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(54) AN ISOTOPE-ENRICHMENT UNIT AND A PROCESS
 FOR ISOTOPE SEPARATION

(71) We, EXXON NUCLEAR COMPANY INC., a corporation organized and existing under the laws of the State of Delaware, United States of America, of 777-106, Avenue NE, Bellevue, State of Washington, United States of America, do hereby declare the invention, for which we pray that a patent may be granted to us, and the method by which it is to be performed, to be particularly described in and by the following statement:-

The invention relates to an isotope-enrichment unit and to a process for isotope separation.

The separation of two nuclear isotopes which differ slightly in mass, such as uranium-235 and uranium-238, generally requires expensive equipment and great amounts of energy. Although gas-centrifugation processes for producing uranium hexafluoride (UF₆) enriched in uranium-235 for nuclear reactor fuels promise to require substantially less energy than gaseous-diffusion processes in present use, the energy requirements for a commercial gas-centrifuge uranium-enrichment facility are nonetheless enormous. Gas centrifuge isotope-enrichment plants are therefore designed to operate as efficiently as possible to minimize the cost of energy consumption. A second significant economic factor is the cost of the plant itself. Gas-centrifuge plants are therefore designed to require as little equipment as practical, consistent with the need for safe operation.

A gas centrifuge for enriching uranium generally has an input into which gaseous uranium hexafluoride is introduced, a light-fraction output of which a light fraction enriched in ²³⁵UF₆ is withdrawn, and a heavy-fraction output out of which a heavy fraction depleted in ²³⁵UF₆ is withdrawn. One aspect of the performance of such a gas centrifuge is measured by the separation factor α , which is defined by the following formula:

$$\alpha = \frac{X_L}{1-X_L} \cdot \frac{1-X_H}{X_H}$$

where X_L is the mole fraction of ²³⁵UF₆ in the light fraction and X_H is the mole fraction of ²³⁵UF₆ in the heavy fraction. When the mole fractions X_L and X_H are much less than 1, as is the case when uranium hexafluoride containing 3 mole percent or so of ²³⁵UF₆ for enriched-uranium reactors for electric power generation is being produced, α approximately equals the ratio of the mole fraction of ²³⁵UF₆ in the light fraction to the mole fraction of ²³⁵UF₆ in the heavy fraction. The value of α for a particular gas centrifuge depends both on the design of the centrifuge and the conditions under which it is operated.

Typically the separation factors of present-day gas centrifuges under ordinary operating conditions are too low to permit natural-abundance uranium hexafluoride in a single pass through a gas centrifuge to be enriched in uranium-235 sufficiently for use as a fuel in an enriched-uranium reactor. However if a number of gas centrifuges are connected in series so that an output of one centrifuge feeds an input of another, it is possible to enrich uranium hexafluoride progressively to the concentrations of uranium-235 required by such reactors. Thus gas centrifuges for use in producing enriched uranium are ordinarily interconnected to form what are termed *cascades*. A cascade includes one or more *stages* of gas centrifuges, the term stage referring to a group of gas centrifuges connected in parallel. Pressure and flow regulators are used to control the flow of uranium hexafluoride among the stages and

gas centrifuges. Cascade designs for commercial uranium enrichment plants often incorporate hundreds or even thousands of gas centrifuges. Generally the stages of a cascade are interconnected so that each input of a stage is supplied with uranium hexafluoride from heavy-fraction outputs of stages above it and from light-fraction outputs of stages below it. Thus uranium hexafluoride passing "upward" through a cascade becomes progressively enriched in uranium-235 while uranium hexafluoride passing "downward" becomes progressively depleted in uranium-235. The stages of a cascade are generally divided into two groups, termed *enriching stages* and *stripping stages*, an enriching stage being one into which a feedstock is introduced or located higher in the cascade. As used herein, the term cascade can refer to a single stage. The stage of a single-stage cascade would be termed an enriching stage according to the above definition since feedstock is introduced into it.

Since it is costly to enrich the uranium-235 concentration in uranium hexafluoride, mixing two streams of uranium hexafluoride having different degrees of enrichment represents an expense. Cascades are thus ordinarily designed to minimize any such mixing losses in the operation of the cascade. Specific designs of such no-mix cascades for interconnecting various types of gas centrifuges are well known in the art and for conciseness will not be described here. See, for example, H. R. Pratt, *Countercurrent Separation Processes*, Elsevier Publishing Co., New York (1967). It will be noted, however, that considerations concerning the economics of operating a cascade imply that cascades for enriching natural abundance uranium preferably include several stripping stages. Thus, in addition to producing a product fraction enriched in uranium-235 to the degree needed for reactor fuel, cascades of gas centrifuges for enriching natural-abundance uranium hexafluoride also generally produce a waste fraction depleted in $^{235}\text{UF}_6$ to a predetermined concentration, typically about 0.2-0.35 mole percent.

A commercial uranium-enrichment facility must provide uranium enriched in uranium-235 to varying degrees since different reactors require fuels having significantly different concentrations of uranium-235. Thus a gas-centrifuge plant would normally include a number of cascades, the cascades having different numbers of enriching stages so that products of different concentrations are produced when the cascades are supplied with natural-abundance uranium hexafluoride.

Figure 1 depicts a schematic flow graph of a representative prior-art isotope-enrichment unit 100 for enriching natural-abundance uranium hexafluoride. The isotope-enrichment unit 100 will be described in detail to illustrate the flow graph of Figure 1, since this type of flow graph is employed in connection with various preferred embodiments of the present invention disclosed below. The heavy vertical lines of Figure 1 represent cascades of gas centrifuges, with filled-in diamonds representing inputs to the cascades and filled-in squares representing outputs. Thus a cascade 112A has an input 114A, a heavy-fraction output 116A, and a light-fraction output 118A. The input 114A of the cascade 112A is connected to a feedstock supply line 140. The heavy-fraction output 116A is connected to a waste-fraction discharge line 142 and the light-fraction output 118A is connected to a first product-fraction discharge line 144. Connected in parallel with the cascade 112A are other operationally-equivalent cascades such as cascades 112J and 112K to form a first subunit 110. An input 114J of the cascade 112J is connected to the feed stock supply line 140. The heavy-fraction and light-fraction outputs 116J and 118J are respectively connected to the waste-fraction and first product-fraction discharge lines 142 and 144. The cascade 112K and other cascades included in group 110 but not shown in Figure 1 are connected to the supply line 140 and the discharge lines 142 and 144 in the same manner as the cascades 112A and 112J.

The vertical axis of the flow graph of Figure 1 represents the concentration of $^{235}\text{UF}_6$ relative to the concentration of $^{235}\text{UF}_6$ in the feedstock in a logarithmic scale to a base equal to the separation factor α . The drawings of this application are based on gas centrifuges having a separation factor of 1.5. Although the separation factor of a gas centrifuge typically varies somewhat with its position within a cascade, such variations are ordinarily sufficiently small as to be negligible in the context of understanding the present invention. Referring to the vertical coordinate of the light-fraction outputs 118A-118K and the light-fraction discharge line 144 in Figure 1, it may be seen that the cascades of the first subunit 110 produce a product fraction enriched in uranium-235 relative to the feedstock ideally by a factor α^3 . For a separation factor α of 1.5 this corresponds to a $^{235}\text{UF}_6$ concentration of about 2.40 mole percent. The cascades of the first subunit 110 also produce a waste fraction depleted in uranium-235 ideally by a factor of α^{-3} , as may be read from the vertical axis of Figure 1, which corresponds to a $^{235}\text{UF}_6$ concentration of about 0.21 mole percent. One cascade design which is termed in the prior art a one-up/one-down countercurrent cascade can accomplish isotope enrichment and depletion by these factors with six stages of gas centrifuges with separation factors equal to α in the enriching section

and five such stages in the stripping section. Other cascade designs may require different numbers of stages in the two sections.

The isotope enrichment unit 100 also includes a second subunit of cascades 120 and a third subunit 130. Included in the second subunit 120 are cascades 122A-122M which have respectively inputs 124A-124M, heavy-fraction outputs 126A-126M, and light-fraction outputs 128A-128M. The inputs 124A-124M are connected to the feedstock supply line 140 and the waste fraction outputs 126A-126M are connected to the waste fraction discharge line 142. The light fraction outputs 128A-128M are connected to a second product discharge line 146. The cascades of the second group 120 ideally produce a product fraction enriched in uranium-235 by a factor of $\alpha^{3.5}$ and a waste fraction depleted in that isotope by α^{-3} . Similarly the third subunit 130 produces a product fraction enriched in uranium-235 by a factor of α^4 and a waste fraction having substantially the same concentration as the waste fractions produced by the first and second subunits 110 and 120. The cascades 132A-132N of the third subunit have inputs 134A-134N connected to the feedstock supply line 140, heavy-fraction outputs 136A-136N are connected to the waste discharge line 142 and the light fraction outputs 138A-138N are connected to a third product discharge line 148.

The cascades of the three subunits have the same number of stripping stages and thus ideally all produce a heavy fraction of the same concentration of uranium-235. Combining the waste fractions produced by the three subunits therefore does not give rise to any significant mixing losses. The three groups of cascades differ, however, in the number of enriching stages. For the one-up/one-down countercurrent cascade design referred to above, cascades of the first, second, and third subunits would all have five stripping stages, but would have respectively six, seven, and eight enriching stages. Thus the isotope-enrichment unit 100 when supplied with natural-abundance uranium hexafluoride on feedstock supply line 140 produces one waste fraction which is withdrawn over the waste discharge line 142 and three product fractions of enriched uranium which are withdrawn over the first, second and third product discharge lines 144, 146, and 148. The rate at which a given product fraction is produced by the isotope-enrichment unit 100 depends on the number and individual capacity of the cascades in the corresponding subunit.

Not only are reactor fuels of different concentrations of uranium-235 required at any given time, but as time goes on the demand profile for fuels enriched to different degrees is likely to change. The changing demand profile for reactor fuels in part results from the fact that nuclear reactors generally require fuels of higher concentrations of uranium-235 for reloading than for starting up. Thus, if, as is likely to be the case, the customers of a new uranium enrichment plant are primarily new nuclear power plants, then the demand profile will shift in time towards higher average concentrations of uranium-235. In addition, reactor designs can be expected to continue to evolve, which leads to changes in the demand profile as new reactors are built.

The changing demand profile for enriched uranium presents a serious problem in designing a uranium-enrichment facility. One way to provide the capability of meeting changes in the demand profile is to have the facility produce a wide spectrum of product fractions of different concentrations of uranium-235 by having numerous subunits of cascades with varying numbers of enriching stages. Uranium hexafluoride of particular concentrations could be made by blending product fractions and changes in the demand profile could be met by adjusting the product blends. However, as noted earlier, such blending is wasteful since isotope separation is such an expensive process. Moreover the average concentration of uranium-235 in the enriched-uranium products of such a plant can only be decreased by blending, and then only by mixing one or more product fractions with natural-abundance uranium or the waste fraction, which in either case results in extremely high mixing losses.

A second way to change the concentrations of products of a uranium enrichment plant which can reduce the problems of mixing losses inherent in blending is to redistribute cascades among the various subunits of the plant by "repiping" some of the cascades to change the number of stages in their enriching sections. To increase the average concentration of $^{235}\text{UF}_6$ in the enriched product, for example, a number of the cascades from a subunit having few enriching stages could be repiped into cascades having more enriching stages. Changing even by only one the number of enriching stages for most cascade designs, however, requires changing the number of gas centrifuges in each stage and altering the flow rates of uranium hexafluoride between all of the stages. Thus repiping a large cascade is a major undertaking which involves extended down time and considerable expense. The difficulties which attend repiping a cascade are compounded when the cascade has been handling radioactive material. Moreover, if a commercial gas centrifuge plant is to meet by redistributing cascades among subunits a shift in the product demand profile which stems from supplying a group of reactors at which at one time only 40% require fuel for reloading, but of which 90% require fuel for reloading three years later,

then about 27% of the cascades in the plant must be repiped. Repiping over a quarter of the cascades in a gas centrifuge plant after they have been handled radioactive uranium hexafluoride is an undertaking comparable in scale to interconnecting all of the gas centrifuges of the plant initially.

- 5 The present invention seeks to provide an isotope-enrichment unit and a method for isotope separation in which mixing losses can be reduced or eliminated and whose distribution of products can be changed quickly and relatively inexpensively to meet changes in the demand profile. 5

10 The present invention provides a method of separating a supply of gaseous-mixture feedstock comprising a compound of a light nuclear isotope at a predetermined concentration and a compound of a heavy nuclear isotope at a predetermined concentration into at least two unit-output fractions including at least one waste fraction depleted in the light isotope to a predetermined concentration and at least one product fraction enriched in the light isotope to a predetermined concentration, comprising the steps of: 10

- 15 (a) directing gaseous-mixture feedstock into each cascade input of a principal group of cascades of gas centrifuges to introduce the gaseous-mixture feedstock into the cascades; 15

(b) centrifugally processing the gaseous-mixture feedstock introduced into each cascade of the principal group with a plurality of enriching stages and a plurality of stripping stages of the cascade to separate it into light and heavy gaseous-mixture fractions;

- 20 (c) conveying a first gaseous-mixture fraction produced by the principal group of cascades from the gaseous-mixture feed-stock to an input of an auxiliary cascade of gas centrifuges and directing it into the input to introduce the fraction into the auxiliary cascade; 20

25 (d) centrifugally processing the first gaseous-mixture fraction with the auxiliary cascade to separate it into an auxiliary light fraction and an auxiliary heavy fraction, the mole fraction of the light isotope in the auxiliary light fraction being approximately equal to the mole fraction of light isotope in one of a product fraction, a waste fraction, and the gaseous-mixture feedstock, and the mole fraction of the light isotope in the auxiliary heavy fraction being approximately equal to the mole fraction of light isotope in one of a product fraction, a waste fraction, and the gaseous mixture feedstock; 25

- 30 (e) withdrawing at least a portion of a unit output fraction from one of the auxiliary light fraction and the auxiliary heavy fraction; 30

35 (f) withdrawing at least a portion of a waste fraction from at least one of a heavy fraction produced by the principal group of cascades, the auxiliary light fraction, and the auxiliary heavy fraction, such gaseous mixture fraction from which the portion of waste fraction is withdrawn being depleted in the light isotope to approximately the mole fraction of said waste fractions; and 35

- 40 (g) withdrawing at least a portion of a product fraction from at least one of a light fraction produced by the principal group of cascades, the auxiliary light fraction, and the auxiliary heavy fraction, such gaseous-mixture fraction from which the portion of product fraction is withdrawn being enriched in the light isotope to approximately the mole fraction of said product fraction. 40

45 The present invention also provides an isotope enrichment unit for separating a gaseous-mixture feedstock comprising a compound of a light nuclear isotope at a predetermined concentration and a compound of a heavy nuclear isotope at a predetermined concentration into at least two unit-output fractions including at least one waste fraction depleted in the light isotope to a predetermined concentration and at least one product fraction enriched in the light isotope to a predetermined concentration, comprising: 45

- 50 (a) a principal group of cascades of gas centrifuges, each cascade having a plurality of enriching stages, a plurality of stripping stages, an input, a light-fraction output, and a heavy-fraction output for separating the gaseous-mixture feedstock into light and heavy gaseous-mixture fractions; 50

55 (b) a feedstock inlet system connected to each input of the principal group of cascades for introducing the gaseous-mixture feedstock into each input; 55

(c) a product-fraction collection system connected to at least one light-fraction output of the principal group of cascades for withdrawing at least a portion of one or more product fractions from the principal group of cascades;

- 60 (d) a waste-fraction collection system connected to at least one heavy-fraction output of the principal group of cascades for withdrawing at least a portion of one or more waste fractions from the principal group of cascades; 60

(e) an auxiliary cascade having an input, a light-fraction output, and a heavy-fraction output;

- 65 (f) a first conduit connected between outputs of one or more first cascades included in the principal group and the input of the auxiliary cascade for directing at least a portion of a 65

gaseous-mixture fraction produced by the principal group of cascades into the auxiliary cascade for further separation into a light fraction and a heavy fraction; and

(g) an auxiliary collection system connected to an output of the auxiliary cascade for withdrawing at least a portion of a unit-output fraction from the auxiliary cascade.

5 The present invention also provides an isotope enrichment unit for separating a 5
gaseous-mixture feedstock comprising a compound of a light nuclear isotope at a
predetermined concentration and a compound of a heavy nuclear isotope at a predeter-
mined concentration into at least two unit-output fractions including at least one waste
10 fraction depleted in the light isotope to a predetermined concentration and at least one 10
product fraction enriched in the light isotope to a predetermined concentration,
comprising:

(a) a principal group of cascades of gas centrifuges, each cascade having a plurality of
enriching stages, a plurality of stripping stages, an input, a light-fraction output, and a
15 heavy-fraction output for separating the gaseous-mixture feedstock into light and heavy 15
gaseous-mixture fractions;

(b) a feedstock inlet system connected to each input of the principal group of cascades
for introducing the gaseous-mixture feedstock into each input;

(c) a product-fraction collection system connected to at least one light-fraction output
of the principal group of cascades for withdrawing at least a portion of a product fraction
20 from the principal group of cascades; 20

(d) a waste-fraction collection system connected to at least one heavy-fraction output of
the principal group of cascades for withdrawing at least a portion of a waste fraction from
the principal group of cascades;

(e) an auxiliary cascade having a input, a light-fraction output, and a heavy-fraction
25 output, the heavy-fraction output being a reciprocal output to a light-fraction output of one 25
or more first cascades in the principal group;

(f) an isotope-mixture conveyance system for conveying the light isotope-mixture
fraction from said outputs of the first cascades to the input of the auxiliary cascade and
30 directing it into the input so that at least a portion of a light isotope-mixture fraction 30
produced by the principal group of cascades can be further separated into a light fraction
and a heavy fraction by the auxiliary cascade;

(g) an auxiliary product-fraction collection system connected to the light-fraction
output of the auxiliary cascade for withdrawing at least a portion of a product fraction from
the auxiliary cascade; and

(h) a feedstock collection system connected to the heavy-fraction output of the auxiliary
35 cascade for withdrawing gaseous-mixture feedstock from the auxiliary cascade. 35

Preferably, in the unit and method of the present invention, a light or heavy fraction
produced by the auxiliary cascade has substantially (ideally exactly) the same concentration
of light isotope as the gaseous-mixture feedstock. Herein a light-fraction output of a first
40 cascade and a heavy-fraction output of a second cascade are termed reciprocal outputs if the 40
number of enriching and stripping stages in the two cascades are such that when light
fraction from the output of the first cascade is supplied to the second cascade as a feed, the
heavy fraction from the output of the second cascade has substantially the same mole
fraction of light isotope as the feed supplied to the first cascade. For two conventional
45 one-up/one-down cascades, the light-fraction output of one cascade and the heavy-fraction 45
output of the other are reciprocal outputs if the number of stripping stages of the latter
cascade equals the number of enriching stages minus one of the former. Thus in one
preferred embodiment of the present invention, the heavy-fraction output of the auxiliary
cascade and at least one light-fraction output of one or more first cascades included in the
50 first group of cascades are reciprocal outputs, and the auxiliary cascade is supplied with feed 50
from such light fraction outputs. The heavy fraction produced by the auxiliary cascade can
thus be combined with the gaseous-mixture feedstock and recycled to the first group of
cascades without suffering significant mixing losses. The average concentration of the light
isotope in the product fractions produced by this embodiment is significantly greater than
55 the average concentration of the light isotope in the product fractions from a corresponding 55
conventional isotope-enrichment unit which has a first group of cascades identical to the
first group of the preferred embodiment and has one additional cascade which is connected
in parallel with a cascade of the first group, the additional cascade having the same number
of gas centrifuges as the auxiliary cascade of the preferred embodiment. Conventional
60 isotope-enrichment units can thus be converted to this preferred embodiment in order to 60
meet a shift in the product demand profile towards significantly increased average
concentration of light isotope.

A feature of the present invention is that changes in the distribution of products from an
isotope-enrichment unit can be accomplished without significantly affecting the mixing
65 losses of the unit and without redistributing a large fraction of cascades among subunits. For 65

example, repiping only a few percent of the cascades of a conventional isotope-enrichment unit to convert it to an isotope-enrichment unit of the present invention can change the distribution of the product fractions to approximately the same extent as repiping over twenty-five percent of the cascades of the conventional unit to redistribute them among its subunits. Repiping a relatively few cascades to make an isotope-enrichment unit of the present invention can thus be an economically-attractive strategy for meeting changes in the product demand profile, particularly unanticipated changes.

If shifts in the product demand profile can be predicted in advance, then it may be preferable to use embodiments of the present invention which include valves to enable one or more cascade to be "swung" between two or more alternative modes of operation to change the product distribution economically without having to repipe any cascades. Thus in a preferred embodiment of the present invention, valve means and conduits are included for alternately connecting the input of the auxiliary cascade to one of two sources of gaseous-mixture feed. For example, one source might be the means for introducing the gaseous-mixture feedstock into the inputs of the first group of cascades and the other source a light-fraction discharge line of a subunit of the first group. Alternatively, the input of the auxiliary cascade might be swung between the light-fraction discharge lines of two different subunits which produce light fractions of different compositions. In either embodiment, the auxiliary cascade can be operated in one of two modes, the concentrations of the light isotope in the light and heavy fractions produced by the auxiliary cascade in the two modes being different. In this way the concentration of product fractions can be changed conveniently to meet changes in the product demand profile by simply swinging valves, thereby avoiding the trouble of repiping any cascades which have handled radioactive materials.

An additional feature of the present invention is that a large variety of cascade and gas centrifuge designs can be used to make the present isotope-enrichment unit. Thus in addition to the conventional one-up/one-down cascade design referred to above, the present isotope-enrichment unit may employ other less conventional cascade designs such as, for example, the two-up/one-down cascade described by D. R. Olander in "Nuclear Technology," vol. 29, pp. 108-112 (April 1976). It will of course generally be preferred to use cascade designs which minimize costs by operating most efficiently and requiring the fewest gas centrifuges to process feedstock at a given rate. Similarly it will ordinarily be preferred to use gas centrifuges of the most economical design for the present invention. The engineering details of cascade and gas centrifuge designs are not required to understand or appreciate the present invention and, for conciseness, are not discussed herein.

The present invention may be better appreciated if reference is made to the following drawings.

Figure 1 is a flow graph of a representative prior-art isotope-enrichment unit described above.

Figure 2 is a flow graph of a first embodiment of the isotope-enrichment unit of the present invention for producing three product fractions of different compositions. This embodiment includes a single-stage auxiliary cascade.

Figure 3 is a flow graph of a second embodiment of the present invention for producing four product fractions.

Figure 4 is a flow graph of a third embodiment of the present invention for producing three product fractions.

Figures 5A and 5B are flow graphs of a fourth embodiment of the present invention shown in alternate modes of operation. If operated in the mode depicted in Figure 5A, this embodiment produces three different product fractions. If operated in the mode of Figure 5B, it produces four product fractions.

Figures 6A and 6B depict alternate embodiments of valve means employed in the embodiment of Figures 5A and 5B.

Figure 7 is a flow graph of a fifth embodiment of the present invention. As with the embodiment of Figures 5A and 5B, this embodiment has two modes of operation. For conciseness only one mode of operation is shown in Figure 7.

Figure 8 is a flow graph of a sixth embodiment of the present invention. This embodiment also has two modes of operation, only one of which is shown.

Figure 9 is a flow graph of a seventh embodiment which has two modes of operation, only one of which is shown.

Figure 10 is a flow graph and schematic drawing of an eighth embodiment of the present invention which employs an alternate means for conveying a gaseous-mixture fraction from a subunit of cascades to an auxiliary cascade.

Detailed description of preferred embodiments

Referring now to Figure 2, a first isotope-enrichment unit 200 is shown in a schematic flow graph. The first isotope-enrichment unit 200 includes a first subunit 210, a second subunit 220, and a third subunit 230. The first subunit 210 includes cascades 212A-212J. Similarly, the second subunit 220 includes cascades 222A-222M and the third subunit 230 includes cascades 232A-232N. Each of the cascades included in the three subunits 210, 220, and 230 has a plurality of enriching stages and a plurality of stripping stages. The number of cascades in each subunit is not specified since it is not required to understand the present invention and since it will vary from application to application depending, as will be recognized by those skilled in the art, on the rate at which it is desired to produce the light fraction of the subunit and on the capacity of the cascades included in the subunit.

The cascades 212A-212J of the first subunit 210 have inputs 214A-214J, heavy-fraction outputs 216A-216J, and light-fraction outputs 218A-218J. The light-fraction outputs 218A-218J are connected to a first product-fraction discharge line 244 through which the light fraction of uranium hexafluoride produced by the first subunit 210 can be withdrawn. The inputs 214A-214J are connected to a feedstock supply line 240, as are inputs 224A-224M of the cascades 222A-222M of the second subunit 220 and the inputs 234A-234N of the cascades 232A-232N of the third subunit 230. The feedstock supply line 240 is a conduit through which uranium hexafluoride can be directed to the inputs of the cascades of the three subunits. For simplicity, conventional pressure and flow regulators for metering the uranium-hexafluoride feedstock from the feedstock supply line 240 to the cascades 212, 222, and 232 are not shown in Figure 2, nor are similar conventional control devices shown for discharge lines and other supply lines in this or the other figures. The heavy fraction outputs 216A-216J, 226A-226M, and 236A-236N of the first, second, and third subunits, respectively, are connected to a waste-fraction discharge line 242. The light-fraction outputs 228A-228M of the second subunit 220 are connected to a second product-fraction discharge line 246, and light-fraction outputs 238A-238N are connected to a third product-fraction discharge line 248.

From the vertical axis of the flow graph of Figure 2 it may be seen that the cascades of the first subunit ideally produce a light fraction enriched in $^{235}\text{UF}_6$ by a factor of α^3 relative to the uranium hexafluoride feedstock. The cascades 222A-222M of the second subunit produce a light fraction enriched ideally by the factor of $\alpha^{3.5}$, and the cascades 232A-232N of the third subunit 230 produce a light fraction enriched ideally by the factor of α^4 . For a separation factor α equal to 1.5, and a feedstock of natural abundance UF_6 , the enrichment factors α^3 , $\alpha^{3.5}$, and α^4 respectively correspond to product fractions having $^{235}\text{UF}_6$ concentrations of approximately 2.40, 2.93, and 3.59 mole percent. The cascades of all three subunits produce a heavy fraction depleted in $^{235}\text{UF}_6$ ideally by a factor of α^{-3} , which for α equal to 1.5 corresponds to a waste fraction having a concentration of $^{235}\text{UF}_6$ of about 0.21 mole percent.

A first auxiliary cascade 252 has an input 254, a heavy-fraction output 256, and a light-fraction output 258. A first auxiliary-cascade supply conduit 260 connects the input 254 to the second product-fraction discharge line 246 which in turn is connected to the light fraction outputs 228A-228M of the cascades of the second subunit 220. The second subunit 220 has a capacity sufficient to produce at least enough light fraction to supply the first auxiliary cascade 252. The heavy-fraction output 256 of the first auxiliary cascade 252 is connected to the first product-fraction discharge line 244 by a first auxiliary-cascade heavy-fraction discharge conduit 262 and the light-fraction output 258 is connected to the third product-fraction discharge line 248 by a first auxiliary-cascade light-fraction discharge conduit 264.

The first auxiliary cascade 252 is a single-stage cascade having a separation factor of about α which can separate uranium hexafluoride into a light fraction enriched in $^{235}\text{UF}_6$ ideally by a factor of $\alpha^{0.5}$ and a heavy fraction depleted in $^{235}\text{UF}_6$ ideally by a factor of $\alpha^{-0.5}$. Thus when supplied with uranium hexafluoride from the second product-fraction discharge line 246, which carries uranium hexafluoride enriched ideally by a factor of $\alpha^{3.5}$ relative to natural-abundance uranium, the first auxiliary cascade 252 produces a light fraction enriched by a factor of about α^4 and a heavy fraction enriched by a factor of about α^3 relative to natural-abundance uranium. Thus the light fraction produced by the first auxiliary cascade 252 can be combined with the light fraction produced by the cascades of the third subunit 230, and the heavy fraction produced by the first auxiliary cascade 252 can be combined with the light fraction produced by the cascades of the first subunit 210 without suffering significant mixing losses.

The prior-art isotope-enrichment unit 100 of Figure 1 can be reconstructed into an isotope-enrichment unit of the embodiment illustrated in Figure 2. For example, the cascade 112K of the prior-art unit 100 of Figure 1 could be repiped to make a single-stage cascade having the same number of gas centrifuges and connected to the product-fraction

discharge lines 144, 146, 148 in the way the first auxiliary cascade 252 in Figure 2 is connected to the product-fraction discharge lines 244, 246, 248. The rates at which the three product fractions of such a reconstructed isotope-enrichment unit are produced differ significantly from those of the conventional isotope-enrichment unit from which it was reconstructed: the rate of flow of product fraction produced by the second subunit is reduced while the rates of flow of the product fractions from the first and third subunits are increased. Thus it is possible to alter the distribution of the product fractions of a conventional isotope-enrichment unit such as is shown in Figure 1 by repiping it to make an isotope-enrichment unit of the present invention.

Referring now to Figure 3, a second isotope-enrichment unit 300 includes a first subunit 310, a second subunit 320, and a third subunit 330. The first subunit includes cascades 312A-312J having outputs 314A-314J, heavy-fraction outputs 316A-316J, and light-fraction outputs 318A-318J; the second subunit includes cascades 322A-322M having inputs 324A-324M, heavy-fraction outputs 326A-326M, and light-fraction outputs 328A-328M; and the third subunit 330 includes cascades 332A-332N having inputs 334A-334N, heavy-fraction outputs 336A-336N, and light-fraction outputs 338A-338N. The inputs 314, 324, and 334 are connected to a feedstock supply line 340, and the heavy-fraction outputs 316, 326, and 336 are connected to a waste-fraction discharge line 342. The light-fraction outputs 318 of the first subunit 310 are connected to a first product-fraction discharge line 344; the light-fraction outputs 328 of the second subunit 320 are connected to a second product fraction discharge line 346; and the light-fraction outputs 338 of the third subunit 330 are connected to a third product-fraction discharge line 348. The three subunits 310, 320, and 330 produce product and waste fractions of the same composition as the fractions produced by the corresponding subunits of the embodiment shown in Figure 2.

A second auxiliary cascade 352 has an input 354, a heavy-fraction output 356, and a light-fraction output 358. The input 354 of the second auxiliary cascade 352 is connected to the third product-fraction discharge line 348 by a second auxiliary-cascade supply conduit 360. A second auxiliary-cascade heavy-fraction discharge conduit 362 connects the heavy-fraction output 356 of the second auxiliary cascade 352 to the first product-fraction discharge line 344. The light fraction produced by the second auxiliary cascade 352 can be withdrawn over a second auxiliary-cascade light-fraction discharge line 364.

As may be seen by referring to the vertical axis of the flow graph of Figure 3, the second auxiliary cascade 352 can separate uranium hexafluoride into a light fraction enriched in $^{235}\text{UF}_6$ ideally by a factor of α and a heavy fraction depleted in $^{235}\text{UF}_6$ ideally by a factor of α^{-1} . The second auxiliary cascade can be, for example, a one-up/one-down countercurrent cascade having two enriching stages and one stripping stage. When the second auxiliary cascade 352 is supplied with uranium hexafluoride from the light-fraction outputs 338 of the third subunit 330 which is enriched by a factor of about α^4 relative to natural-abundance uranium, it produces a light fraction enriched by a factor of about α^5 and a heavy fraction enriched by a factor of about α^3 relative to natural-abundance uranium. The heavy fraction thus produced by the second auxiliary cascade 352 can be combined without significant mixing loss with the light fraction produced by the cascades of the first subunit 310. The uranium-hexafluoride light fraction thus produced by the second auxiliary cascade 352 has a concentration of $^{235}\text{UF}_6$ of about 5.39 mole percent, which is enriched to a greater degree than any of the light fractions produced by the three subunits 310, 320, or 330.

A third preferred embodiment of the present invention is illustrated in Figure 4. A third isotope-enrichment unit 400 includes a first subunit 410, a second subunit 420, and a third subunit 430. The first subunit includes cascades 412A-412J which include inputs 414A-414J, heavy-fraction outputs 416A-416J, and light-fraction outputs 418A-418J; the second subunit includes cascades 422A-422M which include inputs 424A-424M, heavy-fraction outputs 426A-426M, and light-fraction outputs 428A-428M; and the third subunit 430 includes cascades 423A-423N which include inputs 434A-434N, heavy-fraction outputs 436A-436N, and light-fraction outputs 438A-438N. The inputs 414, 424, and 434 are connected to a feedstock supply line 440 and the heavy-fraction outputs 416, 426, and 436 are connected to a waste-fraction discharge line 442. The light-fraction outputs 418 of the first subunit 410 are connected to a first product-fraction discharge line 444; the light-fraction outputs 428 of the second subunit 420 are connected to a second product-fraction discharge line 446; and the light-fraction outputs 438 of the third subunit 430 are connected to a third product-fraction discharge line 448. The three subunits 410, 420, and 430 produce product and waste fractions of the same composition as the fractions produced by the corresponding subunits of the embodiments shown in Figures 2 and 3.

A third auxiliary cascade 452 has an input 454, a heavy-fraction output 456, and a light-fraction output 458. The input 454 of the third auxiliary cascade 452 is connected to the first product-fraction discharge line 444 by a third auxiliary-cascade supply conduit 460. A third auxiliary-cascade light-fraction discharge conduit 464 connects the light-fraction

output 458 of the third auxiliary cascade 452 to the third product-fraction discharge line 448. The heavy-fraction output 456 of the third auxiliary cascade 452 is connected by a third auxiliary-cascade heavy-fraction discharge conduit 462 to the feedstock supply line 440 for recycling the uranium-hexafluoride heavy fraction produced by the third auxiliary cascade 452 back to the inputs of the other cascades of the third isotope-enrichment unit 400.

As can be seen in Figure 4, the heavy-fraction output 456 of the third auxiliary cascade 452 and the light-fraction outputs 418 of the cascades 412 of the first subunit 410 are reciprocal outputs. The third auxiliary-cascade 452 can separate uranium hexafluoride into a light fraction enriched in $^{235}\text{UF}_6$ ideally by a factor of α and a heavy fraction depleted in $^{235}\text{UF}_6$ ideally by a factor of α^{-3} . A one-up/one-down countercurrent cascade having two enriching stages and five stripping stages is a preferred choice for the third auxiliary cascade 452. The cascades of the first subunit 410, if of the same one-up/one-down countercurrent design, each have six enriching stages. Thus the number of stripping stages of the third auxiliary cascade 452 equals the number of enriching stages minus one of the cascades 412 of the first subunit 410 which supplies the third auxiliary cascade 452 with enriched uranium-hexafluoride feed. When supplied with the uranium hexafluoride enriched by a factor of about α^3 over the natural-abundance uranium-hexafluoride feedstock from the first subunit 410, the third auxiliary cascade 452 separates it into a light fraction enriched by a factor of α^4 and a heavy fraction which has substantially the same composition as the feedstock. Since the $^{235}\text{UF}_6$ concentration in the heavy fraction produced by the third auxiliary cascade 452 is substantially the same as natural-abundance uranium hexafluoride, it can be mixed with the feedstock without significant mixing loss.

Reconstructing the prior-art isotope-enrichment unit 100 of Figure 1 to make an isotope-enrichment unit of the embodiment of Figure 4 can substantially change the rates at which the three product fractions are produced. In particular, the average concentration of $^{235}\text{UF}_6$ in the product fractions can be increased to a relatively large extent. If it is desired to increase the average enrichment of product fractions to the maximum extent by reconstructing the prior-art isotope-enrichment unit 100 to make an isotope enrichment unit of this embodiment, it is generally preferable for the auxiliary cascade to have few enriching stages. Two competing factors are involved in increasing the average enrichment: (1) the greater the number of enriching stages of an auxiliary cascade, the more enriched is the light fraction it produces, but (2) the greater the number of enriching stages, the lower the rate at which cascades of most designs produce light fraction. The second factor ordinarily dominates for most conventional cascade designs if the number of centrifuges is kept fixed, in the sense that the product of the rate at which the light fraction is produced and the concentration of $^{235}\text{UF}_6$ in the light fraction is greater the fewer the number of enriching stages, because fewer enriching stages leads to more centrifuges in the stripping section and consequently to a greater increase in the average enrichment.

Figures 5A and 5B depict a fourth embodiment of the present invention in alternate modes of operation. Referring now to Figures 5A and 5B, a fourth isotope-enrichment unit 500 includes a first subunit 510, a second subunit 520, and a third subunit 530. The first subunit includes cascades 512A-512J having inputs 514A-514J, heavy-fraction outputs 516A-516J, and light-fraction outputs 518A-518J; the second subunit includes cascades 522A-522M having inputs 524A-524M, heavy-fraction outputs 526A-526M, and light-fraction outputs 528A-528M; and the third subunit 530 includes cascades 532A-532N having inputs 534A-534N, heavy-fraction outputs 536A-536N, and light-fraction outputs 538A-538N. The inputs 514, 524, and 534 are connected to a feedstock supply line 540, and the heavy-fraction outputs 516, 526, and 536 are connected to a waste-fraction discharge line 542. The light-fraction outputs 518 of the first subunit 510 are connected to a first product-fraction discharge line 544; the light-fraction outputs 528 of the second subunit 520 are connected to a second product-fraction discharge line 546; and the light-fraction outputs 538 of the third subunit 530 are connected to a third product-fraction discharge line 548. The three subunits 510, 520, and 530 produce product and waste fractions of the same composition as the fractions produced by the corresponding subunits of the previous embodiments.

A first swinging auxiliary cascade 552 has an input 554, a heavy-fraction output 556, and a light-fraction output 558. Connected to the input 554 is a trunk port of a two-way feed supply valve 570. A first branch port of the supply valve 570 is connected to an end of a lean feed supply conduit 560, and a second branch port of the supply valve 570 to an end of a rich feed supply conduit 561. The other end of the lean feed supply conduit 560 is connected to the feedstock supply line 540 and the other end of the rich feed supply conduit 561 is connected to the first product-fraction discharge line 544. Similarly, the light-fraction output 558 is connected to a two-way light-fraction discharge valve 572, which is connected to a lean light-fraction discharge conduit 564 and to a rich light-fraction conduit 565. The lean light-fraction discharge conduit 564 is also connected to the first product-fraction

discharge line 544. Rich light fraction can be withdrawn from the isotope-enrichment unit 500 over the rich light-fraction discharge line 565. The heavy-fraction output 556 of the first swinging auxiliary cascade 552 is connected to a two-way heavy-fraction discharge valve 574 which is connected to a lean heavy-fraction discharge conduit 562 and to a rich heavy-fraction discharge conduit 563. The lean heavy-fraction discharge conduit 562 is also connected to the waste-fraction discharge line 542. The rich heavy-fraction discharge conduit 563 is connected to the feedstock supply line 540.

The two-way supply and discharge valve 570, 572, and 574 are shown schematically as filled-in triangles in Figures 5A and 5B. A preferred three-port, two-way valve 576 for this application is shown in greater detail in Figure 6A. A trunk conduit 578 for connecting the valve to an input or output of the swinging auxiliary cascade 552 is connected to a valve mechanism 580 through a trunk port 581. The valve mechanism 580 is also connected to a principal branch conduit 582 and to an alternate branch conduit 584 through a principal branch port 583 and an alternate branch port 585 respectively. The trunk port 581 is in closer communication to the input or output of the auxiliary cascade 552 than either of the two branch ports 583 and 585. As shown in Figure 6A, the trunk conduit 578 is in communication with the alternate branch conduit 584 through a channel 586. If the valve mechanism 580 is rotated counterclockwise by ninety degrees the trunk conduit 578 communicates with the principal branch conduit 582. Only one of the two branch conduits 582 and 584 is in communication with the trunk conduit 578 at any given time.

A second example of a two-way valve is a "T"-joint conduit with an on-off valve in each arm of the "T", shown in Figure 6B. The trunk conduit 578 can be alternately connected to the principal branch conduit 582 or the alternate branch conduit 584 by appropriately opening and closing a first on-off valve 590 and a second on-off valve 592, which are connected in series respectively with the principal and alternate branch conduits 582 and 584.

Referring again to Figure 5A, it can be seen that the first swinging auxiliary cascade 552 produces light and heavy fractions respectively enriched in $^{235}\text{UF}_6$ ideally by the same factors as the cascades 512 for the first subunit 510. Thus when the two-way supply and discharge valves 570, 572, and 574 respectively connect the input 554 to the lean feed supply conduit 560, the light-fraction output 558 to the lean light-fraction discharge conduit 564, and the heavy-fraction output 556 to the lean heavy-fraction discharge conduit 562, the swinging auxiliary cascade 552 operates in parallel with the cascades 512 of the first subunit 510. This "lean mode" of operating the fourth isotope-enrichment unit 500 is shown in Figure 5A. In this mode the light and heavy fractions produced by the swinging auxiliary cascade 552 can be combined with the light and heavy fractions produced by the first subunit 510 without significant mixing losses.

On the other hand, if the two-way supply and discharge valves 570, 572, and 574 are switched so that the input 554 of the swinging auxiliary cascade 552 is connected to the rich feed supply conduit 561, the light-fraction output 558 is connected to the rich light-fraction discharge conduit 565, and the heavy-fraction output 556 is connected to the rich heavy-fraction discharge conduit 563, the fourth isotope-enrichment unit 500 operates in the "rich mode" shown in Figure 5B. Note that in the flow graph of Figure 5B the swinging auxiliary cascade 552 is shown in a higher vertical position than in Figure 5A to indicate that the gaseous mixtures at its input and outputs are richer in the sense of having higher concentrations of $^{235}\text{UF}_6$. Thus, for example, when operated in the rich mode the first swinging auxiliary cascade 552 is supplied with uranium hexafluoride enriched in $^{235}\text{UF}_6$ by a factor ideally of α^3 , whereas when operated in the lean mode, it is supplied with natural-abundance uranium hexafluoride.

The heavy-fraction output 556 of the first swinging auxiliary cascade 552 and the light-fraction outputs 518 of the cascades 512 of the first subunit 510 are reciprocal outputs. Thus the heavy fraction produced by the cascade in rich mode of operation of Figure 5B has ideally the same composition as the natural-abundance feedstock. The light fraction produced by the swinging auxiliary cascade 552 in this mode is enriched in $^{235}\text{UF}_6$ by a factor of substantially α^0 . Depending on its mode of operation, the fourth isotope-enrichment unit 500 produces either three or four product fractions. The average concentration of $^{235}\text{UF}_6$ in the four product fractions of the rich mode is significantly greater than the average concentration in the three product fractions of the lean mode. The mixing losses for the two modes of operation are substantially the same and can be made very low.

An isotope-enrichment unit of the present invention which includes a swinging auxiliary cascade and produces the same number of product fractions in both the rich and lean modes of operation is depicted in Figure 7. Referring now to Figure 7, a fifth isotope-enrichment unit 600 includes first, second, and third subunits 610, 620, and 630. The first subunit 610 can enrich uranium hexafluoride ideally by a factor of α^3 , the second subunit 620 by a factor of $\alpha^{4.5}$, and the third subunit 630 by a factor of α^0 . The cascades of these three subunits and

their inputs and outputs are designated in Figure 7 in a manner exactly analogous to the three subunits of the previous embodiments. For conciseness the designations will not be enumerated in the text.

A second swinging auxiliary cascade 652 has an input 654, a heavy-fraction output 656, and a light-fraction output 658. Connected to the input 654 is a trunk port of a two-way supply valve 670 for connecting the input 654 through one of two branch ports either to a lean feed supply conduit 660 or to rich feed supply conduit 661. The lean feed supply conduit 660 is also connected to a feedstock supply line 640 and the rich feed supply conduit 661 is connected to a first product-fraction discharge line 644, which in turn is connected to the light-fraction outputs of the cascades of the first subunit 610. The light-fraction output 658 of the second swinging auxiliary cascade 652 is connected to a two-way light-fraction discharge valve 672 for connecting it either to a lean light-fraction discharge conduit 664 or to a rich light-fraction discharge conduit 665. The lean light-fraction discharge conduit 664 is also connected to the first product-fraction discharge line 644. The rich light-fraction discharge conduit 665 is connected to a third product-fraction discharge conduit 648 which in turn is connected to the light-fraction outputs of the cascades of the third subunit 630. The heavy-fraction output 656 of the second swinging auxiliary cascade 652 is connected to a two-way heavy-fraction discharge valve 674 for connecting the heavy-fraction output 656 either to a lean heavy-fraction discharge conduit 662 or to a rich heavy fraction discharge conduit 663. The lean heavy-fraction discharge conduit 662 is also connected to a waste-fraction discharge line 642 to which the heavy-fraction outputs of the cascades of the three subunits 610, 620, and 630 are also connected. The rich heavy-fraction discharge conduit 663 is connected to the feed-stock supply line 640. The two-way supply and discharge valves 670, 672, and 674 can be valves of the type shown in Figures 6A and 6B.

The second swinging auxiliary cascade 652 produces a light fraction enriched in $^{235}\text{UF}_6$ by a factor of substantially α^3 and a heavy fraction depleted by a factor of substantially α^{-3} . The enrichment and depletion factors of the swinging auxiliary cascade 652 are ideally the same as those of the cascades of the first subunit 610. Thus in the lean mode of operation, not illustrated in Figure 7, the second swinging auxiliary cascade 652 is operated in parallel to the cascades of the first subunit 610 in a manner analogous to the lean mode of operation of the first swinging auxiliary cascade 552 illustrated in Figure 5A. In the rich mode of operation which is illustrated in Figure 7, the two-way supply and discharge valves are set to supply the input 654 of the second swinging-auxiliary cascade 652 with enriched uranium hexafluoride from the light fraction produced by the first subunit 610 and to combine the light and heavy fractions produced by the swinging auxiliary cascade 652 respectively with the light fraction produced by the third subunit 630 and carried in the third product-fraction discharge line 648 and the uranium hexafluoride feedstock carried in the feedstock supply line 640. The heavy-fraction output 656 of the second swinging auxiliary cascade 652 and the light-fraction outputs 618 of the cascades 612 of the first subunit 610 are reciprocal outputs. Thus combining the heavy fraction produced by the second swinging auxiliary cascade 652 with the uranium hexafluoride feedstock leads to no significant mixing losses. Similarly, combining the light fraction produced by the second swinging auxiliary cascade 652 with the light fraction produced by the third subunit 630 leads to substantially no mixing losses because the auxiliary cascade enriches uranium hexafluoride previously enriched by a factor of ideally α^3 by an additional factor of ideally α^3 leading to an overall enrichment factor of substantially α^6 , which is substantially the same enrichment factor as provided by the cascades of the third subunit 630.

A sixth isotope-enrichment unit 700 is shown in Figure 8 and includes first, second, and third subunits 710, 720, and 730 which can respectively enrich uranium hexafluoride by the same factors as the corresponding subunits of the fifth isotope-enrichment unit 600 described above. As in the case of Figure 7 the reference numerals for the cascades of the three subunits and their inputs and outputs will not be enumerated in the text for conciseness.

A third swinging auxiliary cascade 752 has an input 754, a heavy-fraction output 756, and a light-fraction output 758. The input 754 can be connected alternatively to a feedstock supply line 740 or to a third product-fraction discharge line 748 by a two-way supply valve 770 and lean and rich feed supply conduits 760 and 761. A two-way light-fraction discharge valve 772 connects the light-fraction output either to a first product-fraction discharge line 744 by way of a lean light-fraction discharge conduit 764 or to a rich light-fraction discharge conduit 765 through which the light fraction produced by the third swinging auxiliary cascade 752 can be withdrawn in the rich mode of operation. The heavy-fraction output 756 can be connected alternatively by a two-way heavy-fraction discharge valve 774 and lean and rich heavy-fraction discharge conduits 762 and 763 to a waste-fraction discharge line 742 and the first product-fraction discharge line 744. In the rich mode of operation illustrated in Figure 8, the sixth isotope-enrichment unit 700 can produce four product

fractions, one of the product fractions being the light fraction produced by the third swinging auxiliary cascade 752. In the lean mode of operation, not shown, the third swinging auxiliary cascade 752 operates in parallel to the cascades of the first subunit 710. In this mode of operation only three product fractions are produced. Since the heavy fraction produced by the third swinging-auxiliary cascade 752 is not combined with the gaseous-mixture feedstock and recycled back to the cascades of the three subunits 710, 720, and 730 in the rich mode of operation, the increase in the average concentration of $^{235}\text{UF}_6$ in the product fractions upon switching from the lean to the rich mode is relatively small compared to the corresponding change for the fourth and fifth isotope-enrichment units 500 and 600 described above. Although the change in the average condition of $^{235}\text{UF}_6$ may be relatively small, the change in the product distribution is nonetheless substantial and may be useful for some applications.

A seventh isotope-enrichment unit 800 is shown in Figure 9 and includes first, second, and third subunits 810, 820, and 830 which can respectively enrich uranium hexafluoride by the same factors as the corresponding subunits of the fourth isotope-enrichment unit 500 described above. As in the case of Figure 7 the reference numerals for the cascades of the three subunits and their inputs and outputs will not be enumerated in the text for conciseness.

A fourth swinging auxiliary cascade 852 is a single-stage cascade and has an input 854, a heavy-fraction output 856, and a light-fraction output 858. The input 854 can be connected alternatively to a second or a third product-fraction discharge line 846 or 848 by a two-way supply valve 870 and lean and rich feed supply conduits 860 and 861. A two-way light-fraction discharge valve 872 connects the light-fraction output 858 either to a third product-fraction discharge line 848 by way of a lean light-fraction discharge conduit 864 or to a rich light-fraction discharge conduit 865 through which the light fraction produced by the third swinging auxiliary cascade 852 can be withdrawn in the rich mode of operation. The heavy-fraction output 856 can be connected alternatively by a two-way heavy-fraction discharge valve 874 and lean and rich heavy-fraction discharge conduits 862 and 863 to the first or the second product-fraction discharge lines 844 or 846. In the lean mode of operation illustrated in Figure 9, the seventh isotope-enrichment unit 800 can produce three product fractions. In the rich mode of operation, not shown, four product fractions are produced.

It will be recognized that a fourth subunit of cascades which produce a product fraction enriched ideally by a factor of $\alpha^{4.5}$ and a waste fraction depleted by a factor of α^{-3} can be included in the seventh isotope enrichment unit 800, and the rich light-fraction discharge line 865 connected to the light-fraction discharge line connected to the light-fraction outputs of the cascades of the fourth subunit. In this case four product fractions are produced independent of the mode of operation of the swinging auxiliary cascade 852. The rate at which the four product fractions are produced can be varied easily and without incurring significant mixing losses by swinging the single-stage auxiliary cascade 852 between the rich and lean modes of operation.

In operation, the preferred embodiments described above substantially continuously separate a supply of natural-abundance uranium hexafluoride into at least four streams of unit-output fractions including a waste fraction depleted in 235-uranium to about 0.2 mole percent and three or more product fractions enriched in 235-uranium to roughly 3 mole percent suitable for nuclear reactor fuel. A stream of natural-abundance uranium hexafluoride is introduced into each input of a first group of cascades of gas centrifuges over a feedstock supply line to introduce the uranium hexafluoride into the cascades. The streams are centrifugally processed with enriching and stripping stages of the cascades into light-fraction streams and heavy-fraction streams. A first stream of a light gaseous-mixture fraction produced by the first group of cascades is directed into an input of an auxiliary cascade of gas centrifuges to introduce the fraction into the auxiliary cascade. This first light-fraction stream is centrifugally processed with the auxiliary cascade to separate it into an auxiliary light-fraction stream and an auxiliary heavy-fraction stream. The mole fraction of the uranium-235 in the auxiliary light fraction is approximately equal to the mole fraction of uranium-235 in a product fraction, and the mole fraction of uranium-235 in the auxiliary heavy fraction is approximately equal to the mole fraction of the uranium isotope in one of the product fractions, the waste fraction or natural-abundance uranium. A stream of a product fraction is withdrawn at least in part from the auxiliary light-fraction stream; the stream of the waste fraction is withdrawn from the heavy-fraction streams produced by the first group of cascades; and streams of product fractions are withdrawn at least in part from light-fraction streams produced by the first group of cascades. The great flexibility in changing the product distributions for these embodiments is achieved without incurring significant mixing losses, since streams from which the product- and waste fractions streams are withdrawn are respectively enriched and depleted in uranium-235 to approximately the

mole fractions of the corresponding product and waste fractions. It will be recognized that other embodiments of the concept of the present invention may be preferred for other applications, particularly for applications involving nuclear isotopes other than uranium-235 and uranium-238. For uranium or other isotopes, it may be advantageous in certain applications to provide flexibility with respect to the enrichment of the waste fractions by supplying an auxiliary cascade with a heavy gaseous mixture fraction instead of a light gaseous mixture fraction.

Figure 10 illustrates an eighth isotope-enrichment unit 900 suitable for both substantially continuous operation and batch operation which includes first, second, and third subunits 910, 920, and 930 which can respectively enrich uranium hexafluoride by the same factors as the corresponding subunits of the fourth isotope-enrichment unit 500 described above. For conciseness the reference numerals of the three subunits will not be enumerated.

A fifth swinging auxiliary cascade 952 has an input 954, a heavy-fraction output 956, and a light-fraction output 958. The heavy-fraction output 956 of the swinging auxiliary cascade 952 and light-fraction output 918 of cascades 912 of the first subunit 910 are reciprocal outputs. To maximize the increase in the average concentration of the light isotope in the product fractions, the auxiliary cascade 952 includes only one enriching stage.

A first product-fraction discharge line 944 is connected to a condenser 980 for condensing the gaseous product fraction into a pressure tank 984 in a solid or liquid state. The pressure tank 984 is detachably connected to the condenser 980 through a conduit 982. Compressor-refrigerators for condensing gaseous uranium hexafluoride into pressure tanks in a solid state are in standard use in gaseous diffusion plants and are preferred condensers 980 for this embodiment. The input 954 of the fifth swinging auxiliary cascade 952 is connected through a conduit 960 to a gasifier 981 to which the pressure tank 984 can be detachably connected through a conduit 983. The gasifier 981 respectively sublimates or evaporates the solid or liquid product fraction contained in the pressure tank 984. In the case of uranium hexafluoride, the gasifier 981 is preferably a heater such as is in standard use in gaseous diffusion plants for subliming solid uranium hexafluoride from storage tanks. By first condensing product fraction from the first subunit into the pressure tank 984 with the condenser 980, transporting the tank 984 to the gasifier 981, and gasifying the contents of the tank 984 with the gasifier 981 and discharging the gasified contents into the input 954 of the fifth swinging auxiliary cascade 952, product fraction from the first subunit 910 can be conveyed from the first subunit 910 to the input 954 of the auxiliary cascade 952 and directed into the input 954. This mode of conveying gaseous-mixture fraction from a first group of cascades to an auxiliary cascade can be employed in other embodiments of the present invention.

Example

The numerical example set forth in Table I below compares the use of the present invention to shift the product distribution of a gas-centrifuge isotope-enrichment plant for uranium reactor fuel to the conventional method of shifting the product distribution by repiping cascades. The gas centrifuges of the example have separation factors α of 1.5 and are interconnected to form one-up/one-down cascades. Distributions of product rates and of centrifuges among different types of cascades for three plants, each having a total capacity of 1,000,000 kg SWU/y, are listed in Table I.

Referring to Table I, Case 1 is a typical uranium-enrichment plant for producing three product fractions with three types of cascades: those designated A having 7 enriching stages, those designated B having 5, and those designated C having 3. All cascades have 4 stripping stages and are supplied with natural-abundance uranium hexafluoride.

In Case 2, the product distribution is shifted by converting 13.3 percent of the C cascades of Case 1 into auxiliary cascades, designated D. Four percent of the centrifuges of the plant are incorporated in the D auxiliary cascades. The D auxiliary cascades have the same number of stripping and enriching stages as the C cascades, but are supplied with light fraction produced by the B cascades instead of natural-abundance uranium hexafluoride. The heavy-fraction outputs of the D auxiliary cascades and the light-fraction outputs of the B cascades are reciprocal outputs and thus the mole percent of $^{235}\text{UF}_6$ in the heavy fraction produced by the D auxiliary cascades approximately equals 0.711, the value for natural-abundance uranium. For Case 2, the heavy fraction produced by the D auxiliary cascades is combined with the natural-abundance uranium hexafluoride feedstock and recycled to the inputs of the A, B, and C cascades.

Case 3 has the same product distribution as Case 2, but the shift in product distribution is achieved by repiping a number of the B and C cascades into cascades having 8 enriching stages and 4 stripping stages, designated in Table I as E cascades. Note that to achieve the same product distribution as Case 2, cascades including 26.5 percent of the centrifuges of the plant had to be repiped, a substantial undertaking. This shift in product distribution is

conveniently accomplished with the present invention by simply swinging valves to convert C cascades incorporating only 4 percent of the centrifuges of the plant into D auxiliary cascades. For example, more than one auxiliary cascade may be supplied with gaseous-mixture feed by a group of cascades. Swinging auxiliary cascades may be swung among
5 three or more alternative modes of operation. Gaseous mixtures of isotopes other than 5
uranium-235 and uranium-238 can be separated by the present invention.

TABLE I

Cascade signation	Number of Stages	Mole Percent $^{235}\text{UF}_6$		Case 1 Original Product Distribution		Case 2 Prod. Dist. Shifted With Auxiliary Cascades		Case 3 Prod. Dist. Shifted by Conventional Repiping	
		(a) (b) (c)	Light Fraction Feed Heavy Fraction	Product Rate (kg/y)	Fraction of Centrifuges (percent)	Product Rate (kg/y)	Fraction of Centrifuges (percent)	Product Rate (kg/y)	Fraction of Centrifuges (percent)
A	7/4	(a) 2.874 (b) 0.711 (c) 0.259		71642	25.0	71642	25.0	71642	25.0
B	5/4	(a) 1.935 (b) 0.711 (c) 0.259		256057	45.0	128028	45.0	128028	22.5
C	3/4	(a) 1.298 (b) 0.711 (c) 0.259		417542	30.0	361875	26.0	361875	26.0
D	3/4	(a) 3.497 (b) 1.935 (c) 0.711		0	0.0	56243	4.0	0	0.0
E	8/4	(a) 3.497 (b) 0.711 (c) 0.259		0	0.0	0	0.0	56243	26.5

WHAT WE CLAIM IS:

1. A method of separating a gaseous-mixture feedstock comprising a compound of a light nuclear isotope at a predetermined concentration and a compound of a heavy nuclear isotope at a predetermined concentration into at least two unit-output fractions including at least one waste fraction depleted in the light isotope to a predetermined concentration and at least one product fraction enriched in the light isotope to a predetermined concentration, comprising the steps of:
 - (a) directing gaseous-mixture feedstock into each cascade input of a principal group of cascades of gas centrifuges to introduce the gaseous-mixture feedstock into the cascades;
 - (b) centrifugally processing the gaseous-mixture feedstock introduced into each cascade of the principal group with a plurality of enriching stages and a plurality of stripping stages of the cascade to separate it into light and heavy gaseous-mixture fractions;
 - (c) conveying a first gaseous-mixture fraction produced by the principal group of cascades from the gaseous-mixture feedstock to an input of an auxiliary cascade of gas centrifuges and directing it into the input to introduce the fraction into the auxiliary cascade;
 - (d) centrifugally processing the first gaseous-mixture fraction with the auxiliary cascade to separate it into an auxiliary light fraction and an auxiliary heavy fraction, the mole fraction of the light isotope in the auxiliary light fraction being approximately equal to the mole fraction of light isotope in one of a product fraction, a waste fraction, and the gaseous-mixture feedstock, and the mole fraction of the light isotope in the auxiliary heavy fraction being approximately equal to the mole fraction of light isotope in one of a product fraction, a waste fraction, and the gaseous mixture feedstock;
 - (e) withdrawing at least a portion of a unit output fraction from one of the auxiliary light fraction and the auxiliary heavy fraction;
 - (f) withdrawing at least a portion of a waste fraction from at least one of a heavy fraction produced by the principal group of cascades, the auxiliary light fraction, and the auxiliary heavy fraction, such gaseous mixture fraction from which the portion of waste fraction is withdrawn being completed in the light isotope to approximately the mole fraction of the said waste fraction; and
 - (g) withdrawing at least a portion of a product fraction from at least one of a light fraction produced by the principal group of cascades, the auxiliary light fraction, and the auxiliary heavy fraction, such gaseous-mixture fraction from which the portion of product fraction is withdrawn being enriched in the light isotope to approximately the mole fraction of said product fraction.
2. A method according to claim 1 in which:
 - (c.1) said first gaseous-mixture fraction is a light fraction;
 - (d.1) the mole fraction of the light isotope in the auxiliary light fraction is approximately equal to the mole fraction of light isotope in a product fraction, and the mole fraction of the light isotope in the auxiliary heavy fraction is approximately equal to the mole fraction of light isotope in one of a product fraction and the gaseous-mixture feedstock;
 - (e.1) said unit-output fraction at least a portion of which is withdrawn from one of the auxiliary light and heavy fractions is a product fraction; and
 - (f.1) said portion of a waste fraction is withdrawn from a heavy fraction produced by the principal group of cascades.
3. A method according to claim 1 or claim 2 in which the gaseous-mixture feedstock is natural-abundance uranium hexafluoride and the product and waste fractions are respectively enriched and depleted in uranium-235.
4. A method according to claim 3 in which the mole fraction of the light isotope in the auxiliary heavy fraction approximately equals the mole fraction of light isotope in a second light fraction produced by the principal group of cascades.
5. A method according to claim 4 further comprising the step of combining the auxiliary heavy fraction with the second light fraction.
6. A method according to claim 4 or claim 5 in which the mole fraction of the light isotope in the auxiliary light fraction approximately equals the mole fraction of the light isotope in a third light fraction produced by the principal group of cascades.
7. A method according to claim 6 further comprising the step of combining the auxiliary light fraction with the third light fraction.
8. A method according to claim 3 in which the mole fraction of the light isotope in the auxiliary heavy fraction approximately equals the mole fraction of light isotope in the gaseous-mixture feedstock.
9. A method according to claim 8 further comprising the step of combining the auxiliary heavy-fraction with the gaseous-mixture feedstock.
10. A method according to claim 8 or claim 9 in which the mole fraction of the light

isotope in the auxiliary light fraction is approximately equal to the mole fraction of the light isotope in a second light fraction produced by the principal group of cascades.

11. A method according to claim 10 further comprising the step of combining the auxiliary light fraction with the second light fraction.

12. A method according to claim 3 in which the mole fraction of the light isotope in the auxiliary light fraction is no greater than approximately the mole fraction of the light isotope in the light fraction produced by the principal group of cascades having the greatest mole fraction of light isotope and the mole fraction of the light isotope in the auxiliary heavy fraction is no lower than approximately the mole fraction of the light isotope in the heavy fraction produced by the principal group of cascades having the least mole fraction of light isotope.

13. A method according to any one of claims 1 to 12 in which the step of conveying a first gaseous-mixture fraction produced by the principal group of cascades to an input of an auxiliary cascade includes the steps of:

(c.1) collecting a quantity of the first gaseous-mixture fraction in a container; and
(c.2) discharging the first gaseous-mixture fraction from the container into said input of the auxiliary cascade.

14. A method according to claim 13 in which the step of collecting the first gaseous-mixture fraction includes condensing the first gaseous-mixture fraction in the container in a solid or liquid state, and the step of discharging the first gaseous-mixture fraction includes gasifying the solid or liquid fraction in the container.

15. A method according to any one of claims 1 to 12 in which the step of conveying a first gaseous-mixture fraction produced by the principal group of cascades to an input of an auxiliary cascade includes the step of substantially continuously directing a first stream of gaseous-mixture fraction produced by the principal group of cascades into said input of the auxiliary cascade.

16. An isotope-enrichment unit for separating a gaseous-mixture feedstock comprising a compound of a light nuclear isotope at a predetermined concentration and a compound of a heavy nuclear isotope at a predetermined concentration into at least two unit-output fractions including at least one waste fraction depleted in the light isotope to a predetermined concentration and at least one product fraction enriched in the light isotope to a predetermined concentration, comprising:

(a) a principal group of cascades of gas centrifuges, each cascade having a plurality of enriching stages, a plurality of stripping stages, an input, a light-fraction output, and a heavy-fraction output for separating the gaseous-mixture feedstock into light and heavy gaseous-mixture fractions;

(b) a feedstock inlet system connected to each input of the principal group of cascades for introducing the gaseous-mixture feedstock into each input;

(c) a product-fraction collection system connected to at least one light-fraction output of the principal group of cascades for withdrawing at least a portion of one or more product fractions from the principal group of cascades;

(d) a waste-fraction collection system connected to at least one heavy-fraction output of the principal group of cascades for withdrawing at least a portion of one or more waste fractions from the principal group of cascades;

(e) an auxiliary cascade having an input, a light-fraction output, and a heavy-fraction output;

(f) a first conduit connected between outputs of one or more first cascades included in the principal group and the input of the auxiliary cascade for directing at least a portion of a gaseous-mixture fraction produced by the principal group of cascades into the auxiliary cascade for further separation into a light fraction and a heavy fraction; and

(g) an auxiliary collection system connected to an output of the auxiliary cascade for withdrawing at least a portion of a unit-output fraction from the auxiliary cascade.

17. An isotope-enrichment unit according to claim 16 in which the auxiliary cascade is a single-stage cascade.

18. An isotope-enrichment unit according to claim 16 or claim 17 in which said one or more outputs of the first cascades are light-fraction outputs, the first conduit thereby directing at least a portion of a light fraction produced by the principal group of cascades to the auxiliary cascade for further separation into a light fraction and a heavy fraction.

19. An isotope-enrichment unit according to any one of claims 16 to 18 in which each of said outputs of the first cascades and the heavy-fraction output of the auxiliary cascade are reciprocal outputs.

20. An isotope-enrichment unit according to any one of claims 16 to 19 in which the auxiliary cascade has a number of stripping stages equal to the number of enriching stages of each of the first cascades minus one.

21. An isotope-enrichment unit according to any one of claims 16 to 20 in which the

auxiliary collection system comprises a second conduit connected between the light-fraction output of the auxiliary cascade and the product-fraction collection system of the principal group of cascades for combining the light fraction produced by the auxiliary cascade with a product fraction from the principal group of cascades.

5 22. An isotope-enrichment unit according to claim 21 in which each of said outputs of the first cascades and the heavy-fraction output of the auxiliary cascade are reciprocal outputs and which further comprises a third conduit connected between the heavy-fraction output of the auxiliary cascade and the feedstock inlet system of the principal group of cascades for combining the heavy fraction produced by the auxiliary cascade with the
10 gaseous-mixture feedstock.

23. An isotope-enrichment unit according to claim 22 in which the auxiliary cascade has five stripping stages and each of the first cascades has six enriching stages.

24. An isotope-enrichment unit according to claim 22 further comprising first, second, and third flow regulators connected respectively in series with the first, second, and third
15 conduits for controlling the flow of gaseous mixtures in the three conduits.

25. An isotope-enrichment according to any one of claims 16 to 24 further comprising:

(h) a first valve assembly for selectively permitting fluid flow between a trunk port and one of a principal branch port and an alternate branch port, the trunk port and the principal branch port being connected in series with the first conduit, with the trunk port being in
20 closer communication with the input of the auxiliary cascade than the branch parts; and

(i) a first alternate conduit connected between the alternate branch port of the first valve assembly and an alternate source of a gaseous-mixture fraction.

26. An isotope-enrichment unit according to claim 25 in which said one or more outputs of the first cascades to which the first conduit is connected are light-fraction outputs and the
25 alternate source of a gaseous-mixture fraction includes one or more light-fraction outputs of second cascades included in the principal group of cascades, the number of enriching stages of the second cascades differing from the number of enriching stages of the first cascades.

27. An isotope-enrichment unit according to claim 25 or claim 26 in which:
the auxiliary cascade is a single-stage cascade;

30 the product-fraction collection system of the principal group of cascades comprises a first, a second, a third, and a fourth product-fraction discharge line, each discharge line being connected to one or more light-fraction outputs of cascades included in the principal group of cascades thereby defining a sub-group of one or more cascades, the four subgroups of cascades being made up of cascades having different numbers of enriching stages; and
35 the auxiliary collection system comprises:

(g.1) a second conduit connected between the heavy-fraction output of the auxiliary cascade and the first product-fraction discharge line;

(g.2) a second valve assembly for selectively permitting fluid flow between a trunk port and one of a principal branch port and an alternate branch port, the trunk port and the
40 principal branch port being connected in series with the second conduit, with the trunk port being in closer communication with the output of the auxiliary cascade than the branch ports;

(g.3) a second alternate conduit connected between the alternate branch port of the second valve assembly and the second product-fraction discharge line;

(g.4) a third conduit connected between the light-fraction output of the auxiliary
45 cascade and the third product-fraction discharge line;

(g.5) a third valve assembly for selectively permitting fluid flow between a trunk port and one of a principal branch port and an alternate branch port, the trunk port and the
50 principal branch port being connected in series with the third conduit, with the trunk port being in closer communication with the output of the auxiliary cascade than the branch ports; and

(g.6) a third alternate conduit connected between the alternate branch port of the third valve assembly and the fourth product-fraction discharge line.

28. An isotope-enrichment unit according to claim 27 in which the first, second, and
55 third valve assembly each comprises a three-port, two-way valve.

29. An isotope-enrichment unit according to claim 27 in which the first, second, and third valve assembly each comprises a "T"-joint conduit with an on-off valve in each arm of the "T".

30. An isotope-enrichment unit according to claim 25 in which each of said outputs of the first cascades to which the first conduit is connected in a light-fraction output and the
60 alternate source of a gaseous-mixture fraction is the feedstock inlet system.

31. An isotope-enrichment unit according to claim 30 in which:

each of said outputs of the first cascades and the heavy-fraction output of the auxiliary cascade are reciprocal outputs; and
65 the auxiliary collection system comprises:

(g.1) a second conduit connected between the heavy-fraction output of the auxiliary cascade and the feedstock inlet system;

5 (g.2) a second valve assembly for selectively permitting fluid flow between a trunk port and one of a principal branch port and an alternate branch port, the trunk port and the principal branch port being connected in series with the second conduit, with the trunk port being in closer communication with the output of the auxiliary cascade than the branch ports; and 5

10 (g.3) a second alternate conduit connected between the alternate branch port of the second valve assembly and the waste-fraction collection system of the principal group of cascades. 10

32. An isotope-enrichment unit according to claim 31 in which:

15 the product-fraction collection system of the principal group of cascades comprises a first and a second product-fraction discharge line, each discharge line being connected to one or more light-fraction outputs of cascades included in the principal group of cascades thereby defining a subgroup of one or more cascades, the two subgroups of cascades being made up 15 of cascades having different numbers of enriching stages; and

the auxiliary collection system further comprises:

20 (g.4) a third conduit connected between the light-fraction output of the auxiliary cascade and the first product-fraction discharge line; 20

(g.5) a third valve assembly for selectively permitting fluid flow between a trunk port and one of a principal branch port and an alternate branch port, the trunk port and the principal branch port being connected in series with the third conduit, with the trunk port being in closer communication with the output of the auxiliary cascade than the branch ports; and

25 (g.6) a third alternate conduit connected between the alternate branch of the third valve assembly and the second product-fraction discharge line. 25

33. An isotope-enrichment unit for separating a gaseous-mixture feedstock comprising a compound of a light nuclear isotope at a predetermined concentration and a compound of a heavy nuclear isotope at a predetermined concentration into at least two unit-output 30 fractions including at least one waste fraction depleted in the light isotope to a predetermined concentration and at least one product fraction enriched in the light isotope to a predetermined concentration, comprising: 30

35 (a) a principal group of cascades of gas centrifuges, each cascade having a plurality of enriching stages, a plurality of stripping stages, an input, a light-fraction output, and a heavy-fraction output for separating the gaseous-mixture feedstock into light and heavy gaseous-mixture fractions; 35

(b) a feedstock inlet system connected to each input of the principal group of cascades for introducing the gaseous-mixture feedstock into each input;

40 (c) a product-fraction collection system connected to at least one light-fraction output of the principal group of cascades for withdrawing at least a portion of a product fraction from the principal group of cascades; 40

(d) a waste-fraction collection system connected to at least one heavy-fraction output of the principal group of cascades for withdrawing at least a portion of a waste fraction from the principal group of cascades;

45 (e) an auxiliary cascade having an input, a light-fraction output, and a heavy-fraction output, the heavy-fraction output being a reciprocal output to a light-fraction output of one or more first cascades in the principal group; 45

50 (f) an isotope-mixture conveyance system for conveying the light isotope-mixture fraction from said outputs of the first cascades to the input of the auxiliary cascade and directing it into the input so that at least a portion of a light isotope-mixture fraction produced by the principal group of cascades can be further separated into a light fraction and a heavy fraction by the auxiliary cascade; 50

55 (g) an auxiliary product-fraction collection system connected to the light-fraction output of the auxiliary cascade for withdrawing at least a portion of a product fraction from the auxiliary cascade; and 55

(h) a feedstock collection system connected to the heavy-fraction output of the auxiliary cascade for withdrawing gaseous-mixture feedstock from the auxiliary cascade.

34. An isotope-enrichment unit according to claim 33 in which the isotope-mixture conveyance system includes:

60 (f.1) a tank detachably connectable to a discharge line in communication with said outputs of the first cascades for receiving the light isotope-mixture fraction from the first cascades and to the input of the auxiliary cascade for discharging gaseous-mixture fraction into the auxiliary cascade. 60

35. An isotope-enrichment unit according to claim 34 in which the isotope-mixture conveyance system further includes: 65

(f.2) a condenser for condensing the gaseous light fraction into the tank in a solid or liquid state; and

(f.3) a gasifier for respectively subliming or evaporating solid or liquid contents of the tank into the input of the auxiliary cascade.

5 36. An isotope-enrichment unit according to any one of claims 33 to 35 in which the isotope-mixture conveyance system includes a first conduit connected between said outputs of the first cascades and the input of the auxiliary cascade. 5

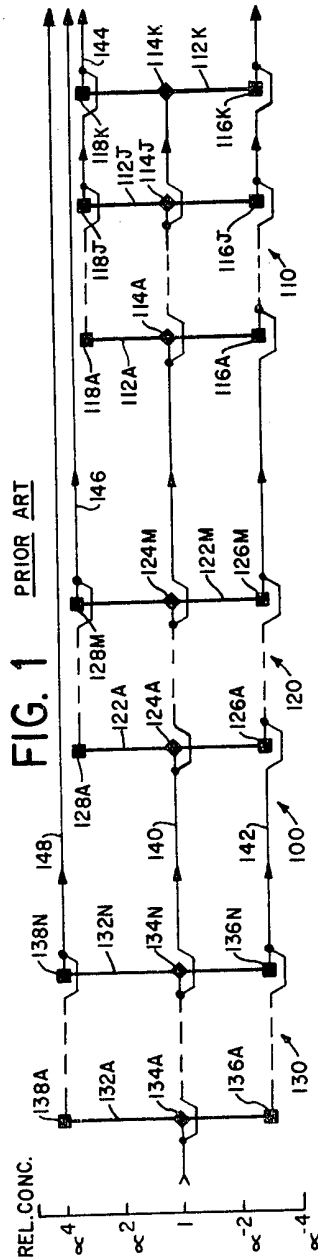
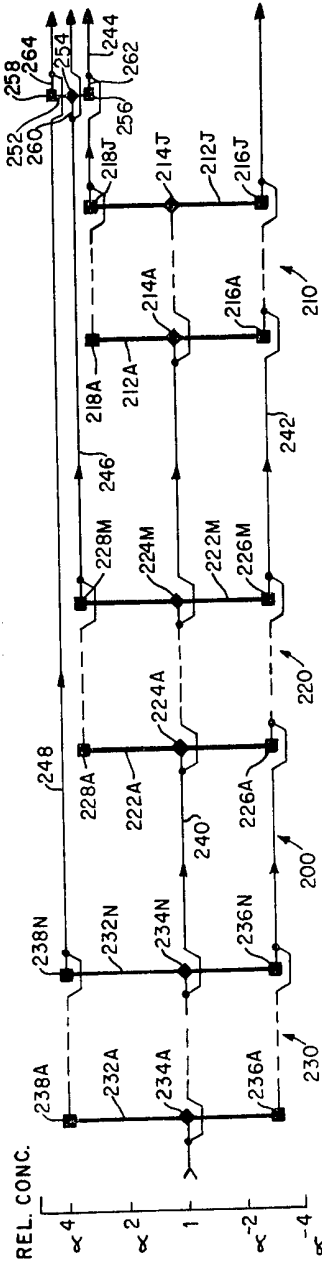
10 37. An isotope-enrichment unit according to claim 36 in which the auxiliary product-fraction collection system includes a second conduit connected between the light-fraction output of an auxiliary cascade and the product-fraction collection system of the principal group of cascades for combining the light fraction produced by the auxiliary cascade with a product fraction from the principal group of cascades. 10

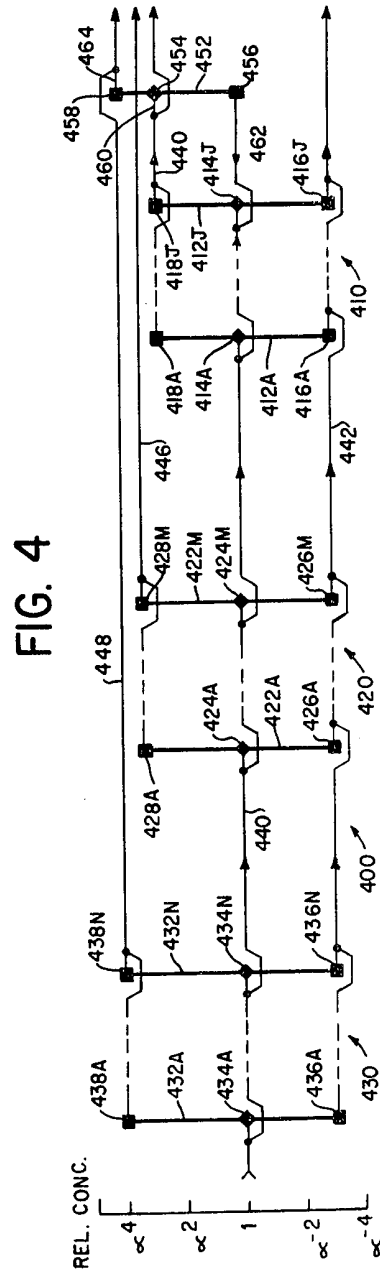
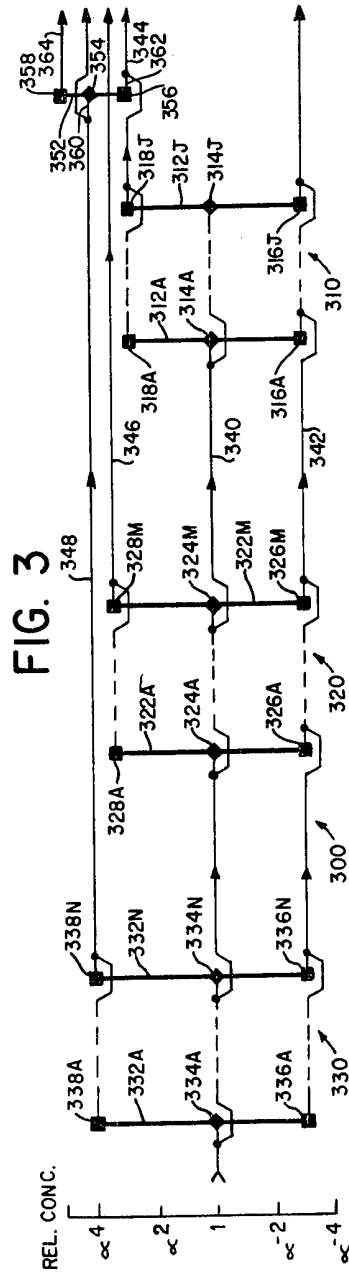
15 38. An isotope-enrichment unit according to any one of claims 33 to 37 in which the feedstock collection system includes a third conduit connected between the heavy-fraction output of the auxiliary cascade and the feedstock inlet system of the principal group of cascades for combining the heavy fraction produced by the auxiliary cascade with the gaseous-mixture feedstock supplied to the principal group of cascade. 15

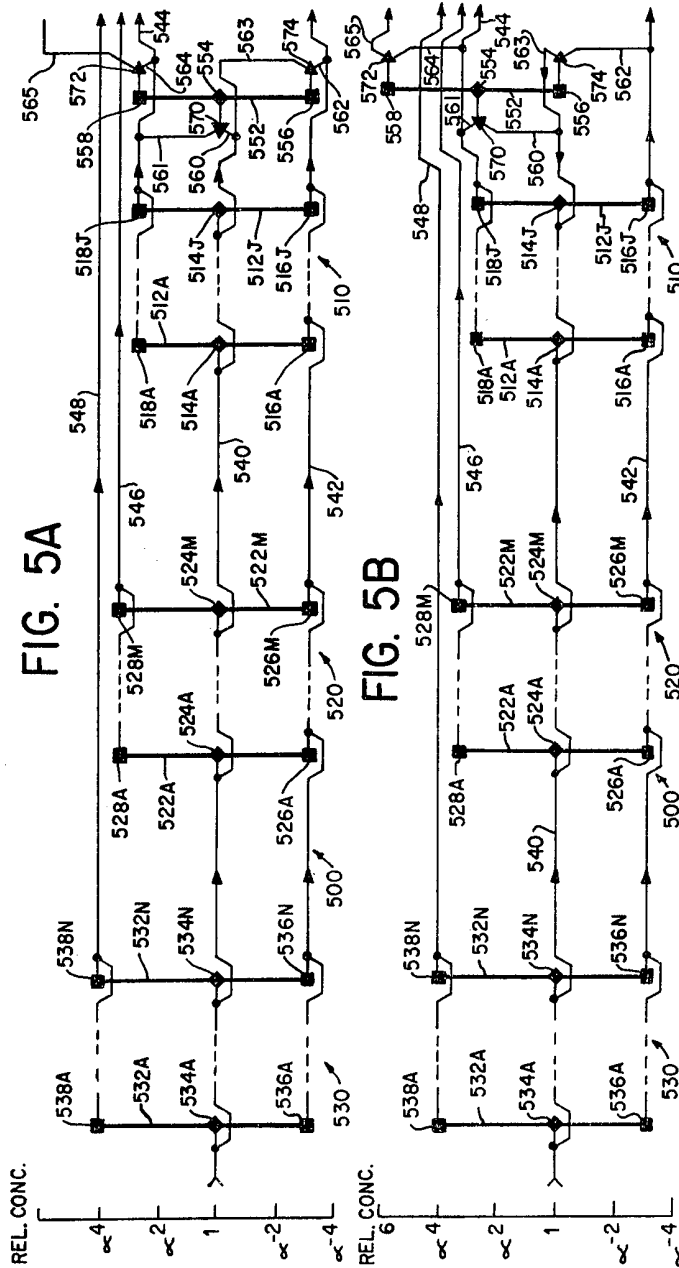
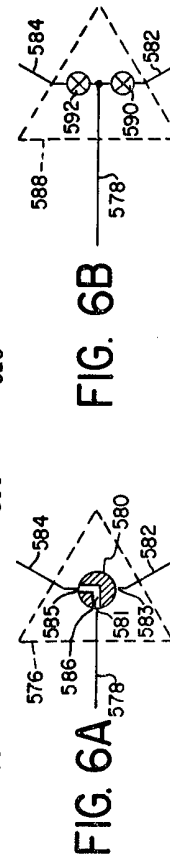
20 39. A method of separating a gaseous-mixture feedstock comprising a compound of a light nuclear isotope at a predetermined concentration and a compound of a heavy nuclear isotope at a predetermined concentration into at least two unit-output fractions including at least one waste fraction depleted in the light isotope to a predetermined concentration and at least one product fraction enriched in the light isotope to a predetermined concentration, according to claim 1 substantially as herein described, with reference to and as illustrated in Figure 2, Figure 3, Figure 4, Figures 5A, 5B and 6A, Figures 5A, 5B and 6B, Figure 7, Figure 8, Figure 9 or Figure 10 of the accompanying drawings. 20

25 40. An isotope-enrichment unit for separating a gaseous-mixture feedstock comprising a compound of a light nuclear isotope at a predetermined concentration and a compound of a heavy nuclear isotope at a predetermined concentration into at least two unit-output fractions including at least one waste fraction depleted in the light isotope to a predetermined concentration and at least one product fraction enriched in the light isotope to a predetermined concentration substantially as hereinbefore with reference to and as illustrated in Figure 2, Figure 3, Figure 4, Figures 5A, 5B and 6A, Figures 5A, 5B and 6B, Figure 7, Figure 8, Figure 9 or Figure 10 of the accompanying drawings. 25

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**FIG. 2**



**FIG. 5B****FIG. 6B**

