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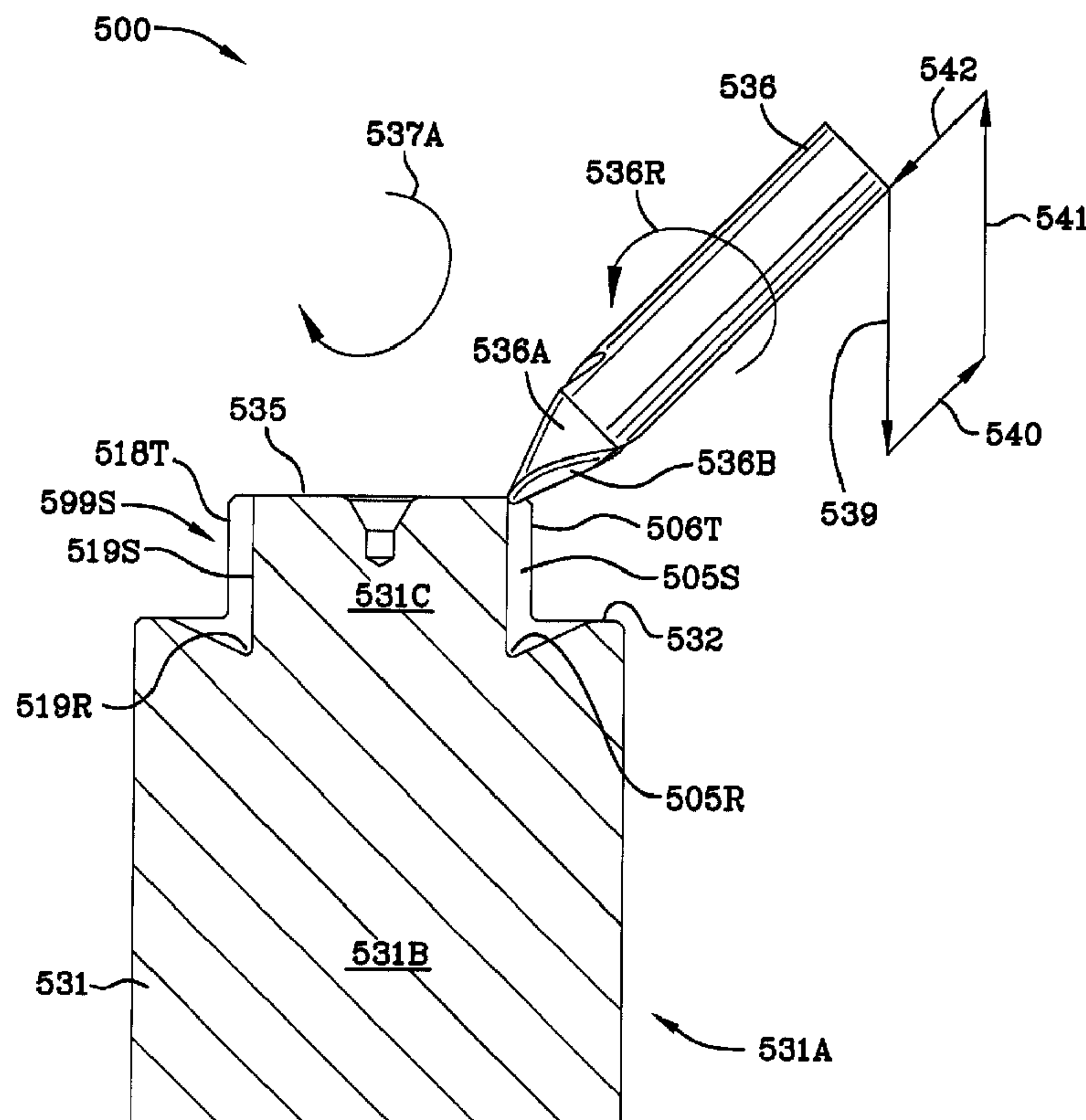
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(54) Title: SMILLED SPLINE APPARATUS AND SMILLING PROCESS FOR MANUFACTURING THE SMILLED SPLINE
APPARATUS



(57) Abrégé/Abstract:

By combining shaping and milling actions, or smilling, the cutting tool can move through the entire usable portion of the spline and machine a tool relief into the face of the adjacent feature such as a shoulder before retracting, reversing direction, and repeating



(57) **Abrégé(suite)/Abstract(continued):**

the cycle. The smilling apparatus and manufacturing method eliminates the need for an annular spline relief and the full length of spline engagement can be utilized for strength. The effective width of the spline connection apparatus manufactured by the smilling process conserves space and increases the load carrying capability of the spline connection.

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Abstract

By combining shaping and milling actions, or smilling, the cutting tool can move through the entire usable portion of the spline and machine a tool relief into the face of the adjacent feature such as a shoulder before retracting, reversing direction, and repeating the cycle. The smilling apparatus and manufacturing method eliminates the need for an annular spline relief and the full length of spline engagement can be utilized for strength. The effective width of the spline connection apparatus manufactured by the smilling process conserves space and increases the load carrying capability of the spline connection.

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5 **SMILLED SPLINE APPARATUS AND SMILLING PROCESS FOR
 MANUFACTURING THE SMILLED SPLINE APPARATUS**

Field of the Invention

10 The invention is in the field of splines having adjacent features such as shoulders and counterbore surfaces in proximity to splines.

Background of the Invention

15 A mechanical spline is commonly used to couple a shaft and collar to transmit rotational motion and torque. If no adjacent feature such as a shoulder on the shaft or a counter bore on the collar exists, the full length of spline is engaged and can be utilized for strength and traditional manufacturing methods can be used to produce each component. However, if one or both members have adjacent features, a spline relief is required to allow for tool clearance. The length (or width) of the annular relief(s) reduce(s) the full length of spline engagement which reduces the strength of the connection proportionally. Common prior art methods of machining splines close to adjacent features include shaping and milling. Shaping involves a fixed cutting tool parallel to the spline axis, moving through the usable portion of the spline, into the annularly shaped relived area, and stopping short of the adjacent feature before retracting, reversing direction, and repeating the cycle. Milling involves a rotating cutting tool normal to the spline axis, moving through the usable portion of the spline, into the annularly shaped relived area, and stopping short of the adjacent feature before retracting, reversing direction, and repeating the cycle.

25 Fig. 1 is a cross-sectional diagrammatic view 100 taken along the lines 1-1 of Fig. 1A of the prior art external spline illustrating the workpiece 101A having a base 101, shoulder 102, cylindrical external spline portion 199, and annular tool relief 103 together with a traditional cutter-shaper 106 and its operating path 108. The cylindrical external spline includes a plurality of teeth 104. Reference numeral 105 indicates the top end portion of the spline.

30 Still referring to Fig. 1, the cutter-shaper tool 106 includes a plurality of cutter-shaper tool blades 107 which cut the workpiece 101A, or more particularly, which cut the cylindrical spline portion 199. Cutter motion 108 includes a downward stroke 109 of cutter-shaper 106, then a lateral or transverse stroke 110 removing the cutter-shaper tool 106 from the spline (workpiece),

5 then a longitudinal or upward stroke 111 of the cutter-shaper tool, and finally a repositioning stroke 112 moving the cutter-shaper tool 106 in alignment for another cut. Several or multiple passes of the cutter-shaper tool are made to produce a finished part. The workpiece 101A is simultaneously rotated with the cutter shaper tool 106.

10 Fig. 1A is a perspective view 100A of Fig. 1 and illustrates the annular cutter-shaper tool relief 103 extending circumferentially around the upper cylindrical portion bearing the external spline and underneath the external spline teeth. Referring to Fig. 1A, tooth 121, side of tooth 122 and tooth fillet 123 are illustrated. Fig. 1B is an elevation view 100B of prior art Fig. 1A. Fig. 1C is a top view 100C of prior art Fig. 1A illustrating the same components described above. .

15 Fig. 2 is a perspective view 200 illustrating the base 201, counterbore engagement surface 206, cylindrical internal spline portion (tooth 205, tooth space 204), and shaper-cutter tool relief 203 of the female connection member (collar member) 201A. Reference numeral 202 is used to denote the top of the female connection member 201A. Reference numeral 220A denotes the internal spline. Not shown is the prior art cutter-shaper tool which makes the female collar connection.

20 Fig. 2A is a cross-sectional view 200A of prior art taken along the lines 2A-2A of Fig. 2. Inner circumferential shaper-cutter tool annular tool relief 203 is illustrated well in Fig. 2A as is counterbore engagement surface 206. Representative tooth 205 and representative tooth space 204 are illustrated well in Figs. 2A and 2B. Fig. 2B is a top view 200B of Fig. 2.

25 Fig. 3 is a cross-sectional schematic view 300 of a prior art internal spline 220A and a prior art external spline 199 coupled together illustrating the effective face width, EF, annular cutter-shaper tool reliefs 103, 203 and the total length of the spline connection, SC. EF, the effective face width, of the prior art spline connection is relatively short and thus the length limits the load. By relatively short, it is meant that the effective face width, EF, is just a portion of the spline connection length. The EF of the prior art spline connections may be only 50% of the length of the spline connections. As illustrated in Fig. 3, the manufactured face width, FW, of the exterior spline 199 and the interior spline 220A, are equal.

30

In designing a spline, the load (torque) required to be transmitted by the spline connection is identified. Next, the spline size as a function of torque required determines an approximate

5 range of the necessary pitch diameter. The torque carrying capacity of a spline is a function the
pitch diameter, the shear stress and the length of the spline connection, SC. Once the pitch
diameter is specified, the design engineer then calculates the length of the spline connection
taking into account that all teeth of the inner and external spline teeth may not be in engagement.
It is important to efficiently use the spline connection and to maximize the effective face width,
10 EF in order to transmit torque efficiently. In the prior art illustrated in Figs. 1, 1A, 1B, 1C, 2, 2A,
2B, and 3, a large annular cutter-shaper relief is required between the end of the spline and an
adjacent feature to allow the cutter-shaper to fully cut and retract from the spline. The annular
cutter-shaper relief is designated as CR on Fig. 3 and the effective face width is expressed as
follows:

$$EF=SC-2CR$$

15 Therefore, it can be readily seen from Fig. 3 that length of the annular cutter-shaper tool
reliefs reduce the effective face width of the prior art spline connection. The problem with
annular cutter-shaper tool reliefs occurs whenever splines are manufactured adjacent features.
Typically, the adjacent features are shoulders and counterbores but any adjacent feature
regardless of the name applied to it will cause a problem as it will require a substantial tool relief.

20 **Summary of the Invention**

The form of the spline is defined by the shape of the tool and can be straight sided,
angular sided, involute, full curve, or other forms that may be advantageous to the design.
Smilling can be performed on both external shafts and internal collars with common machine
equipment and relatively inexpensive tooling. Smilling is a combination of the words shaping
25 and milling. The smilling process has some characteristics of shaping and some characteristics of
rotary milling, and therefore, the name given to this process is "smilling." The products
produced with the smilling process are said to have been "smilled."

By combining shaping and milling actions, or smilling, the cutting tool can move through
the entire usable portion of the spline and machine an angular relief into the face of the adjacent
30 feature before retracting, reversing direction, and repeating the cycle. The angular relief includes

5 a partially conically shaped portion. The smilling design and manufacturing method eliminates the need for an annular spline relief and the full length of spline engagement can be utilized for strength. The effective width of the spline connection apparatus manufactured by the smilling process conserves space and increases the load carrying capability of the spline connection.

10 Use of the smilling tool cutter requires just one pass to finish size each tooth space. The rotating cutter is basically standard with the shape of the end producing the form of the tooth space. The form can be straight sided (90°), angular (30° or 45°), involute (as defined by a base circle and pressure angle), full radius (similar to a sine wave), etc. The workpiece is indexed at the completion of each tooth space ($360^\circ/\text{number of teeth}$). The holding angle (inclination angle) would be up to the tool designer (45° provides a stiff angle of attack when entering the shoulder to create the angular relief). One prominent aspect is to smill just beyond the full length of spline engagement into the adjacent shoulder such that the mating parts locate shoulder-to-shoulder with maximum engagement. The relief pockets beyond the shoulder do not engage one another.

The smilling spline connection has been tested satisfactorily with 64% torque carrying capacity above the conventional shape and relief configuration.

20 A male spline connection apparatus is disclosed which comprises a base portion, a shoulder portion and a cylindrical portion. The shoulder portion resides intermediate the base portion and the cylindrical portion. The cylindrical portion includes an external spline thereon and the external spline includes a plurality of tooth spaces therein circumferentially spaced apart from each other forming a plurality of teeth between adjacent tooth spaces. The tooth spaces are formed by sides of adjacent teeth and a fillet joining the adjacent teeth. Each of the plurality of tooth spaces includes a spline relief portion for tool clearance extending angularly into the shoulder and the base portion of the male spline connection apparatus. Each of the plurality of teeth of the external spline includes sides which may be angular sides, straight sides, involute sides, full curve sides, or straight sides.

30 A female collar connection apparatus is disclosed which comprises a base portion and an upper portion. The upper portion includes a generally cylindrically shaped hub portion recessed therein. The hub portion includes an internal spline which terminates in a counterbore engagement surface. The internal spline includes a plurality of tooth spaces therein

5 circumferentially spaced apart from each other forming a plurality of teeth between adjacent
tooth spaces. The tooth spaces are formed by sides of adjacent teeth and a fillet joining the
adjacent teeth. Each of the plurality of tooth spaces includes an angularly oriented spline relief
portion for tool clearance extending angularly into the counterbore engagement surface. Each of
the plurality of teeth of the internal spline includes sides which may be angular sides, straight
10 sides, involute sides, full curve sides, or straight sides.

A spline connection apparatus is disclosed herein and comprises a male spline apparatus
and a female collar apparatus. The male spline connection apparatus includes: a base portion, a
shoulder portion and a cylindrical portion. The shoulder portion resides intermediate the base
portion and the cylindrical portion. An external spline resides on the cylindrical portion and
15 includes a plurality of first tooth spaces therein circumferentially spaced apart from each other
forming external spline teeth between adjacent first tooth spaces. Each of the plurality of first
tooth spaces are formed by sides of adjacent external spline teeth and a fillet joining the adjacent
external spline teeth. Each of the plurality of first tooth spaces includes an angular spline relief
portion for tool clearance extending angularly into the shoulder and base portion of the male
20 spline apparatus. The female collar apparatus includes: a base portion and an upper portion. A
generally cylindrically shaped hub portion is recessed in the upper portion of the female collar
apparatus. The recessed hub portion includes an inner circumference and an internal spline. The
internal spline terminates in a counterbore engagement surface. The internal spline includes a
plurality of second tooth spaces therein circumferentially spaced apart from each other forming
25 internal spline teeth between adjacent second tooth spaces. The second tooth spaces are formed
by sides of adjacent internal spline teeth and a fillet joining the adjacent internal spline teeth.
Each of the plurality of second tooth spaces includes an internal spline relief portion for tool
clearance extending angularly into the counterbore engagement surface.

Each of the plurality of external spline teeth of the external spline resides in a respective
30 one of the plurality of the second tooth spaces of the internal spline. Each of the plurality of
internal spline teeth of the internal spline resides in a respective one of the plurality of the first
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5 plurality of internal spline teeth may interengage two of the plurality of the external spline teeth
of the external spline. Each of the plurality of external spline teeth of the external spline of the
male spline apparatus has a first length and each of the plurality of the internal spline teeth of the
internal spline of the hub portion of the female collar apparatus has a second length equal to the
first length. The first and second lengths are the effective face width, EFs, of the spline
10 connection apparatus made by the smiling process. The entire length of the external spline
engages the entire second length of the internal spline to maximize the effectiveness of the torque
transfer.

The cylindrical portion of the male spline apparatus engages the counterbore engagement
surface of the generally cylindrically shaped hub portion recessed in the upper portion of the
15 female collar apparatus and the shoulder of the male spline apparatus engages the upper portion
of the female collar apparatus. As stated above, a portion of the plurality of the external spline
teeth interengages a portion of the plurality of the internal spline teeth.

Another expression of the invention includes a spline connection apparatus, comprising:
a male member and female member. The male member includes a shoulder portion and a
20 cylindrical portion. The cylindrical portion of the male member extends from the shoulder
portion to the top of the upper portion and includes an external spline thereon having a first
length. The female member includes a base portion and an upper portion. The upper portion
includes a counterbore therein having an internal spline having a second length. The internal
spline terminates in a counterbore engagement surface. The male and female members are
25 coupled together with the shoulder portion of the male member engaging the upper portion of the
female member. The upper surface of the cylindrical portion of the male member engages the
counterbore engagement surface of the female member. The first and second lengths of the
splines are equal. The external spline is completely intermeshed with the internal spline and the
effective face width of the smiled connection is equal to the first and second length of the
30 splines.

A smiling process for manufacturing an external spline is disclosed and claimed. The
process includes the step of determining the load to be carried by the external spline. The load is
determined by parameters of the application. A pitch diameter is selected for the external spline

5 based on the determined load. The number of teeth are then selected such that the circular pitch is sufficiently large and that the teeth of the external spline are sufficiently large and capable of handling the specified load. A length of the external spline is then determined based on the determined load and the selected pitch diameter of the external spline. Next, a tool inclination angle, β , is selected and a part space included angle, α , is also selected. The part space included
 10 angle is selected from a reasonable range of angles typically desired to accommodate appropriate pressure angles. A tool cone included angle, 2τ , is calculated based on an algorithm expressed in terms of β and α . Once the tool cone included angle, 2τ , is known, the length of the rotary cutting tool is determined based on the actual external spline dimensions required. The rotary cutting tool has a cutting portion which is generally conically shaped. Next, the workpiece is
 15 chucked in an appropriate workpiece in an endmill. Following the chucking, the workpiece is milled creating an appropriate external space angle (tooth space) using the smilling process with the appropriately sized tool and a 5 axis Mazak endmill. The process further includes smilling an angular tool relief in an adjacent structure of the workpiece for clearance of the tool. The relief is partially conically shaped. Typically, the workpiece is cylindrically shaped and the adjacent
 20 structure is a shoulder or a counterbore surface. To create the spline, the workpiece is rotatably indexed which enables milling of a plurality of equally spaced angles about the circumference of the workpiece forming circumferentially spaced spline teeth.

The step of sizing the tool based on the actual external spline dimensions required includes use of an algorithm expressed in terms of the inclination angle, β , and the part space
 25 included angle α , to arrive at a tool space included angle, 2τ . Once 2τ is known, a cap radius down to the form diameter establishes one end of the tool and the tool cone extends long enough out of the spline to completely smill the spline as desired. Typically, but not exclusively, the inclination angle, β , is preferably in the range of 30-60° and the part space angle, α , is preferably in the range of 40-75°. The algorithm can be performed using an Excel spreadsheet, for example,
 30 incorporating the methodology expressed herein below.

The rotary cutting tool includes a carbide conically-shaped cutting portion and the tool includes two straight flutes and a radius cap for creating an angular spline. A single flute may also be used in smilling an angular spline. If an involute spline is desired then the cutting tool

5 includes a plurality of involute radii to produce the appropriate space angle (tooth space) and involute teeth. The involute radii are determined by the desired shape of the involute tooth.

A process for manufacturing an internal spline is disclosed and claimed. The process includes the step of determining the load to be carried by the internal spline which is the same step as described above in connection with the external spline. Next, a pitch diameter of a mating
 10 external spline is selected as described above. Next, the length of the internal spline apparatus based on the determined load and the selected pitch diameter of the external spline apparatus is determined. Next, the number of teeth, N , is selected such that the circular pitch of the external spline is sufficiently large and that the teeth of the external spline are capable of handling the load. Next, an external part space included angle, $2\alpha^\circ$, is selected and an internal part space
 15 included angle is determined using the formula, $2\alpha^\circ - ((360/N)^\circ)$. A tool inclination angle, β , is selected to determine a tool cone included angle, 2τ , based on an algorithm expressed in terms of tool inclination angle β and the internal part space included angle, $2\alpha^\circ - ((360/N)^\circ)$. The rotary cutting end mill tool is then sized based on the algorithm expressed in terms of the inclination angle β and the internal part space included angle $2\alpha^\circ - ((360/N)^\circ)$, to arrive at 2τ , the tool space
 20 included angle. Once 2τ is known, a cap radius down to the form diameter establishes one end of the tool and the tool cone extends long enough out of the part to completely smill the part as desired. An appropriate workpiece is then chucked in a Mazak endmill or any other multiple axis commercially available endmill. The workpiece is then smilled using the rotary cutting carbide tool and an endmill producing an appropriate internal space angle (tooth space) in the workpiece.
 25 A rotary cutting carbide tool angularly shaped relief is then smilled in an adjacent structure of the workpiece. Typically, the appropriate workpiece includes a counterbore therein and the counterbore, in turn, has an inner circumference. To produce appropriate circumferentially spaced internal spline teeth and equally spaced appropriate internal space angles (tooth spaces), the workpiece is rotatably indexed which enables smilling a plurality of equally spaced
 30 appropriate internal space angles (tooth spaces) about the inner circumference of the counterbore of the workpiece thus forming circumferentially spaced internal spline teeth. The rotary cutting tool used is much less expensive than the shaper-cutter tools which are typically used for manufacturing splines having an annular tool relief.

5 A process for manufacturing a spline in proximity to an adjacent structure is disclosed and claimed. The workpiece includes an upper cylindrical portion and an adjacent structure, and the upper cylindrical portion includes an end portion and a length. A rotary cutting tool is oriented at an inclination angle with respect to the upper cylindrical portion of the workpiece and, of course, the rotary cutting tool is rotating to perform the desired cutting action. An end portion
10 of the upper cylindrical portion of the workpiece is engaged by the rotating rotary cutting tool. The rotary cutting tool is moved from the end portion of the upper cylindrical portion of the workpiece removing material by its cutting action along the length of the upper cylindrical portion and into the adjacent structure of the workpiece forming a rotary cutting tool relief. The rotary cutting tool relief is in the form of an angular pocket formed by the conically shaped
15 cutting tool. Tooth spaces are also formed by the cutting action of the tool. Next, the rotary cutting tool is retracted from the adjacent structure of the workpiece along the angle of inclination of the rotating rotary cutting tool. The rotary cutting tool is then returned vertically to its initial position (home) and the workpiece is positioned for the next milling operation. The workpiece is rotated, or indexed, after cutting each tooth space. The steps of: engaging the end
20 portion of the upper cylindrical portion of the workpiece with the rotating rotary cutting tool; moving the rotating rotary cutting tool from the end portion of the upper cylindrical portion of the workpiece removing material by its cutting action along the length of the upper portion and into the adjacent structure of the workpiece forming a rotary cutting tool relief; and, retracting the rotary cutting tool from the adjacent structure of the workpiece along the angle of inclination of
25 the rotating rotary cutting tool are then repeated.

In connection with this process, a step of sizing the rotary cutting tool for an external spline is based on the part space included angle and the angle of inclination. The just stated process may produce an external spline where the adjacent structure is a shoulder and the rotary cutting tool relief extends at the inclination angle into the shoulder.

30 Another process for manufacturing a spline in proximity to an adjacent structure is disclosed and claimed. The steps of the process include securing a workpiece having a counterbore therein and an adjacent structure in proximity to the counterbore. The counterbore includes an end portion and a length. In home position, the rotary cutting tool is oriented at an

5 inclination angle with respect to the end portion of the counterbore of the workpiece. The rotary cutting tool is, of course, rotated and brought into engagement with the end portion of the counterbore of the workpiece. Next, the rotating rotary cutting tool moves from the end portion of the counterbore of the workpiece removing material by its cutting action along the length of the counterbore and into the adjacent structure of the workpiece forming a rotary cutting tool relief. Following creation of the rotary cutting tool relief, the rotary cutting tool is retracted from the adjacent structure of the workpiece along the angle of inclination of the rotating rotary cutting tool.

The further steps of the process include: returning the rotary cutting tool to an initial position (home position); indexing the workpiece by rotating the workpiece after creation of each tooth space; and, repeating the steps of: engaging the end portion of the counterbore of the workpiece with the rotating rotary cutting tool; moving the rotating rotary cutting tool from the end portion of the counterbore of the workpiece removing material by its cutting action along the length of the counterbore and into the adjacent structure of the workpiece forming a rotary cutting tool relief; and, retracting the rotary cutting tool from the adjacent structure of the workpiece along the angle of inclination of the rotating rotary cutting tool.

The just stated process may produce an internal spline and the adjacent structure may be a counterbore engagement surface and the rotary cutting tool relief extends at the inclination angle into the counterbore. In connection with this process, a step of sizing the rotary cutting tool is based on the part space included angle and the angle of inclination to arrive at a tool cone included angle.

It is an object of the invention is to make the smiled spline connection length shorter than a conventional spline connection using annular reliefs for the same load carrying capacity.

It is another object of the invention is to make the smiled spline effective face width equal to the width of the spline connection.

30 It is another object of the invention to increase the load carrying capacity for a given spline connection length and a given pitch diameter.

It is a further object of the present invention to produce a smiled spline connection comprised of a male spline connection apparatus and a female spline connection apparatus

5 wherein angular reliefs or conically shaped reliefs are milled into adjacent shoulders and counterbores.

It is a further object of the present invention to produce a male spline connection apparatus or a female spline connection apparatus which may be used with a pre-existing (used) spline.

10 It is a further object of the present invention to eliminate annular reliefs in spline connections to maximize their effective face width and to make their effective face width (or length) equal to the spline connection length.

These and other objects of the invention will be best understood when reference is made to the drawing figures and description of the invention set forth below.

15 **Brief Description of the Drawings**

Fig. 1 is a cross-sectional diagrammatic view taken along the lines 1-1 of Fig. 1A of the prior art illustrating the base, shoulder, cylindrical external spline portion, and relief together with a traditional cutter-shaper and its operating path.

Fig. 1A is a perspective view of Fig. 1.

20 Fig. 1B is an elevation view of prior art Fig. 1A.

Fig. 1C is a top view of prior art Fig. 1A.

Fig. 2 is a perspective view of the prior art illustrating the base, shoulder, cylindrical internal spline portion, and relief of the female connection member (collar member).

Fig. 2A is a cross-sectional view of prior art taken along the lines 2A-2A of Fig. 2.

25 Fig. 2B is a top view of Fig. 2.

Fig. 3 is a cross-sectional schematic view of a prior art internal and external spline coupled together illustrating the effective face width, annular cutter reliefs and the total length of the spline connection.

30 Fig. 4 is a schematic of the external and internal splines of an angular spline connection apparatus manufactured using the smiling process illustrating the pitch diameter, the major and minor external diameters, the major and minor internal diameters and the circular pitch.

Fig. 4A is a schematic of the external and internal splines of an angular spline connection apparatus manufactured using the smiling process illustrating the external space angle, the

5 internal tooth angle, the internal space angle, and the external tooth angle.

Fig. 4B is a schematic of the external and internal splines of an involute spline connection apparatus manufactured using the smilling process illustrating the pitch diameter, the major and minor external diameters, the major and minor internal diameters and the circular pitch.

10 Fig. 5 is a partial cross-sectional diagrammatic view of a workpiece, taken along the lines 5-5 of Fig. 5A, being machined with an angular carbide endmill to produce an external spline with angular reliefs cut into a shoulder portion and a base portion of the workpiece.

Fig. 5A is a perspective diagrammatic view of a workpiece illustrating a finished external spline on an upper cylindrical portion, and, angular reliefs for tool clearance cut into the intermediate shoulder and base portion.

15 Fig. 5B is a top diagrammatic view of the workpiece depicted in Fig. 5.

Fig. 5C is a cross-sectional view taken along the lines 5C-5C of Fig. 5B.

Fig. 6 is a perspective schematic view of the internal spline residing in a counterbore in the workpiece, the counterbore terminating in a counterbore engagement surface.

20 Fig. 6A is a cross-sectional view taken along the lines 6A-6A of Fig. 6 illustrating the internal spline and the angular reliefs cut into the counterbore engagement surface and the upper portion of the workpiece.

Fig. 6B is a top view of the workpiece illustrated in Figs. 6 and 6A illustrating the upper surface of the top portion of the workpiece.

25 Fig. 7 is a cross-sectional schematic of the male spline apparatus and the female collar apparatus completely interengaged or coupled together.

Fig. 7A is a cross-sectional schematic of the male spline apparatus and the female collar apparatus partially interengaged or coupled together.

Fig. 7B is a cross-sectional view of the male spline apparatus and the female collar apparatus separated apart from one another.

30 Fig. 7C is a cross-sectional view taken along the lines 7C-7C of Fig. 7 illustrating the external spline of the male spline apparatus and the internal spline of the female spline apparatus in interengagement.

Fig. 7D is an enlarged portion of Fig. 7C.

5 Fig. 7E is a cross-sectional schematic view of both Fig. 7 and Fig. 3, shown in relation to each other, illustrating that the apparatus shown in Fig. 7 made by the smilling process has an effective face width EFs equal to the length of the spline connection, SC, and that the effective face width EF of the prior art in Fig. 3 is much smaller than EFs for the same length of spline connection, SC.

10 Fig. 8 is a front view of an example of the invention, namely, a male spline apparatus illustrating an external spline being smilled on a workpiece using an endmill tool oriented at an inclination angle of 45° .

Fig. 8A is a perspective view 800A of another workpiece.

Fig. 8B is a top view 800B of the workpiece of Fig. 8A.

15 Fig. 8C is a cross-sectional view 800C of Fig. 8B taken along the lines 8C-8C of Fig. 8B.

Fig. 8D is another example of the invention, namely, a workpiece similar to the workpiece illustrated in Fig. 8 and 8A, with a circumferential relief in the shoulder adjacent the external spline.

Fig. 8E is a top view of Fig. 8D.

20 Fig. 8F is a cross-sectional view taken along the lines 8F-8F of Fig. 8E.

Fig. 8G is a top view taken along the lines 8G-8G of Fig. 8 illustrating the tool smilling an external space (tooth space) into a cylindrical portion of male spline apparatus which is capable of mating with a tooth of an internal spline.

25 Fig. 9 is a schematic representation of the smilling process illustrating the smilling cutter carbide tool at an inclination angle of 45° with respect to the workpiece.

Fig. 9A is a schematic representation of the smilling cutter carbide tool at an inclination angle, β , and a part space included angle, 2α , shown as part of an elliptical projection, to determine the tool cone included angle, 2τ .

30 Fig. 9B is a view taken along the lines of 9B-9B of Fig. 9A with the elliptical projection rotated 90° counterclockwise orienting the elliptical projection of the part space included angle with the cutting profile of tool as illustrated in Fig. 9C.

Fig. 9C is an enlarged portion of Fig. 8G illustrating the carbide smilling cutter oriented in the direction of the elliptical projection of the part space included angle.

5 Fig. 9D is a schematic similar to Fig. 9A illustrating material not yet removed from the workpiece.

Fig. 9E is a schematic representation of the tool, tool inclination angle and part space half angle upon which the equation for the tool cone included angle is based.

10 Fig. 10 is a carrier with counterbore and internal spline therein made by the smilling process.

Fig. 10A is a top view of Fig. 10.

Fig. 11 is a front view of the involute carbide end mill cutting tool having first and second flutes.

15 Fig. 11A is an end view of the involute carbide end mill cutting tool taken in the direction of the lines 11A-11A.

Fig. 11B is an enlargement of the surfaces of the involute end mill illustrating different radii, R1, R2 and R3.

Fig. 12 is front view of an angular carbide end mill cutting tool.

Fig. 12A is an end view of the angular carbide end mill cutting tool of Fig. 12.

20 **Description of the Invention**

Fig. 4 is a schematic 400 of the external and internal splines of an angular spline connection apparatus manufactured using the smilling process illustrating the pitch diameter, D, the major internal diameter, Dri, the major external diameter, Dae, the minor internal diameter, Dai, the minor external diameter, Dre, and the circular pitch, CP. Fig. 4 also illustrates the tooth thickness, TT, of the angular external teeth and the space width, SW, of the internal spline. Dfi, form internal diameter, and Dfe, form external diameter, are illustrated on Fig. 4 as are the WD, working depth, and Cr, clearance between the external spline teeth and Dri, major internal diameter.

30 Fig. 4A is a schematic 400A of the external and internal splines of an angular spline connection apparatus manufactured using the smilling process illustrating the external space angle, SAe, the internal tooth angle, TAI, the internal space angle, SAI, and the external tooth angle, TAE. SAe is assumed to be 60° which is equal to 2α and the value for α , the part slot half angle, is used to calculate the tool cone included angle, 2τ . Once 2τ is known, a cap radius down

5 to the form diameter establishes one end of the tool and the tool cone extends long enough out of the part to make a complete part. The internal part space, SA_i , included angle $(2\alpha^\circ - ((360/N)^\circ))$ is illustrated in Fig. 4A where α is the part slot half angle and N is the number of teeth. Backlash, B , is also illustrated in Fig. 4A.

10 Fig. 4B is a schematic 400B of the external and internal splines of an involute spline connection apparatus manufactured using the smilling process illustrating the pitch diameter, D , the major internal diameter, D_{ri} , the major external diameter, D_{ae} , the minor internal diameter, D_{ai} , the minor external diameter, D_{re} , and the circular pitch, CP . Fig. 4B also illustrates the tooth thickness, TT , of the involute external teeth and the space width, SW , of the internal spline. D_{fi} , form internal diameter, and D_{fe} , form external diameter, are illustrated on Fig. 4B. The pressure angle Φ and the backlash, B , are also illustrated in Fig. 4B. In the instance of the involute example, the SA_e is assumed to be 60° which is equal to 2α , and the value for α , the part slot half angle, and the inclination angle are used to calculate the tool included angle which is then used along with other parameters to calculate the tool size for actual smilling of the splines. Once 2τ is known, a cap radius down to the form diameter establishes one end of the tool and the tool cone extends long enough out of the part to smill a complete part. The internal part space, SA_i , included angle $(2\alpha^\circ - ((360/N)^\circ))$ where α is the part slot half angle and N is the number of teeth, is used to calculate the tool included angle which is then used along with other parameters to calculate the tool size for actual smilling of the splines. Once 2τ is known, a cap radius down to the form diameter establishes one end of the tool and the tool cone extends long enough out of the part to smill a complete part. Backlash, B , and the base circle are also illustrated in Fig. 4B.

30 Fig. 11 is a front view 1100 of the involute carbide end mill cutting tool 1102 having first 1104 and second 1105 flutes. Reference numeral 1101 is used to express the length of the tool and reference numeral 1103 signifies the diameter of the shank. Fig. 11A is an end view 1100A of the involute carbide end mill cutting tool 1102 taken in the direction of the lines 11A-11A. Fig. 11B is an enlargement 1100B of the surfaces of the involute end mill illustrating different radii, R_1 , R_2 and R_3 . These radii cut and involute tooth on either an external spline or an internal spline as described herein. Reference numeral 1107 expresses an angle which is τ , the tool cone

5 included half angle.

Fig. 12 is front view 1200 of an angular carbide end mill cutting tool 1201A which is generally conically shaped. Fig. 12A is an end view 1200A of the angular carbide end mill cutting tool 1201A of Fig. 12. Shank diameter 1201 of angular carbide end mill cutting tool 1201A, length 1202 of cutting tool, and the tool cone included angle 1203 are illustrated in Fig. 12A. Cutting surface length 1204 and length 1205 of the flute surfaces are also illustrated in Fig. 12A. Reference numerals 1206, 1207 indicate the first flute and reference 1208, 1209 indicate the second flute.

Referring to Fig. 4A, for a part space included angle of $2\alpha = 60^\circ$, and an inclination angle, β , 45° , the tool cone included angle 1203 is calculated to be 41.40° using the formulas set forth below derived from Fig. 9E. Once 2τ is known, a cap radius down to the form diameter establishes one end of the tool and the tool cone extends long enough out of the part to smill a complete part.

Fig. 9 is a schematic representation 900 of the smilling process illustrating the angular smilling cutter carbide tool 536 at an inclination angle of 45° with respect to the workpiece cutting the workpiece. Reference numeral 845T is a tooth behind the cutting tool 536.

Referring to Fig. 4A and Fig. 9, reference numeral 846S represents the external space angle, SA_e , although only one tooth, 845T, is visible in Fig. 9. By combining shaping and milling actions, or smilling, the cutting tool can move through the entire usable portion of the spline and machine a cutting tool relief 846R into the face of the adjacent feature 836 before retracting 540, reversing direction 541, and repeating the cycle 542, 539, 540, 541. In this example the adjacent features 836 is a shoulder. The smilling design and manufacturing method eliminates the need for an annular spline relief located circumferentially beneath or above the spline. Using the smilling apparatus and process, the full length of the spline may be used for engagement for increased spline connection strength. The effective width of the spline connection apparatus conserves space and increases load carrying capability.

Still referring to Fig. 9, angular oriented cutting tool 536 makes only one pass downwardly as illustrated in Fig. 9. The cutting tool 536 as shown is a right hand cutter. However, any cutting orientation can be used, for instance, a left hand cutter could be used. Fig.

5 9 also illustrates D_{ae} , the external major diameter, and D_{re} , the external minor diameter.

Still referring to Fig. 9, an end portion 837 of the upper cylindrical portion of the workpiece is engaged along the path 542 by the rotating rotary cutting tool 536. The rotary cutting tool 536 is moved from the end portion 837 of the upper cylindrical portion of the workpiece along the length of the upper cylindrical portion according to the diagrammatic path 10 539 forming the space angle 846S (tooth space) and into the adjacent structure 836 (i.e., shoulder 836) of the workpiece forming a rotary cutting tool relief 846R. Next, the rotary cutting tool 536 is retracted from the adjacent structure (shoulder 836) of the workpiece along the path 540 at the angle of inclination of the rotating rotary cutting tool 536. The rotary cutting tool 536 is then returned along path 541 to its initial position and the workpiece is positioned for the next 15 smilling operation. The workpiece is rotatably indexed before the next smilling operation. The steps of: engaging along the path 542 the end portion 837 of the upper cylindrical portion of the workpiece with the rotating rotary cutting tool; moving the rotating rotary cutting tool from the end portion 837 of the upper cylindrical portion of the workpiece along the path 539 and length of the upper portion and into the adjacent structure 836 of the workpiece forming a rotary cutting 20 tool relief; and, retracting the rotary cutting tool along the path 540 from the adjacent structure of the workpiece along the angle of inclination of the rotating rotary cutting tool are then repeated. The rotary cutting tool 536 is then returned along path 541 to its initial position and the workpiece is positioned for the next smilling operation.

Fig. 9D is a schematic similar to Fig. 9A illustrating material not yet removed from the 25 workpiece. As stated previously, only one pass is required to remove the material from an external spline or an internal spline.

Fig. 9A is a schematic representation 900A of the smilling cutter carbide tool at an inclination angle, β , in an orthogonal view and a part space included angle, 2α , shown as part of an elliptical projection in a transverse view. Fig. 9B is a view 900B taken along the lines of 9B- 30 9B of Fig. 9A with the elliptical projection rotated 90° counterclockwise orienting the elliptical projection of the part space included angle with the cutting profile of the tool as illustrated in Fig. 9C. Fig. 9C is an enlarged portion 900C of Fig. 8G illustrating the carbide smilling cutter tool 536 oriented in the direction of the elliptical projection of the part space included angle, 2α .

The object of the analysis illustrated in Fig. 9E is the determination of the tool cone included angle, 2τ . Knowledge of the tool cone included angle, 2τ , allows the tool designer to make the tool with the right proportions given the inclination angle, β and the part space half angle, α . The derivation of the solution for τ , given α , the part slot half angle, and β , the inclination angle is as follows based on Fig. 9E. An equivalent derivation could be performed in regard to Figs. 9A and 9B but is not shown here. Referring to Fig. 9E, locate X, Y coordinates of point P on the tool ellipse that is tangent to part slot surface, where, W_1 =tool ellipse major semi-axis, W_2 =tool ellipse minor semi-axis, then find height A which leads to desired result, τ .

Formula of ellipse is:

$$\frac{X^2}{W_1^2} + \frac{Y^2}{W_2^2} = 1 \quad \text{equation (1)}$$

Take the first derivative of the equation for the ellipse to find the tangent line slope at any point P on the ellipse.

$$\frac{2 \cdot X}{W_1^2} \cdot \frac{dX}{dX} + \frac{2 \cdot Y}{W_2^2} \cdot \frac{dY}{dX} = 0 \quad \text{where}$$

$$\frac{dX}{dX} = 1 \quad \frac{dY}{dX} = m \quad \text{and then:}$$

$$\frac{2 \cdot X}{W_1^2} + \frac{2 \cdot mY}{W_2^2} = 0 \quad \text{solve for Y}$$

$$Y = -\frac{W_2^2 \cdot X}{W_1^2 \cdot m} \quad \text{and then substitute Y into equation (1) above and solve for X,}$$

$$X = \frac{W_1}{\sqrt{1 + \frac{W_2^2}{W_1^2 \cdot m^2}}}$$

where $W_1=1$,

$$W_2 = W_1 \cdot \cos\beta$$

$$m = \tan(90 - \alpha) = \frac{1}{\tan\alpha}$$

and by substitution:

$$X = \frac{1}{\sqrt{1 + \cos^2\beta \cdot \tan^2\alpha}}$$

and:

$$Y = \cos\beta \cdot \sqrt{1 - X^2}$$

the values for "a" and τ are obtained from the trigonometry of Fig. 9E.

$$a = \frac{X}{(\tan\alpha)} + Y$$

$$\tau = \arctan\left(\sin\frac{\beta}{a}\right)$$

Referring to Fig. 9E, once the tool cone half included angle τ is known, then, obviously 2τ is known which is the tool cone included angle. Once 2τ is known, a cap radius down to the

5 form diameter establishes one end of the tool and the tool cone extends long enough out of the part to make a complete part. The actual configuration of the spline external space angle, 2α , together with the desired specifications of the external spline must be taken into consideration.

The procedure for sizing the tool for the rotating angular carbide end mill cutting tool and for the rotating involute carbide end mill cutting tool is substantially the same with the addition
10 of determining the radii R1, R2, and R3 in connection with the involute tool. A design engineer sizes R1, R2 and R3 through a trial and error process based on the dimensions of the involute teeth.

The materials that can be utilized for making splines with the smilling process are any engineering material that can handle the intended loads, such as but not limited to alloy steels
15 8620, 8820, 4820, 4320, 4340, 4140, 9310, etc. or ductile iron grades D4512, D5506, D7003, etc., or stainless steels of the 300 series.

Fig. 5 is a partial cross-sectional diagrammatic view 500 of a workpiece 531, taken along the lines 5-5 of Fig. 5A, being machined with an angular carbide endmill 536 to produce an external spline with angular cutting tool reliefs 503R, 505R, 507R, 509R, 511R, 513R, 515R,
20 517R, 519R, 521R, 523R, 525R, 527R, 529R cut into a shoulder portion 532 and a base portion 531B of the workpiece 531.

Fig. 5A is a perspective diagrammatic view 500A of a workpiece illustrating a finished external spline with external spline teeth 504T, 506T, 508T, 510T, 512T, 514T, 516T, 518T, 520T, 522T, 524T, 526T, 528T, 530T on an upper cylindrical portion 531C, and, angular reliefs
25 503R, 505R, 507R, 509R, 511R, 513R, 515R, 517R, 519R, 521R, 523R, 525R, 527R, 529R for tool clearance cut into the intermediate shoulder 532 and base portion 531B. Also illustrated in Fig. 5A, are the external spaces (tooth spaces) 503S, 505S, 507S, 509S, 511S, 513S, 515S, 517S, 519S, 521S, 523S, 525A, 527S, 529S for mating with internal spline teeth. The cylinder top 535 engages a counterbore engagement surface 630C as described herein below when the external
30 spline apparatus 531A is coupled to the internal spline apparatus 631A as shown in Figs 7.

Referring to Figs. 5 and 5A, again, as stated above the rotary cutting tool 536 is shown at the top of the workpiece 531 where it would begin cutting. However, as shown the external space angle (tooth space) is indicated with reference numeral 505S. The tool 536 as illustrated in

5 Fig. 5 is a right hand cutting tool and the arrow 536R illustrates rotation of the tool. Cutting flutes 536A, 536B, are shown on the tool. The tool could also be a left hand cutting tool and it could use just one flute.

10 The home position of the tool is at the top of arrow 541. The tool 536 is brought into engagement with the workpiece along the path of arrow 542 at the inclination angle, β . The tool next proceeds downwardly along the path of arrow 539 cutting material from the outer circumference of the upper cylindrical portion 531C which results in the cut illustrating slot/ space angle/ tooth space 505S and the formation of external spline tooth 506T behind the cut. Other tool paths can be used to produce the identical smilling process. For instance the home position could be higher when viewing Fig. 5. The tool continues along path 539 and cuts an
15 angular relief into the shoulder 532 and the base 531B. Reference numeral 540 represents the retraction of the tool along the inclination angle, β . Reference numeral 541 represents the repositioning of the tool along the path 541 to the home position of the tool. While the tool is being moved to its home position, the workpiece 531 is rotated or indexed as indicated by arrow 537A to reposition the workpiece for the next smilling operation. Still referring to Fig. 5, slot
20 /external space angle/ tooth space 519S and external spline tooth 518T are illustrated. Reference numeral 519R illustrates an additional angular relief which has been cut into shoulder 532. Each tooth space has a respective angular relief.

Fig. 5B is a top diagrammatic view 500B of the workpiece depicted in Fig. 5 and illustrates the external spline reliefs 503R, 505R, 507R, 509R, 511R, 513R, 515R, 517R, 519R,
25 521R, 523R, 525R, 527R, 529R for tool clearance, the external spaces (tooth spaces) 503S, 505S, 507S, 509S, 511S, 513S, 515S, 517S, 519S, 521S, 523S, 525A, 527S, 529S for mating with internal spline teeth, and the external spline teeth 504T, 506T, 508T, 510T, 512T, 514T, 516T, 518T, 520T, 522T, 524T, 526T, 528T, 530T.

Fig. 5C is a cross-sectional view 500C taken along the lines 5C-5C of Fig. 5B and it is
30 this view (Fig. 5C) of the external spline that is used in Fig. 7 as discussed hereinbelow in more detail.

Referring to Figs. 5 and 5A, a male spline connection apparatus 531A is disclosed which comprises a base portion 531B, a shoulder portion 532 and a cylindrical portion 531C. The

5 shoulder portion 532 resides intermediate the base portion 531B and the cylindrical portion 531C. The cylindrical portion 531C includes an external spline 599S thereon and the external spline includes a plurality of tooth spaces 503S, 505S, 507S, 509S, 511S, 513S, 515S, 517S, 519S, 521S, 523S, 525A, 527S, 529S therein circumferentially spaced apart from each other forming a plurality of external spline teeth 504T, 506T, 508T, 510T, 512T, 514T, 516T, 518T, 10 520T, 522T, 524T, 526T, 528T, 530T between adjacent tooth spaces. The tooth spaces are formed by sides of adjacent teeth and a fillet joining the adjacent teeth. Each of the plurality of tooth spaces includes a spline relief portion for tool clearance extending angularly into the shoulder 532 and the base portion of the male spline connection apparatus. Each of the plurality of teeth of the external spline includes sides which may be angular sides, straight sides, involute 15 sides, full curve sides, or straight sides.

Fig. 6 is a perspective schematic view 600 of an internal spline manufactured by the smilling process wherein counterbore 631B resides generally in the center of the workpiece 631A. The workpiece 631A includes a base portion 631 and an upper portion 632. Sometimes, as used herein, the term female collar apparatus is used to define the structure set forth in Figs. 6, 20 6A and 6B. Circumferential counterbore 631B terminates in an adjacent structure, namely, a counterbore engagement surface 630C. Fig. 6A is a cross-sectional view 600A taken along the lines 6A-6A of Fig. 6 illustrating the internal spline 631B, the angular tool reliefs 602R, 604R, 604R, 508R, 610R, 612R, 614R, 616R, 618R, 620R, 622R, 624R, 626R, 628R cut into the counterbore engagement surface 630C and the upper portion of the workpiece 632T. Fig. 6A is 25 used in Fig. 7 as will be described hereinbelow in greater detail. Fig. 6B is a top view 600B of the workpiece illustrated in Figs. 6 and 6A depicting the upper surface 632T of the top portion of the workpiece.

Figs. 6, 6A and 6B illustrate a generally circumferential counterbore 631B in the upper portion of the workpiece 631A. A plurality of internal spaces (tooth spaces) for interengagement 30 by external spline mating teeth, 602S, 604S, 606S, 608S, 610S, 612S, 614S, 616S, 618S, 620S, 622S, 624A, 626S, 628S are illustrated in Figs. 6, 6A and 6B as being equally spaced about the inner circumference of the counterbore. The counterbore continues into the top of the workpiece 631A to a desired depth (or the depth can be expressed as a length) and terminates in a flat

5 counterbore engagement surface 630C. The counterbore engagement surface 630C is an adjacent structure in which angular tool reliefs are created using the smiling process. A plurality of internal spline teeth, 603T, 605T, 607T, 609T, 611T, 613T, 615T, 617T, 619T, 621T, 623T, 625T, 627T, angular tool reliefs 602R, 604R, 604R, 508R, 610R, 612R, 614R, 616R, 618R, 620R, 622R, 624R, 626R, 628R and the counterbore engagement surface 630C are also shown in
10 Figs. 6, 6A and 6B. Each tooth space has a respective angular tool relief associated therewith.

Referring to Figs. 6, 6A and 6B, a female collar connection apparatus 631A is disclosed which comprises a base portion 631 and an upper portion 632. The upper portion includes a generally cylindrically shaped hub portion 631B recessed therein. The hub portion includes an internal spline which terminates in a counterbore engagement surface 630C. The internal spline
15 includes a plurality of tooth spaces 602S, 604S, 606S, 608S, 610S, 612S, 614S, 616S, 618S, 620S, 622S, 624A, 626S, 628S therein circumferentially spaced apart from each other forming a plurality of teeth 603T, 605T, 607T, 609T, 611T, 613T, 615T, 617T, 619T, 621T, 623T, 625T, 627T between adjacent tooth spaces. The tooth spaces are formed by sides of adjacent teeth and a fillet joining the adjacent teeth. Each of the plurality of tooth spaces includes a spline relief
20 portion for tool clearance extending angularly into the counterbore engagement surface 630C. Each of the plurality of teeth of the internal spline includes sides which may be angular sides, straight sides, involute sides, full curve sides, or straight sides.

Fig. 7 is a cross-sectional schematic 700 of the smiled male spline apparatus 531 and the smiled female collar apparatus 631 completely interengaged or coupled together. Fig. 7 is taken
25 along the lines 7-7 of Fig. 7C. The female collar apparatus as illustrated in Fig. 6A is illustrated in Fig. 7. The male spline apparatus 531 as is illustrated in Fig. 5C is illustrated in Fig. 7 in mating engagement with the female collar apparatus 631. Still referring to Fig. 7, when the male spline and female spline apparatus are fully coupled, the top surface 535 of the cylindrical portion of the external spline interengages the counterbore engagement surface 630C. External
30 spline tooth 504T is shown in slot or internal space (tooth space) 618S of the internal spline apparatus. External spline tooth 518T is shown in slot or internal space (tooth space) 604S of the female member. Angular tool reliefs 618R, 604R are illustrated as being cut into the counterbore engagement surface 630C which resides in the upper portion 632. Top 632T of the female

5 (internal) spline apparatus (female collar apparatus) engages intermediate shoulder 532 of the male (external) spline apparatus. Angular tool reliefs of the male spline are obscured in the view of Fig. 7 because the cross-sectional cut is taken through external spline teeth 504T-518T as illustrated in Fig. 5B as being along the line 5C-5C.

10 Still referring to Fig. 7, the effective face width (smiling), EFs, is equal to the spline connection length, SC. Utilization of the entire length of external spline teeth and internal spline teeth, wherein the lengths of the external spline teeth, L_1 , and the internal spline teeth, L_2 , are the same enables considerably increased load carrying ability for a given spline connection length, and a given pitch diameter of the internal spline teeth and structure. See Fig. 7B where L_1 and L_2 are shown.

15 Still referring to Figs. 5-7, a spline connection apparatus 701 is disclosed therein and comprises a male spline apparatus 531A and a female collar apparatus 631A. The male spline connection apparatus 531A includes: a base portion 531, a shoulder portion 532 and a cylindrical portion 531C. The shoulder portion 532 resides intermediate the base portion 531B and the cylindrical portion, 531C. An external spline resides on the cylindrical portion 531C and includes
 20 a plurality of first tooth spaces 503S, 505S, 507S, 509S, 511S, 513S, 515S, 517S, 519S, 521S, 523S, 525A, 527S, 529S therein circumferentially spaced apart from each other forming external spline teeth between adjacent first tooth spaces. Each of the plurality of first tooth spaces are formed by sides of adjacent external spline teeth and a fillet joining the adjacent external spline teeth. Each of the plurality of first tooth spaces includes a spline relief portion for tool clearance
 25 extending angularly into the shoulder and base portion of the male spline apparatus. The female collar apparatus 631A includes: a base portion 631 and an upper portion 632. A generally cylindrically shaped hub portion is recessed in the upper portion 632 of the female collar apparatus. The recessed hub portion includes an inner circumference and an internal spline. The internal spline terminates in a counterbore engagement surface 630C. The internal spline includes
 30 a plurality of second tooth spaces 602S, 604S, 606S, 608S, 610S, 612S, 614S, 616S, 618S, 620S, 622S, 624A, 626S, 628S therein circumferentially spaced apart from each other forming internal spline teeth between adjacent second tooth spaces. The second tooth spaces are formed by sides of adjacent internal spline teeth and a fillet joining the adjacent internal spline teeth. Each of the

5 plurality of second tooth spaces includes an internal spline relief portion for tool clearance extending angularly into the counterbore engagement surface.

Each of the plurality of external spline teeth of the external spline resides in a respective one of the plurality of the second tooth spaces of the internal spline. Each of the plurality of internal spline teeth of the internal spline resides in a respective one of the plurality of the first
10 tooth spaces of the external spline. Each of the plurality of the external spline teeth of the external spline may interengage two of the plurality of the internal spline teeth and each of the plurality of internal spline teeth may interengage two of the plurality of the external spline teeth of the external spline.

Referring to Figs. 5A and 7, each of the plurality of external spline teeth of the external
15 spline of the male spline apparatus has a first length, L_1 , as measured from the shoulder 532 to the top surface 535 of the cylindrical portion 531C. Referring to Figs. 6A and 7B, each of the plurality of the internal spline teeth of the internal spline of the hub portion of the female collar apparatus has a second length, L_2 , as measured from the top 632T of the upper portion 632 to the counterbore engagement surface 630C. The first length, L_1 , of external spline is equal to the
20 second length, L_2 , of the internal spline. The first, L_1 , and second, L_2 , lengths are the effective face width, EFs, of the spline connection apparatus made by the milling process as shown in Fig. 7.

Referring to the cylindrical portion 535 of the male spline apparatus 531A engages the counterbore engagement surface 630C of the generally cylindrically shaped hub portion recessed
25 in the upper portion 632 of the female collar apparatus 631A and the shoulder 532 of the male spline apparatus 531A engages the top surface 632T of the upper portion 632 of the female collar apparatus 632. As stated above, a portion of the plurality of the external spline teeth interengage a portion of the plurality of the internal spline teeth. The engagement of the teeth may be full engagement or partial engagement.

30 Another example or statement of the invention refers to a spline connection apparatus which includes a male member and female member. The male member includes a shoulder portion 532 and a cylindrical portion 531C. The cylindrical portion 531C of the male member extends from the shoulder portion to the top of the upper portion and includes an external spline

5 599S thereon having a first length, L_1 . The female member includes a base portion 631 and an upper portion 632. The upper portion includes a counterbore 631 therein having an internal spline having a second length, L_2 . The internal spline terminates in a counterbore engagement surface 630C. The male and female members are coupled together with the shoulder portion of the male member engaging the upper portion of the female member. The upper surface of the
 10 cylindrical portion of the male member engages the counterbore engagement surface of the female member. The first, L_1 , and second, L_2 , lengths of the splines are equal. The external spline is completely intermeshed with the internal spline and the effective face width length, EFs of the smiled connection is equal to the first, L_1 , and second, L_2 , length of the splines.

Fig. 7A is a cross-sectional schematic 700A of the male spline apparatus 531 and the
 15 female collar apparatus 631 partially interengaged or coupled together. Fig. 7A illustrates female internal spline teeth 605T, 607T, 609T, 611T, 613T, 615T and 617T which interengage with slots/ space angles/ tooth spaces in the external spline. Tooth 504T partially engages slot or space (tooth space) 618S and tooth 518T partially engages slot or space (tooth space) 604S. Tooth spaces 604S, 606S, 608s, 610S, 612S, 614S, 616S and 618S as illustrated in Fig. 7A as
 20 well. It will be noted that external means are used to ensure that the spline is held together as, for example, when it is fully engaged as shown in Fig. 7.

Fig. 7B is a cross-sectional view 700B of the male spline apparatus 531 and the female collar apparatus 631 separated apart from one another. Fig. 7C is a cross-sectional view 700C taken along the lines 7C-7C of Fig. 7 illustrating the external spline of the male spline apparatus
 25 and the internal spline of the female spline apparatus in interengagement. All internal spline teeth, all external spline teeth, all external slots/space angles/tooth spaces, and all internal slots / space angles/ tooth spaces are shown in Fig. 7C. Fig. 7D is an enlarged portion 700D of Fig. 7C. External spline teeth 520T, 522T, 524T are illustrated in the enlarged view 700D as are internal teeth 601T, 627T, and 625T. Exterior slots or tooth spaces 521S, 523S and 525S are illustrated in
 30 Fig. 7D as are interior slots or tooth spaces 602S, 628S, and 626S.

Fig. 7E is a cross-sectional schematic view 700E of both Fig. 7 and Fig. 3, shown in relation to each other, illustrating that the apparatus shown in Fig. 7 made by the smiling process has an effective face width EFs equal to the length of the spline connection, SC, and that the

5 effective face width EF of the prior art in Fig. 3 is much smaller than EFs for the same length of spline connection, SC. As indicated in Fig. 3, the manufactured face width, FW, of the exterior spline 199 and the interior spline 220A are equal in length.

The effective face width EF of the prior art is as follows:

10
$$EF = SC - 2CR$$

and is much smaller than the effective face width (smiling), EFs, as follows:

15
$$EFs = SC$$

Fig. 7E allows a direct graphical comparison of the smiling spline connection to the prior art of Fig. 3. The smiled spline connection is much more efficient and for a given connecton length, SC, the effective width EFs of the smiled connection is much larger than the EF of the prior art.

Fig. 8 is a front view 800 of an example of the invention, namely, a male spline apparatus illustrating an external spline 899 being smiled on a workpiece using an endmill tool oriented at an inclination angle of 45°. Reference numerals 869T, 871T, 873T, 875T, 877T refer to external spline teeth of the example of Fig. 8 and reference numerals 870S, 872S, 874S, 876S, 878S refer to the space angles (or tooth spaces) for receiving teeth of the mating internal spline. Reference numeral 801 refers to the base of the workpiece, reference numeral 802 refers to the intermediate portion of the workpiece, reference numeral 803 refers to the top of cylindrical portion of the workpiece and reference numeral 804 refers to the shoulder on workpiece. Reference numeral 820 refers to the tool holder, reference numeral 821 refers to the chuck, and reference numeral 825 refers to the Mazak, 5 axis end mill. Any end mill capable of orienting the rotary cutting tool 536 at a suitable inclination angle will be suitable for performing the smiling process. Reference

5 numerals 888, 889 represent chucks holding the workpiece in place.

An additional advantage of the milling process is reduced machine set-up time as a machine such as, for example, a Mazak 5- axis endmill is able to machine all of the features of one side of the workpiece with one set-up of the machine and the workpiece does not have to be transported to other work stations around a shop. Still additionally, since all of the machining
 10 operations for a given side of the workpiece are performed by a single endmill such as the Mazak 5-axis endmill, alignment errors are virtually eliminated. In other words, if one of the external spline teeth is to be aligned with respect to another feature of the workpiece, or, a particular circumferential position of the workpiece is to be aligned with respect to another feature of the workpiece, then since there is a single chucking per side of the workpiece, misalignment errors
 15 due re-chucking (multiple set-ups) are eliminated.

Fig. 8A is a perspective view 800A of another workpiece 831, a spindle. Rim 832 includes threaded bolt holes for affixing the spindle to another structure. Recess 860 extends circumferentially around the cylindrical spindle 834. Passageway 880 passes through the spindle. Shoulder 836 is a structure adjacent the external spline 897. External spline teeth 839T, 841T,
 20 843T, 845T, space angles/ tooth spaces/ slots 847T, 840S, 842S, 844S, 846S, 848S for receiving a tooth of a mating internal spline, and tool clearance reliefs 840R, 842R, 844R, 846R, 848R are illustrated in Fig. 8A.

Fig. 8B is a top view 800B of the workpiece/ spindle 831 of Fig. 8A illustrating the features set forth in Fig. 8A. Fig. 8C is a cross-sectional view 800C of the top view of
 25 spindle/workpiece 831 of Fig. 8B taken along the lines 8C-8C of Fig. 8B illustrating tooth space 846S and relief 846R.

Fig. 8D is another example of the invention, namely, a workpiece similar to the workpiece illustrated in Figs. 8 and 8A shown in a perspective view 800D, with a circumferential groove 836G in the shoulder 836A adjacent the external spline 897A. In the view of Fig. 8D, a
 30 groove 836G and a chamfer 836C within the groove are shown. In the process to make the tooth spaces of the example of Fig. 8D, tool clearance reliefs are not necessary as the groove 836G functions as the relief. Fig. 8E is a top view 800 E of Fig. 8D illustrating the same elements and features of Fig. 8D. Fig. 8F is a cross-sectional view taken along the lines 8F-8F of Fig. 8E

5 illustrating tooth space 846S, groove 836G and the chamfer 836C.

Fig. 8G is a top view taken along the lines 8G-8G of Fig. 8 illustrating the tool smilling an unnumbered external tooth space into a cylindrical portion of male spline apparatus 831 which is capable of mating with a tooth of an internal spline. Fig. 8G is used in connection with Fig. 9C to illustrate some of the aspects of the tool.

10 Fig. 10 is a perspective view of a carrier 1000 with counterbore and internal spline 1020 therein made by the smilling process. Fig. 10A is a top view 1000A of Fig. 10. The carrier includes a plurality of teeth 1003T, 1005T, 1007T, equally spaced about the inner circumference of the device. Tooth spaces 1002S, 1004S, 1006S and 1008S are equally spaced about the inner circumference of the carrier and are capable of mating with external spline teeth. Carbide cutting
15 cone tool 536 is shown in the process of smilling a tooth space in the inner circumference of the counterbore 1020 as described above.

A process for manufacturing a spline in proximity to an adjacent structure is disclosed and claimed which includes the step of securing a workpiece as well as many other steps. Referring to Figs. 5 and 9, the workpiece 531A includes an upper cylindrical portion 531C and
20 an adjacent structure 532, and the upper cylindrical portion includes an end or top portion 535 and a length. A rotary cutting tool 536 is oriented at an inclination angle, β , with respect to the upper cylindrical portion 531C of the workpiece and, of course, the rotary cutting tool 536 is rotated 536R. An end portion 535 of the upper cylindrical portion of the workpiece is engaged by moving the tool 536 from its home position (tip of the 541 arrow) by the rotating rotary cutting
25 tool 536. The rotary cutting tool is moved along the line or vector 539 from the end portion 536 of the upper cylindrical portion of the workpiece removing material by its cutting action along the length of the upper cylindrical portion 531C and into the adjacent structure 532 of the workpiece 531A forming a rotary cutting tool relief 505R. Tooth spaces, such as tooth space 505S, are formed by the cutting action of the tool 536. Next, the rotary cutting tool 536 is
30 retracted along the line or vector 540 from the adjacent structure of the workpiece along the angle of inclination of the rotating rotary cutting tool 536. The rotary cutting tool is then returned vertically along the line or vector 541 to its initial position (home) and the workpiece is positioned for the next smilling operation. The workpiece 531A is rotated, or indexed, after

5 cutting each tooth space so that another tooth space may be formed. A spline tooth is formed between two spaced apart tooth spaces. The steps of: engaging the end portion of the upper cylindrical portion of the workpiece with the rotating rotary cutting tool; moving the rotating rotary cutting tool from the end portion of the upper cylindrical portion of the workpiece removing material by its cutting action along the length of the upper portion and into the adjacent structure of the workpiece forming a rotary cutting tool relief; and, retracting the rotary cutting tool from the adjacent structure of the workpiece along the angle of inclination of the rotating rotary cutting tool are then repeated.

10 In connection with this process, a step of sizing the rotary cutting tool 536 for an external spline is based on the tool cone included angle, 2τ , determined as set forth hereinabove in connection with Fig. 9E, the part space included angle, 2α , which is chosen by the designer as being nominally 60° , and the inclination angle β . Once the angle 2τ is known, the length of the rotary tool is determined. A cap radius is established at the form diameter and the tool cone extends long enough out of the part to completely mill the spaces/ slots of the part. The just stated process may produce an external spline where the adjacent structure is a shoulder and the rotary cutting tool relief extends at the inclination angle into the shoulder.

20 Another process for manufacturing a spline in proximity to an adjacent structure is disclosed and claimed in reference to Fig. 10 and other Figs. Referring to Fig. 10, the steps of the process include securing a workpiece having a counterbore 1020 therein and an adjacent structure 1030C in proximity to the counterbore 1020. Reference numeral 1020 is being used to generally indicate the counterbore and the internal spline formed on the inner circumference of the counterbore. The counterbore 1020 extends to a depth of the counterbore engagement surface 1020. The counterbore includes an end portion 1001 and a length as the distance from the end portion 1001 to the counterbore engagement surface 1030C. In home position, the rotary cutting tool is oriented at an inclination angle with respect to the end portion 1001 of the counterbore 1020 of the workpiece. The rotary cutting tool 536 is, of course, rotated 536R and brought into engagement with the end portion 1001 of the counterbore of the workpiece. Next, the rotating rotary cutting tool 536 moves from the end portion of the counterbore of the workpiece removing material by its cutting action along the length of the counterbore (from end

5 1001 to counterbore 1020) and into the adjacent structure 1030C of the workpiece forming a rotary cutting tool relief, for example, 1002R. Following creation of the rotary cutting tool relief, the rotary cutting tool is retracted from the adjacent structure of the workpiece along the angle of inclination of the rotating rotary cutting tool.

10 The further steps of the process include: returning the rotary cutting tool to an initial position (home position); indexing the workpiece by rotating the workpiece after creation of each tooth space; and, repeating the steps of: engaging the end portion of the counterbore of the workpiece with the rotating rotary cutting tool; moving the rotating rotary cutting tool from the end portion of the counterbore of the workpiece removing material by its cutting action along the length of the counterbore and into the adjacent structure of the workpiece forming an angular
15 rotary cutting tool relief; and, retracting the rotary cutting tool from the adjacent structure of the workpiece along the angle of inclination of the rotating rotary cutting tool.

The just stated process may produce an internal spline and the adjacent structure may be a counterbore engagement surface and the rotary cutting tool relief extends at the inclination angle into the counterbore. In connection with this process, a step of sizing the rotary cutting tool is
20 based on the tool cone included angle, based on the part space included angle and inclination angle. A smilling process for manufacturing an external spline is disclosed and claimed. The process includes the step of determining the load to be carried by the external spline. The load is determined by parameters of the application. Referring to Figs. 4-4C and Figs. 9-9B, a pitch diameter, D , is selected for the external spline based on the determined load. The number of
25 teeth, N , are then selected such that the circular pitch, CP , is sufficiently large and that the teeth of the external spline are sufficiently large and capable of handling the specified load. A length of the external spline is then determined based on the determined load, the selected pitch diameter of the external spline, the circular pitch, CP , shear and compressive stresses on the teeth and shaft, the fit of the spline and the interengagement obtainable between the internal spline teeth
30 and external spline teeth. Next, a tool inclination angle, β , is selected and a part space included angle, 2α , is also selected. The part space included angle is selected in a reasonable range of angles. A tool cone included angle, 2τ , is calculated based on an algorithm expressed in terms of β and α . Once the tool cone included angle 2τ is known, a cap radius down to the form diameter

5 establishes one end of the tool and the tool cone extends long enough out of the part to make a complete part.

Next, the workpiece is chucked in an appropriate endmill. Following the chucking, the workpiece is smiled creating an appropriate external space angle (tooth space) using the smiling process with the appropriately sized tool and a 5 axis Mazak endmill. The process further
 10 includes smiling an angular relief in an adjacent structure of the workpiece for clearance of the tool. Typically, the workpiece is cylindrically shaped and the adjacent structure is a shoulder. To create the smiled spline the workpiece is rotatably indexed which enables smiling a plurality of equally spaced angles (tooth spaces) about the circumference of the workpiece forming circumferentially spaced external spline teeth.

15 The step of sizing the tool includes use of the algorithm expressed in terms of the inclination angle, β , and the part space included angle α , to arrive at a tool cone included angle 2τ . Once 2τ is known, a cap radius down to the form diameter establishes one end of the tool and the tool cone extends long enough out of the part to make a complete part. Typically, but not exclusively, the inclination angle, β , is preferably in the range of 30-60° and the part space angle,
 20 α , is preferably in the range of 40-75°.

The rotary cutting tool includes a carbide cutting portion and the tool includes two straight flutes and a radius cap for creating an angular spline. A single flute may be used in an angular application. If an involute spline is desired then the cutting tool includes a plurality of involute radii to produce the appropriate space angle (tooth space) and involute teeth. Several
 25 flutes may be used to produce an involute tooth.

If a straight-sided spline is smiled, the rotary cutting tool (endmill) would approach the shape of a cylinder and the inclination angle would approach 90°. The relief smiled into an adjacent structure such as a shoulder would approach a circular path whose depth would be the diameter of the cylindrical-shaped rotary cutting tool.

30 A process for manufacturing an internal spline is disclosed and claimed and is similar to the process for manufacturing an external spline. The process includes the step of determining the load to be carried by the internal spline which is the same step as described above in connection with the external spline. Next, a pitch diameter of a mating external spline is selected

5 as described above. Next, the length of the internal spline apparatus based on the determined load and the selected pitch diameter of the external spline apparatus is determined. Next, the number of teeth, N , is selected such that the circular pitch of the external spline is sufficiently large and that the teeth of the external spline are capable of handling the load. Next, an external part space included angle, $2\alpha^\circ$ is selected and an internal part space included angle is determined using the
 10 formula, $2\alpha^\circ - ((360/N)^\circ)$. The rotary cutting end mill tool is then sized based on the algorithm expressed in terms of the inclination angle β and the internal part space included angle $2\alpha^\circ - ((360/N)^\circ)$, to arrive at a tool cone included angle, 2τ . Once 2τ is determined, then the cap radius is located at the form diameter and the other end of the tool extends far enough out of the part to ensure complete smilling of the slots/spaces. An appropriate workpiece is then chucked in a
 15 Mazak endmill or any other multiple axis commercially available endmill. The workpiece is then smilled using the rotary cutting carbide tool and an endmill producing an appropriate internal space angle in the workpiece. A rotary cutting carbide tool angular relief is then smilled in an adjacent structure of the workpiece. Typically, the appropriate workpiece includes a counterbore therein and the counterbore, in turn, has an inner circumference. To produce appropriate
 20 circumferentially spaced internal spline teeth and equally spaced appropriate internal space angles (tooth space), the workpiece is rotatably indexed which enables smilling a plurality of equally spaced appropriate internal space angles (tooth spaces) about the inner circumference of the workpiece and thus forming circumferentially spaced internal spline teeth.

25 **Reference Numerals**

- 100- cross-sectional diagrammatic view of the prior art taken male connection member (shaft member) along the line 1-1 of Fig. 1A illustrating the base, shoulder, cylindrical external spline portion, and relief together with a traditional cutter-shaper and its operating path
- 100A- perspective view of prior art
- 30 100B- elevation view of prior art Fig. 1A
- 100C- top view of prior art Fig. 1A
- 101-base
- 101A-workpiece

- 5 102-shoulder
- 103-relief
- 104-tooth
- 105-top of cylindrical section
- 106-cutter-shaper
- 10 107-cutting blade
- 108-diagram of cutter motion
- 109-downward stroke of cutter-shaper
- 110-lateral or transverse stroke removing the cutter-shaper tool from the spline (workpiece)
- 111-longitudinal or upward stroke of the cutter-shaper tool
- 15 112-repositioning stroke moving the cutter-shaper tool in alignment
- 121- tooth
- 122-flank or side of tooth
- 123- fillet
- 199-cylindrical section
- 20 200-perspective view of the prior art illustrating the base, shoulder, cylindrical internal spline portion, and relief of the female connection member (collar member)
- 200A-cross-sectional view of prior art taken along the lines 2A-2A of Fig. 2
- 200B- top view of Fig. 2
- 201-base of the female connection member
- 25 201A- female connection member
- 202-top of the female connection member
- 203-relief of the female connection member
- 204-tooth space
- 205-tooth of the female connection member
- 30 206- shoulder or bottom of the female connection member
- 300- cross-sectional view of the male and female connection members interengaged
- 400- schematic of angular spline arrangement and principal terms
- 400A- schematic of involute spline arrangement and principal terms

- 5 400B- is a schematic of the external and internal splines of an involute spline connection apparatus manufactured using the smilling process illustrating the pitch diameter, the major and minor external diameters, the major and minor internal diameters and the circular pitch
- 500-a partial cross-sectional diagrammatic view of a workpiece, taken along the lines 5-5 of Fig. 10 5A, being machined with an angular carbide endmill to produce an external spline with reliefs cut into a shoulder portion and a base portion of the workpiece
- 500A-a perspective diagrammatic view of a workpiece illustrating a finished external spline on an upper cylindrical portion, and, reliefs for tool clearance cut into the intermediate shoulder and base portion
- 15 500B-a top diagrammatic view of the workpiece depicted in Fig. 5
- 500C-a cross-sectional view taken along the lines 5C-5C of Fig. 5B
- 503R, 505R, 507R, 509R, 511R, 513R, 515R, 517R, 519R, 521R, 523R, 525R, 527R, 529R- external spline relief for tool clearance
- 503S, 505S, 507S, 509S, 511S, 513S, 515S, 517S, 519S, 521S, 523S, 525A, 527S, 529S- tooth 20 spaces, external space for internal mating tooth
- 504T, 506T, 508T, 510T, 512T, 514T, 516T, 518T, 520T, 522T, 524T, 526T, 528T, 530T- external spline teeth
- 531-male connection apparatus, workpiece
- 531A-male or external spline connection apparatus
- 25 531B-base portion of male connection apparatus
- 531C-cylinder portion of male connection apparatus
- 532- shoulder on male
- 535-top of cylinder
- 536-end mill tool, angular, straight, or involute
- 30 536A- fluted end of tool
- 536B-fluted end of tool
- 536R- arrow indicating rotation of the tool 506
- 537A-rotation of workpiece 501 positioning it for the next pass of tool 506

- 5 539-downward stroke/pass of end mill tool 506
- 540-withdrawal vector of the tool along the profile of the relief
- 541-vertical vector of the tool
- 542-positioning vector of the tool
- 599S-arrow to the external spline
- 10 600- a perspective schematic view of the internal spline residing in a counterbore in the
workpiece, the counterbore terminating in a counterbore engagement surface
- 600A- a cross-sectional view taken along the lines 6A-6A of Fig. 6 illustrating the internal spline
and the reliefs cut into the counterbore engagement surface and the upper portion of the
workpiece
- 15 600B- a top view of the workpiece illustrated in Figs. 6 and 6A illustrating the upper surface of
the top portion of the workpiece.
- 602R, 604R, 604R, 508R, 610R, 612R, 614R, 616R, 618R, 620R, 622R, 624R, 626R, 628R-
external spline relief for tool clearance
- 602S, 604S, 606S, 608S, 610S, 612S, 614S, 616S, 618S, 620S, 622S, 624A, 626S, 628S- tooth
- 20 spaces, internal space for external spline mating tooth
- 603T, 605T, 607T, 609T, 611T, 613T, 615T, 617T, 619T, 621T, 623T, 625T, 627T, internal
spline teeth
- 630C- counterbore engagement surface
- 631- base portion of female collar apparatus
- 25 631A- internal spline connection apparatus
- 631B- internal spline in the counterbore
- 632- upper portion of female collar apparatus
- 700- cross-sectional schematic of the male spline apparatus and the female collar apparatus
completely interengaged or coupled together
- 30 700A- cross-sectional schematic of the male spline apparatus and the female collar apparatus
partially interengaged or coupled together
- 700B- cross-sectional view of the male spline apparatus and the female collar apparatus
separated apart from one another

- 5 700C- cross-sectional view taken along the lines 7C-7C of Fig. 7 illustrating the external spline of the male spline apparatus and the internal spline of the female spline apparatus in interengagement
- 700D- is an enlarged view of a portion of Fig. 7C
- 700E- a cross-sectional schematic view of both Fig. 7 shown in relation to the prior art view of
- 10 Fig. 3, illustrating that the apparatus made by the smiling process has an effective face width EFs equal to the length of the spline connection, SC, and that the effective face width EF of the prior art is much smaller than EFs for the same length of the spline connection, SC
- 800- a front view of an example of the invention, namely, a male spline apparatus illustrating
- 15 an external spline being smiled on a workpiece using an endmill tool oriented at an inclination angle of 45° .
- 800A- a perspective view of an example of the invention, namely, a spindle, having a male spline apparatus, including an external spline after completion of the smiling process on a workpiece.
- 20 800B- is a top view of the workpiece of Fig. 8A.
- 800C- a cross-sectional view of Fig. 8B taken along the lines 8C-8C of Fig. 8B.
- 800D- another example of the invention, namely, a workpiece similar to the workpiece illustrated in Fig. 8A, with an circumferential relief in the shoulder adjacent the external spline.
- 25 800E- a top view of Fig. 8D.
- 800F- a cross-sectional view taken along the lines 8F-8F of Fig. 8E.
- 800G- a top view taken along the lines 8G-8G of Fig. 8 illustrating the tool smiling an external space into a cylindrical portion of male spline apparatus which is capable of mating with a tooth of an internal spline.
- 30 801- base of workpiece
- 802- intermediate portion of workpiece
- 803- top of cylindrical portion of workpiece
- 804- shoulder on workpiece

- 5 820- tool holder
- 821- chuck
- 825- Mazak 5 axis end mill
- 831- spindle workpiece
- 832- rim of spindle
- 10 833- threaded bolt holes
- 834- spindle
- 836- adjacent shoulder
- 836A- adjacent shoulder
- 836G- groove in adjacent shoulder 836A
- 15 836C- chamfer, part of groove 836G
- 837- top of cylindrical portion of male spline apparatus
- 839T, 841T, 843T, 845T, 847T-external spline tooth
- 840R, 842R, 844R, 846R, 848R- tool clearance relief
- 840S, 842S, 844S, 846S, 848S- space angle for receiving a tooth of a mating internal spline
- 20 860- recess in the rim 831 of the spindle
- 869T, 871T, 873T, 875T, 877T-external spline tooth
- 870S, 872S, 874S, 876S, 878S- space angle for receiving a tooth of a mating internal spline
- 880- passageway in spindle
- 888, 889- workpiece chuck
- 25 897- arrow pointing to external spline of Fig. 8A
- 897A- external spline
- 900- a schematic representation of the smilling process illustrating the smilling cutter carbide tool at an inclination angle of 45° with respect to the workpiece.
- 900A- is a schematic representation of the smilling cutter carbide tool at an inclination angle, β ,
- 30 and a part space included angle, 2α , shown as part of an elliptical projection, to determine the tool cone included angle, 2τ .
- 900B- is a view taken along the lines of 9B-9B of Fig. 9A with the elliptical projection rotated 90° counterclockwise orienting the elliptical projection of the part space included angle

- 5 with the cutting profile of tool as illustrated in Fig. 9C.
- 900C- is an enlarged portion of Fig. 8G illustrating the carbide smilling cutter oriented in the direction of the elliptical projection of the part space included angle.
- 900D- a view similar to Fig. 9 illustrating material not yet removed by smilling
- 900E- a schematic view of the tool, inclination angle, part space angle and an ellipse for
- 10 calculating the tool cone included angle
- 901- direction of smilling carbide tool cutter
- 1000- carrier with counterbore and internal spline therein made by the smilling process
- 1000A- a top view of Fig. 10.
- 1003T, 1005T, 1007T-internal spline teeth
- 15 1002R, 1004R, 1006R, 1008R- relief in the counterbore engagement surface 1030C
- 1002S, 1004S, 1006S, 1008S- space angle for receiving a tooth of a mating external spline
- 1020- counterbore and internal spline
- 1030C-counterbore engagement surface
- 1100- a front view of the involute carbide end mill cutting tool having first and second flutes
- 20 1100A-an end view of the involute carbide end mill cutting tool
- 1100B-an enlargement of the surfaces of the involute end mill illustrating different radii, R1, R2 and R3
- 1101- length of tool, approximately 4 inches
- 1102- involute end mill carbide cutting tool
- 25 1103- shank diameter of tool, approximately 0.56 inches
- 1104- first flute
- 1105- second flute
- 1107- first cutting angle modified by radii, R1, R2, and R3
- 1200- front view of an angular carbide end mill cutting tool.
- 30 1200A-an end view of the angular carbide end mill cutting tool of Fig. 12.
- 1201- shank diameter of angular carbide end mill cutting tool, approximately 0.56 inches
- 1202- length of cutting tool, 4 inches
- 1203- tool space included angle 41.40°

- 5 1204- length of cutting surfaces, approximately 0.543 inches
 1205- length of flute surfaces approximately 0.875 inches
 1206, 1207-first flute
 1208, 1209-second flute
 B-backlash
- 10 BC-base circle, the circle from which involute spline tooth profiles are constructed
 CR-root clearance
 D-pitch diameter, the diameter of the pitch circle, which is determined as the ratio of the number
 of teeth to the diametral pitch
 Db-the diameter of the base circle
- 15 CP-circular pitch, the distance along the pitch circle between corresponding points of adjacent
 spline teeth
 L₁ - length of external spline made by smilling process
 L₂ - length of internal spline made by smilling process
 P-diametral pitch, the number of spline teeth per inch of pitch diameter
- 20 R1, R2, R3- radii on the involute end mill cutting tool 1102
 TT- tooth thickness at pitch diameter
 SW-space width at pitch diameter
 Dfi -form internal diameter
 Dfe-form external diameter
- 25 Dai-minor internal diameter
 Dre-minor external diameter
 Dae-major external diameter
 Dri-major internal diameter
 SAi-space angle, internal
- 30 SAe-space angle, external
 TAI-tooth angle, internal
 TAe-tooth angle, external
 C_r -prior art annular cutter relief, equal to annular reliefs 103, 203

- 5 SC-length of spline connection
 EF -effective face width length, prior art
 EFs -effective face width length, smilling
 FW- manufactured face width length
 α - part space half angle
- 10 β - inclination angle
 τ - tool cone half angle
 X-coordinate on elliptical projection
 Y-coordinate on elliptical projection
 W_1 =tool ellipse major semi-axis,
- 15 W_2 =tool ellipse minor semi-axis,
 Φ -pressure angle, the angle between a line tangent to an involute and radial line through the point
 of tangency

The invention has been set forth by way of example only in accordance with the invention
 fully disclosed herein. Changes and modifications to the examples provided herein may be made
 20 and those changes and modifications are specifically included herein and any such changes and
 modifications are within the scope of the appended claims.

5 **Claims:**

1. A male spline connection apparatus, comprising:

a base portion, a shoulder portion and a cylindrical portion;

said shoulder portion resides intermediate said base portion and said cylindrical portion;

said cylindrical portion includes an external spline thereon, said external spline includes a

10 plurality of tooth spaces therein circumferentially spaced apart from each other forming a

plurality of teeth between adjacent tooth spaces, said tooth spaces are formed by sides of adjacent teeth and a fillet joining said adjacent teeth; and,

each of said plurality of said tooth spaces includes a spline relief portion for tool clearance extending angularly into said shoulder and said base portion of said male spline connection apparatus.

15

2. A male spline connection apparatus as claimed in claim 1, wherein each of said plurality of teeth of said external spline includes angular sides.

3. A male spline connection apparatus as claimed in claim 1, wherein each of said plurality of said teeth of said external spline includes straight sides.

20 4. A male spline connection apparatus as claimed in claim 1, wherein each of said plurality of said teeth of said external spline includes involute sides.

5. A male spline connection apparatus as claimed in claim 1, wherein each of said plurality of said teeth of said external spline includes full curve sides.

6. A female collar connection apparatus, comprising

25 a base portion and an upper portion;

a generally cylindrically shaped hub portion, said hub portion includes an internal spline therein;

said internal spline terminating in a counterbore engagement surface;

said internal spline includes a plurality of tooth spaces therein circumferentially spaced

30 apart from each other forming a plurality of teeth between adjacent tooth spaces, said tooth spaces are formed by sides of adjacent teeth and a fillet joining said adjacent teeth; and,

each of said plurality of said tooth spaces includes a spline relief portion for tool clearance extending angularly into said counterbore engagement surface.

5 7. A female collar connection apparatus as claimed in claim 6, wherein each of said plurality of teeth of said internal spline includes angular sides.

8. A female collar connection apparatus as claimed in claim 6, wherein each of said plurality of teeth of said internal spline includes straight sides.

10 9. A female collar connection apparatus as claimed in claim 6, wherein each of said plurality of teeth of said internal spline includes involute sides.

10. A female collar connection apparatus as claimed in claim 6, wherein each of said plurality of teeth of said internal spline includes full curve sides.

11. A spline connection apparatus, comprising:

15 a male spline apparatus, said male spline apparatus includes: a base portion, a shoulder portion and a cylindrical portion; said shoulder portion resides intermediate said base portion and said cylindrical portion; said cylindrical portion includes an external spline thereon, said external spline includes a plurality of first tooth spaces therein circumferentially spaced apart from each other forming external spline teeth between adjacent first tooth spaces, each of said first tooth spaces are formed by sides of adjacent external spline teeth and a fillet joining said adjacent
20 external spline teeth; and, each of said plurality of said first tooth spaces includes a spline relief portion for tool clearance extending angularly and conically into said shoulder and base portion of said male spline apparatus;

25 a female collar apparatus, said female collar apparatus includes: a base portion and an upper portion; a generally cylindrically shaped hub portion having an inner circumference, said hub portion includes an internal spline therein; said internal spline terminating in a counterbore engagement surface; said internal spline includes a plurality of second tooth spaces therein circumferentially spaced apart from each other forming internal spline teeth between adjacent second tooth spaces, said second tooth spaces are formed by sides of adjacent internal spline teeth and a fillet joining said adjacent internal spline teeth; and, each of said plurality of said
30 second tooth spaces includes an internal spline relief portion for tool clearance extending angularly and conically into said counterbore engagement surface;

each of said plurality of external spline teeth of said external spline resides in a respective one of said plurality of said second tooth spaces of said internal spline; and,

5 each of said plurality of internal spline teeth of said internal spline resides in a respective one of said plurality of said first tooth spaces of said external spline.

12. A spline connection apparatus, as claimed in claim 11, wherein:

10 each of said plurality of said external spline teeth of said external spline may interengage two of said plurality of said internal spline teeth and wherein each of said plurality of internal spline teeth may interengage two of said plurality of said external spline teeth of said external spline.

13. A spline connection apparatus as claimed in claim 11, wherein each of said plurality of said external spline teeth of said external spline of said male spline apparatus has a first length and wherein each of said plurality of said internal spline teeth of internal spline of said hub
15 portion of said female collar apparatus has a second length, and said first length and said second length are equal.

14. A spline connection apparatus as claimed in claim 12, wherein each of said plurality of said external spline teeth of said external spline of said male spline apparatus has a first length and wherein each of said plurality of said internal spline teeth of internal spline of said hub
20 portion of said female collar apparatus has a second length, and said first length and said second length are equal.

15. A spline connection apparatus as claimed in claim 13 wherein said first and second lengths are the effective face width of: said external spline of said male spline apparatus; and, said internal spline of said female collar apparatus.

25 16. A spline connection apparatus as claimed in claim 11 wherein:

 said cylindrical portion of said male spline apparatus engages said counterbore engagement surface of said generally cylindrically shaped hub portion recessed in said upper portion of said female collar apparatus; and,

30 said shoulder of said male spline apparatus engages said upper portion of said female collar portion.

17. A spline connection apparatus as claimed in claim 15 wherein:

 said cylindrical portion of said male spline apparatus engages said counterbore engagement surface of said generally cylindrically shaped hub portion recessed in said upper

5 portion of said female collar apparatus; and,

said shoulder of said male spline apparatus engages said upper portion of said female collar portion.

18. A spline connection apparatus as claimed in claim 11, wherein:

10 a portion of said plurality of said external spline teeth of said external spline teeth interengages a portion of said plurality of said internal spline teeth.

19. A spline connection apparatus as claimed in claim 11, wherein:

each of said plurality of external spline teeth of said external spline includes angular sides; and,

each of said plurality of internal spline teeth of said internal spline includes angular sides.

20. A spline connection apparatus as claimed in claim 11, wherein:

15 each of said plurality of external spline teeth of said external spline includes straight sides; and,

each of said plurality of internal spline teeth of said internal spline includes straight sides.

21. A spline connection apparatus as claimed in claim 11, wherein:

20 each of said plurality of external spline teeth of said external spline includes involute sides; and,

each of said plurality of internal spline teeth of said internal spline includes involute sides.

22. A spline connection apparatus as claimed in claim 11, wherein:

25 each of said plurality of external spline teeth of said external spline includes full curve sides; and,

each of said plurality of internal spline teeth of said internal spline includes full curve sides.

23. A spline connection apparatus, comprising:

30 a male member, said male member includes: a shoulder portion and a cylindrical portion; said cylindrical portion includes an upper surface and an external spline thereon, said external spline includes a plurality of first tooth spaces therein circumferentially spaced apart from each other forming external spline teeth between adjacent first tooth spaces, each of said plurality of said first tooth spaces includes a spline relief portion for tool clearance extending angularly into

5 said shoulder of said male member;

a female member, said female member includes: a base portion and an upper portion; a generally cylindrically shaped hub portion having an inner circumference, said hub portion includes an internal spline therein; said internal spline terminating in a counterbore engagement surface; said internal spline includes a plurality of second tooth spaces therein circumferentially spaced apart from each other forming internal spline teeth between adjacent second tooth spaces, said second tooth spaces are formed by sides of adjacent internal spline teeth and a fillet joining said adjacent internal spline teeth; and, each of said plurality of said second tooth spaces includes an internal spline relief portion for tool clearance extending angularly into said counterbore engagement surface;

15 said external teeth of said external spline have a first length and said internal teeth of said internal spline have a second length, said first and second lengths are equal;

said male and female members being coupled together, said shoulder portion of said male member engages said upper portion of said female member, said upper surface of said cylindrical portion of said male member engages said counterbore engagement surface of said female member, said external teeth of said external spline completely intermeshed with said internal teeth of said internal spline along said first length of said external teeth and said second length of said internal teeth such that the effective face width of said engagement is equal to the length of said external and internal teeth.

24. A spline connection apparatus, comprising:

25 a male member, said male member includes: a shoulder portion and a cylindrical portion; said cylindrical portion includes an upper surface; said cylindrical portion of said male member extends from said shoulder portion and includes an external spline having a first length;

a female member, said female member includes: a base portion and an upper portion; said upper portion includes a counterbore therein having an internal spline therein having a second length; said internal spline terminating in a counterbore engagement surface;

30 said male and female members being coupled together, said shoulder portion of said male member engaging said upper portion of said female member, said upper surface of said cylindrical portion of said male member engaging said counterbore engagement surface of said

5 female member, said first and second lengths being equal, said external spline completely intermeshed said internal spline, and said effective face width of said connection is equal to said first and second length of said splines.

25. A process for manufacturing an external spline, comprising the steps of:

determining the load to be carried by said external spline;

10 selecting a pitch diameter of said external spline based on said determined load;

selecting the number of teeth such that the circular pitch is sufficiently large and that said teeth of said external spline are sufficiently large and capable of handling said load;

determining a length of said external spline based on said determined load and said selected pitch diameter of said external splines;

15 selecting a tool inclination angle, β ;

selecting a part space included angle, α ;

determining a tool cone included angle, 2τ , based on an algorithm expressed in terms of β and α ;

sizing the tool based on the actual external spline dimensions required;

20 chucking an appropriate workpiece in an endmill;

milling, using said tool and an endmill, an appropriate tooth space in said workpiece.

26. A process for manufacturing an external spline as claimed in claim 25

wherein said step of sizing the tool includes forming a cap radius at one end of the tool and establishing a tool length such that the tool cone extends long enough out of said external spline.

25 27. A process for manufacturing an external spline as claimed in claim 25, wherein said inclination angle, β , is preferably in the range of 30-60°.

28. A process for manufacturing an external spline as claimed in claim 25, wherein said part space angle, α , is preferably in the range of 40-75°.

29. A process for manufacturing an external spline as claimed in claim 25, further
30 comprising the steps of:

milling a relief in an adjacent structure of said workpiece for clearance of said tool.

30. A process for manufacturing an external spline as claimed in claim 25 wherein said workpiece is cylindrically shaped and said adjacent structure is a shoulder.

5 31. A process for manufacturing an external spline as claimed in claim 25 further comprising the step of:

rotatably indexing said workpiece and enabling the milling of a plurality of equally spaced tooth spaces about the circumference of said workpiece forming circumferentially spaced external spline teeth.

10 32. A process for manufacturing an external spline as claimed in claim 25 wherein said tool includes two straight flutes and a radius cap.

33. A process for manufacturing an external spline as claimed in claim 25 wherein said tool includes a plurality of involute radii to produce said appropriate space angle (tooth space) and involute teeth.

15 34. A process for manufacturing an internal spline, comprising the steps of:
determining the load to be carried by said internal spline;
selecting a pitch diameter of a mating external spline;
determining a length of said internal spline apparatus based on said determined load and said selected pitch diameter of said external spline apparatus;

20 selecting the number of teeth, N , such that the circular pitch of said external spline is sufficiently large and that said teeth of said external spline are capable of handling said load;

selecting an external part space included angle, $2\alpha^\circ$;

determining an internal part space included angle using the formula, $2\alpha^\circ - ((360/N)^\circ)$;

selecting a tool inclination angle, β ;

25 determining a tool cone included angle, 2τ , based on an algorithm expressed in terms of tool inclination angle β and said internal part space included angle, $2\alpha^\circ - ((360/N)^\circ)$;

sizing the tool establishing a cap radius at the form diameter at one end of said tool and extending said tool cone long enough out of said part to form a second end of said tool;

chucking an appropriate workpiece in an endmill;

30 milling, using said tool and an endmill, an appropriate internal space angle (tooth space) in said workpiece.

35. A process for manufacturing an internal spline as claimed in claim 34, further comprising the steps of:

5 milling a relief in an adjacent structure of said workpiece.

36. A process for manufacturing an internal spline as claimed in claim 34 wherein said appropriate workpiece includes a counterbore therein, said counterbore having an inner circumference.

10 37. A process for manufacturing an internal spline as claimed in claim 34 further comprising the step of:

rotatably indexing said workpiece and enabling the milling of a plurality of equally spaced appropriate internal space angles (tooth spaces) about the inner circumference of said workpiece forming circumferentially spaced internal spline teeth.

15 38. A process for manufacturing a spline in proximity to an adjacent structure, comprising the steps of:

securing a workpiece, said workpiece includes an upper cylindrical portion and an adjacent structure, and said upper cylindrical portion includes an end portion and a length;

orienting a rotary cutting tool at an inclination angle with respect to said upper cylindrical portion of said workpiece;

20 rotating said rotary cutting tool;

engaging said end portion of said upper cylindrical portion of said workpiece with said rotating rotary cutting tool;

25 moving said rotating rotary cutting tool from said end portion of said upper cylindrical portion of said workpiece along said length of said upper portion removing material from said upper cylindrical portion of said workpiece and into said adjacent structure of said workpiece forming a rotary cutting tool relief; and,

retracting said rotary cutting tool from said adjacent structure of said workpiece along said angle of inclination of said rotating rotary cutting tool.

30 39. A process for manufacturing a spline in proximity to an adjacent structure, as claimed in claim 38 further comprising the steps of:

returning said rotary cutting tool to an initial position;

indexing said workpiece;

repeating said steps of: engaging said end portion of said upper cylindrical portion of said

5 workpiece with said rotating rotary cutting tool; moving said rotating rotary cutting tool from
 said end portion of said upper cylindrical portion of said workpiece along said length of said
 upper portion removing material from said upper cylindrical portion of said workpiece and into
 said adjacent structure of said workpiece forming a rotary cutting tool relief; and, retracting said
 rotary cutting tool from said adjacent structure of said workpiece along said angle of inclination
 10 of said rotating rotary cutting tool.

40. A process for manufacturing a spline in proximity to an adjacent structure, as claimed
 in claim 38 wherein said spline is an external spline, said adjacent structure is a shoulder and said
 rotary cutting tool relief extends at said inclination angle into said shoulder.

41. A process for manufacturing a spline in proximity to an adjacent structure, as claimed
 15 in claim 38 wherein said spline is an external spline and wherein said rotary cutting tool is sized
 based on the tool cone included angle, the part space included angle, and the inclination angle of
 said tool.

42. A process for manufacturing a spline in proximity to an adjacent structure, comprising
 the steps of:

20 securing a workpiece, said workpiece includes a counterbore therein and adjacent
 structure, said counterbore includes an end portion and a length;

orienting a rotary cutting tool at an inclination angle with respect to said end portion of
 said counterbore of said workpiece;

rotating said rotary cutting tool;

25 engaging said end portion of said counterbore of said workpiece with said rotating rotary
 cutting tool;

moving said rotating rotary cutting tool from said end portion of said counterbore of said
 workpiece along said length of said counterbore and into said adjacent structure of said
 workpiece forming a rotary cutting tool relief; and,

30 retracting said rotary cutting tool from said adjacent structure of said workpiece along
 said angle of inclination of said rotating rotary cutting tool.

43. A process for manufacturing a spline in proximity to an adjacent structure, as claimed
 in claim 38 further comprising the steps of:

5 returning said rotary cutting tool to an initial position;
 indexing said workpiece;
 repeating said steps of: engaging said end portion of said counterbore of said workpiece
with said rotating rotary cutting tool; moving said rotating rotary cutting tool from said end
portion of said counterbore of said workpiece along said length of said counterbore and into said
10 adjacent structure of said workpiece forming a rotary cutting tool relief; and, retracting said
rotary cutting tool from said adjacent structure of said workpiece along said angle of inclination
of said rotating rotary cutting tool.

 44. A process for manufacturing a spline in proximity to an adjacent structure, as claimed
in claim 42 wherein said spline is an internal spline, said adjacent structure is a counterbore
15 engagement surface, and said rotary cutting tool relief extends at said inclination angle into said
counterbore.

 45. A process for manufacturing a spline in proximity to an adjacent structure, as claimed
in claim 42 wherein:

 said spline is an internal spline;
20 said rotary cutting tool is sized based on: a tool cone included angle as a function of a part
space included angle and an inclination angle;
 a cap radius is formed at the form diameter establishing a first end of said tool and the
tool cone extends long enough out of said spline to form a second end of said tool.

25

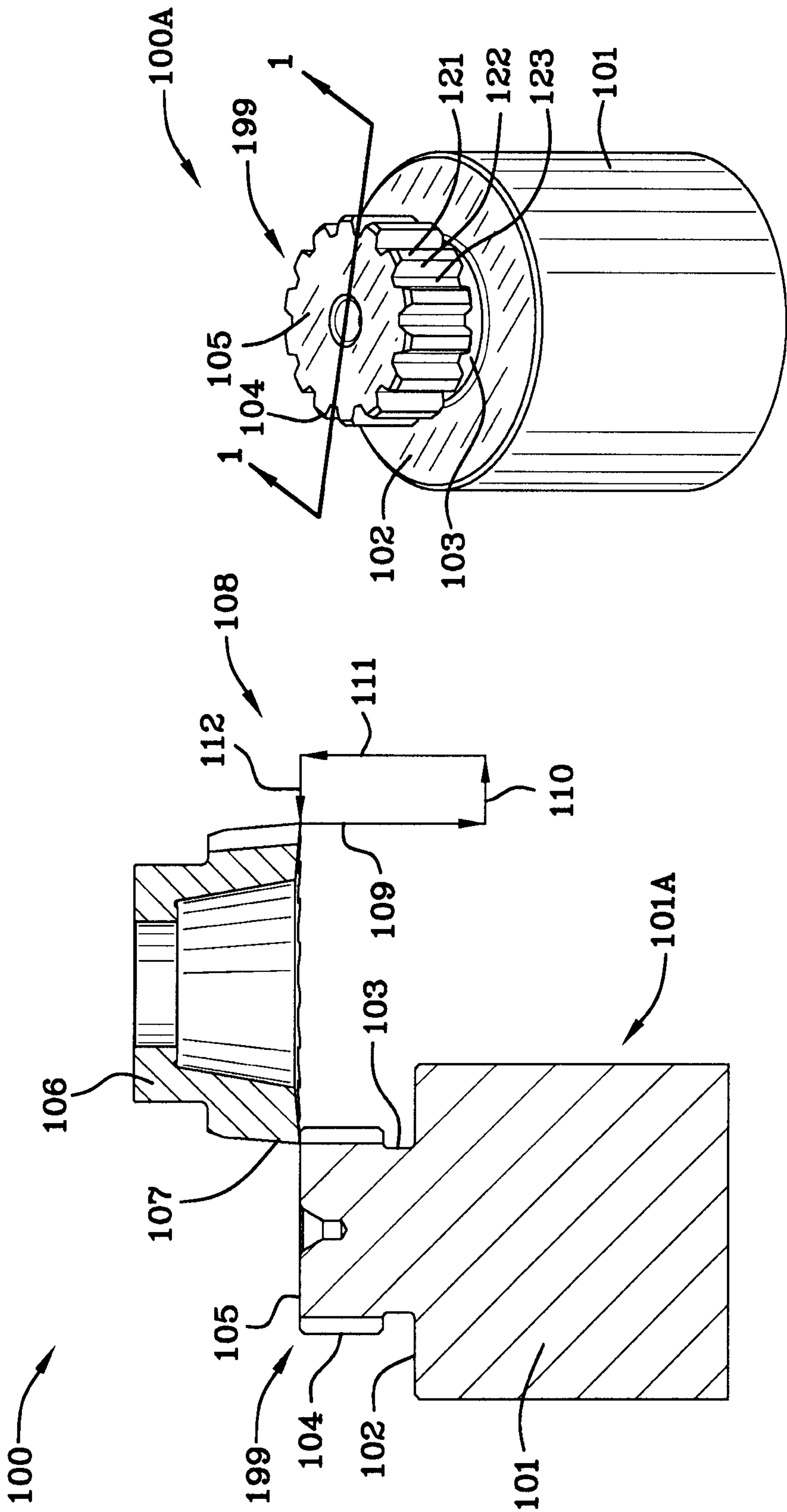


FIG. 1 (Prior Art)

FIG. 1A (Prior Art)

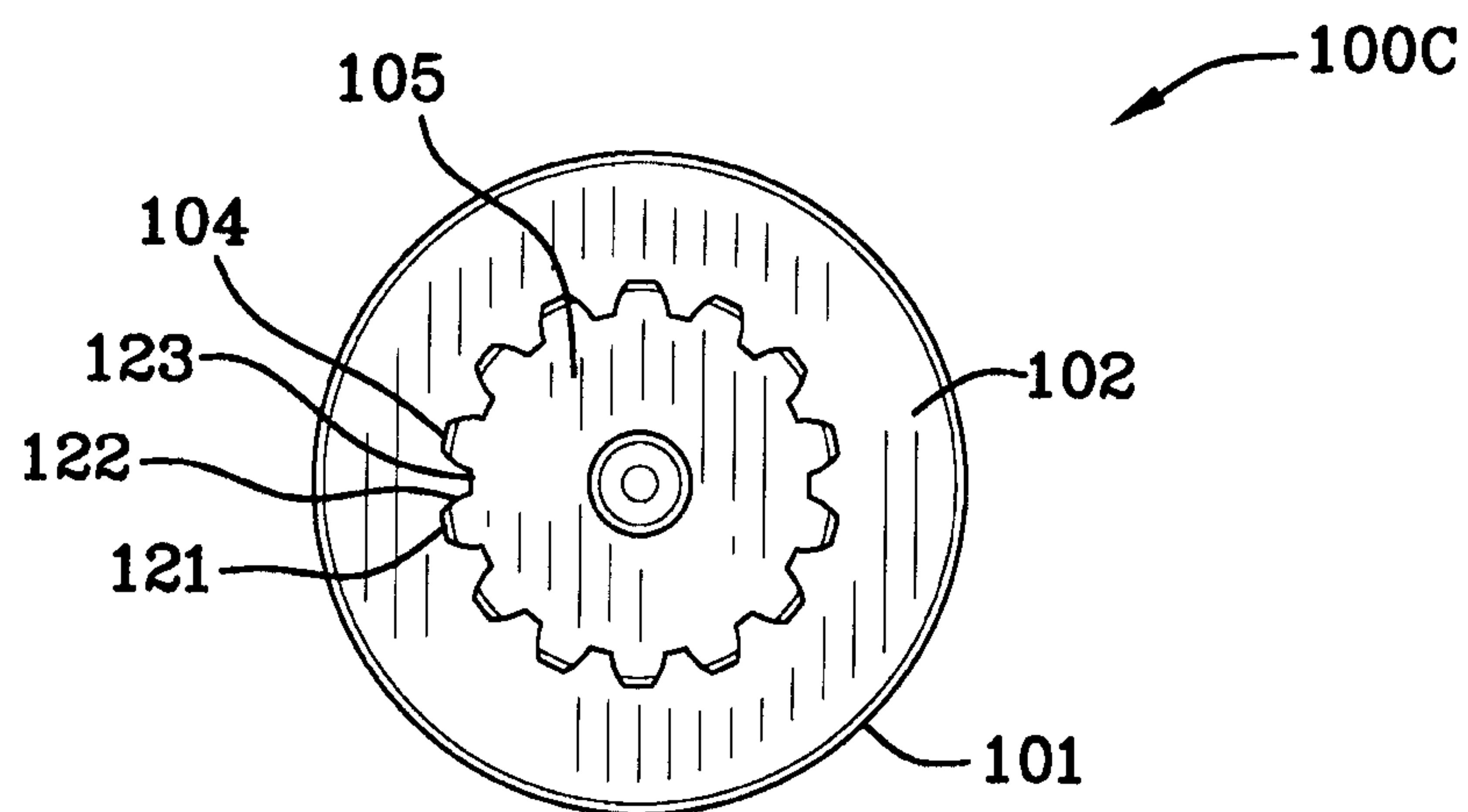


FIG. 1C (Prior Art)

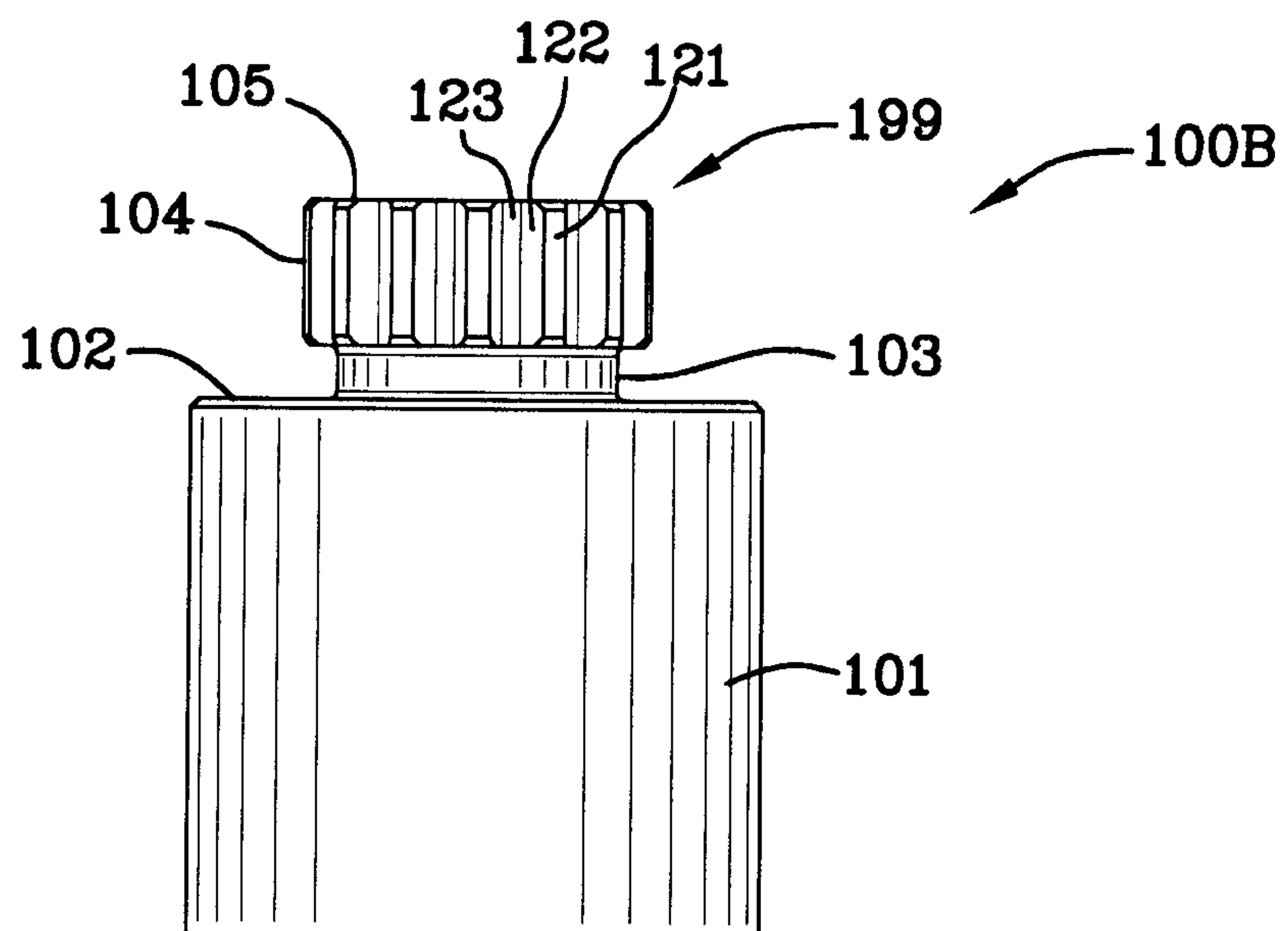


FIG. 1B (Prior Art)

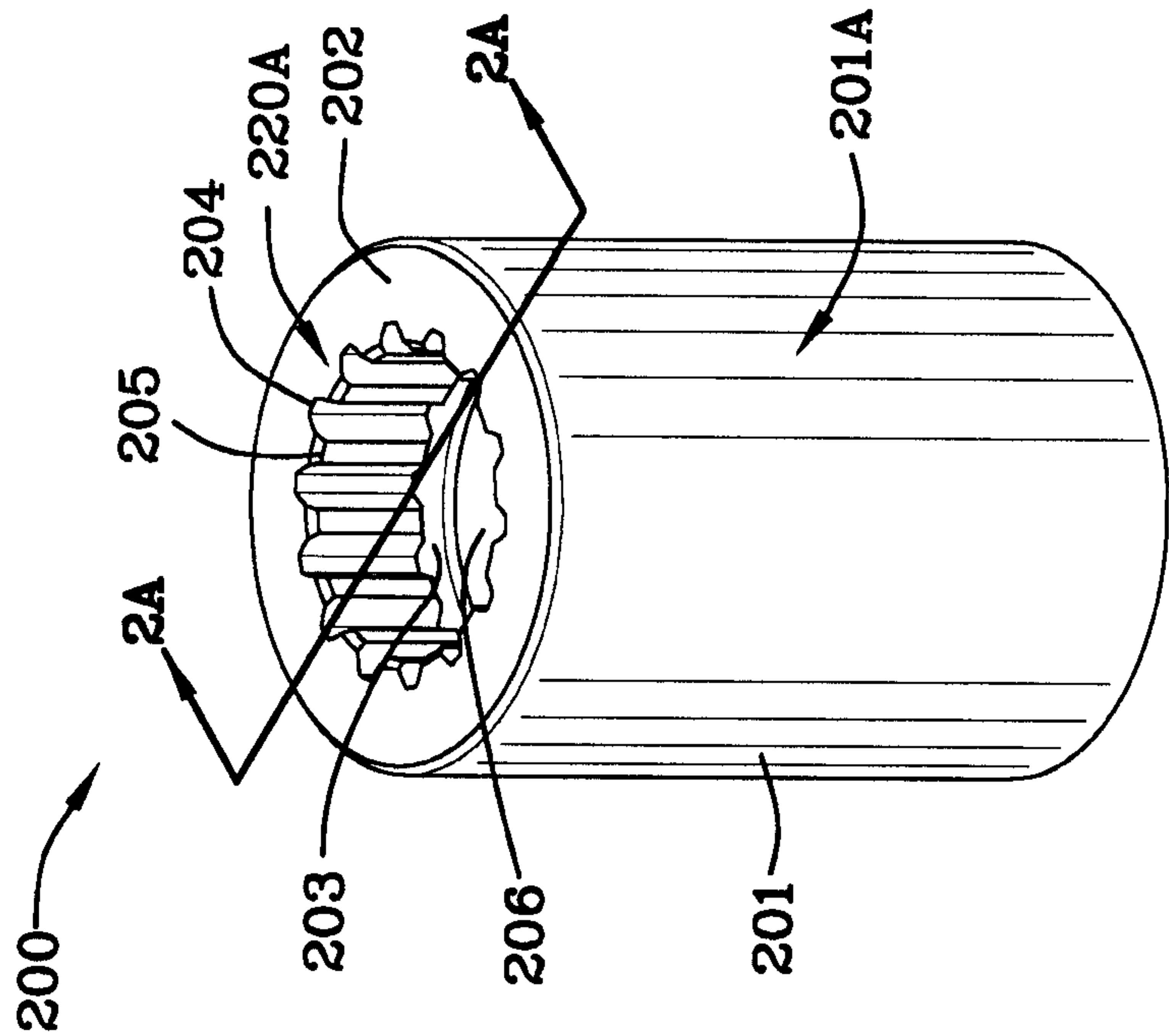


FIG. 2 (Prior Art)

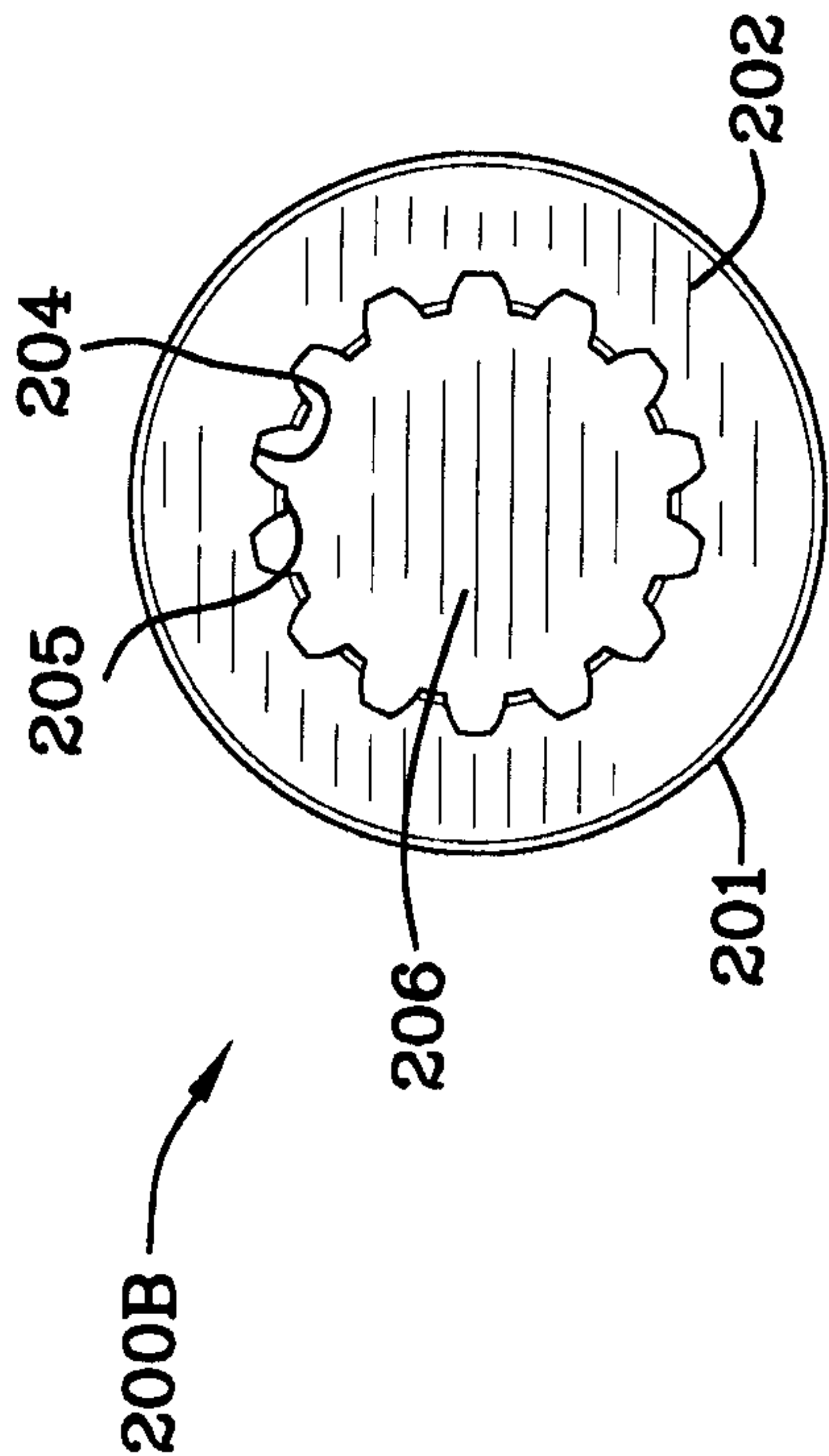


FIG. 2B (Prior Art)

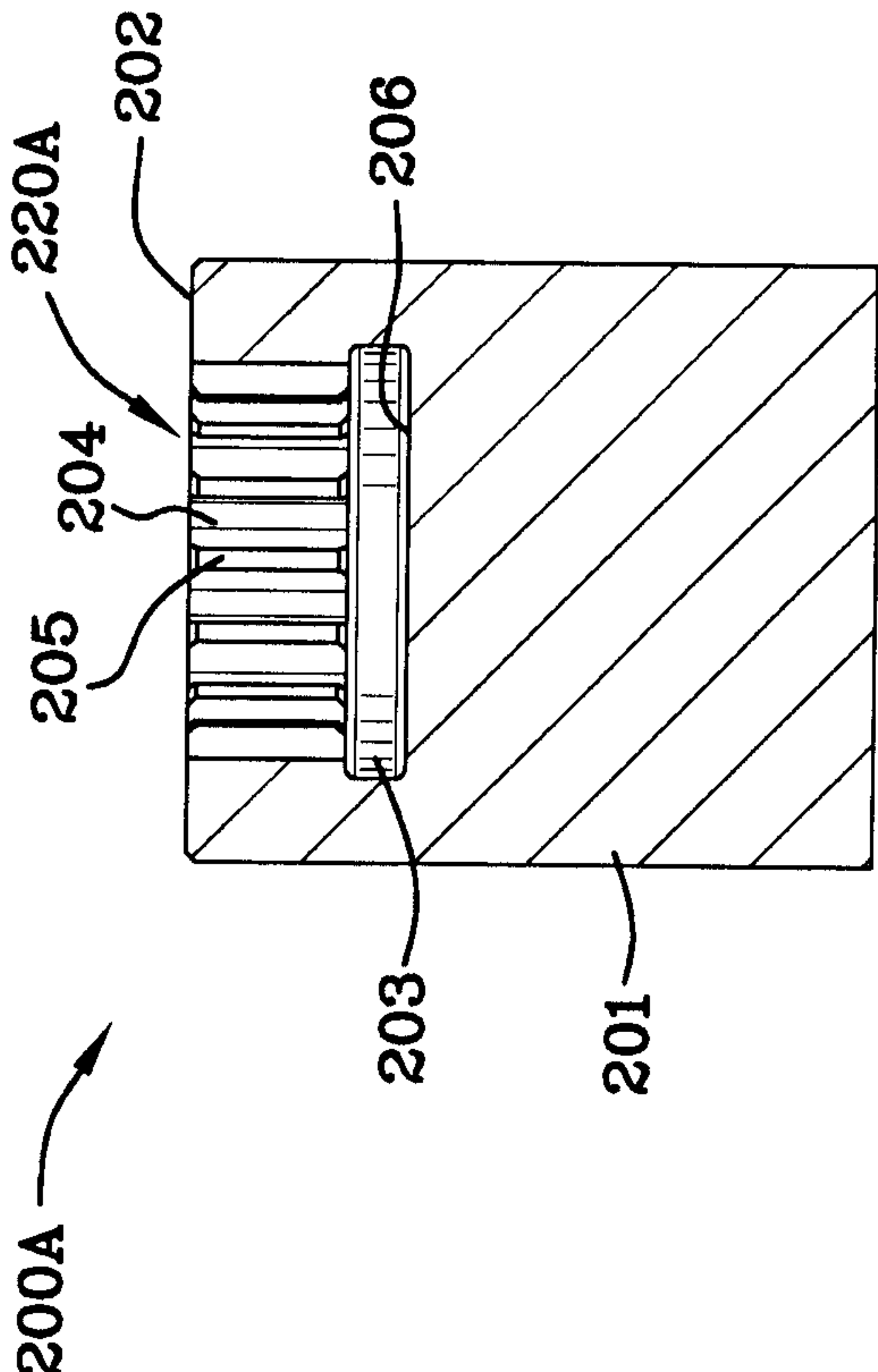
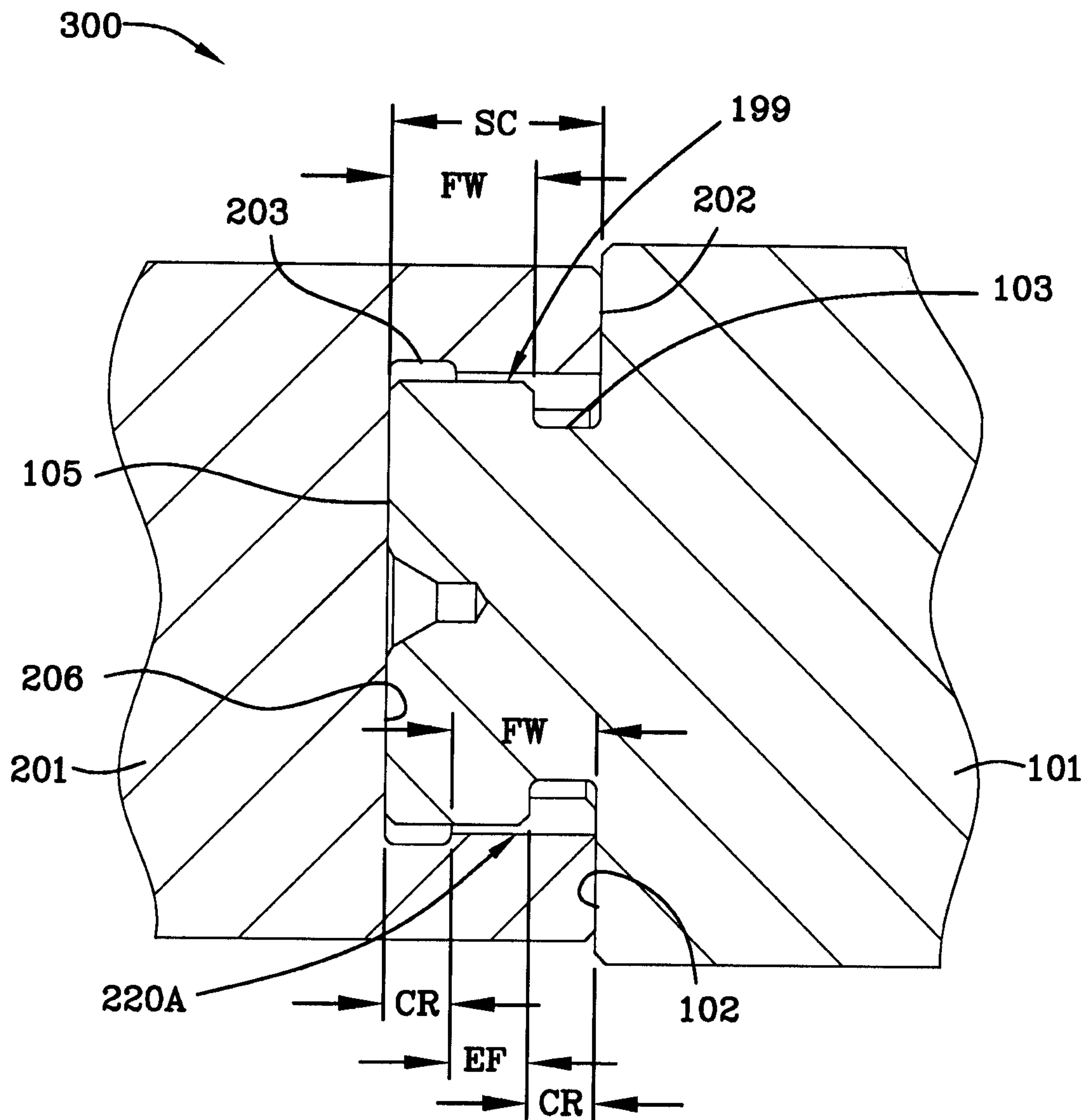


FIG. 2A (Prior Art)



FW = Face Width Length
EF = Effective Face Width Length
CR = Annular Relief Length
SC = Spline Connection Length

$$EF = SC - 2CR$$

$$SC = FW + CR$$

FIG. 3 (Prior Art)

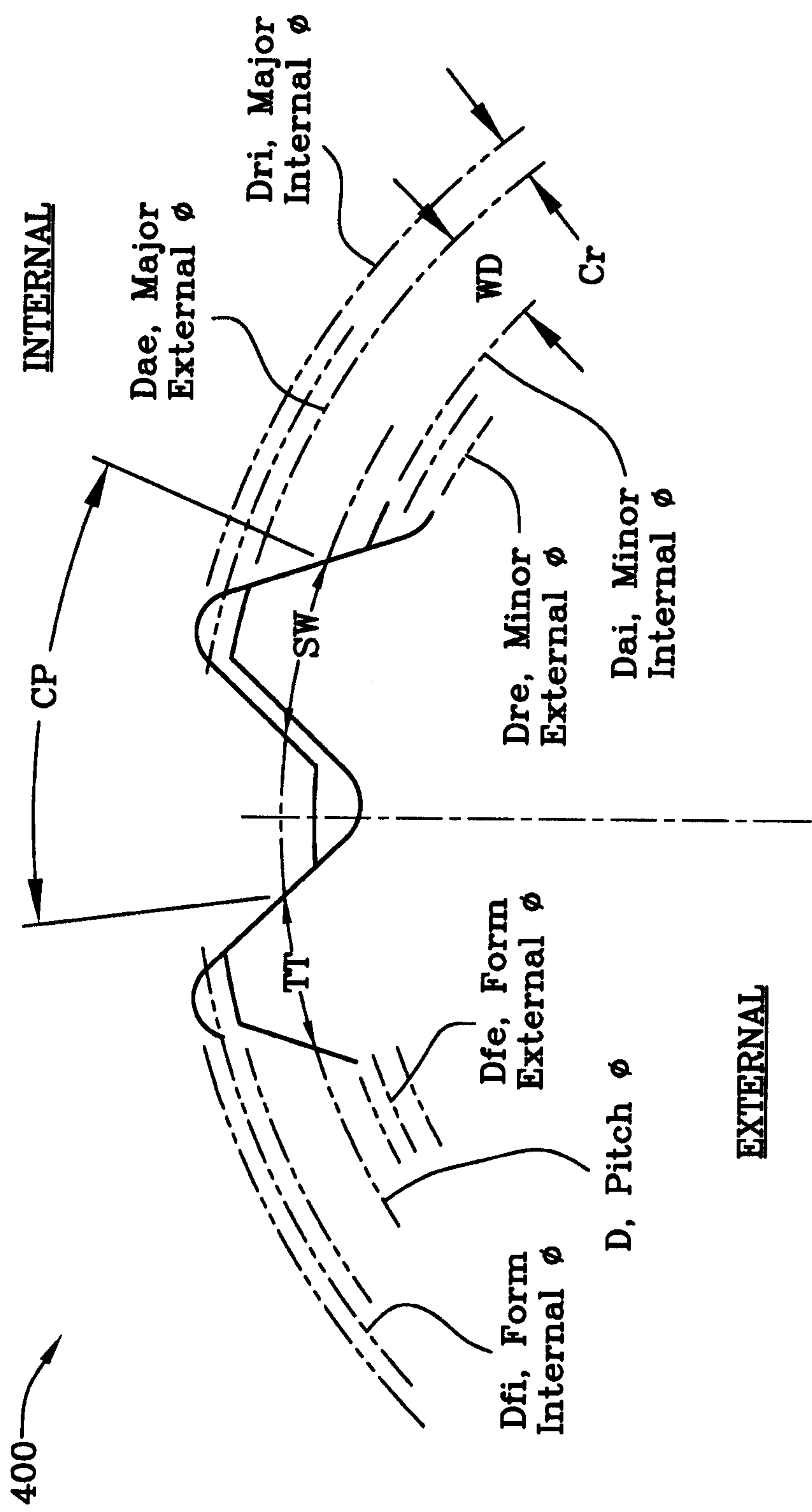


FIG. 4

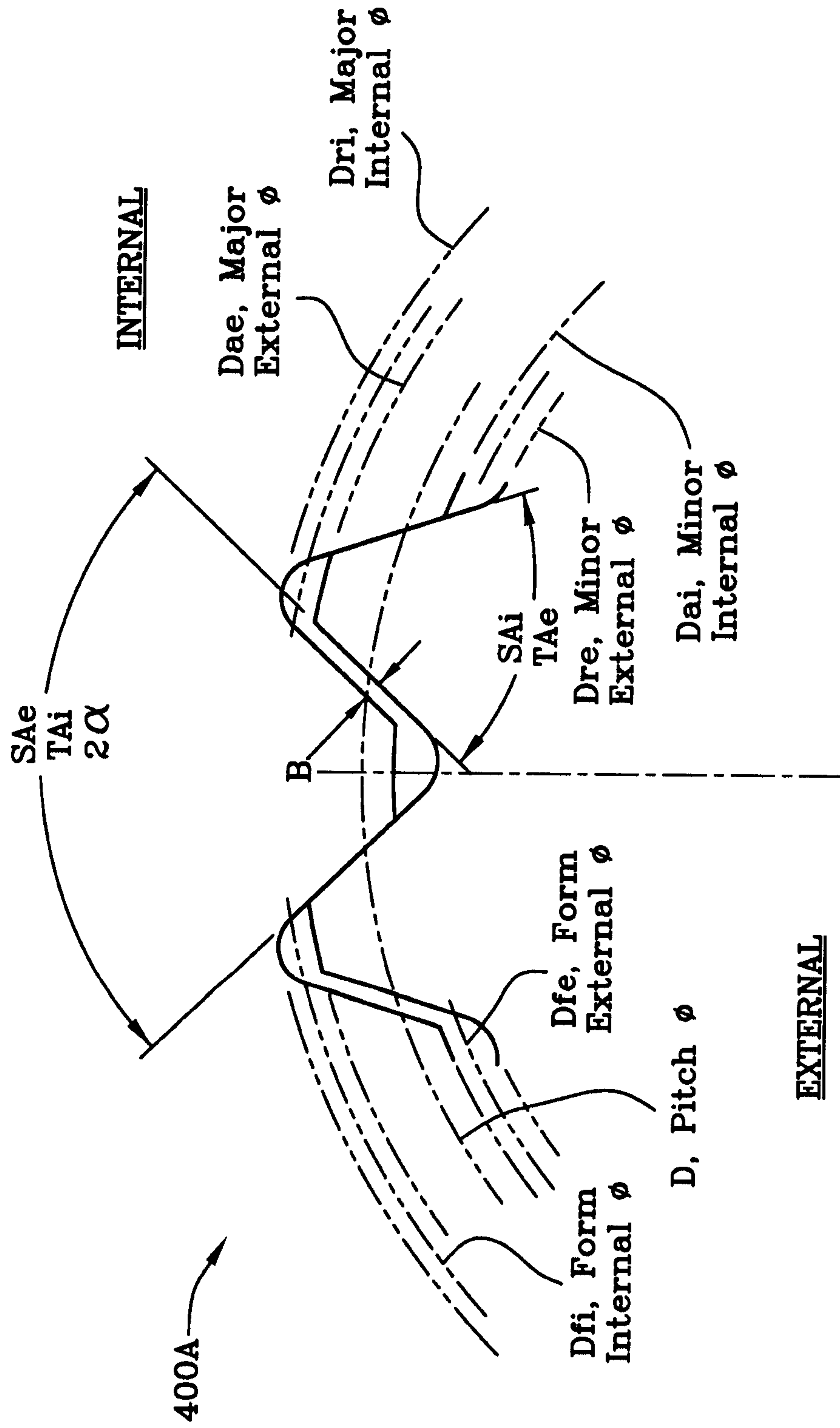


FIG. 4A

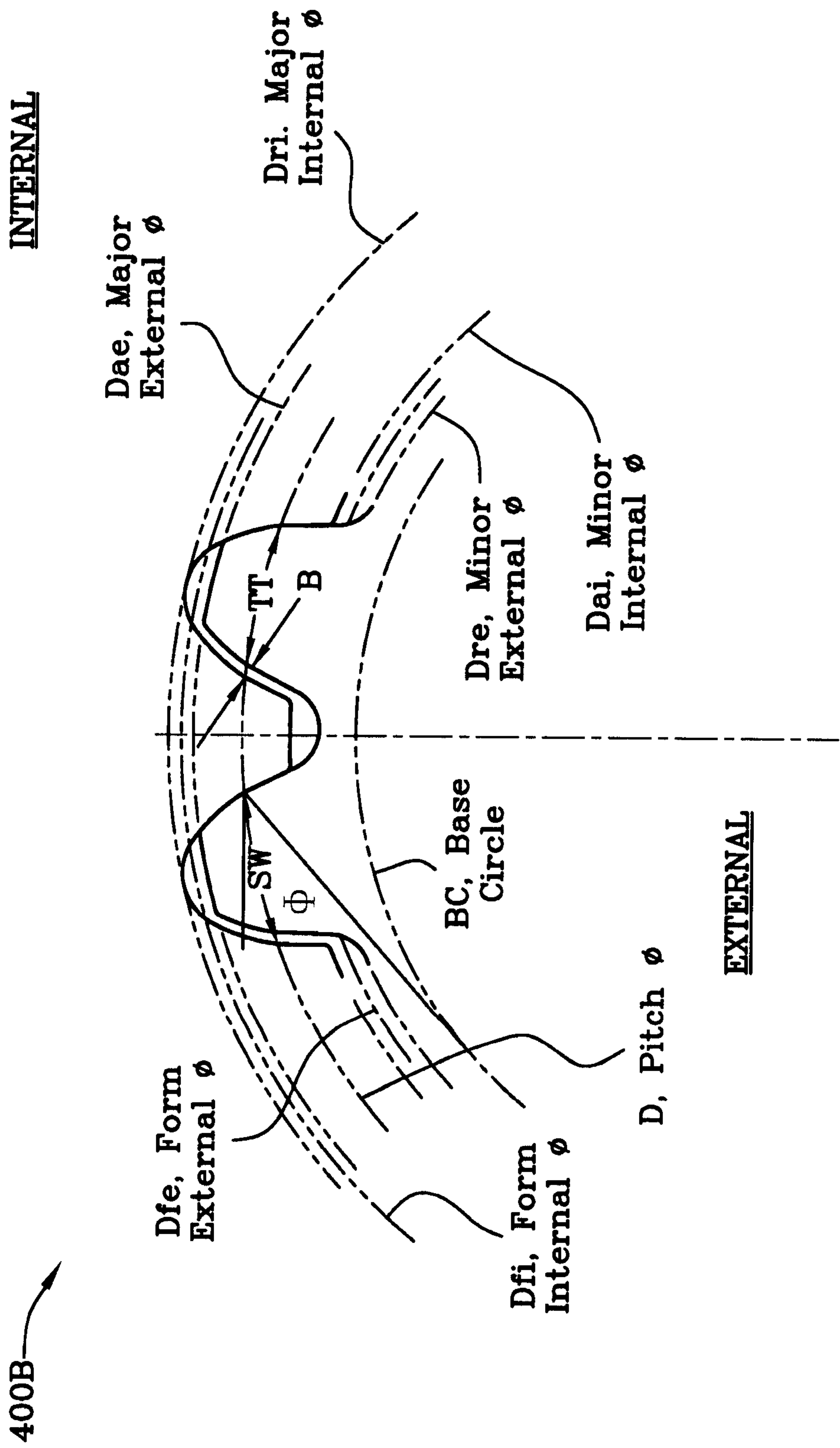


FIG. 4B

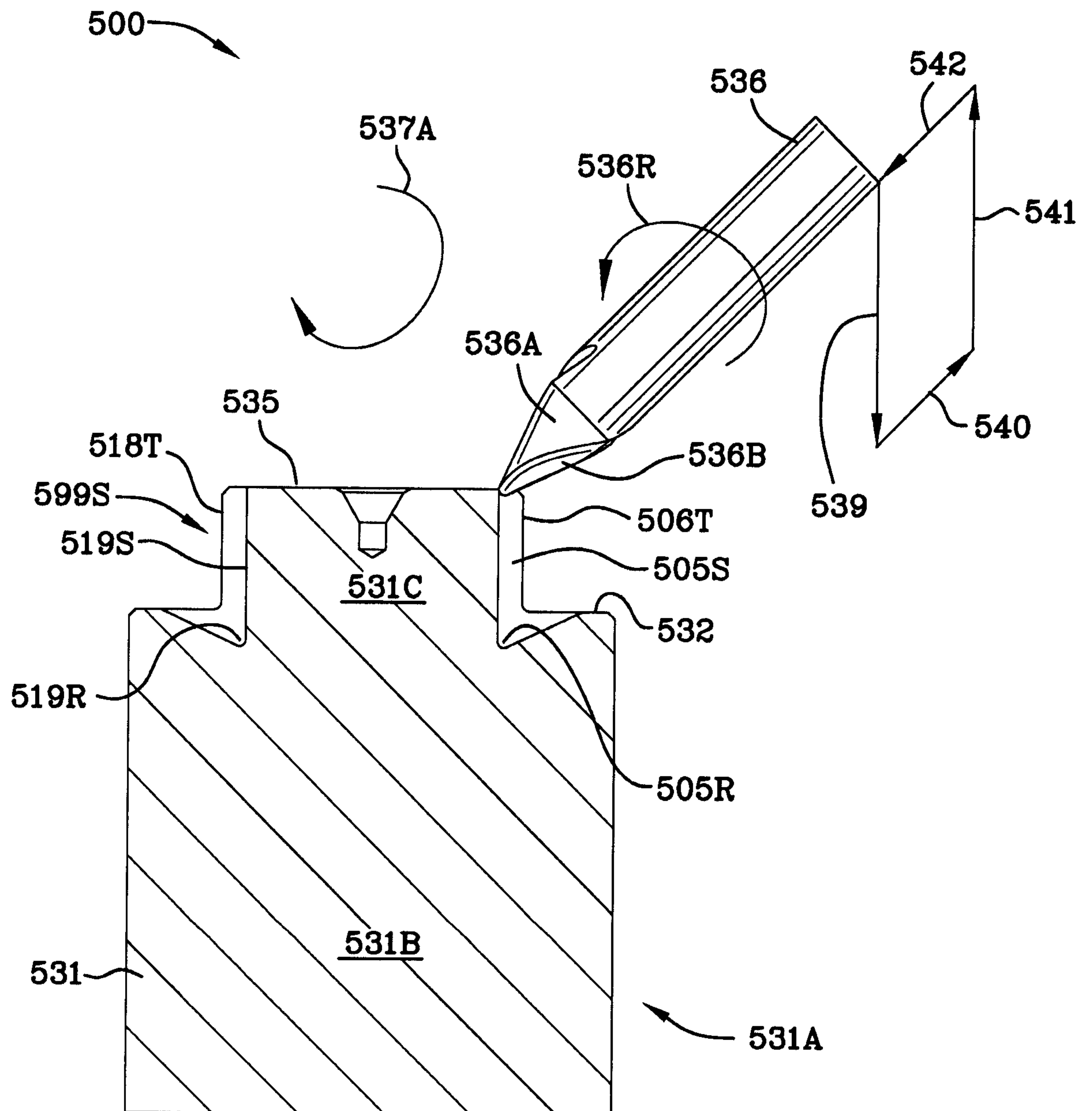


FIG. 5

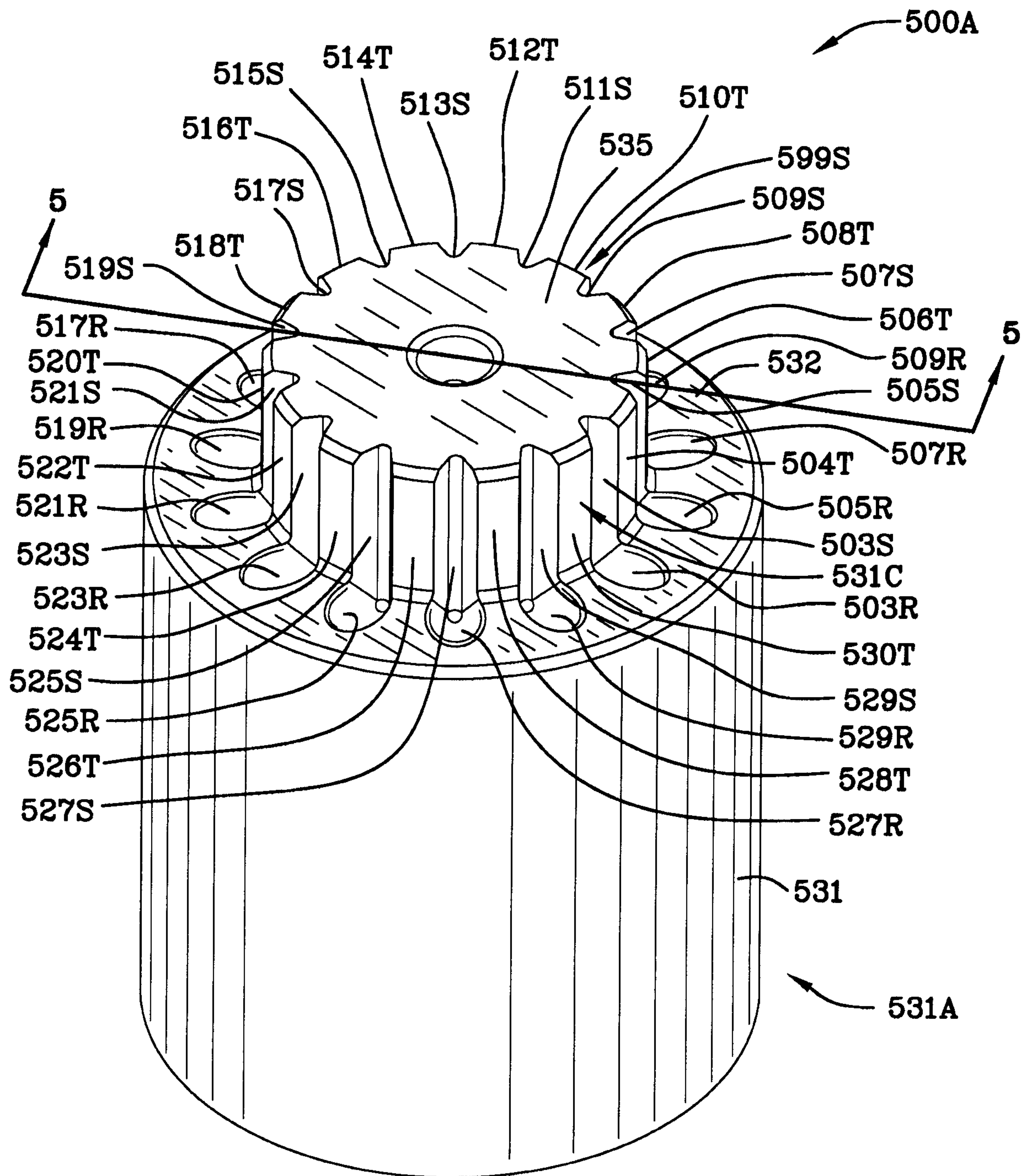


FIG. 5A

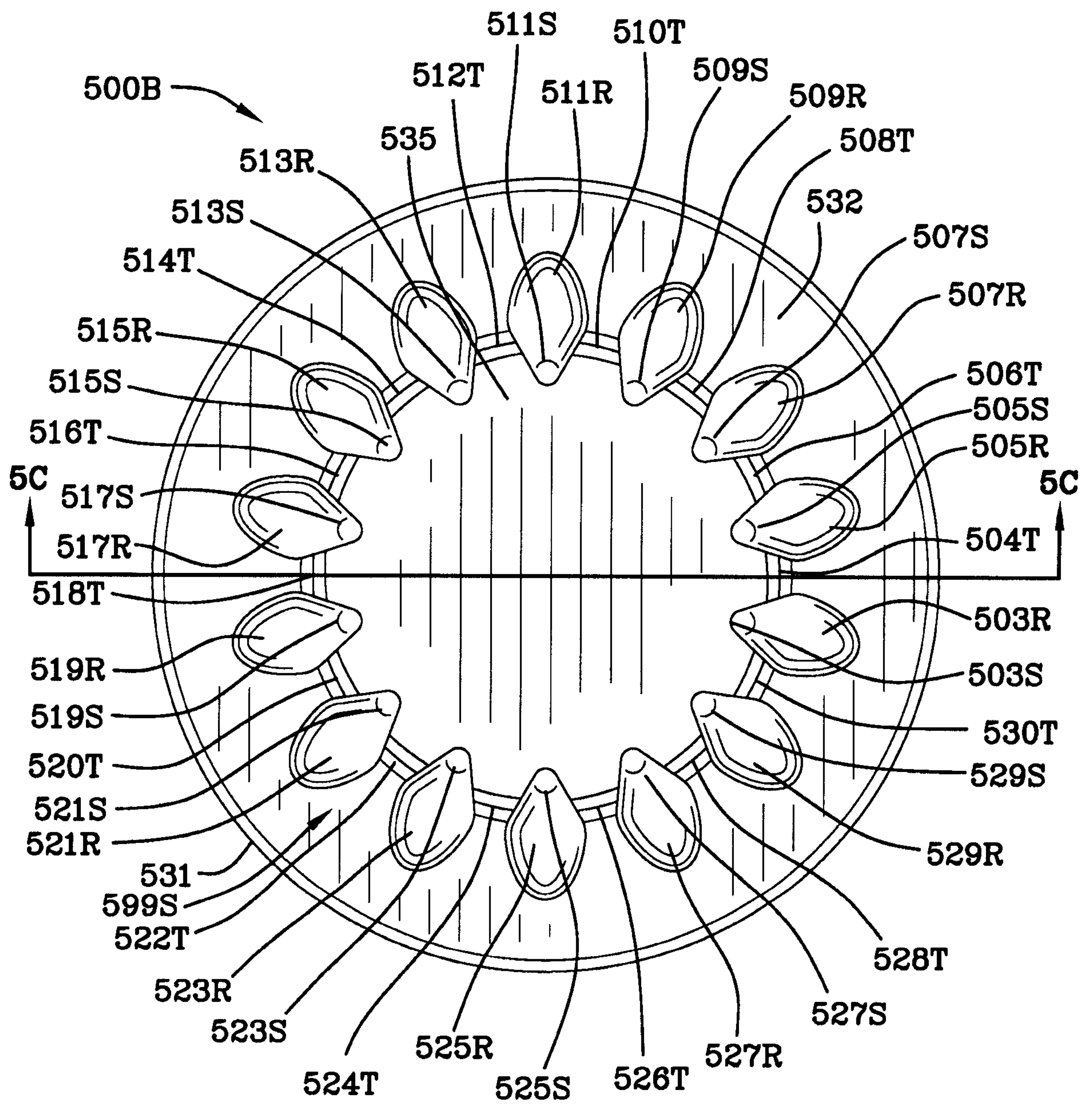


FIG. 5B

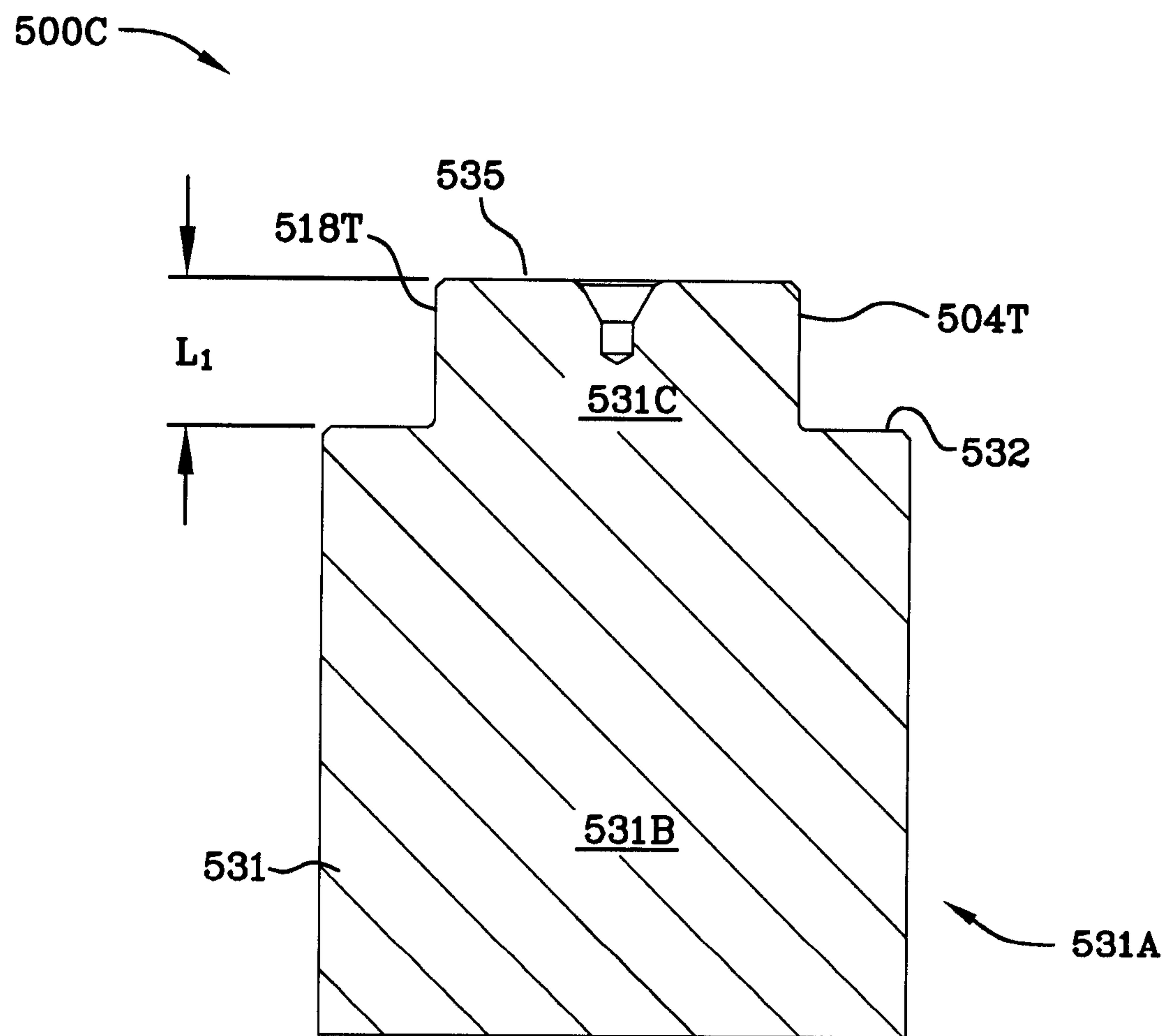


FIG. 5C

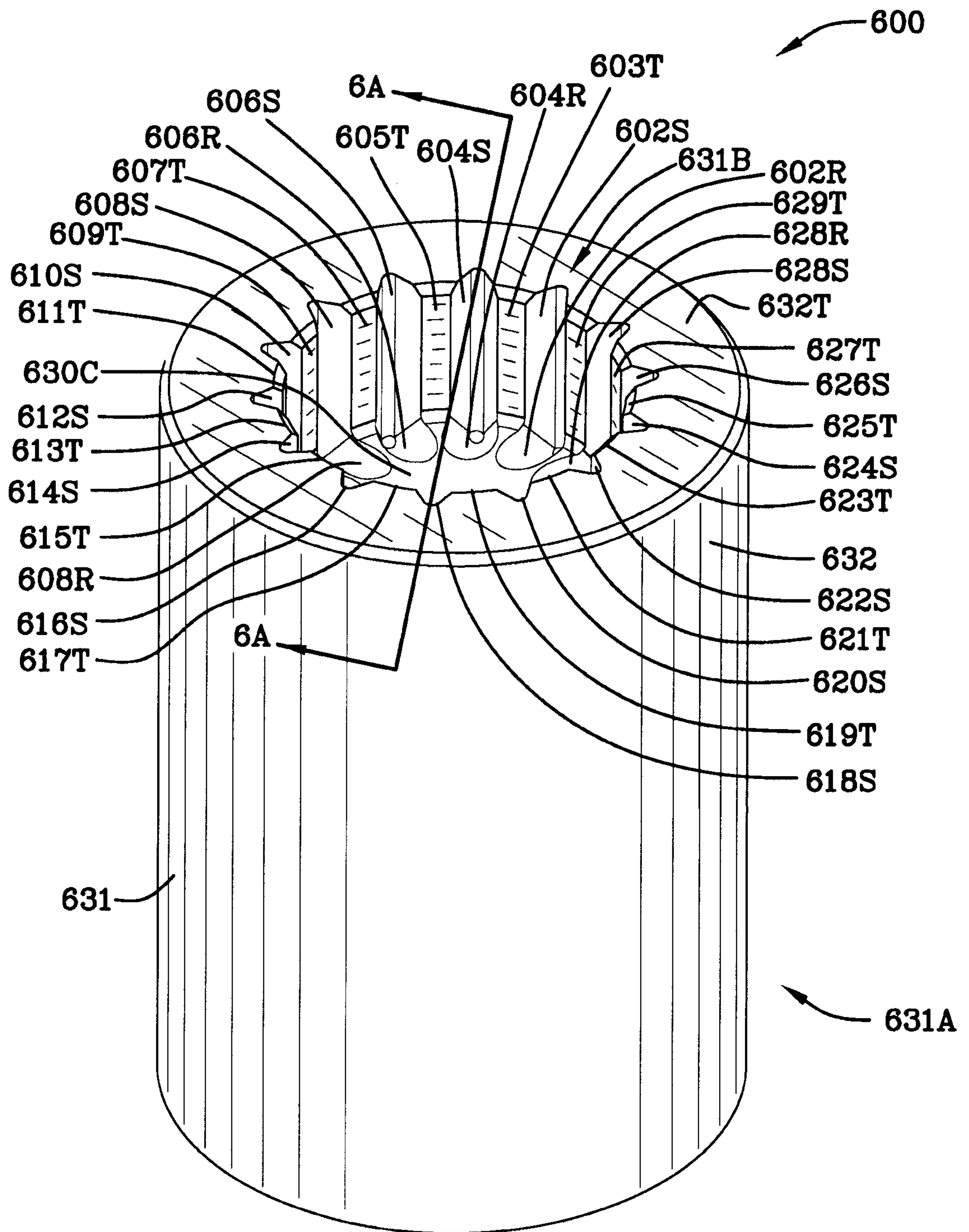


FIG. 6

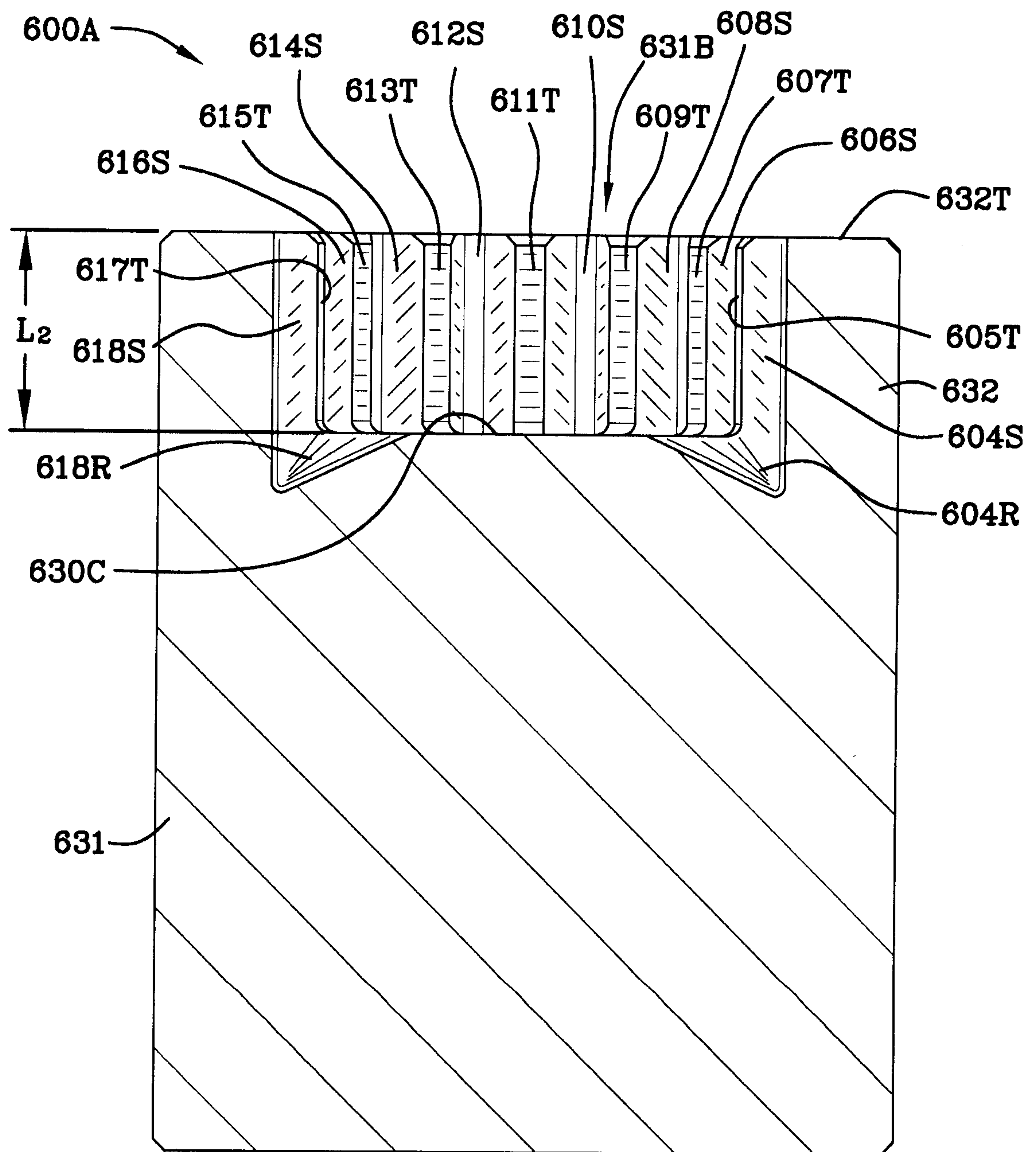


FIG. 6A

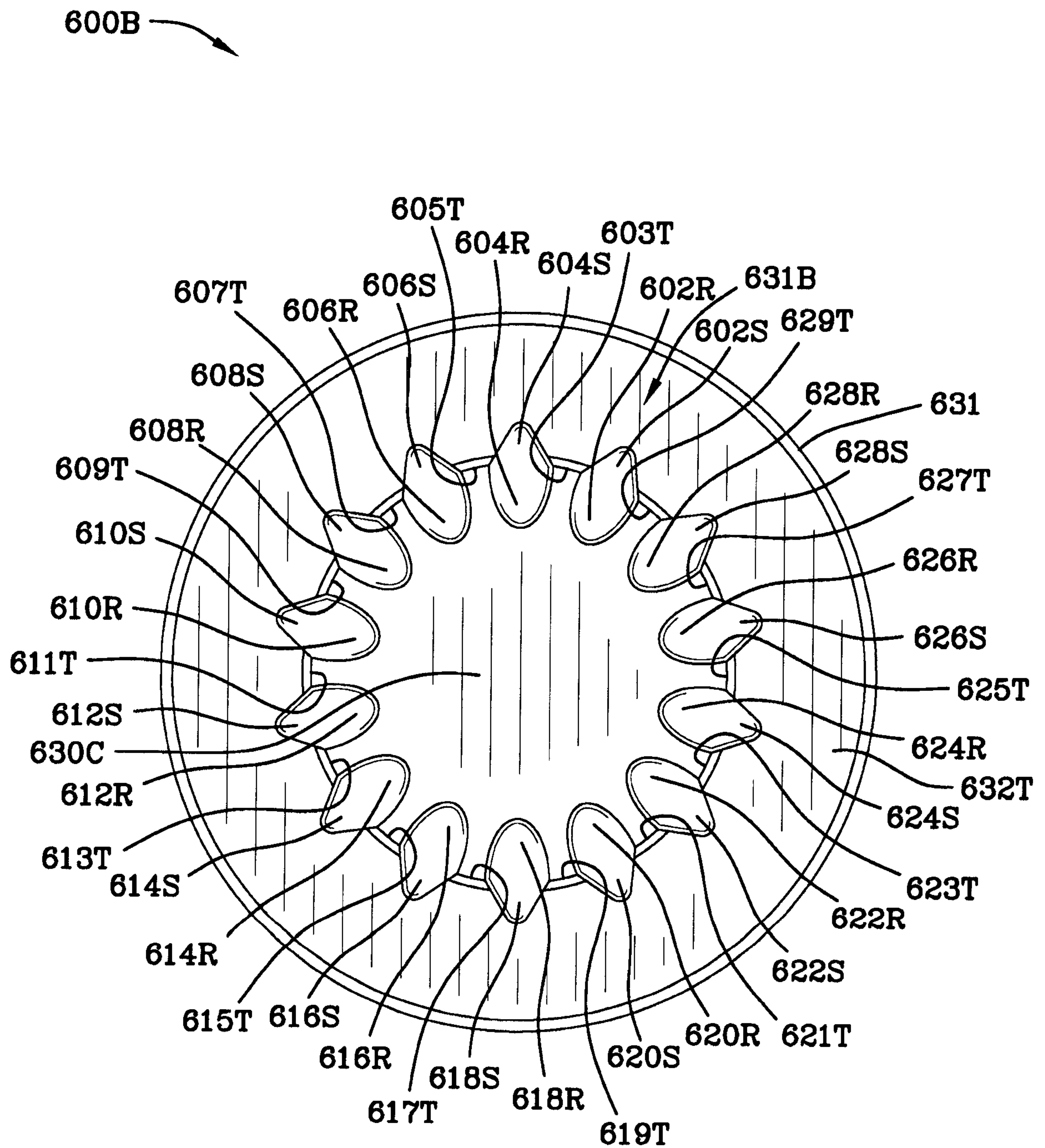
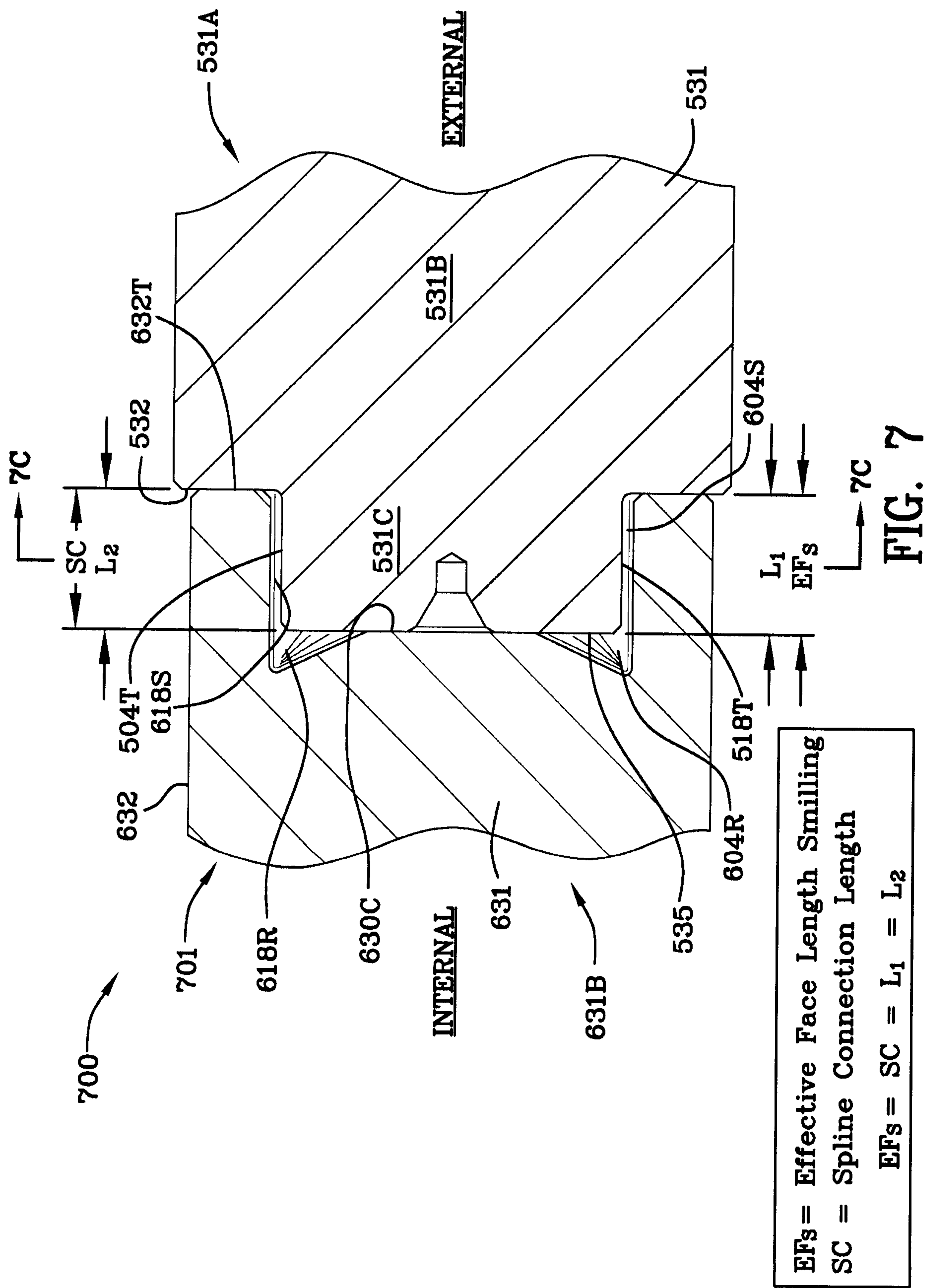


FIG. 6B



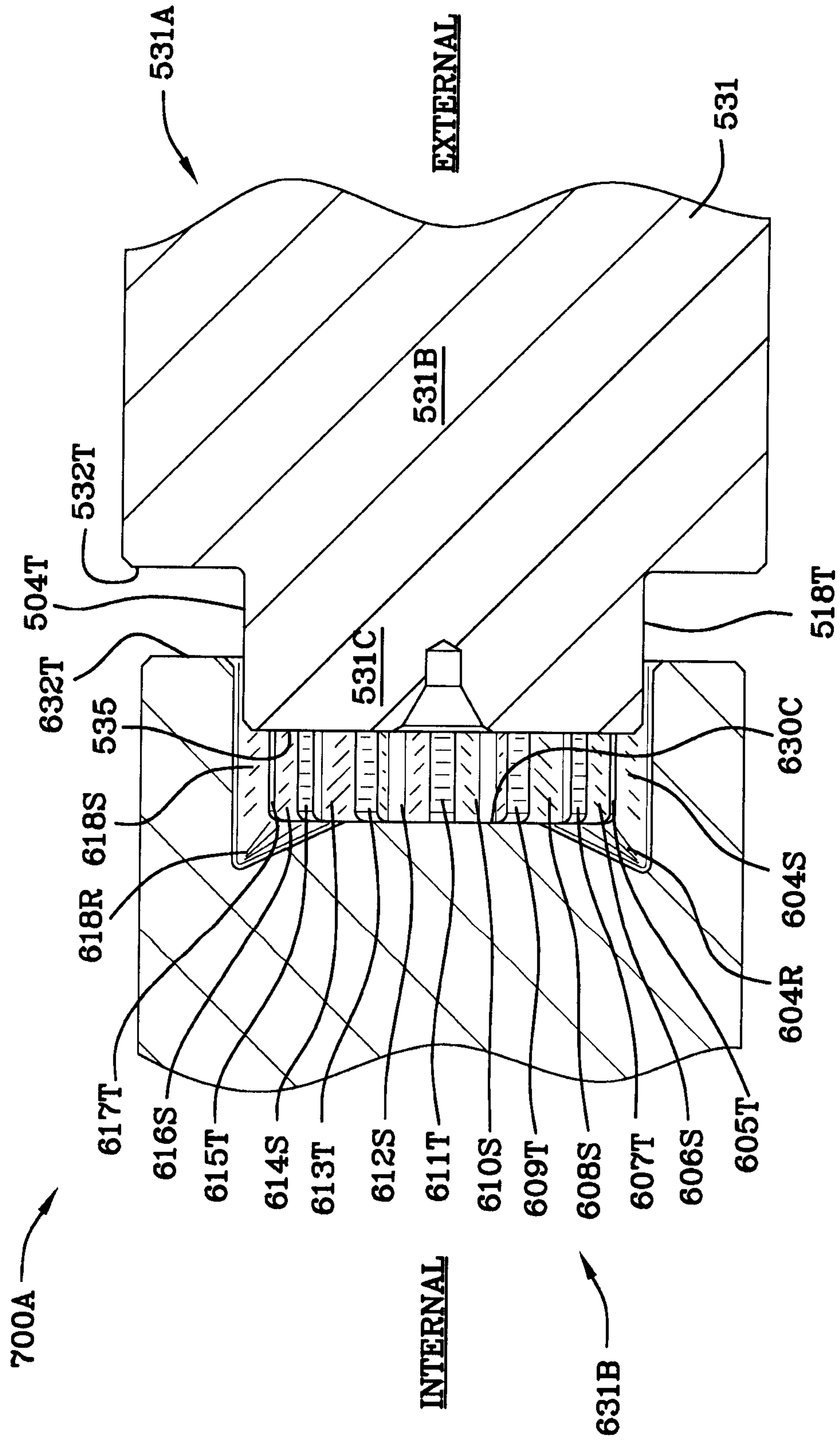


FIG. 7A

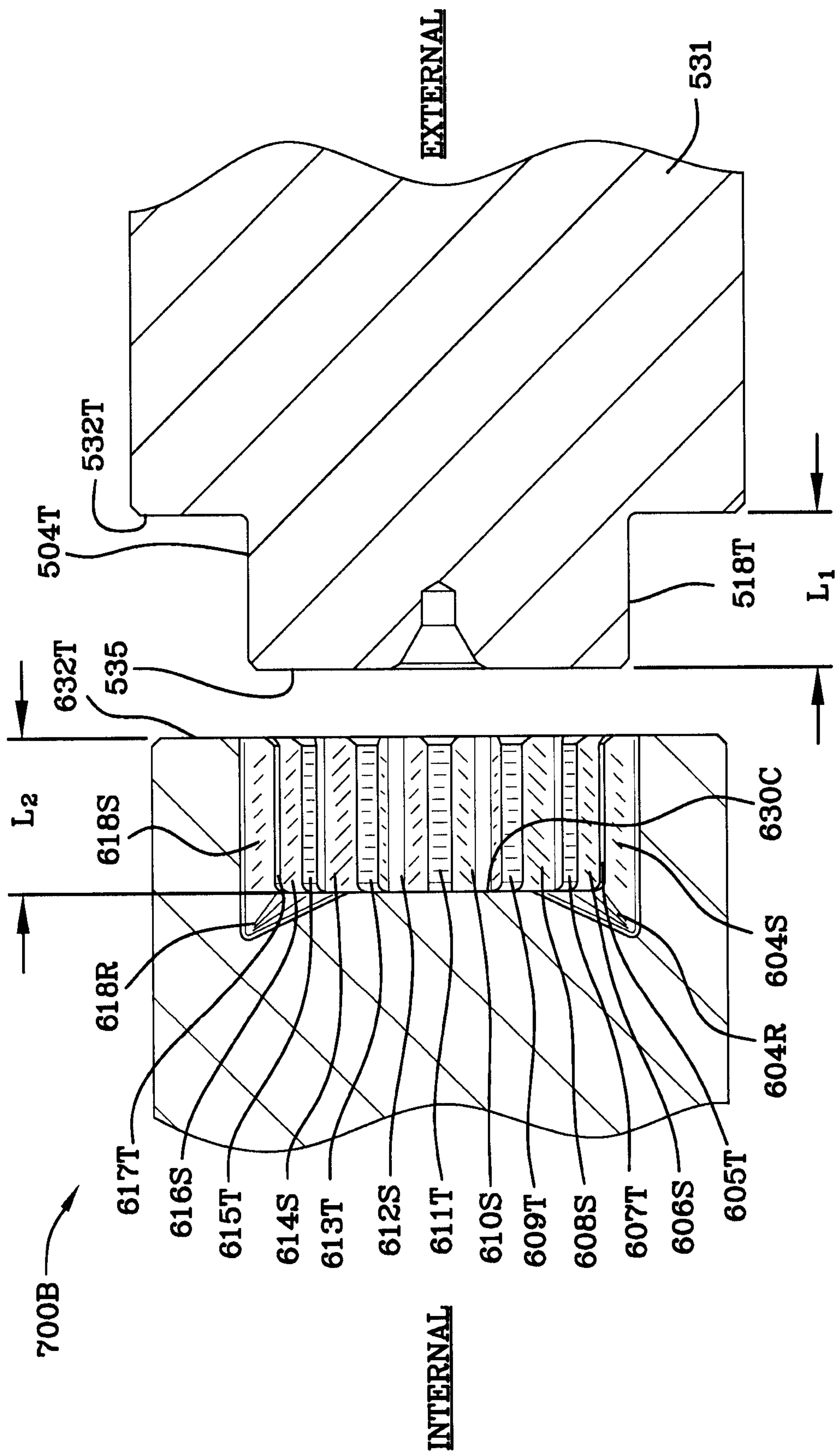


FIG. 7B

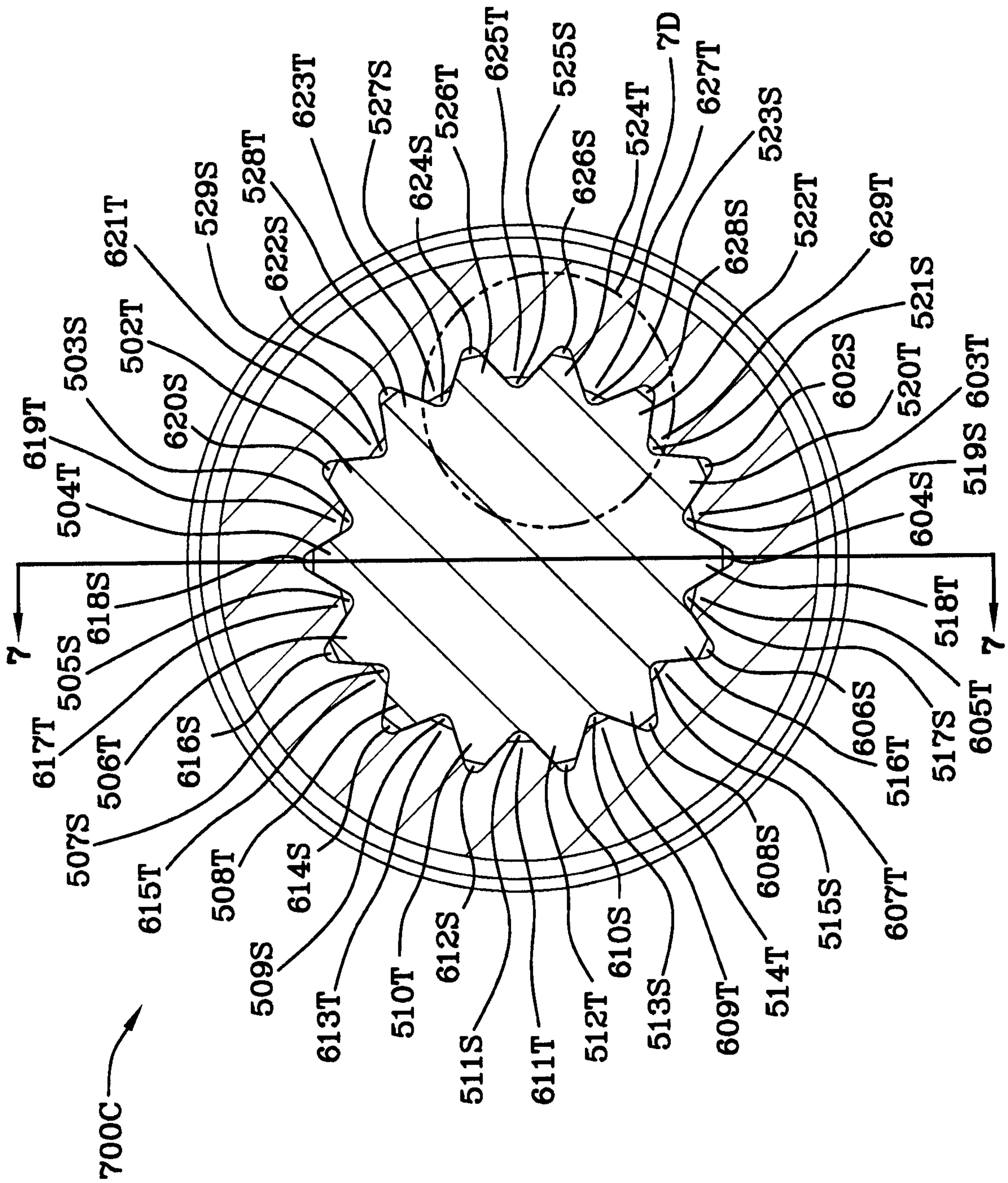
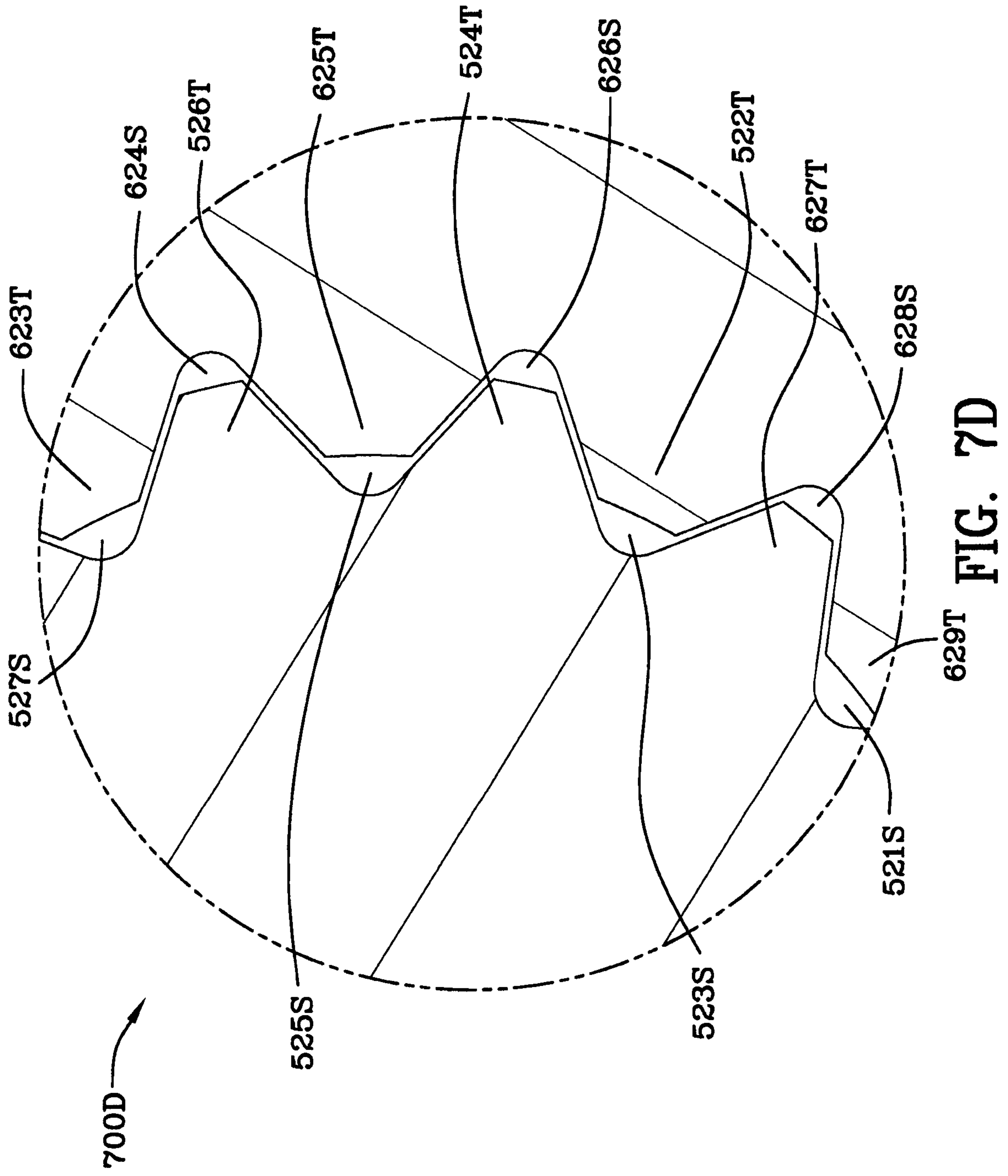
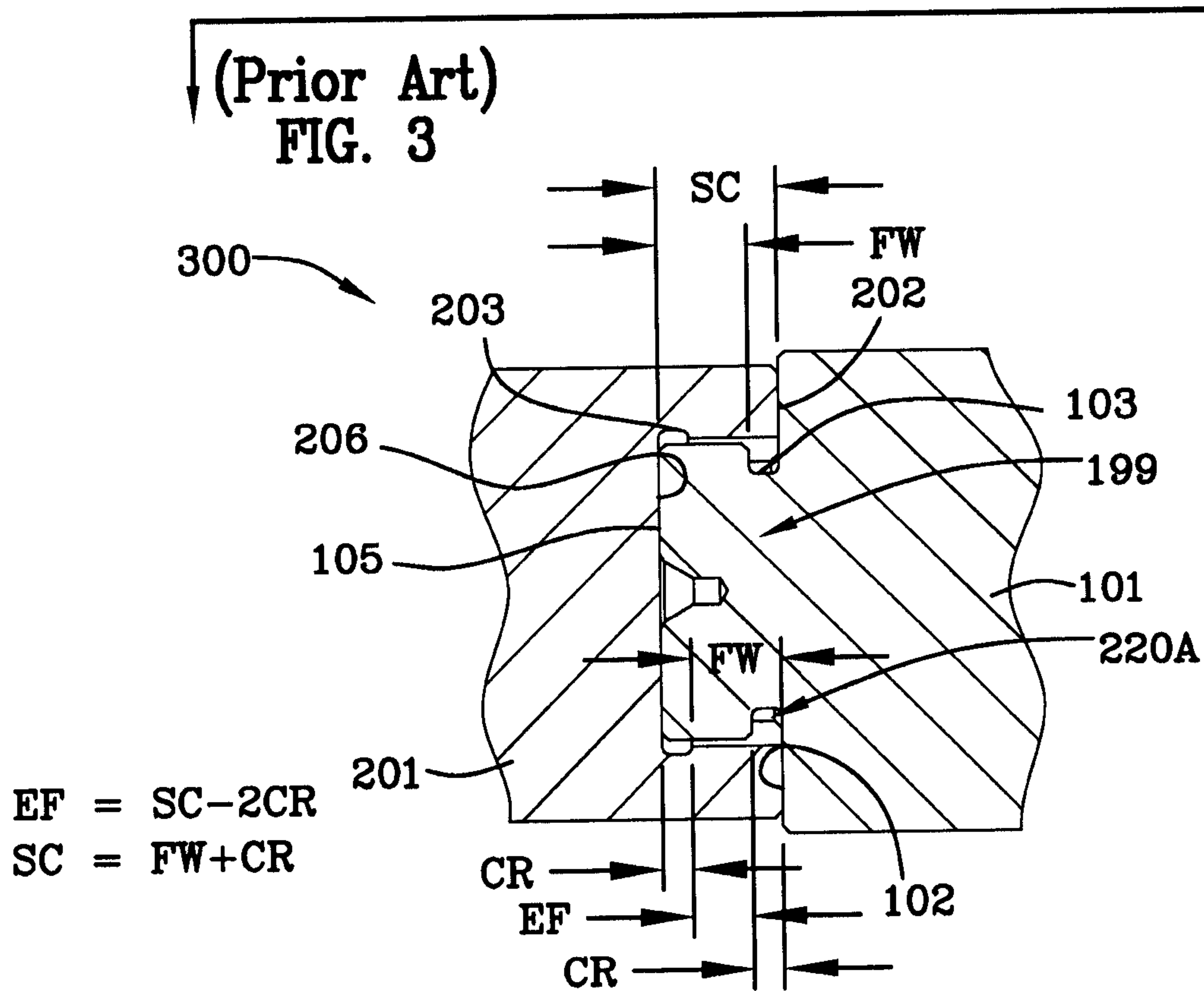
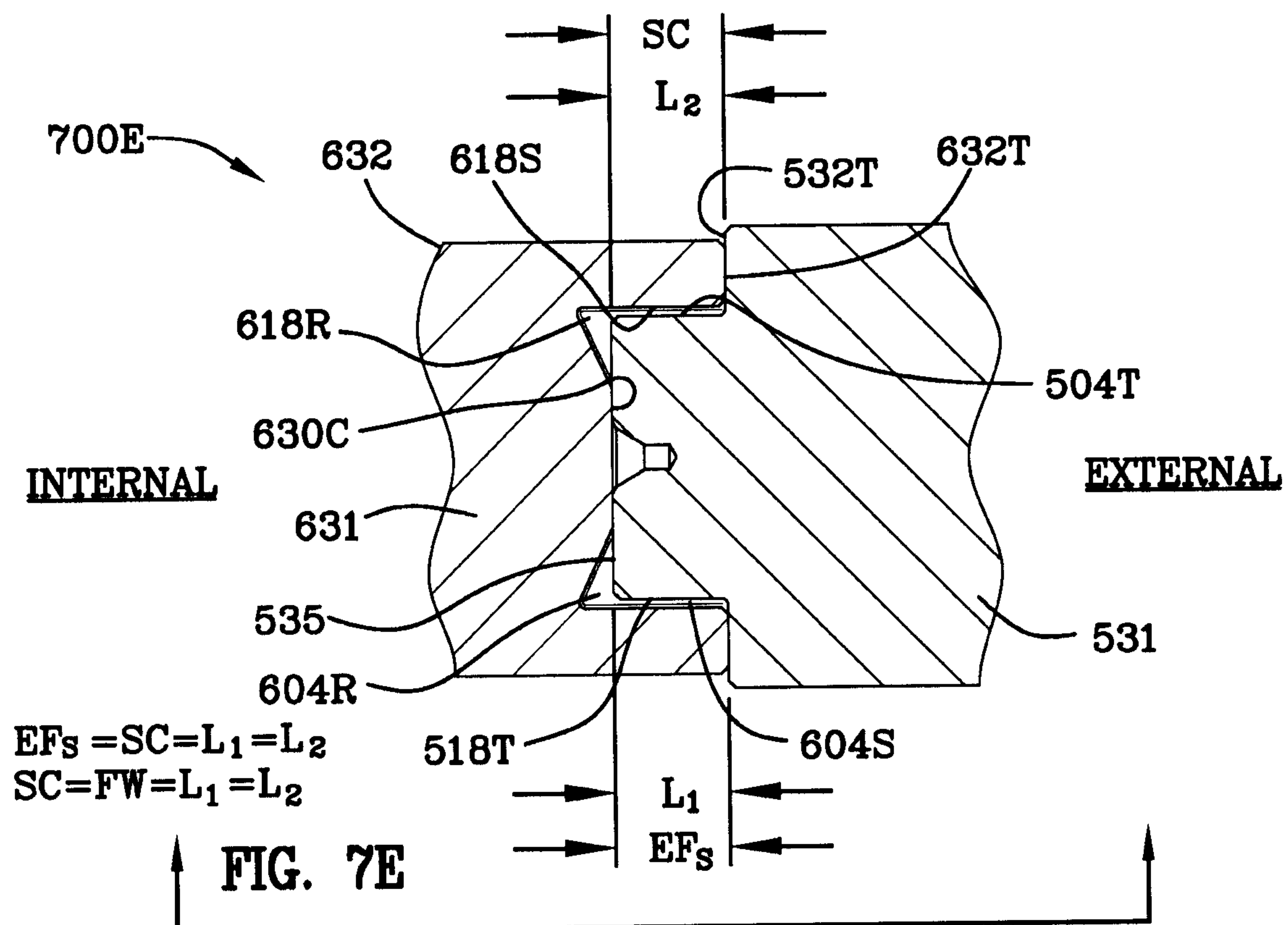


FIG. 7C





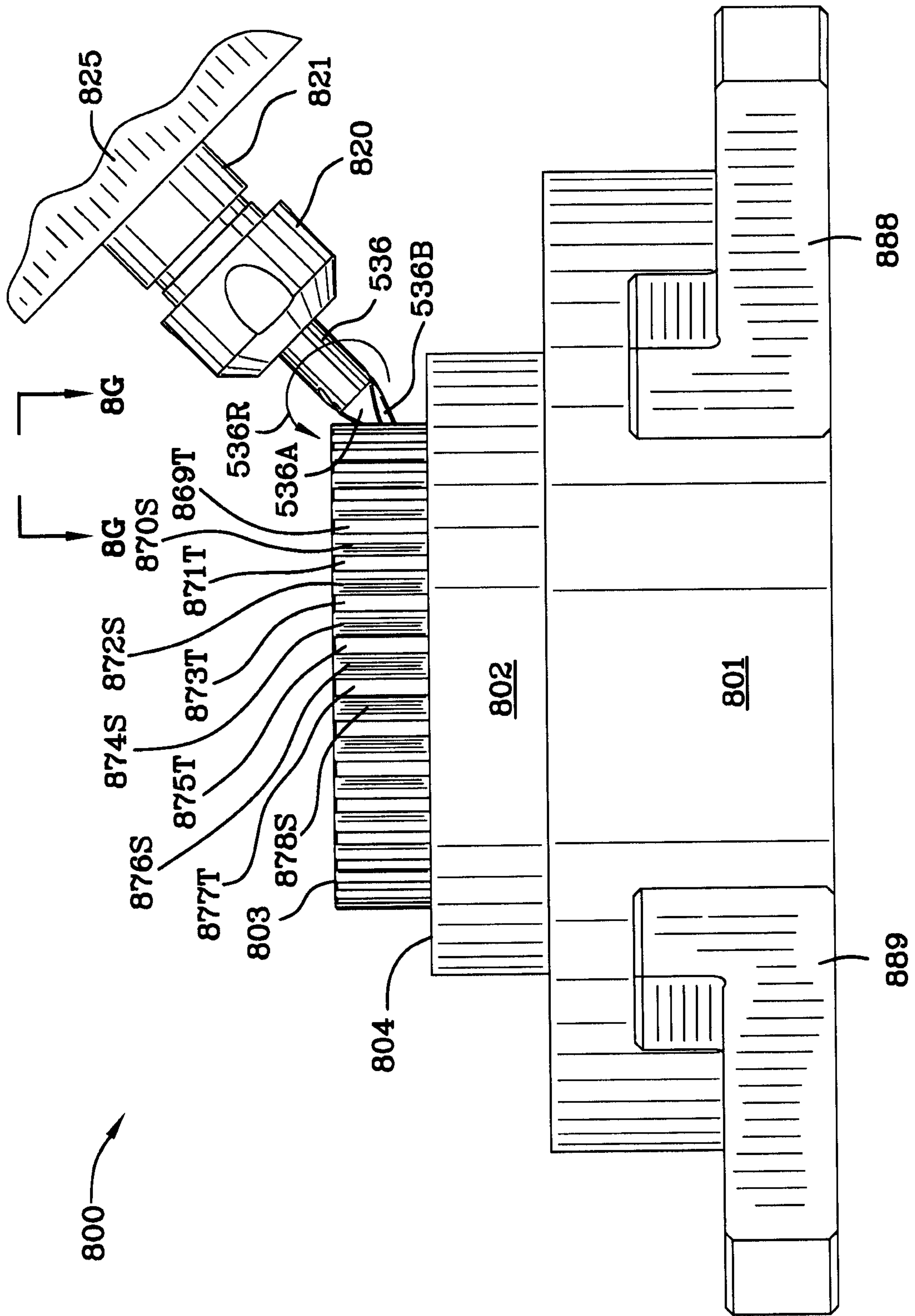


FIG. 8

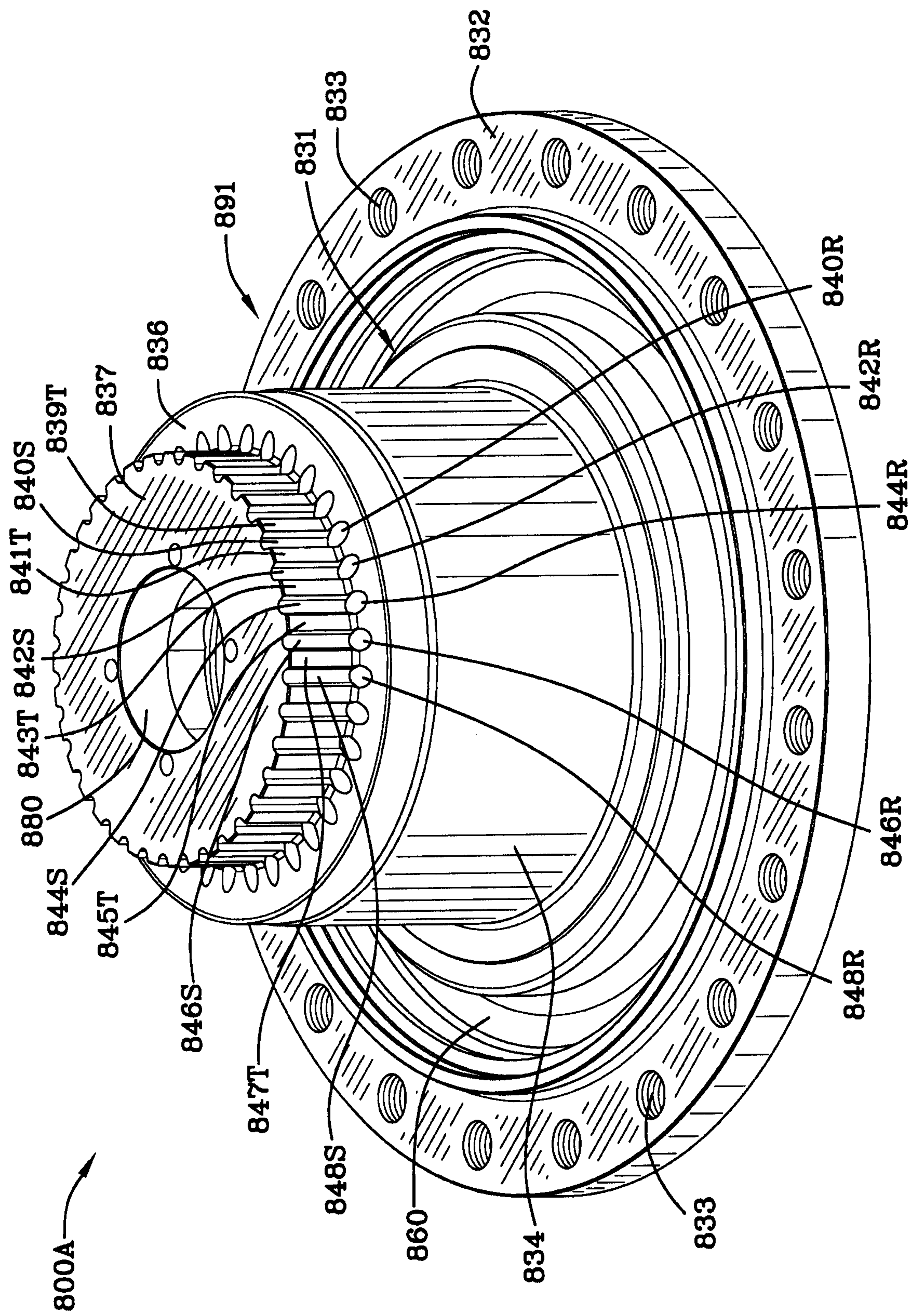


FIG. 8A

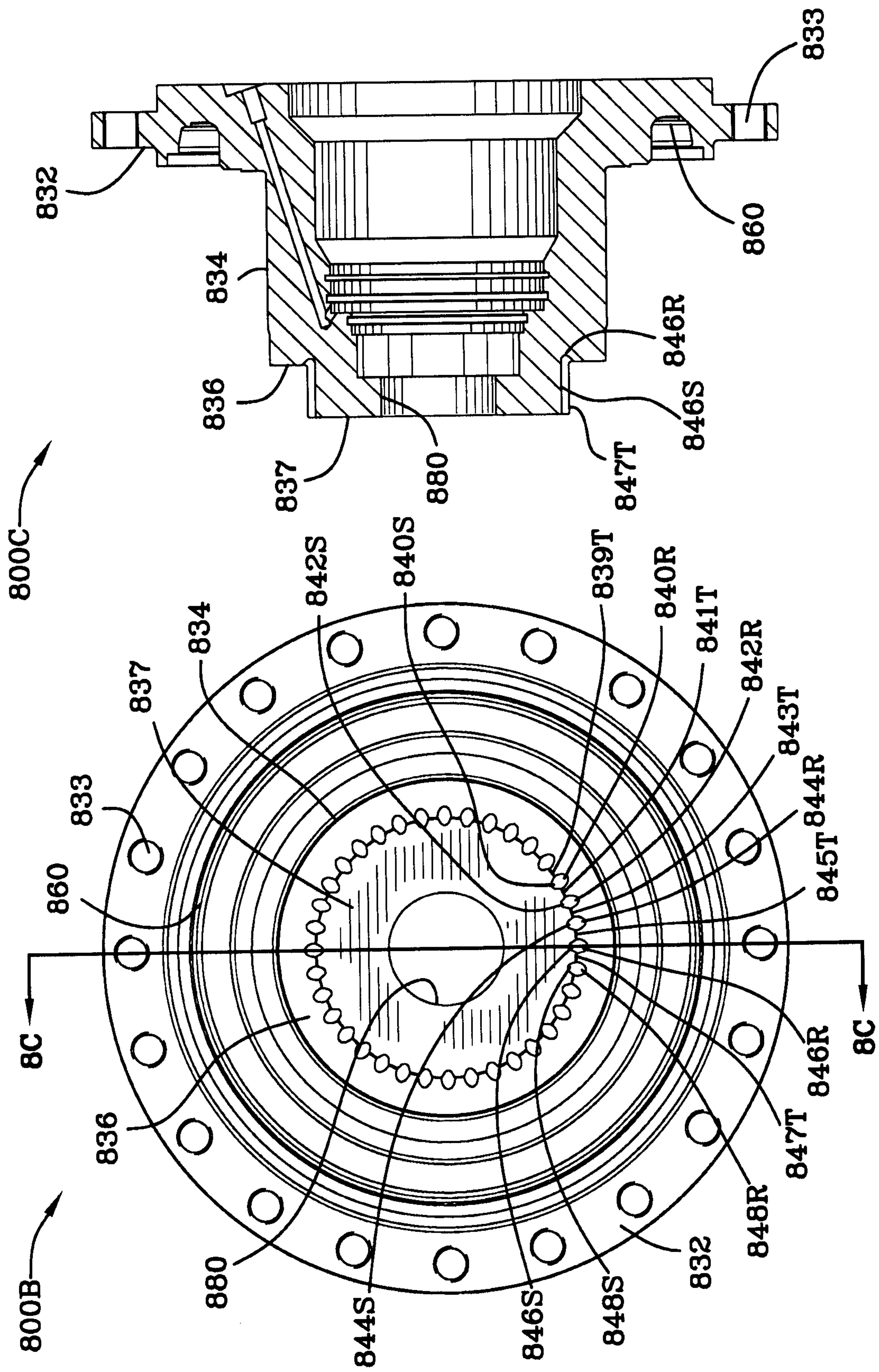


FIG. 8C

FIG. 8B

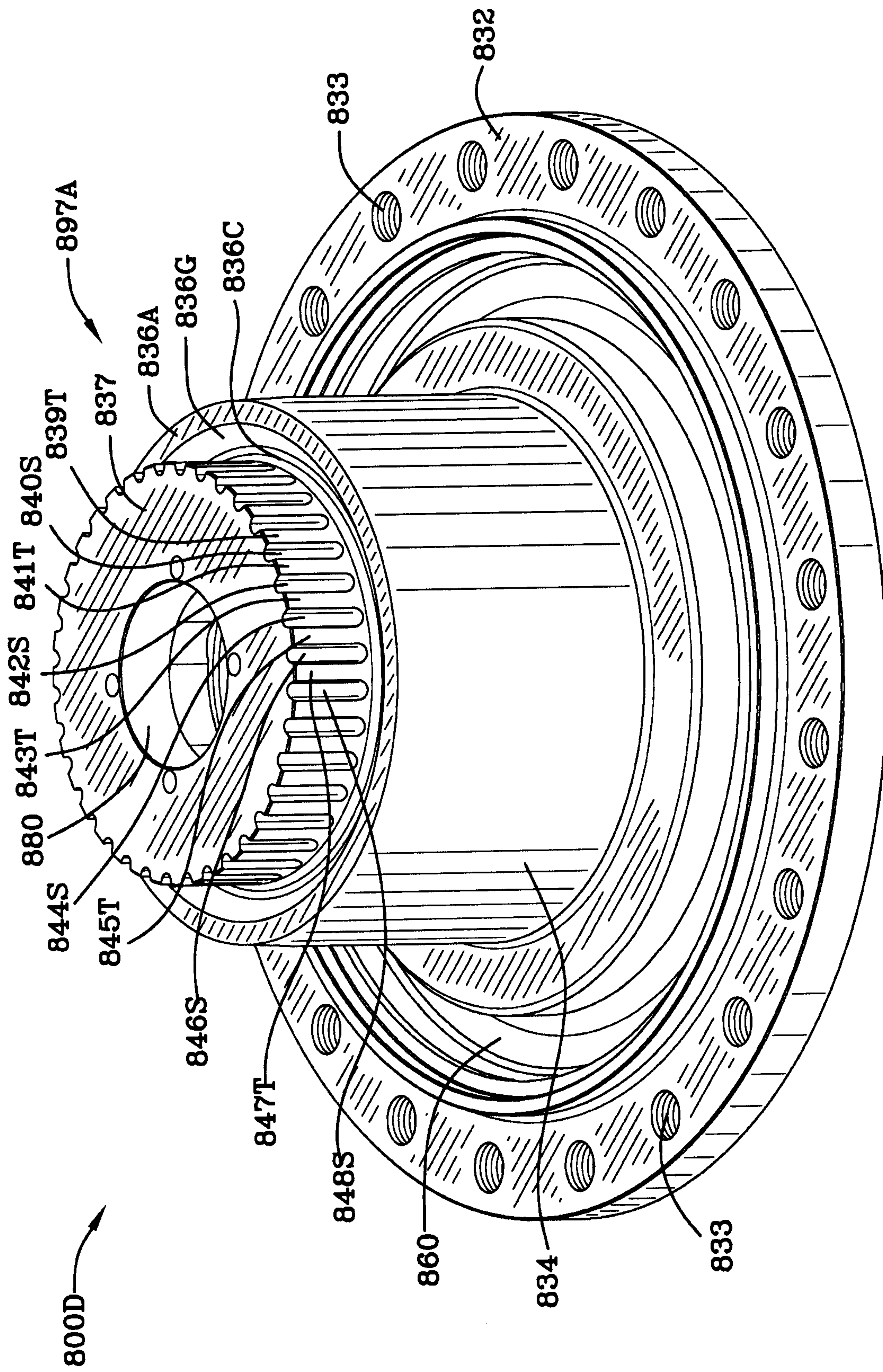


FIG. 8D

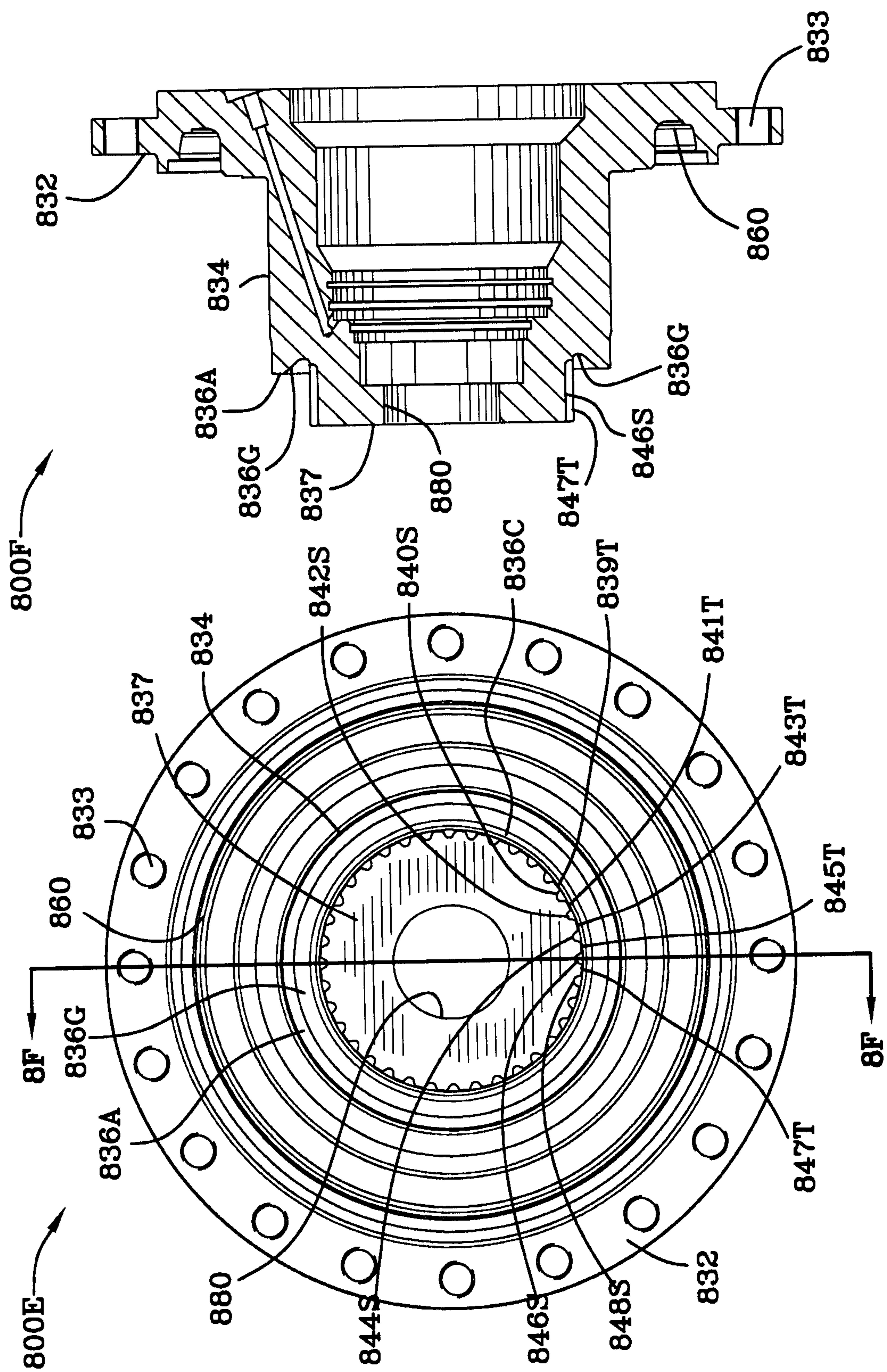


FIG. 8F

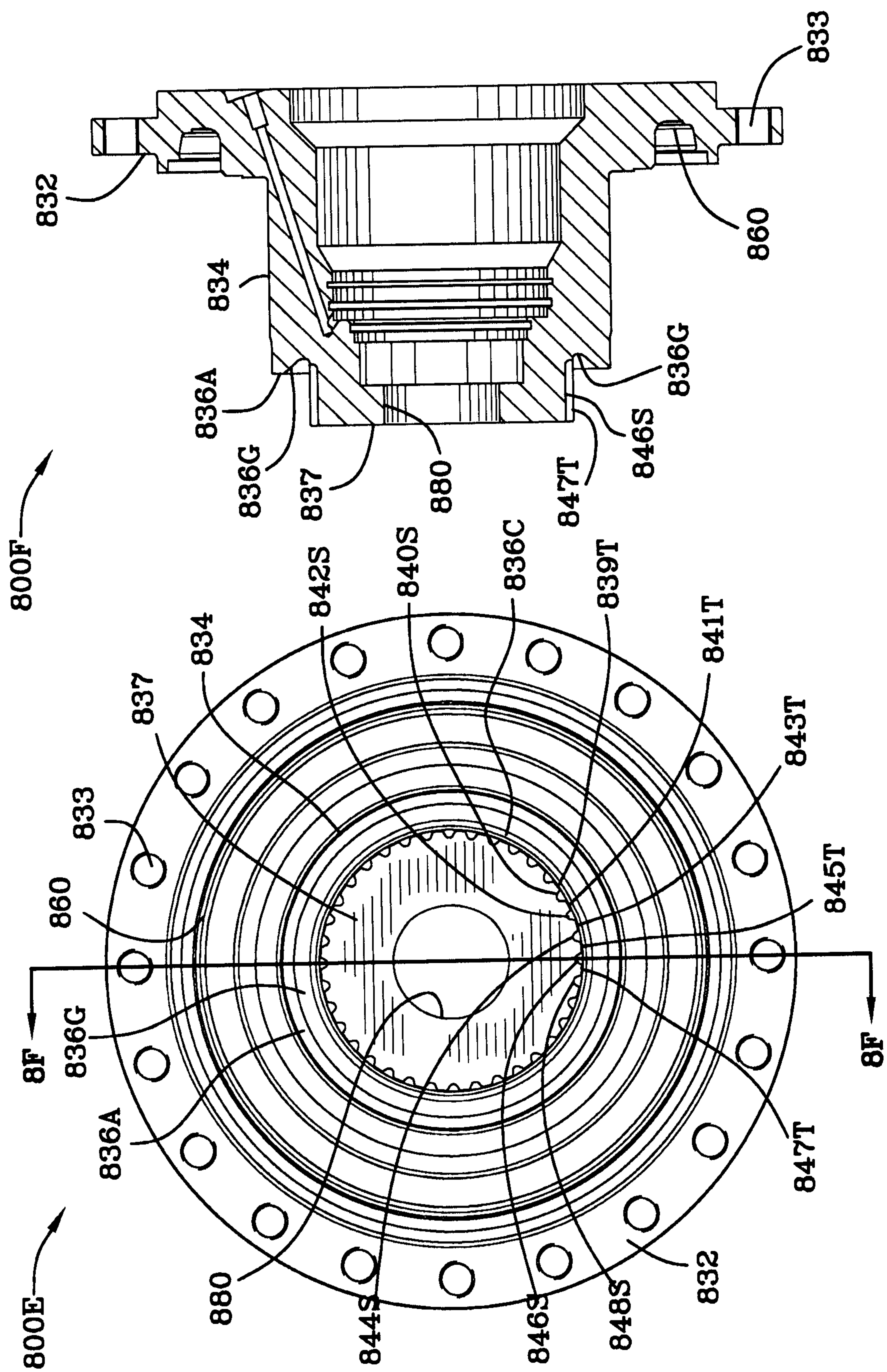


FIG. 8E

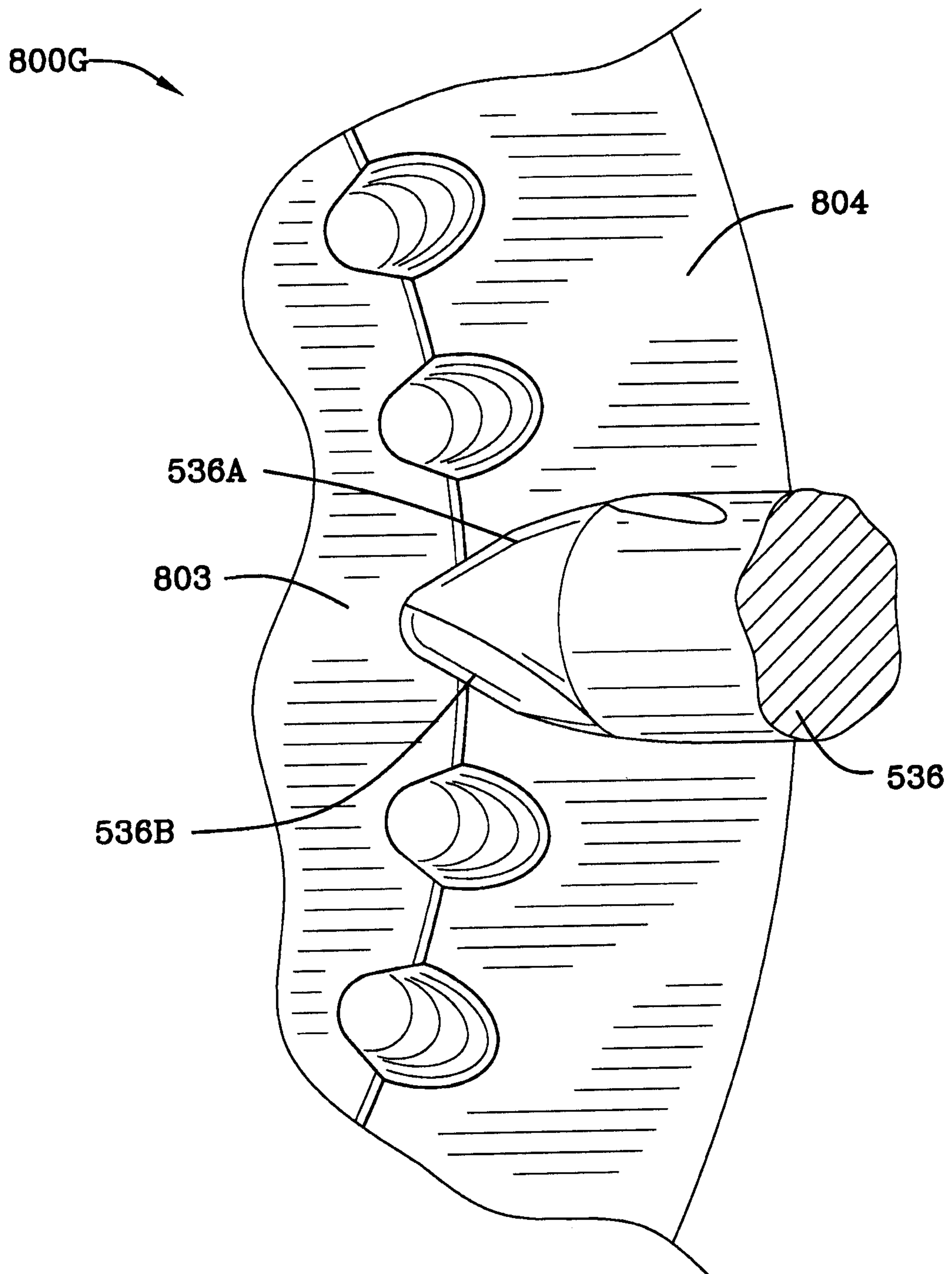


FIG. 8G

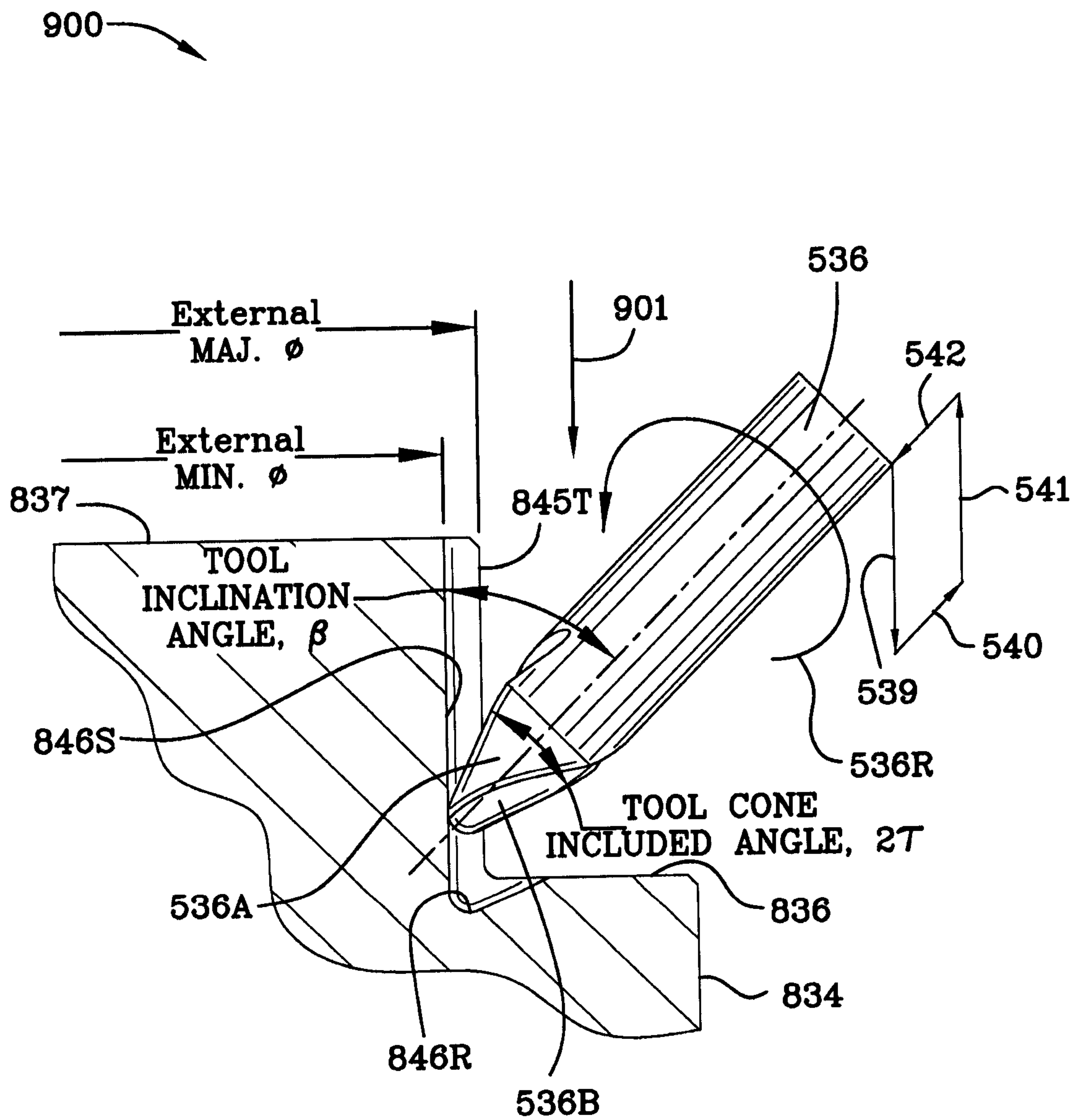


FIG. 9

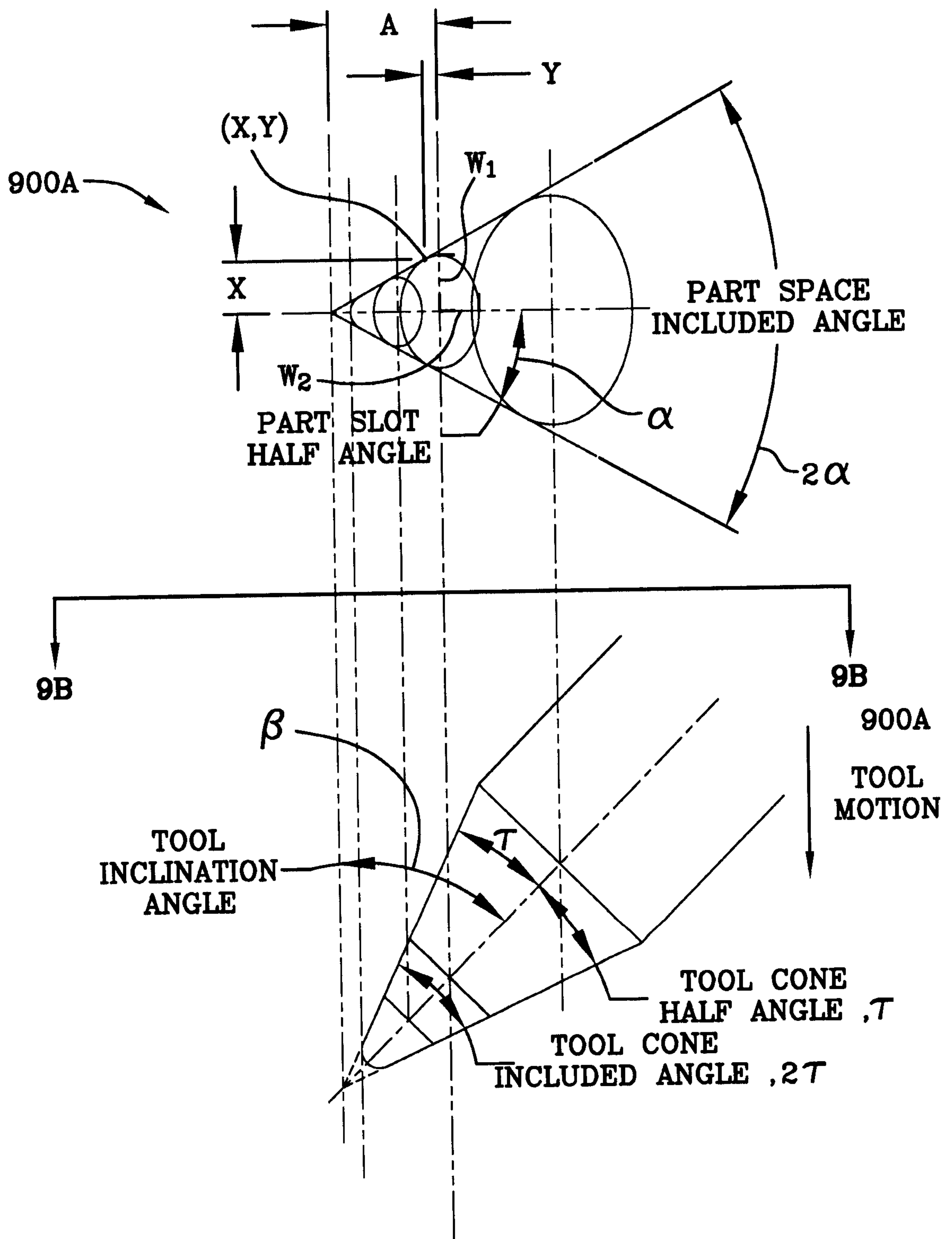


FIG. 9A

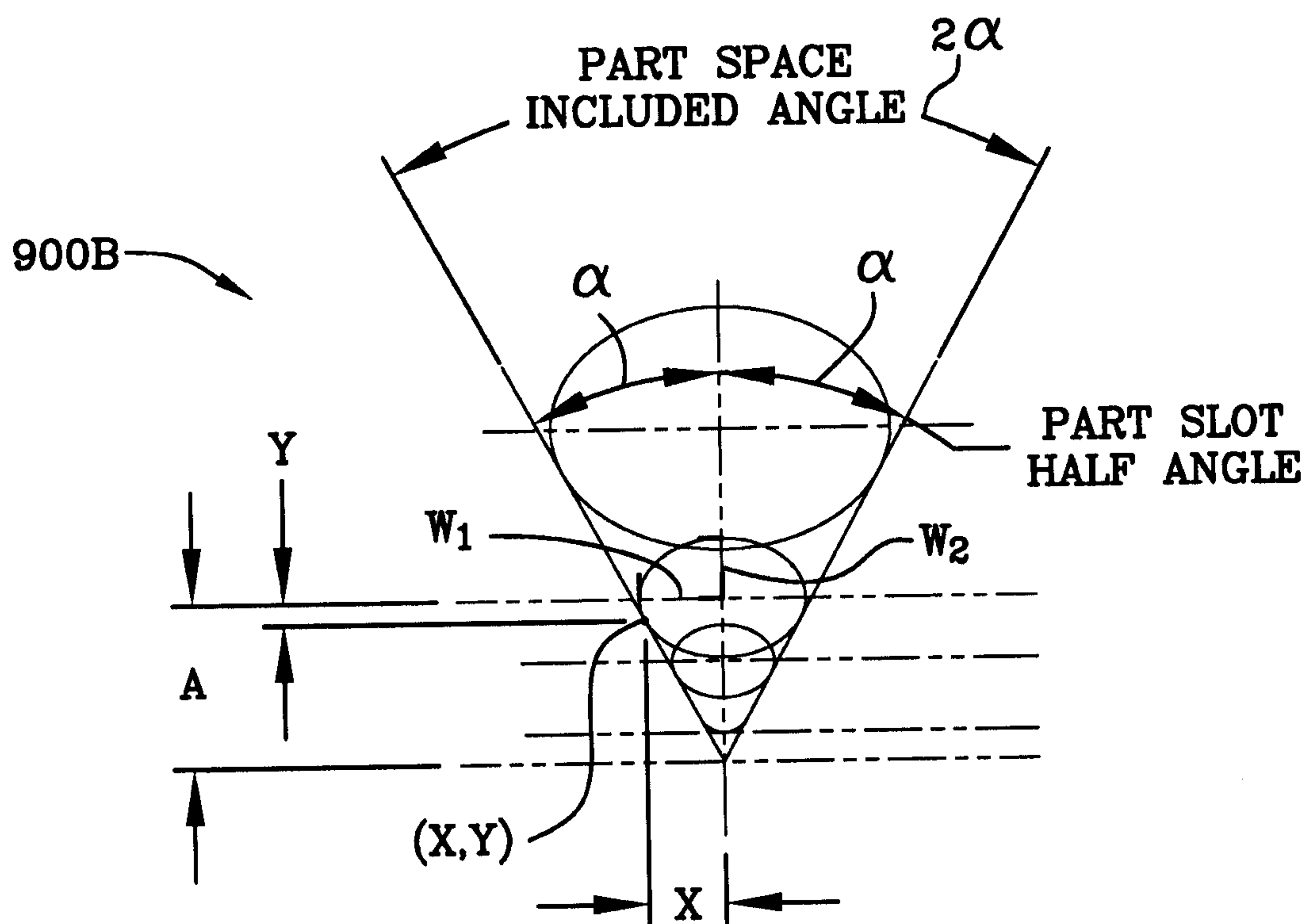


FIG. 9B

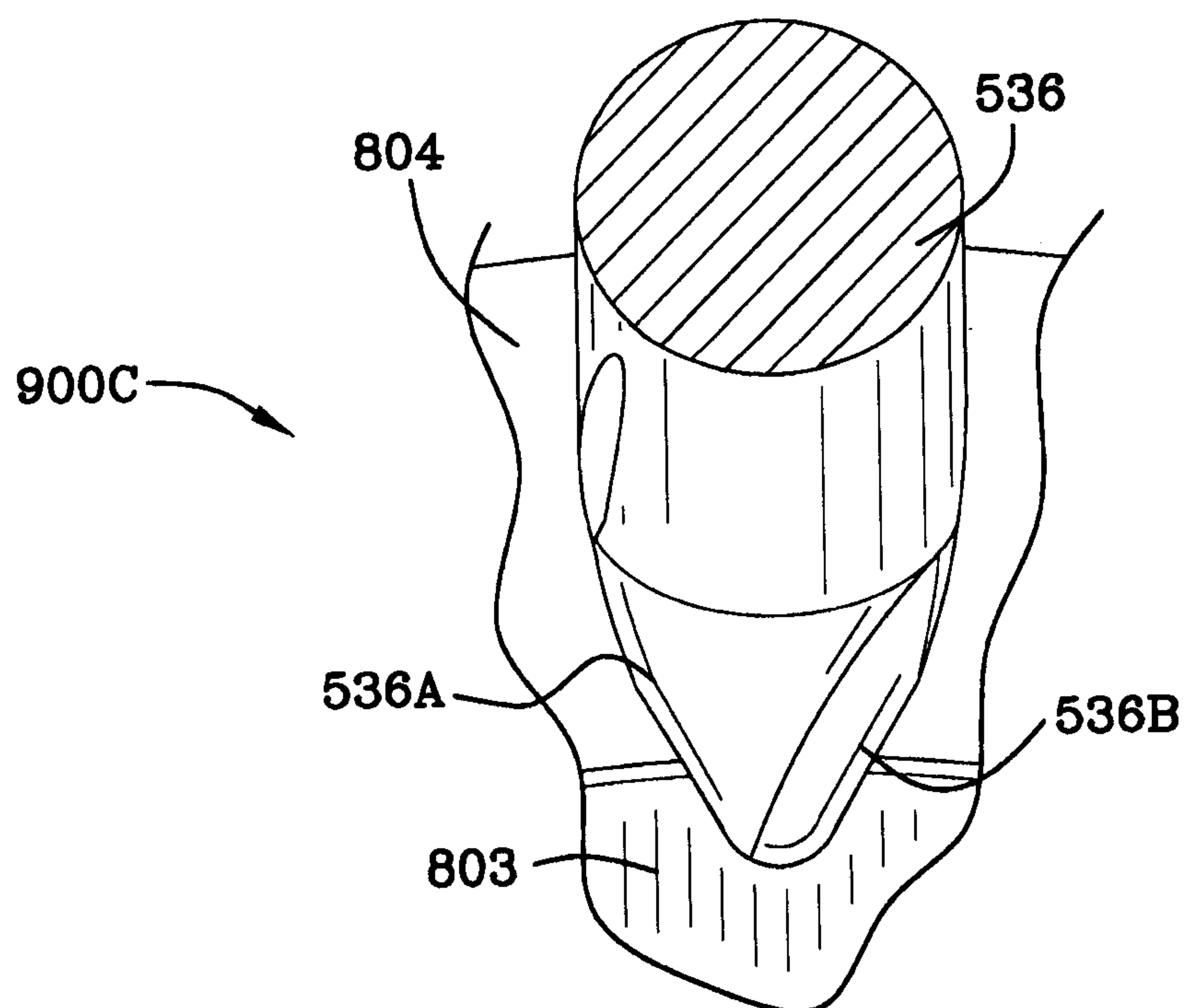


FIG. 9C

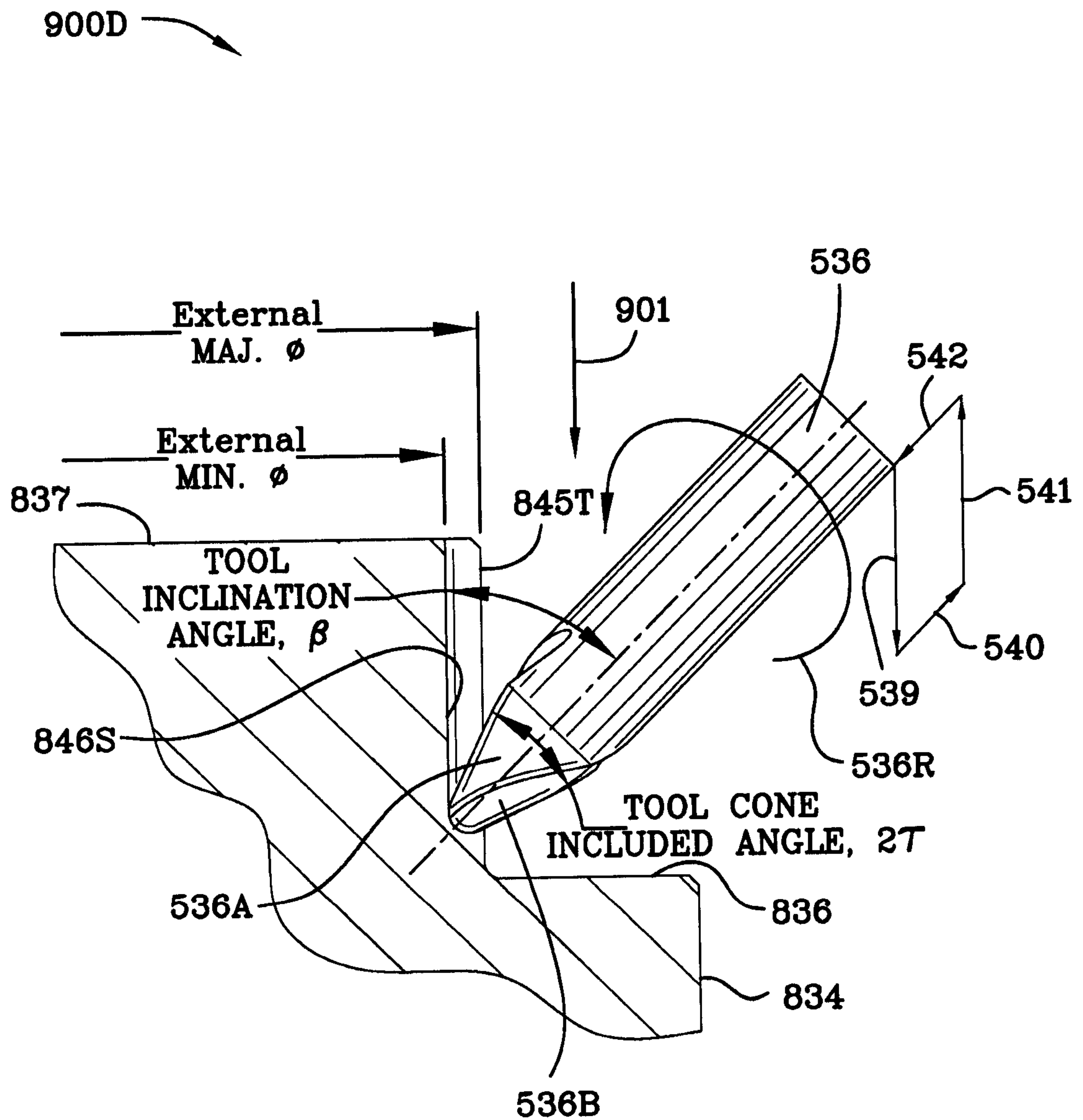


FIG. 9D

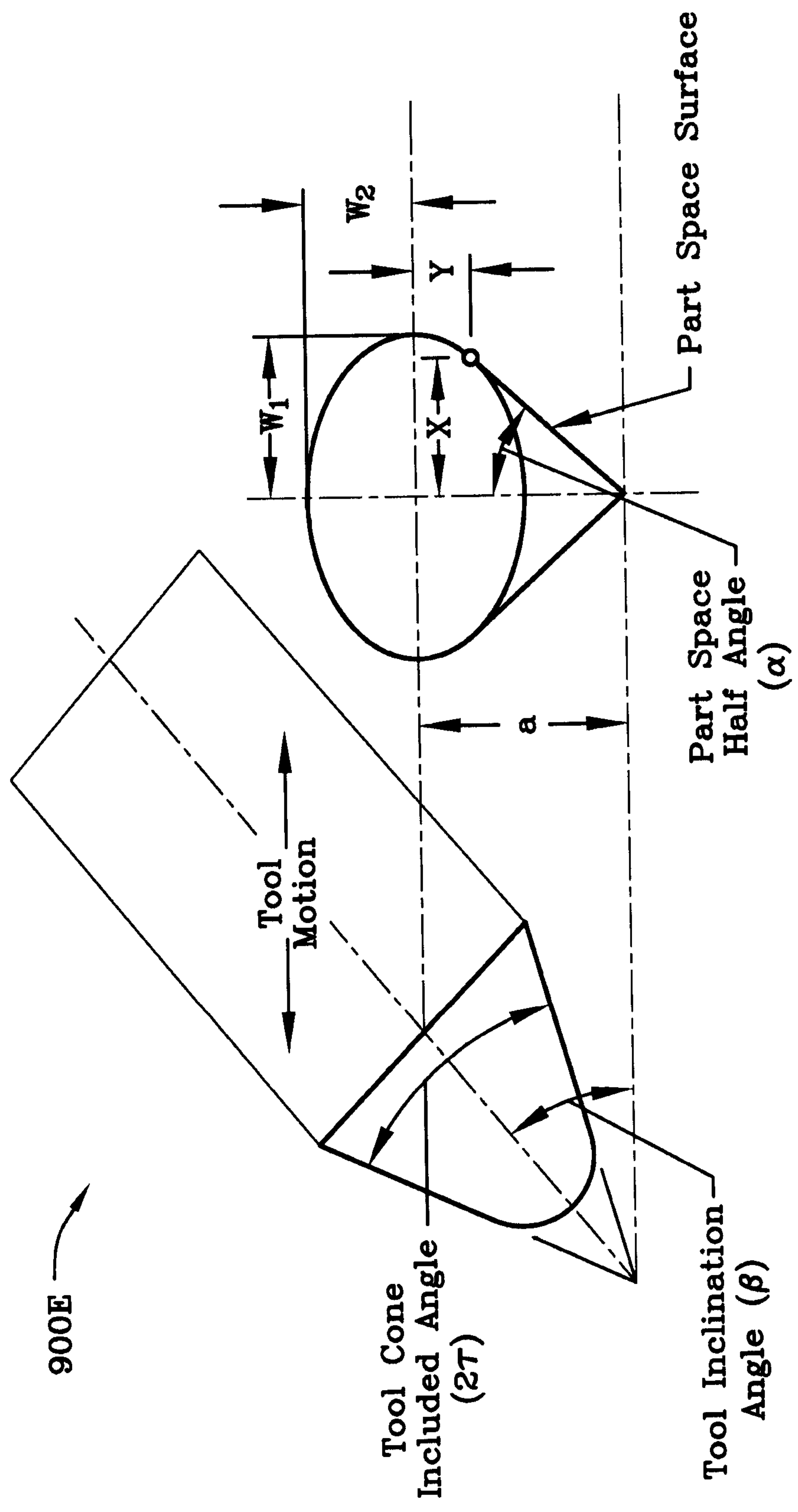


FIG. 9E

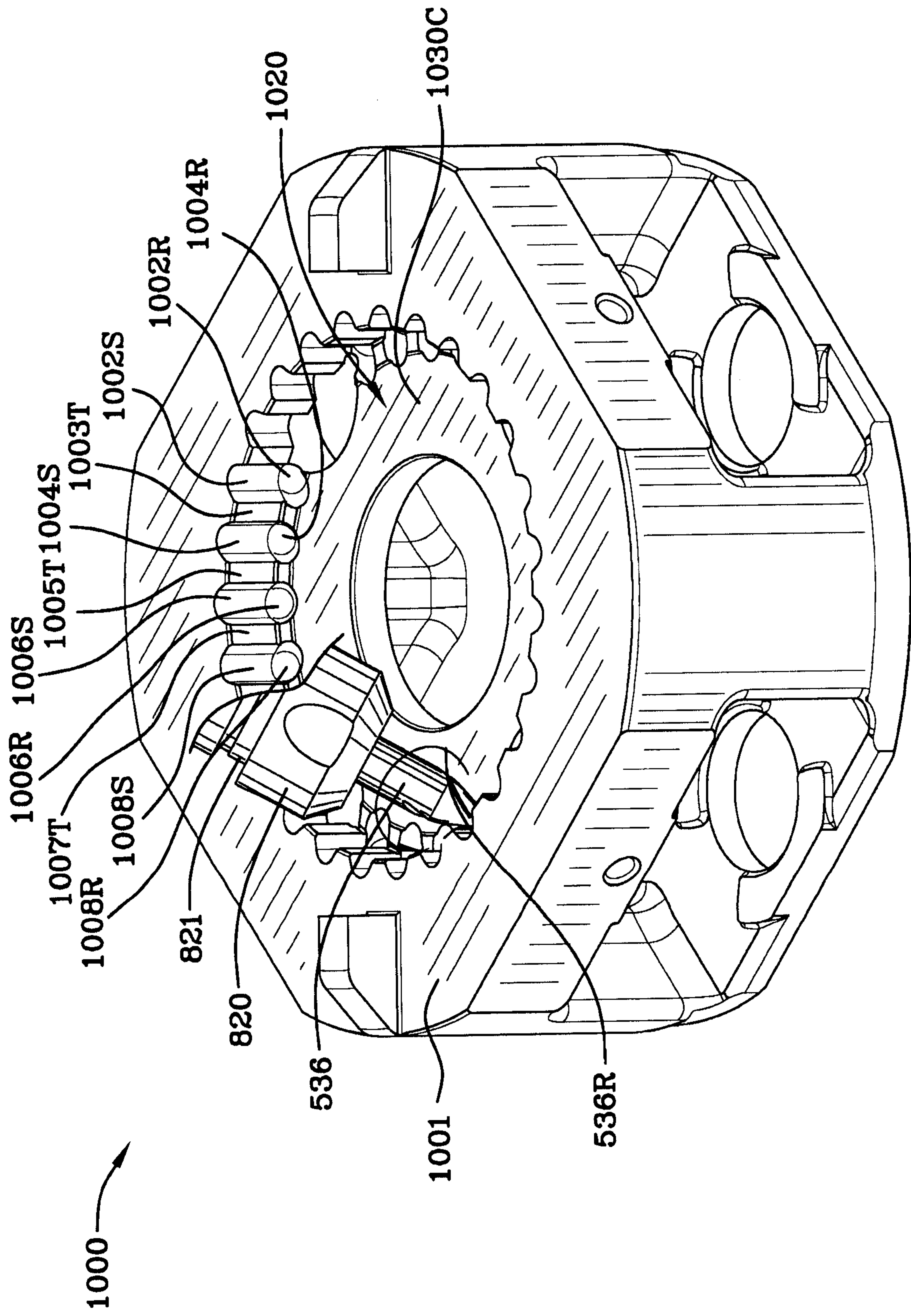


FIG. 10

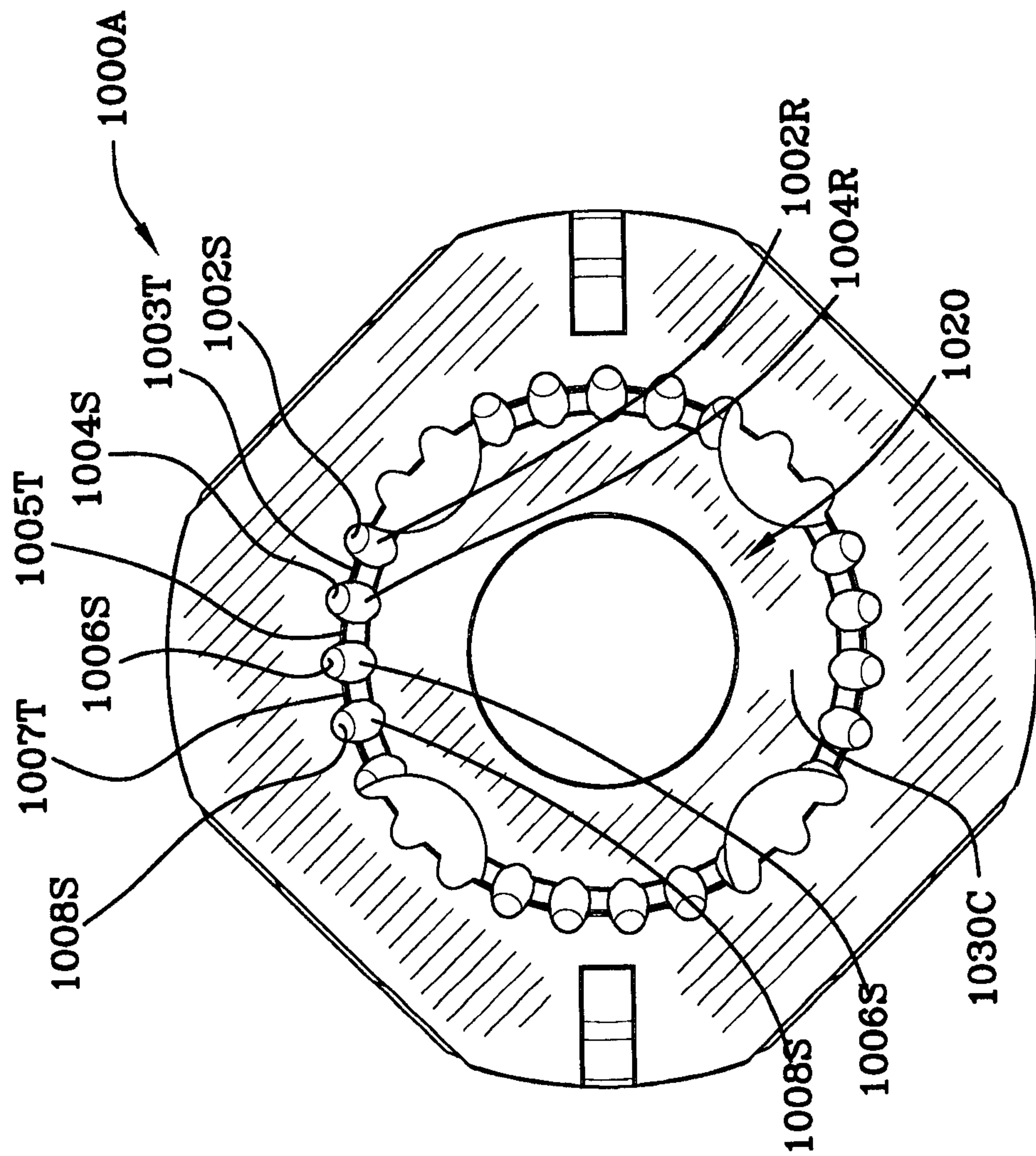


FIG. 10A

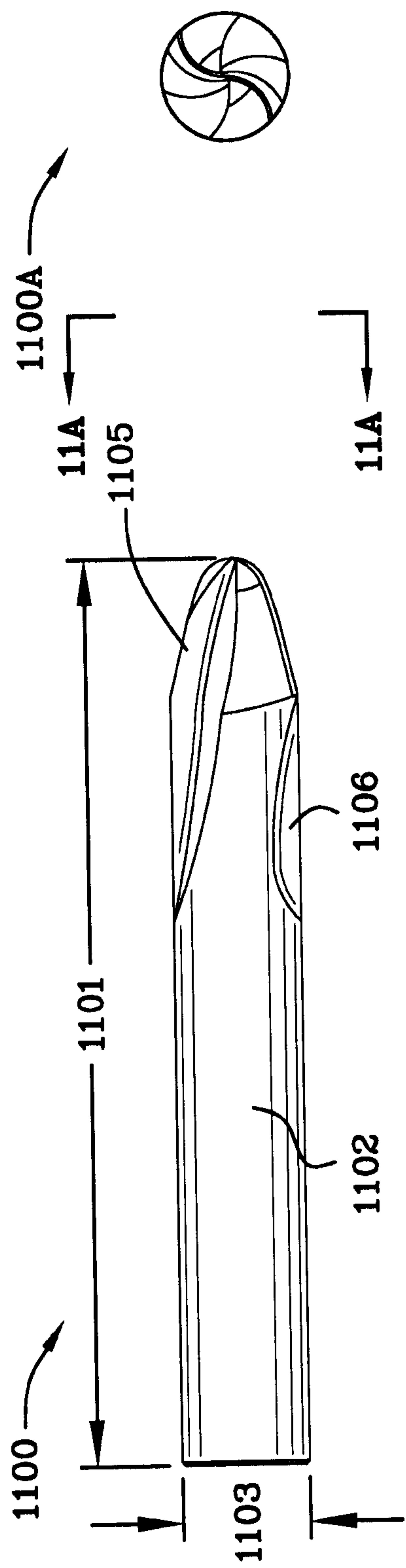


FIG. 11A

FIG. 11

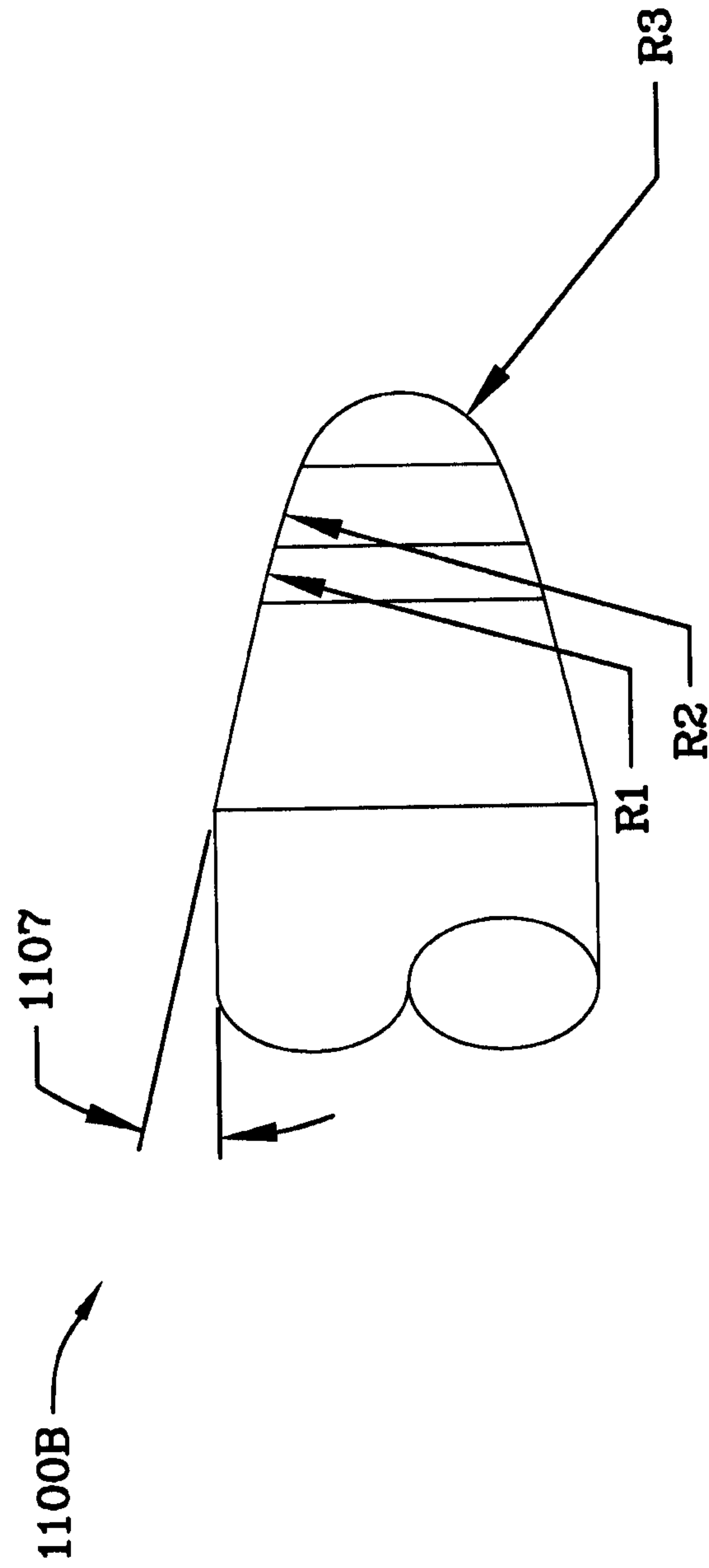


FIG. 11B

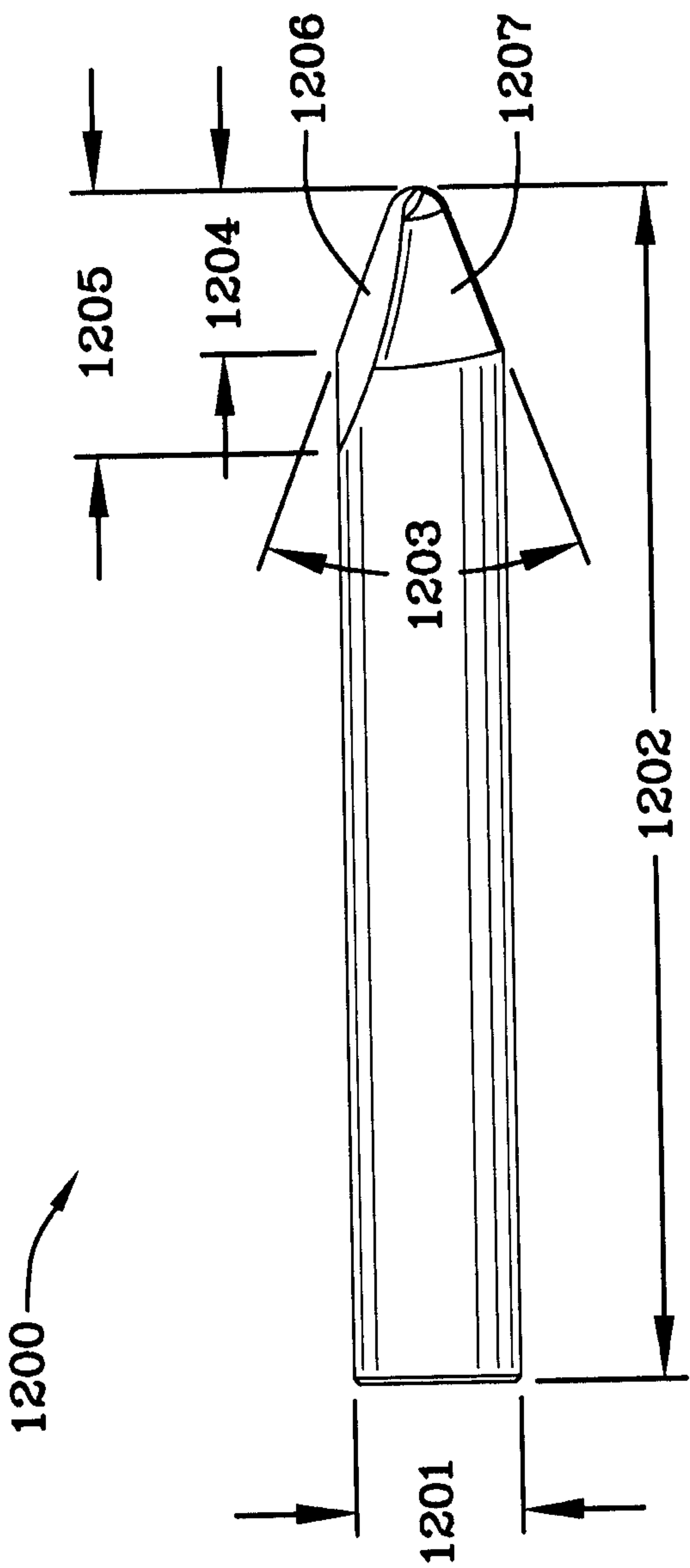


FIG. 12

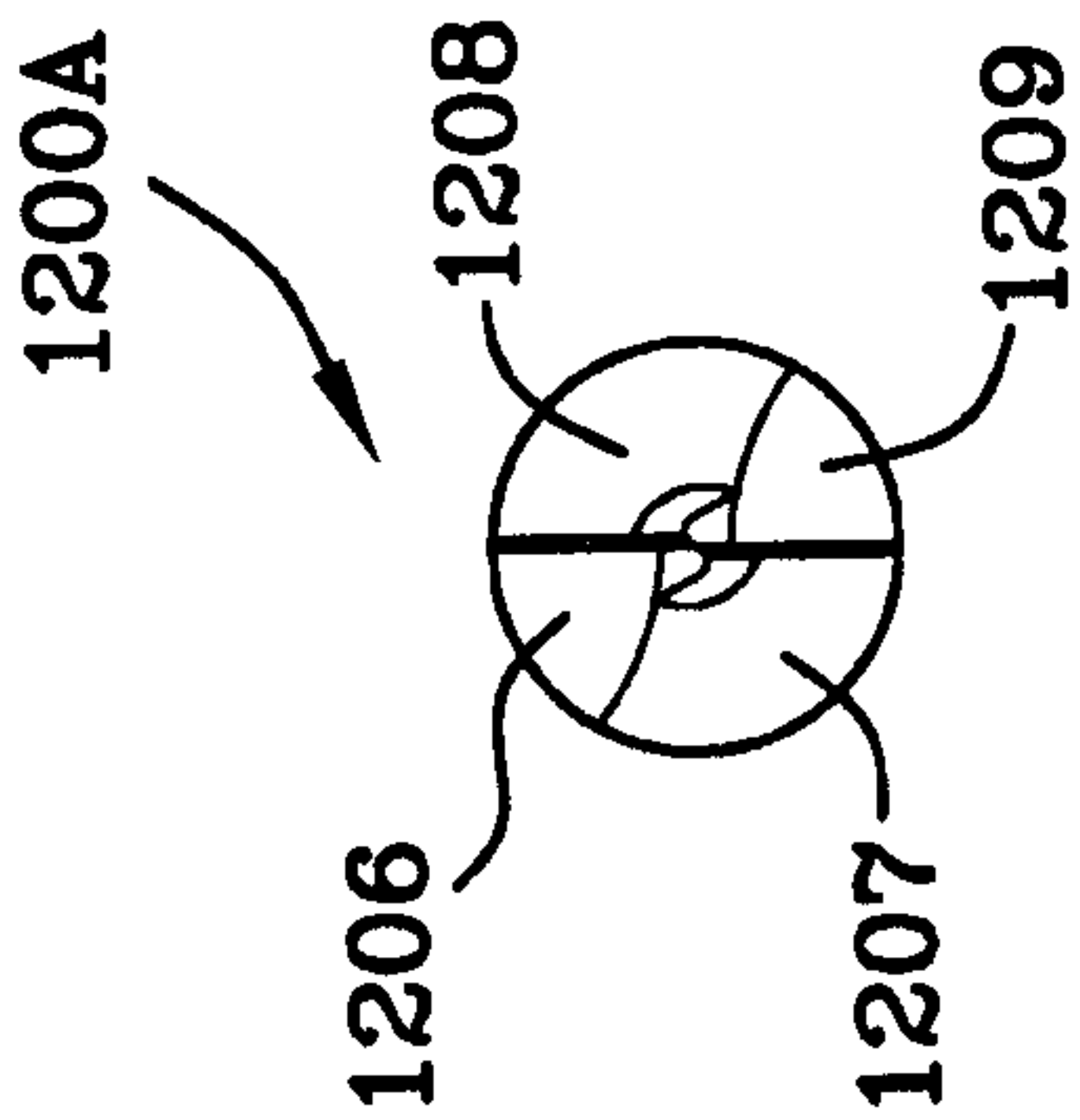


FIG. 12A

