

(43) International Publication Date
25 September 2014 (25.09.2014)

WIPO | PCT

(10) International Publication Number
WO 2014/146978 A1

(51) International Patent Classification:

G01S 17/89 (2006.01) *G01S 17/36* (2006.01)
G01S 7/491 (2006.01)

(21) International Application Number:

PCT/EP2014/055068

(22) International Filing Date:

14 March 2014 (14.03.2014)

(25) Filing Language:

English

(26) Publication Language:

English

(30) Priority Data:

LU 92 173 20 March 2013 (20.03.2013)

LU

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(81) Designated States (unless otherwise indicated, for every kind of national protection available): AE, AG, AL, AM, AO, AT, AU, AZ, BA, BB, BG, BH, BN, BR, BW, BY, BZ, CA, CH, CL, CN, CO, CR, CU, CZ, DE, DK, DM, DO, DZ, EC, EE, EG, ES, FI, GB, GD, GE, GH, GM, GT, HN, HR, HU, ID, IL, IN, IR, IS, JP, KE, KG, KN, KP, KR, KZ, LA, LC, LK, LR, LS, LT, LU, LY, MA, MD, ME, MG, MK, MN, MW, MX, MY, MZ, NA, NG, NI, NO, NZ, OM, PA, PE, PG, PH, PL, PT, QA, RO, RS, RU, RW, SA, SC, SD, SE, SG, SK, SL, SM, ST, SV, SY, TH, TJ, TM, TN, TR, TT, TZ, UA, UG, US, UZ, VC, VN, ZA, ZM, ZW.

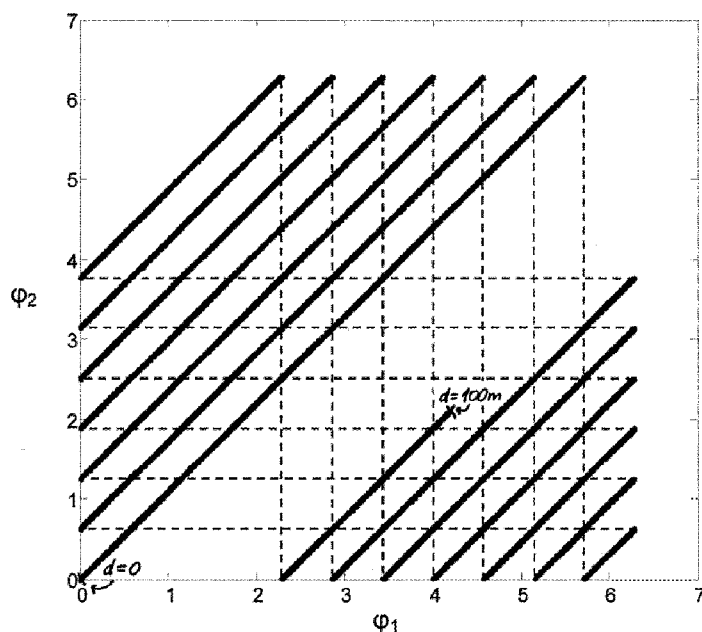
(84) Designated States (unless otherwise indicated, for every kind of regional protection available): ARIPO (BW, GH, GM, KE, LR, LS, MW, MZ, NA, RW, SD, SL, SZ, TZ, UG, ZM, ZW), Eurasian (AM, AZ, BY, KG, KZ, RU, TJ, TM), European (AL, AT, BE, BG, CH, CY, CZ, DE, DK, EE, ES, FI, FR, GB, GR, HR, HU, IE, IS, IT, LT, LU, LV, MC, MK, MT, NL, NO, PL, PT, RO, RS, SE, SI, SK, SM, TR), OAPI (BF, BJ, CF, CG, CI, CM, GA, GN, GQ, GW, KM, ML, MR, NE, SN, TD, TG).

Published:

— with international search report (Art. 21(3))

(54) Title: DISTANCE DETERMINATION METHOD

Fig. 1



(57) Abstract: A method for determining a distance comprises: providing at least two phase measurements made with modulated light of different modulation wavelengths, each phase measurement being indicative of the distance up to an integer multiple of a respective modulation wavelength; providing a set of possible wraparound count combinations; for each one of the possible wraparound count combinations, calculating a combination of unwrapped phase hypotheses corresponding to the at least two phase measurements; and selecting a most plausible combination of unwrapped phase hypotheses among the combinations of unwrapped phase hypotheses and calculating the distance based upon the selected most plausible combination of unwrapped phase hypotheses.

DESCRIPTION

DISTANCE DETERMINATION METHOD

Technical field

[0001] The present invention generally relates to a method for determining a distance based upon a plurality of phase measurements, made at different wavelengths, each of the phase measurements, taken individually, being ambiguous in the sense that it indicates the distance only up to an integer multiple of the respective wavelength.

Background Art

[0002] Distance measuring equipment often relies on the time-of-flight (TOF) measurement principle. Distance (also: depth) information is in this case obtained by emitting modulated light into the direction of the target and measuring the phase shift of the modulation between the emitted and the reflected light. The measured phase is proportional to the distance between the measurement equipment and the target, modulo the wavelength of the modulation. This relationship may be expressed as:

$$\varphi = \text{mod}\left(\frac{d \cdot 4\pi \cdot f}{c}, 2\pi\right),$$

where φ is the modulation phase in radians, d is the distance, f is the modulation frequency, and c is the speed of light. The modulation wavelength λ is given as $\lambda = c/f$. The extra factor 2 (4π instead of 2π) in the first argument of the mod function is due to the fact that the light travels twice the distance between the distance measuring equipment and the target. The above relationship expresses that the phase measurement is ambiguous, i.e. the distance value d' calculated as $d' = \varphi \cdot c / (4\pi \cdot f)$ may be different from the actual distance by an a priori unknown integer number of modulation wavelengths.

[0003] The distance $d_u = c/(2 \cdot f)$ is called the “unambiguity range”, because if it is known beforehand that the measured distance is less than d_u , the modulo function may be inverted, yielding an unambiguous distance. However, if the target may be located at greater distances from the target than d_u , any phase measurement will be comprised in the interval $[0, 2\pi[$: one says that the measurements are “wrapped” into

the unambiguity range. As a consequence, retrieving the actual distance from the ambiguous measurement, or, otherwise stated, determining the integer number of modulation wavelengths to add to the distance value d' in order to arrive at the actual distance, is called "phase unwrapping".

5 [0004] In a single-frequency system, the usable distance measurement range is bounded by the unambiguity range unless assumptions are made on the smoothness of the scene (neighbouring pixels) and on the smoothness of the evolution in time of a distance measurement. Such assumptions cannot be made in all circumstances and for all applications. Specifically, in an adaptive driver assistance system, such
10 assumptions are normally not permitted. When operating a 3D TOF camera or other distance measuring equipment, the usable unambiguity range may not be sufficient when employing a single modulation frequency. To overcome that drawback, n ($n > 1$) measurements of the same distance may be made with n different modulation frequencies. The usable distance measurement range can thereby be extended by
15 combining the results of the different measurements and finding, or estimating (in the case of presence of measurement noise), the unknown distance by trying to invert the modulo function. When using two frequencies ($n=2$), the combination is easily performed by calculating the difference between the measured phases at the first and second modulation frequency, but when using three frequencies or more in order to
20 further reduce the measurement error in presence of noise compared to using only two frequencies, a method which is as simple as calculating the phase difference does not exist.

[0005] The paper "Multi-frequency Phase Unwrapping for Time-of-Flight Cameras", D. Droschel, D. Holz and S. Behnke, Proceedings of IEEE/RSJ International
25 Conference on Intelligent Robots and Systems (IROS), Taipei, Taiwan, October 2010, discloses a probabilistic phase unwrapping approach, which takes into account the neighbourhood of each pixel. The paper also mentions the possibility of using two modulation frequencies for detecting phase wrapping. It is proposed to compare the two distance values obtained from the two measured phases. If these distance
30 values coincide, the distance lies in the unambiguity range; if they do not coincide, at least one of the phases has been wrapped into the $[0, 2\pi[$ interval and the phase has to be unwrapped.

[0006] Document DE 100 39 422 C2 discloses a photoelectronic mixing device (PMD) operating at plural frequencies for carrying out measurements of speed and/or distance.

[0007] US patent 7,791,715 B1 relates to a method and system for dealiasing (unwrapping) in TOF systems. The system uses at least two close-together modulation frequencies f_1 and f_2 that are close to the maximum modulation frequency supported by the system. The distance Z is then calculated as:

$$Z = \frac{c \cdot \Delta\varphi}{4\pi \cdot \Delta f},$$

where $\Delta\varphi$ is the difference of the measured phases at f_1 and f_2 , respectively, and where $\Delta f = f_1 - f_2$. When more than two different frequencies are available, the phase measurements are combined in pairs and the same formula is applied.

[0008] Whereas it is known from the prior art to combine plural frequencies in order to achieve a greater (combined) unambiguity range, the known methods have drawbacks when measurement noise comes into play. Furthermore, the computational effort necessary to carry these methods out may be too important for low-cost implementations.

Technical problem

[0009] It is an object of the present invention to provide a practically implementable method for estimating the unknown distance when using two or more modulation frequencies. This object is achieved by a method as claimed in claim 1.

General Description of the Invention

[0010] According to the invention, a method for determining a distance comprises

- providing at least two phase measurements made with modulated light of different modulation wavelengths, each phase measurement being indicative of the distance up to an integer multiple of a respective modulation wavelength;
- providing a set of possible wraparound count combinations;

- for each one of the possible wraparound count combinations, calculating a combination of unwrapped phase hypotheses corresponding to the at least two phase measurements; and
- selecting a most plausible combination of unwrapped phase hypotheses among the combinations of unwrapped phase hypotheses and calculating the distance based upon the selected most plausible combination of unwrapped phase hypotheses.

[0011] The distance may e.g. be calculated as an average over the distance values associated with the unwrapped phase hypotheses of the most plausible combination of unwrapped phase hypotheses.

[0012] According to preferred possible embodiment the selecting of the most plausible combination of unwrapped phase hypotheses among the combinations of unwrapped phase hypotheses comprises

- for each combination of unwrapped phase hypotheses, calculating a combination of distance values associated with the unwrapped phase hypotheses of the respective combination of unwrapped phase hypotheses,
- for each combination of unwrapped phase hypotheses, calculating a variance or standard deviation of the respective combination of distance values, and
- selecting as the most plausible combination of unwrapped phase hypotheses the one for which the variance or standard deviation is smallest.

[0013] According to a preferred embodiment of the invention, the selecting of the most plausible combination of unwrapped phase hypotheses among the combinations of unwrapped phase hypotheses comprises

- for each combination of unwrapped phase hypotheses, calculating a gap between a point having the respective unwrapped phase hypotheses as coordinates and an origin-crossing straight line having a direction vector with coordinate representation $[1/\lambda_1, \dots, 1/\lambda_n]$, where $\lambda_1, \dots, \lambda_n$ designate the different modulation wavelengths, and
- selecting as the most plausible combination of unwrapped phase hypotheses the one for which the gap is smallest.

[0014] The distance may advantageously be calculated as

$$\frac{\|\vec{\varphi}'_{est}\| \cdot c}{4\pi \cdot \|\vec{u}\|},$$

where $\vec{\varphi}'_{est}$ is an orthogonal projection onto the origin-crossing straight line of a point having the most plausible combination of unwrapped phase hypotheses as coordinates, and $\vec{u}$ is the direction vector $[c/\lambda_1, \dots, c/\lambda_n]$.

- 5 [0015] Yet more advantageously, the calculating of the gap may be carried out in a rotated coordinate system, in which the origin-crossing straight line is a coordinate axis. In this case, the distance is preferably calculated as calculated as

$$\frac{(\vec{\varphi}''_{j_opt})_1 \cdot c}{4\pi \cdot \|\vec{u}\|}$$

- 10 where $(\vec{\varphi}''_{j_opt})_1$ is a coordinate of the point having the most plausible combination of unwrapped phase hypotheses as coordinates in the rotated coordinate system, and $\vec{u}$ is the direction vector $[c/\lambda_1, \dots, c/\lambda_n]$.

[0016] A preferred aspect of the invention concerns a computer program, comprising computer-implementable instructions, which, when executed by a computer, cause the computer to carry out the method described hereinabove.

- 15 [0017] Another preferred aspect of the invention relates to a time-of-flight distance-measuring device, comprising an electronic control unit with a memory, the memory having stored therein a computer program as described hereinabove, the electronic control unit being configured to execute the computer program when determining a distance.

- 20 [0018] Yet another preferred aspect of the invention relates to a time-of-flight distance-measuring device, comprising an FPGA (field-programmable gate array) or ASIC (application-specific integrated circuit) configured and arranged to carry out the method described hereinabove.

Brief Description of the Drawings

- 25 [0019] Preferred, non-limiting, embodiments of the invention will now be described, by way of example, with reference to the accompanying drawings in which:

Fig. 1 is a graph illustrating phase couples (φ_1, φ_2) obtainable through ideal phase measurements at two different modulation frequencies for distances between 0 and a maximum distance;

Fig. 2 is a graph illustrating phase triples $(\varphi_1, \varphi_2, \varphi_3)$ obtainable through ideal phase measurements at three different modulation frequencies for distances between 0 and a maximum distance;

Fig. 3 is a schematic flowchart of a first embodiment of a method for estimating the unknown distance from n phase measurements made at n different frequencies;

Fig. 4 is a schematic flowchart of a second embodiment of a method for estimating the unknown distance from n phase measurements made at n different frequencies;

Fig. 5 is a schematic flowchart of a third embodiment of a method for estimating the unknown distance from n phase measurements made at n different frequencies;

Fig. 6 is a schematic illustration of a preferred embodiment of a 3D-TOF camera

Description of Preferred Embodiments

[0020] Embodiments of the invention are going to be discussed, for illustration purposes, in the context of a 3D TOF camera that delivers, for each of its pixels, a phase information φ in rad which is indicative of the distance d in meters between the camera and the target, and is given by:

$$\varphi = \text{mod}\left(\frac{d \cdot 4\pi \cdot f}{c}, 2\pi\right),$$

where mod is the modulo function (which returns the remainder of the division of the first argument by the second argument), f is the modulation frequency in Hz, and c is the speed of light in m/s. The modulation wavelength λ is given as $\lambda = c/f$.

[0021] As can be seen, the phase φ repeats itself periodically with the distance, implying that there is a limited unambiguity range of the distance measurement. The unambiguity range is given by:

$$d_u = \frac{c}{2f}.$$

[0022] The usable distance measurement range is bounded by the unambiguity range. When performing n measurements with n different frequencies of the same

scene, the usable distance measurement range can be extended by combining the results of the different measurements and finding, or estimating in the case of presence of measurement noise, the unknown distance by “inverting” the modulo function.

5 [0023] A first problem that needs to be addressed is how to select the frequency values so as to maximize the allowed measurement noise when a defined usable distance measurement range is required. When sufficient noise is present, the modulo function inversion leads to a distance estimation error.

[0024] To illustrate this problem for a 2-frequency measurement, Fig. 1 shows the
 10 relation between ideally measured (i.e. not affected by noise) phases φ_1 and φ_2 , respectively corresponding to modulation frequencies f_1 and f_2 , when the unknown distance ranges between 0 and the required usable distance measurement range. For Fig.1, f_1 and f_2 have been assumed to be 10 MHz and 11 MHz, respectively, and the maximum usable distance measurement range has been set to 100 m. It can be
 15 seen that φ_1 and φ_2 “wrap around” each time they arrive at 2π (illustrated by dashed lines). If no noise is present on the measurements, the point (φ_1, φ_2) defined by the measured phases φ_1 and φ_2 lies on one of the line segments shown in Fig. 1. However, if noise is present on the phase measurements, the measured point $(\tilde{\varphi}_1, \tilde{\varphi}_2)$ may differ from the a priori unknown ideal point (φ_1, φ_2) and be located in the
 20 “forbidden areas” between the line segments. If the noise is sufficiently high, the measured point $(\tilde{\varphi}_1, \tilde{\varphi}_2)$ may be closer to a line segment that corresponds to a distance that is completely different from the actual distance. Therefore, the distance between the line segments shown on Fig. 1 must be maximized for a given required usable distance measurement range by appropriately selecting the frequencies f_1 and
 25 f_2 . The same applies for an n-frequency measurement. For the illustration of a 3-frequency measurement, Fig. 2 shows a graph similar to the one of Fig. 1 for the frequencies 10 MHz, 11 MHz and 13 MHz. The three frequencies result in a 3D plot.

[0025] The maximization of the distances between the line segments may be achieved by a brute force approach. The range in which the modulation frequencies
 30 can lie is known beforehand, and is defined for example by the maximum operating frequency of the active illumination and by the minimum frequency which still yields an acceptable imager noise level. Within this range all n frequencies are varied, for

example by linearly sweeping or randomly selecting. For each set of n frequencies, (frequency n -tuple), the distance trajectories are drawn in the n -dimensional phase space, and the minimum distance between each possible line segment pair is searched. Finally, the optimal frequency n -tuple that achieves the maximum of the minimum line segment distances is kept and used for the application. The minimum line segment distance value h_1 for the optimal frequency n -tuple is also kept and is used in the application to check the confidence level of the measured phase n -tuple.

[0026] In the following, the n frequencies are assumed to be known. For illustration purposes, they will be given certain values, but it shall be understood that these frequencies are not necessarily optimal with regard to the above criterion of maximal separation between the line segments.

[0027] A first embodiment of a method for estimating the unknown distance from n phase measurements at n different frequencies will now be described, with reference to Fig. 3. In a first step, the modulation frequencies $f_1, \dots, f_n$ are fixed (step 301) and for the unknown distance ranging between zero and the usable distance measurement range, a list with all the possibly occurring distinct combinations of phase wraparound counts of each of the n phases is established (step 302). For example, using a 3-frequency measurement with the same parameters as for Fig. 2 (frequencies $f_1=10$ MHz, $f_2=11$ MHz and $f_3=13$ MHz) the following table results:

$nwrap_1$	0	0	0	1	1	1	2	2	2	3	3	3	3	4	4	4	5	5	5	6	6	6
$nwrap_2$	0	0	1	1	1	2	2	2	3	3	3	4	4	4	5	5	5	5	6	6	6	7
$nwrap_3$	0	1	1	1	2	2	2	3	3	3	4	4	5	5	5	6	6	7	7	7	8	8

where $nwrap_1$ is the wraparound count of φ_1 for frequency f_1 , $nwrap_2$ the wraparound count of φ_2 for frequency f_2 and $nwrap_3$ the wraparound count of φ_3 for frequency f_3 . It is worthwhile noting that each column in the above table corresponds to one segment in Fig. 2. The table of phase wraparound counts can be calculated offline, that is to say only once during the configuration of the measurement system, and its results can be permanently stored in the application's non volatile memory, as the only information needed are the n frequencies and the required usable distance measurement range, which are known beforehand.

[0028] For each row i and column j in the table, a distance hypothesis may be calculated as:

$$d_{ij} = \frac{(\varphi_i + nwrap_{ij} \cdot 2\pi) \cdot c}{4\pi \cdot f_i}$$

[0029] During the measurement, a phase n-tuple $[\varphi_1, \dots, \varphi_n]$ is measured (step 303). Using the wraparound count table above, a distance hypothesis is estimated for each cell in the table using the above formula for d_{ij} (step 304).

- 5 [0030] Then, the optimal column j_{opt} in the table is searched for. This column corresponds to the most plausible combination of phase wraparound counts. According to the first embodiment of the method, the optimal column is the one for which the variance or the standard deviation of the n distances d_{ij} in the column is minimal. The variance σ_j^2 of each wraparound count combination j may be calculated
- 10 (step 305) as: $\sigma_j^2 = \frac{1}{n} \sum_{i=1}^n d_{ij}^2 - \frac{1}{n} \sum_{i=1}^n d_{ij}$ and the minimum variance be determined (step 306).

[0031] The ratio of the standard deviation (found for j_{opt}) to the minimum line segment distance h_1 can be used as an indicator of the confidence level of the distance measurement (the smaller the ratio the better).

- 15 [0032] Finally, the mean (average) $\langle d_{j_{opt}} \rangle = \frac{1}{n} \sum_{i=1}^n d_{ij_{opt}}$ of the distances $d_{ij_{opt}}$ of the column j_{opt} serves as an estimation of the unknown distance (step 307).

- [0033] A second embodiment of the method for estimating the unknown distance from n phase measurements at n different frequencies will now be described with reference to Fig. 4. This embodiment takes advantage from the fact that the actual
- 20 required distance measurement range is typically smaller than the target detection range from which no folding back into the required distance measurement range must occur, but where the actual target distance does not need to be measured. In many application it is necessary only that the TOF measurement device is able to measure the unknown distance over a restricted range. Targets beyond this range
- 25 and still within the range where the TOF measurement device detects a target must not fold back into the required distance measurement range, but their distance does not need to be known. For example, in an automotive 'advanced driver assistance system', only the distances to targets which are within, e.g. 20 m in front of the car shall be measured, but at the same time highly reflective targets up to 100 m in front
- 30 of the car must not be folded back into the required distance measurement range.

For this example, the detection range is 100 m, but the required distance measurement range is only 20 m. This implies that the frequency selection process (step 401) takes into account

- 1) the distances between any two line segments representing distances within the required measurement range,
- 2) the distances between any pair of one line segment representing a distance within the required measurement range and one line segment representing a distance that is outside the required measurement range but still within the equipment's detection range

but does not take into account the distances between any two line segments representing distances, which are outside the required measurement range but still within the equipment's detection range. The minimum line segment distance value (hereinafter noted h_2) that is found (step 403) is kept and used in the application to check the confidence level of the measured phase n-tuple.

[0034] For the unknown distance ranging between zero and the required measurement range, a list with all the possibly occurring distinct combinations of phase wraparound counts of each of the n phases is established. For example, using 3-frequency measurement with the same parameters as for Fig. 2 and a wanted measurement range of 20 m, the following table results:

$nwrap_1$	0	0	0	1	1
$nwrap_2$	0	0	1	1	1
$nwrap_3$	0	1	1	1	2

where $nwrap_1$ is again the wraparound count of φ_1 for frequency f_1 , $nwrap_2$ the wraparound count of φ_2 for frequency f_2 and $nwrap_3$ the wraparound count of φ_3 for frequency f_3 . The set of frequencies and the table of wraparound count can be calculated offline (steps 401 and 402), that is only once during the configuration of the measurement system and its results can be permanently stored in the application's non volatile memory, as the only information needed are the n frequencies, the wanted measurement range and the required extended unambiguity distance, which are known beforehand.

[0035] Using the wraparound count table above, the column which best unwraps the n-tuple of measured phases $[\varphi_1, \dots, \varphi_n]$, leading to an optimal estimation of the unknown distance, is searched for.

[0036] The online calculation starts with the providing of the phase measurements (step 405), which may be represented as phase n-tuple $[\varphi_1, \dots, \varphi_n]$ or vector $\vec{\varphi}$. For each row i and column j in the list and for a combination of measured phases (n-tuple $[\varphi_1, \dots, \varphi_n]$), the unwrapped phase is calculated (step 406) using the formula:

$$\varphi'_{ij} = \varphi_i + nwrap_{ij} \cdot 2\pi.$$

[0037] Then, for each column j , the gap g_j in the n-dimensional phase space between the unwrapped phase n-tuple $[\varphi'_{1j}, \dots, \varphi'_{nj}]$ and the origin-crossing straight line having the direction vector

$$\vec{u} = [f_1, \dots, f_n] = [c/\lambda_1, \dots, c/\lambda_n]$$

is calculated (step 407). This can for example be done by calculating the length of the vector cross product of the unwrapped phase n-tuple $[\varphi'_{1j}, \dots, \varphi'_{nj}]$, which we will designate by $\vec{\varphi}'_j$ for simplicity, and the normalized vector $\vec{u}$:

$$g_j = \left\| \vec{\varphi}'_j \times \frac{\vec{u}}{\|\vec{u}\|} \right\|$$

where $\times$ designated the vector cross product and $\|\cdot\|$ the length of vector a vector. It is worthwhile noting that the vector $\vec{u}$ is preferably determined beforehand (step 404).

[0038] Then, the smallest g_j (hereinafter denoted g_{j_opt}) is searched among all the g_j (step 408) and then the unwrapped phase n-tuple $\vec{\varphi}'_{j_opt} = [\varphi'_{1j_opt}, \dots, \varphi'_{nj_opt}]$ corresponding to g_{j_opt} is selected.

[0039] g_{j_opt} is compared (step 409) with $h_2/2$ found in the frequency selection process described above. If $g_{j_opt} < h_2/2$, then the distance to be determined lies within the required measurement range, if $g_{j_opt} \geq h_2/2$, then it lies outside the required measurement range (but within the detection range, for otherwise there would be no phase measurement values) and is not considered a valid distance (step 410).

[0040] Preferably, the squares of the g_j are computed instead because doing this is computationally less expensive. $g_{j_opt}^2$ is then compared with the offline computed parameter $h_z^2/4$.

[0041] The unknown distance d_{est} is finally computed by projecting the found
5 unwrapped phase n-tuple $\bar{\varphi}'_{j_opt} = [\varphi'_{1j_opt}, \dots, \varphi'_{nj_opt}]$ onto the origin-crossing line with direction vector $\vec{u}$ (step 411), measuring the distance of the projection to the origin.

[0042] Noting

$$\bar{\varphi}'_{est} = \frac{1}{\|\vec{u}\|^2} (\bar{\varphi}'_{j_opt} \bullet \vec{u}) \vec{u}$$

the projection of the found unwrapped phase n-tuple $\bar{\varphi}'_{j_opt} = [\varphi'_{1j_opt}, \dots, \varphi'_{nj_opt}]$ onto
10 the origin-crossing line with direction vector $\vec{u}$ (“•” designated the dot product between two vectors), the distance can be estimated (step 412) as:

$$d_{est} = \frac{\|\bar{\varphi}'_{est}\| \cdot c}{4\pi \cdot \|\vec{u}\|}.$$

[0043] A preferred implementation of the second embodiment, which is computationally inexpensive will now be explained with reference to Fig. 5. This
15 implementation is similar to the implementation of Fig. 4, except that the n-dimensional phase space is rotated around the origin in such a way that the vector $\vec{u} = [f_1, f_2, f_3]$ will be rotated into alignment with the x-axis unit vector $\vec{i} = [1, 0, 0]$. The y and z-axis unit vectors would allow the same inexpensive implementation, but for the sake of simplicity only the case for the x axis unit vector will be described. There is a
20 virtually infinite number of ways to achieve this transformation, and for simplicity the rotation will be performed around the unity-length normal vector $\vec{n}$ of the plane spanned by $\vec{u}$ and $\vec{i}$, and the angle of rotation will be the angle α between $\vec{u}$ and $\vec{i}$:

[0044] With $\vec{v} = \vec{u} / \|\vec{u}\|$, $\vec{n}$ may be expressed as:

$$\vec{n} = \frac{\vec{v} \times \vec{i}}{\|\vec{v} \times \vec{i}\|}.$$

25 [0045] The angle can be calculated as: $\alpha = \arccos(\vec{v} \bullet \vec{i})$.

[0046] The rotation matrix R , which performs the rotation operation described above is defined by:

$$R = \begin{pmatrix} n_1 n_1 (1 - \cos \alpha) + \cos \alpha & n_2 n_1 (1 - \cos \alpha) - n_3 \sin \alpha & n_3 n_1 (1 - \cos \alpha) + n_2 \sin \alpha \\ n_1 n_2 (1 - \cos \alpha) + n_3 \sin \alpha & n_2 n_2 (1 - \cos \alpha) + \cos \alpha & n_3 n_2 (1 - \cos \alpha) - n_1 \sin \alpha \\ n_1 n_3 (1 - \cos \alpha) - n_2 \sin \alpha & n_2 n_3 (1 - \cos \alpha) + n_1 \sin \alpha & n_3 n_3 (1 - \cos \alpha) + \cos \alpha \end{pmatrix},$$

with $\vec{n} = (n_1, n_2, n_3)$.

- 5 [0047] The offline computation comprises the selection of the modulation frequencies (step 501), the calculation of the wraparound count table (step 502) and the calculation of the rotation matrix R (step 503), as indicated above, and the calculation of the parameter h_2 (step 505).

- [0048] The online calculation begins with providing the n phase measurements (step 10 506). Instead of calculating, for each column j , the gap g_j in the n -dimensional phase space between the unwrapped phase n -tuple $(\varphi'_{1j}, \dots, \varphi'_{nj})$ and the origin-crossing straight line having the direction vector $\vec{u} = [f_1, \dots, f_n]$, in this implementation, one calculates, for each column j , the gap g'_j between the rotated unwrapped phase n -tuple $R[\varphi'_{1j}, \dots, \varphi'_{nj}] = R\vec{\varphi}'_j$ and the x -axis (i.e. the rotated origin-crossing straight line 15 having $\vec{u} = [f_1, \dots, f_n]$ as direction vector). Since the rotation does not change the measures, $g'_j = g_j$.

[0049] The rotated unwrapped phase n -tuple $\vec{\varphi}''_j$ may be calculated (step 507) as:

$$\vec{\varphi}''_j = R\vec{\varphi}'_j = R\vec{\varphi} + R \overrightarrow{wrap}_j \cdot 2\pi,$$

- Where $\overrightarrow{wrap}_j$ is the j -th column vector of the phase wraparound table. It is 20 worthwhile noting that $R \overrightarrow{wrap}_j \cdot 2\pi$ can be calculate upfront (as step 504 of the offline calculations), which means that this calculation does not take any processing time in the online calculations.

- [0050] It shall also be noted that the gap g_j depends only on the second and third coordinates of $\vec{\varphi}''_j$, which we denote by $(\vec{\varphi}''_j)_2$ and $(\vec{\varphi}''_j)_3$. For the square of the gap 25 g_j , the following equation holds:

$$g_j^2 = (\vec{\varphi}''_j)_2^2 + (\vec{\varphi}''_j)_3^2.$$

[0051] The smallest gap is searched for among all the g_j . The smallest gap found, g_{j_opt} , is compared with $h_2/2$ found in the offline frequency selection process. If $g_{j_opt} < h_2/2$, then the distance to be determined lies within the required measurement range, if $g_{j_opt} \geq h_2/2$, then it lies outside the required measurement range (but within
 5 the detection range, for otherwise there would be no phase measurement values) and is not considered a valid distance. It is possible to compute only the squares of the g_j (step 508). In this case, the smallest squared gap is searched for among all the g_j^2 (step 509), and the value found, $g_{j_opt}^2$, is compared with the offline computed parameter $h_2^2/4$ (step 510). If $g_{j_opt}^2 \geq (h_2/2)^2$, the rotated unwrapped phase n-tuple
 10 $\bar{\varphi}''_{j_opt}$ is considered to represent the most plausible combination of unwrapped phase hypotheses, otherwise the target is considered to lie outside the measurement range (step 511).

[0052] The unknown distance d_{est} is computed by orthogonally projecting the rotated unwrapped phase n-tuple $\bar{\varphi}''_{j_opt}$ onto the x-axis (i.e. the rotated origin-crossing line
 15 with direction vector $\vec{u}$). Noting $(\bar{\varphi}''_{j_opt})_1$ the first coordinate of $\bar{\varphi}''_{j_opt}$, the projected point has $((\bar{\varphi}''_{j_opt})_1, 0, 0)$ as coordinates.

[0053] The distance can finally be estimated (step 512) as:

$$d_{est} = \frac{(\bar{\varphi}''_{j_opt})_1 \cdot c}{4\pi \cdot \|\vec{u}\|}.$$

20 [0054] The difference between the computational efforts for the first implementation of the method described above, the second implementation and the computationally inexpensive version described above is now illustrated by means of an example. Only the online computation effort is estimated, since the offline computations do not consume any processing time during the measurements. Only the multiplications and
 25 square root operations are counted as they are the most expensive to implement.

[0055] When using the first implementation and using the parameters given as example, an initial scaling of $[\varphi_1, \varphi_2, \varphi_3]$ in order to reduce the computational effort in calculating the distance hypotheses d_{ij} requires 3 scalar multiplications for each column in the wraparound list (there are 22 columns in the example), one
 30 multiplication for the computation of the mean value, 3 multiplications for the variance (easier to compute than the standard deviation but fulfils the same purpose), and for

the calculation of the final result (distance) one scalar multiplication, resulting in: $3 + 22 * (1 + 3) + 1 = 92$ multiplications and no square root operation.

[0056] When using the second method described above and using the parameters given as example, for each column in the wraparound list (there are 5 columns), a vector cross product (6 multiplications), a vector squared length calculation (3 multiplications), and for the final result, a vector dot product (3 multiplications), a vector scalar product (3 multiplications), a vector length calculation (3 multiplications and a square root) and a scalar multiplication are required, resulting in: $5 * (6 + 3) + 3 + 3 + 3 + 1 = 55$ multiplications and one square root operation.

[0057] When using the computationally inexpensive version described above and using the parameters given as example, the initial rotation requires 9 multiplications, for each column in the wraparound list (there are 5 columns), a 2-dimensional vector squared length calculation (2 multiplications), and for the final result, a scalar multiplication are required, resulting in: $9 + 5 * 2 + 1 = 20$ multiplications and no square root operation.

[0058] In the above-disclosed distance estimation methods the actual value of the measurement phase noise is preferably known or estimated during the measurement. Indeed, if the phase noise is too large, it may happen that the noisy unknown distance n-tuple in the n-phase space jumps from the vicinity of the line segment, which the actual unknown distance phase n-tuple belongs to, into the vicinity of a completely different line segment in the phase space. Eventually, this leads to wrong distance estimation. Therefore, measurements, which have too large phase noise, are preferably declared invalid. The phase noise can be estimated or measured by measuring the amplitude, or by measuring the amplitude and intensity of the received modulated light and combining the amplitude and intensity. How this can be done is, for example, described in '3D Time-of-Flight Distance Measurement with Custom Solid-State Image Sensors in CMOS/CCD-Technology' by R. Lange.

[0059] Fig. 6 shows a preferred embodiment of a 3D TOF camera, generally identified by reference numeral 10. The 3D TOF camera 10 comprises an illumination unit 12 emitting light onto a scene, and an imaging sensor 14 imaging the scene. The imaging sensor 14 comprises, in a manner known per se, the required optical accessories such as a focusing lens (not shown) and an electronic camera chip 16

executed in any suitable technology, such as CCD, CMOS, TFA or the like. The imaging sensor 14 comprises a two-dimensional array of individual lock-in pixel sensor cells 18, each of which receives light from a small portion of the scene to be imaged for creating a pixel-by-pixel image thereof.

5 [0060] The illumination unit 12 comprises several individual light emitting devices 20 such as light emitting diodes (LEDs), which are collectively driven by means of an illumination driver 22. A signal source 24 provides the input signals for the illumination driver 22 and a photo gate driver 26. The output of the photo gate driver 26 is connected to the imaging sensor 14. An evaluation unit 28 comprising a suitable
10 electronic calculation device, e.g. a digital signal processor (DSP), is connected to the output of the imaging sensor 14.

[0061] When operating, the signal source 24 generates a modulation signal E1 on its output and feeds this modulation signal E1 to the illumination driver 22. The latter drives the illumination unit 12 with a drive signal E2 to emit an intensity-modulated
15 light signal L1 into a target scene comprising an object 30 (for illustration purposes). The modulated light signal L1 is partially reflected by the object 30 so as to form a returning light signal L2 which is received as incident light by the imaging sensor 14. The modulation signal E1 is also fed to the photo gate driver 26, which provides a demodulation signal E3. The imaging sensor 14 receives this demodulation signal E3
20 and produces a phase information signal E4, which is fed to the evaluation unit 28. The signal source 24 cycles through the plurality of different modulation frequencies $f_1, \dots, f_n$.

[0062] The 3D TOF camera 10 further comprises a reference pixel 32 mounted in the illumination unit 12 contiguous to the light emitting devices 20 in such a way that
25 it gathers light from the light emitting devices 18. The reference pixel 32 produces an output signal E5, which corresponds essentially to a modulation phase reference (comparable to a “zero” distance measurement). A reference subtraction stage 34 within the evaluation unit 28, outputs, for each pixel, phase information φ_i in rad corresponding to the modulation frequency f_i . The distance information for each
30 camera pixel 18 is then calculated in a distance calculation stage 36, in accordance with the method of the present invention. The evaluation unit 28 comprises a non-volatile memory 38, in which the calibration data, in particular the parameters that

may be calculated offline, are stored. The distance calculation stage 36 has access to these parameters for executing the method.

[0063] It is worthwhile noting that in an actual implementation of the evaluation unit 28, the phase subtraction stage 34 and the distance calculation stage 36 are not necessarily physically separate components. The different operations may, in particular, be carried out by a single (multi-purpose) processor.

[0064] While specific embodiments have been described in detail, those skilled in the art will appreciate that various modifications and alternatives to those details could be developed in light of the overall teachings of the disclosure. Accordingly, the particular arrangements disclosed are meant to be illustrative only and not limiting as to the scope of the invention, which is to be given the full breadth of the appended claims and any and all equivalents thereof.

Claims

1. Method for determining a distance, comprising:

providing at least two phase measurements made with modulated light of different modulation wavelengths, each phase measurement being indicative of said distance up to an integer multiple of a respective modulation wavelength;

providing a set of possible wraparound count combinations;

for each one of said possible wraparound count combinations, calculating a combination of unwrapped phase hypotheses corresponding to said at least two phase measurements; and

selecting a most plausible combination of unwrapped phase hypotheses among said combinations of unwrapped phase hypotheses and calculating said distance based upon said selected most plausible combination of unwrapped phase hypotheses,

said method being characterized in that said selecting of the most plausible combination of unwrapped phase hypotheses among said combinations of unwrapped phase hypotheses comprises

for each combination of unwrapped phase hypotheses, calculating a gap between a point having the respective unwrapped phase hypotheses as coordinates and an origin-crossing straight line having a direction vector with coordinate representation $[c/\lambda_1, \dots, c/\lambda_n]$, where $\lambda_1, \dots, \lambda_n$ designate the different modulation wavelengths and c designates the speed of light, and

selecting as said most plausible combination of unwrapped phase hypotheses the one for which said gap is smallest.

2. Method as claimed in claim 1, wherein said distance is calculated as an average over distance values associated with the unwrapped phase hypotheses of said most plausible combination of unwrapped phase hypotheses.

3. Method as claimed in claim 1 or 2, wherein said selecting of the most plausible combination of unwrapped phase hypotheses among said combinations of unwrapped phase hypotheses comprises

for each combination of unwrapped phase hypotheses, calculating a combination of distance values associated with the unwrapped phase hypotheses of the respective combination of unwrapped phase hypotheses,

for each combination of unwrapped phase hypotheses, calculating a variance or standard deviation of the respective combination of distance values, and selecting as said most plausible combination of unwrapped phase hypotheses the one for which said variance or standard deviation is smallest.

- 5 4. Method as claimed in any one of claims 1 to 3, wherein said distance is calculated as

$$\frac{\|\vec{\varphi}'_{est}\| \cdot c}{4\pi \cdot \|\vec{u}\|},$$

where $\vec{\varphi}'_{est}$ is an orthogonal projection onto said origin-crossing straight line of a point having said most plausible combination of unwrapped phase hypotheses as coordinates, and $\vec{u}$ is said direction vector $[c/\lambda_1, \dots, c/\lambda_n]$.

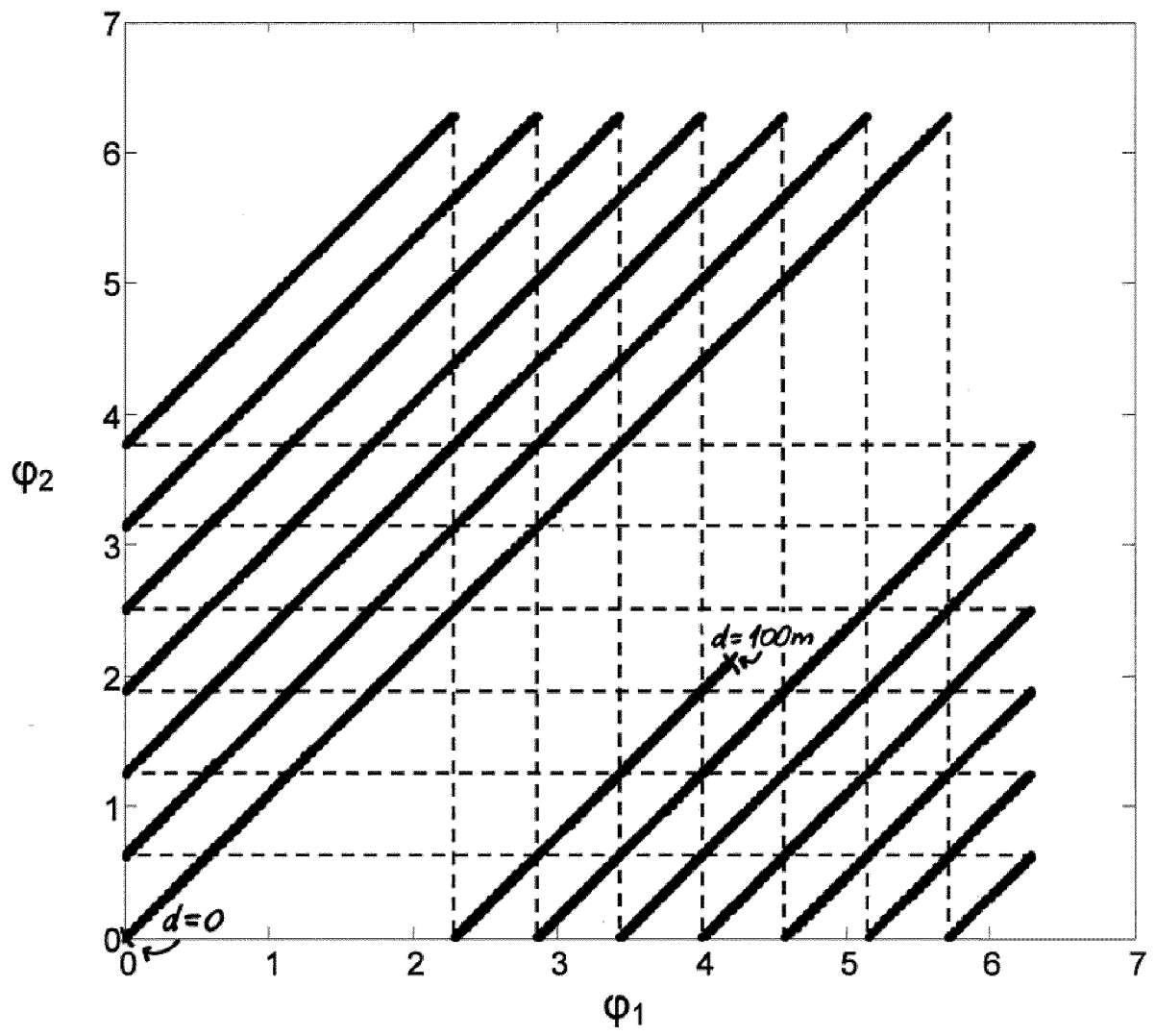
- 10 5. Method as claimed in any one of claims 1 to 3, wherein said calculating of the gap is carried out in a rotated coordinate system, in which said origin-crossing straight line is a coordinate axis.
6. Method as claimed in claim 5, wherein said distance is calculated as

15
$$\frac{(\vec{\varphi}''_{j_opt})_1 \cdot c}{4\pi \cdot \|\vec{u}\|}$$

where $(\vec{\varphi}''_{j_opt})_1$ is a coordinate of said point having said most plausible combination of unwrapped phase hypotheses as coordinates in said rotated coordinate system, and $\vec{u}$ is said direction vector $[c/\lambda_1, \dots, c/\lambda_n]$.

- 20 7. Computer program, comprising computer-implementable instructions, which, when executed by a computer, cause said computer to carry out the method as claimed in any one of claims 1 to 6.
8. Time-of-flight distance measuring device, comprising an electronic control unit with a memory, said memory having stored therein a computer program as claimed in claim 7, said electronic control unit being configured to execute said
- 25 computer program when determining a distance.
9. Time-of-flight distance measuring device, comprising an electronic control unit with and FPGA and/or an ASIC, said FPGA and/or ASIC configured and arranged to carry out the method as claimed in any one of claims 1 to 6.

Fig. 1



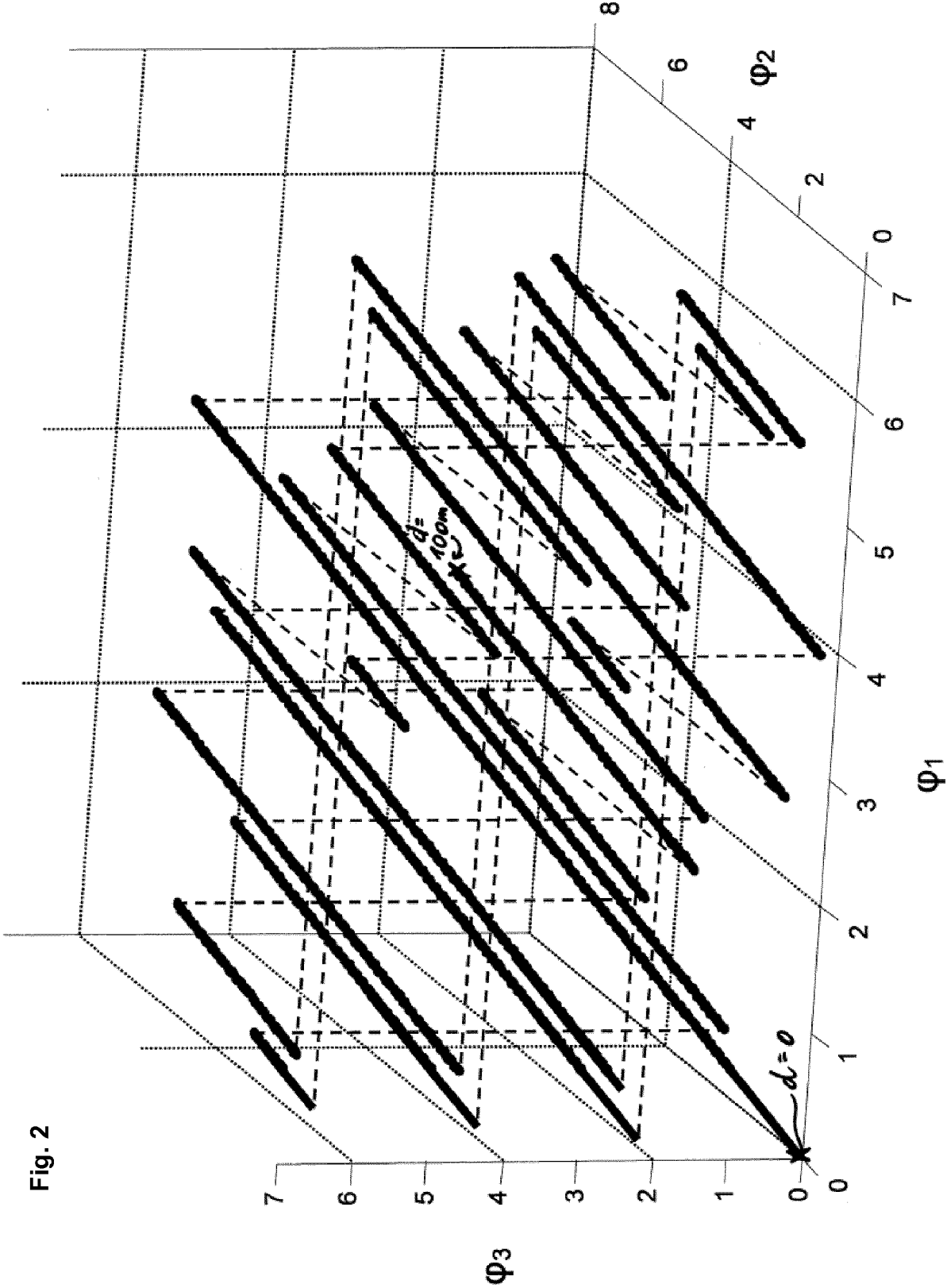


Fig. 3

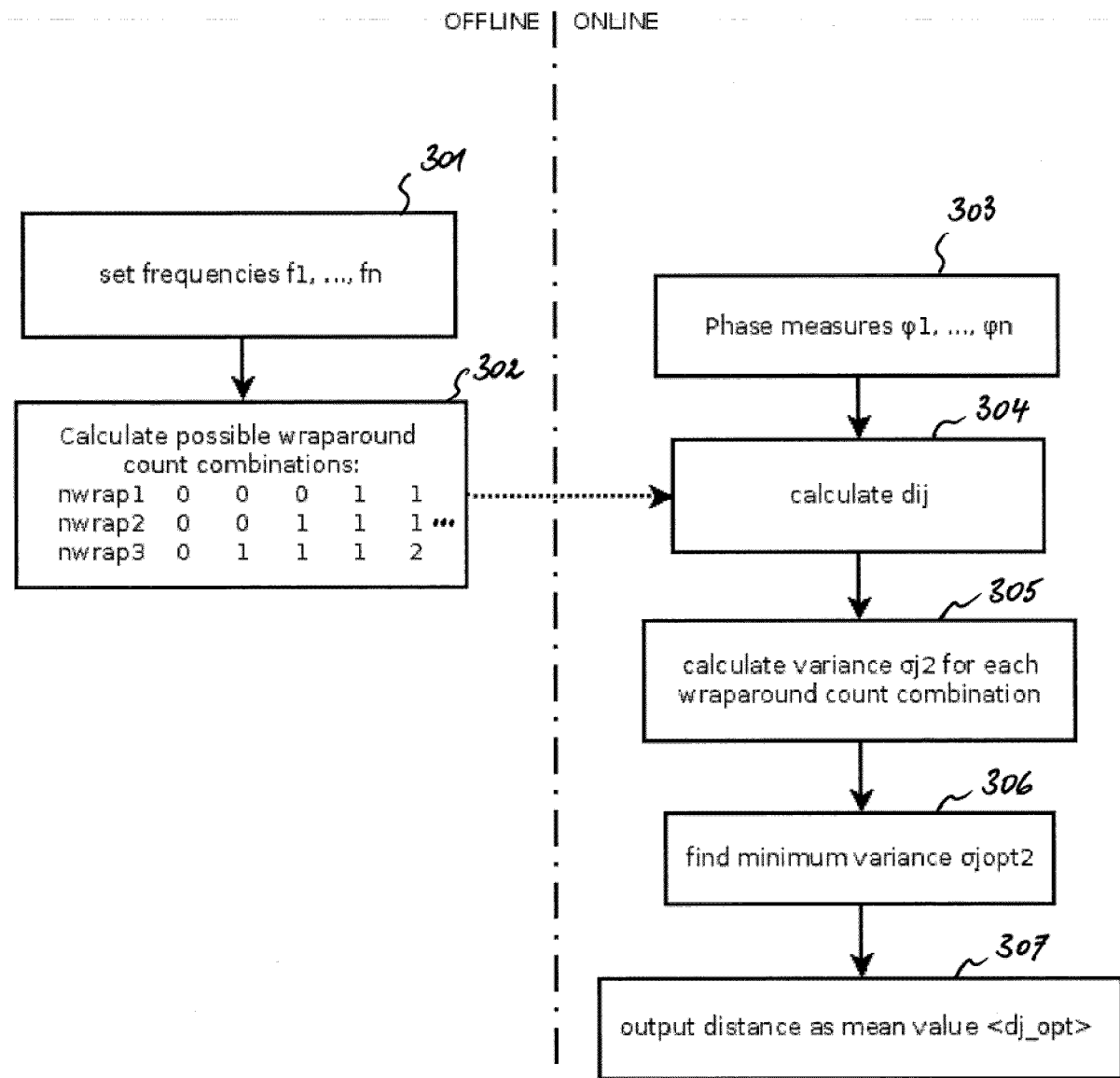


Fig. 4

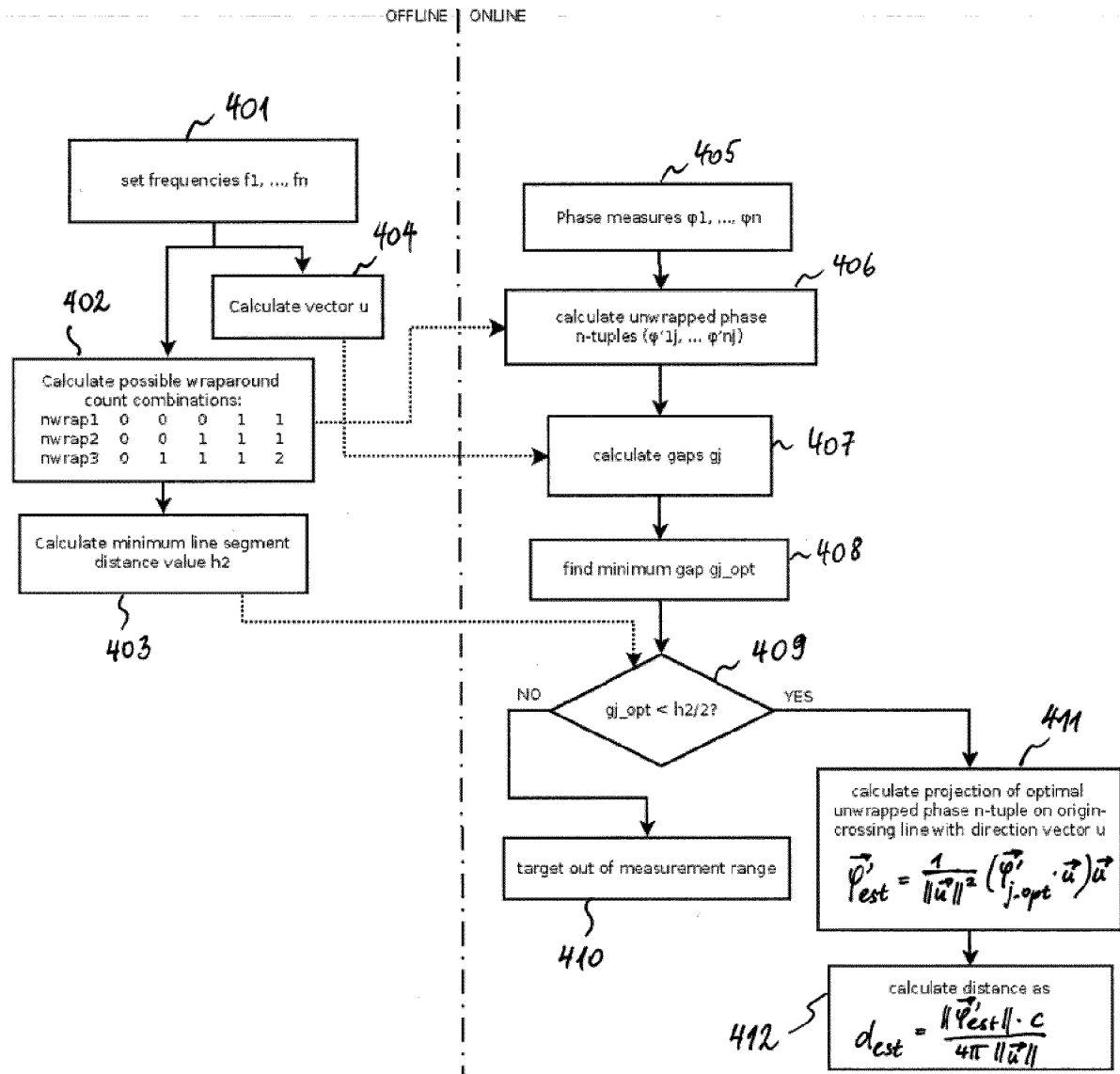


Fig. 5

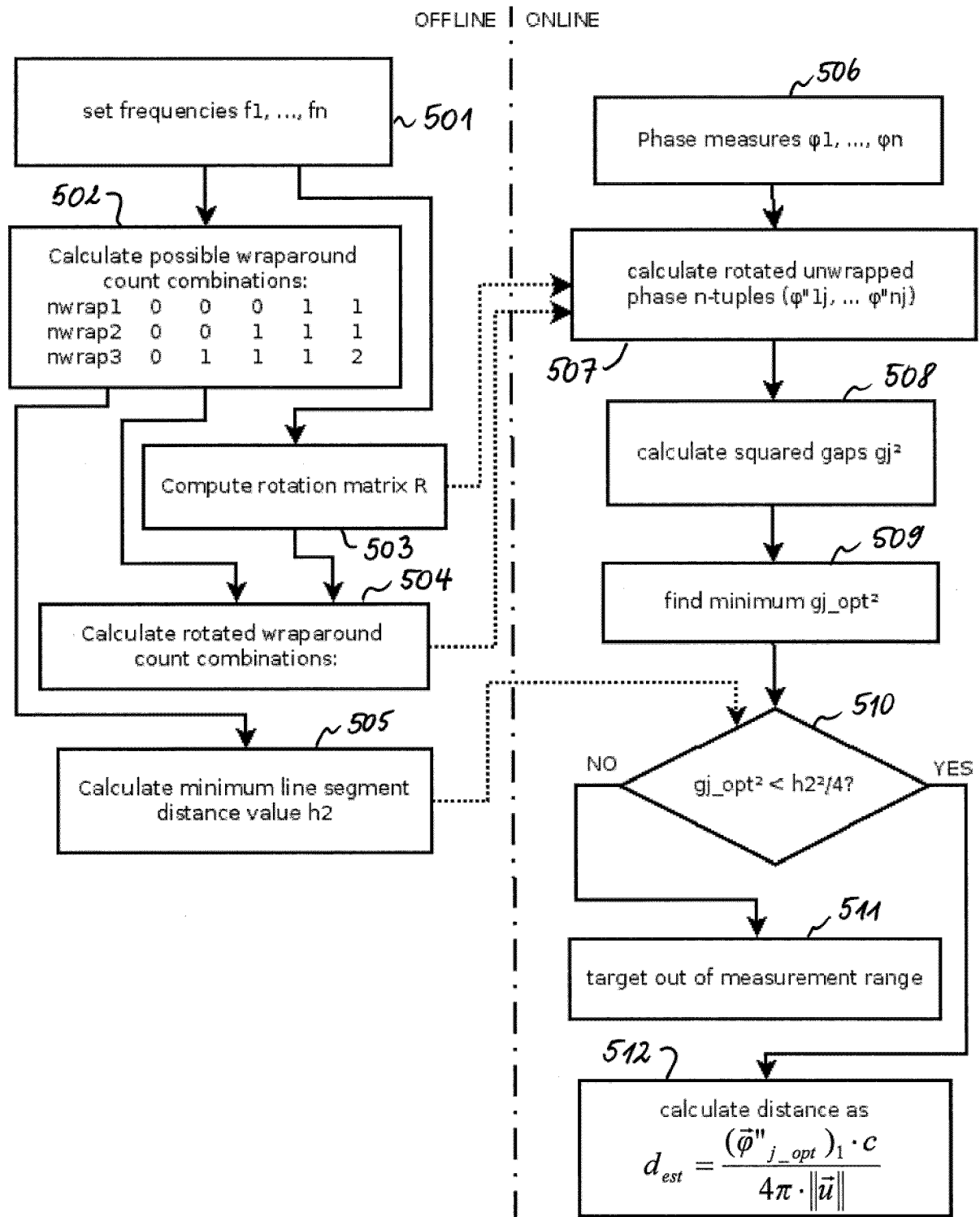
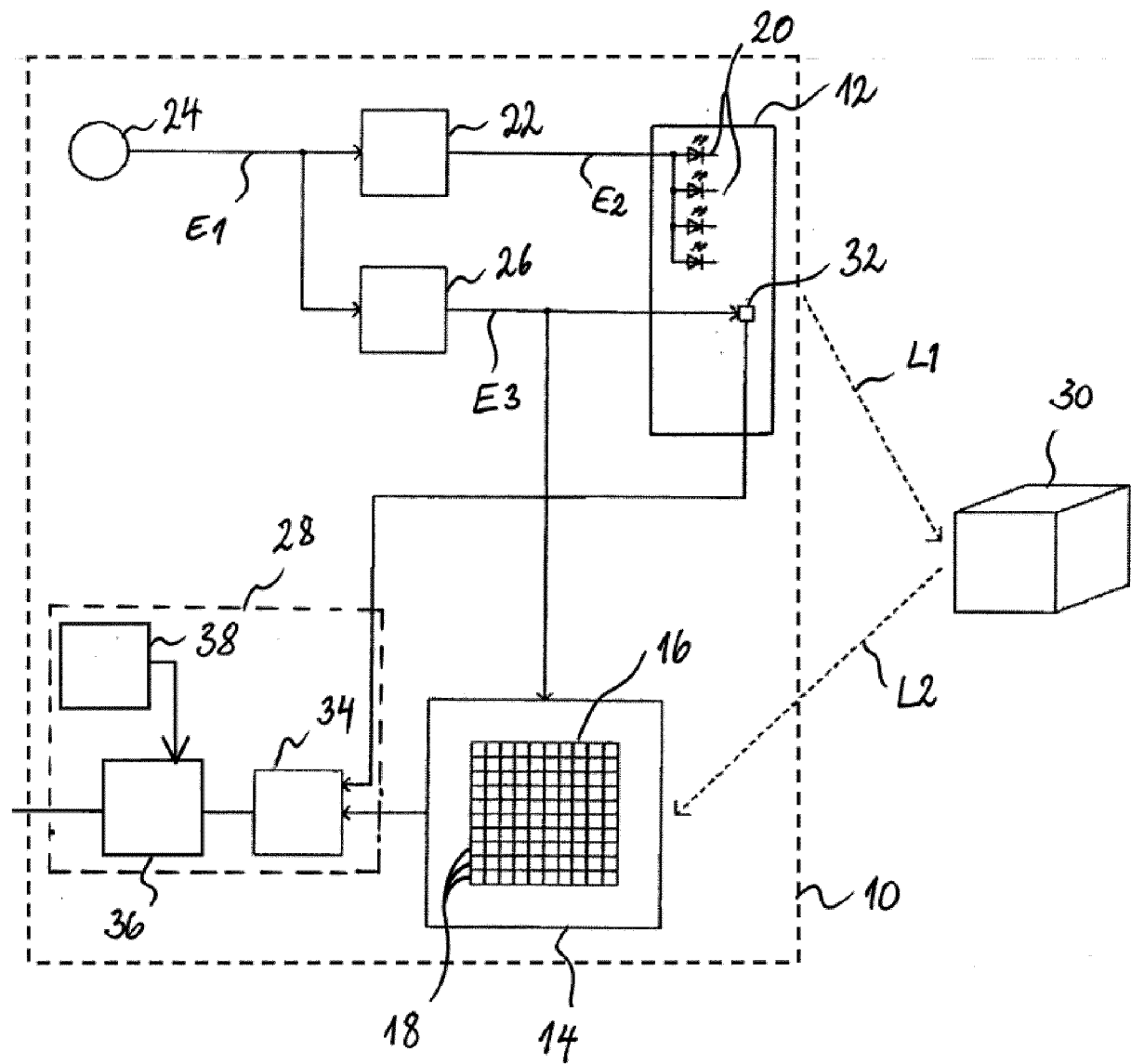


Fig. 6



INTERNATIONAL SEARCH REPORT

International application No
PCT/EP2014/055068

A. CLASSIFICATION OF SUBJECT MATTER INV. G01S17/89 G01S7/491 G01S17/36 ADD.		
According to International Patent Classification (IPC) or to both national classification and IPC		
B. FIELDS SEARCHED Minimum documentation searched (classification system followed by classification symbols) G01S Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched Electronic data base consulted during the international search (name of data base and, where practicable, search terms used) EPO-Internal, WPI Data, COMPENDEX, INSPEC		
C. DOCUMENTS CONSIDERED TO BE RELEVANT		
Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
A	DORRINGTON A A ET AL: "Achieving sub-millimetre precision with a solid-state full-field heterodyning range imaging camera; Sub-millimetre precision with a heterodyning range imaging camera", MEASUREMENT SCIENCE AND TECHNOLOGY, IOP, BRISTOL, GB, vol. 18, no. 9, 20 July 2007 (2007-07-20), pages 2809-2816, XP020118817, ISSN: 0957-0233, DOI: 10.1088/0957-0233/18/9/010 abstract page 2813, right-hand column, line 26 - line 54; figures 3,4 ----- -/--	1-9
☒ Further documents are listed in the continuation of Box C. ☒ See patent family annex.		
* Special categories of cited documents : "A" document defining the general state of the art which is not considered to be of particular relevance "E" earlier application or patent but published on or after the international filing date "L" document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified) "O" document referring to an oral disclosure, use, exhibition or other means "P" document published prior to the international filing date but later than the priority date claimed "T" later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention "X" document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step when the document is taken alone "Y" document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art "&" document member of the same patent family		
Date of the actual completion of the international search 14 May 2014		Date of mailing of the international search report 20/05/2014
Name and mailing address of the ISA/ European Patent Office, P.B. 5818 Patentlaan 2 NL - 2280 HV Rijswijk Tel. (+31-70) 340-2040, Fax: (+31-70) 340-3016		Authorized officer Mercier, Francois

INTERNATIONAL SEARCH REPORT

International application No
PCT/EP2014/055068

C(Continuation). DOCUMENTS CONSIDERED TO BE RELEVANT		
Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
A	PAYNE ANDREW D ET AL: "Multiple frequency range imaging to remove measurement ambiguity", 9TH CONFERENCE ON OPTICAL 3-D MEASUREMENT TECHNIQUES JUL 1, 2009 - JUL 3, 2009. VIENNA, AUSTRIA, 2 July 2009 (2009-07-02), pages 139-148, XP002660844, Retrieved from the Internet: URL:http://researchcommons.waikato.ac.nz/bitstream/10289/4032/1/Multiple%20Frequency%20Range%20Imaging.pdf abstract	1-9
A	----- DE 100 39 422 A1 (SIEMENS AG [DE]) 28 February 2002 (2002-02-28) cited in the application abstract	1-9
A	----- US 7 791 715 B1 (BAMJI CYRUS [US]) 7 September 2010 (2010-09-07) cited in the application abstract	1-9
A	----- DROESCHEL D ET AL: "Multi-frequency Phase Unwrapping for Time-of-Flight cameras", INTELLIGENT ROBOTS AND SYSTEMS (IROS), 2010 IEEE/RSJ INTERNATIONAL CONFERENCE ON, IEEE, PISCATAWAY, NJ, USA, 18 October 2010 (2010-10-18), pages 1463-1469, XP031920128, DOI: 10.1109/IROS.2010.5649488 ISBN: 978-1-4244-6674-0 cited in the application the whole document -----	1-9

INTERNATIONAL SEARCH REPORT

Information on patent family members

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