

(19) World Intellectual Property Organization  
International Bureau



(43) International Publication Date  
18 October 2007 (18.10.2007)

PCT

(10) International Publication Number  
**WO 2007/116262 A1**

(51) International Patent Classification:

G06F 7/72 (2006.01)

(21) International Application Number:

PCT/IB2007/000728

(22) International Filing Date: 23 March 2007 (23.03.2007)

(25) Filing Language: English

(26) Publication Language: English

(30) Priority Data:

06300320.6 31 March 2006 (31.03.2006) EP

(71) Applicant (for all designated States except US): AXALTO SA [FR/FR]; 6 Rue De La Verrerie, F-92197 Meudon (FR).

(72) Inventors; and

(75) Inventors/Applicants (for US only): VIGILANT, David [FR/FR]; C/o Axalto Sa, Intellectual Property Dpt, 06 rue de la Verrerie, F-92197 Meudon (FR). FUMAROLI, Guillaume [FR/FR]; C/o Axalto Sa, 06 Rue De La Verrerie, F-92197 Meudon (FR).

(74) Common Representative: AXALTO SA; C/O WLO-DARCZYK Lukasz, 6 Rue de la Verrerie, F-92197 Meudon (FR).

(81) Designated States (unless otherwise indicated, for every kind of national protection available): AE, AG, AL, AM,

AT, AU, AZ, BA, BB, BG, BH, BR, BW, BY, BZ, CA, CH, CN, CO, CR, CU, CZ, DE, DK, DM, DZ, EC, EE, EG, ES, FI, GB, GD, GE, GH, GM, GT, HN, HR, HU, ID, IL, IN, IS, JP, KE, KG, KM, KN, KP, KR, KZ, LA, LC, LK, LR, LS, LT, LU, LY, MA, MD, MG, MK, MN, MW, MX, MY, MZ, NA, NG, NI, NO, NZ, OM, PG, PH, PL, PT, RO, RS, RU, SC, SD, SE, SG, SK, SL, SM, SV, SY, TJ, TM, TN, TR, TT, TZ, UA, UG, US, UZ, VC, VN, ZA, ZM, ZW.

(84) Designated States (unless otherwise indicated, for every kind of regional protection available): ARIPO (BW, GH, GM, KE, LS, MW, MZ, NA, SD, SL, SZ, TZ, UG, ZM, ZW), Eurasian (AM, AZ, BY, KG, KZ, MD, RU, TJ, TM), European (AT, BE, BG, CH, CY, CZ, DE, DK, EE, ES, FI, FR, GB, GR, HU, IE, IS, IT, LT, LU, LV, MC, MT, NL, PL, PT, RO, SE, SI, SK, TR), OAPI (BF, BJ, CF, CG, CI, CM, GA, GN, GQ, GW, ML, MR, NE, SN, TD, TG).

Declaration under Rule 4.17:

— of inventorship (Rule 4.17(iv))

Published:

— with international search report  
— before the expiration of the time limit for amending the claims and to be republished in the event of receipt of amendments

[Continued on next page]

(54) Title: PROTECTION AGAINST SIDE CHANNEL ATTACKS

A cryptographic mechanism according to the invention

INPUT:  $X, D = \{d_0, d_1, \dots, d_{n-1}\}_2$

OUTPUT:  $X^D$

1. generate a random number  $R$  having an inverse (denoted  $R^{-1}$ )
2.  $VAR_0 \leftarrow R, VAR_1 \leftarrow X * R, MSK_n \leftarrow R^{-1}$
3. For  $i$  from  $n-1$  down to 0 do
  - {MUL}  $VAR_{1-di} \leftarrow VAR_{1-di} * VAR_{di}$
  - {SQ}  $VAR_{di} \leftarrow VAR_{di} * VAR_{di}$
  - {SQ\_RD}  $MSK_i \leftarrow MSK_{i+1} * MSK_{i+1}$
4. Return  $VAR_0 * MSK_0$

(57) Abstract: The invention relates to a cryptographic mechanism and to a cryptographic device incorporating such cryptographic mechanism. The cryptographic mechanism offers a better resistance to side channel attacks than that of known cryptographic mechanisms by incorporating a new type of masking mechanism.

WO 2007/116262 A1



---

*For two-letter codes and other abbreviations, refer to the "Guidance Notes on Codes and Abbreviations" appearing at the beginning of each regular issue of the PCT Gazette.*

### Protection against side channel attacks

The invention relates to methods for protecting cryptographic devices  
5 against side channel attacks, and to cryptographic devices embedding such methods.

As known in the art, cryptographic devices are devices implementing cryptographic mechanisms. Examples of cryptographic devices include smart  
10 cards, USB keys, dongles, Personal Digital Assistants (a.k.a PDAs), mobile phones, personal computers (a.k.a PCs), etc. Such cryptographic devices are used in particular for securing a user's electronic transactions. The expression "electronic transaction" is to be taken in its broadest meaning. I.E. it is not limited to financial transaction but also contain any Internet transaction, any transaction  
15 occurring through a telecommunication network etc. Securing electronic transactions may comprise the cryptographic mechanisms of digitally signing electronic documents, decrypting electronic documents, negotiating session keys with a third party and/or authenticating a user. The above four cryptographic mechanisms are well known in the art. They are not limitative (other  
20 cryptographic mechanisms exist), and not mandatory (for example a cryptographic device does not necessarily embed a digital signature mechanism).

Cryptographic mechanisms have an input and an output. For example, an encryption mechanism may have an input consisting of a plaintext and an output  
25 consisting of a ciphertext. When first cryptographic devices were designed, people had the feeling that the only attacks possible on their cryptographic mechanisms consisted in attacking the input and output. However, it turned out that cryptographic devices are also susceptible to so-called "side channel attacks". Side channel attacks rely on the fact that a cryptographic device has  
30 input and output means other than the legitimate input and output means. For example use of illegitimate input means may comprise altering cryptographic

operations by heating the cryptographic device, by modifying its clock (e.g. speeding up above the recommended limit), by putting it under UV light, X-Ray, or ultrasonic waves, by shaking it or otherwise mechanically acting on it, etc. Such alteration can be carefully designed (for example a glitch can be introduced at the exact moment that a counter is about to be decremented) or can be random (for example the aim might simply be to induce a random fault and analyze the consequence of the fault, which may leak sensitive information). Use of illegitimate output means may comprise analyzing the power consumption of the cryptographic device (e.g. an electronic component requires more electric power to perform a complex operation such as "square and multiply" than it does for a simple operation such as "square only"), analyzing the electromagnetic field created by the cryptographic device, analyzing the sounds emitted by the cryptographic device, etc. Well-known side channel attacks include Simple Power Analysis (SPA), Differential Power Analysis (DPA) or Differential Fault Analysis (DFA).

Cryptographic mechanisms consist of mechanisms involving at least a secret  $D$  which is supposed to be stored securely in a cryptographic device.  $D$  should not be leaked outside the cryptographic device through any attack. In a manner known in the art,  $D$  can be represented in the form of an  $n$ -bit number  $(d_0, d_1, \dots, d_{n-1})_2$ , where  $d_i$  is a bit (for each integer  $i$  between 0 and  $n-1$ ). In the rest of the document, the exponent  $D$  will be denoted  $\{d_0, d_1, \dots, d_{n-1}\}_2$  instead of  $(d_0, d_1, \dots, d_{n-1})_2$  as is usually the case in mathematics in order not to introduce any ambiguity with the reference signs placed in the claims between parentheses as per the European Patent Convention.

In abstract algebra, which is a branch of mathematics, a monoid  $(M, \perp)$  is defined as an algebraic set, the set being closed under an associative binary operation  $\perp$ , the set having an identity element. Contrary to a group, in a monoid every element does not necessarily have an inverse. The operation  $\perp$  can also be represented with other symbols. For example, the operation  $\perp$  can be represented as an additive operation (symbol  $+$ ), as a multiplicative operation (symbol  $*$ ), etc. This representation is purely formal and does not affect the

properties of the monoid. In the rest of the application, monoids will be represented with the multiplicative operation  $*$ , and will be denoted  $\{M, *\}$  instead of  $(M, *)$  in order not to introduce any ambiguity with the reference signs placed in the claims between parentheses as per the European Patent Convention.

5 Monoids are widespread in cryptography. The most widespread monoids in the field of cryptography are large monoids having many invertible elements, e.g.  $2^{80}$  invertible elements. For example, with the RSA algorithm, almost all elements are invertible (the exceptions being in particular the multiples of  $p$  and  $q$ ).  $M^*$  denotes the set containing all invertible elements of the set  $M$  of the  
10 monoid  $\{M, *\}$ .

In the rest of the application, all monoids are abelian monoids, that is monoids in which all elements commute.

Cryptographic mechanisms particularly sensitive to side channel attacks comprise mechanisms in which for each  $d_i$  equal to a certain value  $v$  (i.e.  $v=0$  or  
15  $v=1$ ), the mechanism calculates  $X^2$  and  $Y*Z$  (where  $X$ ,  $Y$  and  $Z$  are three elements of a monoid  $\{M, *\}$ ), and for each  $d_i$  equal to the other value ( $d_i = 1-v$ ), the mechanism calculates  $T^2$  (where  $T$  is an element of the monoid  $\{M, *\}$ ). Examples of such mechanisms include RSA modular exponentiation.

$X^2$  is called a squaring operation and stands for  $X*X$ .

20  $X^n$  stands for  $X*X*...*X$  where  $X$  appears  $n$  times.

Note: in a monoid with an additive notation,  $X^2$  would be written  $2X$  and would stand for  $X+X$ . Similarly,  $X^n$  would be written  $nX$  and would stand for  $X+X+...+X$  where  $X$  appears  $n$  times.

$Y*Z$  is called a multiplication operation.

25 The invention improves the resistance of above-mentioned particularly sensitive cryptographic mechanisms to side channel attacks. Examples of such mechanisms include elliptic curve point multiplications, and modular exponentiations used when performing an RSA operation or a Diffie Hellman key establishment. The invention also limits the amount of processing required for  
30 securing the cryptographic mechanisms. It does so by introducing a particular type of masking mechanism (also known as blinding mechanism).

The invention and its advantages will be explained more in details in the following specification referring to the appended drawings, in which:

5        Figure 1 represents a typical cryptographic mechanism without any protections against side channel attacks.

Figure 2 represents a cryptographic mechanism with a first level of protection against side channel attacks, known in the art as the "balanced modular exponentiation algorithm".

10       Figure 3 represents a cryptographic mechanism with a second level of protection against side channel attacks, known in the art as "Joye & Al. modular exponentiation algorithm".

Figure 4 represents a possible masking mechanism for modular exponentiation.

15       Figure 5 represents a preferred cryptographic mechanism according to the invention, offering a higher level of protection against side channel attacks.

Figure 6 and Figure 7 represent variants of the mechanism of Figure 5.

Figure 1 describes an example of cryptographic mechanism consisting of  
20 a modular exponentiation. This sort of modular exponentiations is implemented in particular with RSA and Diffie Hellman algorithms.

As can be seen on step 2, for each bit  $d_i$  of the exponent  $D$ , a modular squaring is performed (sub-step 2.i). When  $d_i$  is equal to 1, a modular multiplication is performed (sub-step 2.ii).

25        $D$  is usually derived from a random number. In general, the hamming weight of  $D$  is approximately  $n/2$ . Therefore, in general the method of Figure 1 involves  $n$  modular squaring operations and around  $n/2$  modular multiplications.

As known in the art, this type of cryptographic mechanisms is extremely sensitive even to the simplest side channel attacks such as SPA. Indeed, the  
30 power consumption is not the same during the execution of the multiplication operation and of the squaring operation. Therefore, one can put a probe on the

cryptographic device implementing the cryptographic mechanism, measure the power consumption, and distinguish the multiplication and the squaring in the power trace, thereby identifying the value of all bits  $d_i$ . The exponent  $D$  is then recovered by the attacker.

5

Figure 2 describes an example of cryptographic mechanism comprising a first level of protection against side channel attacks, known in the art as the "balanced modular exponentiation algorithm"

10 This method is similar to the one of Figure 1, except that when  $d_i$  is equal to 0, a third step iii is added, in which a dummy multiplication is executed. Thanks to this third step, the power consumption is very close whether the bit is equal to 0 or to 1.

The complexity of this method is increased since there are  $n$  multiplications and  $n$  square operations. However its resistance to basic side  
15 channel attacks is improved as well, as indicated above.

Unfortunately, this method remains very sensitive to another side channel attack known as the SE attack (safe error attack). Indeed, if the cryptographic mechanism is disrupted during a dummy multiplication, the multiplication fails, but the final result remains unaffected since the dummy multiplication is not used  
20 for the final result. Therefore an attacker can find out the dummy bits, which are bits equal to 0 in this example, and infer that all other bits are equal to 1, which results in the secret value of  $D$  being recovered.

Figure 3 describes an example of known cryptographic mechanism  
25 comprising a second level of protection against side channel attacks, known in the art as "Joye & Al. modular exponentiation algorithm", and disclosed at CHES 2002 by Joye and Yen. It is based on the Montgomery Ladder algorithm.

The cryptographic mechanism of Figure 3 aims at overcoming the limitation of the cryptographic mechanism of Figure 2.

To this end, there is no more dummy operation. Instead, The result of all multiplications is used in the final result (except in the last round). Therefore disturbing the mechanism always leads to an erroneous output.

The complexity of this cryptographic mechanism is the same as the one of  
5 Figure 2 (n multiplications, n square operations).

However, this cryptographic mechanism is still sensitive to DPA attacks. As known in the art, in a DPA attack, if the attacker is able to set the value of the input X, he can predict the value of the next intermediate value of steps i and ii by making assumptions on the values of  $d_i$  and verifying them by studying  
10 correlations in the power consumption over a number of selected samples.

It is an object of the invention to improve known techniques such as the cryptographic mechanism of Figure 3.

It would be possible to combine the teaching of Figure 3 with a masking  
15 mechanism, as shown on Figure 4. The masking may consist in multiplying the input element with a random number, thereby rendering the prediction step of the DPA attacks impossible. Unfortunately, the technique shown on Figure 4 requires approximately  $4*n$  operations, which makes it twice slower than previous techniques. The technique shown on Figure 4 also performs the modular  
20 exponentiation twice. A first time for the masked input, and another time for the mask used for the masking. Due to this double modular exponentiation, the secret exponent D is used twice, which potentially weakens the mechanism.

A cryptographic mechanism according to the invention involves a secret D  
25 which can be represented as an n-bit number  $\{d_0, d_1, \dots, d_{n-1}\}_2$ . The cryptographic mechanism is arranged to calculate an output element OUT equal to  $X^D$ , X being an element of a monoid  $\{M, *\}$ . The mechanism comprises a first variable  $VAR_0$  and a second variable  $VAR_1$ . The cryptographic mechanism comprises n steps  $\{MUL_i\}_{i=n-1..0}$  such that during each step  $MUL_i$ , the cryptographic device calculates  
30  $VAR_{1-di} * VAR_{di}$ , and n other steps  $\{SQ_i\}_{i=n-1..0}$  such that during each step  $SQ_i$ , the cryptographic device calculates  $VAR_{di} * VAR_{di}$ . Each step  $SQ_i$  is executed after the



step  $MUL_i$  for any  $i$  between 0 and  $n-1$ , and each step  $MUL_{i-1}$  is executed after step  $MUL_i$  for any  $i$  between 1 and  $n-1$ . The mechanism is characterized in that it comprises the steps of:

- a. generating a random element  $MSK\_INPUT$ ,
- 5 b. creating a masked element  $MASKED\_X$  by using the element  $X$  and the random element  $MSK\_INPUT$ ,
- c. calculating a masked output element  $MASKED\_OUT$  using the masked element  $MASKED\_X$ , the calculation of the masked output element  $MASKED\_OUT$  involving the abovementioned steps
- 10  $\{MUL_i\}_{i=n-1..0}$  and  $\{SQ_i\}_{i=n-1..0}$ ,
- d. calculating an output mask  $MSK\_OUTPUT$  from the random element  $MSK\_INPUT$  without involving the secret  $D$ ,
- e. calculating the output element  $OUT$  using the masked output element  $MASKED\_OUT$  and the output mask  $MSK\_OUTPUT$ ,
- 15 wherein the step d occurs at any time between step a and step e, and wherein the steps a, b, c, e are consecutive.

As seen on Figure 5, the computation of the output mask can take place together with the computation of the masked output element. As seen on Figure 6, this computation can also take place serially (either after, as shown on step 4 of the figure, or before). It is also possible to perform this computation in parallel,

20 for example inside two different threads, as depicted on Figure 7 (C.F. steps 3a and 3b).

Thanks to the masking operation, the DPA attack is no longer applicable, as the attacker does not know the mask and does not have the possibility to

25 make assumptions regarding the intermediate results.

The element  $X$  can be an input element supplied to the cryptographic mechanism by another mechanism, or can be generated inside the cryptographic mechanism. For example, in a cryptographic mechanism consisting of a timestamp mechanism, the current time may be determined securely inside the

30 mechanism and then digitally signed inside the mechanism.

Similarly, the output element OUT can be communicated by the cryptographic mechanism to another mechanism, can be kept internally in the cryptographic mechanism, or can be post-processed in the cryptographic mechanism and sent to another mechanism in the post-processed form.

5 In preferred embodiments, the cryptographic mechanism according to the invention is such that the random element MSK\_INPUT belongs to  $M^*$  (the set of invertible elements of  $M$ , as seen above). If MSK\_INPUT is equal to a value  $R$ , we denote by  $R^{-1}$  the inverse of  $R$  for the operation  $*$  of the monoid  $\{M, *\}$ . With cryptographic mechanisms where the function  $f: \text{MASKED\_X} \rightarrow \text{MASKED\_OUT}$   
 10 is such that there exists a function  $g$  such that  $f(R*X) = g(R)*f(X)$ , one can apply a mask MSK\_INPUT on the element  $X$  by multiplying  $X$  and  $R$ , and compute the output mask  $(g(R))^{-1}$  to apply on the masked output in order to obtain the output element. In certain instances  $(g(R))^{-1}$  may be equal to  $g(R^{-1})$ . In such embodiments, the inverse element  $R^{-1}$  may therefore be used to compute the  
 15 output mask MSK\_OUTPUT.

Preferred cryptographic mechanisms according to the invention may be such that the calculation of the output mask MSK\_OUTPUT comprises  $n$  steps  $\{R\_SQ_i\}_{i=n-1..0}$ , such that during each step  $R\_SQ_i$ , the cryptographic device calculates  $MSK_i * MSK_{i+1}$ ,  $MSK_i$  being an element of the monoid  $\{M, *\}$ , the initial  
 20 value  $MSK_n$  being obtained from the inverse of the random number  $R$ , the last value  $MSK_0$  being the output mask MSK\_OUTPUT used to unmask the value of the masked output MASKED\_OUT. This is advantageous in particular for mechanisms associated with a function  $g$  such that the computation of the function  $g$  may be executed by involving the steps  $R\_SQ_i$ .

25 More specifically, in a preferred mechanism according to the invention,  $MSK_i$  may be equal to  $MSK_{i+1} * MSK_{i+1}$  for  $i$  equal to  $n-1$  down to 0. This is particularly advantageous for mechanisms associated with a function  $g: MSK_n \rightarrow MSK_0$  where  $MSK_i = MSK_{i+1} * MSK_{i+1}$  for  $i$  equal to  $n-1$  down to 0.

In a preferred cryptographic mechanism, the masked element MASKED\_X  
 30 is equal to  $X*R$  and the output element OUT is equal to  $\text{MASKED\_OUT} * MSK_0$ ,  $MSK_n$  being equal to  $R^{-1}$ , the initial value of the first variable  $VAR_0$  being set to

the value  $R$  of the random element, the initial value of the second variable  $VAR_1$  being set to the value of the masked element  $MASKED\_X$ , each step  $MUL_i$  consisting in calculating  $VAR_{1-di} * VAR_{di}$  and storing the result in  $VAR_{1-di}$ , each step  $SQ_i$  consisting in calculating  $VAR_{di} * VAR_{di}$  and storing the result in  $VAR_{di}$ .

Figure 5 describes an example of such preferred embodiment of the invention comprising:

1. a first step in which a random number is generated. This can be done for example by a hardware random number generator embedded in a cryptographic device implementing the cryptographic mechanism. Indeed, the random number is preferably as unpredictable as possible, which is best achieved with hardware means as known in the art;
2. a second step in which variables  $VAR_0$ ,  $VAR_1$  and  $MSK_n$  are initialized;
3. a third step in which a masked output (value of  $VAR_0$  after the last round of the loop) is calculated from the masked element, and an output mask  $MSK_0$  is calculated;
4. a fourth step in which the masked output is unmasked with the output mask  $MSK_0$  and is returned to the entity which invoked the cryptographic mechanism.

The cryptographic mechanism uses the element  $X$  and the secret  $D$  as inputs. In preferred embodiments, the secret  $D$  is stored securely and therefore does not need to be passed to the cryptographic mechanism each time the cryptographic mechanism is invoked. The element  $X$  is generally passed to the cryptographic mechanism as an input parameter, but may also be determined by the cryptographic mechanism itself (e.g. as seen above with time stamps based on a clock available in the cryptographic mechanism, etc.).

The invention also concerns a cryptographic device storing a secret  $D$  and implementing a cryptographic mechanism as described above. The invention concerns more particularly cryptographic devices of the smart card type.

The invention is particularly advantageous for embedded systems such as smart cards as it has very few additional requirements compared to state of the art cryptographic mechanisms. It is well suited to the RSA algorithm. Indeed, it does not require any additional information on the key material compared to traditional cryptographic mechanisms. In particular, it does not require the public exponent of the RSA key pair to be available to the cryptographic mechanism.

It is similarly advantageous for the Diffie Hellman algorithm, as it does not require any extra parameter, and is therefore very convenient in particular for establishing session keys in static mode.

It is also advantageous for both above algorithms in that it does not require an additive mask on the exponent, nor on the element  $X$ , which would require a more powerful processor (or crypto processor in case the cryptographic algorithms are implemented partially or fully in hardware).

The complexity of the preferred embodiment of Figure 5 involves approximately  $2 \cdot n$  square operations and  $n$  multiplications, i.e. around  $3 \cdot n$  CPU intensive operations, which is only 50% more than the closest method (Montgomery ladder of Figure 3), and does not require much more RAM (50% at most).

It should be noted that for some random elements used as input masks, the steps  $SQ\_RD_i$  may lead (for a certain value  $i\_weak$  of the index  $i$ ) to  $MSK_{i\_weak} = 1$ , in which case all subsequent values ( $MSK_{i\_weak-1}$ ,  $MSK_{i\_weak-2}$ , etc.) are equal to 1 as well. This situation corresponds to a weak output mask, since it is equivalent to not having an output mask (the masked output and the output are equal). However, this weakness is hard to exploit, and is very unlikely to happen. The probability of a random element leading to a weak mask is very low. For example, it is estimated that for RSA 2048, the probability of picking a weak random element is at most equal to  $1.9 \cdot 10^{-7}$ . The probability depends on the value of the RSA key, and in practice it is often much lower than the above value. The probability can be made arbitrarily small by picking several invertible random elements and multiplying them together (only if all elements are weak will the product of the elements be weak).

## CLAIMS

1. Cryptographic mechanism involving a secret  $D$  which can be represented as an  $n$ -bit number  $\{d_0, d_1, \dots, d_{n-1}\}_2$ , the cryptographic mechanism being arranged to calculate an output element  $OUT$  equal to  $X^D$ ,  $X$  being an element of a monoid  $\{M, *\}$ , the mechanism comprising a first variable  $VAR_0$  and a second variable  $VAR_1$ , the cryptographic mechanism comprising  $n$  steps  $\{MUL_i\}_{i=n-1..0}$  such that during each step  $MUL_i$ , the cryptographic device calculates  $VAR_{1-di} * VAR_{di}$ , the cryptographic mechanism comprising  $n$  other steps  $\{SQ_i\}_{i=n-1..0}$  such that during each step  $SQ_i$ , the cryptographic device calculates  $VAR_{di} * VAR_{di}$ , each step  $SQ_i$  being executed after the step  $MUL_i$  for any  $i$  between 0 and  $n-1$ , each step  $MUL_{i-1}$  being executed after step  $MUL_i$  for any  $i$  between 1 and  $n-1$ , the mechanism being characterized in that it comprises the steps of:
  - a. generating a random element  $MSK\_INPUT$  ( $R$ ),
  - b. creating a masked element  $MASKED\_X$  ( $VAR_1$ ) by using the element  $X$  and the random element  $MSK\_INPUT$ ,
  - c. calculating a masked output element  $MASKED\_OUT$  ( $VAR_0$ ) using the masked element  $MASKED\_X$ , the calculation of the masked output element  $MASKED\_OUT$  involving the abovementioned steps  $\{MUL_i\}_{i=n-1..0}$  and  $\{SQ_i\}_{i=n-1..0}$ ,
  - d. calculating an output mask  $MSK\_OUTPUT$  ( $MSK_0$ ) from the random element  $MSK\_INPUT$  without involving the secret  $D$ ,
  - e. calculating the output element  $OUT$  using the masked output element  $MASKED\_OUT$  and the output mask  $MSK\_OUTPUT$ ,
 wherein the step d occurs at any time between step a and step e, and wherein the steps a, b, c, e are consecutive.
2. Cryptographic mechanism according to claim 1, wherein the random element  $MSK\_INPUT$  ( $R$ ) has an inverse element ( $R^{-1}$ ) for the operation  $*$

of the monoid  $\{M, *\}$ , the inverse element being usable to compute the output mask  $MSK\_OUTPUT$ .

3. Cryptographic mechanism according to claim a, wherein the calculation of the output mask  $MSK\_OUTPUT$  comprises  $n$  steps  $\{R\_SQ_i\}_{i=n-1..0}$ , such that during each step  $R\_SQ_i$ , the cryptographic device calculates  $MSK_i * MSK_i$ ,  $MSK_i$  being an element of the monoid  $\{M, *\}$ , the initial value  $MSK_n$  being obtained from the inverse element  $(R^{-1})$  of the random element  $MSK\_INPUT$ , the last value  $MSK_0$  being the output mask  $MSK\_OUTPUT$  used to unmask the value of the masked output  $MASKED\_OUT$ .
4. Cryptographic mechanism according to claim 3, wherein  $MSK_i$  is equal to  $MSK_{i+1} * MSK_{i+1}$  for  $i$  equal to  $n-1$  down to 0.
5. Cryptographic mechanism according to claim 4, wherein the masked element  $MASKED\_X$  is equal to  $X * R$  and wherein the output element  $OUT$  is equal to  $MASKED\_OUT * MSK_0$ ,  $MSK_n$  being equal to the inverse of  $R$ , the initial value of the first variable  $VAR_0$  being set to the value  $(R)$  of the random element, the initial value of the second variable  $VAR_1$  being set to the value of the masked element  $MASKED\_X$ , each step  $MUL_i$  consisting in calculating  $VAR_{1-di} * VAR_{di}$  and storing the result in  $VAR_{1-di}$ , each step  $SQ_i$  consisting in calculating  $VAR_{di} * VAR_{di}$  and storing the result in  $VAR_{di}$ .
6. Cryptographic device storing a secret  $D$ , characterized in that it implements a cryptographic mechanism according to any previous claim.
7. Smart card storing a secret  $D$ , characterized in that it implements a cryptographic mechanism according to any claim from claim 1 to claim 5.

## Typical modular exponentiation algorithm

INPUT:  $X$ ,  $D = \{d_0, d_1, \dots, d_{n-1}\}_2$ ,  $N$

OUTPUT:  $X^D \bmod N$

1.  $A \leftarrow 1$
2. For  $k$  from  $n-1$  down to  $0$  do
  - i.  $A \leftarrow A^2 \bmod N$
  - ii. If  $d_k = 1$  then  $A \leftarrow A * X \bmod N$
3. Return  $A$

Figure 1

## Balanced modular exponentiation algorithm

INPUT:  $X$ ,  $D = \{d_0, d_1, \dots, d_{n-1}\}_2$ ,  $N$

OUTPUT:  $X^D \bmod N$

1.  $A \leftarrow 1$
2. For  $k$  from  $n-1$  down to  $0$  do
  - i.  $A \leftarrow A^2 \bmod N$
  - ii. If  $d_k = 1$  then  $A \leftarrow A * X \bmod N$
  - iii. Else  $B \leftarrow A * X \bmod N$
3. Return  $A$

Figure 2



## Joye &amp; Al. modular exponentiation algorithm

INPUT:  $X, D = \{d_0, d_1, \dots, d_{n-1}\}_2, N$

OUTPUT:  $X^D \bmod N$

1.  $a_0 \leftarrow 1, a_1 \leftarrow X$
2. For  $k$  from  $n-1$  down to  $0$  do
  - i.  $a_{1-dk} \leftarrow a_{1-dk} * a_{dk} \bmod N$
  - ii.  $a_{dk} \leftarrow (a_{dk})^2 \bmod N$
3. Return  $a_0$

Figure 3

A possible masking mechanism for modular exponentiation

INPUT:  $X$ ,  $D = \{d_0, d_1, \dots, d_{n-1}\}_2$ ,  $N$

OUTPUT:  $X^D \bmod N$

1. generate a random number  $R$  having an inverse (denoted  $R^{-1}$ )
2.  $a_0 \leftarrow 1$ ,  $a_1 \leftarrow X \cdot R$
3. For  $k$  from  $n-1$  down to 0 do
  - i.  $a_{1-dk} \leftarrow a_{1-dk} \cdot a_{dk} \bmod N$
  - ii.  $a_{dk} \leftarrow (a_{dk})^2 \bmod N$
4.  $b_0 \leftarrow 1$ ,  $b_1 \leftarrow R^{-1}$
5. For  $k$  from  $n-1$  down to 0 do
  - i.  $b_{1-dk} \leftarrow b_{1-dk} \cdot b_{dk} \bmod N$
  - ii.  $b_{dk} \leftarrow (b_{dk})^2 \bmod N$
6. Return  $a_0 \cdot b_0$

Figure 4

A cryptographic mechanism according to the invention

INPUT:  $X, D = \{d_0, d_1, \dots, d_{n-1}\}_2$

OUTPUT:  $X^D$

1. generate a random number  $R$  having an inverse (denoted  $R^{-1}$ )
2.  $VAR_0 \leftarrow R, VAR_1 \leftarrow X \cdot R, MSK_n \leftarrow R^{-1}$
3. For  $i$  from  $n-1$  down to  $0$  do
 

{MUL <sub>i</sub> }	$VAR_{1-di} \leftarrow VAR_{1-di} * VAR_{di}$
{SQ <sub>i</sub> }	$VAR_{di} \leftarrow VAR_{di} * VAR_{di}$
{SQ_RD <sub>i</sub> }	$MSK_i \leftarrow MSK_{i+1} * MSK_{i+1}$
4. Return  $VAR_0 * MSK_0$

Figure 5

A variant of the cryptographic mechanism according to the invention

INPUT:  $X, D = \{d_0, d_1, \dots, d_{n-1}\}_2$

OUTPUT:  $X^D$

1. generate a random number  $R$  having an inverse (denoted  $R^{-1}$ )
2.  $VAR_0 \leftarrow R, VAR_1 \leftarrow X \cdot R, MSK_n \leftarrow R^{-1}$
3. For  $i$  from  $n-1$  down to  $0$  do
 

$\{MUL_i\} \quad VAR_{1-di} \leftarrow VAR_{1-di} * VAR_{di}$   
 $\{SQ_i\} \quad VAR_{di} \leftarrow VAR_{di} * VAR_{di}$
4. For  $i$  from  $n-1$  down to  $0$  do
 

$\{SQ_{RD_i}\} \quad MSK_i \leftarrow MSK_{i+1} * MSK_{i+1}$
5. Return  $VAR_0 * MSK_0$

Figure 6

Another variant of the cryptographic mechanism according to the invention

INPUT:  $X, D = \{d_0, d_1, \dots, d_{n-1}\}_2$

OUTPUT:  $X^D$

1. generate a random number  $R$  having an inverse (denoted  $R^{-1}$ )
2.  $VAR_0 \leftarrow R, VAR_1 \leftarrow X \cdot R, MSK_n \leftarrow R^{-1}$
3. parallel execution of the following two threads:

*Thread 3a*

For  $i$  from  $n-1$  down to 0 do

$\{MUL_i\} VAR_{1-di} \leftarrow VAR_{1-di} * VAR_{di}$

$\{SQ_i\} VAR_{di} \leftarrow VAR_{di} * VAR_{di}$

4. Return  $VAR_0 * MSK_0$

*Thread 3b*

For  $i$  from  $n-1$  down to 0 do

$\{SQ_{RD}_i\} MSK_i \leftarrow MSK_{i+1} * MSK_{i+1}$

Figure 7

## INTERNATIONAL SEARCH REPORT

International application No

PCT/IB2007/000728

**A. CLASSIFICATION OF SUBJECT MATTER**  
INV. G06F7/72

According to International Patent Classification (IPC) or to both national classification and IPC

**B. FIELDS SEARCHED**

Minimum documentation searched (classification system followed by classification symbols)

G06F

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

Electronic data base consulted during the international search (name of data base and, where practical, search terms used)

EPO-Internal, WPI Data, INSPEC, COMPENDEX, IBM-TDB, PAJ

**C. DOCUMENTS CONSIDERED TO BE RELEVANT**

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
Y	JOYE M ET AL: "THE MONTGOMERY POWERING LADDER" CRYPTOGRAPHIC HARDWARE AND EMBEDDED SYSTEMS. INTERNATIONAL WORKSHOP, 13 August 2002 (2002-08-13), pages 291-302, XP001160513 the whole document	1-7
Y	----- US 2005/084098 A1 (BRICKELL ERNIE F [US]) 21 April 2005 (2005-04-21) abstract table 3	1-7
A	----- US 2004/267859 A1 (FISCHER WIELAND ET AL) 30 December 2004 (2004-12-30) abstract; compounds 1-3 paragraph [0044] - paragraph [0060] ----- -/--	1-7

☒ Further documents are listed in the continuation of Box C.☒ See patent family annex.

## \* Special categories of cited documents:

- \*A\* document defining the general state of the art which is not considered to be of particular relevance
- \*E\* earlier document but published on or after the international filing date
- \*L\* document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)
- \*O\* document referring to an oral disclosure, use, exhibition or other means
- \*P\* document published prior to the international filing date but later than the priority date claimed

\*T\* later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention

\*X\* document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step when the document is taken alone

\*Y\* document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art.

\*G\* document member of the same patent family

Date of the actual completion of the international search

6 August 2007

Date of mailing of the international search report

14/08/2007

Name and mailing address of the ISA/

European Patent Office, P.B. 5818 Patentlaan 2  
NL - 2280 HV Rijswijk  
Tel. (+31-70) 340-2040, Tx. 31 651 epo nl,  
Fax: (+31-70) 340-3016

Authorized officer

Post, Katharina

# INTERNATIONAL SEARCH REPORT

International application No

PCT/IB2007/000728

## C(Continuation). DOCUMENTS CONSIDERED TO BE RELEVANT

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
A	<p>TRICHINA E ET AL: "IMPLEMENTATION OF ELLIPTIC CURVE CRYPTOGRAPHY WITH BUILT-IN COUNTER MEASURES AGAINST SIDE CHANNEL ATTACKS"</p> <p>CRYPTOGRAPHIC HARDWARE AND EMBEDDED SYSTEMS. INTERNATIONAL WORKSHOP, 13 August 2002 (2002-08-13), pages 98-113, XP001160524</p> <p>chapter 3.2 A multiplicative mask</p> <p>-----</p>	1-7
A	<p>WO 2004/070497 A (INFINEON TECHNOLOGIES AG; FISCHER, WIELAND)</p> <p>19 August 2004 (2004-08-19)</p> <p>abstract</p> <p>-----</p>	1-7
A	<p>SUNG-MING YEN ET AL: "Improvement on Ha-Moon Randomized Exponentiation Algorithm"</p> <p>SPRINGER VERLAG BERLIN HEIDELBERG 2005, 2005, pages 154-167, XP019010693</p> <p>abstract</p> <p>-----</p>	1-7

# INTERNATIONAL SEARCH REPORT

Information on patent family members

International application No

PCT/IB2007/000728

Patent document cited in search report		Publication date	Patent family member(s)	Publication date
US 2005084098	A1	21-04-2005	NONE	
US 2004267859	A1	30-12-2004	AU 2002340556 A1 DE 10151129 A1 WO 03034172 A2 EP 1428112 A2 TW 589547 B	28-04-2003 08-05-2003 24-04-2003 16-06-2004 01-06-2004
WO 2004070497	A	19-08-2004	DE 10304451 B3 EP 1590731 A2 KR 20050106416 A US 2007064930 A1	02-09-2004 02-11-2005 09-11-2005 22-03-2007