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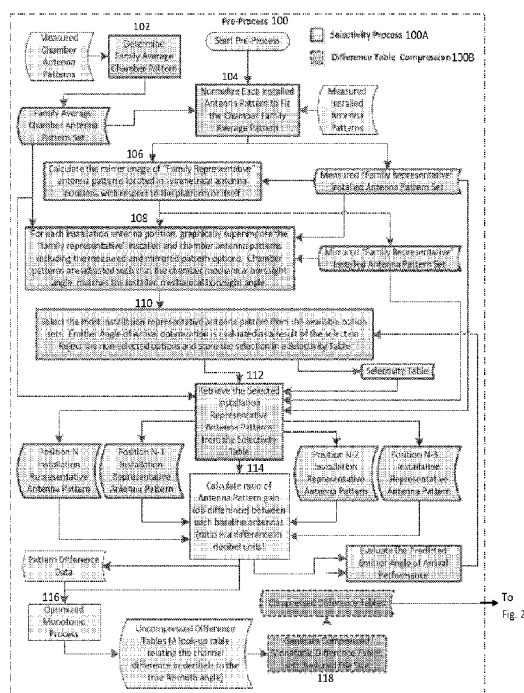
(54) **Title:** SYSTEMS AND METHODS FOR ANTENNA ANALYSIS AND VALIDATION

Figure 1

(57) **Abstract:** Systems and methods are disclosed herein which facilitate generating and utilizing look-up tables for determining an AoA of a radar signal received from an emitter. In example embodiments, the systems and methods may involve a selectivity process for selecting, for each of a plurality of installation positions, an installation-representative antenna pattern as selected from an option set. Thus, the selectivity process may, for example, include indexing a plurality of data sets of antenna patterns associated with an antenna position and selecting a most representative data set from at least one of the indexed data sets. In some embodiments, the system and methods may further apply a compression algorithm which identifies changes in slope with respect to adjacent pairs of antenna positions (vertex pairs) in the look-up table. The algorithm may then discard any antenna position (any vertex) that does not meet a slope difference threshold with respect to changes in the slope.



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## SYSTEMS AND METHODS FOR ANTENNA ANALYSIS AND VALIDATION

### Background:

The subject application relates generally to the field of radar signal processing, and more particularly to an approach to generating and utilizing look-up tables for determining an angle of arrival of a radar signal received from an emitter.

Angle of Arrival (AoA) determination requires an accurate description of the antenna performance over azimuth or elevation angle while avoiding ambiguity. Currently, the standard industry practice is to curve fit the antenna radiation pattern. One criterion by which radar receivers, such as Radar Warning Receivers (RWR), are evaluated is the Root Mean Square (RMS) angular error, which is principally determined by the quality of the radiation pattern and the curve fit.

U.S. Patent Application No. 13/958,240 (published as U.S. Publication No. 2015/0035696), entitled "Optimized Monotonic Radiation Pattern Fit with Ambiguity Resolution" and filed August 2, 2013 describes systems and methods for characterizing a radiation pattern of an antenna to improve the determination of an angle of arrival of a radar signal received by the antenna. In particular, U.S. Patent Application No. 13/958,240 features an optimized monotonic fitting approach to characterizing the radiation pattern. As disclosed therein, an approximation of the radiation pattern is represented as a window map having a plurality of windows. An optimized monotonic fit of the radiation pattern is determined by adjusting the window map, one window at a time, and testing the resulting new approximations. U.S. Patent Application No.

13/958,240 tangentially relates to example embodiments of the subject application and the entire contents thereof are hereby incorporated herein by reference.

U.S. Patent No. 6,657,596, entitled "Method of Measuring a Pattern of Electromagnetic Radiation" and issued December 2, 2003, describes systems and methods for measuring electromagnetic radiation patterns for antennas. U.S. Patent No. 6,657,596 provides useful background information relating to measuring and characterizing antenna patterns and the entire contents thereof are hereby incorporated herein by reference.

RWR systems, e.g., such as described in U.S. Patent Application No. 13/958,240, require extensive analysis in order to validate system performance. System performance validation often includes evaluation of antennas, cables, microcircuits, receivers, and other signal sensors when installed on aircraft platforms and when uninstalled. Furthermore, performance needs to be assessed within hostile environments (hot, cold, vibrations, etc.). Typically, validation may include the evaluation of system "amplitude difference lookup tables," AoA, aircraft structure sensor interference, accuracy predictions, error identification, calibration processes, and other similar criteria.

Validation analyses are often not conjoined and typically require considerable time investment, and are not cost effective. Typically, the analysis of antenna radiation performance data is performed manually and occasionally with the aid of statistical tools. For example, an analyst may evaluate individual antenna radiation pattern plots for correct isotropic gain levels, beamwidth, and beam squint. This can involve several

parallel manual analyses, such as effective antenna aperture gain predictions. Another example analysis is AoA calculation. Unfortunately, conventional AoA evaluations are not associated with other comparative analyses and therefore may often result in AoA calculation errors. Unreliable equipment setup and/or testing apparatus may also result in additional AoA calculation error. Furthermore, current practice is to limit frequency and polarization analyses by compensating with interpolation and extrapolation resulting in less accurate performance representation.

Thus traditional validation and evaluation methods are time consuming and prone to inaccurate determination. Under the conventional methods, it is often not possible to meet customer schedule when thousands of performance characterizations are required. Moreover, these methods fail to make use of High Power Computing (HPC) with distributive techniques. Conventional evaluation methods are also not able to perform comparative analyses in order to select the most useful solution.

Under conventional systems and methods, suboptimal antenna field of view radiation pattern performance may result from various inaccuracies such as measurement and calculation errors. Accordingly, systems and methods are needed in order to yield optimal antenna patterns.

#### Summary:

In example embodiments, methods are disclosed for generating a look-up table for determining an angle of arrival (AoA) of a radar signal received from an emitter. In example embodiments, these methods may include (i) for each of a plurality of antenna

installation positions, selecting an installation-representative antenna pattern from an indexed plurality of data sets of antenna patterns associated with the antenna installation position, wherein the selected installation-representative antenna pattern is a most representative data set as scored against a predetermined set of weighted criteria; and (ii) calculating and recording differences between the selected installation-representative patterns for each set of adjacent antenna installation positions in a look-up table. In some embodiments, the selected antenna pattern for each of the plurality of antenna installation positions may be stored in a selectivity table.

In example embodiments, the indexed plurality of data sets of antenna patterns may include a plurality of measured family-representative installed antenna patterns. Thus, e.g., the measured family-representative installed antenna patterns may be normalized relative to an antenna chamber pattern such as where the antenna chamber pattern is an average antenna chamber pattern for the family. In further example embodiments, the indexed plurality of data sets further includes mirrored data sets of measured family-representative installed antenna patterns for other antenna installation positions, mirrored with respect to a mounting platform. In some embodiments, the mirrored data sets may be mirrored front to back. In other embodiments, the mirrored data sets may be mirrored side to side. In further example embodiments, the indexed plurality of data sets further may include mirrored data sets of the measured family-representative installed antenna patterns, mirrored with respect to the antenna. In some embodiments, the plurality of data sets of antenna patterns may be evaluated with respect to each of a plurality of angle bins around a boresight.

In example embodiments, selecting the installation-representative antenna pattern from the indexed plurality of data sets may include scoring each indexed data set against the predetermined set of weighted criteria and choosing a data set having the greatest possible score. In some embodiments, a training set may be utilized to facilitate determining relative weighting factors for the set of weighted criteria. For example, a machine learning approach may be applied to determine a scoring algorithm as a function of the set of weighted criteria.

In example embodiments, the differences between selected installation-representative patterns for each set of adjacent installation positions may be indexed by true azimuth angle.

In example embodiments, a ratio of antenna pattern gains may be calculated for each set of adjacent installation positions based on the selected installation-representative antenna patterns for those positions. In some embodiments, the ratio of antenna pattern gains may be expressed as a difference in decibel units. In example embodiments, the ratio of antenna pattern gains may use an optimized monotonic process. For example, the ratio of antenna pattern gains may be calculated based on an absolute value of the difference between optimized monotonic fits for the selected installation-representative antenna patterns.

In example embodiments, the look-up table relating pattern difference data with respect to antenna installation position is utilized to calculate the AoA of a radar signal. In some embodiments, methods may further include compressing the data in the look-up table utilizing a compression algorithm which (i) identifies changes in slope with respect to

adjacent pairs of antenna installation positions in the look-up table and (ii) discards any antenna installation position that does not meet a slope difference threshold with respect to the changes in the slope. In some embodiments, at least a portion of the compressed data may be represented linearly. In other embodiments at least a portion of the compressed data may be represented by a piecewise function calculated based in part on points of inflection where slope changes sign.

In example embodiments, methods are presented for compressing data in a pattern difference look-up table. In general such methods may include (i) identifying changes in slope with respect to adjacent pairs of antenna installation positions in the look-up table and (ii) discarding any antenna installation position that does not meet a slope difference threshold with respect to the changes in the slope.

For a better understanding of the present teachings, together with other and further objects thereof, reference is made to the accompanying drawings and detailed description.

Brief Description of the Drawings:

**Figures 1 and 2** depict exemplary algorithms for generating (Fig. 1) and utilizing (Fig. 2) pattern difference look-up tables, according to the present disclosure.

**Figure 3** depicts an exemplary automatic selectivity algorithm, as further illustrated in and described with respect to sub-Figures 3A-3D, according to the present disclosure.



**Figures 3A-3D** are sub-Figures of Figure 3 representing partitions of Figure 3 as illustrated and referenced in Figure 3, according to the present disclosure.

**Figure 4** depicts an exemplary training method for the selectivity algorithm of Figure 3 and sub-Figures 3A-3D, as further illustrated in and described with respect to sub-Figures 4A-4D, according to the present disclosure.

**Figures 4A-4D** are sub-Figures of Figure 4, representing partitions of Figure 4 as illustrated and referenced in Figure 4, according to the present disclosure.

**Figure 5** depicts an exemplary compression algorithm, as further illustrated in and described with respect to sub-Figures 5A-5F, according to the present disclosure.

**Figures 5A-5F** are sub-Figures of Figure 5, representing partitions of Figure 5 as illustrated and referenced in Figure 5 therein, according to the present disclosure.

**Figures 6-10** illustrate exemplary data analysis of antenna patterns using a selectivity process, according to the present disclosure.

**Figure 11** is a block diagram of an example radar receiver system, according to the present disclosure.

#### Detailed Description:

Systems and methods are disclosed herein which facilitate generating and utilizing look-up tables for determining an AoA of a radar signal received from an emitter. In example embodiments, the systems and methods may involve a selectivity process for selecting,

for each of a plurality of installation positions, an installation-representative antenna pattern as selected from an option set. Thus, the selectivity process may, for example, include indexing a plurality of data sets of antenna patterns associated with an antenna position and selecting a most representative data set from at least one of the indexed data sets. Advantageously, the step of selecting a most representative data set may, in some embodiments, include scoring each indexed data set against a set of weighted criteria and choosing a data set having the greatest possible score based upon all possible pattern selections against the predetermined weighted selection criteria. Advantageously, a training set may be utilized to facilitate determining relative weighting factors for the weighted criteria. In some embodiments, a machine learning approach (e.g., SVM, neural net, decision tree or the like) may be applied to determine a scoring algorithm as a function of the weighted criteria (e.g., wherein the scoring algorithm may appropriately reflect and account for the relative weighting between the criteria).

Selected installation-representative antenna patterns for each installation position (e.g., resulting from the selectivity process) may be stored in a selectivity table for further analysis and evaluation whereas non-selected antenna patterns may be rejected/discarded. Advantageously, AoA performance may be evaluated based on the selected installation-representative antenna patterns. Thus, differences between selected installation-representative patterns for each set of adjacent installation positions (pattern difference data) may be calculated and recorded, such as in a look-up table, e.g., as indexed by position (e.g., by true azimuth angle) . For example, a ratio of antenna pattern gains may be calculated for each set of adjacent installation positions based on the selected installation-representative antenna patterns for those positions.

The ratio may be expressed, e.g., as a difference in decibel units (dB difference). In example embodiments, the calculation of the ratio of antenna pattern gains may involve an optimized monotonic process, e.g., such as described in U.S. Patent Application No. 13/958,240. Thus, for example, in some embodiments, the ratio of antenna pattern gains may be calculated based on the absolute value of the difference between optimized monotonic fits for the selected installation-representative antenna patterns.

Similar to as is disclosed with respect to Figures 10A and 10B of U.S. Patent Application No. 13/958,240, look-up tables described herein relating pattern difference data with respect to antenna position (e.g., with respect to true azimuth angle) may be utilized to calculate the AoA of a radar signal. Thus, the various antenna positions are compared to determine which one has the highest effective radiated power (ERP). The sector containing the installation position with the highest ERP is referred to herein as the emitter sector. The emitter sector and the next strongest adjacent sector are compared and an ERP ratio of the two sectors is calculated (which may be calculated as a difference of the two ERPs when expressed in decibel units). The ERP ratio may be used to resolve the AoA, e.g., in the azimuth plane, based on the look-up table. Advantageously, the emitter sector and subsector (e.g., quadrant and octant) may be used to restrict the search domain within the difference table for resolving the AoA.

Notably, pattern difference data look-up tables, such as described herein, may be compressed using various compression algorithms. In example embodiments, a monotonic optimization process may be applied to produce a compressed monotonic (e.g., monotonically increasing or decreasing) look-up table. See, e.g., U.S. Patent

Application No. 13/958,240. In some embodiments, other compression algorithms may be applied separately or in conjunction with the monotonic optimization process.

In example embodiments, the system and methods may utilize a compression algorithm which identifies changes in slope with respect to adjacent pairs of antenna positions (vertex pairs) in the look-up table. The algorithm then discards any antenna position (any vertex) that does not meet a slope difference threshold with respect to changes in the slope. In exemplary embodiments, the compressed data may be represented linearly, e.g., as a monotonic piece-wise linear representation, using the difference data for the remaining antenna positions, e.g., for the remaining vertices. Alternatively, the compressed data may be represented using one or more piecewise functions. For example, points of inflection may be determined based on the slope of the look-up table changing sign, (e.g., with respect to adjacent pairs of antenna positions either prior to the slope difference threshold discarding of vertices or subsequent thereto). Piecewise functions may then be calculated/determined between adjacent vertices which reflect the points of inflection.

Based on empirical testing to date, the systems and methods described herein have proven to be exceptional in reducing validation time and cost and have proven useful for identifying outlier performances in sensor perturbations. The selectivity algorithm and associated interface advantageously enable a user to select aircraft elevations, polarizations, performance mirroring, signal ports, installed and/or chamber performance, and the like as part of the validation process. Thus, generated look-up tables (e.g., for determining AoA) may account for a complete system performance

(e.g., antenna, cable, cords, installation configuration, etc.) as opposed to just accounting for the antenna. Thus the systems and methods of the present disclosure have the ability to map the installed field of view performance in 3 dimensions (3D) onto a full size aircraft. Screening processes evaluate the free space (no aircraft) antenna family performance variance with correlation to aircraft installed performance. This process is capable of making use of HPC distributive methods for improved computational processing time. Furthermore, the systems and methods of the present disclosure are able to substantially reduce the memory size for look-up tables, e.g., by applying various compression algorithms disclosed herein.

With initial reference to Figures 1 and 2 an example algorithm for generating and utilizing pattern difference look-up tables is depicted. More particularly, Figure 1 depicts a pre-process 100 for generating a pattern difference look-up table and Figure 2 depicts a system process 200 for resolving AoA based on the generated look-up table of Figure 1.

With specific reference to Figure 1, the pre-process 100 may advantageously include a selectivity process 100A and a data compression process 100B, as part of the generation of the pattern difference look-up table. In general the selectivity process 100A may include indexing a plurality of data sets of antenna patterns associated with an antenna position and selecting a most representative data set from at least one of the indexed data sets. As reflected in Figure 1, example embodiments indexing the plurality of data sets of antenna patterns may include steps of e.g., 102 determining a family average chamber pattern (e.g., based on measured antenna chamber patterns),

104 normalizing each installed antenna pattern to fit the family average chamber pattern (e.g., based on measured installed patterns to produce a measured family-representative installed antenna pattern set) and 106 calculating mirror images for the measured family-representative installed antenna pattern set and the family average chamber pattern (e.g., with respect to the platform and/or with respect to the antenna itself). Advantageously, for each installation antenna position, each indexed antenna pattern (e.g., the original and mirrored family average chamber pattern and measured family-representative installed antenna pattern set) may be superimposed (e.g. with the mechanical boresight angles matching). Outlier patterns may then be easily identified and rejected. At step 110 a most installation-representative antenna pattern may be selected from the indexed patterns (e.g., for later utilization in the generation of the pattern difference look-up table for AoA resolution). Notably, the selected antenna pattern for each antenna installation position may be stored in a selectivity table. An example algorithm for selecting the most installation-representative antenna patterns is described with respect to Figures 3 and 4, herein.

At step 112 the selected installation-representative antenna patterns are retrieved from the selectivity table and at step 114 differences between selected installation-representative patterns for each set of adjacent installation positions (pattern difference data) is calculated and recorded, such as in a look-up table, e.g., as indexed by position (e.g., by true azimuth angle) . For example, a ratio of antenna pattern gains may be calculated for each set of adjacent installation positions based on the selected installation-representative antenna patterns for those positions. The ratio may be expressed, e.g., as a difference in decibel units (dB difference). In example

embodiments, the calculation of the ratio of antenna pattern gains may involve an optimized monotonic process, e.g., such as described in U.S. Patent Application No. 13/958,240. Thus, for example, in some embodiments, the ratio of antenna pattern gains may be calculated based on the absolute value of the difference between optimized monotonic fits for the selected installation-representative antenna patterns. In other embodiments, a monotonic compression may be applied with respect to the pattern difference data. Finally, at step 118 a compression algorithm may be applied for compressing the data in the pattern difference look-up table. An example compression algorithm is described with respect to Figure 5, herein.

With reference now to Figure 2, the look-up table generated according to the pre-process 100 of Figure 1 may be utilized as part of a system process 200 to calculate the AoA of a radar signal. Thus, at step 202, the various antenna positions are compared to determine which one has the highest ERP. The identified installation position with the highest ERP is referred to herein as the emitter sector. At step 204, the emitter sector and the next strongest adjacent sector are compared and an ERP ratio of the two sectors is calculated (which may be calculated as a difference of the two ERPs when expressed in decibel units). The ERP ratio may then be used at step 206 to resolve the AoA, e.g., in the azimuth plane, based on the look-up table. Advantageously, the emitter sector and subsector (e.g., quadrant and octant) may be used to restrict the search domain within the difference table for resolving the AoA.

With reference now to Figure 3 and sub-Figures 3A-3D, an exemplary automatic selectivity algorithm 300 is presented for scoring and selecting a most representative

installation pattern, e.g., for a particular application based on a predetermined set of criteria. In particular, algorithm 300 may include steps of scoring each indexed data set against a set of weighted criteria and choosing a data set having the greatest possible score based upon all possible pattern selections against the predetermined weighted selection criteria. In the example embodiment of Figure 3 and sub-Figures 3A-3D, algorithm 300 includes at step 310, for each possible pattern selection, calculating a correlation between the pattern selection (after normalization thereof) and the chamber pattern in a plurality of azimuth bins (e.g., relative to the antenna boresight). In particular, a standard deviation may be calculated for each bin, e.g., to evaluate pattern scalloping. In exemplary embodiments, the bins may be +15 to +30, +30 to +45, +45 to +60, -15 to -30, -30 to -45, and -45 to -60 from the antenna azimuth boresight angle. In exemplary embodiments, each correlation with respect to one of the bins may represent a separate scoring criterion (e.g., with a separate weighting factor). As depicted in Figure 3 and sub-Figures 3A-3D, other scoring criteria may include, e.g., for each possible pattern selection, at step 304 calculating gain difference between max azimuth gain of the pattern and the chamber boresight gain and/or at step 306 (in the case of a forward pattern) calculating a difference between maximum azimuth gain of the forward pattern and the average maximum gain of the corresponding possible aft patterns. It is noted that other criteria may be utilized in determining the scoring parameters. Moreover, each of the criteria may be separately weighted in determining an overall weighted score for each indexed pattern. Notably, at step 308 the highest scoring pattern may be selected, e.g., for the selectivity table and further processing such as described in Figure 1.



As depicted in Figure 4 and sub-Figures 4A-4D, in some embodiments, a training set may be utilized, e.g., to facilitate determining relative weighting factors for the weighted criteria. Thus, according to the training algorithm 400 of Figure 4 and sub-Figures 4A-4D, weight factors may be calculated at step 402 for each of a plurality of criteria so as to best represent a plurality of selected patterns in a training set, e.g., relative to the other non-selected patterns in the training set. In some embodiments, a machine learning approach (e.g., SVM, neural net, decision tree or the like) may be applied to determine a scoring algorithm as a function of the weighted criteria (e.g., wherein the scoring algorithm may appropriately reflect and account for the relative weighting between the criteria).

With reference now to Figure 5, an exemplary compression algorithm 500 is depicted for reducing the memory load of a pattern difference look-up table. The compression algorithm 500, advantageously, at step 502 identifies changes in slope with respect to adjacent pairs of antenna positions (vertex pairs) in the look-up table and then at step 504 discards any antenna position (any vertex) that does not meet a slope difference threshold with respect to the changes in the slope. In particular, as depicted in Figure 5 and sub-Figures 5A-5F, for each vertex pair the algorithm calculates the slope between the vertices of the vertex pair as well as the slope between the left vertex of the pair and the neighboring vertex to the left of the pair and the slope between the right vertex of the pair and the neighboring vertex to the right of the pair. A slope difference is then calculated between the slope of the vertex pair and the slope between the left vertex of the pair with the left neighboring vertex. If the slope difference with respect to the left vertex is less than a predetermined threshold the left vertex of the pair is discarded.

Similarly, a slope difference may be calculated between the slope of the vertex pair and the slope between the right vertex of the pair with the right neighboring vertex. As with the left vertex, if the slope difference with respect to the right vertex is less than a predetermined threshold, the right vertex of the pair is discarded.

As depicted in Figure 5 and sub-Figures 5A-5F, the compressed data may be represented linearly 506, e.g., as a monotonic piecewise linear representation, using the difference data for the remaining antenna positions, e.g., for the remaining vertices. Alternatively, the compressed data may be represented using one or more piecewise functions 508. For example, at step 510 points of inflection may be determined based on the slope of the look-up table changing sign, (e.g. with respect to adjacent pairs of antenna positions either prior to the slope difference threshold discarding of vertices or subsequent thereto). Piecewise functions which reflect the points of inflection may then be calculated/determined (e.g., at step 512) between adjacent vertices. Notably, the piecewise fitting process may be a recursive/iterative process with a threshold number of iterations prior to selecting the best candidate parameters for the piecewise function. Notably, in some embodiments the piecewise function should be monotonic on either side of an inflection point. In some embodiments, a combination of linear and piecewise functions may be used in representing the data table.

Figure 6 depicts an example embodiment where raw data input 602 is evaluated by a selectivity process (automated or manual) to detect erroneous performance resulting in AoA inaccuracies. In the depicted example embodiment, the raw data 602 illustrates a signal ripple error 610, a signal fading error 620, level error agreement 630 and a

scalloping error 640. In exemplary embodiments, selectivity may be used to generate a golden set of antenna patterns from the raw data 602, e.g., by eliminating outliers from consideration. In example embodiments, a training algorithm or weighting function may facilitate the selectivity process. In some embodiments, evaluation of an antenna pattern may be done in a segmented manner, e.g., based on a plurality of bins of ranges of azimuth angles relative to a boresight angle. Thus, each bin may be evaluated for errors such as noted with respect to Fig. 6. In example embodiments, scalloping error may be evaluated based on standard deviation within a given bin. In further example embodiments, level error agreement may be evaluated by comparing theoretical gain for an adjacent quadrant. As illustrated the raw data 602 may also be evaluated with or without antenna installation (602 vs. 604). Figure 7 illustrates an example embodiment wherein raw data input is evaluated by a selectivity process (automated or manual) to detect erroneous performance resulting in AoA inaccuracies. In general, the selectivity process may evaluate for erroneous performance for complete 360° coverage around the aircraft. As previously noted the selectivity process may aim to reduce or eliminate scalloping effects, e.g., since such effects are not representative of the correct performance of the sensors.

As depicted in Figure 8, the selectivity process may, in some embodiments, evaluate antenna gain, beam width, and beam squint for correct performance based on predictions (such as known antenna performance without aircraft perturbations). For example, in some embodiments, a specific antenna cannot have more gain than a maximum allowable antenna effective aperture size.

As depicted in Figure 9, in example embodiments, the selectivity process may detect/evaluate two different patterns levels. Thus, for example, the selectivity process may enable selection of patterns yielding most appropriate crossovers between quadrants, e.g., based on symmetry between left and right quadrants. In some embodiments, symmetry between quadrants may be defined based on closest possible gain at one or more angular positions (for example at -90). Outliers (e.g., non-symmetrical pairs) may be rejected. Thus, as depicted in Figure 9, a pattern for the forward right sensor quadrant may be selected (red) as optimal over a pattern in the forward left quadrant (blue). The forward left quadrant pattern may then be replaced with a mirrored pattern of the forward right sensor pattern. Once selected the pattern can then be further evaluated, e.g., to reduce ripple, remove scalloping effects, correct gain, check versus family performance variance, or add performance characteristics of other system components (such as cables, radomes and microcircuit switching).

With reference now to Figure 10, in example embodiments, selectivity may gather all available performance data inputs (radomes, antennas, cables, RF switches, receiver, including temperatures effects ) and analyze (in auto mode or manually) all performances to eliminate or reduce system degradation (for example, with respect to AoA performance detection and location accuracy improvement). One output of the selectivity process (as described in the examples above) may include what can be referred to as the "Golden Patterns." These patterns are not necessarily antenna patterns in isolation. Rather these patterns produced as selectivity output can include RF receiver sensitivity detection optimization, temperature effects upon antenna/radome performance, etc. Figure 10 depicts how the system impact, e.g., of cable transmission

microcircuits, may be evaluated with respect to the antenna pattern variance and family performance.

FIG. 11 shows an example aircraft 1000 with a radar receiver system 105 for determining a location of an emitter 1100 from an angle of arrival of a radar signal 1150 sent from the emitter 1100. The radar receiver system 1050 includes antennas 1200 (typically four) communicatively coupled to a radar receiver 1250 to receive and process (e.g., detect) the radar signal 1150. How accurate the radar receiver system 1050 determines the location of the emitter 1100 depends on how well the radiation patterns of the installed antennas 1200 (or "radar receiver antenna patterns") are characterized. The radar receiver system 1050 may also include an approximating engine 3000 communicatively coupled to the radar receiver 1250. The approximating engine 3000 may in example embodiments generate an approximation or fit of the radiation pattern called an "optimized monotonic fit." In turn, the radar receiver system 1050 may calculate the angle of arrival of the radar signal and determines the location of the emitter, either in whole or in part, based on the optimized monotonic fit. In some embodiments, the approximation engine 3000 may be configured to implement a selectivity process and/or a compression algorithm as disclosed herein.

Although these teachings have been described with respect to various embodiments, it should be realized these teachings are also capable of a wide variety of further embodiments.

## Claims:

1. A method for generating a look-up table for determining an angle of arrival (AoA) of a radar signal received from an emitter, the method comprising:
  - a. for each of a plurality of antenna installation positions, selecting an installation-representative antenna pattern from an indexed plurality of data sets of antenna patterns associated with the antenna installation position, wherein the selected installation-representative antenna pattern is a most representative data set as scored against a predetermined set of weighted criteria; and
  - b. calculating and recording differences between the selected installation-representative patterns for each set of adjacent antenna installation positions in a look-up table.
2. The method of claim 1, wherein the selected antenna pattern for each of the plurality of antenna installation positions are stored in a selectivity table.
3. The method of claim 1, wherein the indexed plurality of data sets of antenna patterns includes a plurality of measured family-representative installed antenna patterns.
4. The method of claim 3, wherein the measured family-representative installed antenna patterns are normalized relative to an antenna chamber pattern.
5. The method of claim 4, wherein the antenna chamber pattern is an average antenna chamber pattern for the family.
6. The method of claim 3, wherein the indexed plurality of data sets further includes mirrored data sets of measured family-representative installed antenna patterns

for other antenna installation positions, mirrored with respect to a mounting platform.

7. The method of claim 6, wherein mirrored data sets are mirrored front to back.
8. The method of claim 6, wherein mirrored data sets are mirrored side to side.
9. The method of claim 3, wherein the indexed plurality of data sets further includes mirrored data sets of the measured family-representative installed antenna patterns, mirrored with respect to the antenna.
10. The method of claim 1, wherein the plurality of data sets of antenna patterns are evaluated with respect to each of a plurality of angle bins around a boresight.
11. The method of claim 1, wherein selecting the installation-representative antenna pattern from the indexed plurality of data sets includes scoring each indexed data set against the predetermined set of weighted criteria and choosing a data set having the greatest possible score.
12. The method of claim 1, wherein a training set is utilized to facilitate determining relative weighting factors for the set of weighted criteria.
13. The method of claim 1, wherein a machine learning approach is applied to determine a scoring algorithm as a function of the set of weighted criteria.
14. The method of claim 1, wherein the differences between selected installation-representative patterns for each set of adjacent installation positions is indexed by true azimuth angle.
15. The method of claim 1, wherein a ratio of antenna pattern gains is calculated for each set of adjacent installation positions based on the selected installation-representative antenna patterns for those positions.

16. The method of claim 15, wherein the ratio of antenna pattern gains is expressed as a difference in decibel units.
17. The method of claim 15, wherein the calculation of the ratio of antenna pattern gains uses an optimized monotonic process.
18. The method of claim 17, wherein the ratio of antenna pattern gains is calculated based on an absolute value of the difference between optimized monotonic fits for the selected installation-representative antenna patterns.
19. The method of claim 1, wherein the look-up table relating pattern difference data with respect to antenna installation position is utilized to calculate the AoA of a radar signal.
20. The method of claim 1, further comprising compressing the data in the look-up table utilizing a compression algorithm which (i) identifies changes in slope with respect to adjacent pairs of antenna installation positions in the look-up table and (ii) discards any antenna installation position that does not meet a slope difference threshold with respect to the changes in the slope.
21. The method of claim 20, wherein at least a portion of the compressed data is represented linearly.
22. The method of claim 20, wherein at least a portion of the compressed data is represented by a piecewise function calculated based in part on points of inflection where slope changes sign.
23. A method for compressing data in a pattern difference look-up table, the method comprising:



- a. identifying changes in slope with respect to adjacent pairs of antenna installation positions in the look-up table and
- b. discarding any antenna installation position that does not meet a slope difference threshold with respect to the changes in the slope.

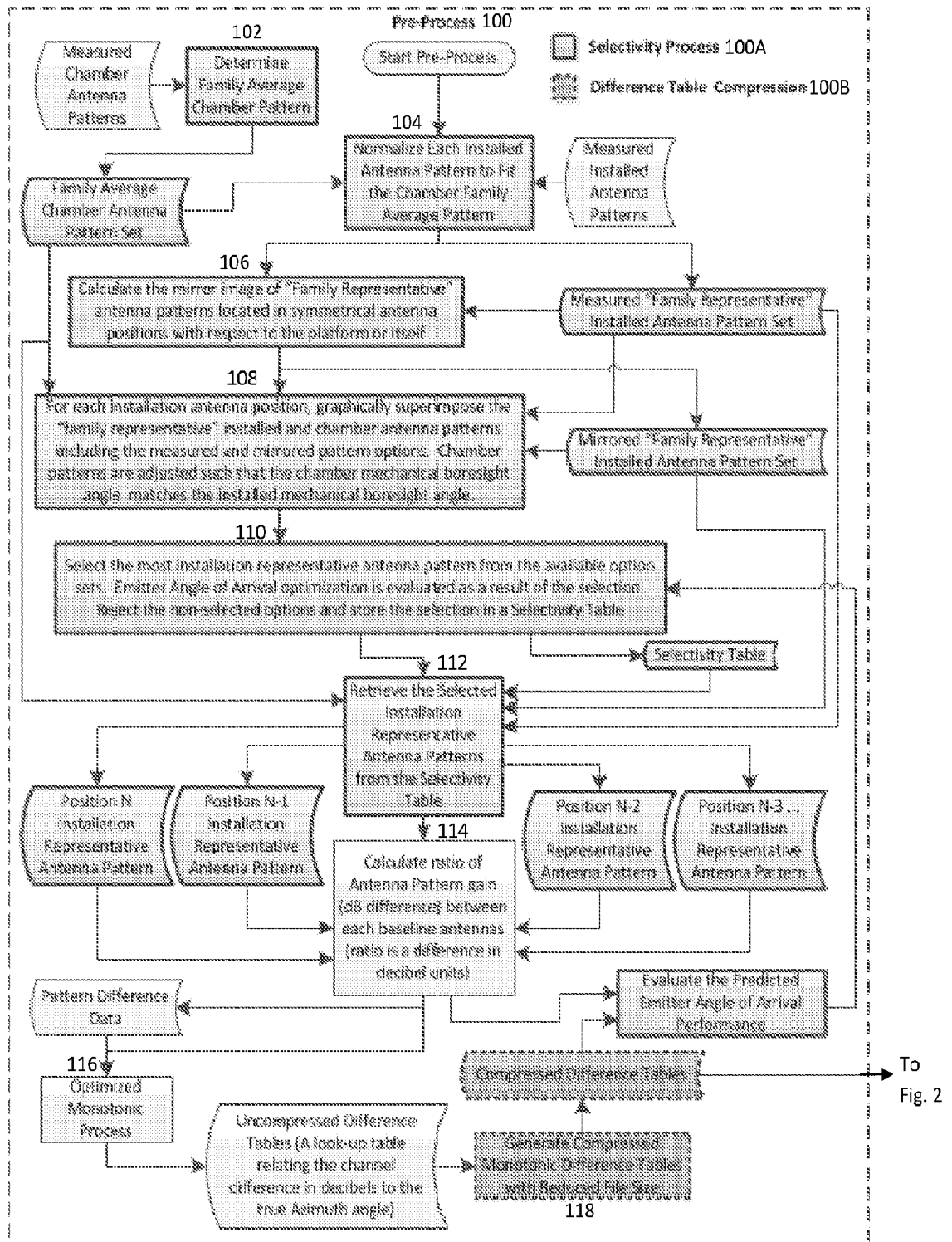


Figure 1

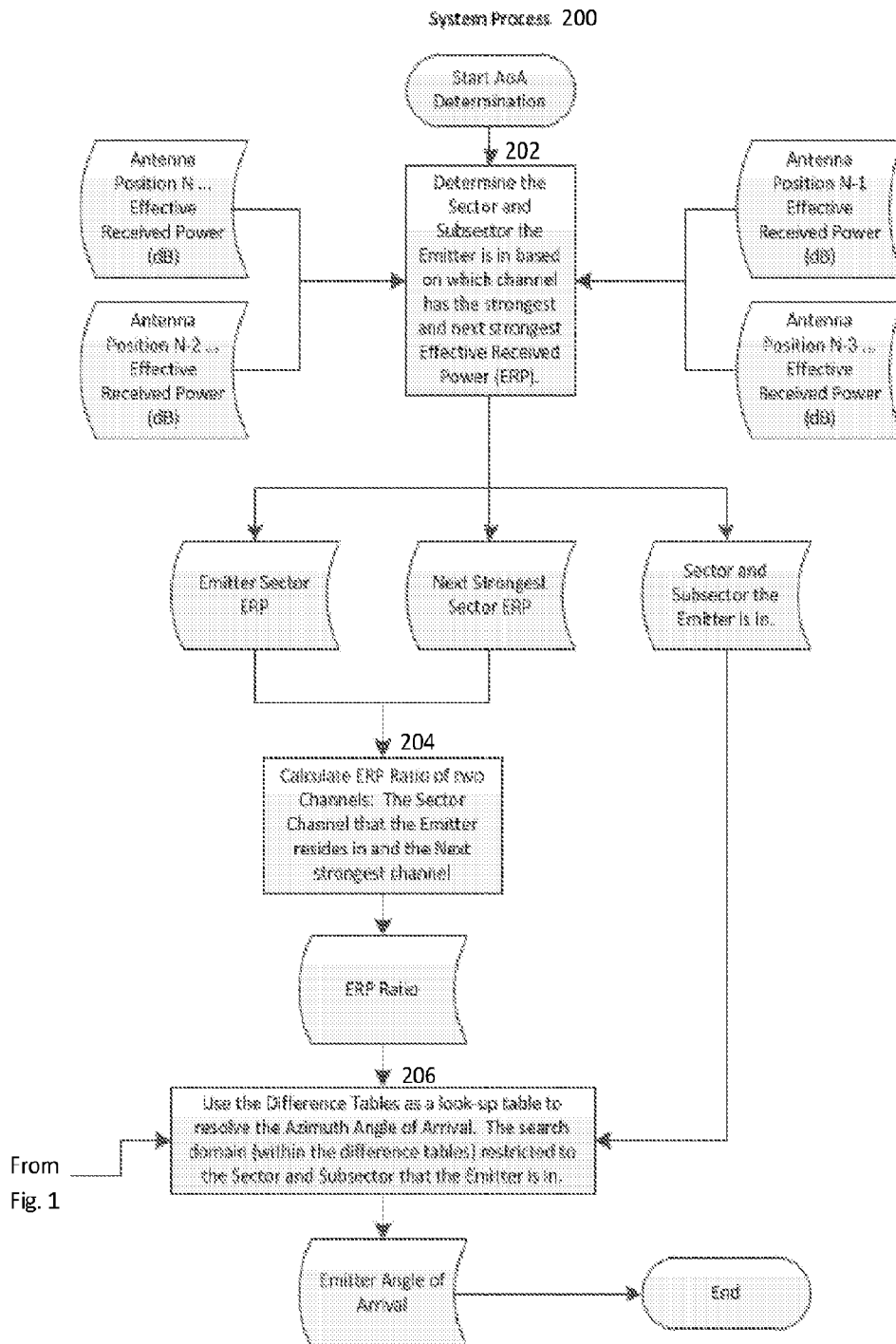


Figure 2

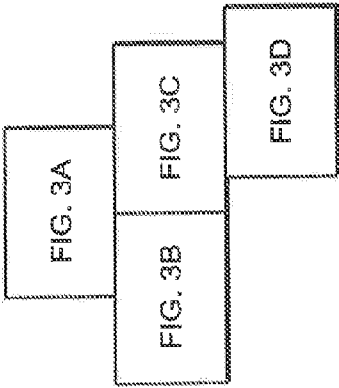


FIG. 3

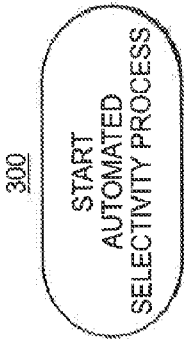


FIG. 3A



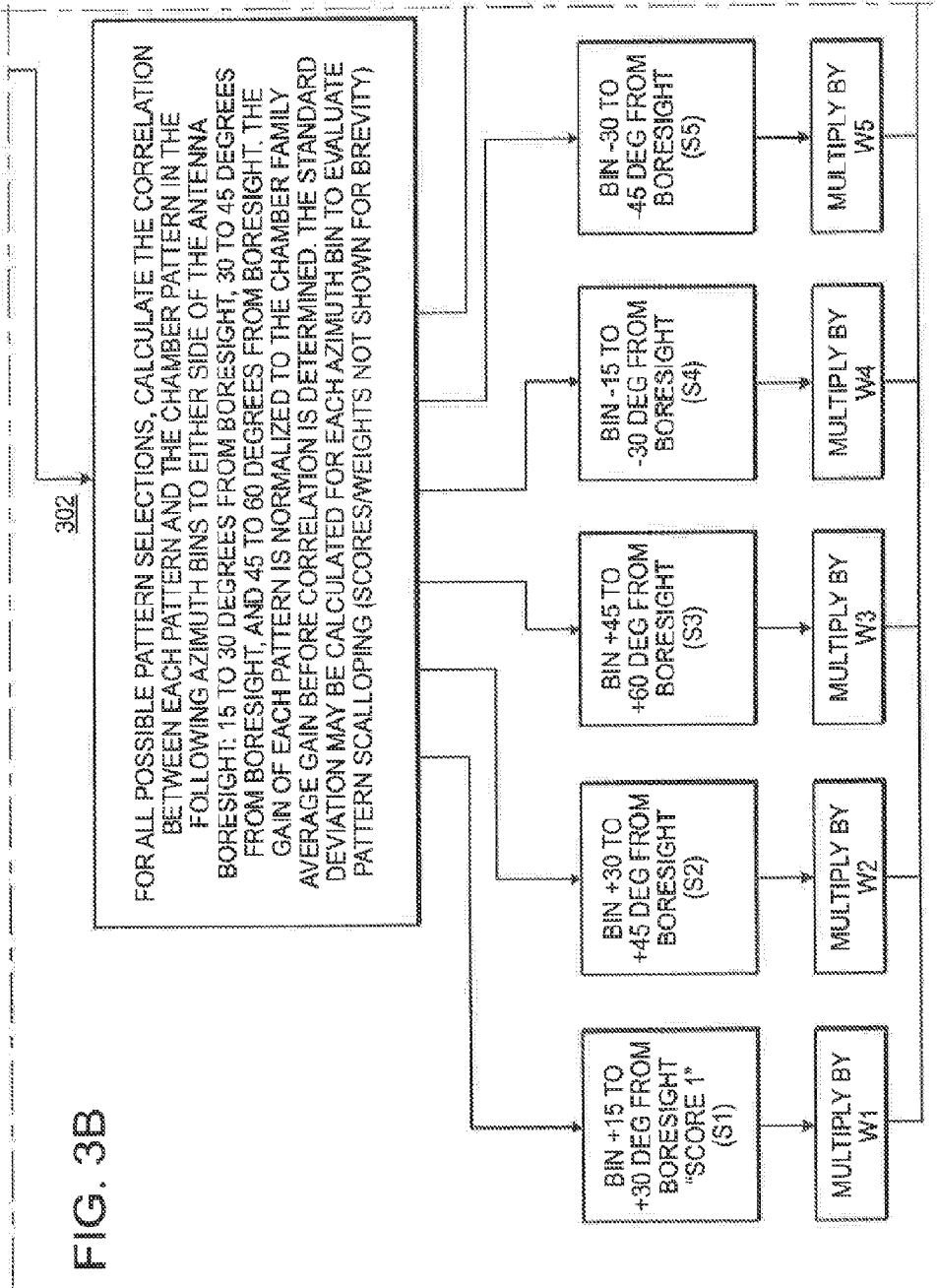
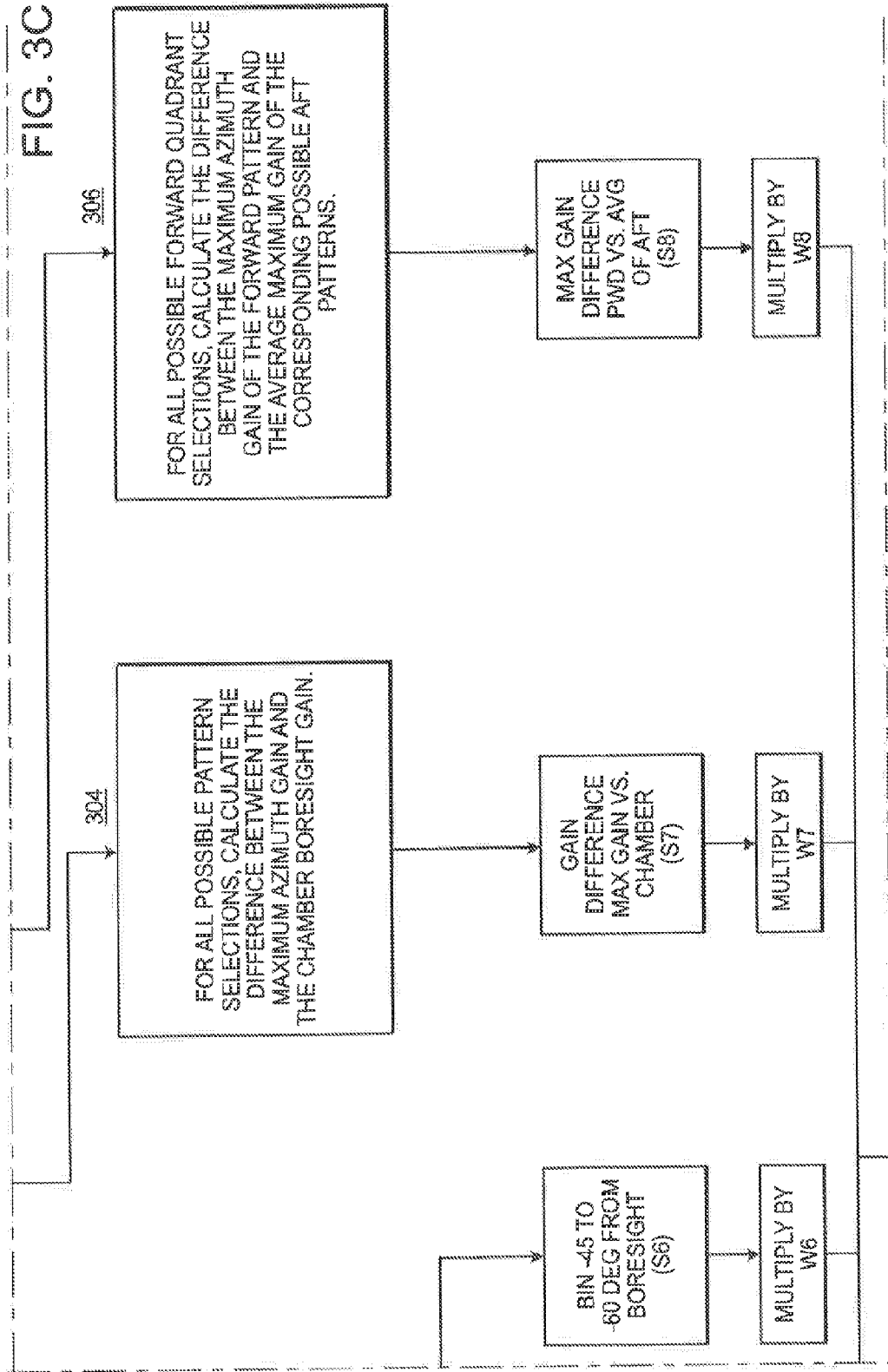


FIG. 3C



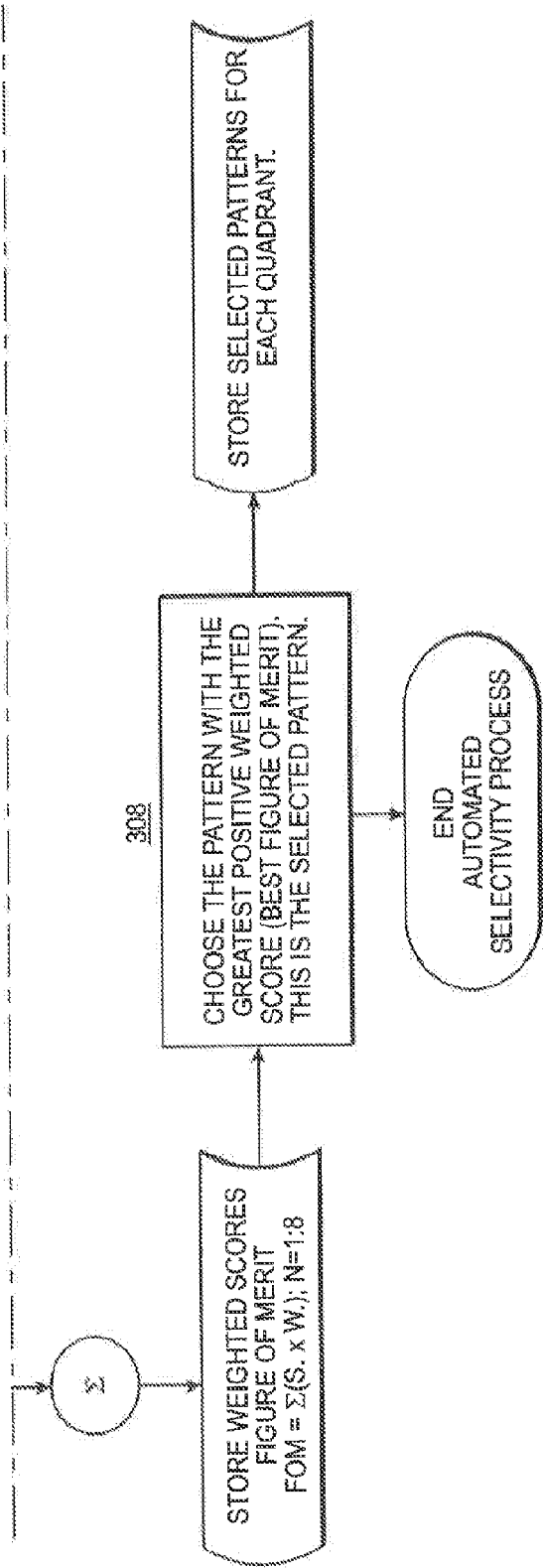


FIG. 3D

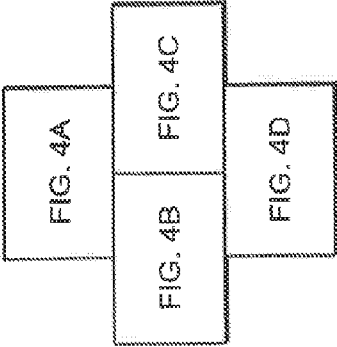


FIG. 4

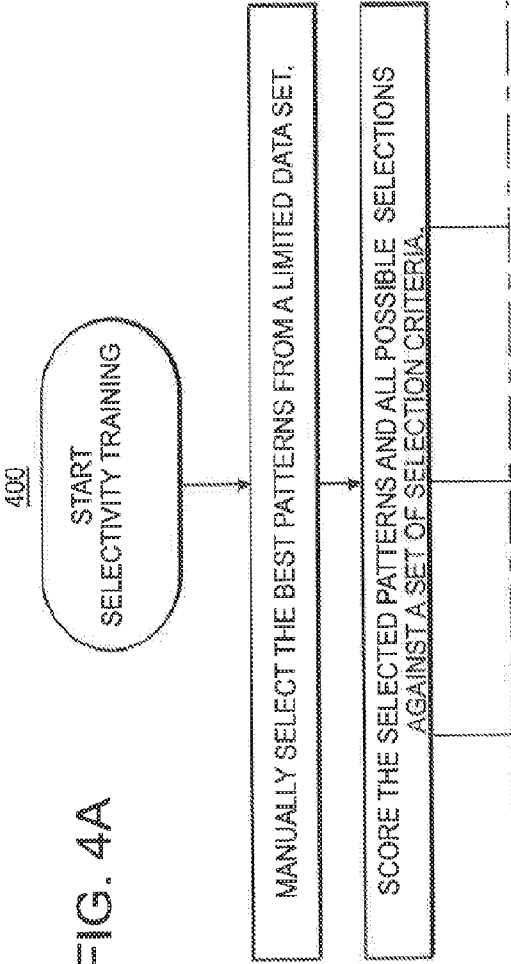
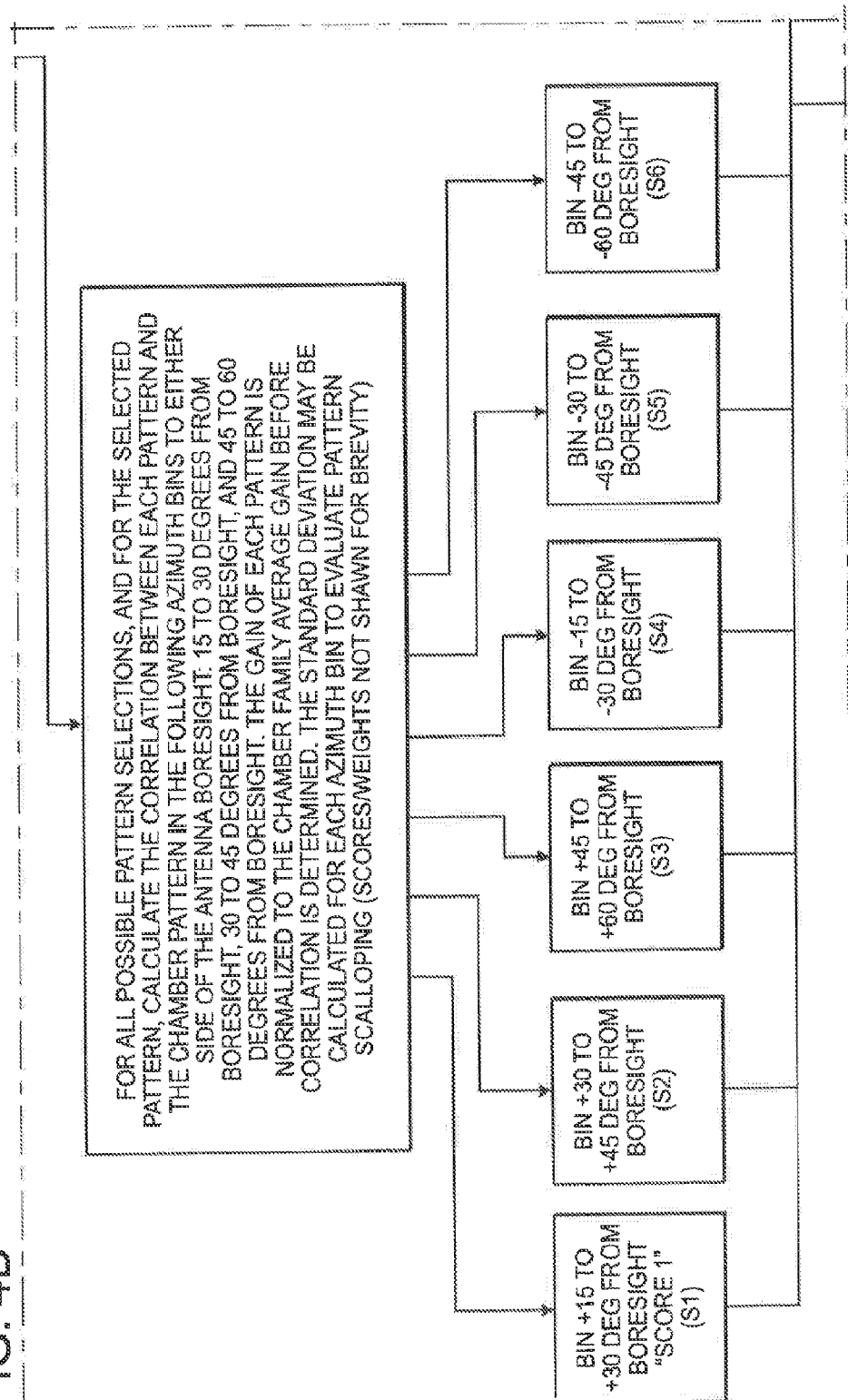


FIG. 4A

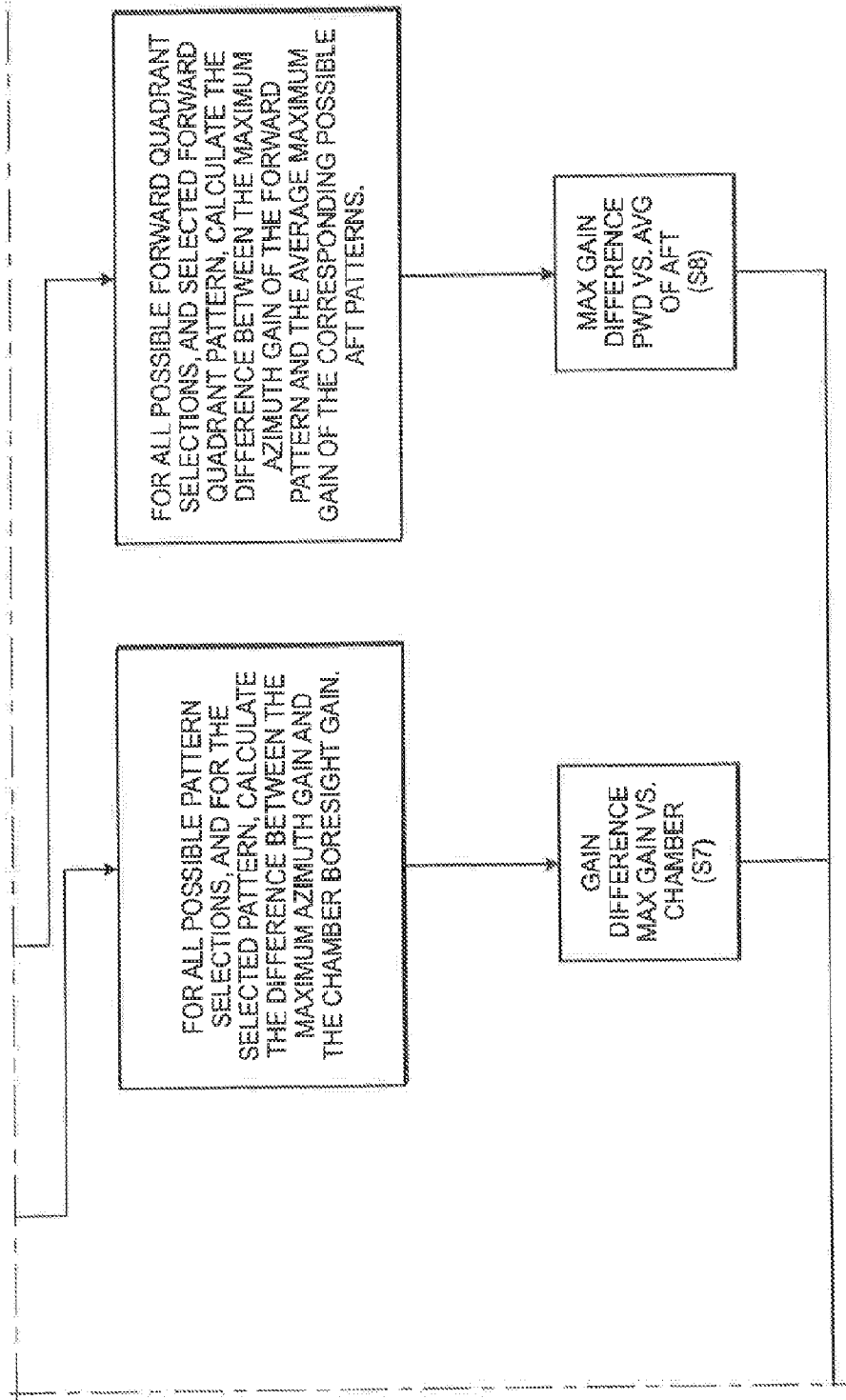


FIG. 4B



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FIG. 4C



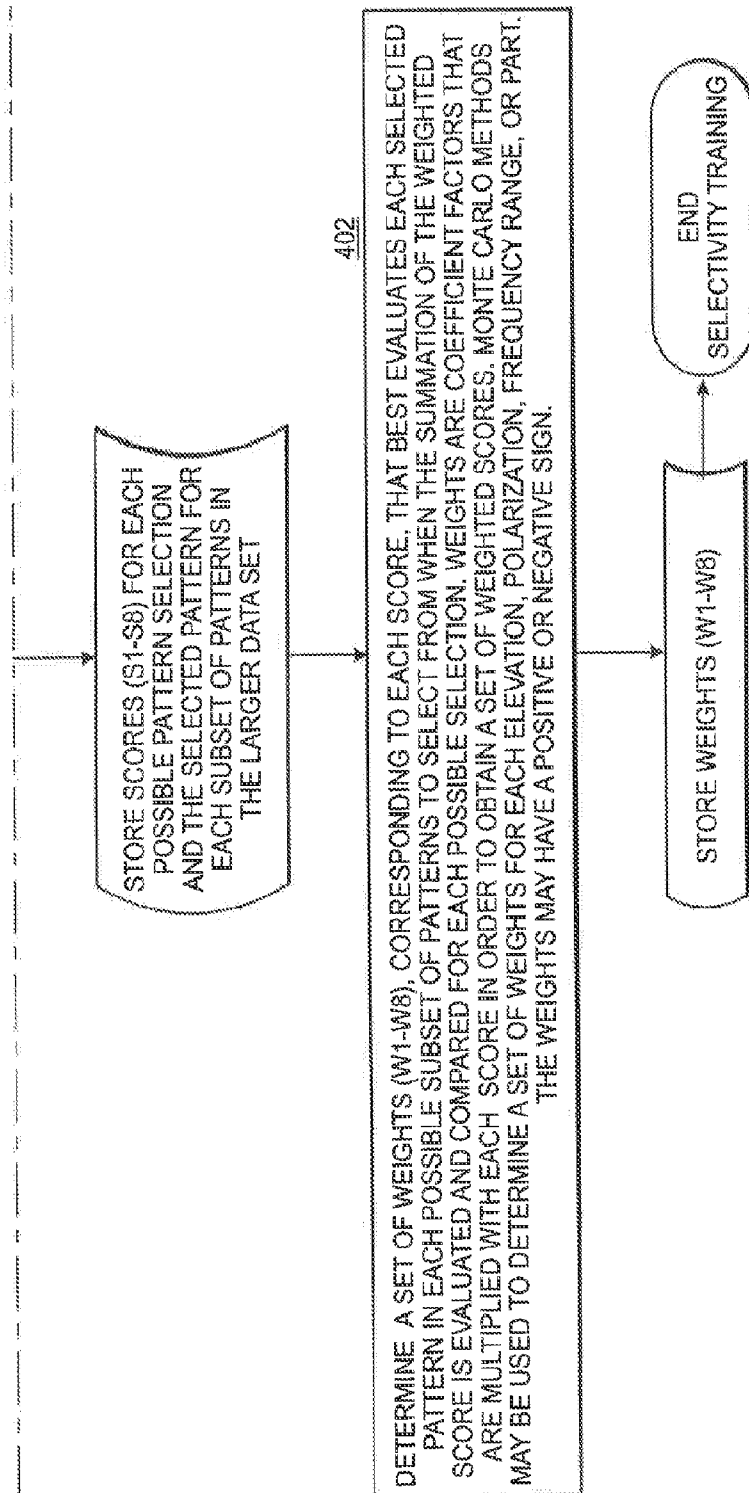
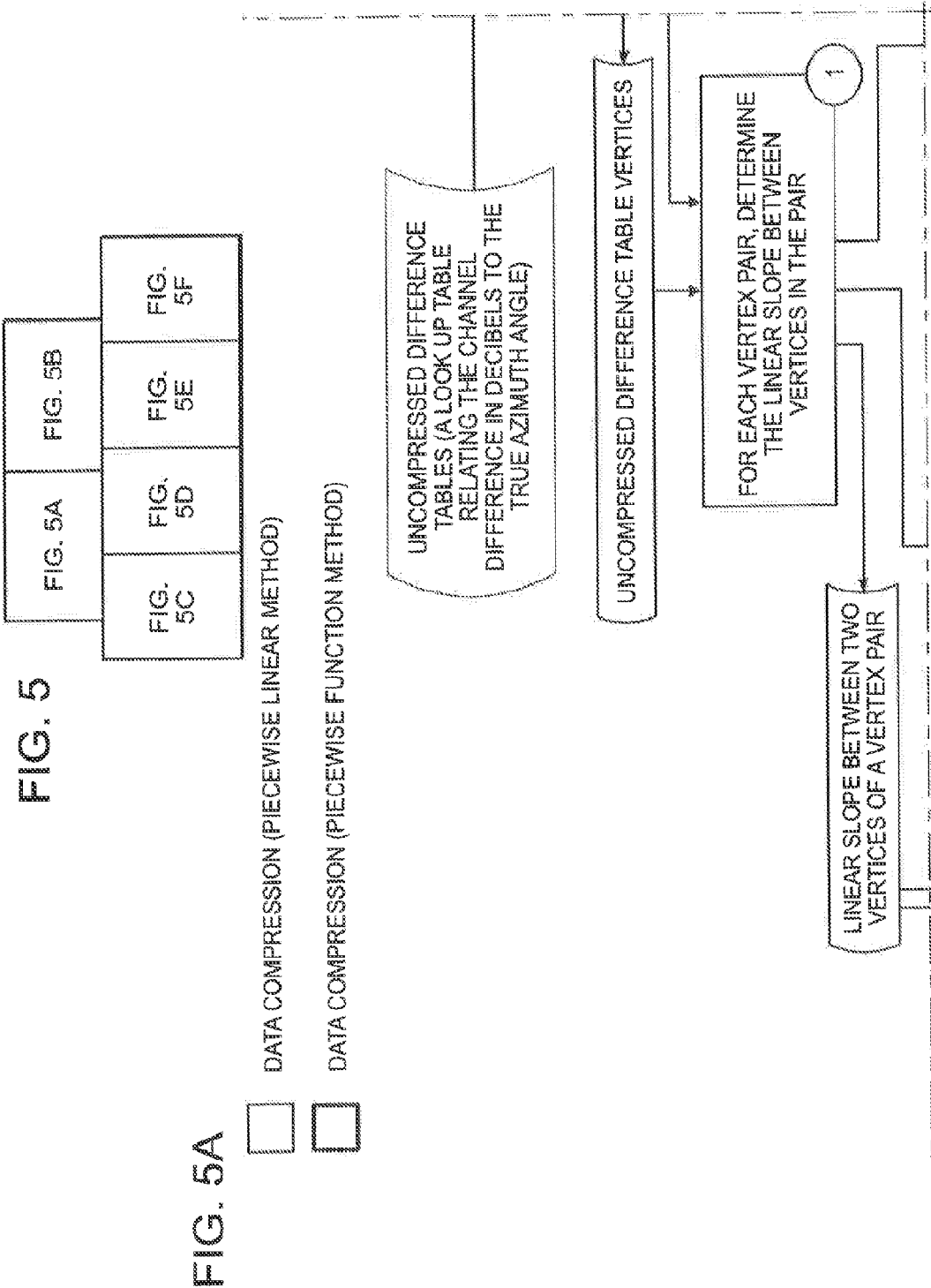


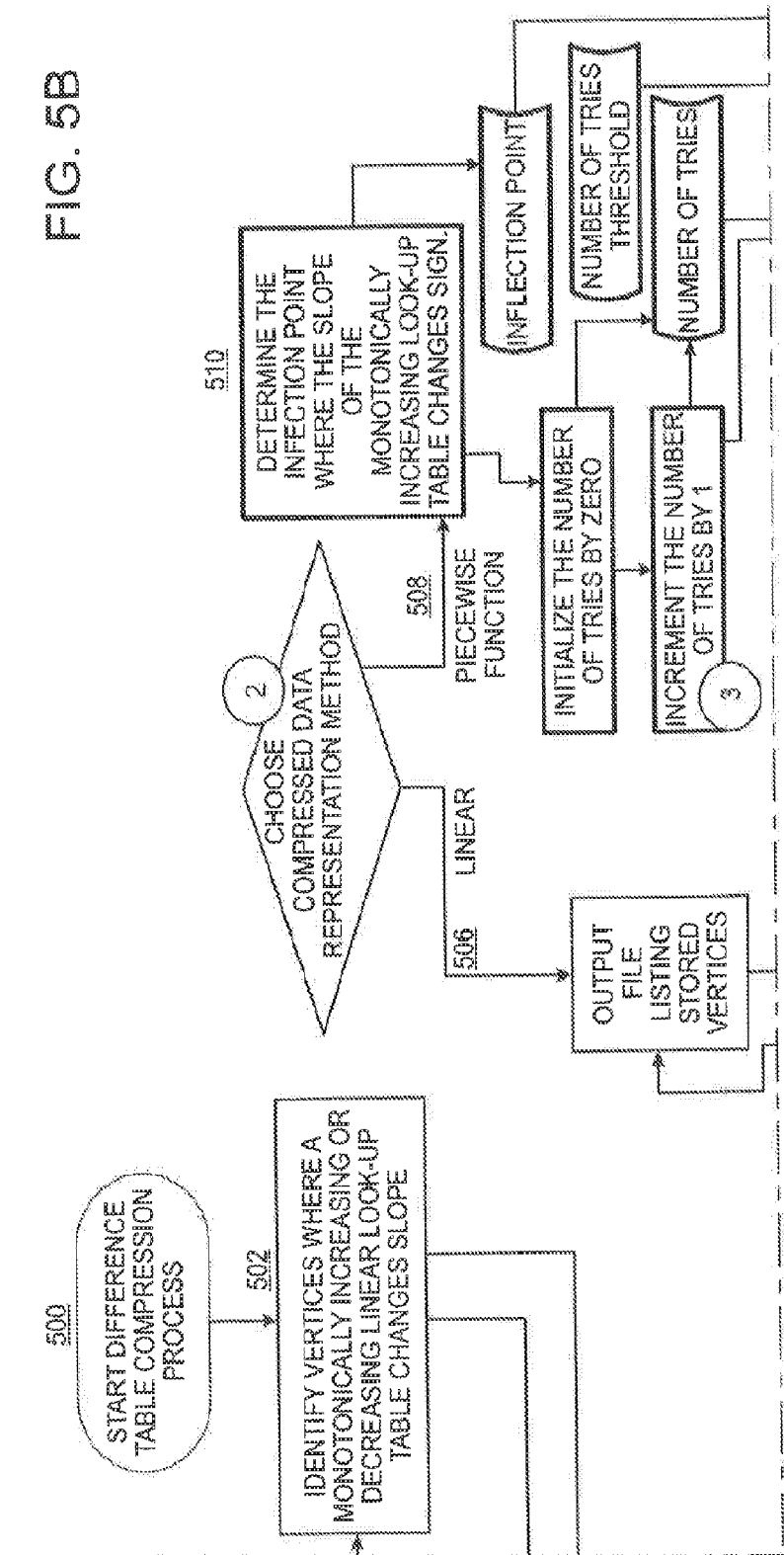
FIG. 4D

SUBSTITUTE SHEET (RULE 26)



SUBSTITUTE SHEET (RULE 26)

FIG. 5B



SUBSTITUTE SHEET (RULE 26)

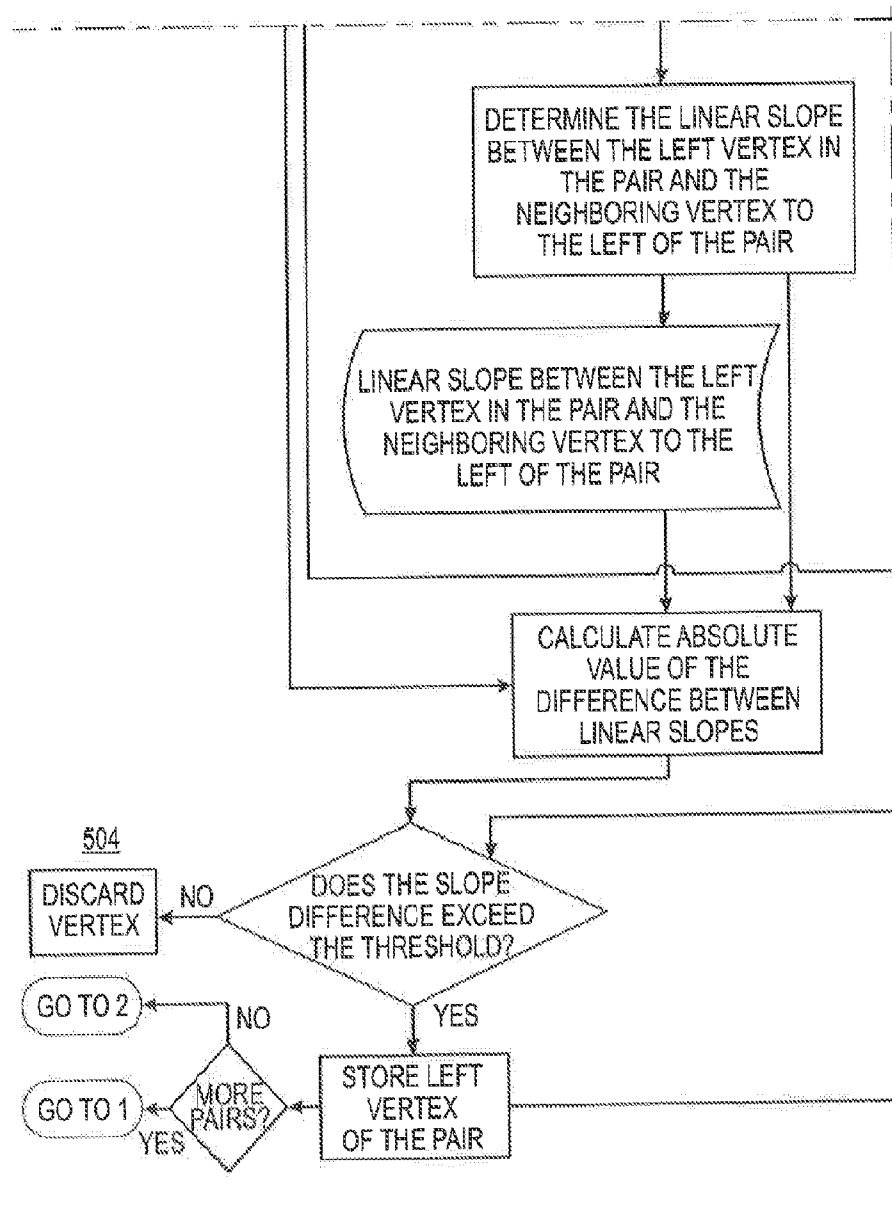


FIG. 5C

SUBSTITUTE SHEET (RULE 26)

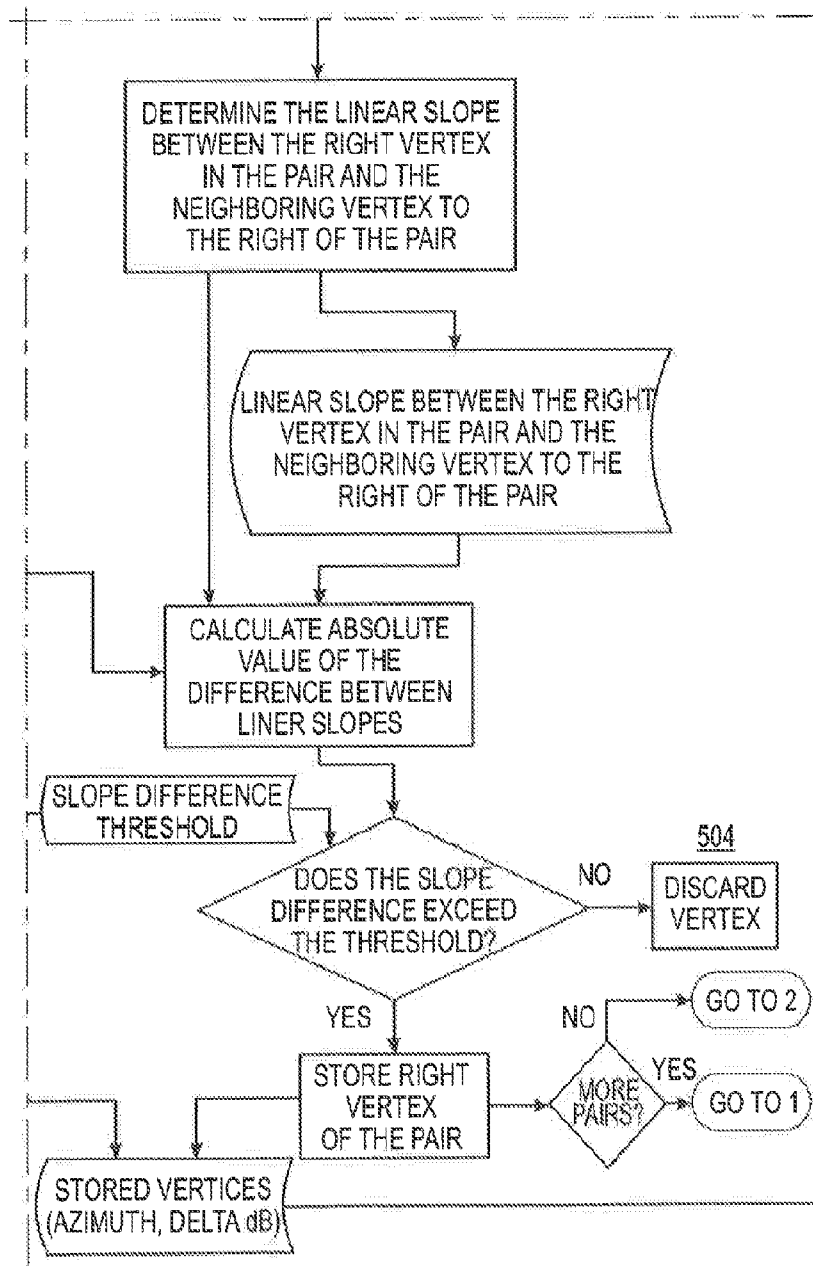


FIG. 5D

SUBSTITUTE SHEET (RULE 26)

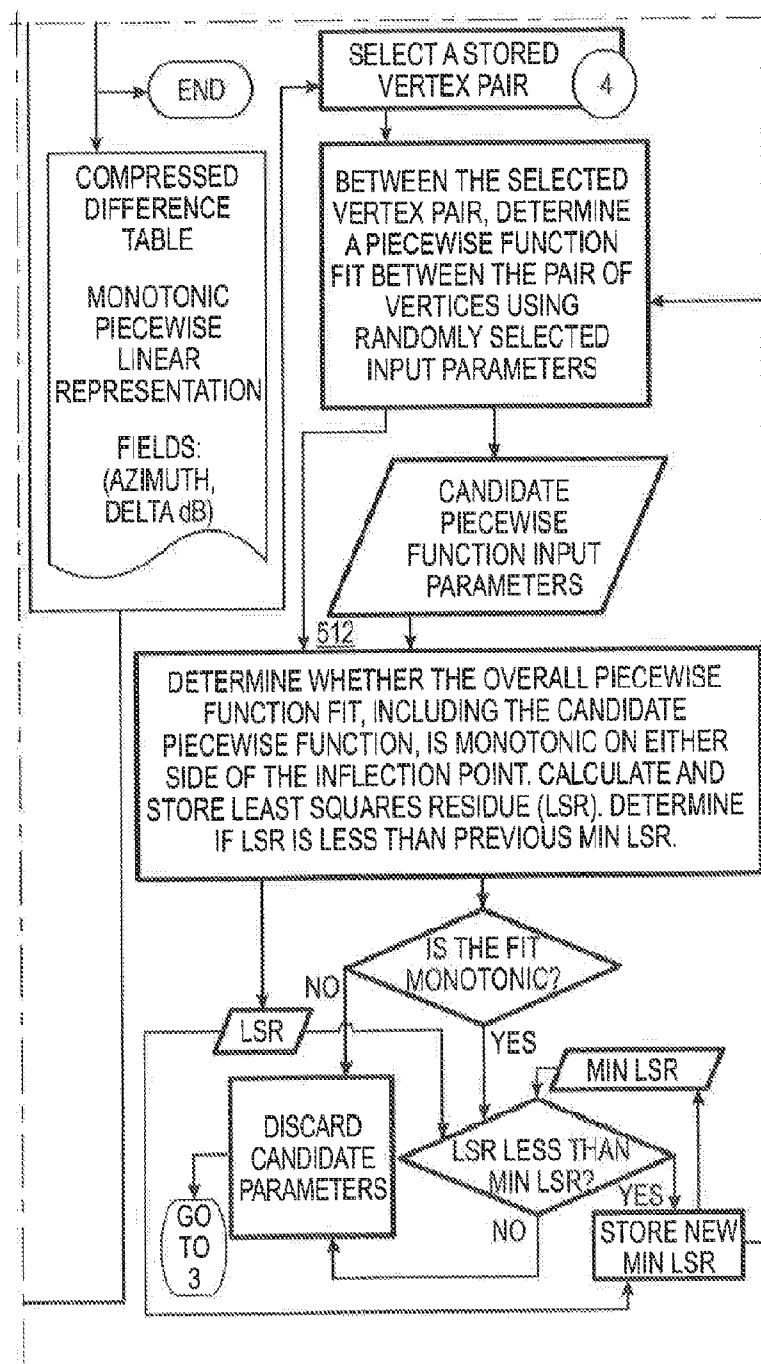


FIG. 5E

SUBSTITUTE SHEET (RULE 26)



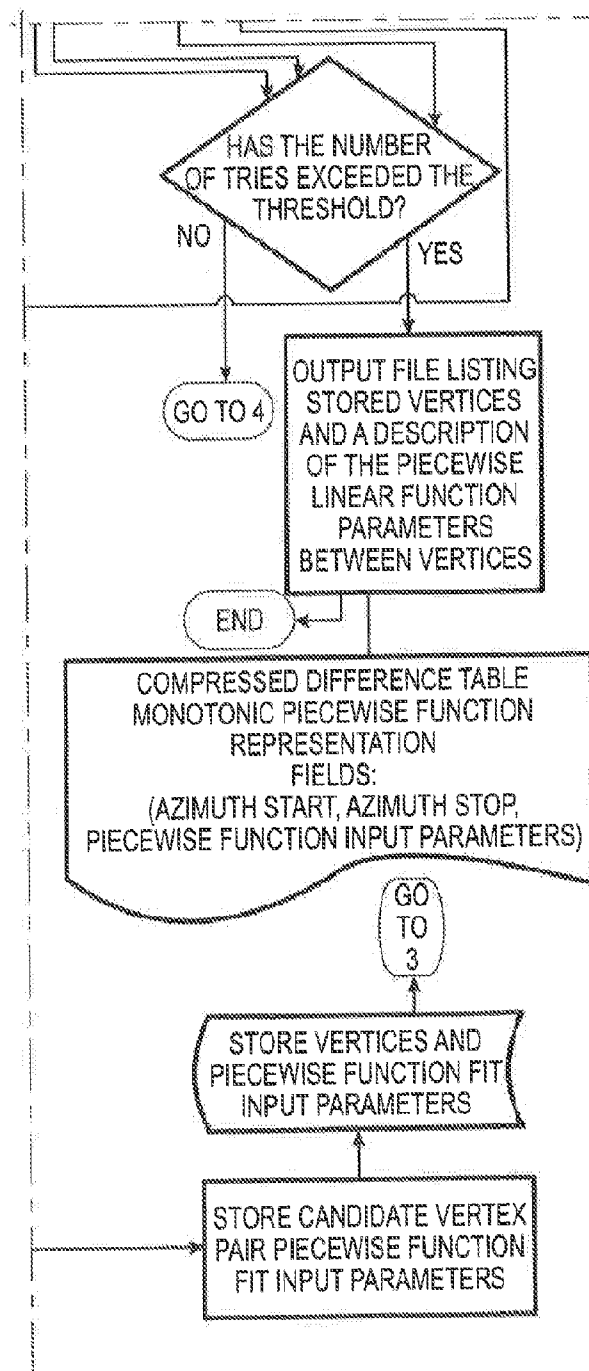


FIG. 5F

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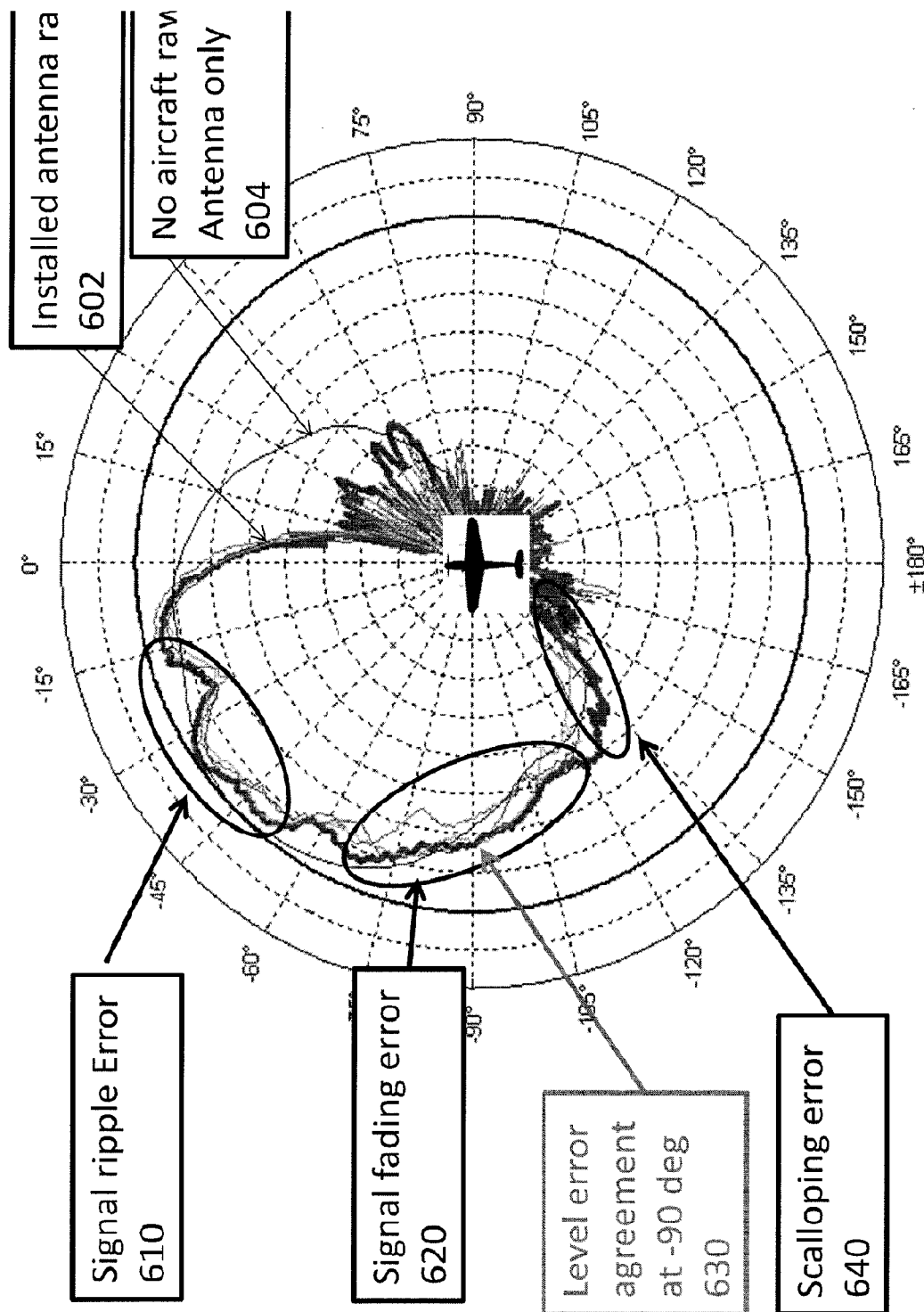


Figure 6

SUBSTITUTE SHEET (RULE 26)

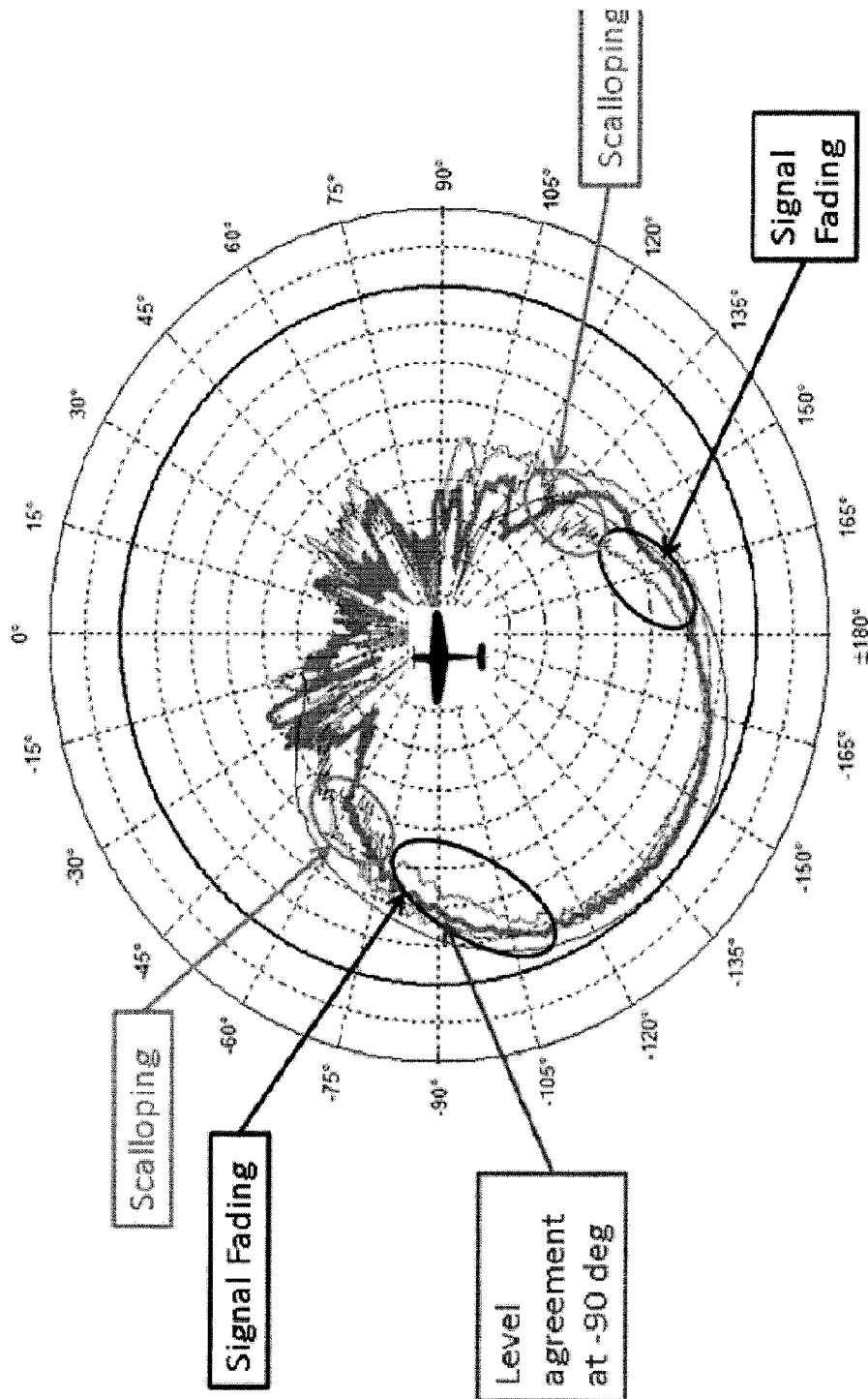


Figure 7

SUBSTITUTE SHEET (RULE 26)

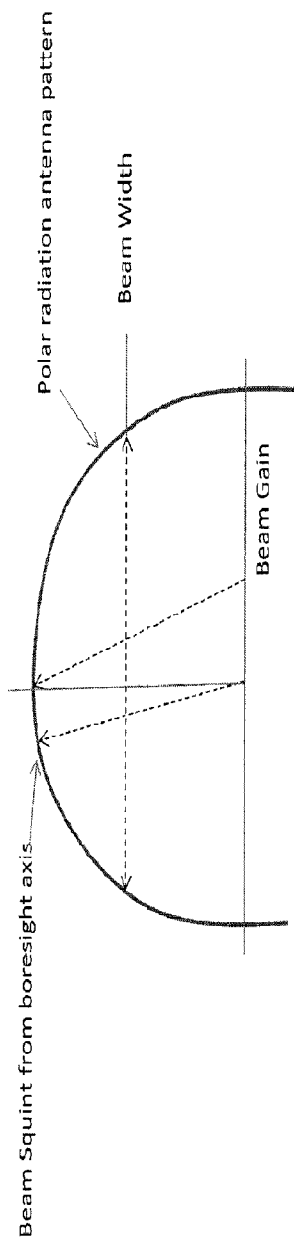
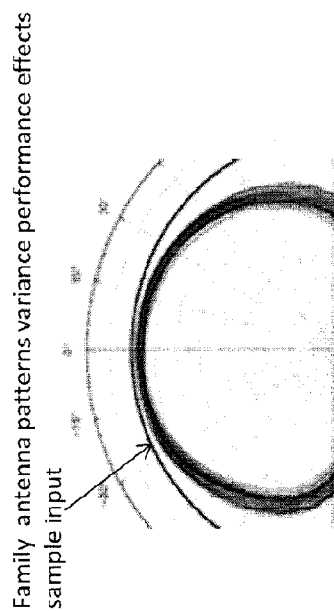
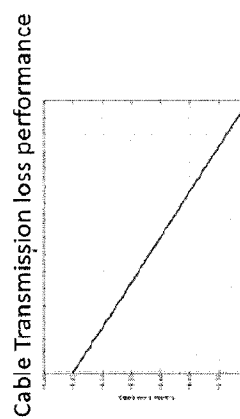


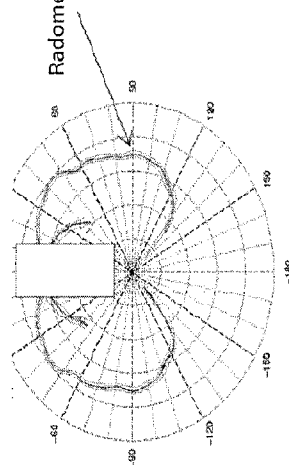
Figure 88



# Microcircuits (such as hybrid, Rf switch sample input



Cable Transmission loss performance



## Figure 9

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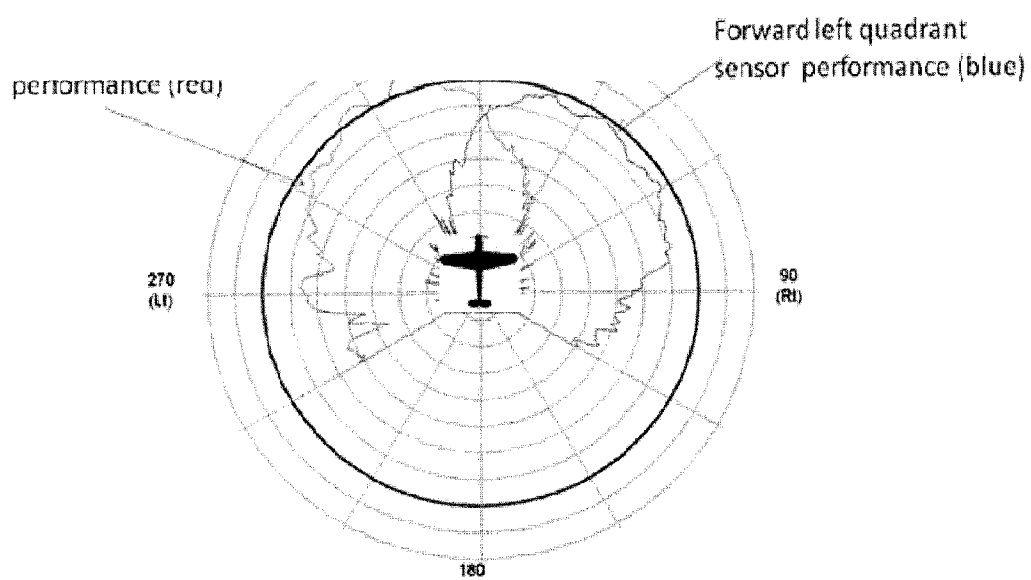


Figure 10

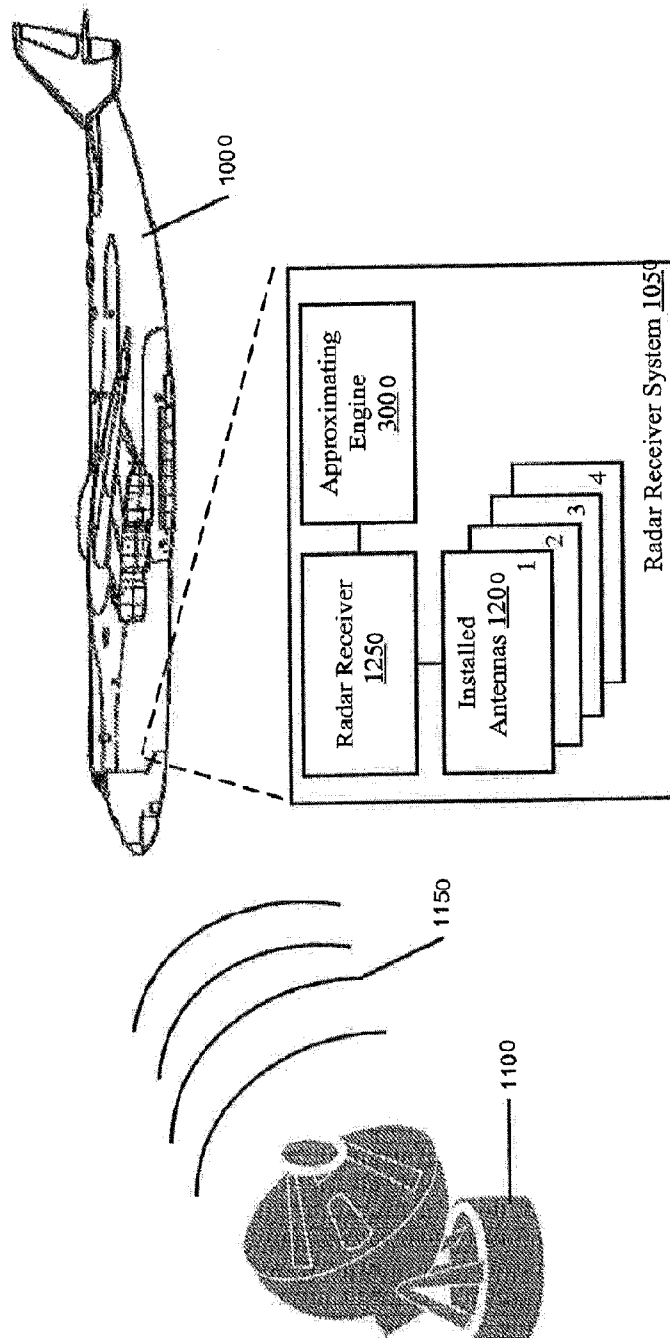


FIG. 11

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# INTERNATIONAL SEARCH REPORT

International application No  
PCT/US2016/023879

## A. CLASSIFICATION OF SUBJECT MATTER

INV. G01S3/02 G01S3/14 G01S7/02  
ADD.

According to International Patent Classification (IPC) or to both national classification and IPC

## B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)

G01S G01R

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

Electronic data base consulted during the international search (name of data base and, where practicable, search terms used)

EP0-Internal, WPI Data

## C. DOCUMENTS CONSIDERED TO BE RELEVANT

| Category* | Citation of document, with indication, where appropriate, of the relevant passages                                                                                                                                           | Relevant to claim No. |
|-----------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------|
| X         | GREGOIRE D G ET AL: "Advanced ESM AOA and location techniques",<br>19890522; 19890522 - 19890526,<br>22 May 1989 (1989-05-22), pages 917-924,<br>XP010086621,<br>Section "LOOK UP ANTENNA CALIBRATION";<br>page 918<br>----- | 1-15,19               |
| X         | US 2015/035696 A1 (HUARD ANDREW [US] ET<br>AL) 5 February 2015 (2015-02-05)<br>cited in the application<br>paragraph [0030] - paragraph [0065];<br>figure 2<br>-----                                                         | 1,16-18,<br>20-23     |
| A         | US 2001/040526 A1 (SMITH MARK D [US])<br>15 November 2001 (2001-11-15)<br>paragraph [0026] - paragraph [0042];<br>figures 3-7<br>-----<br>-/--                                                                               | 1-23                  |



Further documents are listed in the continuation of Box C.



See patent family annex.

\* Special categories of cited documents :

"A" document defining the general state of the art which is not considered to be of particular relevance

"E" earlier application or patent but published on or after the international filing date

"L" document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)

"O" document referring to an oral disclosure, use, exhibition or other means

"P" document published prior to the international filing date but later than the priority date claimed

"T" later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention

"X" document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step when the document is taken alone

"Y" document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art

"&" document member of the same patent family

Date of the actual completion of the international search

1 June 2016

Date of mailing of the international search report

27/06/2016

Name and mailing address of the ISA/

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Authorized officer

Fanjul Caudevilla, J

## INTERNATIONAL SEARCH REPORT

International application No.  
PCT/US2016/023879

### Box No. II Observations where certain claims were found unsearchable (Continuation of item 2 of first sheet)

This international search report has not been established in respect of certain claims under Article 17(2)(a) for the following reasons:

1. ☐ Claims Nos.:  
because they relate to subject matter not required to be searched by this Authority, namely:
2. ☐ Claims Nos.:  
because they relate to parts of the international application that do not comply with the prescribed requirements to such an extent that no meaningful international search can be carried out, specifically:
3. ☐ Claims Nos.:  
because they are dependent claims and are not drafted in accordance with the second and third sentences of Rule 6.4(a).

### Box No. III Observations where unity of invention is lacking (Continuation of item 3 of first sheet)

This International Searching Authority found multiple inventions in this international application, as follows:

see additional sheet

1. ☐ As all required additional search fees were timely paid by the applicant, this international search report covers all searchable claims.
2. ☒ As all searchable claims could be searched without effort justifying an additional fees, this Authority did not invite payment of additional fees.
3. ☐ As only some of the required additional search fees were timely paid by the applicant, this international search report covers only those claims for which fees were paid, specifically claims Nos.:
4. ☐ No required additional search fees were timely paid by the applicant. Consequently, this international search report is restricted to the invention first mentioned in the claims; it is covered by claims Nos.:

#### Remark on Protest

- ☐ The additional search fees were accompanied by the applicant's protest and, where applicable, the payment of a protest fee.
- ☐ The additional search fees were accompanied by the applicant's protest but the applicable protest fee was not paid within the time limit specified in the invitation.
- ☐ No protest accompanied the payment of additional search fees.



**FURTHER INFORMATION CONTINUED FROM PCT/ISA/ 210**

This International Searching Authority found multiple (groups of) inventions in this international application, as follows:

1. claims: 1-23

Method for generating a look-up table for determining an angle of arrival (AoA) of a radar signal received from an emitter.

1.1. claim: 23

Method for compressing data in a pattern difference look-up table.

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# INTERNATIONAL SEARCH REPORT

International application No  
PCT/US2016/023879

C(Continuation). DOCUMENTS CONSIDERED TO BE RELEVANT

| Category* | Citation of document, with indication, where appropriate, of the relevant passages                                                                           | Relevant to claim No. |
|-----------|--------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------|
| A         | <p>US 5 541 608 A (MURPHY MYLES P [US] ET AL)<br/> 30 July 1996 (1996-07-30)<br/> column 6, line 35 - column 10, line 52;<br/> figures 5-10</p> <p>-----</p> | 1-23                  |

# INTERNATIONAL SEARCH REPORT

Information on patent family members

International application No

PCT/US2016/023879

| Patent document<br>cited in search report | Publication<br>date | Patent family<br>member(s)                                                                                             | Publication<br>date                                                                            |
|-------------------------------------------|---------------------|------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------|
| US 2015035696 A1                          | 05-02-2015          | AU 2014296789 A1<br>CA 2917947 A1<br>EP 3028062 A1<br>US 2015035696 A1<br>WO 2015017010 A1                             | 07-01-2016<br>05-02-2015<br>08-06-2016<br>05-02-2015<br>05-02-2015                             |
| US 2001040526 A1                          | 15-11-2001          | AU 1570101 A<br>CA 2387374 A1<br>CN 1402836 A<br>EP 1226450 A1<br>JP 2003511706 A<br>US 2001040526 A1<br>WO 0127650 A1 | 23-04-2001<br>19-04-2001<br>12-03-2003<br>31-07-2002<br>25-03-2003<br>15-11-2001<br>19-04-2001 |
| US 5541608 A                              | 30-07-1996          | AU 692386 B2<br>AU 5418696 A<br>DE 69618814 D1<br>DE 69618814 T2<br>EP 0868668 A1<br>US 5541608 A<br>WO 9630779 A1     | 04-06-1998<br>16-10-1996<br>14-03-2002<br>18-07-2002<br>07-10-1998<br>30-07-1996<br>03-10-1996 |