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H4F

H4T

Selected US specifications from IPC sub-class H04N

(54) **Video scanning using a fractal curve**

(57) Conventionally, transmission of television images is performed by Raster scanning. To avoid the problems associated with flyback, and the limiting of Raster scanning to image scanning standards it is proposed to transmit images by scanning along a locus defined by a fractal curve. A Peano curve is particularly suitable. Image resolution may be varied by varying the order of curve used to scan the image. Smoothing of a curve of a given order results in a graceful degradation to a curve of lower order so that the image created by a given order is still recognisable when displayed by a lower or high order.

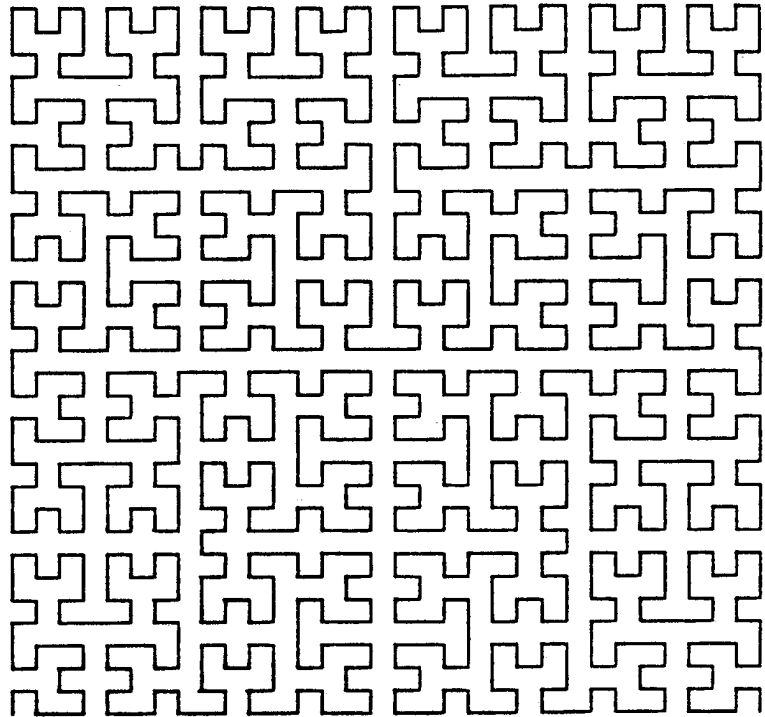
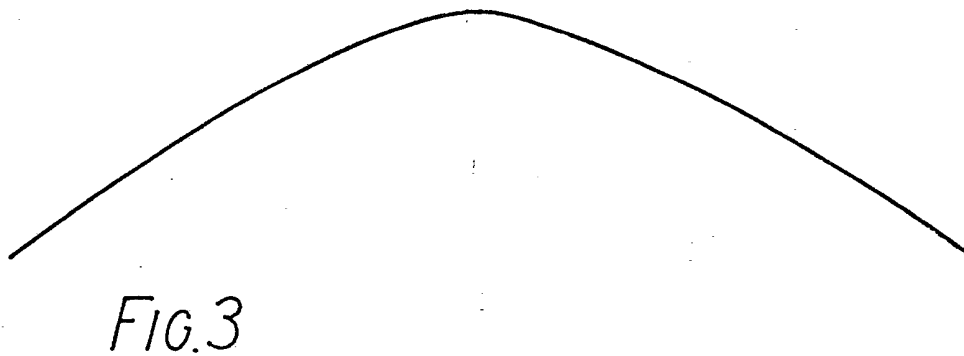
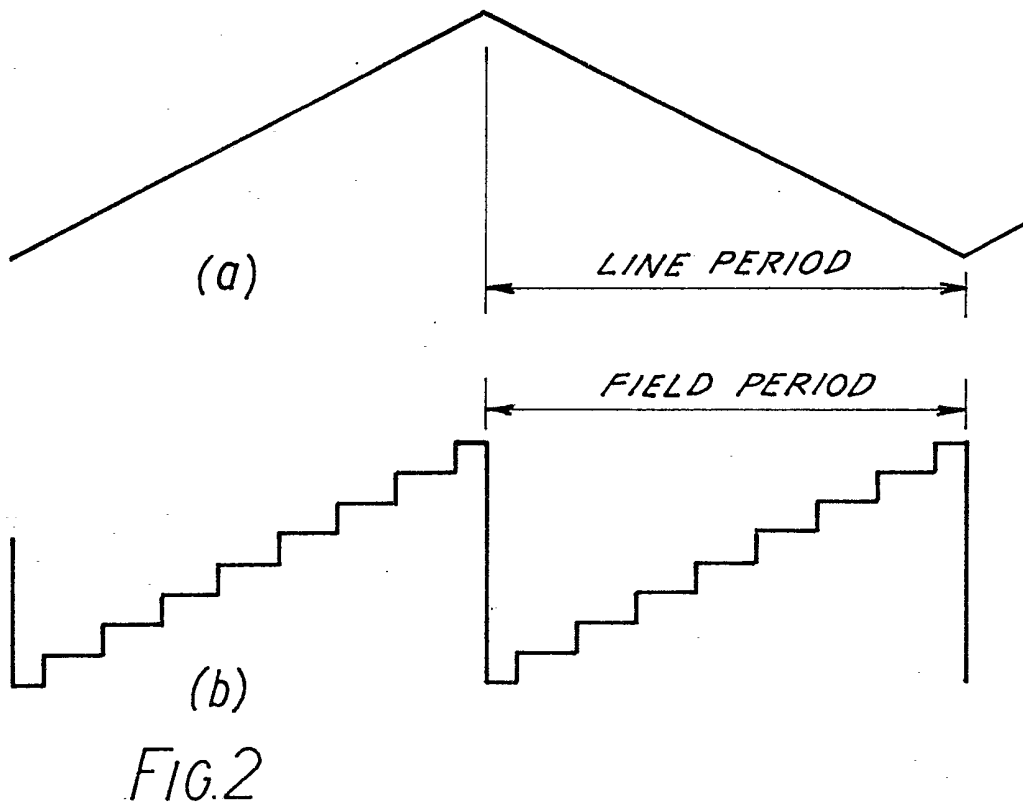
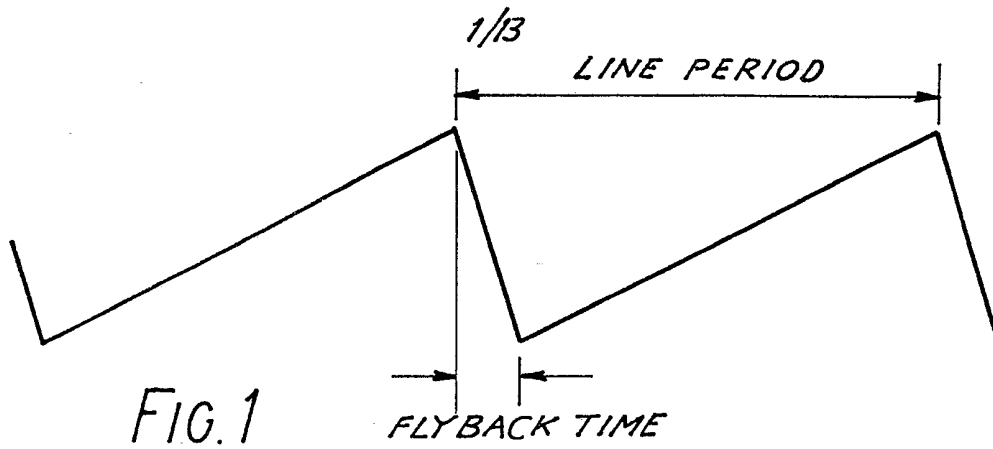


FIG. 5

GB 2 193 411 A



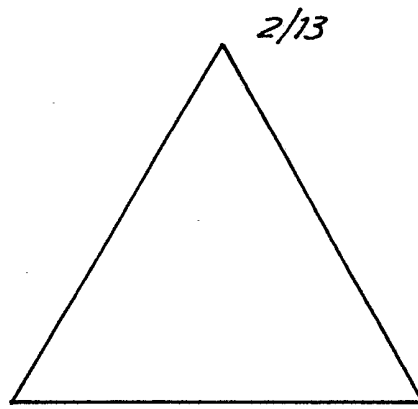


FIG.4b

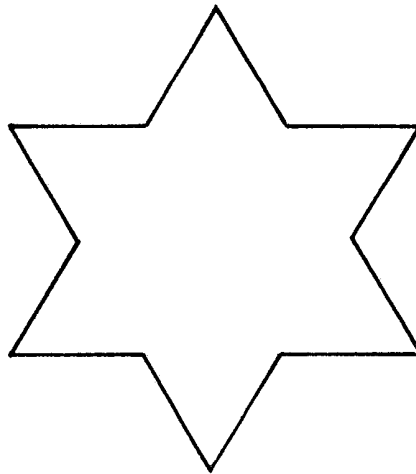


FIG.4c

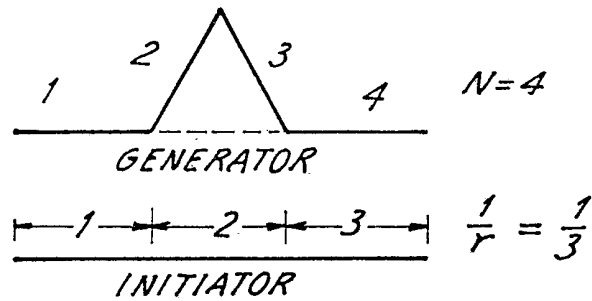


FIG.4a

3/13

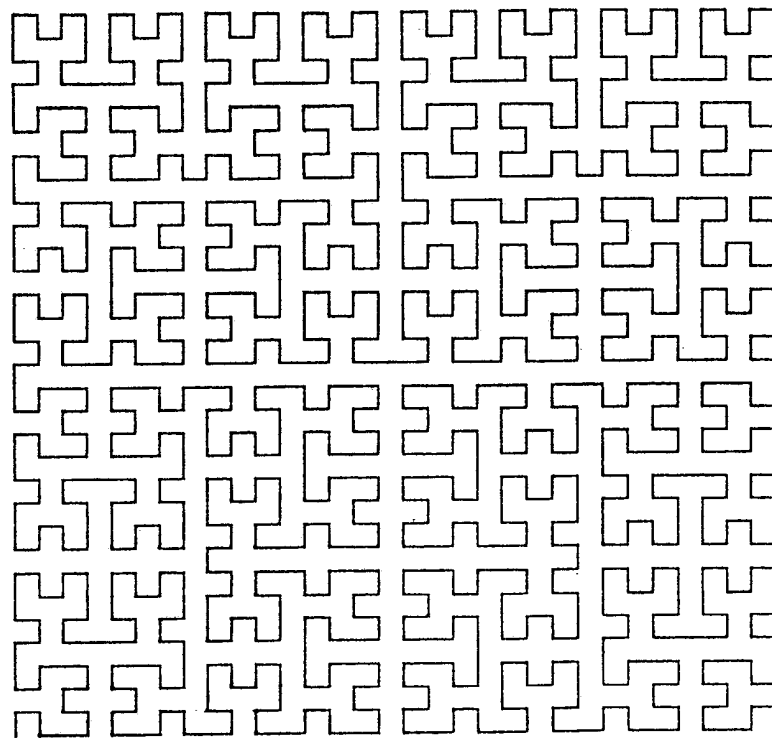


FIG. 5

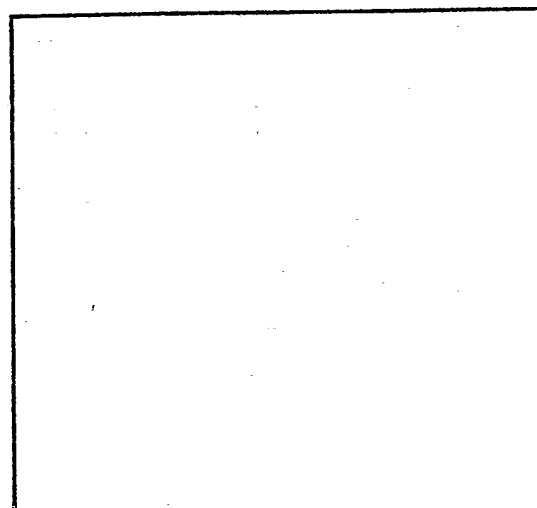


FIG. 6

4/13

FIG. 7

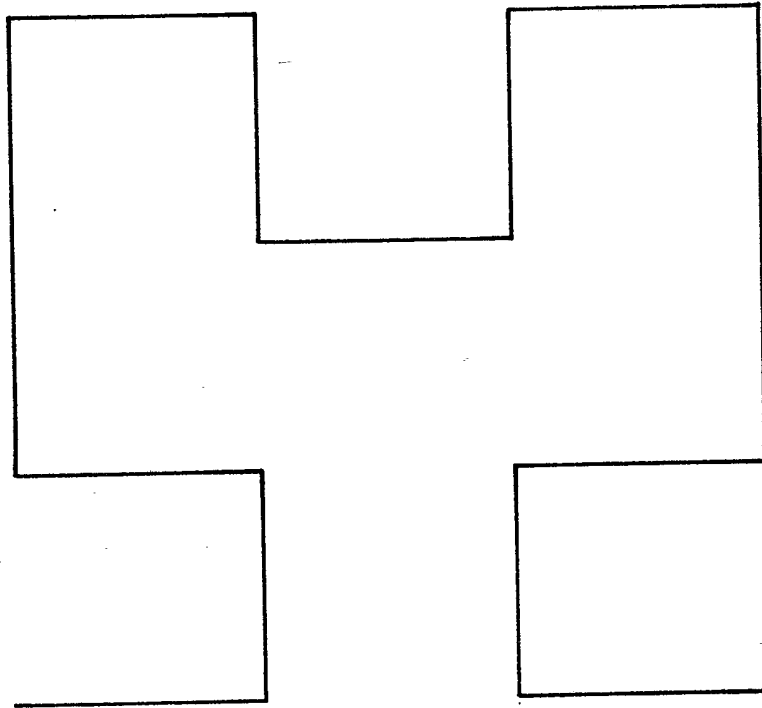


FIG. 8

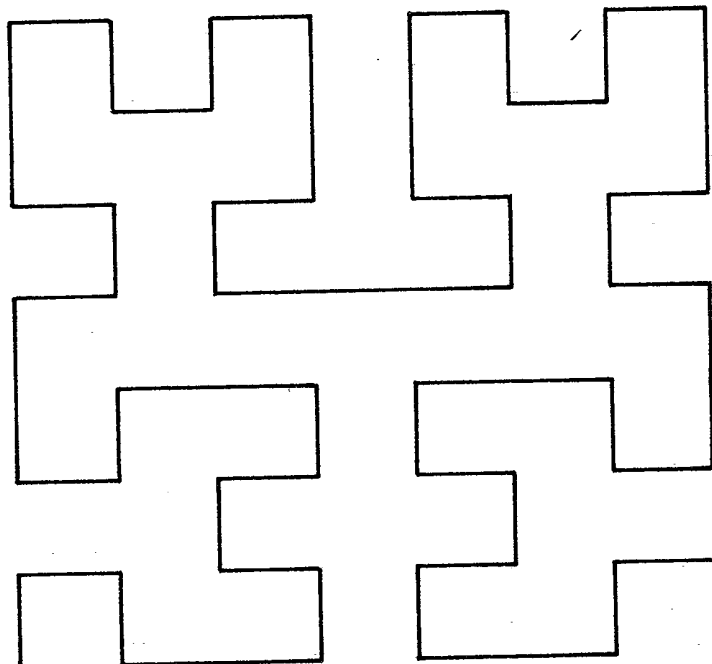


FIG. 9

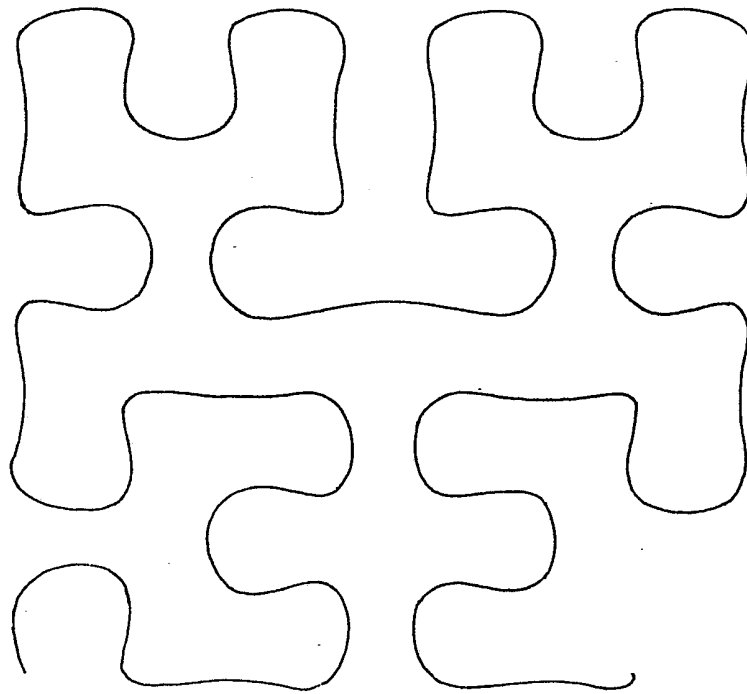
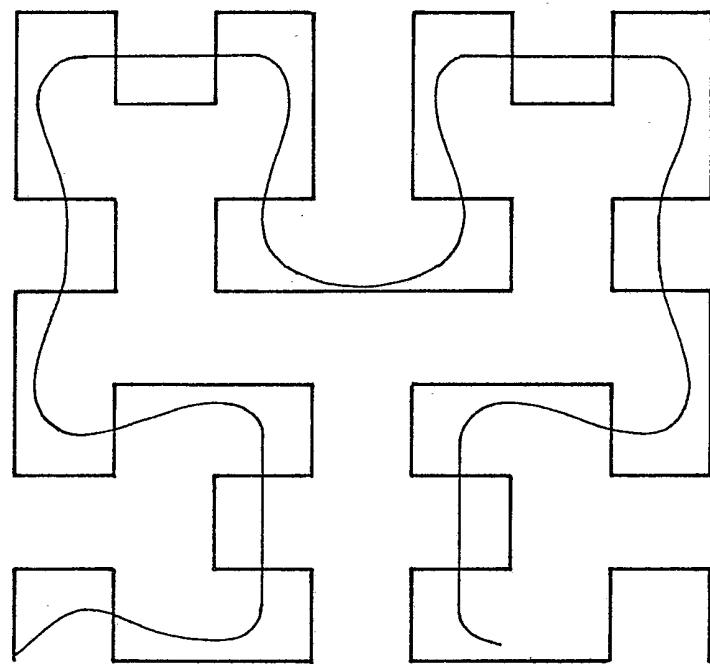


FIG. 11



6/13

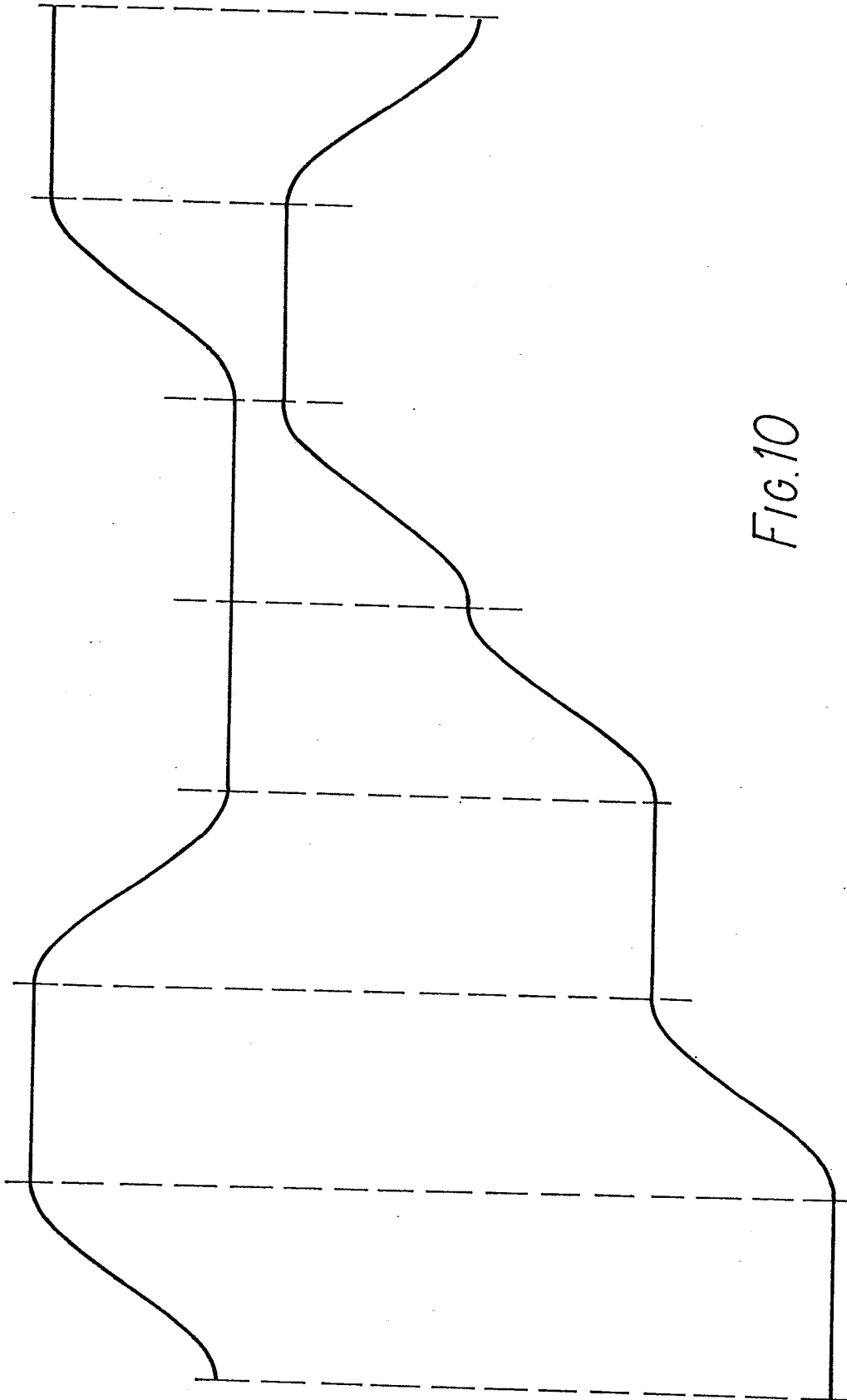


FIG.10

7/13

FIG.12

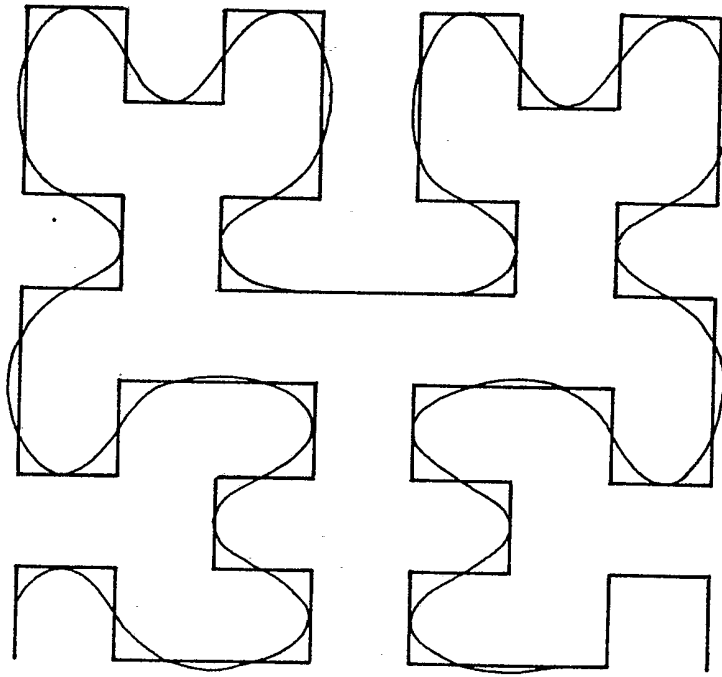
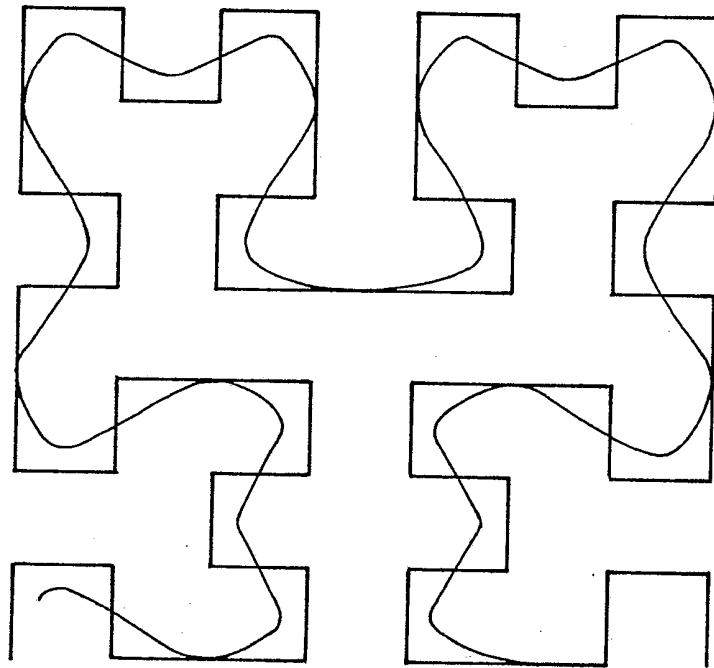


FIG.13



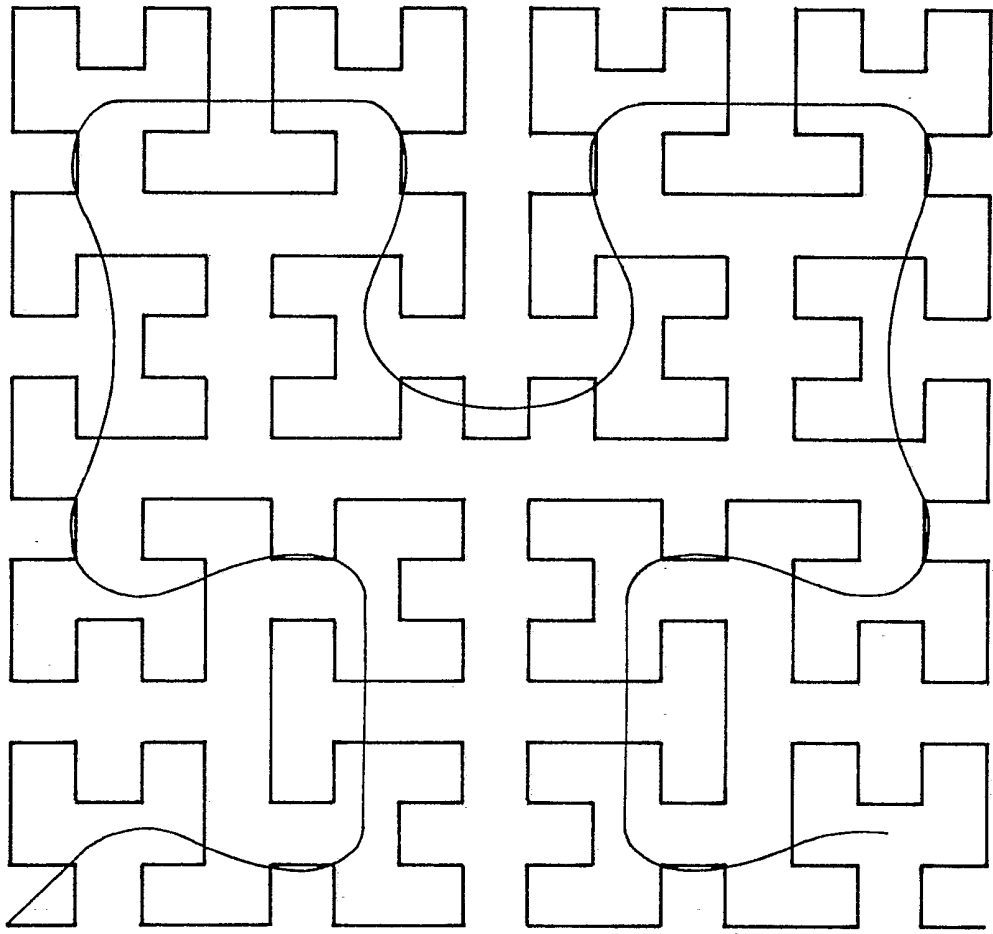


FIG. 14

9/13

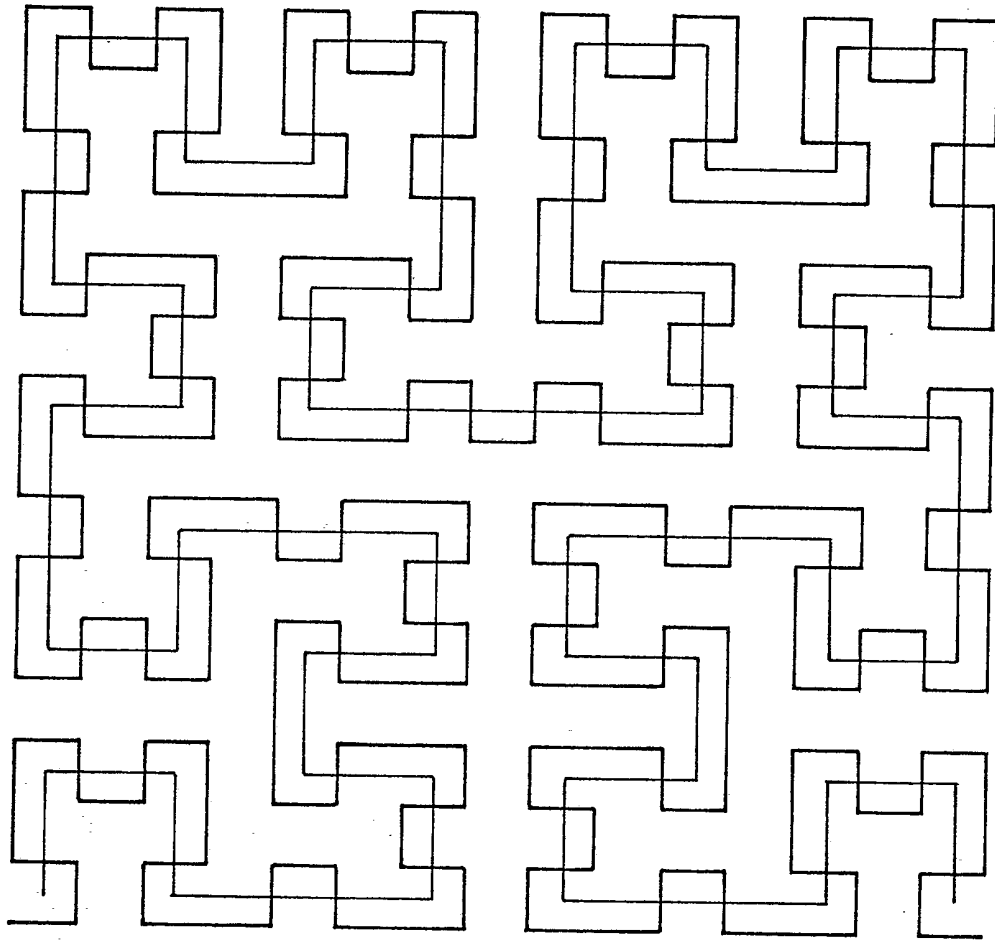


FIG. 15

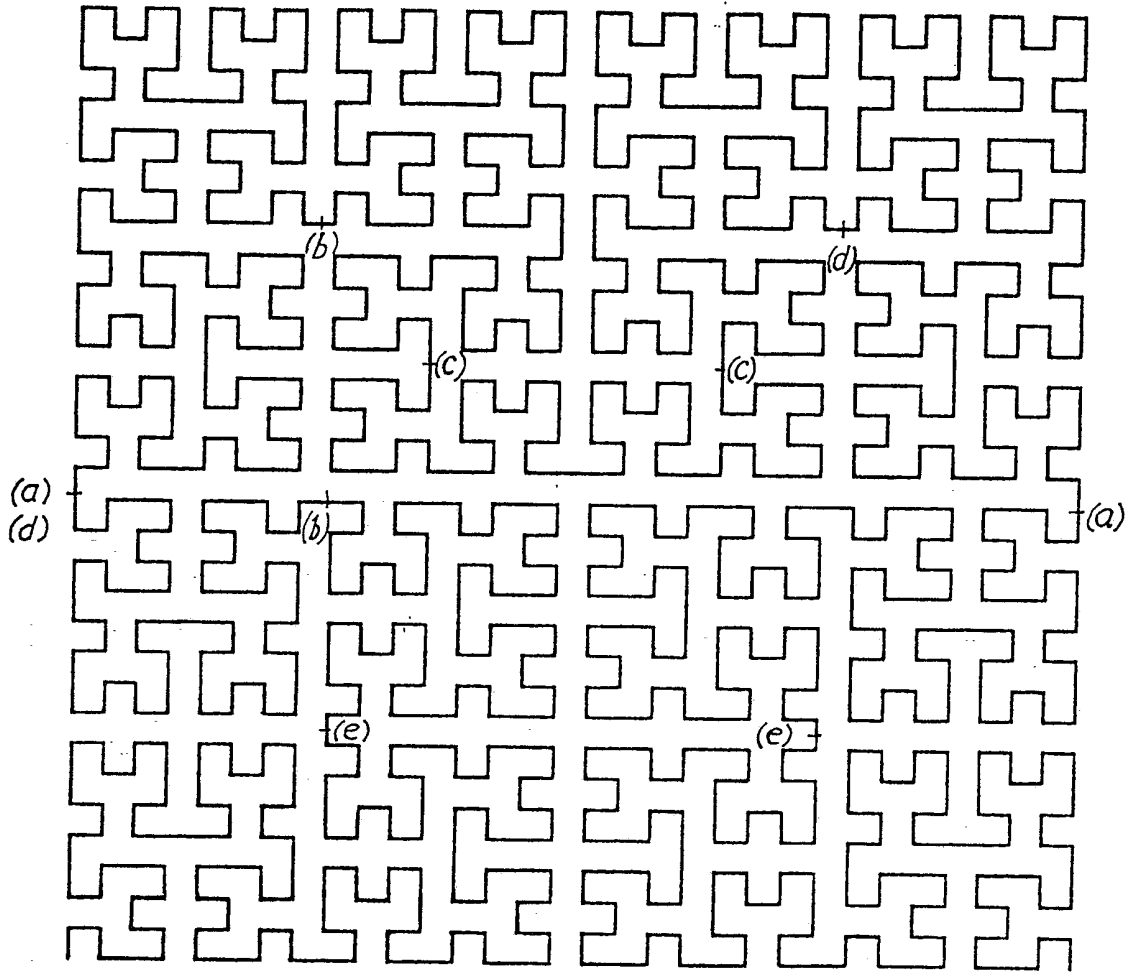


FIG. 16

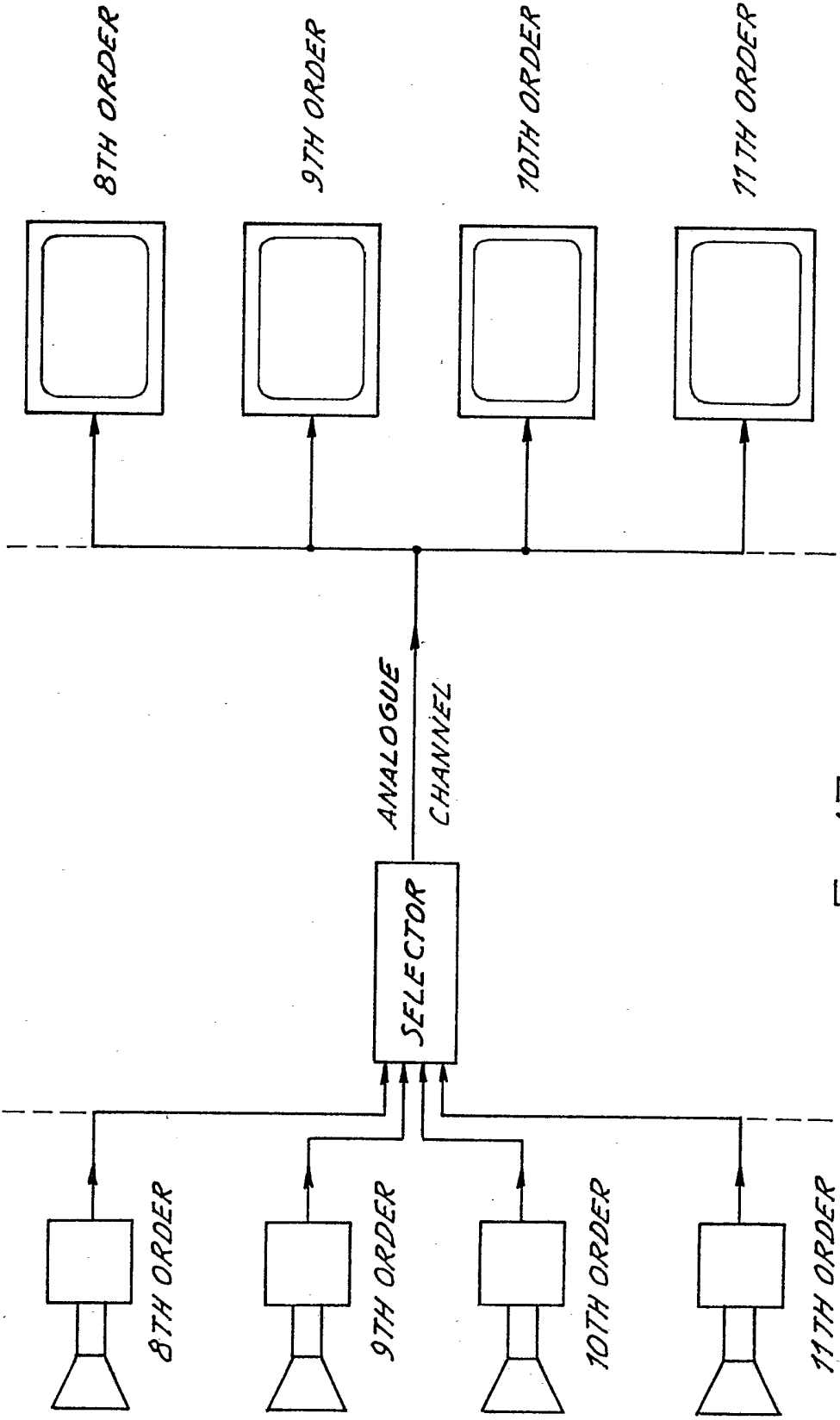


FIG.17

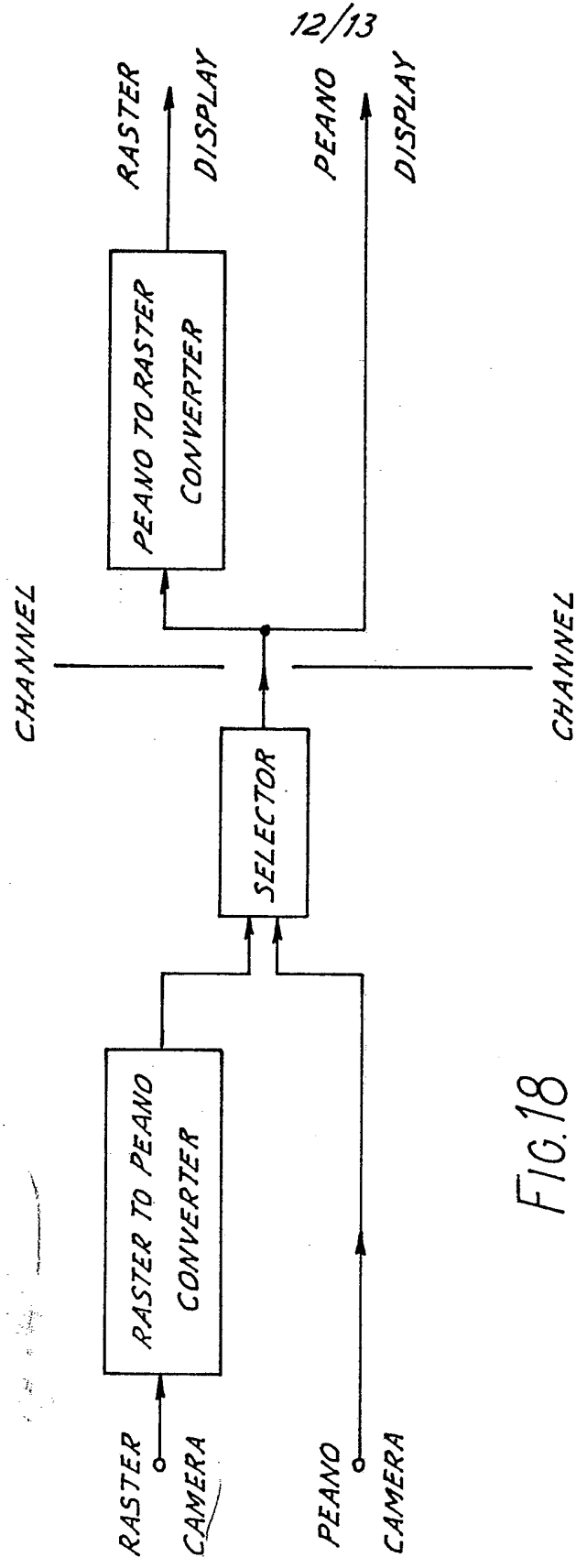


FIG. 18

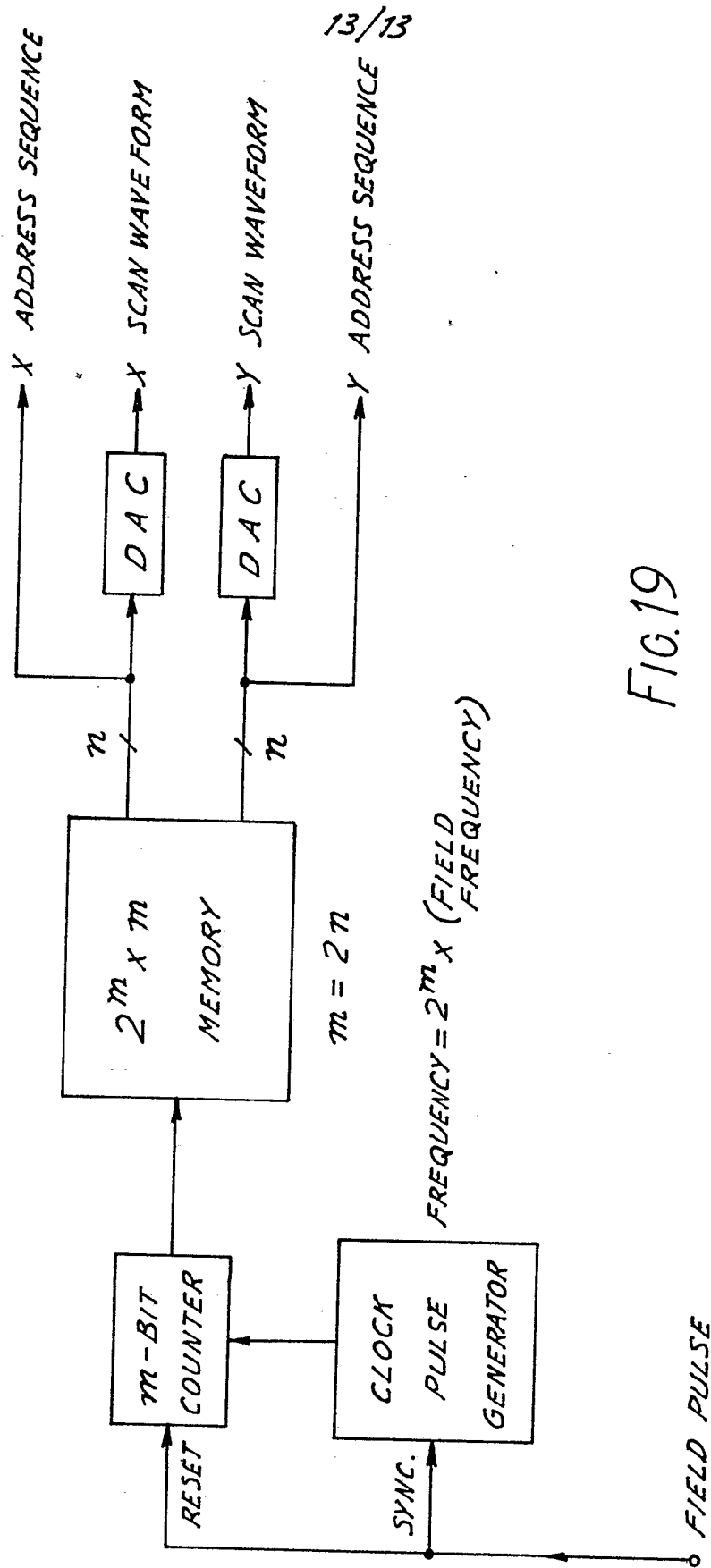


FIG.19

SPECIFICATION

Video scanning systems

- 5 This invention relates to video scanning systems for use for example in television. 5
- Transmission of images by television is conventionally performed by raster scanning in which a signal is formed by scanning the image in a series of parallel lines, either horizontal or vertical. In broadcast television the scan starts at the top left hand corner and finishes at the bottom right hand corner, the scan lines being horizontal. Moreover, each line is scanned in the same
- 10 direction so that the scan must return to the beginning of each line in, ideally, an infinitesimally short time. Such an action is known as the flyback. 10
- The scanning in conventional imaging and display devices is by way of a continuously moving electronic beam which is deflected by electric or, usually, magnetic fields. With such devices the beam flyback takes a finite time which is, therefore, an "overhead". The horizontal scanning
- 15 waveform, which is proportional to the deflecting field, therefore appears as in Figure 1, the idealised version of which is known as a sawtooth waveform. 15
- Similarly, the vertical scanning waveform needed to ensure the equal spacing of the scan lines is another sawtooth, though of much lower frequency. This has a corresponding flyback, imposing a further "overhead". It should be noted that the continuous nature of the vertical scan
- 20 imposes a continuous vertical displacement on the scan lines so that they are not strictly horizontal. However, the skew thus imposed is negligible. 20
- The large rate of change of the flyback in the horizontal scan waveform is used to provide the high voltage needed in a conventional CRT display. However, it can cause problems if the line rate is increased to provide scanning for higher definition formats since the flyback time of
- 25 conventional deflection circuits may become a significant proportion of the line period. For this reason, UK Patent Application 2,137,844A has proposed a boustrophedonic scanning format in which lines are alternately scanned in opposite directions. This requires a triangular form for the horizontal scan waveform as shown in Figure 2 (a). This eliminates the flyback, but the sawtooth
- 30 of the vertical scan must now be modified to a stepped form as shown in Figure 2 (b) to ensure that adjacent lines are parallel. It also requires that non-linearities in the horizontal scan waveform result in a symmetrical function as shown in Figure 3. 30
- A disadvantage of raster-based scanning is that it is committed to a standard in the form of lines in the picture. This means that once an image scanning standard is chosen the display must adopt the same standard, or convert the incoming signal to its own line standard, which is
- 35 a complex and costly process. Moreover, any curtailment in the bandwidth of an analogue channel used to carry the signal will affect only the horizontal resolution of the image, not the vertical resolution. Excessive curtailment will therefore give an unacceptable image quality, inferior to that which could be obtained with equal horizontal and vertical resolutions. 35
- The present invention is defined by the appended claims to which reference should now be
- 40 made. 40
- The invention is applicable to both analogue and digital scans. In the former case the image is scanned along a trace formed by a defined co-ordinate sequence, and in the latter case the pixels of the image are scanned in that co-ordinate sequence.
- We have appreciated that it would be possible to have a scanning format which is not
- 45 committed to a line standard and therefore is open to evolution, i.e., the image scanning may be upgraded in acuity without needing a change in the structure of the display. This means that it is downwards compatible. Moreover, it is possible for such a format to be upwards compatible such that the display can be upgraded without changing the source scanning format. Such a technique relies on the use of FRACTALS for defining the scanning locus. 45
- 50 Fractals may be described as structures whose length is undefinable or infinite as the finer the scale used to observe the structure, the greater the apparent length. An example of such a structure is a coastline. The closer it is observed, the greater its length becomes as finer detail becomes resolved. 50
- Such self-similar shapes are neither one- nor two-dimensional shapes as they are defined by conventional Euclidian geometry. That is, they have a fractional dimension. 55
- 60 Fractals may be identical on each level or scale, or may be irregular. A coastline is an irregular fractal. Figure 4 shows how a regular fractal may be generated. This example is the well known Koch curve or Koch snowflake. The straight sides of an equilateral triangle Fig. 4b (the initiator shown in Figure 4a) are operated on by a generator shown in Figure 4a. This operation produces the result shown in Figure 4c. The operator is then applied to each of the sides of the shape of Figure 4c and then subsequently to the sides of the resultant figure, and so on. The result is a figure resembling a snowflake. 60

It can be shown that the fractal dimension can be defined as

$$D = - \log (N) / \log \left(\frac{1}{r} \right)$$

5 5

where N is the number of parts of the object generated and $\frac{1}{r}$ is the similarity ratio which is used to divide the initiator. For the

10 Koch curve of Figure 4; $N = 4$ and $\frac{1}{r} = \frac{1}{3}$ 10
so that $D = 1.26$

A fuller description of fractals can be found in the book: Mandelbrot FRACTALS—Form,
15 Chance and Dimension, W.H. Freeman, ISBN 0-7167-0473-0. The use of fractals in the field of 15
computer graphics to simulate texture is well established. The use of a fractal curve to explore a
multi-dimensional space is known from Stevens, R.J., Lehar, A.F. and Preston, F.H. 1982, "Data
ordering and compression of multi-spectral images using the Peano scan", International Confer-
ence on electronic image processing 26-28 July and compression of multi-spectral images using
20 the Peano scan", International Conference on electronic image processing 26-28 July 1982, IEE 20
conference publication No. 214 pages 209-213. However, the use of a fractal curve to scan an
image for transmission and display, with its attendant advantages is thought to be novel.

The invention will be disclosed in terms of a particular fractal El Peano curve, named after the
Italian mathematician Giuseppe Peano, see "Selected works of Guiseppe Peano" translated and
25 edited by Hubert C. Kennedy, ISBN 0-04-164002-0, Allen and Unwin. It is also called Hilbert 25
curve. However, other forms of fractal may be more suitable, in particular the Sierpinski curve,
described by Writh, N. in "Algorithms + data structures = programs", Prentice-Hall Inc., ISBN
0-13-022418-9 pages 134-137. In general, the curve may be multi-dimensional; only the two
dimensional form is discussed in detail here.

30 The invention will be described by way of example with reference to the drawings, in which: 30

Figure 1 (referred to above) illustrates the sawtooth waveform of conventional raster scanning;

Figure 2 (referred to above) shows the waveforms required for boustrophedonic scanning in (a)
the horizontal (b) the vertical directions;

Figure 3 (referred to above) illustrates the permissible non-linearity of the horizontal scan in
35 boustrophedonic scanning; 35

Figure 4 (referred to above) illustrates the steps in generating a Koch curve;

Figure 5 illustrates a fifth-order (32×32) Peano curve;

Figure 6 illustrates a first-order (basic) Peano curve;

Figure 7 illustrates a second-order Peano curve;

40 Figure 8 illustrates a third-order Peano curve; 40

Figure 9 shows the smoothed third-order curve resulting from band-limiting the coordinate
waveforms fairly sharply to half the pixel frequency;

Figure 10 illustrates a portion of the horizontal and vertical waveforms interpolated by a raised
cosine filter;

45 Figure 11 illustrates the effect of four-fold averaging and interpolation (filtering) of the scan; 45

Figure 12 illustrates the effect of two-fold averaging of the scan;

Figure 13 illustrates the effect of three-fold averaging of the scan;

Figure 14 illustrates the effect of 16-fold averaging of the scan;

Figure 15 illustrates the superposition of the third and fourth-order scans;

50 Figure 16 shows the starting and finishing points for various aspect ratios: (a) 2:1 (b) 3:1 (c) 50
4:1 (d) 3:2 (e) 4:3;

Figure 17 is a block diagram of a television system embodying the invention;

Figure 18 is a block diagram illustrating conversion for compatibility with the current techno-
logy; and

55 Figure 19 is a block diagram of a basic circuit for generating an n-th order scan. 55

Figure 5 shows a two-dimensional fifth-order Peano curve, i.e., a curve connecting an array of
 32×32 points. Close inspection shows that it can be divided into quarters, each of which is
connected by a single step. The quarters, in turn, can be further subdivided into quarters, again
connected by only a single step, and so on. Further, the quarters are seen to be replicas, either
60 directly or rotated through a right angle. 60

Figures 6, 7 and 8 show the first, second and third order curves respectively. It can be seen
that each order is derived from the previous order according to simple geometrical rules.

Alternatively, the derivation of each order can be considered by way of the Cartesian coordinate
sequences as shown in the Appendix below. These sequences, when interpolated, are the
65 waveforms that would need to be applied to the horizontal and vertical deflection circuits of a 65

Table 1		Table 2				
x	y	x	y	x	y	
5						5
	0	00	00	10	10	
	0	01	00	10	11	
10	1	01	01	11	11	10
	1	00	01	11	10	
		00	10	11	01	
15		00	11	10	01	15
		01	11	10	00	
		01	10	11	00	
20						20

Table 3									
	x	y	x	y	x	y	x	y	
	000	000	000	100	100	100	111	011	
30	000	001	001	100	101	100	111	010	30
	001	001	001	101	101	101	110	010	
	001	000	000	101	100	101	110	011	
35	010	000	000	110	100	110	101	011	35
	011	000	000	111	100	111	100	011	
	011	001	001	111	101	111	100	010	
40	010	001	001	110	101	110	101	010	40
	010	010	010	110	110	110	101	001	
	011	010	010	111	110	111	100	001	
45	011	011	011	111	111	111	100	000	45
	010	011	011	110	111	110	101	000	
	001	011	011	101	111	101	110	000	
50	001	010	010	101	110	101	110	001	50
	000	010	010	100	110	100	111	001	
	000	011	011	100	111	100	111	000	
55									55

Development of the higher order cases proceeds along the same rules. The third-order case, shown in Table 3, has 64 entries of three bit values, the sequences of the first two bits of x and y being the same as those of the corresponding second-order case, each entry being replicated four times. The least significant bit of the x coordinate has the sequence XXXX YXXY YXXY X Y Y X where X and Y represent the same sequences as before. It can be seen that the initial sequence of each group of four follows the same pattern as the sequences in the first group. Likewise, the least significant bit of the y coordinate has the sequence YXXY XXXX XXXX Y X X Y. It will be noted that the least significant bits are appropriately palindromic or complementary palindromic.

images such that an image scanned by one member of the family may be displayed by another member of the family without knowledge of the first member. Such an arrangement allows an evolution of scanning acuity to occur.

5 An apparent theoretical objection to the idea is that it can be applied only to square arrays of points. Arbitrary image aspect ratios are not possible. However, ratios of 2:1 3:1 4:1 3:2 and 4:3 are possible by starting and finishing at the points shown in Figure 16. Small deviations from these values are possible by altering the pixel aspect ratio without departing significantly from the spirit of isotropic resolution. 5

10 Because the scan is contiguous there is no flyback except between fields and thus time is saved. Even field flybacks may be eliminated by using a modified square scan consisting of two 2:1 scans joined at their endpoints. Alternatively, a Sierpinski curve may be used which has an inherently endless form. In such a case, synchronising information would have to be sparse, compared with the present systems, possibly consisting of a recognisable framing pattern. 10

15 The system is particularly suitable for use with imaging and display devices which are based on discrete rather than continuous scanning. These include systems comprising cameras based on charge-coupled devices (CCDs) for example. Addressable display devices would be particularly suitable. 15

An outline block diagram of a television system embodying the invention is shown in Figure 17. Synchronised cameras operating with various orders of scan may be selected at will and their signals transmitted through the channel. The ninth-order scan camera represents, approximately, the current system. The eighth order scan camera represents, say, a low-resolution lightweight 'electronic journalism' camera whilst the 10th-order scan camera represents a high definition camera. They could be used in different programmes or even in the same programme. The 11th-order scan camera represents a camera which could be developed in the future, being introduced when required. The same remarks apply to the hierarchy of displays, the eighth-order display representing, say, a wrist-watch receiver based on a liquid crystal display. 20 25

The system is capable of being introduced piecemeal and so thus coexisting with current scanning technology. If it were introduced on the channel then compatibility with current technology would require raster-to-Peano converters in conventional cameras and Peano-to-Raster converters in conventional displays, as shown in Figure 18, the converters merely re-ordering the sequence of incoming pixel values. Such converters would consist simply of a picture store which would write the pixel data in one sequence and read it in another. This re-ordering of data could also be regarded as a scrambling technique to prevent unauthorised reception of a newly-introduced service. 30

35 The scan could be generated using a memory addressed by a counter as shown in Figure 19. An nth order scan would require a memory of 2^{2n} locations, each of $2n$ bits, containing n -bit x and y values and a $2n$ -bit memory counter able to count from 0 to $2^{2n} - 1$. The contents of the memory could be derived according to the method described in the appendix below. The two outputs of the memory can be used directly to address a discrete scanning device. 40

40 However, for a continuous scanning device the memory outputs need to be fed to two n -bit digital-to-analogue converters to produce continuous wave forms. 40

APPENDIX DERIVATION OF THE SEQUENCES

45 The x and y coordinate sequences for the first order case of Figure 6 are shown in Table 1, in units of the scan step. The y sequence is a palindrome and the x sequence is a complementary palindrome. The coordinate sequences of the second-order case, written in binary form, are shown in Table 2. As there are 4×4 points, each coordinate requires 2 bits and there are 16 entries. The more significant bit is seen to be a replication of the corresponding first-order pattern, each entry being replicated four times. The less significant bit is seen to be the sequence YXXY for the x coordinate or XYYX for the y coordinate where X and Y are the first-order patterns of the x and y coordinates. The first of these sequences is a complementary palindrome and the second is a palindrome. 50

Table 1		Table 2				
x	y	x	y	x	y	
5						5
	0	00	00	10	10	
	0	01	00	10	11	
10	1	01	01	11	11	10
	1	00	01	11	10	
		00	10	11	01	
15		00	11	10	01	15
		01	11	10	00	
		01	10	11	00	
20						20

Table 3

25	x	y	x	y	x	y	x	y	25
	000	000	000	100	100	100	111	011	
30	000	001	001	100	101	100	111	010	30
	001	001	001	101	101	101	110	010	
	001	000	000	101	100	101	110	011	
35	010	000	000	110	100	110	101	011	35
	011	000	000	111	100	111	100	011	
	011	001	001	111	101	111	100	010	
40	010	001	001	110	101	110	101	010	40
	010	010	010	110	110	110	101	001	
	011	010	010	111	110	111	100	001	
45	011	011	011	111	111	111	100	000	45
	010	011	011	110	111	110	101	000	
	001	011	011	101	111	101	110	000	
50	001	010	010	101	110	101	110	001	50
	000	010	010	100	110	100	111	001	
	000	011	011	100	111	100	111	000	
55									55

Development of the higher order cases proceeds along the same rules. The third-order case, shown in Table 3, has 64 entries of three bit values, the sequences of the first two bits of x and y being the same as those of the corresponding second-order case, each entry being replicated four times. The least significant bit of the x coordinate has the sequence XXXY YXXY YXXY X Y Y X where X and Y represent the same sequences as before. It can be seen that the initial sequence of each group of four follows the same pattern as the sequences in the first group. Likewise, the least significant bit of the y coordinate has the sequence YXXY XXXY XXXY Y X X Y. It will be noted that the least significant bits are appropriately palindromic or complementary palindromic.

The rule for derivation of the higher order cases is therefore.

1. The sequences of all but the least significant bit are those of the previous order, each entry being replicated four times.
2. The sequence of the least significant bit consists of groups of four sub-sequences, each taking the form ABBA .
3. The first sub-sequence of the nth group of four is the same as the nth sub-sequence.
4. A can be X or Y or X or Y . If A is X then B is Y and vice versa.
5. The first sub-sequence of x is X if the order is odd and Y if it is even, and vice versa for y.
6. X and Y are the x and y sequences of the first order case.

CLAIMS

1. A method of scanning an image to produce a signal for transmission and display, comprising scanning the image along a trace formed by a co-ordinate sequence defined by one order of a hierarchical set of fractal curves.
2. A method of scanning an image to produce a signal for transmission and display, comprising scanning the pixels of an image in a co-ordinate sequence defined by one order of a hierarchical set of fractal curves.
3. A method of scanning according to claim 1 or 2 wherein the co-ordinate sequence is filtered by means of a filter having a raised-cosine pulse response.
4. A method of scanning according to claim 1 or 2 wherein the fractal curve is smoothed by filtering the co-ordinate sequence according to a filter characteristic which cuts at half the pixel frequency.
5. A method according to claim 4 wherein the running average of four coordinate values filtered to smooth said fractal curve.
6. A method according to any one of claims 1 to 4 wherein co-ordinate sequence is defined by a Hilbert curve.
7. A method according to any one of claims 1 to 4 wherein the co-ordinate sequence is defined by a Sierpinski curve.
8. A television camera, comprising means for forming a signal indicative of an image to be transmitted, the signal forming means comprising means for scanning the image in a co-ordinate sequence defined by one order of a hierarchical set of fractal curves.
9. A television camera according to claim 8 wherein the camera is one of a plurality of synchronised cameras each having said signal forming means, each camera being coupled to a selector means for selecting the output from one of said cameras and transmitting the output to a display, the selector being capable of selecting signals representing different orders of fractal curves.
10. A television receiver, comprising means for receiving a signal indicative of an image to be displayed, the signal receiving means comprising means for scanning the display along a co-ordinate sequence defined by one order of a hierarchical set of fractal curves to form said image from said signal.
11. A television receiver according to claim 10, comprising signal converting means for converting the received fractal signal into a signal suitable for display on a raster display.
12. Apparatus according to any one of claims 8 to 11 wherein the scanning means comprises means for scanning along a co-ordinate sequence defined by one order of a Hilbert curve.
13. Apparatus according to any one of claims 8 to 11 wherein the scanning means comprises means for scanning along a co-ordinate sequence defined by one order of a Sierpinski curve.
14. A television camera comprising a conventional raster camera, the raster output of which is coupled with converting means for converting a signal produced by a raster scan to a factual signal.
15. A television camera according to claim 14 wherein the converting means comprises picture storage means, means for writing pixel data from the raster scan into said picture storage means in a given sequence; and means for reading said pixel data from said storage means in a different given sequence.