character "a" is processed in response to receiving the code 311. In this case, the received compressed code is greater than

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1 the value 266 in the decompressor Code Counter. The
block 167 of Figure 7 directs processing to the blocks
200 and 201 of Figure 8 to perform the recovery of the
run characters. In actions 7 and 8, control returns
5 to LZW processing at block 162 of Figure 7 to detect
the beginning of the run of the character "c".

In actions 9 and 10, the run of the character
"c" is processed. In action 9, the Reserved Code 260
is received as detected at block 166 of Figure 7 and
10 the run processing of blocks 201-204 of Figure 8 is
invoked. In action 9, the Count of 2710 is received
and in action 10 converted to the run count of 14998.
The conversion is performed at block 204 of Figure 8
using the process 152 of Figure 6.

15 In actions 11-13, conventional LZW decompression
decodes the remainder of the input compressed code stream.

More detailed descriptions of the actions of
Figure 10 relative to the blocks of Figures 7 and 8 are
readily apparent and will not be provided for brevity.

20 As appreciated from Figure 3, the run detection
of block 74 and the run processing of block 75 is
interposed in the LZW data compression cycle of Figure
3 at the point in the LZW cycle where the longest match
has been output, the Dictionary has been updated with
25 the extended string and the character that caused the
mismatch has been fetched and resides in the Current
Character register. In this manner, full compression
advantage is obtained with respect to strings already
stored in the Dictionary. If the mismatching character
30 should begin a run, this character is output at block
80 of Figure 4 permitting the decompressor Dictionary
to store the same extended string as stored in the
compressor Dictionary. When the run processing of Figure
4 is concluded, the mismatching character following the
35 run is in the Current Character register and is then
available at the block 76 of Figure 3 to continue the
LZW processing from this point. Thus, at the block 76

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1 of Figure 3, the Current Match register utilized in the
LZW process either receives the mismatching character
from the LZW processing of the blocks 60-70 or from the
run processing block 75.

5 It is appreciated that the predetermined processes
of Figures 2 and 6 utilize subtraction and addition to
decrease and increase the Count, respectively. Other
procedures may be utilized in the context of the present
invention to process long runs. For example, other
10 mathematical procedures with greater number reducing
and increasing capabilities than subtraction and addition
may be utilized. Multiplication, division, exponentiation
and hashing techniques may be employed to provide this
capability.

15 It is understood that the protocols utilized
in the compressor 10 and the decompressor 110 should
be compatible with respect to each other. The compressor
and decompressor should operate over the same alphabet
size and initial conditions such as Code Size. The above-
20 described compressor and decompressor embodiment can
readily be utilized with dictionaries that are either
not initialized or are initialized with all of the single
character strings. As described above, single characters
can be distinguished from compressed codes by the
25 respective values thereof. The single characters can
be represented by the values of the characters themselves
or by any other well-known coding scheme. The single
character protocol that is used in the compressor should
also be utilized in the decompressor.

30 It is appreciated that the input to the compressor
can be over any size alphabet having any corresponding
character bit size. For example, the data characters
can be textual, such as ASCII characters, over an
alphabet, such as the 256 character ASCII alphabet of
35 8-bit characters. The input data can also be binary
characters over the two character binary alphabet 1 and
0 having a 1-bit sized character. It is appreciated

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1 that textual data can also be compressed over the two
character alphabet of the underlying binary data.

It is appreciated that the above-described
embodiment of the invention may be implemented in
5 hardware, firmware, software or a combination thereof.
Discrete circuit components may readily be implemented
for performing the various described functions. In a
software embodiment, appropriate modules, programmed
with coding readily generated from the above-described
10 flow charts, may be utilized.

While the invention has been described in its
preferred embodiments, it is to be understood that the
words which have been used are words of description rather
than of limitation and that changes may be made within
15 the purview of the appended claims without departing
from the true scope and spirit of the invention in its
broader aspects.

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CLAIMS

- 1 1. A data compression method for compressing an
input stream of data characters into an output stream
of compressed codes, said method including an LZW data
compression process, said LZW data compression process
5 including storing strings of data characters, assigning
respective codes to said stored strings from a code
counter and incrementing said code counter for each said
stored string, said method comprising:
detecting when a run of data characters is
10 occurring in said input stream by detecting when a
predetermined number of adjacent data characters of said
input stream are the same with respect to each other,
counting data characters in said detected run
to provide a run count,
15 providing a modified code by combining the
existing code in said code counter with said run count,
using said LZW data compression process to
compress said input stream when a run is not occurring
therein by comparing said input stream to said stored
20 strings to determine longest matches therewith and
providing said codes assigned thereto, thereby providing
LZW compressed codes, and
outputting said modified code and said LZW
compressed codes so as to provide said output stream.
25
2. The method of claim 1 wherein said providing
step comprises providing said modified code so that when
said modified code is received by an LZW data
decompression process, said run count may be recovered
30 by combining the received modified code with the existing
code in the code counter used in said LZW data
decompression process.

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1 3. The method of claim 1 wherein said outputting
step further comprises

outputting the data character of said detected
run prior to said modified code.

5

4. The method of claim 1 wherein

said steps of detecting when a run of data
characters is occurring, counting data characters in
said detected run, providing a modified code and

10 outputting said modified code comprises run processing,
said storing step of said LZW data compression
process comprises storing extended strings, each
comprising a longest match extended by the next following
data character in said input stream,

15 said method further including

performing said run processing during said step
of using said LZW data compression process after
determining a longest match, storing the extended string
corresponding thereto and providing the code assigned

20 to said longest match.

5. The method of claim 2 wherein said step of
providing a modified code comprises

providing said modified code by adding said run
25 count to said existing code in said code counter of said
LZW data compression process.

6. The method of claim 5 wherein said run count
is recovered by subtracting said existing code in said

30 code counter of said LZW data decompression process from
said received modified code.

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1 7. The method of claim 4 wherein said LZW data
compression process determines said longest match by
fetching said next following data character in said input
stream thereby resulting in a mismatch with said stored
5 strings, said fetched input data character being a
mismatching character,

said performing step further comprises performing
said run processing beginning with said mismatching
character, and

10 said detecting step further comprises detecting
when said run is occurring by detecting when said
predetermined number of said adjacent data characters
are the same as said mismatching character.

15 8. The method of claim 7 wherein said step of
outputting further comprises outputting the data character
of said detected run prior to said modified code,
said data character of said detected run
comprising said mismatching character.

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- 1 9. A data compression method for compressing an
input stream of data characters into an output stream
of compressed codes, said method including an LZW data
compression process, said LZW data compression process
5 including storing strings of data characters, assigning
respective codes to said stored strings from a code
counter and incrementing said code counter for each said
stored string, said method comprising:
detecting when a run of data characters is
10 occurring in said input stream by detecting when a
predetermined number of adjacent data characters of said
input stream are the same with respect to each other,
counting data characters in said detected run
to provide a run count,
15 providing a reduced count by reducing said run
count to less than a predetermined number by using a
selected predetermined process,
providing a reserved code corresponding to said
selected predetermined process,
20 using said LZW data compression process to
compress said input stream when a run is not occurring
therein by comparing said input stream to said stored
strings to determine longest matches therewith and
providing said codes assigned thereto, thereby providing
25 LZW compressed codes, and
outputting said reserved code, said reduced count
and said LZW compressed codes so as to provide said output
stream.
- 30 10. The method of claim 9 wherein said providing
steps comprise providing said reserved code and said
reduced count so that when said reserved code and said
reduced count are received by an LZW data decompression
process, said run count may be recovered by increasing
35 said received reduced count by using the inverse of said
selected predetermined process.

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1 11. The method of claim 9 wherein said outputting
step comprises

outputting the data character of said detected
run prior to said reserved code.

5

12. The method of claim 9 wherein said steps of
detecting when a run of data characters is occurring,
counting data characters in said detected run, providing
a reduced count, providing a reserved code and outputting
10 said reserved code and said reduced count comprises run
processing,

said storing step of said LZW data compression
process comprises storing extended strings, each
comprising a longest match extended by the next following
15 data character in said input stream,

said method further including
performing said run processing during said step
of using said LZW data compression process after
determining a longest match, storing the extended string
20 corresponding thereto and providing the code assigned
to said longest match.

13. The method of claim 10 wherein said selected
predetermined process comprises subtracting a
25 predetermined constant from said run count so as to reduce
said run count to less than said predetermined number,
said reserved code corresponding to said
predetermined constant.

30 14. The method of claim 13 wherein said run count
is recovered by adding said predetermined constant
corresponding to said received reserved code to said
received reduced count.

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1 15. The method of claim 12 wherein said LZW data
compression process determines said longest match by
fetching said next following data character in said input
stream thereby resulting in a mismatch with said stored
5 strings, said fetched input data character being a
mismatching character,

said performing step further comprises performing
said run processing beginning with said mismatching
character, and

10 said detecting step further comprises detecting
when said run is occurring by detecting when said
predetermined number of said adjacent data characters
are the same as said mismatching character.

15 16. The method of claim 15 wherein said step of
outputting further comprises outputting the data character
of said detected run prior to said reserved code,
said data character of said detected run
comprising said mismatching character.

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1 17. A data decompression method for decompressing
an input stream of compressed codes to recover an output
stream of data characters corresponding thereto, said
method including an LZW data decompression process, said
5 LZW data decompression process including storing strings
of data characters, assigning respective codes to said
stored strings from a code counter and incrementing said
code counter for each said stored string, said method
comprising:

10 comparing a received input compressed code to
the existing code in said code counter to determine if
said received input compressed code represents a run
count,
recovering said run count by combining said
15 received input compressed code with said existing code
in said code counter,
repeatedly providing the data character
represented by the compressed code received prior to
said received input compressed code, said data character
20 being repeatedly provided a number of times corresponding
to said recovered run count, thereby providing a recovered
run,
using said LZW data decompression process to
provide said stored strings corresponding to received
25 compressed codes when said received compressed codes
do not denote run counts, thereby providing LZW recovered
strings, and
outputting said recovered run and said LZW
recovered strings so as to provide said output stream.
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1 18. The method of claim 17 wherein said comparing
step comprises

comparing said received input compressed code
to said existing code in said code counter to determine
5 if said received input compressed code is greater than
said existing code in said code counter, thereby
determining that said received input compressed code
represents a run count.

10 19. The method of claim 17 wherein said recovering
step comprises

recovering said run count by subtracting said
existing code in said code counter from said received
input compressed code, thereby providing said recovered
15 run count.

20. The method of claim 17 wherein said storing step
of said LZW data decompression process comprises storing
extended strings,

20 said storing step including storing an extended
string that is extended by said data character represented
by said prior received compressed code.

21. The method of claim 17 wherein
25 said steps of comparing a received input
compressed code, recovering said run count, repeatedly
providing the data character and outputting said recovered
run comprises run processing,

said LZW data decompression process includes
30 an initial processing point at which a first compressed
code is fetched,

said method further including
returning to said initial processing point after
performing said run processing.

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- 1 22. A data decompression method for decompressing
an input stream of compressed codes to recover an output
stream of data characters corresponding thereto, said
method including an LZW data decompression process, said
5 LZW data decompression process including storing strings
of data characters, assigning respective codes to said
stored strings from a code counter and incrementing said
code counter for each said stored string, said method
comprising:
- 10 determining if a received input compressed code
is equal to a reserved code, said reserved code denoting
that a run count will follow that has been reduced by
a selected predetermined process corresponding to said
received reserved code,
- 15 fetching said reduced run count,
recovering said run count by increasing said
fetched reduced run count by using the inverse of said
selected predetermined process corresponding to said
received reserved code,
- 20 repeatedly providing the data character
represented by the compressed code received prior to
said received reserved code, said data character being
repeatedly provided a number of times corresponding to
said recovered run count, thereby providing a recovered
25 run,
- using said LZW data decompression process to
provide said stored strings corresponding to received
compressed codes when said received compressed codes
do not denote run counts, thereby providing LZW recovered
30 strings, and
- outputting said recovered run and said LZW
recovered strings so as to provide said output stream.

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1 23. The method of claim 22 wherein said selected
predetermined process comprises subtracting a
predetermined constant corresponding to said reserved
code from said run count, thereby providing said reduced
5 run count.

24. The method of claim 23 wherein said recovering
step comprises
recovering said run count by adding said
10 predetermined constant corresponding to said received
reserved code to said fetched reduced run count.

25. The method of claim 22 wherein said storing step
of said LZW data decompression process comprises storing
15 extended strings,
said storing step including storing an extended
string that is extended by said data character represented
by said prior received compressed code.

20 26. The method of claim 22 wherein
said steps of determining if a received input
compressed code is equal to a reserved code, fetching
said reduced run count, recovering said run count,
repeatedly providing the data character and outputting
25 said recovered run comprises run processing,
said LZW data decompression process includes
an initial processing point at which a first compressed
code is fetched,
said method further including
30 returning to said initial processing point after
performing said run processing.

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1 27. Data compression apparatus for compressing an
input stream of data characters into an output stream
of compressed codes, said apparatus including an LZW
data compressor, said LZW data compressor including means
5 for storing strings of data characters, a code counter
for assigning respective codes to said stored strings
and means for incrementing said code counter for each
said stored string, said apparatus comprising:

means for detecting when a run of data characters
10 is occurring in said input stream by detecting when a
predetermined number of adjacent data characters of said
input stream are the same with respect to each other,

means for counting data characters in said
detected run to provide a run count,

15 means for providing a modified code by combining
the existing code in said code counter with said run
count,

said LZW data compressor being operative to
compress said input stream when a run is not occurring
20 therein by comparing said input stream to said stored
strings to determine longest matches therewith and
providing said codes assigned thereto, thereby providing
LZW compressed codes, and

means for outputting said modified code and said
25 LZW compressed codes so as to provide said output stream.

28. The apparatus of claim 27 wherein said means
for providing comprises means for providing said modified
code so that when said modified code is received by an
30 LZW data decompressor, said run count may be recovered
by combining the received modified code with the existing
code in the code counter in said LZW data decompressor.

29. The apparatus of claim 27 wherein said means
35 for outputting further comprises

means for outputting the data character of said
detected run prior to said modified code.

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1 30. The apparatus of claim 27 wherein

said means for detecting when a run of data
characters is occurring, said means for counting data
characters in said detected run, said means for providing
5 a modified code and said means for outputting said
modified code comprise means for performing run
processing,

said means for storing included in said LZW data
compressor comprises means for storing extended strings,
10 each comprising a longest match extended by the next
following data character in said input stream,

said means for performing being operative in
performing said run processing after said LZW data
compressor determines a longest match, stores the extended
15 string corresponding thereto and provides the code
assigned to said longest match.

31. The apparatus of claim 28 wherein said means
for providing a modified code comprises

20 means for providing said modified code by adding
said run count to said existing code in said code counter
of said LZW data compressor.

32. The apparatus of claim 31 wherein said run count
25 is recovered by subtracting said existing code in said
code counter of said LZW data decompressor from said
received modified code.

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1 33. The apparatus of claim 30 wherein said LZW data
compressor is operative to determine said longest match
by fetching said next following data character in said
input stream thereby resulting in a mismatch with said
5 stored strings, said fetched input data character being
a mismatching character,

said means for performing further comprises means
for performing said run processing beginning with said
mismatching character, and

10 said means for detecting further comprises means
for detecting when said run is occurring by detecting
when said predetermined number of said adjacent data
characters are the same as said mismatching character.

15 34. The apparatus of claim 33 wherein said means
for outputting further comprises means for outputting
the data character of said detected run prior to said
modified code,

said data character of said detected run
20 comprising said mismatching character.

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- 1 35. Data compression apparatus for compressing an
input stream of data characters into an output stream
of compressed codes, said apparatus including an LZW
data compressor, said LZW data compressor including means
5 for storing strings of data characters, a code counter
for assigning respective codes to said stored strings
and means for incrementing said code counter for each
said stored string, said apparatus comprising:
- means for detecting when a run of data characters
10 is occurring in said input stream by detecting when a
predetermined number of adjacent data characters of said
input stream are the same with respect to each other,
means for counting data characters in said
detected run to provide a run count,
- 15 means for providing a reduced count by reducing
said run count to less than a predetermined number by
using a selected predetermined process,
means for providing a reserved code corresponding
to said selected predetermined process,
- 20 said LZW data compressor being operative to
compress said input stream when a run is not occurring
therein by comparing said input stream to said stored
strings to determine longest matches therewith and
providing said codes assigned thereto, thereby providing
25 LZW compressed codes, and
means for outputting said reserved code, said
reduced count and said LZW compressed codes so as to
provide said output stream.
- 30 36. The apparatus of claim 35 wherein said means
for providing comprise means for providing said reserved
code and said reduced count so that when said reserved
code and said reduced count are received by an LZW data
decompressor, said run count may be recovered by
35 increasing said received reduced count by using the
inverse of said selected predetermined process.

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1 37. The apparatus of claim 35 wherein said means
for outputting comprises

means for outputting the data character of said
detected run prior to said reserved code.

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38. The apparatus of claim 35 wherein said means
for detecting when a run of data characters is occurring,
said means for counting data characters in said detected
run, said means for providing a reduced count, said means
10 for providing a reserved code and said means for
outputting said reserved code and said reduced count
comprises means for performing run processing,

said means for storing included in said LZW data
compressor comprises means for storing extended strings,
15 each comprising a longest match extended by the next
following data character in said input stream,

said means for performing being operative in
performing said run processing after said LZW data
compressor determines a longest match, stores the extended
20 string corresponding thereto and provides the code
assigned to said longest match.

39. The apparatus of claim 36 wherein said selected
predetermined process comprises subtracting a
25 predetermined constant from said run count so as to reduce
said run count to less than said predetermined number,

said reserved code corresponding to said
predetermined constant.

30 40. The apparatus of claim 39 wherein said run count
is recovered by adding said predetermined constant
corresponding to said received reserved code to said
received reduced count.

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1 41. The apparatus of claim 38 wherein said LZW data
compressor is operative to determine said longest match
by fetching said next following data character in said
input stream thereby resulting in a mismatch with said
5 stored strings, said fetched input data character being
a mismatching character,

said means for performing further comprises means
for performing said run processing beginning with said
mismatching character, and

10 said means for detecting further comprises means
for detecting when said run is occurring by detecting
when said predetermined number of said adjacent data
characters are the same as said mismatching character.

15 42. The apparatus of claim 41 wherein said means
for outputting further comprises means for outputting
the data character of said detected run prior to said
reserved code,

said data character of said detected run
20 comprising said mismatching character.

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1 43. Data decompression apparatus for decompressing
an input stream of compressed codes to recover an output
stream of data characters corresponding thereto, said
apparatus including an LZW data decompressor, said LZW
5 data decompressor including means for storing strings
of data characters, a code counter for assigning
respective codes to said stored strings and means for
incrementing said code counter for each said stored
string, said apparatus comprising:

10 means for comparing a received input compressed
code to the existing code in said code counter to
determine if said received input compressed code
represents a run count,
means for recovering said run count by combining
15 said received input compressed code with said existing
code in said code counter,
means for repeatedly providing the data character
represented by the compressed code received prior to
said received input compressed code, said data character
20 being repeatedly provided a number of times corresponding
to said recovered run count, thereby providing a recovered
run,
said LZW data decompressor being operative to
provide said stored strings corresponding to received
25 compressed codes when said received compressed codes
do not denote run counts, thereby providing LZW recovered
strings, and
means for outputting said recovered run and said
LZW recovered strings so as to provide said output stream.
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1 44. The apparatus of claim 43 wherein said means
for comparing comprises

means for comparing said received input compressed
code to said existing code in said code counter to
5 determine if said received input compressed code is
greater than said existing code in said code counter,
thereby determining that said received input compressed
code represents a run count.

10 45. The apparatus of claim 43 wherein said means
for recovering comprises

means for recovering said run count by subtracting
said existing code in said code counter from said received
input compressed code, thereby providing said recovered
15 run count.

46. The apparatus of claim 43 wherein said means
for storing included in said LZW data decompressor
comprises means for storing extended strings,

20 said means for storing comprising means for
storing an extended string that is extended by said data
character represented by said prior received compressed
code.

25 47. The apparatus of claim 43 wherein

said means for comparing a received input
compressed code, said means for recovering said run count,
said means for repeatedly providing the data character
and said means for outputting said recovered run comprises
30 means for performing run processing,

said LZW data decompressor being operative to
include an initial processing point at which a first
compressed code is fetched,

said apparatus further including
35 means for returning to said initial processing
point after performing said run processing.

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1 48. Data decompression apparatus for decompressing
an input stream of compressed codes to recover an output
stream of data characters corresponding thereto, said
apparatus including an LZW data decompressor, said LZW
5 data decompressor including means for storing strings
of data characters, a code counter for assigning
respective codes to said stored strings and means for
incrementing said code counter for each said stored
string, said apparatus comprising:

10 means for determining if a received input
compressed code is equal to a reserved code, said reserved
code denoting that a run count will follow that has been
reduced by a selected predetermined process corresponding
to said received reserved code,

15 means for fetching said reduced run count,
means for recovering said run count by increasing
said fetched reduced run count by using the inverse of
said selected predetermined process corresponding to
said received reserved code,

20 means for repeatedly providing the data character
represented by the compressed code received prior to
said received reserved code, said data character being
repeatedly provided a number of times corresponding to
said recovered run count, thereby providing a recovered
25 run,

said LZW data decompressor being operative to
provide said stored strings corresponding to received
compressed codes when said received compressed codes
do not denote run counts, thereby providing LZW recovered
30 strings, and

means for outputting said recovered run and said
LZW recovered strings so as to provide said output stream.

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1 49. The apparatus of claim 48 wherein said selected
predetermined process comprises subtracting a
predetermined constant corresponding to said reserved
code from said run count, thereby providing said reduced
5 run count.

50. The apparatus of claim 49 wherein said means
for recovering comprises
means for recovering said run count by adding
10 said predetermined constant corresponding to said received
reserved code to said fetched reduced run count.

51. The apparatus of claim 48 wherein said means
for storing included in said LZW data decompressor
15 comprises means for storing extended strings,
said means for storing comprising means for
storing an extended string that is extended by said data
character represented by said prior received compressed
code.

20 52. The apparatus of claim 48 wherein
said means for determining if a received input
compressed code is equal to a reserved code, said means
for fetching said reduced run count, said means for
25 recovering said run count, said means for repeatedly
providing the data character and said means for outputting
said recovered run comprises means for performing run
processing,

said LZW data decompressor being operative to
30 include an initial processing point at which a first
compressed code is fetched,

said apparatus further including
means for returning to said initial processing
point after performing said run processing.

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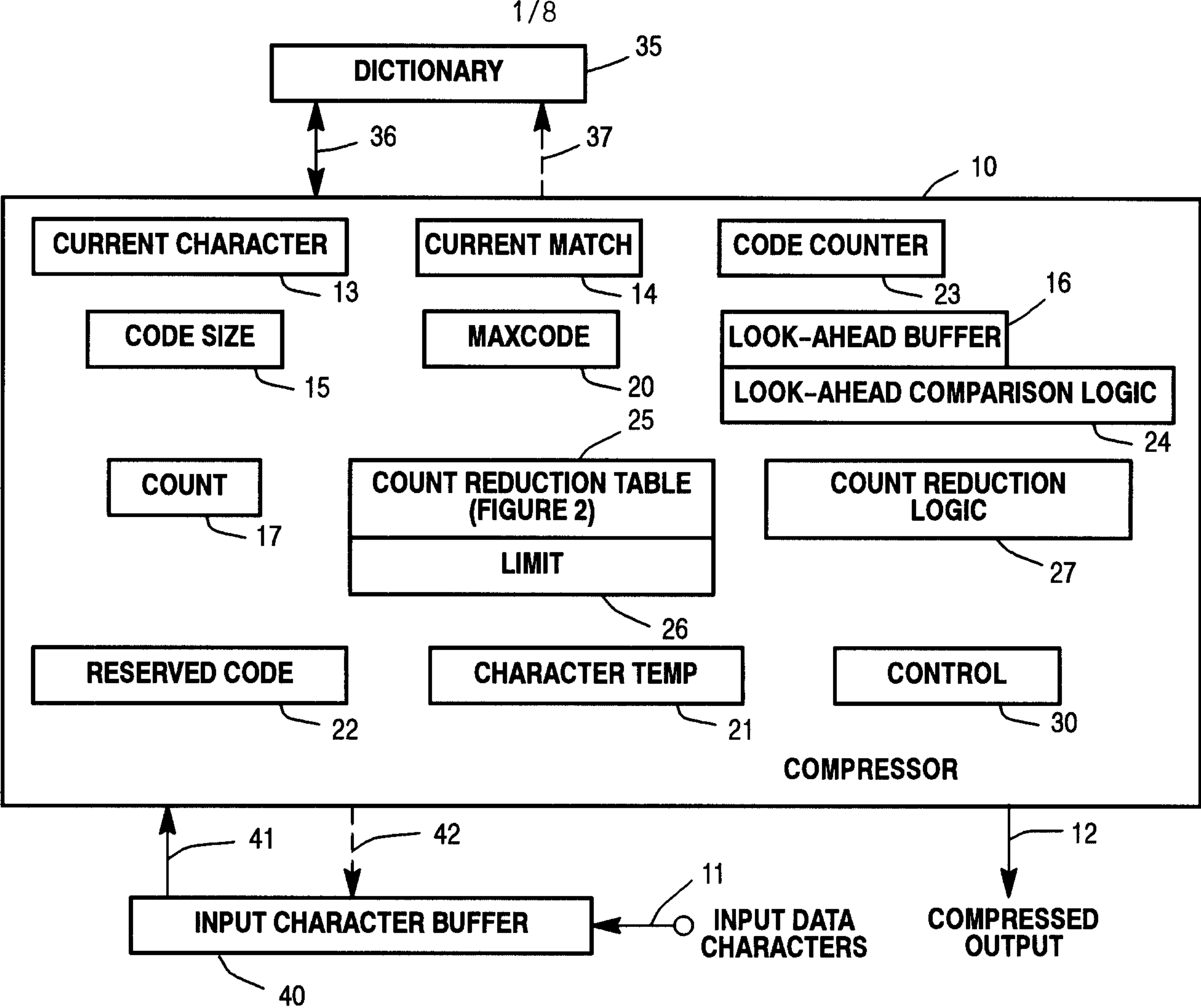


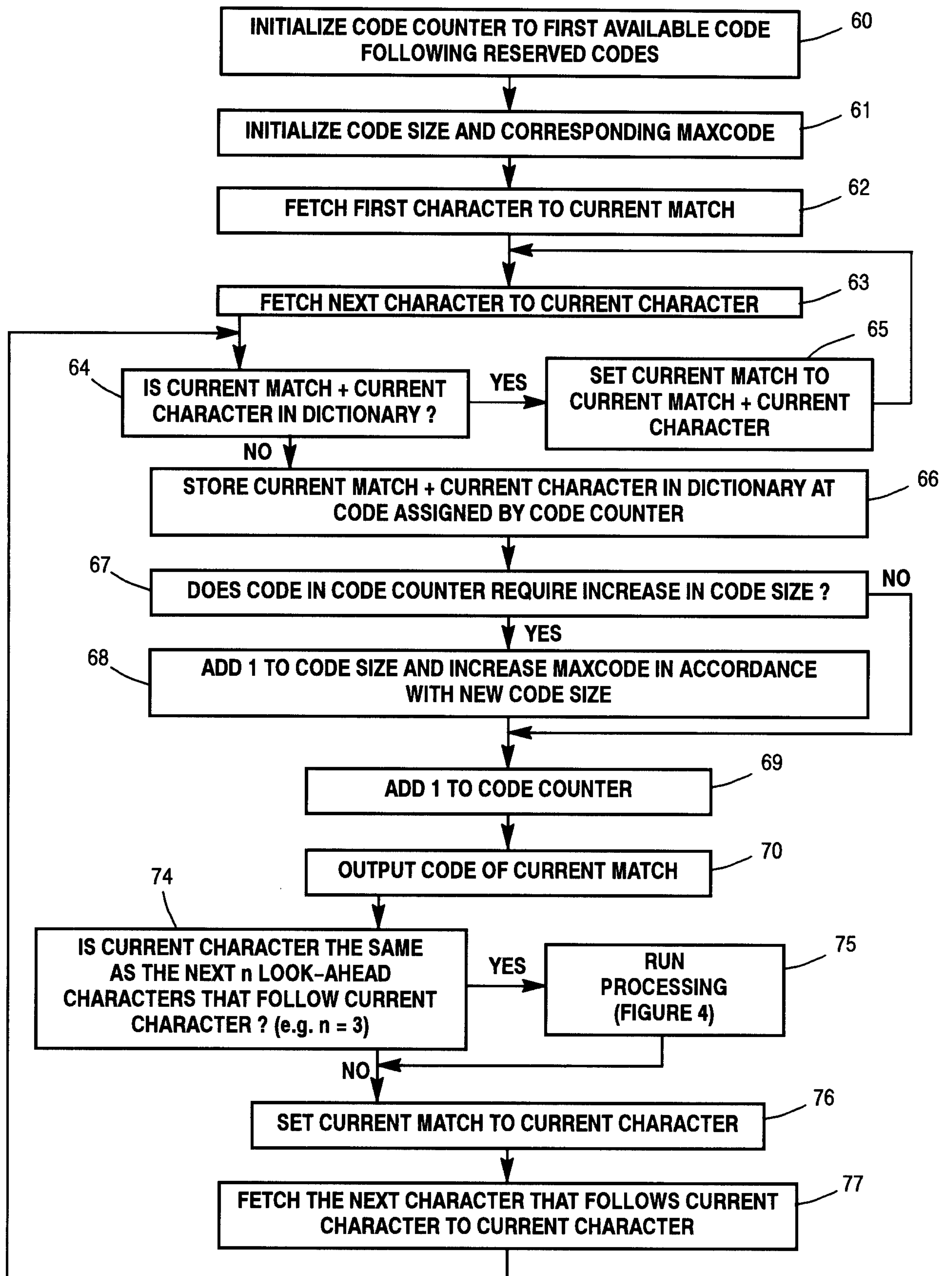
Figure 1

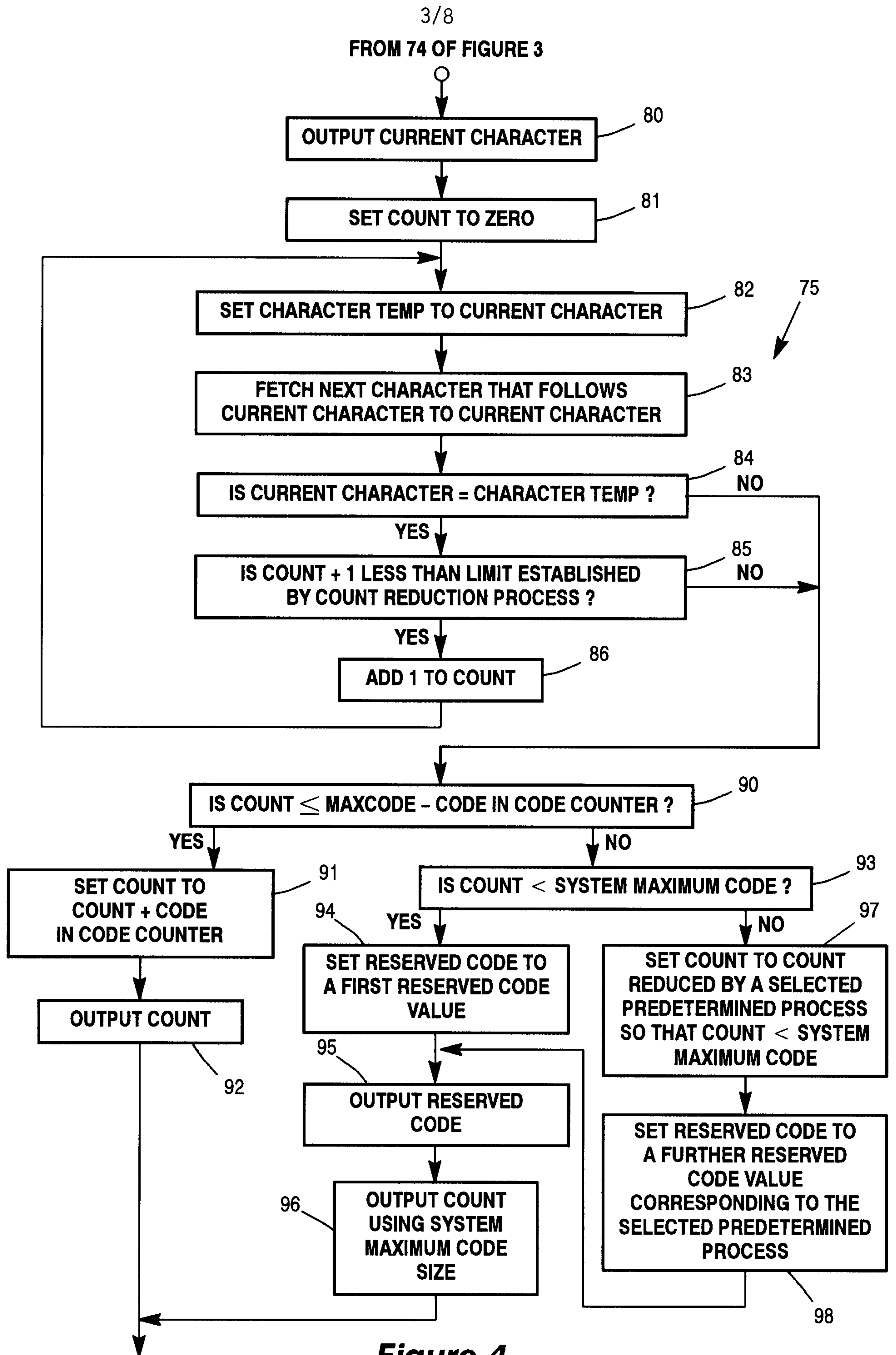
25

COUNT	DECIMAL VALUE OF UPPER LIMIT	REDUCED COUNT	RESERVED CODE
COUNT < 2 ¹²	4096	-----	257
2 ¹² ≤ COUNT < 2x2 ¹²	8192	COUNT - 2 ¹²	258
2x2 ¹² ≤ COUNT < 3x2 ¹²	12288	COUNT - 2x2 ¹²	259
3x2 ¹² ≤ COUNT < 4x2 ¹²	16384	COUNT - 3x2 ¹²	260
4x2 ¹² ≤ COUNT < 5x2 ¹²	20480	COUNT - 4x2 ¹²	261
LIMIT = 5x2 ¹² = 20480 CHARACTERS			

Figure 2

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**Figure 3**



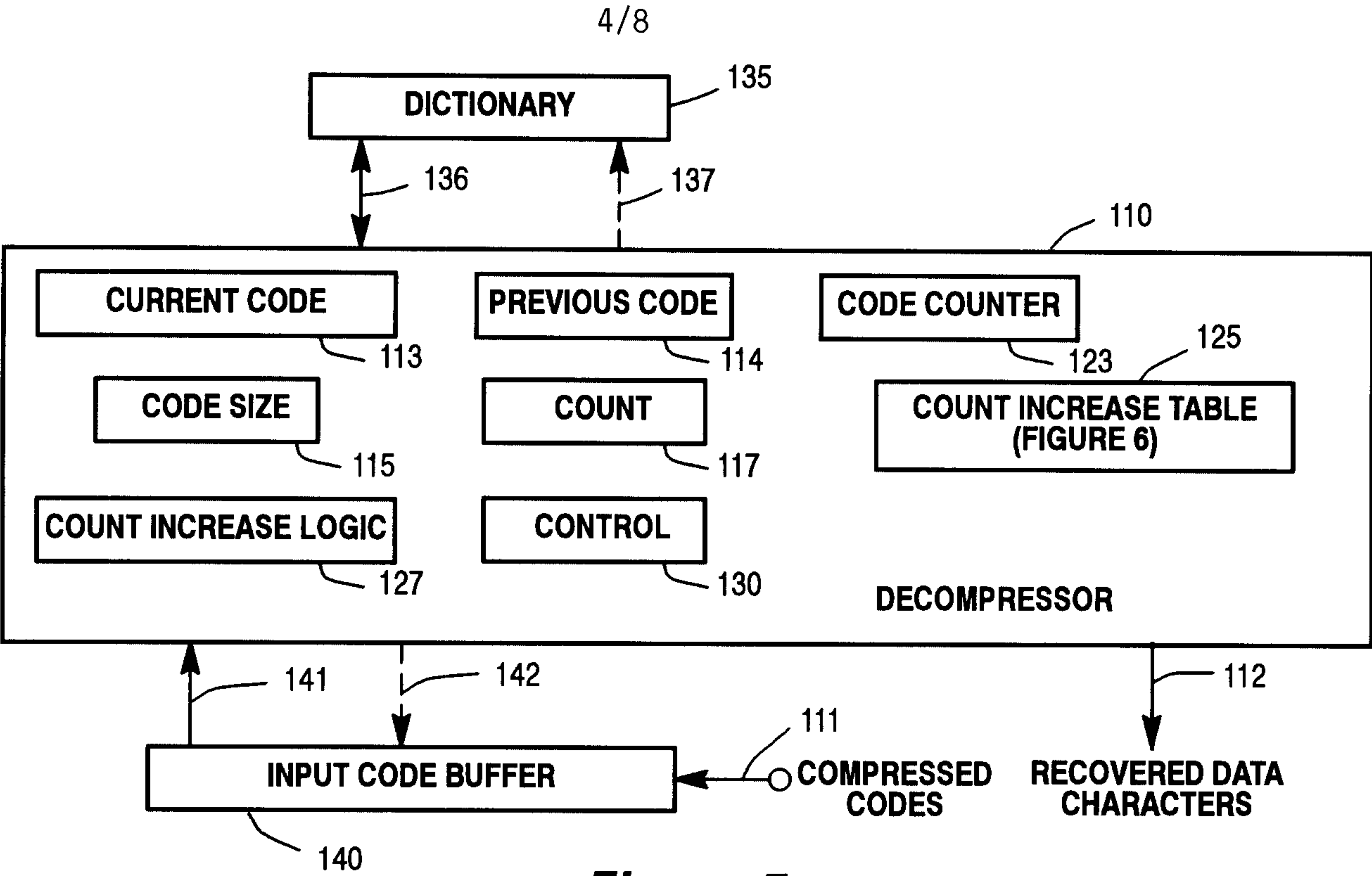
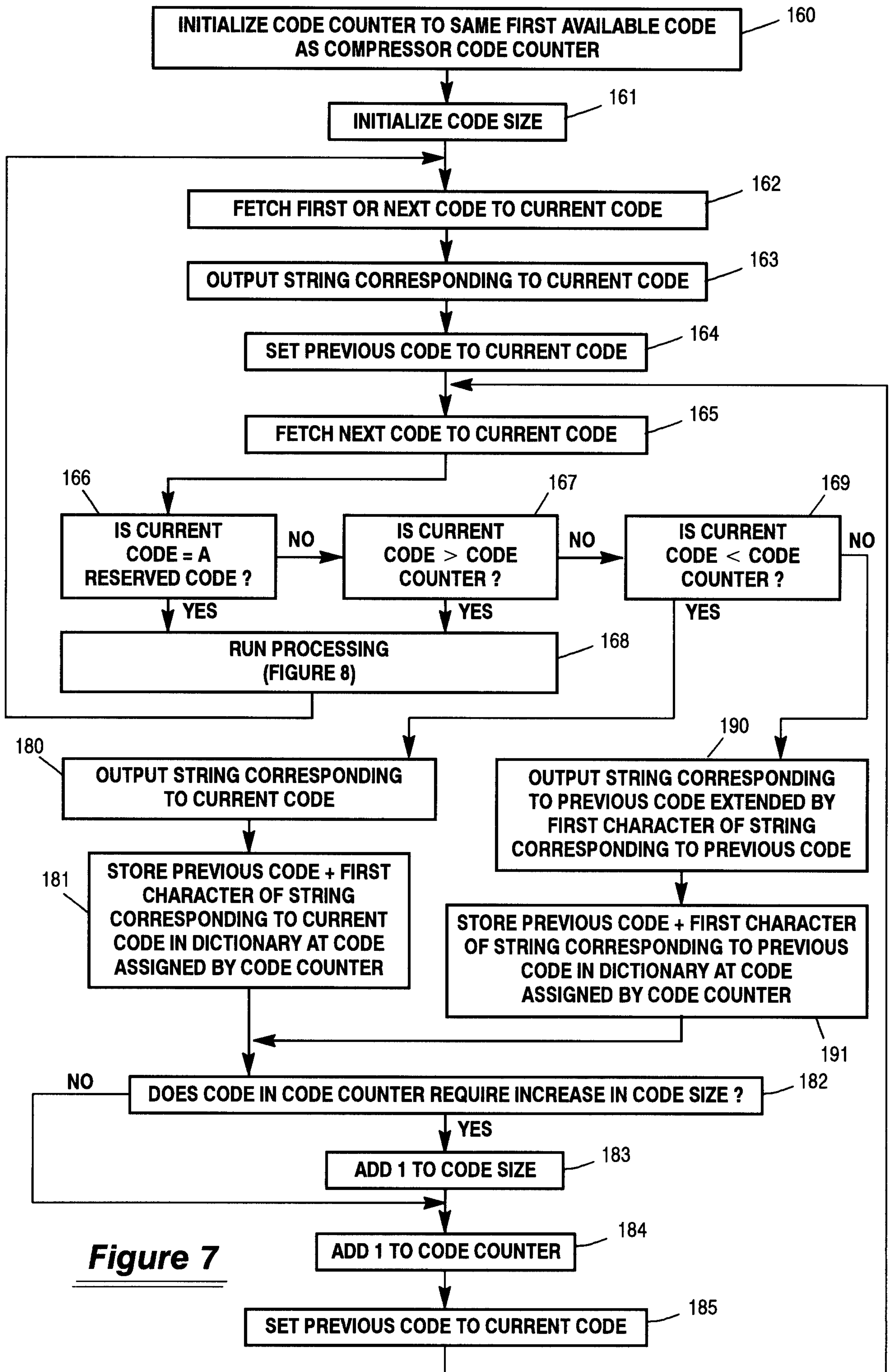


Figure 5

125	
RESERVED CODE	INCREASED COUNT
257	-----
258	COUNT + 2 ¹²
259	COUNT + 2x2 ¹²
260	COUNT + 3x2 ¹²
261	COUNT + 4x2 ¹²

Figure 6

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**Figure 7**

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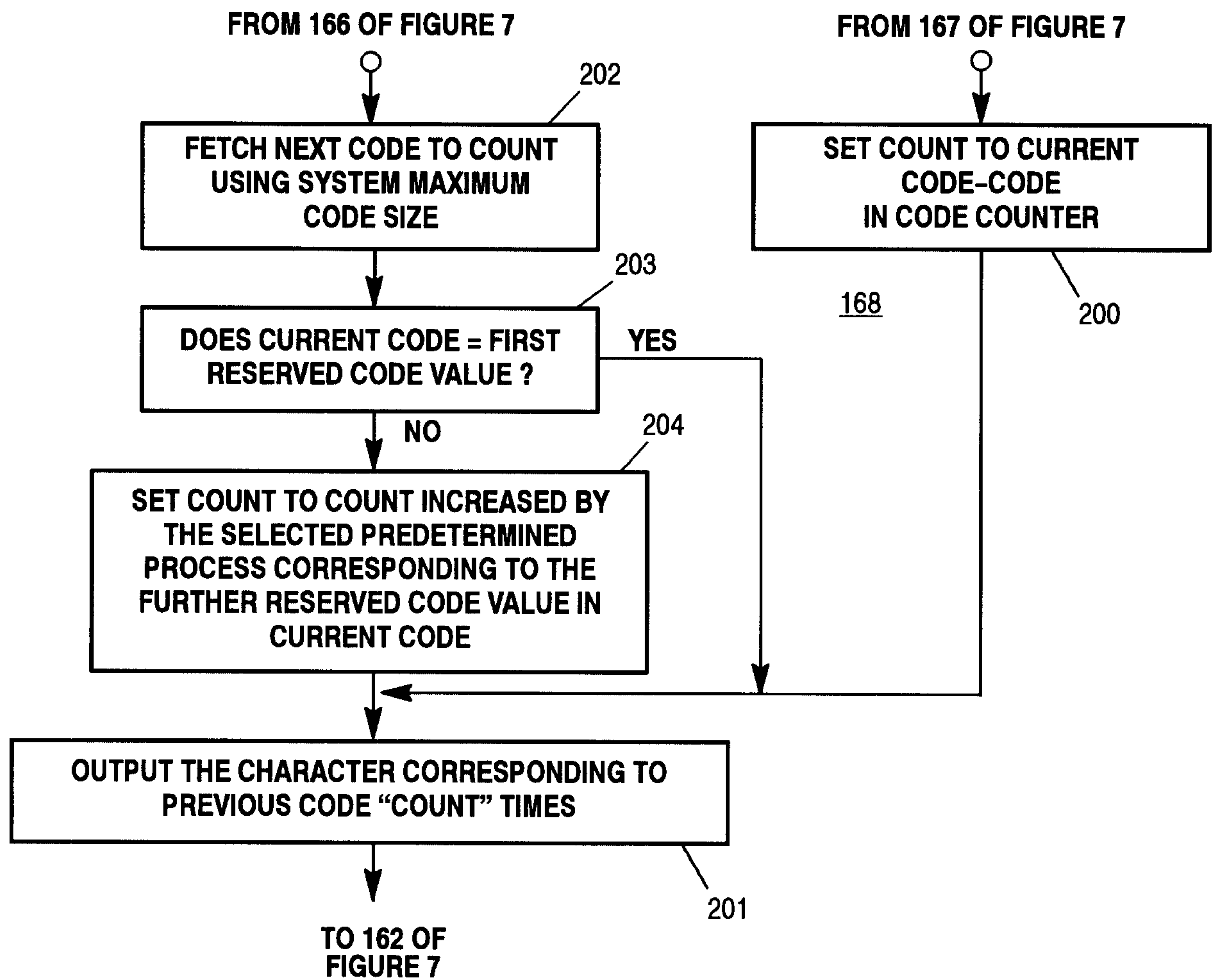


Figure 8
RUN PROCESSING

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INPUT DATA CHARACTER STREAM

a₁ b₁ a₂ b₂ a₃ b₃ a₄ a₅ a₆ a₅₀ c₁ c₂ c₁₅₀₀₀ d e x

ACT- IONS	CURR MATCH	CURRENT CHARACT	CODE CNTR	DICT		OUT- PUT	CHARACT TEMP	RESVD CODE	COUNT	BLOCKS OF FIGS. 3 & 4
				CODE	CHAR					
1	a ₁	b ₁	262	a ₁	b ₁					60-64,66
2	b ₁	a ₂	263	b ₁	a ₂	a ₁				69,70,74,76, 77,64,66
3	a ₂	b ₂	264			b ₁				69,70,74,76,77
4	262	a ₃		262	a ₃					64,65,63,66
5	a ₃	b ₃	265			262				69,70,74,76,77
6	262	a ₄								64,65,63
7	264	a ₅		264	a ₅					64,65,63,66
8			266			264				69,70,74,75
9		a ₆				a ₅	a ₅		0	80-85
10		a ₇					a ₆		1	86,82-85
		86,82-85
11		a ₅₀					a ₄₉		44	86,82-85
12		c ₁					a ₅₀		45	86,82-84,90
13	c ₁	c ₂		c ₁	c ₂	311			311	91,92,76,77, 64,66
14			267			c ₁				69,70,74,75
15		c ₃				c ₂	c ₂		0	80-85
16		c ₄					c ₃		1	86,82-85
		86,82-85
17		c ₁₅₀₀₀					c ₁₄₉₉₉		14997	86,82-85
18		d					c ₁₅₀₀₀		14998	86,82-84,90,93
19						260		260	2710	97,98,95
20	d	e		d	e	2710				96,76,77,64,66
21	e	x	268	e	x	d				69,70,74,76, 77,64,66
22	x		269			e				69,70,74,76

Figure 9

INPUT COMPRESSED CODE STREAM
a₁ b₁ 262 264 a₅ 311 c₁ c₂ 260 2710 d e

ACTIONS	PREVIOUS CODE	CURRENT CODE	CODE COUNTER	DICTIONARY		COUNT	OUTPUT	BLOCKS OF FIGS. 7 & 8
				CODE	CHAR			
1	a ₁	a ₁	262				a ₁	160-164
2		b ₁		a ₁	b ₁		b ₁	165,169,180,181
3	b ₁	262	263	b ₁	a ₁		a ₁ b ₁	184,185,165,169,180,181
4	262	264	264	262	a ₁		a ₁ b ₁ a ₁	184,185,165,190,191
5	264	a ₅	265	264	a ₅		a ₅	184,185,165,169,180,181
6	a ₅	311	266			45	a ₆ -a ₅₀	184,185,165,167,200,201
7	c ₁	c ₁					c ₁	162-164
8		c ₂		c ₁	c ₂		c ₂	165,169,180,181
9	c ₂	260	267			2710		184,185,165,166,202,203
10						14998	c ₃ -c ₁₅₀₀₀	204,201
11	d	d					d	162-164
12		e		d	e		e	165,169,180,181
13	e		268					184,185

Figure 10

