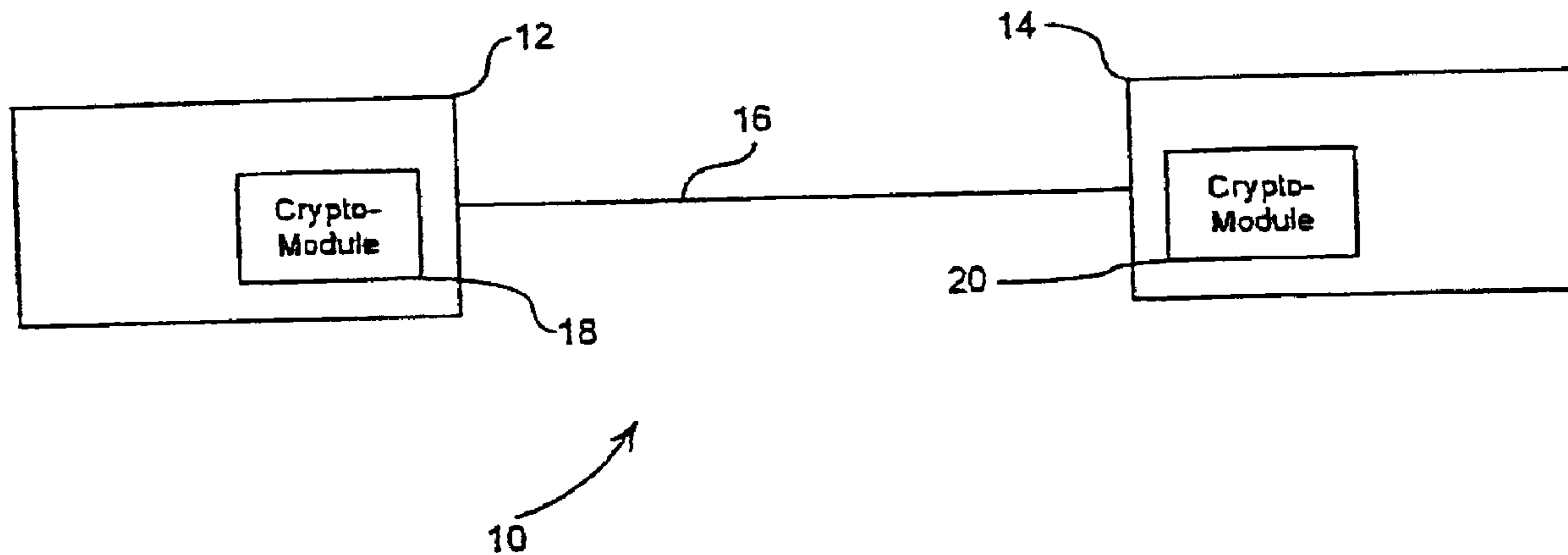




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(54) Titre : SIGNATURES ECDSA COMPRESSEES  
 (54) Title: COMPRESSED ECDSA SIGNATURES



(57) **Abrégé/Abstract:**

An improved compression scheme for compressing an ECDSA signature is provided. The scheme substitutes the integer  $s$  in a signature  $(r, s)$  by a smaller value  $c$ . The value  $c$  is derived from  $s$  and another value  $d$ ,  $d$  being small enough such that  $c$  is smaller than  $s$ . The compressed signature  $(r, c)$  is verified by computing a value using  $r$  and  $e$ ,  $e$  being a hash of a message  $m$ , and using this value with a value  $R$  recovered from  $r$  to derive the value  $d$ . The value  $s$  can then be recovered and the full signature then recovered and verified.

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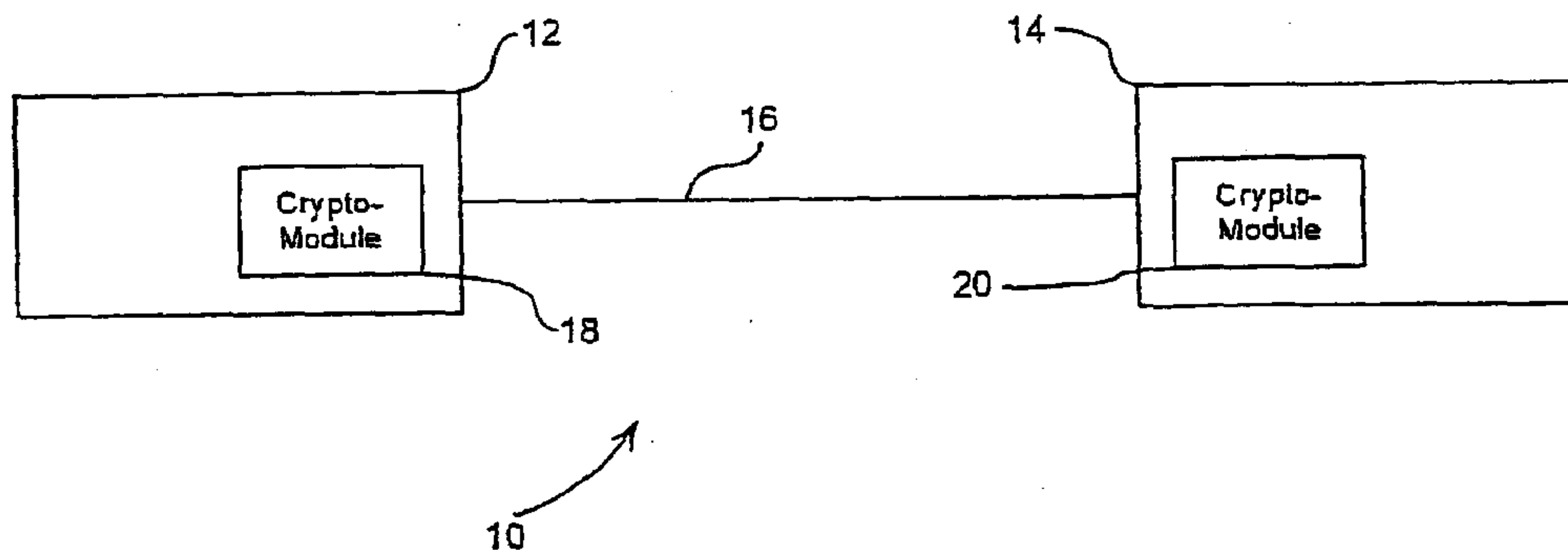
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WO 2008/058377 A1

**COMPRESSED ECDSA SIGNATURES**

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**FIELD OF THE INVENTION:**

**[0001]** The present invention relates to cryptographic schemes and has particular utility in digital signature algorithms.

**DESCRIPTION OF THE PRIOR ART**

**[0002]** A digital signature of a message is a number dependent on some secret known only to the signer, and, additionally, on the content of the message being signed. Signatures are meant to be verifiable. If a dispute arises as to whether a party signed a document (caused by either a signer trying to repudiate a signature it did create, or a fraudulent claimant), an unbiased third party should be able to resolve the matter equitably, without requiring access to the signer's secret information (e.g. a private key).

**[0003]** Digital signatures have many applications in information security, in particular, as they are used in cryptographic schemes. Some applications include authentication, data integrity, and non-repudiation. One particularly significant application of digital signatures is the certification of public keys in large networks. Certification is a means for a trusted third party to bind the identity of a user to a public key, so that at some later time, other entities can authenticate a public key without assistance from the trusted third party.

**[0004]** A cryptographic scheme known as the Digital Signature Algorithm (DSA) is based on the well known and often discussed intractability of the discrete logarithm problem. The DSA was proposed by the U.S. National Institute of Standards and Technology (NIST) in 1991 and has become a U.S. Federal Information Processing Standard (FIPS 186) called the Digital Signature Standard (DSS). The algorithm is a variant of the well known ElGamal signature scheme, and can be classified as a digital signature with appendix (i.e. one that relies on cryptographic hash functions rather than customized redundancy functions).

**[0005]** The Elliptic Curve Digital Signature Algorithm (ECDSA) is a signature scheme that may be used in elliptic curve cryptosystem and has attributes similar to the DSA. It is generally regarded as the most widely standardized elliptic curve-based signature scheme, appearing in the ANSI X9.62, FIPS 186-2, IEEE 1363-2000 and ISO/IEC 15946-2 standards as well as several draft standards.

1 [0006] ECDSA signature generation operates on several domain parameters, a private  
2 key  $d$ , and a message  $m$ . The outputs are the signature  $(r,s)$ , where the signature components  
3  $r$  and  $s$  are integers, and proceeds as follows.

- 4 1. Select a random integer  $k \in_R [1, n - 1]$ ,  $n$  being one of the domain parameters.
- 5 2. Compute  $kP = (x_1, y_1)$  and convert  $x_1$  to an integer  $\bar{x}_1$ , where  $P$  is a point on an  
6 elliptic curve  $E$  and is one of the domain parameters.
- 7 3. Compute  $r = \bar{x}_1 \bmod n$ , wherein if  $r = 0$ , then go back to step 1.
- 8 4. Compute  $e = H(m)$ , where  $H$  denotes a cryptographic hash function whose outputs  
9 have a bit length no more than that of  $n$  (if this condition is not satisfied, then the  
10 outputs of  $H$  can be truncated).
- 11 5. Compute  $s = k^{-1}(e + \alpha r) \bmod n$ , where  $\alpha$  is a long term private key of the signor.  
12 If  
13  $s = 0$ , then go back to step 1.
- 14 6. Output the pair  $(r, s)$  as the ECDSA signature of the message  $m$ .

15 [0007] ECDSA signature verification operates on several domain parameters, a long term  
16 public key  $Q$  where  $Q = \alpha P$ , the message  $m$ , and the signature  $(r, s)$  derived above. ECDSA  
17 signature verification outputs a rejection or acceptance of the signature, and proceeds as  
18 follows.

- 19 1. Verify that  $r$  and  $s$  are integers in the interval  $[1, n-1]$ . If any verification fails  
20 then a rejection is returned.
- 21 2. Compute  $e = H(m)$ .
- 22 3. Compute  $w = s^{-1} \bmod n$ .
- 23 4. Compute  $u_1 = ew \bmod n$  and  $u_2 = rw \bmod n$ .
- 24 5. Compute  $R = u_1P + u_2Q = s^{-1} (eP + rQ)$  (from 3 and 4 above)

1           6. If  $R = \infty$  then the signature is rejected.

2           7. Convert the x-coordinate  $x_1$  of  $R$  to an integer  $\bar{x}_1$ ; compute  $v = \bar{x}_1 \bmod n$ .

3           8. If  $v = r$  then the signature is accepted, if not then the signature is rejected.

4   **[0008]**    To improve the efficiency of ECDSA signature verification, in particular step 5  
5   above that includes an inversion of  $s$ , the ECDSA signature has been known to be  
6   compressed by truncating  $s$  by omitting  $2b$  bits. Such compression is at the cost of additional  
7   verification steps, which has been known to cost the verifier approximately  $2^{2b}$  extra elliptic  
8   curve group operations.

9   **[0009]**    Signature compression is particularly desirable in cryptographic applications  
10   where bandwidth conservation is of paramount importance, and additional cryptographic  
11   operations can be readily handled by the verifier. An example is a two-dimensional barcode,  
12   where bandwidth is very limited, but the verifier processor may be fast. Another example is  
13   RFID tags, which need power from a radio frequency field in order to transmit data, and  
14   therefore low transmission bandwidth is very desirable.

15   **[0010]**    A scheme for ECDSA signature compression is needed that has a cost to the  
16   verifier that is less than such previous compression schemes.

17   **[0011]**    It is therefore an object of the present invention to obviate or mitigate at least one  
18   of the above-mentioned disadvantages.

## 19   SUMMARY OF THE INVENTION

20   **[0012]**    In one aspect, there is provided a method of compressing a digital signature of a  
21   message, the signature comprising a pair of signature components  $r$ ,  $s$ , the method comprising  
22   obtaining a pair of values  $c$ ,  $d$ , related mathematically to  $s$  and with one of the values being  
23   smaller than  $s$ , substituting the one value for the signature component  $s$ , in the digital  
24   signature and forwarding the signature to a recipient.

25   **[0013]**    In another aspect, there is provided, a cryptographic system for generating a  
26   compressed signature from a pair of signature components  $r$ ,  $s$ , the system having an

1 arithmetic unit to provide a pair of values  $c$ ,  $d$  mathematically related to the component  $s$ , and  
2 a signature generator to substitute one of the values for the signature  $s$ .

3 [0014] In yet another aspect, there is provided a cryptographic system for verifying a  
4 signature  $r$ ,  $c$  received from a sender using a system as defined above comprising an  
5 arithmetic unit to recover the other of the values and compare the other value with predefined  
6 criteria.

7 [0015] In yet another aspect, a method of compressing a digital signature  $(r, s)$  is  
8 provided that includes the steps of substituting the value  $s$  with a smaller value  $c$ , the value  $c$   
9 being derived from  $s$  and another value  $d$ , the value  $d$  being small enough such that  $c$  is  
10 smaller than  $s$ ; and substituting the value  $s$  with the value  $c$  to obtain a compressed signature  
11  $(r, c)$ .

12 [0016] In yet another aspect, a method of verifying a compressed signature is provided,  
13 the compressed signature including a value  $c$  substituted for a value  $s$  of a full signature  $(r, s)$ ,  
14 the method comprising the steps of computing a value  $d$  using parameters of the compressed  
15 signature and a message, the value  $c$  being derived from the value  $d$  and the value  $s$ ; and  
16 verifying the compressed signature if a value for  $d$  can be found according to predetermined  
17 criteria.

## 18 BRIEF DESCRIPTION OF THE DRAWINGS

19 [0017] An embodiment of the invention will now be described by way of example only  
20 with reference to the appended drawings wherein:

21 [0018] Figure 1 is a cryptographic communication system;

22 [0019] Figure 2 is a flow chart illustrating one embodiment of a signature compression  
23 scheme and a signature verification scheme of a compressed signature; and

24 [0020] Figure 3 is flow chart illustrating another embodiment of a signature compression  
25 scheme and a signature verification scheme of a compressed signature.

## 1 DETAILED DESCRIPTION OF THE INVENTION

2 [0021] Referring therefore to Figure 1, a cryptographic communication system is  
3 generally denoted by numeral 10. The system 10 has a first correspondent 12 and a second  
4 correspondent 14 that may communicate with each other over a communication channel 16.  
5 The communication channel 16 may or may not be secure. Each correspondent has a  
6 cryptographic module 18 and 20 respectively, for performing cryptographic operations.

7 [0022] Each cryptographic module 18 and 20 is capable of performing elliptic curve  
8 cryptographic operations such as ECDSA signature generation and verification schemes  
9 operating on the elliptic curve  $E$  defined over a field  $\mathbb{F}_q$ . The embodiments described herein  
10 are particularly suitable for an ECDSA algorithm where, for example, the integer  $s$  in the  
11 signature  $(r, s)$  can be compressed at the cost of the verifier needing to perform additional  
12 cryptographic operations.

13 [0023] In a first embodiment exemplified in Figure 2, the correspondent 12 may be  
14 referred to as a “signer”, and the correspondent 14 may be referred to as a “verifier”. An  
15 ECDSA signature  $(r, s)$ , generated by the signer 12 for a message  $m$ , is produced as described  
16 above. To reduce bandwidth, the signature can be compressed by substituting, for example  $s$ ,  
17 by a smaller value  $c$ . The values  $s$  and  $c$  in this example are related by the expression

18  $s \equiv \frac{c}{d} \pmod{n}$ , the value of  $d$  being chosen such that  $c$  is a smaller value than  $s$ . The possible

19 range of values or ‘bounds’ for  $d$  is part of the system parameters and is used in the  
20 verification step for determining if a recovered  $d$  is acceptable.

21 [0024] Values for  $c$  and  $d$  may be obtained by using a variant of the extended Euclidean  
22 algorithm to find an equation of the form  $ds + un = c$ . More precisely, the intermediate steps  
23 in the extended Euclidean algorithm compute values  $x, y, z$  such that  $xs + yn = z$ . Normally,  
24 the extended Euclidean algorithm begins with small  $x$  and  $y$  (valued at 0 or 1) and large  $z$  (as  
25 large as  $n$  or  $s$ ), and ends with large  $x$  and  $y$  (about the size of  $n$  and  $s$  respectively) and small  
26  $z$  (usually 1, unless  $n$  and  $s$  have a common factor which will not occur for the choice of  $n$   
27 and  $s$  in ECDSA). In the present embodiment, the extended Euclidean algorithm is stopped  
28 part way, to obtain values of  $x$  and  $y$  that are intermediate in size, and meet the requirements  
29 for  $d$  and  $c$ , respectively.

1 [0025] The value obtained for  $c$  is substituted for  $s$  in the signature to provide the  
2 compressed signature  $(r, c)$ . This is then sent from the signer to a recipient.

3 [0026] The compressed signature  $(r, c)$  may be verified by a recipient by computing a  
4 point  $R$ , where  $R$  can be recovered from  $r$ . Recovering  $R$  from  $r$  may provide several  
5 possibilities for  $R$ , in which case, the following verification scheme may be attempted by the  
6 verifier 14 for each such  $R$ . Alternatively, extra information may be sent with, or embedded  
7 in, the signature or message  $m$  to indicate which of the possible values is the correct choice  
8 for  $R$ . This may be, for example, the first bit of the value of the  $y$  co-ordinate of  $R$  or a  
9 similar technique. For each such  $R$ , the full signature  $(r, s)$  is valid, by definition, if and only  
10 if  $R = s^{-1}(eP + rQ)$ , which according to the above notation, is equivalent to  
11  $cR = d(eP + rQ)$ .

12 [0027] To verify the signature  $(r, c)$ , the verifier 14 first computes  $W = eP + rQ$  which  
13 can be done using public information available to the recipient. As discussed above,  $e$  is  
14 generally computed as a hash of the message  $m$ , e.g.  $e = H(m)$ . The verifier 14 then attempts  
15 to compute  $d = \log_w(cR)$ , using knowledge that  $d$  is smaller than a predetermined bound  
16 agreed by the signer and verifier for purposes of signature compression. If no such  $d$  can be  
17 found within the bound, then the compressed signature  $(r, c)$  is rejected as being invalid.  
18 Similarly, if a value of  $d$  is obtained that meets the bounds agreed, the signature may be  
19 considered verified. Such discrete logarithm algorithms generally take time proportional to  
20  $\sqrt{d}$ . If  $\sqrt{d}$  is small enough, then it is quite practical for the verifier 14 to use such an  
21 algorithm. Once (and if)  $d$  is obtained by the verifier 14, the full signature  $(r, s)$  can be  
22 recovered by computing  $s = c / d \bmod n$ , allowing the verifier 14 to also use or verify the full  
23 signature if he wishes.

24 [0028] In another embodiment shown in Figure 3, the compressed signature may be  $(r,$   
25  $d)$ , where  $d$  is the value  $d$  used in the above notation, and in this case, a recovered value of  $c$   
26 is required to meet a particular range of sizes, i.e. be "small enough".

27 [0029] Similar to the above embodiment, the value  $W = eP + rQ$  is first computed, and  
28 then the verifier 14 attempts to compute  $c = \log_r(dW)$  using any suitable method for

1 choosing  $R$ , which can be done if  $c$  is small enough. If no such  $c$  can be found, then the  
2 compressed signature  $(r, d)$  is rejected as being invalid. Once (and if)  $c$  is obtained, the  
3 signature may be considered to be verified although the full signature  $(r, s)$  can be recovered  
4 by computing  $s = c/d \bmod n$ , if the verifier 14 wishes to use or verify the full signature  $(r, s)$ .

5 **[0030]** In many practical applications, the choice of  $R$  can often be narrowed down to a  
6 choice between two values, e.g.  $R$  and  $-R$ , given  $r$  alone. In general, algorithms for solving  
7 discrete logarithms between  $R$  and some point  $W$  will also find a logarithm between  $-R$  and  
8  $W$ , because if the first logarithm is, e.g.,  $u$ , the other is  $-u$ . Typically, it is easy to check that  $-$   
9  $u$  is small enough, so it is generally sufficient to compute one discrete logarithm per pair  $(R, -$   
10  $R)$  of candidates.

11 **[0031]** The above compression scheme may effectively compress an ECDSA signature  
12 by removal of  $2b$  bits at the cost of the verifier 14 performing an extra  $2^b$  elliptic curve group  
13 operations, where  $b$  is a predetermined value selected by the signer. With known  
14 compression techniques the cost of saving  $2b$  bits was  $2^{2b}$  extra signature verifications, which  
15 is considerably more costly for moderate sizes of  $b$ .

16 **[0032]** It should be noted that verification, compression and decompression of an ECDSA  
17 signature  $(r, s)$  can be done without using the private key. From a security perspective, this  
18 means that a compressed ECDSA signature is largely guaranteed to be as secure as a full  
19 signature, since the private key is not needed to compress or decompress the full signature.  
20 From a practical perspective, this means that third parties can provide services using methods  
21 that may include the schemes described above to verify a compressed signature. For example,  
22 a CA may act as an intermediary to compress signatures created by a signor and forward  
23 those to recipients, where they may be verified.

24 **[0033]** Although the invention has been described with reference to certain specific  
25 embodiments, various modifications thereof will be apparent to those skilled in the art. For  
26 example, the technique may be used with other discrete log signature algorithms where an  
27 ephemeral private key is used to generate a first signature component

28

1 that is then bound to the message and the long term private key of the signer to produce a  
2 second signature component. The scope of the claims appended hereto should not be limited  
3 by the preferred embodiments set forth in the present description, but should be given the  
4 broadest interpretation consistent with the description as a whole.

1 **Claims:**

- 2 1. A method of compressing a digital signature of a message, said signature comprising a pair  
3 of signature components  $r$ ,  $s$ , said method being performed by a correspondent in a data  
4 communication system, the correspondent having a cryptographic module for performing  
5 cryptographic operations, said method comprising:
- 6 - said cryptographic module obtaining a pair of values  $c$ ,  $d$  related mathematically to  $s$ ,  
7 one of said values being smaller than  $s$  and said one of said values having a smaller  
8 number of bits than  $s$ ;
  - 9 - said cryptographic module generating a compressed signature by substituting said one  
10 of said values for the signature component  $s$ , in said digital signature; and  
11 - said correspondent forwarding said compressed signature to a recipient.
- 12
- 13 2. The method according to claim 1 wherein both said values  $c$ ,  $d$  meet predetermined criteria.  
14
- 15 3. The method according to claim 2 wherein said value  $d$  is required to fall within predefined  
16 bounds.  
17
- 18 4. The method according to claim 3 wherein said value  $c$  is smaller than said component  $s$ .  
19
- 20 5. The method according to claim 4 wherein said components  $r$ ,  $s$  represent an ECDSA  
21 signature.  
22
- 23 6. The method according to claim 1 wherein  $s$ ,  $c$ , and  $d$  are related such that  $s \equiv \frac{c}{d} \pmod{n}$ .  
24
- 25 7. The method according to claim 6 where said values  $c$ ,  $d$  are obtained to meet predetermined  
26 criteria.  
27

- 1 8. The method according to claim 7 wherein said values  $c$ ,  $d$  are obtained by application of an  
2 extended Euclidean algorithm and wherein iterations of said algorithm are terminated when  
3 said predetermined criteria are met.  
4
- 5 9. The method according to claim 6 wherein said one of said values corresponds to  $c$ .  
6
- 7 10. The method according to claim 6 wherein said one of said values corresponds to  $d$ .  
8
- 9 11. The method according to claim 1, wherein said signature component  $r$  is obtained from an  
10 integer  $k$  and said signature component  $s$  binds said integer  $k$ , a long term private key  $\alpha$  and  
11 said signature component  $r$  to said message.  
12
- 13 12. A method of verifying a compressed signature generated from a digital signature of a  
14 message, the digital signature having signature components  $r, s$ , said compressed signature  
15 having signature components  $r$  and one of a pair of values  $c, d$ , said values  $c, d$  related  
16 mathematically to  $s$ , one of said values being smaller than  $s$  and said one of said values  
17 having a smaller number of bits than  $s$ , said method of verifying said compressed signature  
18 being performed by a correspondent in a data communication system, the correspondent  
19 having a cryptographic module for performing cryptographic operations, said method of  
20 verifying said compressed signature comprising:  
21 - said cryptographic module recovering from said compressed signature the other of said  
22 values; and  
23 - said cryptographic module determining whether said recovered other of said values  
24 meets predefined criteria.  
25
- 26 13. The method of verifying a compressed signature according to claim 12 wherein recovery of  
27 said other of said values is obtained from combining said signature components of said  
28 compressed signature.  
29

- 1 14. The method of verifying a compressed signature according to claim 13 wherein an  
2 intermediate value is obtained from said message and combined with values obtained from  
3 said signature components of said compressed signature to recover said other of said values.  
4
- 5 15. The method of verifying a compressed signature according to claim 12 wherein said  
6 recovered other of said values is required to fall within defined bounds.  
7
- 8 16. The method of verifying a compressed signature according to claim 12 further comprising:  
9 -said cryptographic module rejecting said compressed signature if said recovered other of  
10 said values does not meet said predefined criteria; and  
11 - said cryptographic module accepting said compressed signature if said recovered other  
12 of said values meets said predefined criteria.  
13
- 14 17. The method of verifying a compressed signature according to claim 16 wherein a further  
15 verification is performed on an original signature obtained from application of said one of  
16 said values and said recovered other of said values to said compressed signature.  
17
- 18 18. A cryptographic system for generating a compressed signature from a pair of signature  
19 components  $r$ ,  $s$ , said system comprising:  
20 - an arithmetic unit to provide a pair of values  $c$ ,  $d$  mathematically related to said  
21 component  $s$ , one of said values being smaller than  $s$  and said one of said values having a  
22 smaller number of bits than  $s$ ; and  
23 - a signature generator to substitute said one of said values for said signature component  
24  $s$ .  
25
- 26 19. The cryptographic system according to claim 18, wherein said signature component  $r$  is  
27 obtained from an integer  $k$  and said signature component  $s$  binds said integer  $k$ , a long term  
28 private key  $\alpha$  and said signature component  $r$  to said message.

1 20. A cryptographic system for verifying a compressed signature sender generated using the  
2 system according to claim 18, said cryptographic system comprising an arithmetic unit to  
3 recover the other of said values and compare said other of said values with predefined  
4 criteria.

5

6 21. A correspondent device comprising a cryptographic module for performing cryptographic  
7 operations, the cryptographic module configured to perform the method of any one of claims  
8 1 to 17.

9

10 22. A computer readable medium comprising computer executable instructions adapted to  
11 implement the method of any one of claims 1 to 17.

12

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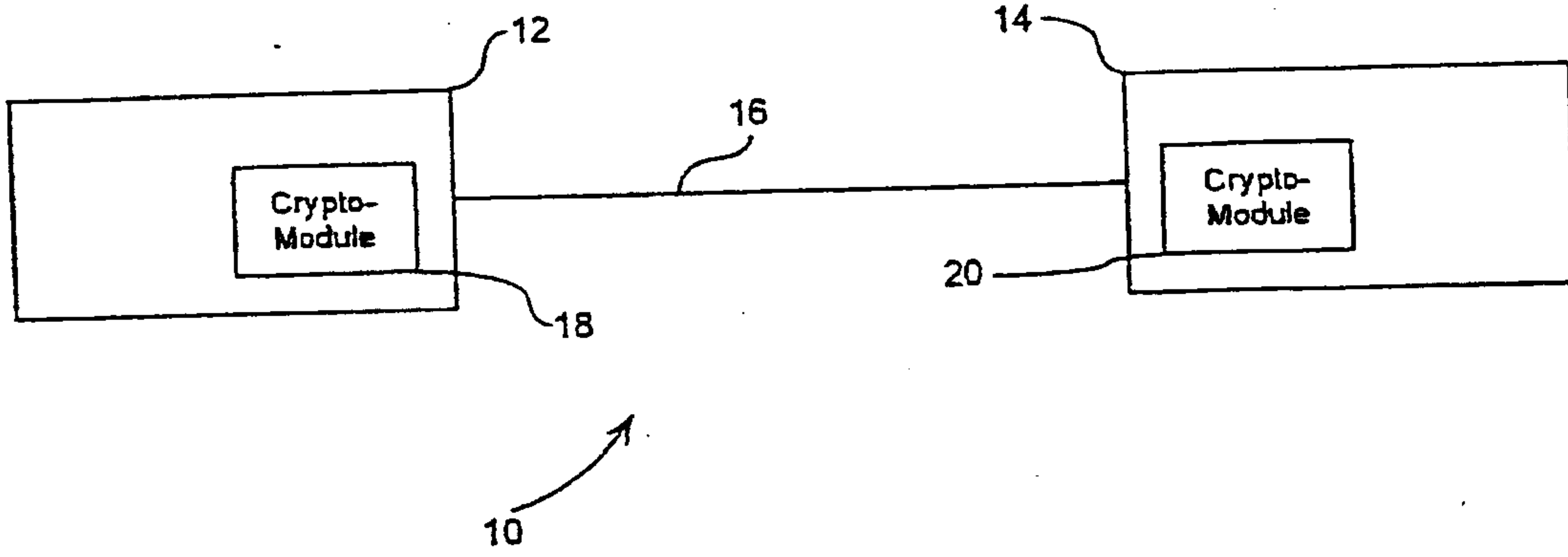


Figure 1

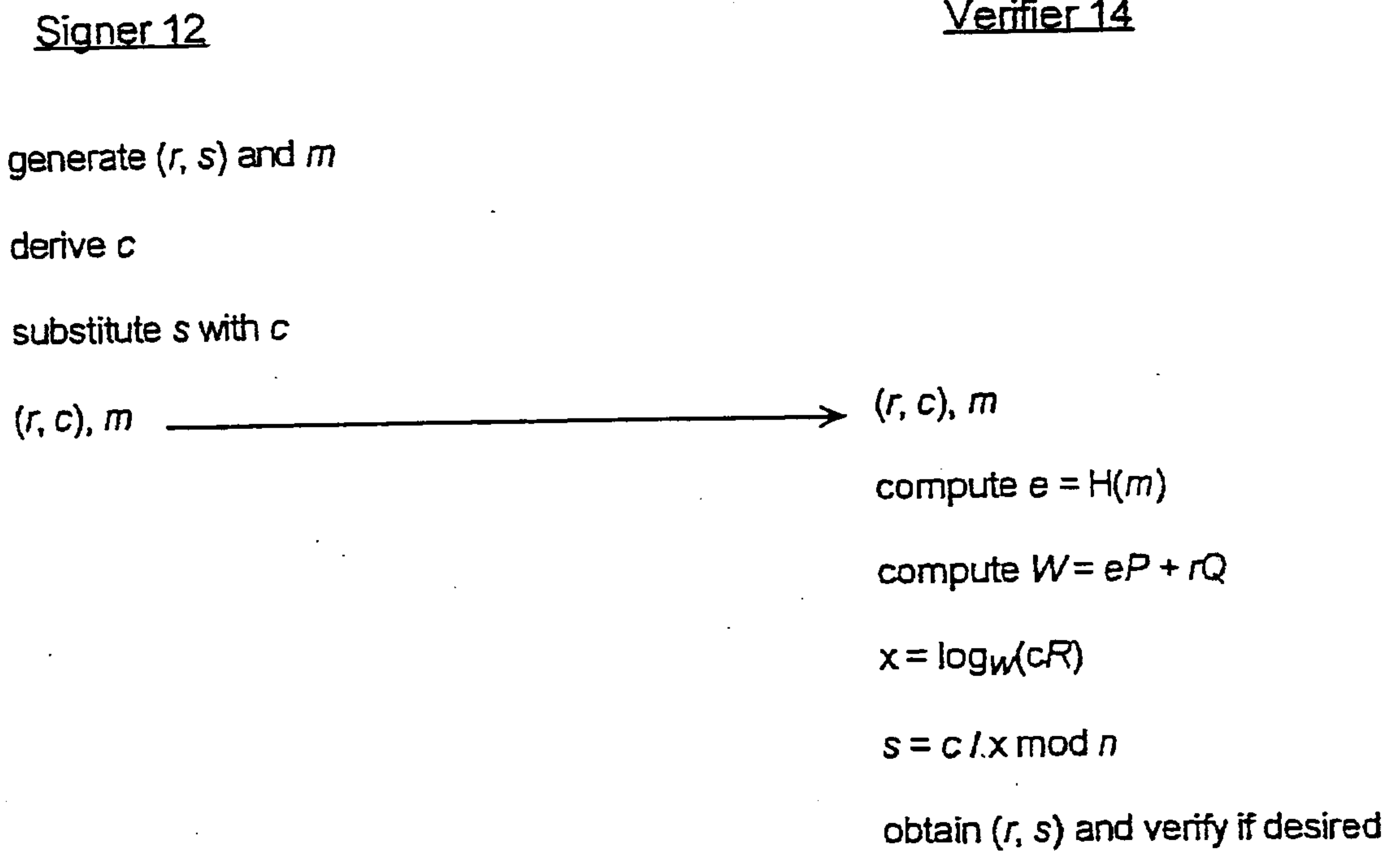
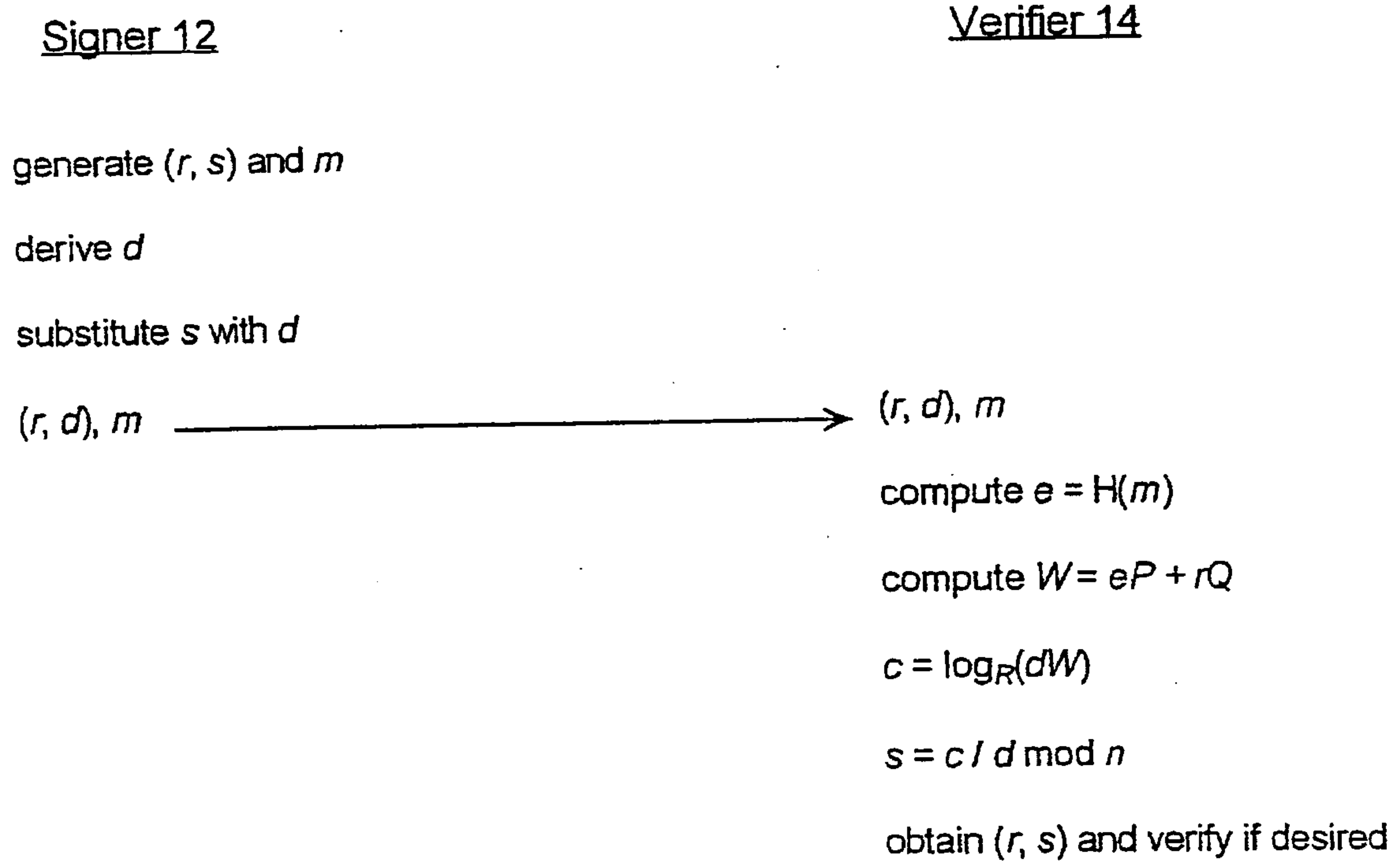


Figure 2

**Figure 3**

