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FIG. 1a

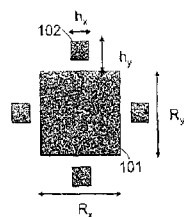


FIG. 1b



FIG. 1d

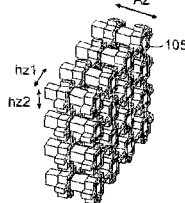


FIG. 1c

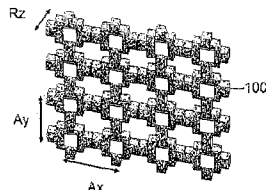
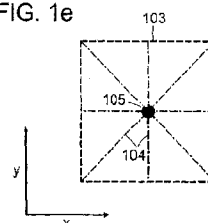


FIG. 1e



(57) Abstract: A methodology for designing structured metamaterials that can reflect, absorb and focus the propagation of both scalar acoustic and vector elastic waves is described. Three exemplary representative inventions based on the disclosed invention are described, illustrating i) compact ultra-wide broadband isolation, ii) sub-wavelength gaps and negative index propagation utilizing a single material platform, and iii) a fundamentally new method of producing multiple high frequency spectral gaps. Such metamaterial designs possess a wide range of potential applications, ranging from but not limited to, isolating an entity from external mechanical or acoustical vibrations, compact focusing lenses as well as cascaded high frequency filters for wave shaping and nonlinear wave propagation control.

PHONONIC METAMATERIALS FOR VIBRATION ISOLATION AND FOCUSING OF ELASTIC WAVES

Sponsorship Information

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Priority Information

This application claims priority U.S. Utility Application Serial No. 13/463,234, filed
on May 3, 2012 and to U.S. Provisional Application Serial No. 61/482,722 filed on May 5,
10 2011, the contents of which are incorporated herein by reference.

Background of the Invention

This invention relates generally to acoustic and mechanical attenuating and focusing
materials and devices, and more particularly to metamaterials suitable for mechanical
15 vibration isolation of sensors, as well as acoustic shields from sound that propagate through a
fluid, for example air or underwater. This invention relates as well to mesoscale, compact
devices for focusing, coupling, localization and controlling the propagation in general of
elastic and acoustic waves utilizing sub-wavelength building blocks.

Phononic metamaterials enable the manipulation of both elastic and acoustic waves in
20 different media, from attenuation (including absorption and reflection) to coupling, tunneling,
negative refraction and focusing. In particular, the attenuation of vibrations, such as vector
mechanical vibrations through a solid, or a scalar acoustic vibration in a fluid, such as in air
or water, is important technologically for applications where the presence of such vibrations
affects the intended performance of the device or entity in question, such as, but not limited
25 to, a sensor or a source of emission, such as a laser which may suffer from reduction in
performance due to losses arising from the coupling of mechanical modes into an acoustic or
an elastic medium. Another example of this is the attenuation of high frequency (>2KHz)
sound in acoustic hearing.

Conventional attenuating materials typically utilize thermally-coupled dissipation mechanisms to reduce the intensity of incident vibrations through dissipation-induced heating of the material. Such a dissipative mechanism does not have frequency selectivity other than the particular material's frequency dependent dissipation; the attenuation performance is dependent monotonically on the thickness of the material being utilized, governed by the

mass-density law, given by $T = \frac{4\gamma \exp(i k_z d)}{(1+\gamma)^2 - (1-\gamma)^2 \exp(2i k_z d)}$, where T is the amplitude transmission coefficient, d is the sample thickness, and γ is the impedance ratio between the different media on both sides of the interface (one medium typically being air). In general, at

low frequencies, $T \approx \frac{i 2 \sqrt{\rho_1 k_1}}{\omega \rho_2 d}$, hence the lower the frequency, the heavier the mass density

needed to achieve the same amount of transmission (attenuation) or the thicker the material required. These materials hence suffer from inadequate low frequency attenuation and implementation issues. As there are characteristic frequency and intensity ranges that have been identified as being detrimental to performance of, as well as to cause mechanical damage to, the device, hence it is desirable to provide an isolating/attenuating material that can be designed to have high attenuation within a target frequency range for broadband vibration and acoustic isolation. Also for certain applications, it is highly desirable to have excellent transmission of certain frequency bands (e.g. receipt of signals) and the ability to design the transmission spectrum across a wide range of frequencies is highly advantageous.

A relevant area of application would be to reduce particular vibrations of a *set* of frequencies from a body or entity or device that needs to be mechanically attached to a platform, hence providing a tradeoff between the requirement for mechanical stability and vibration isolation.

An object of the invention is a structured metamaterial that possesses multiple high-frequency spectral gaps capable of providing acoustic and/or mechanical vibration attenuation at high frequency ranges while retaining mechanical stability with a larger structure and permitting excellent transmission in selected regions.

Another object of the invention relates to acoustic and elastic metamaterials designated as sub-wavelength, meaning that they are able to control waves with wavelengths much greater than the physical structure, such as the unit cell dimension. These metamaterials are also capable of exhibiting double negative index behavior, leading to a general wave phenomenon known as negative refraction. These devices however, typically

require the incorporation of multiple materials (usually greater than 2), to obtain the required double negative index behavior. This presents inherent issues related to scaling down the intended device application to smaller scales, due to fabrication challenges involved in incorporating multiple materials. Some of the issues include the requirement of introducing and fabricating the different material components and adhering the different material interfaces together, which due to their different mechanical properties, limits the choice of material components. This presents challenges in applications involving functioning under dynamic variation in the material mechanical properties, such as thermal fluctuations, thermal cycling and thermal stress arising from differences in thermal expansion coefficients. One further complication of requiring multiple material components include the immediate reduction of throughput due to the fabrication requirements, as well as more complexity in manufacturing, leading to greatly reduced yields.

This invention describes a structured metamaterial that may be fabricated out of a single material that possesses such sub-wavelength negative index behavior, hence addressing several of the above challenges.

Summary of the Invention

A methodology for designing structured metamaterials that reflect, absorb and mold the propagation of both scalar acoustic and vector elastic waves is described. The methodology outlines the building block components formulating the unit cell of the eventual metamaterial array in terms of the function each building block component imparts on the propagation behavior of the metamaterial, through the final band structure dispersion relation. This systematic approach enables a rational approach towards the design of the unit cell of the metamaterial for a specific target application. In order to demonstrate the generality of this approach, three exemplary representative aspects based on the disclosed invention are described, illustrating compact ultrawide broadband isolation, subwavelength negative index propagation utilizing a single material platform, and a fundamentally new method of producing multiple high frequency spectral gaps. Such metamaterials offer a wide range of potential applications ranging from, but not limited to, isolating an entity from external mechanical or acoustical vibrations, compact focusing lenses as well as cascaded high frequency filters for wave shaping and nonlinear wave propagation control.

Methods and guiding principles are disclosed herein to design phononic metamaterials to yield a plurality of structures offering a range of control of elastic and acoustic wave propagation in materials; some of these exemplary embodiments include negative refraction, ultra-wide spectral gaps as well as multiple-high frequency spectral gaps.

5 One particular embodiment of the invention is a metamaterial possessing an ultra-wide spectral gap size, $\Delta\omega/\omega_0$ of 102%. The gap size is hence defined as the ratio between the size of the spectral gap and the central frequency of the gap, where $\Delta\omega = \omega_h - \omega_l$, the difference between the upper and lower bounds of the spectral gap, $\omega_0 = (\omega_h + \omega_l)/2$. Such an embodiment may be utilized for applications including, but not limited to, a band-stop filter
10 for acoustic or elastic vibrations, or as vibration isolation platform fixtures for certain entities, such as sensors, or emission sources such as microlasers which require vibration isolation from certain frequencies, or range of frequencies, of vibrations and noise that would impair the performance of the entity or device.

Another embodiment of this invention is a novel metamaterial structure that includes
15 multiple high-frequency spectral gaps. The formation of these spectral gaps is unique from those that are in the current art and are directly developed from the disclosed invention. Such a metamaterial may be utilized in applications including, but not limited to, multiple frequency sensors and mechanical shields from high intensity vibrations, which typically are nonlinear and hence possess multiple high frequency components in their spectral content.
20 One other possible application would be in the formation of a guiding structure that must be mechanically stable and needs to shield an entity from higher frequency vibrations.

Yet another embodiment is a method of designing metamaterials with sub-wavelength spectral gaps, utilizing only a single material. This is a significant advancement over the current art, in which the presence of a sub-wavelength spectral gap typically requires two or
25 more solid building block components. Our embodiment enables design of phononic metamaterials which can be scaled down to much smaller dimensions, such as the micron and sub-micron scale for applications such as compact phononic lenses for focusing high frequency elastic and acoustic waves at these smaller scale regimes, compatible with existing fabrication techniques, such as optical lithography, or other top-down techniques. In contrast,
30 current methods of fabricating such sub-wavelength devices require multiple steps, are highly dependent on specific material component choices and are not inherently scalable in fabrication length scales, strongly limiting their applicability.

Brief Description of the Drawing

Figs. 1a, b, c, d and e are schematic illustrations of exemplary embodiment of a unit cell(1a) , one dimensional(1b), two dimensional(1c) and three dimensional(1d) arrays of the unit cell in various dimensions of phononic metamaterial, presenting the symmetry elements within the unit cell and the specific Wyckoff position being occupied (1e).

Figs. 2a, b and c are schematic illustrations of a unit cell structure of an embodiment of the invention that possesses a 102% spectral gap, providing a schematic of the two dimensional array(2a), the components of each individual building blocks of the unit cell (2b) and the schematic of the unit cell(2c).

Figs. 3a and b are schematic illustrations of representative building block components constituting the unit cell of an embodiment of the invention, demonstrating the utilization of the lattice net(3a) and the subsequent positioning of the building blocks in various Wyckoff sites within the unit cell(3b).

Fig. 4 is a graph showing the band structure dispersion relation of an embodiment of the invention shown in figs 2 and 3.

Fig. 5a is a graph of intensity versus frequency of a structure with 10 repeat layers under a longitudinally polarized incident excitation over the normalized frequency range (ωa) of 0 to 20.

Fig. 5b is a graph of intensity versus frequency of a structure with 10 repeat layers under a transversely polarized incident excitation over the normalized frequency range (ωa) of 0 to 20.

Fig. 5c is a schematic illustration of an exemplary embodiment of the invention.

Fig. 6a is a graph of intensity versus frequency of an embodiment of the metamaterial, described in Fig. 6b.

Fig. 6b is a schematic illustration of a metamaterial according to an embodiment of the invention.

Fig. 6c is another schematic illustration of a metamaterial in another embodiment of the invention.

Fig. 6d is a graph of intensity versus frequency for an embodiment of the metamaterial disclosed herein in Fig. 6c.

Fig. 7a is a graph of intensity versus frequency for the transmission spectrum of an isolated structure.

- 5 Fig. 7b is a micrograph of an implementation of the structure described herein as an isolation fixture.

Figs. 8a, b and c are schematic illustrations of the unit cell structure of an embodiment of the invention disclosed herein, describing the array(8a), the building components of the unit cell(8b) and the unit cell (8c).

- 10 Figs. 9a, b and c are schematic illustrations of representative building block components constituting the unit cell of a metamaterial designed based on the design methodology disclosed herein, providing the lattice net describing the symmetry elements and the subsequent positioning of the building blocks within the unit cell(9a), the building block components of the unit cell and the placement of the building blocks within the lattice net,
15 conforming to the symmetry elements and Wyckoff positions.

Fig. 10 is a graph describing the band structure dispersion relation for an embodiment of the invention disclosed herein, providing multiple high frequency gaps above the Bragg frequency.

- Fig. 11a is a graph of transmission intensity versus frequency of a structure with 10 repeat
20 layers under a longitudinally polarized incident excitation over the normalized frequency range (ωa) of 0 to 100, described by Fig. 11b.

Fig 11b is a schematic illustration of a metamaterial according to an embodiment of the invention.

- Figs. 12a, b, c and d are schematic illustrations of the unit cell structure of another
25 embodiment of the invention, that possesses a negative index band (arrowed), providing a schematic of the two dimensional array (12a), the components of each individual building blocks of the unit cell (12b,c) and the schematic of the unit cell(12c)

- Figs. 13a, b, c and d are schematic illustrations of representative building block components constituting a unit cell of a metamaterial design of an embodiment of the invention, providing
30 the lattice net with the Wyckoff position, the two constituent eigenmodes (13b,c) and the formation of the unit cell structure.

Fig. 14 is a graph showing the band structure dispersion relation of an embodiment of the invention.

Figs. 15a and b are graphs of intensity versus frequency for a longitudinally polarized incident excitation and a transversely polarized incident excitation across a normalized frequency range (ωa) from 0 to 50.

Fig. 15c is a schematic illustration of a metamaterial according to an embodiment of the invention.

Detailed Description of the Preferred Embodiments

At the outset, it should be understood that the figures and the descriptions of the present invention have been simplified to illustrate elements that are relevant for a clear understanding, while eliminating, for the purpose of clarity, many other elements found in typical attenuating fixtures and focusing devices, and methods of making and using them. Those of ordinary skill in the art may recognize that other elements and/or steps may be desirable in implementing the present invention. However, because such elements and steps are well-known in the art and because they do not facilitate a better understanding of the present invention, a discussion of these elements and steps are not provided herein.

Attenuating materials are generally known and used as a filter of either mechanical vibrations or acoustic sound, propagating in air or underwater, in order to reduce the amount of final intensity of either a single or multiple range of frequencies from reaching a final device or entity. This entity may be an inanimate object, such as a sensor or electronic device, or an entity that is either a transmitter or receiver of information. The entity may also be an animate object, such as a human being. One such example is an application of this attenuating material for protection from high intensity, high frequency noise that impinges onto the ear of a person while maintaining excellent transmission characteristics in key frequency regimes.

This invention is a methodology for designing structured metamaterial that is capable of producing a multiplicity of wave propagation behavior, such as ultra-broadband vibration attenuation, with a compact form factor, meaning it requires fewer repeat layers in order to present the same degree of attenuation as compared with traditional damping materials, presenting both a frequency range specific broadband attenuation within a compact form factor.

Phononic metamaterials are generally known to possess band gaps, which arise due to a correct choice of structure, unit cell and selected features. A phononic metamaterial according to one embodiment of the present invention allows for a broadband attenuation response over a wide frequency range, with a frequency range of operation which can be tailored depending on the choice of structure. Yet another embodiment allows for a multi-spectral attenuation response over an ultra-wide frequency range, utilizing the same material.

A metamaterial usually consists of a regular array of individual units, which are referred to hereafter as unit cells. The array may be attached, connected or appended to other structures to facilitate its particular function. Fig. 1(c) shows exemplary representations of a planar array **100**, with two-dimensional periodicity, with unit cell lengths A_x , A_y , and an associated thickness R_z . Alternatively, it is also possible to stack these planar arrays **100** into a three-dimensional array **105**, Fig. 1(d), whereby the spacing between the planar arrays is A_z . It is also possible to design a three-dimensional embodiment of the metamaterial which does not involve linear stacking of individual planar arrays **100**. Yet another possible embodiment includes a one dimensional array **106** as shown in Fig. 1(b). All of these are possible embodiments of the invention giving rise to the metamaterial structure. It is conceivable for the metamaterial array to be appended, truncated, or bound by structures, surfaces or interfaces which are different from the unit cell making up the array, for example as shown in Figs. 5, 6, 7 and 15. The choice of truncation and hence the formation of the boundary may also involve the inclusion of a structure that serves as the truncation layer. The specific design of this truncation layer will depend on the specific application which the metamaterial has been designed for. While prior art has demonstrated phononic metamaterial [1-4] and crystal [5-7] designs capable of spectral gaps, allowing for broadband transmission attenuation in a range of frequencies, there is a requirement for phononic metamaterial designs with ever larger spectral gaps, as well as a more compact form factor. From the fundamental perspective, there is a lack of a proper design methodology to guide the design of a particular metamaterial structure with a desired set of wave propagation behavior. The approach from prior art [1-9], typically includes the choice of multiple material components, of which one, or more, may be air, or fluid, as the component building blocks. This is particularly evident in the prior art [1-6] approach in developing metamaterials with sub-wavelength propagation behavior, where typically three or more material components need to be utilized [1-5].

Subsequently, by choosing one or more of these material components as the building block and the other component(s) to fill the complimentary phase of a designated unit cell, a space/plane group for the structure is chosen and the volume fraction of one phase is varied, for choices of different sets of material components to search for an overall structure with the desired properties. In this approach, the specific band dispersion depends on the complicated mixture of structural *details* of the system and material choices. Indeed, there is a prevailing opinion that there are no *a priori* guiding principles for selection of the material set and unit cell design to control the final band dispersion. This invention discloses a design methodology offering a systematic design procedure for phononic metamaterial structures, utilizing general principles of group theory [11-13]. The design methodology unifies the different design parameters of fill fraction, space/plane group and material component choices by systematically classifying these design parameters for the unit cell structure into the context of the choice, positioning of the building blocks and the type of mechanical topology within the unit cell.

Fig. 1 may be utilized as an exemplary outline of the design methodology. Fig. 1a shows an exemplary schematic decomposing the building blocks making up the unit cell. The components of the building blocks **101**, with linear dimensions **R_x**, **R_y** and the mechanical connections **102**, with dimensions **h_x**, **h_y** can be selected and varied in a way predicated by the invention to achieve deterministic properties which are desired by the targeted application. As shown in Fig. 1(a), a single unit cell consists of building blocks **101**, here depicted as squares, but it should be understood that other shapes are possible, depending on the particular application being desired, and its mechanical connections **102**. In this example, the dimensions of **101**, are determined by **R_x** and **R_y**; it should however be understood that other shapes and geometries are possible and may be necessary to achieve other properties. The particular choice of the shape is related to the eventual performance of the material and important to the design methodology presented in this patent application. The geometry and material type of building block **101** determines the frequency, or set of frequencies where a desired propagation response, such as a spectral gap, or a particular propagation behavior, such as negative refraction. The orientation and placement of **101** in a particular Wyckoff site, given in figure 1 as **105**, is chosen together with the mechanical connections **102** to form the final unit cell design. The orientation of **101** is defined as the physical placement of **101** with respect to the symmetry elements **104**, which are here mirror lines, present within the chosen unit cell. In general, for example but not restricted to, the

building block **101** possesses self-symmetries, which are point symmetries of the building block itself. Depending on the particular application desired, the building block **101** is oriented in such a way to either align, or misalign, its self-symmetries with those in the unit cell **104**. As the chosen building block always ultimately possess point symmetries that are strictly lower than that of the maximal point symmetry of the final lattice net **103** chosen for the array, the choice of the particular building block geometry will reflect this fact. The lattice net will be defined here to consist of the unit cell outline, the symmetry elements utilized in the design and the Wyckoff position occupied in the particular embodiments being discussed. To elaborate, in this particular example, **101** possess a 4mm point symmetry, which happens to be identical to the maximal point symmetry of the lattice net chosen **103**, also 4mm, as indicated by the two pairs of the mirror planes **104** in Fig. 1(e). The lattice net indicates the plane/space group of the chosen structure, and indicates the symmetry elements **104**, as well as the Wyckoff sites **105** being occupied by the building blocks to form the individual lattice. In Fig 1, **101** is oriented such that it is *aligned* with the symmetry elements **104**, to form the final unit cell design.

The invention utilizes the geometry of the building block, the choice of the plane/space group, in particular the Wyckoff sites **105** to place the building blocks on, and finally on the orientations of the mechanical connections, to deterministically design a particular dispersion relation. As mentioned, the building blocks are chosen in order to achieve a particular set of free resonances, it should be clear to one ordinarily skilled in the art that each building block possesses multiple free resonance frequency modes, corresponding to resonant vibration eigenmodes of different symmetries, such as, but not restricted to, the monopolar, dipolar and higher order modes. The arrangement of the resonance frequencies in terms of the frequency levels needs to be selected correctly in order to achieve a target final dispersion relation. The permissible Wyckoff positions of the building blocks need to also be chosen together with the particular geometry and mechanical topology in order to achieve the desired dispersion relation. The mechanical connections necessarily need to be chosen to evolve the final band dispersion, while conforming to the chosen lattice net **103**. As should be clear to those ordinarily skilled in the art, the size, geometry and shape of the mechanical connections may be varied together with various combinations and orientations, positioning of the building blocks to design various phononic metamaterial structures with certain required properties for applications, besides the three exemplary embodiments disclosed in this application.

The building blocks may be arranged relative to each other, in a plurality of ways within the unit cell. A single unit cell may consist of a single, or multiple building blocks, of identical or different geometries/shapes. The placement of the building blocks within the unit cell naturally conforms to certain symmetry elements, such as a mirror plane (labeled with dashed lines) or a glide plane (labeled with dash-dotted lines) and these all have a strong influence on the final propagation behavior of elastic and acoustic waves within the final metamaterial array. These various positions are known to those ordinarily skilled in the art as the Wyckoff positions, of which a comprehensively tabled database is readily available [10,11]. The choice of the building block position, known here as the Wyckoff site, on the resultant regular array is matched to the correct orientation of the mechanical connections to the building blocks, referred to herein as the *mechanical topology*, in order to obtain a desired final wave propagation response.

Each individual building block is connected to one another through mechanical connections, as shown in Fig. 1, with a one dimensional array **106**, a two-dimensional array **100**, and a three-dimensional array **105**, being illustrative exemplary embodiments. While it is understood that these connections may be made of a different material, in this particular embodiment and for illustrative purposes, they are made with the same material as the building blocks.

A plurality of mechanical connections is possible and can be classified according to the family of orientations, such as $\langle 10 \rangle$, $\langle 11 \rangle$ and so on; those of ordinary skill in the art will recognize that these refer to the crystallographic orientations. There may be more than one family of orientations incorporated as mechanical connections, for example a unit cell may utilize both $\langle 10 \rangle$ and $\langle 11 \rangle$ class of mechanical connections, as in **1201** (Fig. 12(a)). The sizes of the mechanical connections may be varied, in terms of their thickness, widths and length, together with their orientations, and size and positioning of the building blocks to obtain the resultant wave propagation behavior. Example embodiments of this resultant wave propagation are, but not limited to, frequency range of attenuation or isolation, as well as negative refraction.

The variation in the amount of solid material, taken as a ratio over a fully filled space with same lattice basis, is known as the fill fraction, otherwise also known as volume fraction (in three dimensions) or area fraction (in two dimensions) of the metamaterial. All such variations of the amount of solid material for the metamaterial may be divided into the building blocks and its mechanical topology. In other words, by choosing the mechanical

topology to match the positioning of the building blocks, the vibration isolation/attenuation range may be maximized, enabling superior attenuation characteristics, of which the embodiment in Fig. 2a is an example, exemplified by the band structure dispersion relation in Fig 4. The size, given by the lateral width, thickness and the length, of the mechanical connections affect the frequency range of the vibration attenuation, as well as the number of repeat units required to obtain a certain degree of attenuation. Hence the size of the mechanical connections also have to be chosen to match the building block sizes, and hence their mechanical resonances. As a demonstration of the generality of this approach, we describe three different embodiments of the invention to achieve a plurality of applications to exemplify the design methodology disclosed by this invention.

A metamaterial isolator, according to one embodiment of the present invention allows for an ultra-wide flattened vibration frequency isolation response, and hence improved vibration isolation or attenuation. Furthermore, it enables the development of a very *compact* isolator, reducing the number of repeat units which are typically required to achieve such a wide isolation response.

Referring to Fig. 2, a unit cell **201** (Fig. 2(c)) of an exemplary phononic metamaterial is shown, wherein the solid building blocks **202** are connected by mechanical connections **203** defined here by $\mathbf{h}_x$, $\mathbf{h}_y$ and $\mathbf{h}_{xy}$ to indicate the possible variations in the shapes of the mechanical connections; these mechanical connections further may be made of the same, or a different material. This constitutes the unit cell. A multiplicity of this unit cell is repeated and arranged in a regular array to form the resultant metamaterial **200** (Fig. 2(a)). The general final array, in terms of the dimensions and number of repeat unit cells to form the final array depends on the specific implementation; the current embodiment is a simple illustrative example that illustrates the metamaterial sandwiched between two homogeneous slabs, of which the entity to be isolated is on one end of the entire structure, labeled by **701** in Fig. 7. The dispersion relation of an infinite array of **201** is computed in Fig. 4, showing the ultra-wide spectral gap of 102%, computed using silicon as the solid material. Computations were further conducted with a representative class of materials, ranging from metal (aluminum and steel), as well as a typical polymer, such as poly(methyl-methacrylate), or poly(dimethylsiloxane) and these structures yield similar spectral gap widths of approximately 100%, with about a 5% variation. This illustrative computation is to highlight that the property of the spectral gap is a general feature based on the invention method, and is robust across different material platform choices. In Fig. 5, transmission spectra were then

numerically computed for a metamaterial constructed out of a polymer, with mechanical properties of $E=10\text{GPa}$, Poisson ratio = 0.2152, and mass density of 1300kgm^{-3} . As shown clearly, both longitudinal and transverse excitations, launched from **502** and collected at **504**, after passing through **503**, the metamaterial structure, display a 102% spectral gap, with 100dB suppression of intensity in this range. As an example but not restricted to, for such a spectral gap to occur in the 6 to 18KHz regime, the structure depicted in 201 will have the following dimensions: unit cell dimensions A_x, A_y will be 100mm, R_x, R_y will be 56mm, h_x will be 13.7mm, h_y will be 16.6mm and h_{xy} will be 5.7mm.

In accordance with the invention, for this particular embodiment, we choose a building block **202** (Fig. 2(b)), which has a set of resonant frequencies. In order to maximize the size of the spectral gap, the resonant frequency of the building block should be close to the target frequency region of the intended target application. Upon the choice of the arrangement of the final metamaterial array, known as the lattice, the possible position types, labeled by the Wyckoff sites, is now known. Depending on the target dispersion relation, the correct Wyckoff position has to be chosen. In this particular embodiment, lower multiplicity Wyckoff sites **300** (Fig. 3(a)) should be chosen for the occupation by the building blocks in order to ensure that the interaction is predominantly due to the periodicity, which will enhance the interaction and lead to a larger spectral gap. In this embodiment, therefore, the mechanical connections forming the mechanical topology should avoid directions which would mechanically link the building blocks **202** along the mirror lines **301**. Referring to **304**, this implies avoiding connections which will *physically* emphasize symmetry elements such as the mirror line, i.e. along the $\langle 11 \rangle$ family of directions. For this chosen plane group, or lattice net, the remaining possibility is given by the $\langle 10 \rangle$ family of connections, which is the correct mechanical topology of the network connections **303** to be chosen. The specific size and dimensions of the mechanical connections may be tuned to optimize the desired/required spectral gap width, etc. It is contemplated that instead of utilizing the same material throughout the array, building blocks made out of different materials, having different geometric shapes and of similar mechanical but different optical and electrical properties may also be utilized. This would be attractive in optimizing a particular intended function of the device, which may include coupling of mechanical with other properties such as but not limited to, optical or electrical properties. This same rule applies to the mechanical connections **303**. The only requirement is that the totality of the choice and the arrangements still follow the requirement of the building block types and positioning in the lattice array,

taken with the correct interpretation of the correct lattice type. It is also contemplated that building blocks consisting of materials with different linear and/or nonlinear mechanical properties might be utilized, depending on the particular application. This pertains to the possibility of choosing a lattice net with a multiplicity of Wyckoff sites and desiring different behavior in the linear, meaning here the linearly elastic regime, and the nonlinear range, meaning here the non-linear regime, which may occur at large strains, during onset of plasticity and/or specific frequencies of the impinging vibration at high intensities of acoustic or mechanical energy flux. This is further attractive in applications where the metamaterials are designed to focus, localize or deflect acoustic energy in certain directions or locations; hence metamaterial structures may be designed with the incorporation of materials with different mechanical behavior, including viscoelasticity, mechanical damping or thermo-mechanical damping behavior, for optimized absorption of mechanical or acoustic energy, for an exemplary embodiment. The intrinsic properties of possible materials components are rich and diverse, in terms of their linear and nonlinear mechanical behavior, such as but not limited to, elastic, elasto-plastic, visco-elastic; in many cases the particular properties would depend on the intrinsic molecular or atomic structure of the constituent materials. Certain fluids and gels may possess particular properties such as but not limited to, non-Newtonian flow properties such as in dilatant materials, or gels that may undergo phase transitions with a controllable tuning parameter that are attractive to the optimized function of a particular application of the metamaterial. It is contemplated that the combinations of material components with different mechanical behavior, in different spatial, frequency or time-scales may be utilized in the design of the particular metamaterial or device design, depending on the intended application and the desired performance to be optimized. It is further contemplated that the design of the metamaterial structure may consist of liquid objects, combinations of different liquid objects, or materials that may undergo a phase transition, such as a solid-liquid phase transition, during the intended device operation, which may involve the variation of certain operating conditions that lead to the phase transition.

Such a configuration is particularly suited for vibration isolation or attenuation in a lateral fashion. Yet another embodiment includes the building block, connected by mechanical connections in all three dimensions, as shown in Fig. 1(a). In this embodiment, the unit cell is then repeated and arranged in a three-dimensional regular array to form the resultant metamaterial. Such a configuration is particularly suited for attenuation for an isolated entity, such as a sensor, or a biological organ, such as the ear.

Fig. 3 illustrates an exploded view of an exemplary embodiment of the present invention. The building block **202** (Fig. 2(b)) is first chosen to have a desired frequency of response; that is the frequency of operation, whether the operation is for attenuation or vibration. This sets the choice of the building block. The building block is chosen with a particular position **300**, with respect to the intended final formation of the regular array utilized. For this particular embodiment, the position of the building blocks, prior to the insertion of the mechanical connections, is oriented to fulfill the presence of orthogonal symmetry operations, known as glide planes. The particular choice of mechanical connections in this case is to minimize the physical effects of certain symmetry elements **301**. In this particular embodiment, the choice of the building block positions, together with the mechanical connections enhances the frequency range of the vibration attenuation. As shown, the transmission spectrum **600** (Fig. 6(a)) of the metamaterial array is quite impressive, for a structure consisting of only 5 layers is 40dB suppression, for just 3 layers **601** is still a 25dB suppression. Analogous to the **500**, **501** spectra, for **600**, longitudinal excitation was launched from **602**, and collected at **604** after propagating through **603**. For **601**, longitudinal excitation was launched from **605**, and collected at **607** after propagating through **606**. To be clear, **503**, **603** and **606** represent a single repeat unit along the lateral direction, with 10 repeated layers forming the actual metamaterial structure. However, someone ordinarily skilled in the art will realize that this number of repeat layers can be varied in order to achieve the required performance.

The presently disclosed structures are much more compact than existing structures, meaning that it requires fewer repeat units to achieve the same degree of vibration isolation. This is clear from the exemplary attenuation figures, where a three unit layer **601** shows a 30dB suppression of intensity, which is comparable to typical phononic crystal structures requiring ten or more layers [6-9].

Referring to Fig. 7, one exemplary embodiment involves the isolated entity **702**, surrounded by the metamaterial array **701**, which serves as a vibration isolation platform for the entity. An incident source is launched from **703**. The computed transmission spectrum **700** (Fig. 7(a)) at the entity being isolated is computed and shows a 50dB reduction. This particular embodiment demonstrates one potential implementation of this metamaterial array as a vibration isolation platform for the central entity, which may be functioning as a sensor, such as a receiver, or as an active element such as an emission source to prevent mechanically

induced losses. We note here that the size of the object to be isolated can be varied and is not restrictive, for example, to a single Wyckoff position of the vibration isolation structure.

The present invention allows for a compact vibration isolation solution, meaning that it requires significantly fewer repeat layers to perform the same degree of attenuation (greater than 20db) as compared to current commonly known phononic crystals [6,7] or conventional damping materials(1-4). This is a distinctive feature of the invention and allows for a compact vibration isolation material or platform, as shown in Fig. 7.

Yet another embodiment of this invention is a metamaterial array possessing high frequency multiple, meaning in this case two or greater, complete spectral gaps. High frequency is defined here to correspond to frequency regimes which typically fall above the Bragg regime, defined with a normalized frequency, given by $(\omega a/c) \sim 0.5$, where a represents the unit cell dimensions, and c the acoustic velocity of the homogeneous medium being utilized. Possible applications for this include, but are not limited to, shaping multiple harmonic mechanical pulses, breaking up sharp temporal pulses and deflecting nonlinear elastic and acoustic waves.

This second representative embodiment exemplifies the development of a metamaterial with a novel band dispersion relation, which is capable of providing multiple high frequency spectral gaps while maintaining greater quasi-static/lower frequency mechanical stability due to its larger length scale structure. In comparison with conventional phononic crystals, the frequency range of attenuation, is approximately three times higher, based on the same unit cell size as a conventional phononic crystal which one ordinarily skilled in the art would be familiar with[1-7]. Referring to Fig. 8, the unit cell **801** is depicted together with its array/lattice view **800**. This particular embodiment discloses a fundamentally new way of obtaining this particular dispersion relation. **801** consist of the building block components **802** and its mechanical connections **803** forming the topology, and Fig. 9 marks the Wyckoff positions **901** on the lattice net definition **900**. In this embodiment, the building blocks need to be chosen to have the lowest possible self-symmetries, while still fulfilling the governing symmetry operations **902** required in the chosen lattice net. Referring to the lattice net and choosing the positions **901**, the chosen building blocks are only required to have the symmetry of a mirror plane **902**. The particular geometric shape of the building blocks may be varied, while conforming to this requirement or fulfilling any of the other possible point symmetries as a result of the Wyckoff position chosen. In this particular embodiment, the building blocks are chosen on two levels, the first

consisting of the single building block labeled **903**. The resonant frequencies of this building block should lie in the frequency range of interest. Necessarily, because the structure is designed to work at higher frequencies, the Wyckoff positions being considered typically, but not always, need to have a multiplicity of Wyckoff sites greater than 1 per unit cell; in this particular embodiment here there are 4, as shown in **900**. This consideration is general to the invention and can be readily recognized by someone ordinarily skilled in the art.

Referring still to Fig. 9, based on the prescribed lattice net, there are two possible families of mechanical connections to connect the building blocks while conforming to the chosen lattice net **900**. In this chosen embodiment, as the criterion to obtaining the designed dispersion relation exemplified in Fig. 10, one would need to choose mechanical connections that are aligned along the symmetry elements **902** of the individual building blocks; in this particular metamaterial structure, this set of mechanical connections are along the $\langle 11 \rangle$ family of directions. This deterministic method of designing the metamaterial structure as demonstrated illustrates the invention as a rational method of designing the band dispersion of a metamaterial. Referring to Fig. 10, the computed band dispersion relation shows multiple high frequency spectral gaps, above the associated Bragg frequency located nominally at $(\omega a/c) \geq 0.5$. This dispersion relation was computed for amorphous silicon, using material parameters of $E=156\text{GPa}$, Poisson ratio of 0.2152 and mass density of 2330kgm^{-3} . Fig. 11 shows the computed transmission spectrum of a 10 layer structure for longitudinal **1101** excitation; as the spectral gaps are complete, the attenuation for the transverse excitation will be similar. A longitudinal source is launched from **1102**, propagates through the ten repeat unit metamaterial structure **1103**, and the transmission intensity is collected at **1104**. To be clear, **1103** represents a single repeat unit along the lateral direction with 10 repeated layers forming the actual metamaterial structure. However, someone ordinarily skilled in the art will realize that this number of repeat layers can be varied in order to achieve the required performance.

One notes that the primary transmission dip at 30 kHz (for a unit cell size, with $a=1\text{mm}$) corresponds to the Bragg frequency. The multiple high frequency gaps, referring to Fig. 10, present an overall improved attenuation of 50dB or greater in frequency ranges up to 3 times higher ($\sim 120\text{KHz}$) than that of the typical Bragg frequency, which in this exemplary embodiment is at 30KHz. This cascade of multiple high frequency gaps together enable a wide broadband attenuation that replaces the need for a sequence of cascaded structures which may each possess attenuation in a small section of the frequency spectrum, for

example. Importantly, the structure **800** in Fig. 8 possesses high frequency attenuation of ~100% bandwidth (~ 40 to 120 KHz here), while having a structural length scale two times smaller than that typically required for phononic crystals.

The third embodiment describes the design of a metamaterial array with a sub-wavelength gap and double-negative index transmission band, utilizing only a single solid material. This particular embodiment based on the invention enables those ordinarily skilled in the art to realize metamaterial structures with sub-wavelength gaps and a double-negative index transmission band. In current art, the realization of a sub-wavelength metamaterial typically requires the incorporation of multiple material platforms, typically greater than two, with widely varying mechanical properties such as bulk modulus, Young's modulus, mass density, and Poisson ratio[1-6]. In the general case of anisotropic materials utilized in the building blocks, the stiffness and compliance tensor of the constituent materials may be widely different. Hence, the requirements typically involve intrinsic mechanical impedance contrast between the different materials as the fundamental mechanism for the formation of the sub-wavelength gaps and double negative index band and give the impression that the realization of such behavior requires not only a complex design but use of a set of component materials each having special mechanical properties. This invention demonstrates the formation of the subwavelength spectral gap and the double negative index band can be done by utilizing a monolithic, homogeneous, isotropic single material.

Referring to Fig. 12, the unit cell **1201** that is repeated in an array **1200** is demonstrated here. In this particular embodiment, the focus is on creating a subwavelength gap and a double negative index band. The typical requirement for a double negative index band requires building block(s) that have both monopolar and dipolar resonances lying within the desired subwavelength regime, determined by the correct choice of the building block(s), through their geometry, materials choice etc. Usually, more than one type of building block is required, one with the requisite monopolar resonance and the other with the requisite dipolar resonance. Subsequently, by placing the two building blocks with their respective resonances lying in the same frequency range, the two modes hybridize and interact to form a single double negative index band. This double negative band is characterized by both dynamic negative mass density and negative modulus. The particular embodiment here advances this by designing a building block that hybridizes both the monopolar and dipolar resonant modes. The building block **1202** in Fig. 12(b) exhibits both monopolar like motion, captured by its symmetric absolute displacement profile, while its dipolar like motion is

captured by the details of the displacement vector field, which exhibits an anti-symmetric profile that is typical of dipolar-like motion. The size and orientation of the mechanical connections **1203**, **1204** are varied and designed in order to form the eventual double negative band and the sub-wavelength gap. In this embodiment, in order to achieve both resonance
5 modes with a single material, the lattice net **1300** in Fig. 13, is chosen to have low point symmetry. In particular, the choice of Wyckoff position **1301** for the placement of the building block imparts point symmetry of a single 4-fold rotation. This choice of the lattice net enables the hybrid resonant mode **1302** to form the double negative index band **1401**. Fig. 14 provides the computed dispersion relation of the sub-wavelength metamaterial,
10 exhibiting clearly that the band **1401** occurs at a normalized frequency of ~ 0.22 , significantly lower than the typically Bragg frequency, defined as around 0.5. There is also the presence of a narrow sub-wavelength spectral gap of approximately 7% normalized gap width.

Fig. 15 further describes an embodiment of the metamaterial as a sub-wavelength vibration isolation material **1503**, together with its associated transmission spectrum from
15 longitudinal **1500** and transverse **1501** excitations of a 10 layer material; the sub-wavelength gap is clearly present, showing 20dB-30dB suppression in transmission in the sub-wavelength spectral region, with reference to the Bragg frequency. Referring to both **1500** and **1501**, the excitation is launched from **1502** and collected at **1504**, after propagating through the material in **1503**. A second exemplary embodiment of the invention is the
20 formation of the negative index band **1401** of the designed metamaterial, functioning as a compact sub-wavelength lens for focusing vector elastic waves, as exemplified by the double negative index band in **1401**, and by the indicated transmission peak at the corresponding frequency under longitudinal excitation in **1501** and transverse excitation in **1502**, which are
25 indications of the double negative index behavior, because this mode is active under both modes of excitations and its group velocity, defined as $\partial\omega(\mathbf{k})/\partial\mathbf{k}$, is negative, as is clear from the negative slope of **1401**. This demonstrates the focusing effect of incident transverse and longitudinal waves associated with a double negative index metamaterial.

Those of ordinary skill in the art may recognize that many modifications and variations of the present invention may be implemented without departing from the spirit or
30 scope of the invention.

The contents of all of the references listed herein are incorporated herein by reference in their entirety.

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What is claimed is:

- 1 1. Photonic metamaterial device including an array comprising a periodic array of
2 repeated unit cells forming a lattice, with the design of the unit cell determined by a lattice
3 net, wherein the size and geometric shape of the building blocks, the orientation and size of
4 mechanical connections that form the mechanical topology of the lattice are selected to
5 provide specific dispersion relations in the phononic metamaterials.
- 1 2. The device of claim 1, wherein this metamaterial array comprise a sub-component or
2 as part of a vibration isolation platform, a focusing lens, or a filter.
- 1 3. The device of claim 1, where the array is an unsupported monolithic slab of material
2 which can be either silicon or other semiconductor, a metal, a ceramic, a polymer, or a
3 composite (including solid and liquid foams, nanocomposites) as well as gels and fluids and
4 suspensions/emulsions and comprises a lattice array of unit cell building blocks consisting of
5 solid blocks or liquidobjects connected by mechanical connections.
- 1 4. The device of claim 3, where the mechanical connections may consist of the same or
2 different material compared with that utilized for the building block.
- 1 5. The device of claim 3, where different building blocks in a chosen lattice net, should
2 the lattice net possess multiple Wyckoff sites per unit cell, may consist of the same or
3 different material.
- 1 6. The device of claim 3, where the mechanical connections may consist of different
2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
3 the intended function of the device.

1 7. The device of claim 3, where the the different building blocks may consist of different
2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
3 the intended function of the device.

1 8. A vibration isolation platform device capable of up to greater than 30dB vibration
2 reduction.

1 9. The device of claim 8, wherein a portion of the device consists of phononic
2 metamaterial with a spectral gap greater than 80% and greater than 30dB vibration reduction
3 with a one or more repeat-unit structure.

1 10. The device of claim 8, wherein the portion of the device consisting of the phononic
2 metamaterial in the current embodiment possesses a 102% spectral gap and 70 dB vibration
3 reduction with a ten repeat-unit structure.

1 11. The device of claim 8, where the metamaterial can be either silicon or other
2 semiconductor, a metal, a ceramic, a polymer, or a composite (including solid and liquid
3 foams, nanocomposites) as well as gels and fluids and suspensions/emulsions and comprises
4 a lattice array of unit cell building blocks consisting of solid blocks or liquid objects
5 connected by mechanical connections.

1 12. The device of claim 8, where the mechanical connections may consist of the same or
2 different material compared with that utilized for the building block.

1 13. The device of claim 8, where different building blocks in a chosen lattice net, should
2 the lattice net possess multiple Wyckoff sites per unit cell, may consist of the same or
3 different material.

1 14. The device of claim 8, where the mechanical connections may consist of different
2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
3 the intended function of the device.

1 15. The device of claim 8, where the different building blocks may consist of different
2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
3 the intended function of the device.

1 16. The device of claim 8, where the components of the device may consist of different
2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
3 the intended function of the device.

1 17. A vibration isolation platform device capable of up to multiple high frequency range
2 suppression over 40% bandwidth without the need for cascaded filter structures while
3 retaining mechanical stability.

1 18. The device of claim 17, wherein the portion of the device consists of phononic
2 metamaterial with multiple high frequency spectral gaps totaling over 100% in bandwidth
3 and >30 dB suppression for each spectral gap with a ten repeat-unit structure compared with
4 homogeneous materials.

1 19. The device of claim 17, where the metamaterial can be either silicon or other
2 semiconductor, a metal, a ceramic, a polymer, or a composite (including solid and liquid
3 foams, nanocomposites) as well as gels and fluids and suspensions/emulsions and comprises
4 a lattice array of unit cell building blocks consisting of solid blocks or liquid objects
5 connected by mechanical connections.

1 20. The device of claim 17, where the mechanical connections may consist of the same or
2 different material compared with that utilized for the building block.

1 21. The device of claim 17, where different building blocks in a chosen lattice net, should
2 the lattice net possess multiple Wyckoff sites per unit cell, may consist of the same or
3 different material.

1 22. The device of claim 17, where the mechanical connections may consist of different
2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
3 the particular intended function of the device.

1 23. The device of claim 17, where the different building blocks may consist of different
2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
3 the particular intended function of the device.

1 24. A subwavelength device, made of a single material, capable of possessing a
2 subwavelength spectral gap for vibration isolation of long-wavelength vibrations, where the
3 incident wavelength is at least twice the unit cell dimensions.

1 25. The device of claim 24, wherein a portion of the device consists of a phononic
2 metamaterial with one or more sub-wavelength spectral gaps.

1 26. The device of claim 24, where the metamaterial can be either silicon or other
2 semiconductor, a metal, a ceramic, a polymer, or a composite (including solid and liquid
3 foams, nanocomposites) as well as gels and fluids and suspensions/emulsions and comprises
4 a lattice array of unit cell building blocks consisting of solid blocks or liquid objects
5 connected by mechanical connections.

1 27. The device of claim 24, where different building blocks in a chosen lattice net, should
2 the lattice net possess multiple Wyckoff sites per unit cell, may consist of the same or
3 different material.

1 28. The device of claim 24, where the mechanical connections may consist of different
2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
3 the particular intended function of the device.

1 29. The device of claim 24, where the different building blocks may consist of different
2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
3 the particular intended function of the device.

1 30. A subwavelength device, made of a single material, capable of possessing a
2 subwavelength double negative index band for focusing of vector mechanical waves, or
3 vibrations.

1 31. The device of claim 30, wherein the portion of the device consists of phononic
2 metamaterial with a sub-wavelength double negative index band.

1 32. The device of claim 30, where the entire metamaterial can be silicon or other
2 semiconductor, a metal, a ceramic, a polymer, or a composite (including solid and liquid
3 foams, nanocomposites) as well as gels and fluids and suspensions/emulsions and comprises
4 a lattice array of unit cell building blocks consisting of solid blocks or liquid objects
5 connected by mechanical connections.

1 33. The device of claim 30, where different building blocks in a chosen lattice net, should
2 the lattice net possess multiple Wyckoff sites per unit cell, may consist of the same or different
3 material.

1 34. The device of claim 30, where the mechanical connections may consist of different
2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
3 the intended function of the device.

- 1 35. The device of claim 30, where the different building blocks may consist of different
- 2 materials in order to optimize damping of mechanical or acoustical energy, or performance of
- 3 the intended function of the device.

FIG. 1a

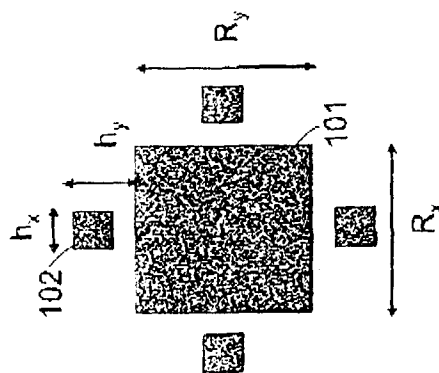


FIG. 1d

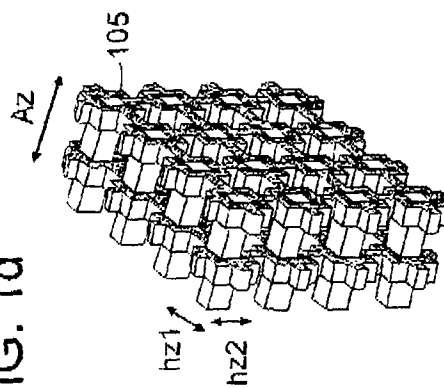


FIG. 1c

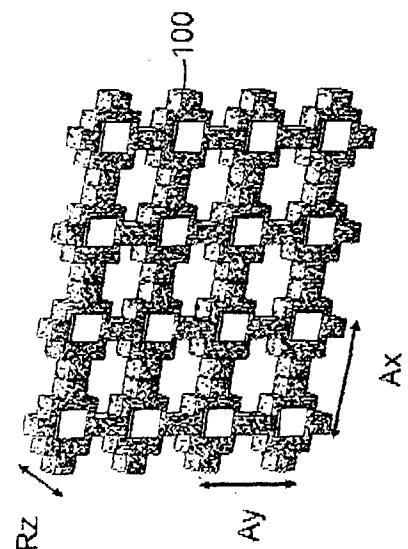


FIG. 1b



FIG. 1e

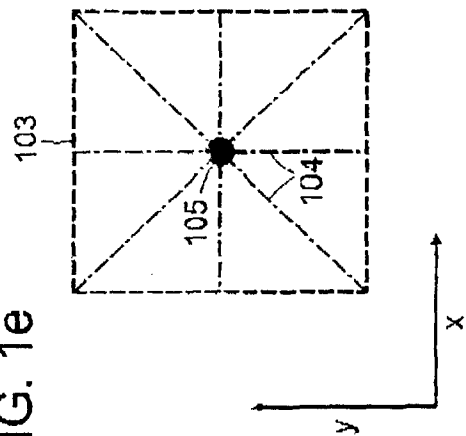


FIG. 2b

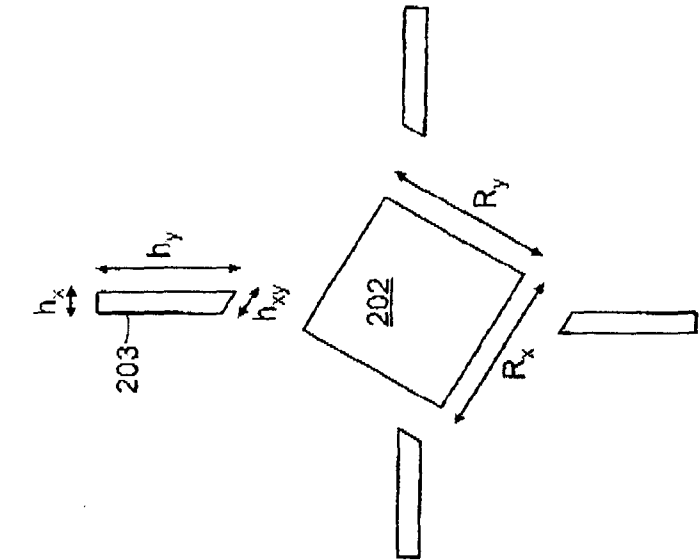


FIG. 2a

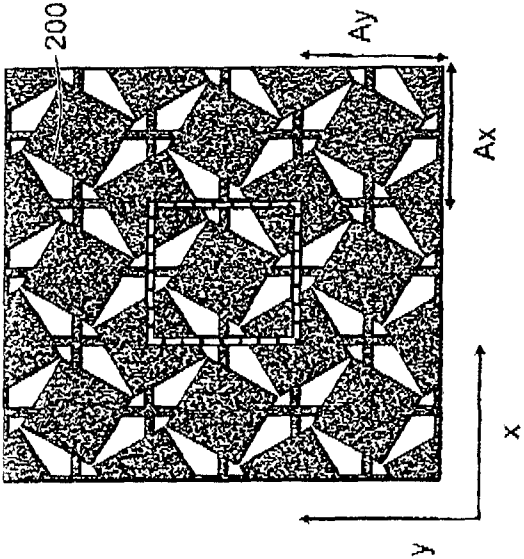
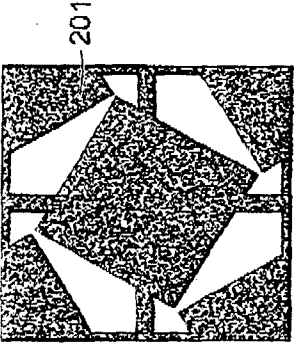


FIG. 2c



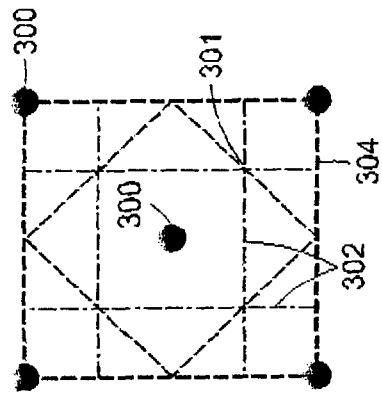


FIG. 3a

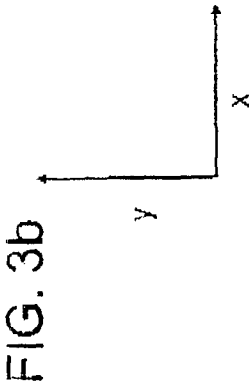
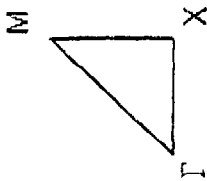
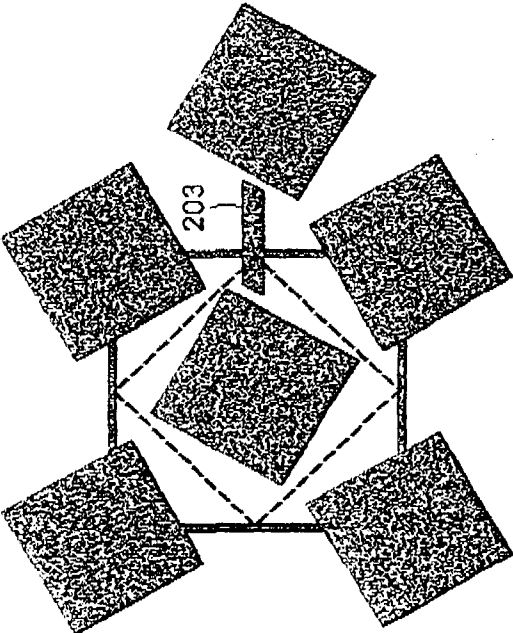


FIG. 3b



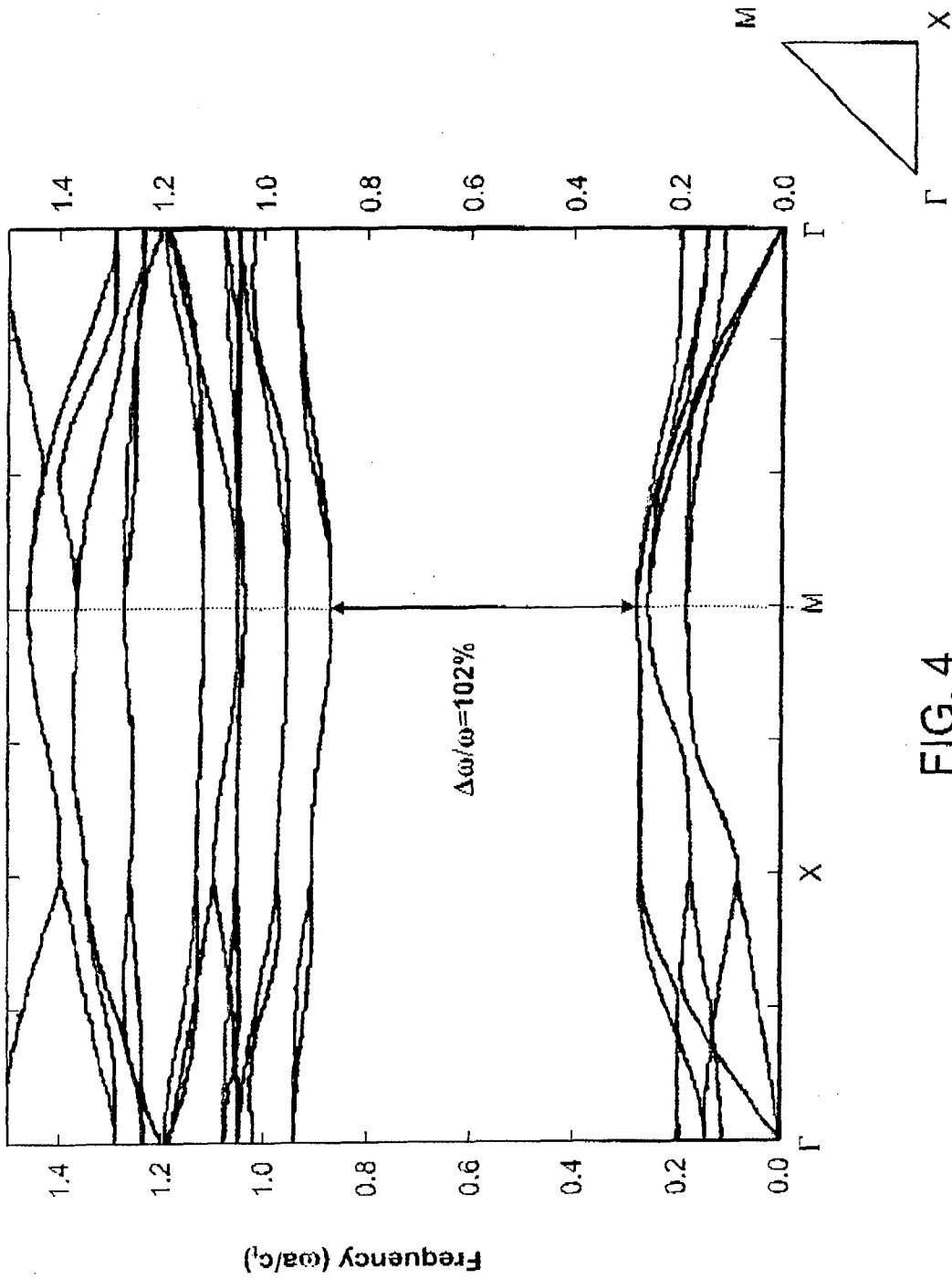


FIG. 4

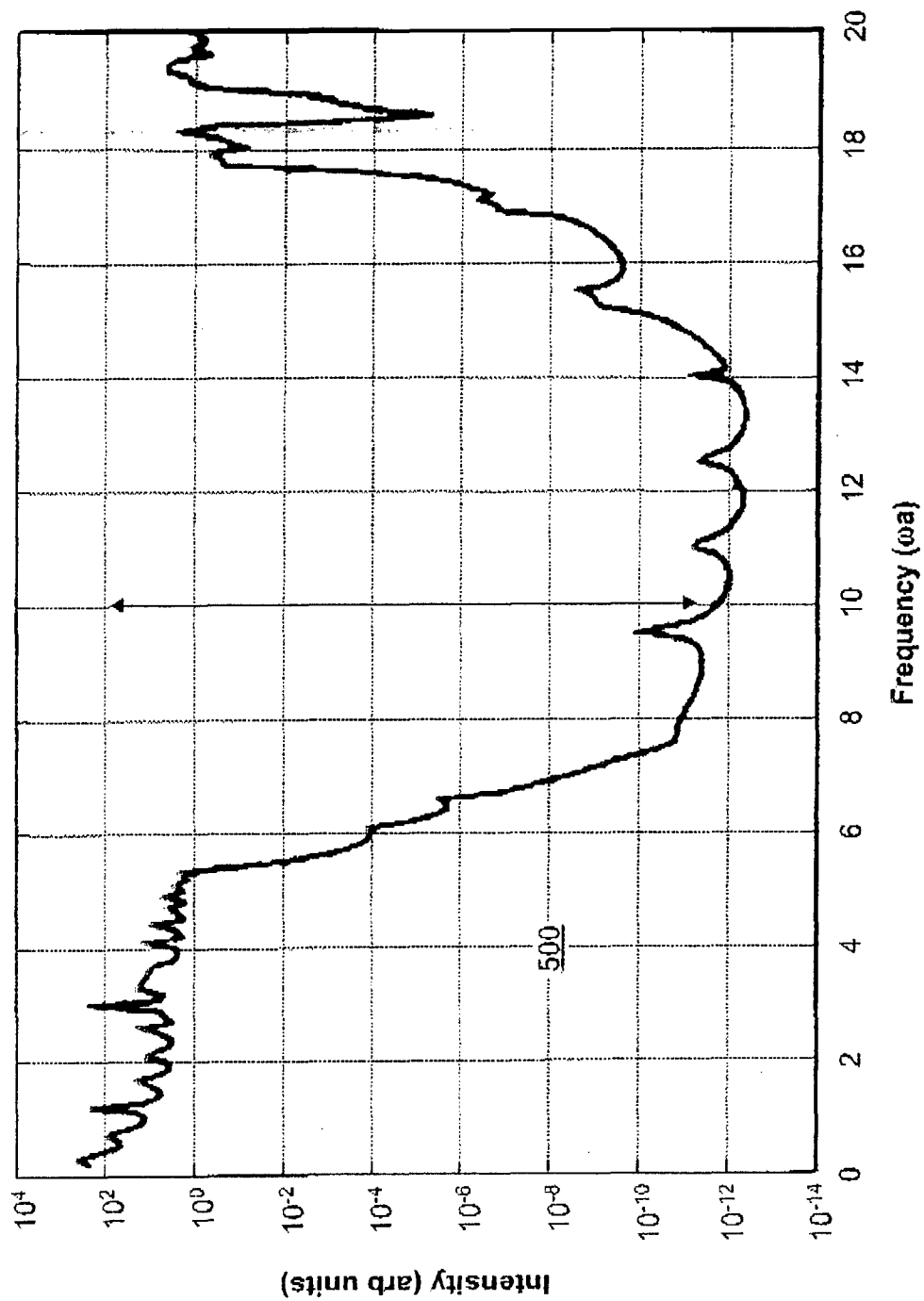
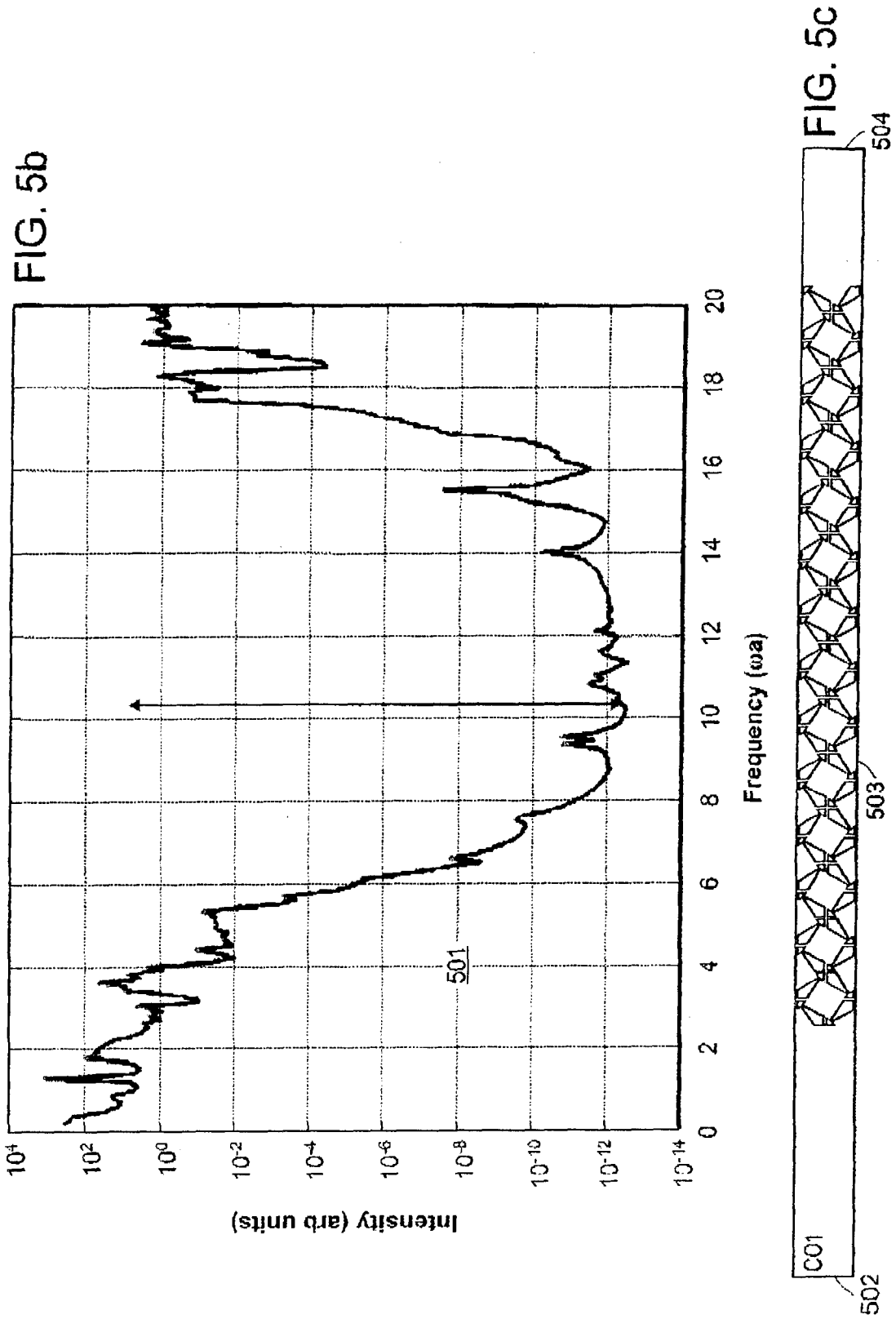


FIG. 5a



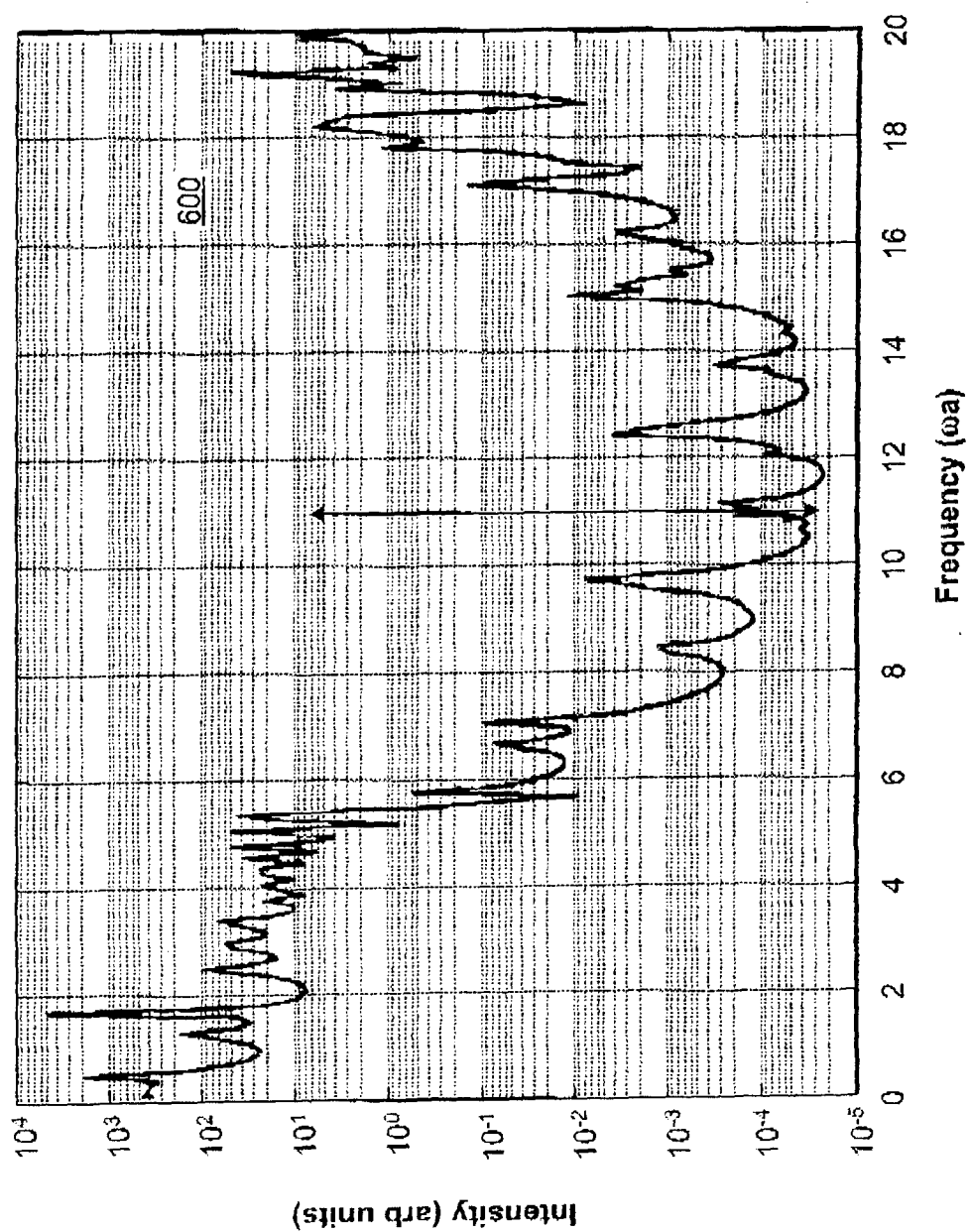


FIG. 6a

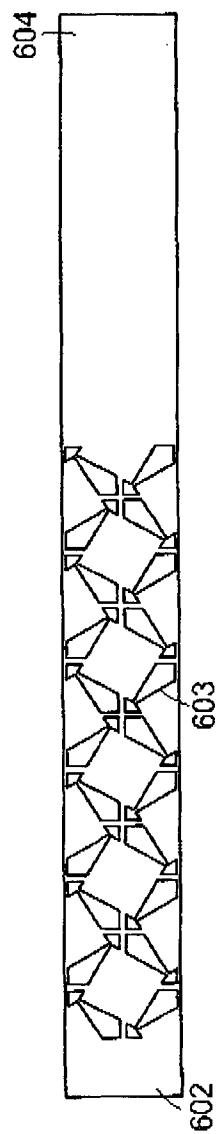


FIG. 6b

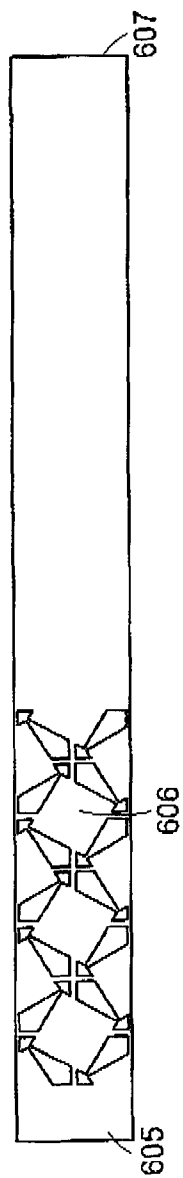


FIG. 6c

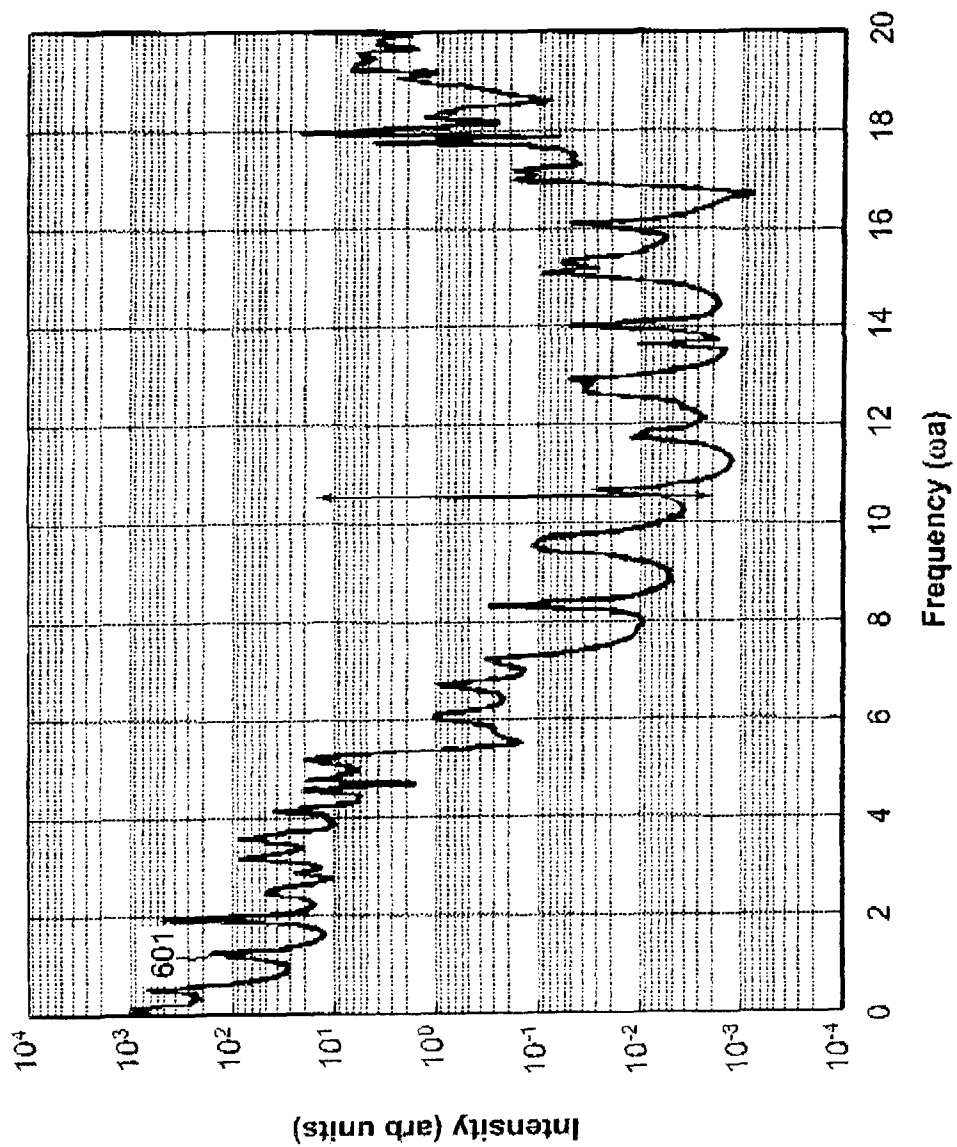


FIG. 6d

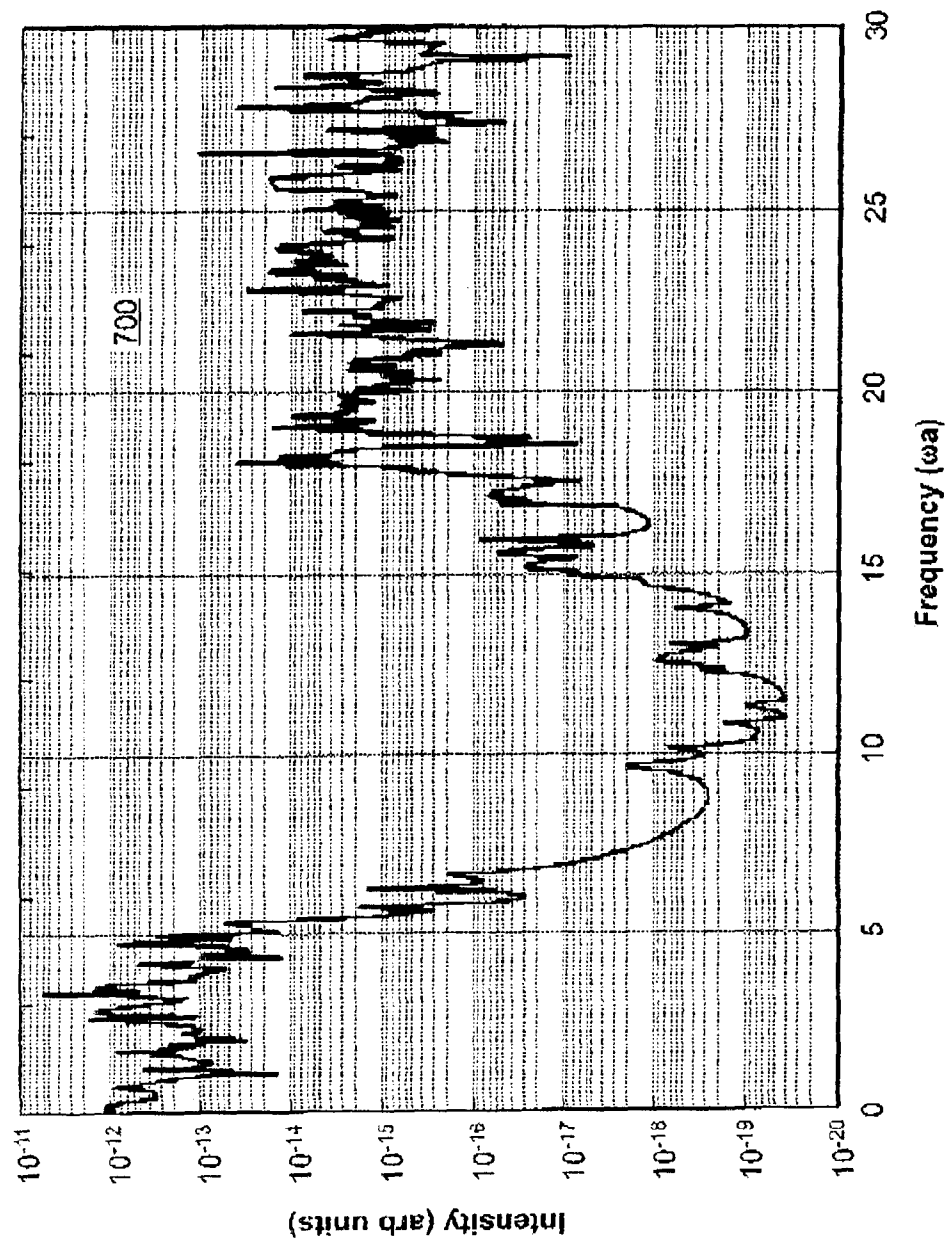


FIG. 7a

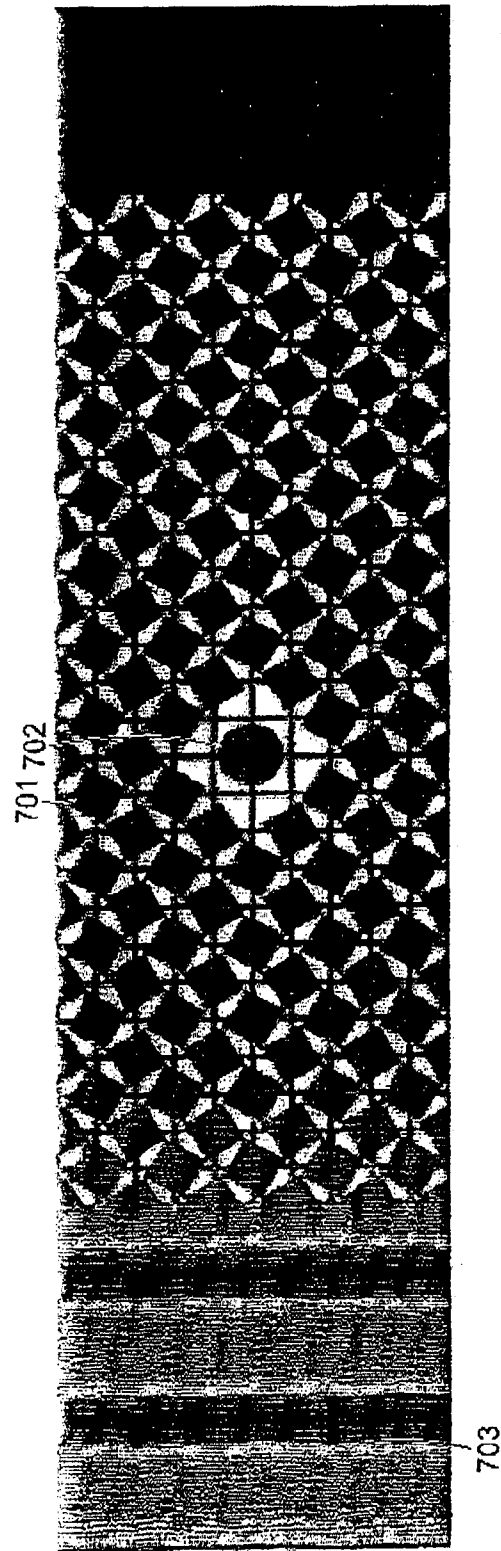


FIG. 7b

FIG. 8a

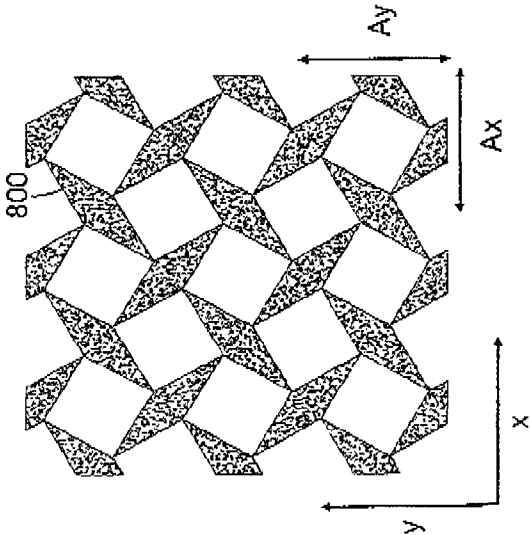


FIG. 8b

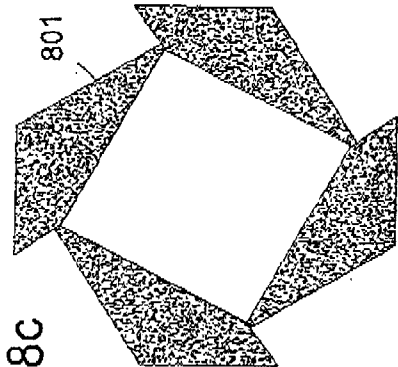
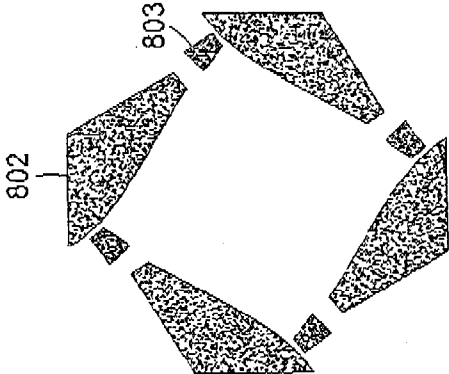


FIG. 9a

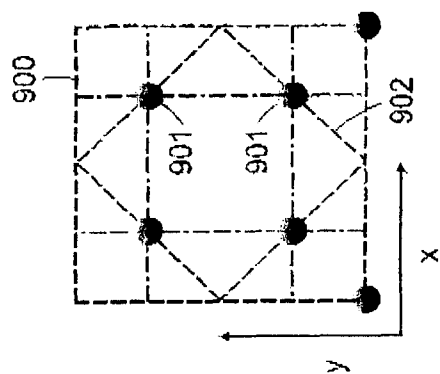


FIG. 9b

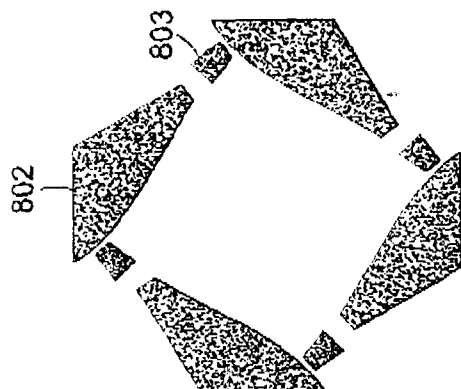
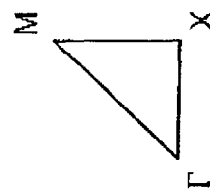
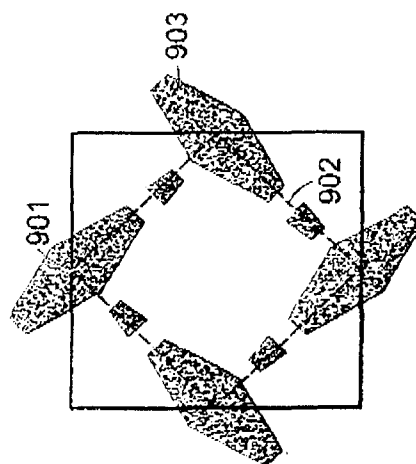


FIG. 9c



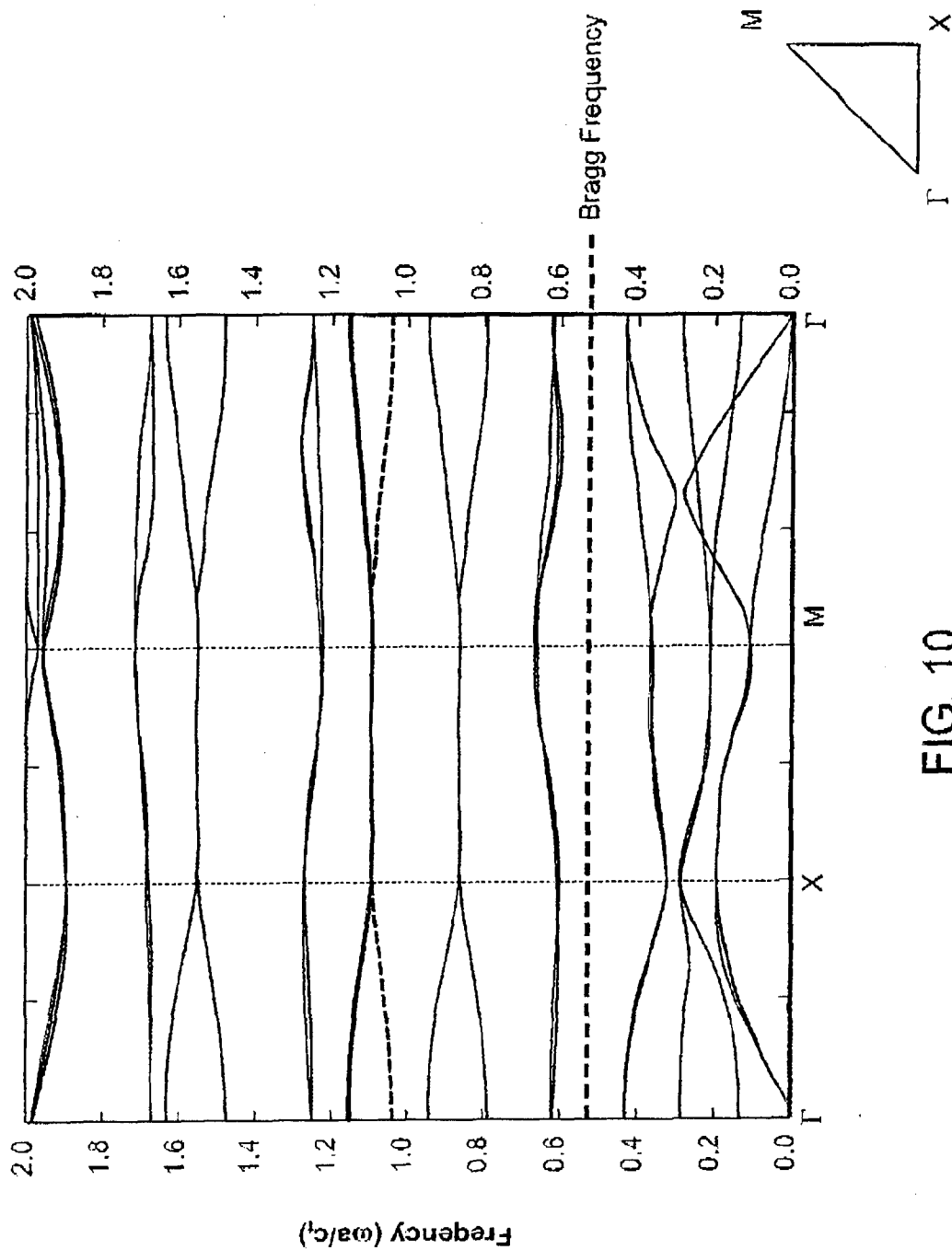
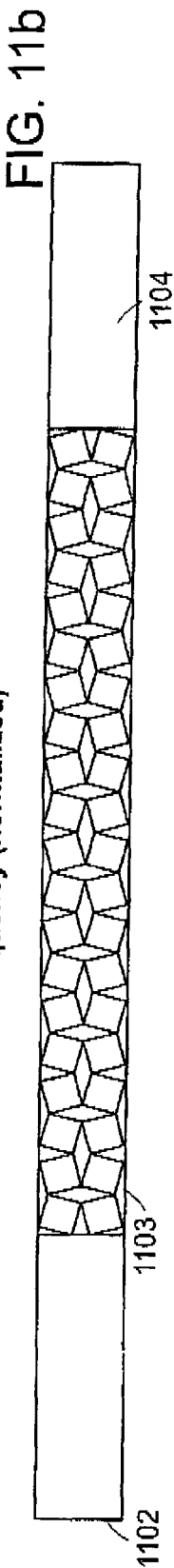
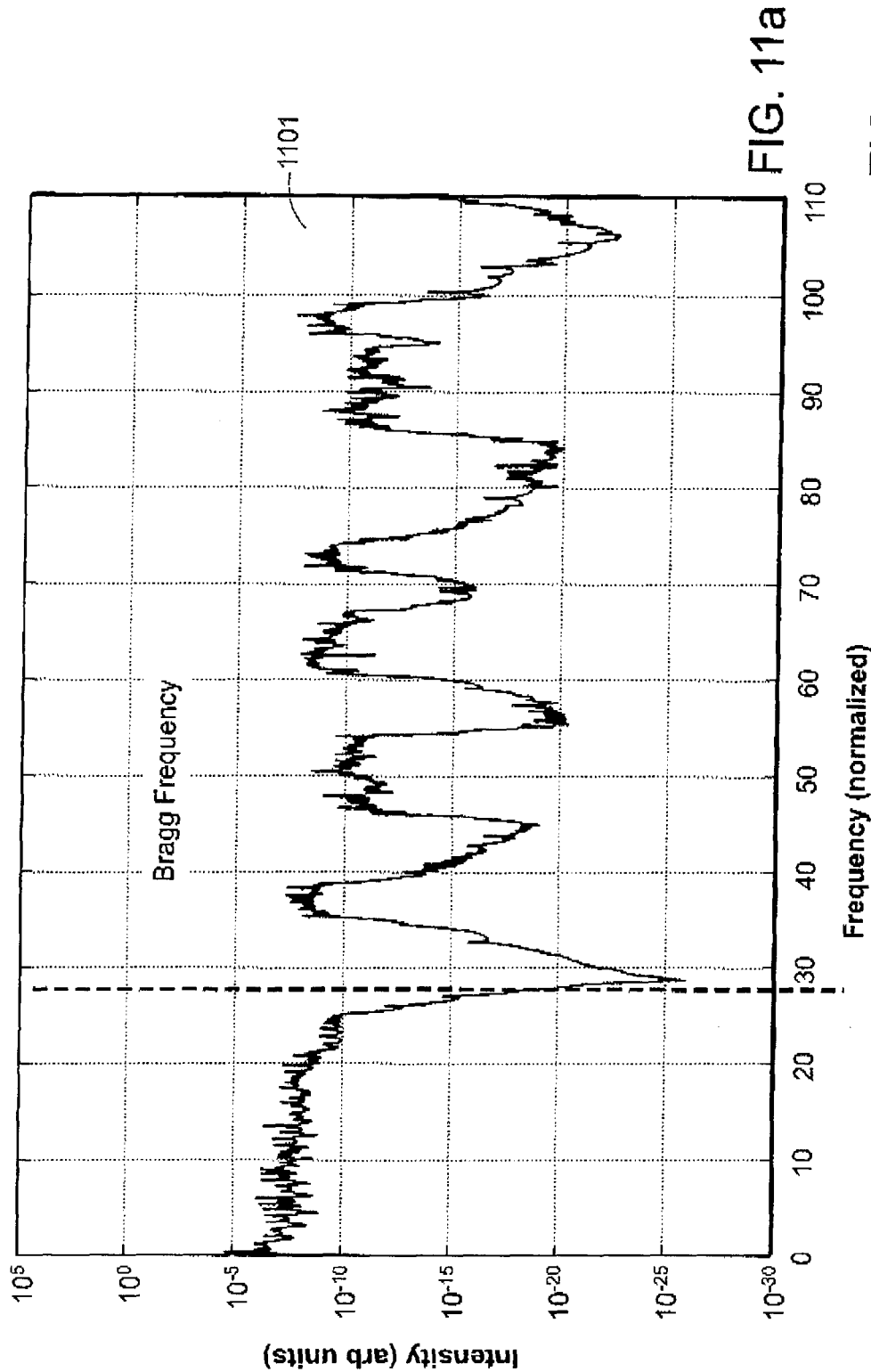


FIG. 10



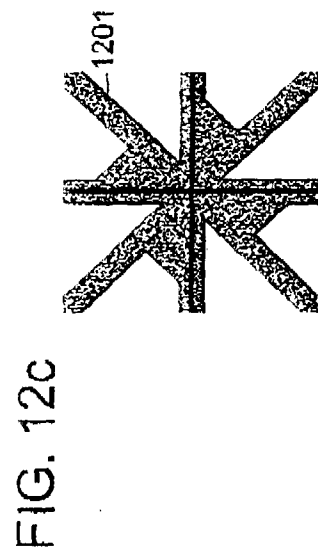
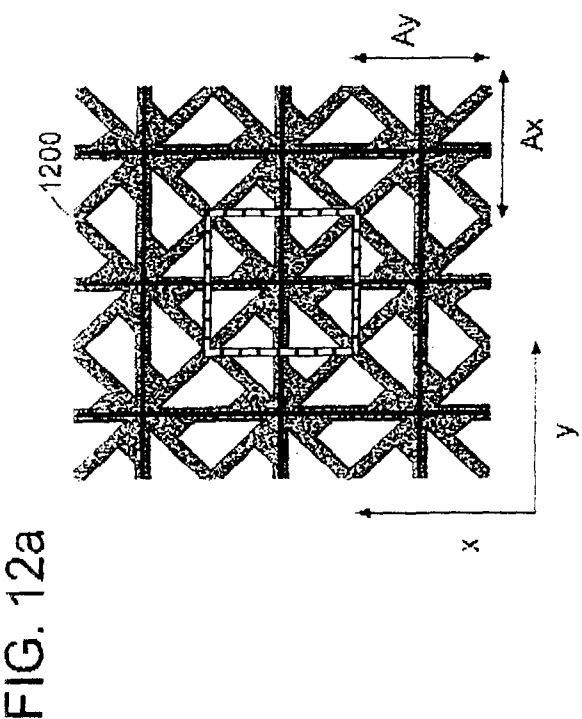
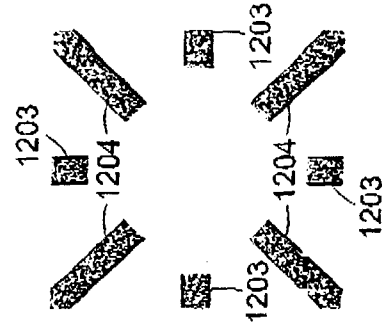
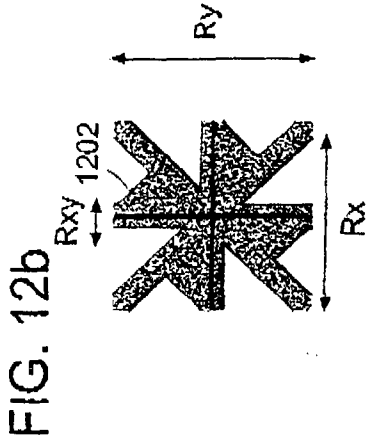


FIG. 13a

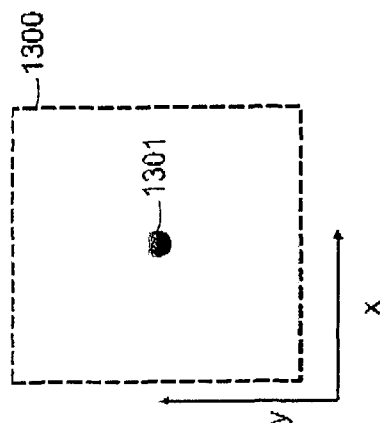


FIG. 13b

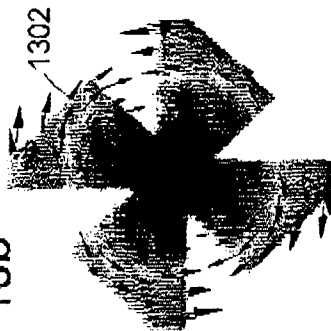


FIG. 13c

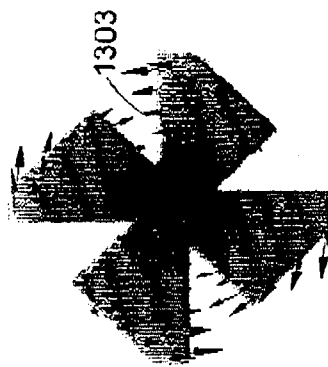
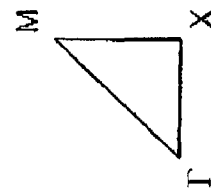
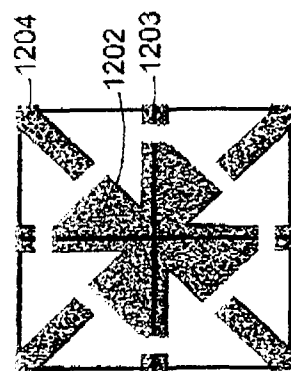


FIG. 13d



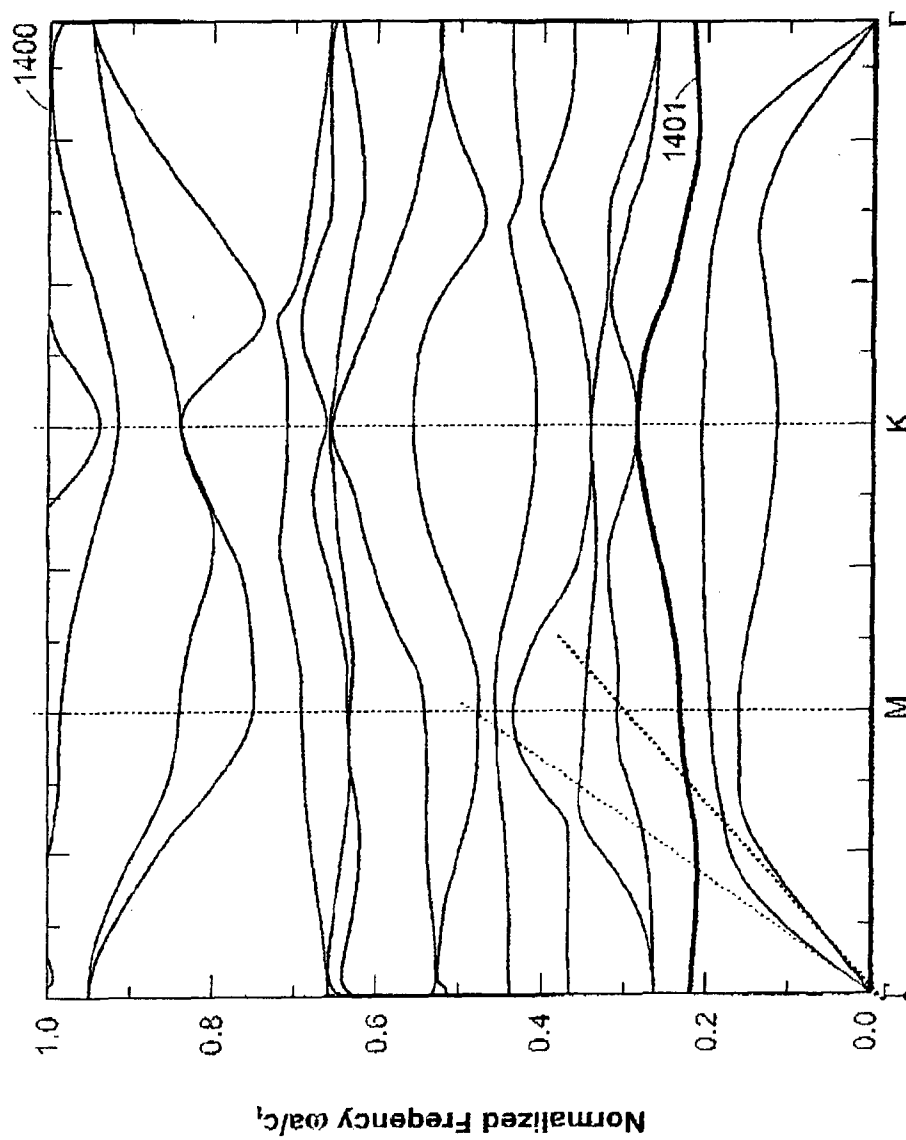


FIG. 14

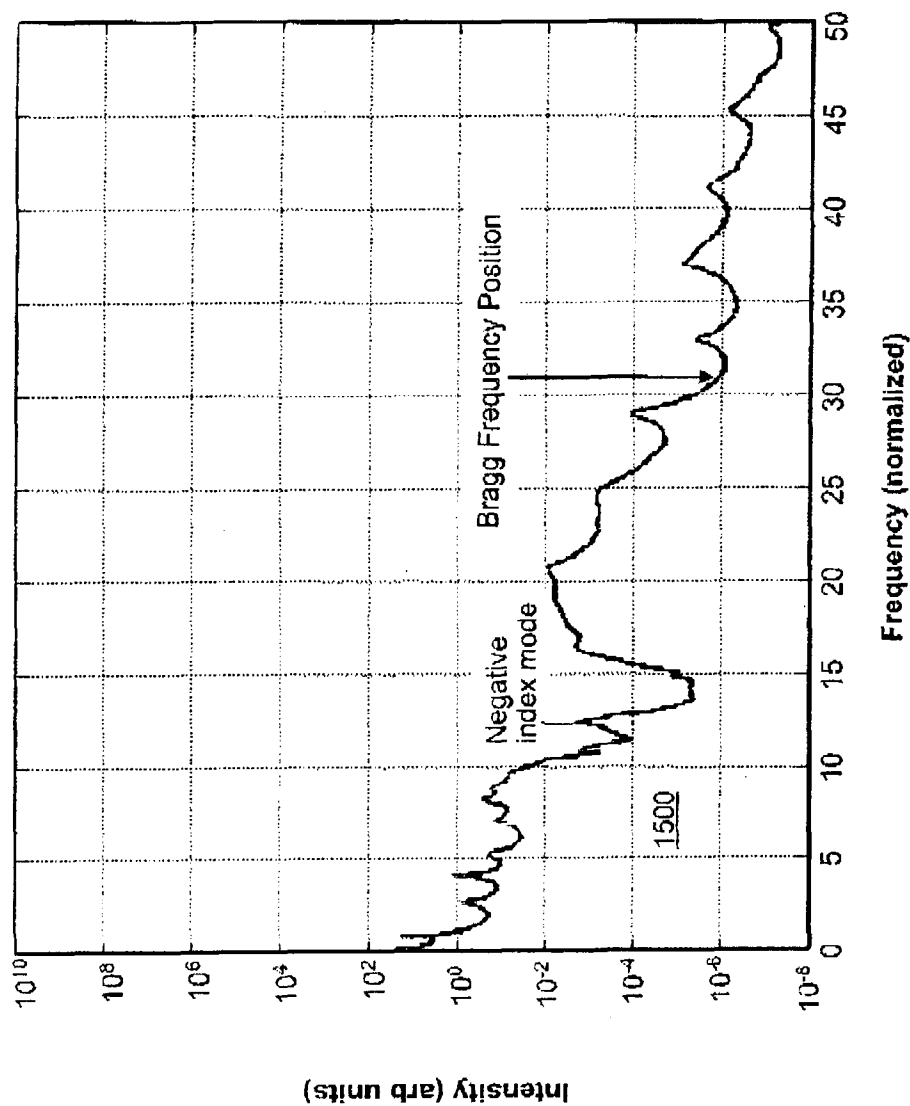


FIG. 15a

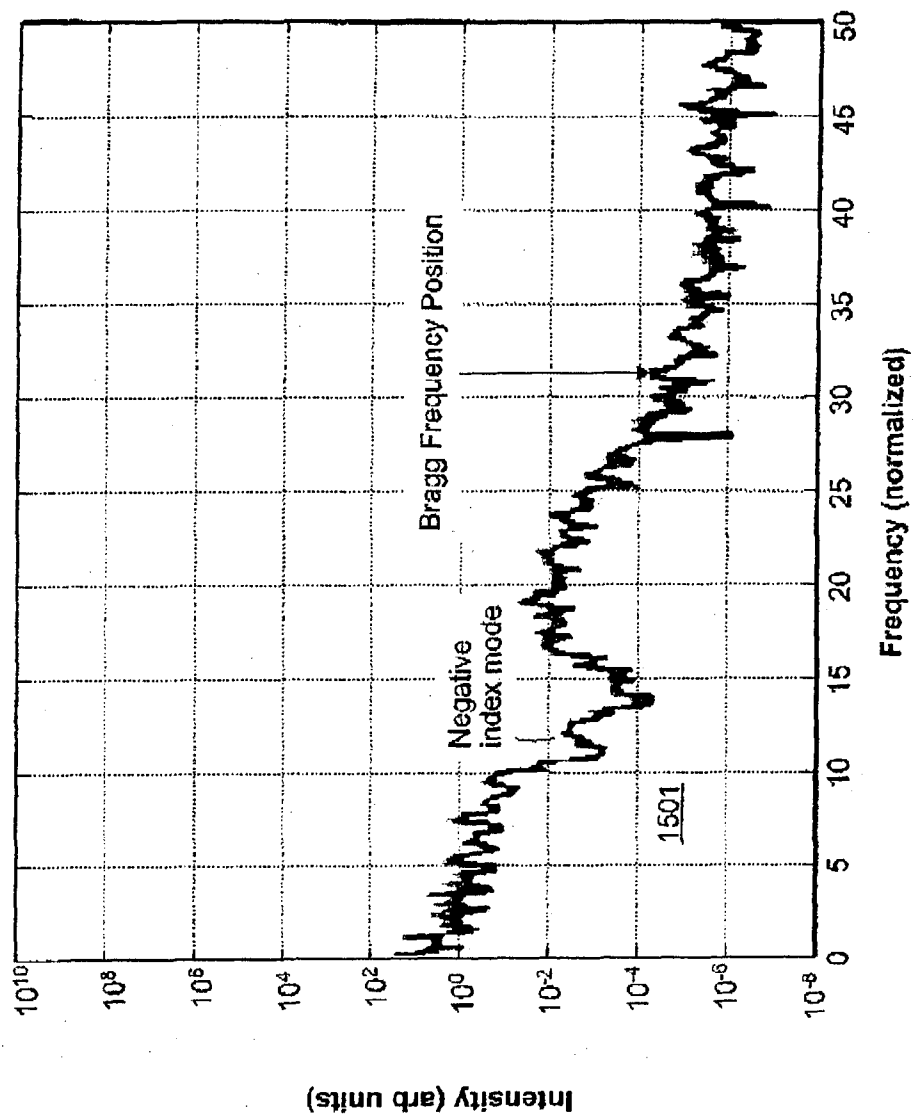


FIG. 15b

