FIG. 1


FIG. 2


FIG. IA


F/G. 2A


FIG. 3


FIG. 4


F/G. 5


FIG 6


# UNITED STATES PATENT OFI 

## 2,211,551

RADIATHNG SYSTEM
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## Application August 19, 1941, Serial No. 407,457

4 Claims. (Cl. 177-386)

## 1

This invention relates to improved directional compressional wave radiating systems of the multielement type. More particularly it relates to radlating systems in which the energy is distributed non-uniformly over the elements of the radiating system to reduce the relative strength of secondary radiation lobes with respect to the main radiation lobe.
A principal object of the invention is therefore to produce directional radiating systems having relatively small secondary radiation lobes.
Another object of the invention is to reduce secondary lobe radiation from multicrystal radiating systems.

A further object is to reduce secondary lobe radiation from multiunit magnetostrictive radiating systems.
Other and further objects will become apparent during the cuarse of the following description and in the appended claims.
The systems of the invention will be more readily understood from the following description of illustrative embodiments taken in conjunction with the accompanying drawing in which:
Fig. 1 illustrates a radiating element of substantial suriace area uniformly driven;

Fig. $1 a$ indicates the directive radiating pattern of the surface of Fig. 1;

Fig. 2 illustrates a radiating element of substantial surface area driven with straight line variation of intensity from zero intensity at the ends to maximum intensity at the center;
Fig. $2 a$ indicates the directive radiating pattern of the surface of Flg. 2;
Fig. 3 infustrates a radiating element of suivstantial surface area driven with sinusoidal variation of intensity from zero intensity at the ends to maximum intensity at the center;
lig. 4 shows a radiating system comprising a plurality of piezoelectric crystals aligned to form a multielement radiating surface, the driving electrode areas of said crystals varying from very narrow areas for the outermost crystals to substantially complete coverage of the central crystal;

Fig. 5 shows a radiating diaphragm of substantial surface area driven by a plurality of magnetostrictive vibrators, the driving intensity varying from small intensity at the outermost vibrators to maximum intensity at the center vibrator; and

Fig. 6 shows a sound radiator of the multisection wave filter type with energy radiation provided from each section of the structure.

In more detail in Fig. 1 a member or diaphragm 10 is assumed to be driven from position $a$ to position $b$ with uniform amplltude at all points thereof. This may be accomplished, for example, by the well known electromagnetic type of driving mechanism employed in the so-called dynamic
type of loudspeaker such as, $f_{1}$ disclosed in United States Pat sued May 7, 1929, to A. I. Abra: driving mechanism is not show it would unnecessarily compli Such mechanisms are well know are not involved in systems of will become apparent presently.

For radiating surfaces of the by member 10 of Fig. 1, characte particle velocity over the surfs well known that the directional will be substantially as indicate acterized by a main lobe 12 of directivity and secondary lobes small but not negligible streng appreciably in angular directivi lobe.

For directive systems in whic] directive indications are desirec of radiators of the type illustrat been found to be objectionables is sometimes misled by minor lok tains false directive indication
It is well known in the art member such as 10 of Fig. 1 uniy have a pattern of the type descri nection with Fig. $1 a$ and represe tion.

$$
\frac{P_{(\theta)}}{P_{N}}=\frac{\sin \left(\frac{\omega L}{2 v} \cos \right.}{\frac{\omega L}{2 v} \cos \theta}
$$

where $L$ is the length or width is $2 \pi$ times the frequency, $v$ i propagation in the medium, $\theta$ i ured between the direction of $t$ length of the radiator as showr the pressure at the angle $\theta$, an sure normal to the radiator. Tr that if most of the radiation within $\pm 1^{\circ}$ from the normal, th be about 57 wave-lengths across plications would be inconvenie

Also, secondary lobes will exi

$$
\left(\frac{\omega L}{2 v} \cos \theta\right)=\frac{3 \pi}{2}
$$

etc., whose values compared to

$$
\frac{2}{3 \pi}=13.5 \mathrm{db} \cdot ; \frac{2}{5 \pi}=17.9 \mathrm{db} \cdot ; \frac{2}{7 \pi} ;
$$

The first lobe is only 13.5 de pared to the main one and ma tioned, introduce some difficu readings.

A method for reducing secc respect to the main one is discu $2,225,312$, issued December 17, 0 thereof, column 1, line 75 to c

As applied to the xadiator of Exg. 1, this method requires the particle velocity at the edge of the radiator to be much less than that at the center. A distribution investigated, by way of example, was one in which the particle velocity was aero at the edges and increased linearly to the center as indicated for the diaphragm 20 of Fig. 2, dotted lines as and $b$ indicating the mode of vibration of diaphresm 20. gor thas distribution the radiathon pattere is ilustrated by curve 82 of सig. $2 a$ and is given by the equation

$$
\begin{equation*}
\frac{P^{H}(\theta)}{P_{(N)}}=\left[\frac{\sin \left(\frac{\omega L}{4 v} \cos \theta\right)}{\frac{\omega L}{4 v} \cos \theta}\right] \tag{3}
\end{equation*}
$$

For this distribution the first minimum comes at twice the angle as for the uniform distribution or Fig. 1, but the secondary lobes are down compared to the tumamental by the values

$$
\begin{align*}
& \left(\frac{2}{3 r}\right)^{2}=27.0 \mathrm{db} ;\left(\frac{2}{5 \pi}\right)^{2}=35.8 \mathrm{db} \text {; } \\
& \left(\frac{2}{7 x}\right)^{2}=41.6 \mathrm{db} ., \text { etc. } \tag{4}
\end{align*}
$$

To get the same shorpness requires a radiator with twice the length, but all the radiation maxima are down twice as far in decibels as for the uniform radiaror.

A sadiator in which the secondary maxima are not down quite as far, but which requires only a 50 per cent lexger radiator to get the same sharpness is shown in Iig. 3. For this radiator the particle velocity of dicjoragm 80 is substantially zero on the two eads and hes a sine wave distribution of particle velocity between dotted lines $a$ and $b$ indicating the mode of vibration of diaphragm 30. A sine wave distribution of energy as applied to a multitube directive acoustic receiver is discussed and analyzed in my abovementioned Patẻnt 2,225,312 on pages 2 and 3 thereof; page 2 , column 2, line 48 to page 3, column 1, line 10. In the device of the patent the areas of the respective tubes, or their orifices, are varied stibstantially in accordance with a sinusoidal law of variation. In this particular instance the yow of tubes is wound about itself to lorm a compact assembly so that the tubes may be more readily associated with a conventional type of receiver-microphone and to facilitate the pointing of the assembly. Fior the type of radiator illustrated by Fig. 3 and the arrangement of my patent jusi meationed the distribution pattern is given by the equation

$$
\begin{equation*}
\frac{P(\theta)}{P(N)}=\frac{\cos \left(\frac{\omega L}{2 v} \cos \theta\right)}{1-\left(\frac{\omega L}{\pi v} \cos \theta\right)^{2}} \tag{5}
\end{equation*}
$$

The nrst minumun comes when

$$
\begin{equation*}
\left(\frac{\operatorname{s} L}{2 \theta} \cos \theta\right)=\frac{3 \pi}{2} \tag{6}
\end{equation*}
$$

which is 50 per cent larger than that of Fig. 1 , but the secondary lobes heve the values with respect to the primary lobe of

$$
\begin{equation*}
\frac{1}{15}=23.5 \mathrm{db} . ; \frac{1}{35}=30.8 \mathrm{db} . ; \frac{1}{63}=36 \mathrm{db} . \tag{7}
\end{equation*}
$$

This decreases the frst secondary lobe with re-7 spect to the primary by 10 decibels at the expense of widening the radiator only 50 per cent to retain the same sharpness of the primary lobe.
Flgs. 4 and 5 show two methods of realizing particle velocity distributions of the above and
similar types for plezoelectric tive radiating systems, respect tric radiator frequently used c or an "array" of substantially salt crystals connected in pa physically to present, substan radiating surface as represen 42, 18 and 66 of Fig. 4.

In one common form the ro all be mounted on a common $b$ for example, could be placed crystals of me. 4 and have the crystals cemented to it, the crystals forming a radiating s able area. An alternate com would be to support all the cry employ radiation from both to of the crystals. The crystals $\varepsilon$ trically in parallel across the lator 48.
To reduce the secondary lob suggested above, we can use arrangements of crystals bu width of the electrodes, or plat trodes are emplosed, so that $\varepsilon$ the crystals 46 on the ends 1 trodes, or plating areas, wher in the center has its sides com the electrodes, and intermedi electrodes of intermediate wid creasing with proximity to the viding that the plating, or elec same length as the crystals $\varepsilon$ vary in width only, the force es dividual crystal will be propori ing or electrode area and the di portional to the force since al similar. Hence, if the area of linearly from the two ends of center, the radiation pattern be obtained, whereas if the ares or plating, is distributed accord curve with the maximum at the zero on the end crystals, the dis tion 5 will be obtained. In tl plating areas should vary as tal of the tubes of the acoustic de mentioned Patent 2,225,312 bee column 2, line 47 as above poil present application being the electric vibrators and a being

$$
\frac{\pi}{n+1}
$$

An alternative arrangement, tenuator for each crystal, or ea at a particular distance from array, would be to use crystals trodes but to limit, by interposi suitable amounts, the energy to tals to obtain an appropriat energy among them.

Flg. 5 shows one way of obtall particle velocity distribution strictive drive. For this cas diaphragm 50 clamped on the a number of magnetostrictive Since the edges are clamped $t$ and the shape assumed by th vibrating will be nearly that giving the radiation patiern sho The central magnetostrictive : course driven most strongly and 56 progressively less strong all energy distribution preferab
tially sinusoidal, from a madimum at the center to minima at the ends. The desired non-uniform distribution of energy may be effected by proportioning the windings of the magnetostrictive members as indicated in Flg. 5 or allested natively by employing attenuators as suggested above for crystal arrays. The magneto-strictive members are connected electrically in parallel across the output of an oscillator 68.
In Fig. 6 a sound radiator in the form of a multi-section wave filter having sixteen sections 80, 81, 82, 83, 88, 85, 86 and 87 (two sections on opposite sides of the center of the structure being assigned the same number plurallty of plezothe left end of the struclosed in a housing member electric crystals $9 n$ enclosediz the structure and 89, are employed a member 88 of absorbing mateat the right end a memberb such energy as may reach the right end of the filter.
Each of the sections comprises a cup-like member of square cross-section, the cup bottoms ${ }^{2}$ serving as diaphragms, coupling adjacent cavities. Each section is provided with several holes from which a small portion of the total energy passing through the filter is radiated. The hole sizes are adjusted so that maximum energy is radiated from the central sections 81 and decreasing amounts of energy from sections 88,85 , 84, 83, 82, 81 and 80, respectively, in accordance with their respective distances from the center. Because of attenuation and loss of energy by radiation the sections on the right half of the structure will have somewhat larger holes in order to radiate the same energy as corresponding sections of the left half of the structure. Again, the distribution of radiated energy may vary from maximum at the central elements to minima at each end in accordance with a straight line, sinusoidal, geometrical progression or other law of variation depending upon the particular performance desired.
The structure of Fig. 6, though of different form and proportions, is of the same general type as that illustrated by Figs. 15, 16 and 17 of, and described in, my copending application, Serial No. 381,236, filed March 1, 1941, entitled "Pipe antennas and prisms."
Obviously, an array of magnetostrictive vibrat-

Ing members similar to the crystal array of 7he. 4 could be employed without a diaphragm, or, conversely, a plurality of crystals could be employed in place of the magnetostrictive vibrators of Fig. 5 to drive the diaphragm 50 , sinusoidally, and numerous other arrangements within the spirit and scope of the invention can readily be devised by those skilled in the art. No attempt to exhaustively cover such arrangements has here been made. The scope of the invention is deflned in the appended clalms.

What is claimed is:

1. A piezoelectric radiator comprising a plurality of substantially identical plezoelectric crystals arranged in line, corresponding radiating ends of the crystals lying in a common plane, a pair of electrodes on each crystal, the electrodes extending in every case the full length of the crystals, the width of the electrodes on the end crystals of the line being small with respect to the width of the crystals, the width of electrodes for intermediate crystals being progressively greater as the center of the line is approached, the central crystal or crystals having electrodes of greatest width whereby minor lobe radiation from said array of crystals is substantially reduced.
2. In a directive radiating system a plurality of substantially identical plezoelectric crystals allgned in parallel relation with particular radiating ends of each in a common plane, the electrode plating on each crystal extending the full length of the crystal, the wldth of the plating varying from a small fraction of the width of the crystal for the outermost crystals to substantially the full width of the crystal for the centrally positioned crystal, the variation in plating area following a substantially slnusoldal law of variation.
3. The radiator of claim 1 the electrode area varying from the central to the end crystals substantially in accordance with a straight line law of variation.
4. The radiator of claim 1 the electrode area
varying from the central to the end crystals substantially in accordance with a power series law of variation.
