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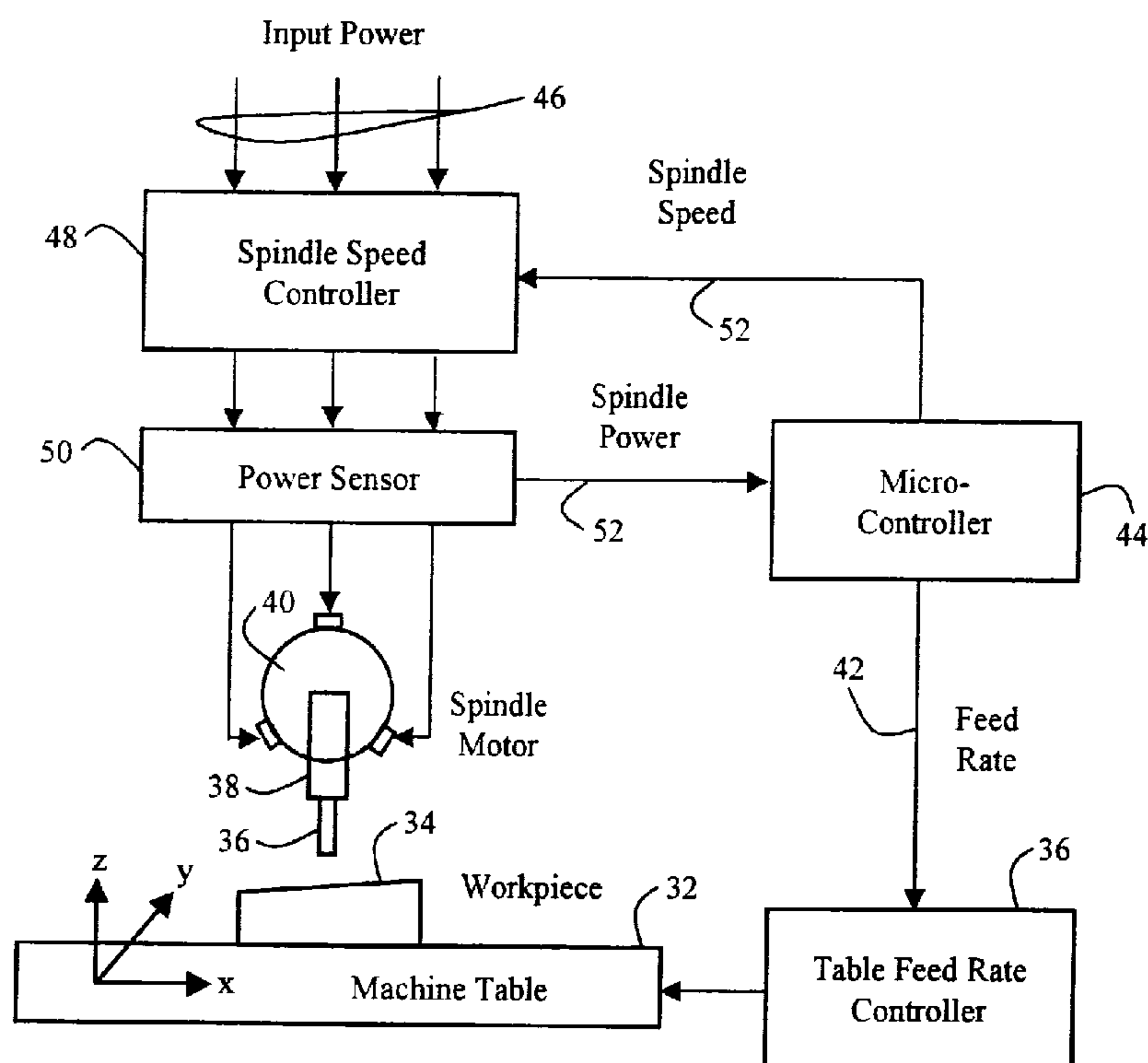
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(54) **MACHINES A COMMANDE PAR ORDINATEUR/COMMANDE  
NUMERIQUE**

(54) **COMPUTER/NUMERICALLY CONTROLLED MACHINES**



(57) A computer-numerically controlled material removal machine, such as a milling machine, lathe, grinding machine, shaping machine, or the like, has drive units for moving the workpiece and the cutting tool to cause the tool to remove material from the workpiece and a computer-numerical control unit for controlling the drive units so as to optimize material removal rates. In some embodiments, the control unit senses electrical energy consumption rate at a cutting tool drive motor and varies either or both of cutting tool speed and workpiece feed rate to maintain the energy consumption rate substantially equal to a preset reference level. In other cases, the control unit derives a signal representing force exerted between the cutting tool and the workpiece, whether by sensing power or by using a dynamometer to measure force between the workpiece and the cutting tool, and controls a plurality of variables, conveniently by means of a fuzzy logic controller.

**ABSTRACT OF THE DISCLOSURE**

A computer-numerically controlled material removal machine, such as a milling machine, lathe, grinding machine, shaping machine, or the like, has drive units for  
5 moving the workpiece and the cutting tool to cause the tool to remove material from the workpiece and a computer-numerical control unit for controlling the drive units so as to optimize material removal rates. In some embodiments, the control unit senses electrical energy consumption rate at a cutting tool drive motor and varies either or both of cutting tool speed and workpiece feed rate to maintain the energy consumption rate substantially  
10 equal to a preset reference level. In other cases, the control unit derives a signal representing force exerted between the cutting tool and the workpiece, whether by sensing power or by using a dynamometer to measure force between the workpiece and the cutting tool, and controls a plurality of variables, conveniently by means of a fuzzy logic controller.

COMPUTER/NUMERICALLY CONTROLLED MACHINES

## DESCRIPTION

## TECHNICAL FIELD:

5           The invention relates to machines for removing material from a workpiece by means of a cutting tool, and is applicable to computer/numerically-controlled milling machines, drilling machines, grinding machines, planing machines, lathes, and other such machines which have at least one drive motor for effecting relative movement between the workpiece and the cutting tool to effect material removal and which employ  
10 computer/numerical control of such movement. The invention also encompasses control systems and for such machines and conversion of existing machines.

## BACKGROUND ART:

          Computer/numerically-controlled machines have a control system which includes  
15 a computer that is programmed with numerical control codes for controlling movement of a workpiece-supporting table relative to a cutting tool, or vice versa. Many such machines have open-loop control systems which are designed to execute numerical control codes regardless of the on-line cutting geometry variation, tool conditions, and the dynamics of the cutting process. This leads to under-utilization of machine capacity,  
20 unsafe machining processes, and excessive human intervention. Usually, one or more rough cuts are made to remove most of the unwanted material quickly. It is desirable to provide closed loop control to maximise material removal rate without exceeding safe limits for the force exerted upon the cutting tool. It is known, therefore, to equip such a machine with a dynamometer mounted between the workpiece and the machine table  
25 to provide a measure of the force exerted between the cutting tool and the workpiece and attempt to maintain the force at a predetermined level by adjusting the feed rate of the table.

          Such a control system has a number of disadvantages. For example, the dynamometer is limited in size, which limits the size of workpiece that can be mounted  
30 upon it, and is exposed to cutting fluid, swarf, and other potential contaminants, as well as, potentially, overload and collision damage. Moreover, such dynamometers are relatively expensive and the systems are complicated to set up and prone to vibration and instability.

**DISCLOSURE OF INVENTION:**

The present invention seeks to eliminate or at least mitigate one or more of the above-mentioned disadvantages and provide a material removal machine which allows better control of material removal rate.

5       According to one aspect of the present invention, there is provided a material removal machine comprising a carrier for carrying a workpiece fixed relative thereto, a holder for a cutting tool, drive means for effecting relative movement between the carrier and the holder to effect material removal, a sensor for monitoring energy consumption rate of an element of the drive means, a control unit responsive to the  
10 sensor for controlling the drive means to vary said relative movement so as to tend to maintain energy consumption rate substantially at a predetermined level.

      According to a second aspect of present invention, there is provided a control system for a material removal machine comprising a carrier for carrying a workpiece fixed relative thereto, a holder for a cutting tool, and drive means for effecting relative  
15 movement between the carrier and the holder to effect material removal, the system comprising a power sensor for monitoring energy consumption rate of an element of the drive means and a control unit responsive to the sensor for controlling the drive means to vary said relative movement so as to maintain energy consumption rate substantially at a predetermined level.

20       It is also desirable to increase material removal rates towards an optimum level for a particular machine, workpiece, and cutting tool. To this end, a third aspect of the present invention comprises a material removal machine in which the number of variables being controlled is greater than the number of variables being monitored.

      According to the third aspect of the invention, a material removal machine  
25 comprises a carrier for carrying a workpiece fixed relative thereto, a support for a cutting tool, drive means for effecting relative movement between the carrier and the support to effect material removal, a sensor operable to provide a signal representing a parameter indicative of energy consumption rate of the drive means or a cutting force exerted between a cutting tool mounted to the support and a workpiece mounted to the  
30 carrier, control means for comparing said signal with a reference and controlling the drive means to maintain the energy consumption or cutting force substantially equal to a desired value, wherein the number of parameters being controlled is greater than the number of number of parameters being monitored.

According to a fourth aspect of the invention, there is provided a control system for a material removal machine comprising a carrier for carrying a workpiece fixed relative thereto, a holder for a cutting tool, and drive means for effecting relative movement between the carrier and the holder to effect material removal, the control  
5 system comprising a sensor operable to provide a signal representing energy consumption rate of the drive means or cutting force exerted between a cutting tool carried by the holder and a workpiece carried by the carrier, and control means for comparing said signal with a reference and controlling two different parameters of the drive means to maintain the force substantially equal to a desired value.

10 Preferably, the control unit controls movement of both the workpiece carrier and the cutting tool. In either case, such movement may be linear or rotational.

In preferred embodiments of the above aspect of the invention, the control unit determines two variables, namely the difference ( $P_{ref} - P(t)$ ) between the instant actual energy consumption rate ( $P(t)$ ) and a reference energy consumption rate ( $P_{ref}$ ), and the  
15 difference ( $P(t) - P(t-1)$ ) between a current actual energy consumption rate ( $P(t)$ ) and a previous actual energy consumption rate ( $P(t-1)$ ), and determines therefrom a value for controlling the relative movement of the cutting tool and workpiece carrier.

In one preferred embodiment, the control unit compares the two variables ( $P_{ref} - P(t)$ ) and ( $P(t) - P(t-1)$ ) with a table of predetermined values for the rate of movement  
20 of the workpiece support or the cutting tool holder to extract therefrom a desired adjustment to cause the actual energy consumption rate to correspond more closely with the desired energy consumption rate.

Thus, in the table, one of the ordinates comprises a range of values of one of the variables ( $P_{ref} - P(t)$ ) and the other ordinate comprises a range of values of the other of  
25 the variables ( $P(t) - P(t-1)$ ), and the control unit uses the instant values of the two variables to select the corresponding recommended value for cutting tool holder movement and/or workpiece carrier movement.

The actual values contained within the table may conveniently be derived empirically, using predetermined data for the workpiece material, type of machine, from  
30 experience and/or by experiment.

Preferably, the control unit has two such tables, one containing values for movement of the workpiece carrier and the other containing values for movement of the cutting tool holder, both tables being indexed by the same variables ( $P_{ref} - P(t)$ ) and ( $P(t)$ )

-  $P(t-1)$ ) and the control unit compares the two variables with both tables, obtains therefrom recommended adjustments ( $\Delta f$  and  $\Delta v$ ) for workpiece carrier movement and cutting tool holder movement, respectively, and controls both accordingly.

Preferably, the control unit employs a fuzzy logic controller to determine the  
5 desired values. Then the fuzzy logic controller fuzzifies the values of  $P(t)-P(t-1)$  and uses them as indexes to select from a table, corresponding sets of fuzzy rules for the respective adjustments. The fuzzy logic controller then uses membership functions to reduce the sets and a defuzzified to convert the resulting recommendations into crisp adjustments values.

10 Another aspect of the invention comprises an assemblage or kit for adapting an existing computer-numerically controlled machine having a carrier, tool holder and a microcontroller, the assemblage or kit comprising a sensor for connection to the drive means for providing a signal representing energy consumption rate of the drive means  
15 or cutting force exerted between a cutting tool carried by the holder and a workpiece carried by the carrier, and software for programming the microcontroller to compare the signal with a reference level and, in dependence thereupon, control the drive means to reduce said difference.

Yet another aspect of the invention comprises the aforementioned software, conveniently carried by a storage medium.

20 Various objects, features and advantages of the invention will become apparent from the following description, taken in conjunction with the accompanying drawings, of preferred embodiments which are described by way of example only.

#### BRIEF DESCRIPTION OF THE DRAWINGS:

- 25 Figure 1, labelled PRIOR ART, illustrates a computer/numerically controlled milling machine employing a dynamometer in a feedback control system;  
Figure 2 illustrates an embodiment of the present invention in the form of a computer-numerically-controlled milling machine employing a power sensor;  
Figure 3 is a block schematic diagram of a control unit of the machine of Figure 2;  
30 Figure 4 illustrates the structure of a fuzzy logic controller of the control unit;  
Figures 5(a) and 5(b) illustrate membership functions used by the fuzzy logic controller;  
Figure 6 illustrates a degree of membership for triangular fuzzy sets;  
Figure 7 illustrates fuzzy inference operation for table feed rate under crisp inputs; and

Figure 8 illustrates defuzzification of feed rate using centre of area (COA).

#### BEST MODE(S) FOR CARRYING OUT THE INVENTION:

Before embodiments of the present invention are described, a prior art machine  
5 tool will be described with reference to Figure 1, labelled PRIOR ART, which illustrates  
a milling machine 10 which has a machine table 12 supporting a workpiece 14 beneath  
a cutting tool 16 mounted upon a spindle 18 driven by a drive motor 20. Three-phase  
electrical power from a supply 22 is supplied to the drive motor 20 by way of a spindle  
control unit 24 which can be adjusted to set the drive motor speed to different, but fixed,  
10 levels.

The table 12 is movable in two or more orthogonal directions, identified in Figure  
1 as  $x$ ,  $y$  and  $z$ , by one or more motors 26 controlled by a control unit 28, specifically  
a microcontroller. A dynamometer 30 is mounted upon the table 12 and the workpiece  
14 is mounted upon the dynamometer 30. During operation of the milling machine 10,  
15 the dynamometer 30 produces a signal representing the force exerted between the  
workpiece 14 and the cutting tool 16 and supplies it to the microcontroller 28 which  
compares it with a reference and, depending upon the difference, controls the motors 26  
to increase or decrease the rate of movement of the table 12.

A disadvantage of such a control using traditional control algorithms is that it is  
20 relatively sensitive to changes in the machine, cutting tool and workpiece. Usually, such  
a machine is developed for very few machine-tool-workpiece combinations. If it is used  
for other machine-tool-workpiece combinations, excessive oscillations, overshoot, and  
instability may occur, leading to premature tool failure and even machine breakdown.  
Also, the dynamometer 30 is exposed to a relatively harsh environment and limits the  
25 size of workpiece which can be machined.

An embodiment of the present invention will now be described which addresses  
these disadvantages by means of a control system which employs both electrical power-  
sensing and fuzzy-logic and is capable of adjusting several machine parameters, for  
example both machine table feed rate and spindle speed.

30 Referring to Figure 2, a milling machine with a control system embodying the  
present invention comprises a machine table 32 supporting a workpiece 34 beneath a  
cutting tool 36 carried by a spindle 38 driven by a drive motor 40. The machine table  
32 is movable in at least two orthogonal directions, identified in Figure 2 as  $x$ ,  $y$  and  $z$ ,

by a table feed controller 36 which comprises several motors controlled in response to a control signal received on line 42 from a microcontroller 44. Three-phase electrical power from a supply 46 is supplied to the drive motor 40 by way of a spindle speed controller 48, which can be adjusted to vary the drive motor speed continuously, and a  
5 power sensor 50 which measures the instantaneous power supplied to the drive motor 40 and supplies a corresponding power signal to the microcontroller 42 via line 52. As will be described more fully later, the microcontroller 44 is programmed to function as a fuzzy logic controller and uses the spindle power signal, and data stored in tables, to compute desired values for the spindle speed control signal and the feed rate control  
10 signal which it supplies on lines 52 and 42 to the spindle control unit 48 and the table feed rate controller 36, respectively.

The spindle control unit 48 comprises an adjustable frequency AC drive unit having a port for the analog spindle control signal and which provides continuous variation of the spindle speed in dependence upon such signal. Such a control unit 48  
15 is of known construction and so will not be described in detail. A suitable such unit is marketed by Saftronics Corporation of Fort Myers, Florida, U.S.A., as a "Model G3".

The microcontroller 44 includes a digital-to-analog converter so that it can supply the spindle speed control signal as an analog signal on line 52.

A suitable power sensor 48, which measures three-phase power consumption  
20 rather than current only, is marketed under the name "Universal Power Cell" by Load Controls Incorporated of Sturbridge, Massachusetts, U.S.A.

In contrast to existing control systems, which require the feed rate for a particular workpiece profile to be calculated in advance and programmed into the microcontroller, in the control system illustrated in Figure 2, the microcontroller 44 has tables storing  
25 control rules for feed rates and spindle speeds and uses so-called fuzzy logic to determine the recommended values of both parameters, despite the fact that the system monitors only the one input variable, namely spindle power.

Referring now to Figure 3, which shows, schematically, the functions performed by the microcontroller 44, the current power consumption level  $P$  from the power sensor  
30 50 is supplied, as a digital value, to a summing device 60 which sums it with the reference power value  $P_{ref}$ , conveniently obtained from memory. A scaling factor 62 multiplies the output of summing device 60, which is the error signal  $EP(t)$ , by a variable  $K_e$  and supplies the resulting value to one input of fuzzy logic controller (FLC)

64. The power sensor 50 also supplies the current power consumption level signal  $P$  to a one sample delay 68 to produce a delayed or "previous" power consumption signal  $P(t-1)$  which summing device 70 subtracts from the current power consumption value  $P$  to produce a power consumption signal value  $CP(t)$ . A second scaling factor 72 multiplies the signal value  $CP(t)$  by variable  $K_c$  and supplies the resulting value to a second input of fuzzy logic controller 64.

The fuzzy logic controller 64 processes the two scaled values  $EP(t)$  and  $CP(t)$  to produce two recommended adjustment values  $\Delta f(t)$  and  $\Delta v(t)$ . More particularly, the fuzzy logic controller 64 uses the two variables, i.e.  $P_{ref} - P(t)$  and  $P - P(t-1)$  to address each of two tables, one table providing a recommended adjustment  $\Delta f(t)$  for controlling the feed rate of the machine table 32 and the other table providing a corresponding recommended adjustment  $\Delta v(t)$  for adjusting the rotational speed of spindle 38 (Figure 2). The values  $\Delta f$  and  $\Delta v$  are supplied to the scaling factors 74 and 76, respectively, which multiply them by variables  $K_f$  and  $K_v$ , respectively, and supply the scaled values to summing devices 78 and 80, respectively, which are coupled also to delay elements 82 and 84, respectively. The latter delay the sample values by one sample period to produce delayed recommended values  $f_{com}(t-1)$  and  $v_{com}(t-1)$ , respectively. The summing devices 78 and 80 sum the recommended values with their respective delayed recommended values to produce the final adjustment values  $f_{com}(t)$  and  $v_{com}(t)$  which are converted to analog signals by digital-to-analog converters (not shown). These analog signals are supplied to the table feed controller 36 and spindle speed controller 48, respectively, for adjusting the table feed rate and spindle speed, respectively.

The tuning mechanism 86 also receives the actual power samples  $P(t)$  and the reference power level  $P_{ref}$ , derives from them a control signal, and uses the control signal to adjust the four scaling factors 62, 72, 74 and 76 so as to provide better stability and avoid "hunting" or erratic variations in the recommended and desired values.

In effect, the summing devices 70, 78 and 80 and delay elements 68, 82 and 84, being connected in feedback loops, constitute low pass filters for smoothing the signals.

As illustrated in Figure 4, the fuzzy logic controller 64 has the usual structure, namely a fuzzifier 88 which receives and "fuzzifies" the sample values  $CP(t)$  and  $EP(t)$ , a fuzzy inference engine 90 which processes the sample values and a defuzzifier 92 which defuzzifies the output of the fuzzy inference engine 90 to provide "crisp" values for the recommended values  $\Delta f(t)$  and  $\Delta v(t)$ . The fuzzy inference engine 90 uses

membership functions and fuzzy rules extracted from Membership Function store 94 and Fuzzy Rule base 96, respectively. Tables of feed rate rules and spindle speed rules are illustrated below in tabular form in Tables 1(a) and 1(b), respectively. In both tables, the horizontal ordinates represent ranges of values of the rate of change of energy  
 5 consumption  $CP(t)$ , which is equal to  $P(t) - P(t-1)$ , and the vertical ordinate represents ranges of values of the error or difference signal  $EP(t)$ , which is equal to  $P_{ref} - P(t)$ . The actual values in the tables are derived empirically from handbooks for the machine, handbooks for specific cutting rates for the material concerned, from experience and/or by experiment.

10 While the structure and operation of the fuzzy logic controller 64 are generally conventional, its operation will now be described briefly with reference also to Figures 5(a) to 8.

#### **Fuzzification of Inputs $CP(t)$ and $EP(t)$ by Fuzzifier 86**

The first step of fuzzy control policy is to take the input values  $CP(t)$  and  $EP(t)$   
 15 and determine the degree to which they belong to each of the appropriate fuzzy sets in the various input universes of discourse. The two inputs power change  $CP(t)$  and power error  $EP(t)$  applied to the fuzzifier 86 shown in Figure 4 are derived from the same power sensor 50.

At each sampling instant,  $t$ , the power error  $EP(t)$  and the power change  $CP(t)$   
 20 are respectively calculated as

$$EP(t) = P_{ref} - P(t) \quad (1)$$

$$CP(t) = P(t) - P(t-1) \quad (2)$$

The scaling factors 62 and 72 multiply them by scaling factors,  $K_e$  and  $K_c$  so as to normalize the power error signals  $EP(t)$  and  $CP(t)$  and map them into suitable  
 25 linguistic values.

The input data  $CP(t)$  and  $EP(t)$  are crisp, and fuzzification is required to map the range of crisp inputs to corresponding fuzzy values for the system input variables. This process can be expressed by:

$$x = \text{fuzzifier}(x_0) \quad (3)$$

30 where  $x_0$  is a vector of crisp values of one input variable from the process, and  $x$  is a vector of fuzzy sets defined for the variable.

#### **Membership Functions (92)**

To transform crisp inputs into fuzzy inputs, membership functions must first be determined for each of the inputs CP(t) and EP(t). Once membership functions are specified, a real time input value, such as a power error, is sampled and used to produce fuzzy inputs via membership function. There are usually several fuzzy inputs  
5 corresponding to a single crisp input since the crisp input can have partial membership grades in several fuzzy sets. The membership grading is represented by a real number ranging between 0 and 1 within the closed interval.

To simplify calculations, triangular shape membership functions were used in this embodiment. As illustrated in Figures 5(a) and 5(b), seven fuzzy sets are used for the  
10 inputs and outputs of the controller 86, namely NB, negative big; NM, negative medium; NS, negative small; ZE, zero; PS, positive small; PM, positive medium; and PB, positive big.

The universe of discourse of all inputs and outputs was within the range of [-1, 1]. It should be noted that any output deviating from zero will trigger an adjustment  
15 when the NS and PS sets intersect at zero and hence lead to unnecessary oscillation. This was remedied by maintaining a narrow open area between NS and PS sets in Figure 5(b).

Mathematically, the membership function,  $\mu_A$ , for a fuzzy set, A, is given by

$$\mu_A : X \rightarrow [0,1] \quad (4)$$

20 Hence, the degree of membership for triangular fuzzy sets, as illustrated in Figure 6, can be defined as:

$$\mu_A(x) = \begin{cases} \frac{x+b}{a+b} & \text{for } -b \leq x \leq a \\ \frac{x-b}{a-b} & \text{for } a \leq x \leq b \end{cases} \quad (5)$$

### Control Rules

One of the most crucial components of the fuzzy controller 86 is the fuzzy control  
25 rule module 94 (Figure 4). The set of control rules defines the system behaviour and replaces the mathematical modelling of the system. The fuzzy rules, which use the fuzzy inputs to determine system actions, are obtained from the knowledge of skilled operators, by experiments, and/or prior knowledge of the end milling processes. Each of the rules

can be written as an IF-THEN statement that describes the action to be taken in response to various fuzzy inputs. For example, as shown in Tables 1(a) and 1(b) below:

If EP(t) is NB and CP is ZE then f is NM; also v is PB

The above rule, in natural language, states that if power error EP(t) falls in the "negative big" (NB) fuzzy set and power change CP(t) is in the "zero" set (ZE), i.e. the actual energy consumption rate P(t) is well below the desired energy consumption rate  $P_{ref}$ , and stable, then the suggested adjustment for table feed rate is negative medium (NM) and the suggested speed adjustment is "positive big" PB, i.e. reduce the table feed rate a moderate amount and increase the cutting tool speed a large amount. Each statement  
 5 such as the one above is called a premise. Usually there are several premises for one input, which leads to a consequence or an action by the controller 86. This process will be discussed in detail in the next section.

Once the fuzzy rules had been formulated, the decision-making tables Table 1(a) and Table 1(b) for the two-input, two-output system were constructed as shown below:

15

**CP**

20

<b>EP</b>		NB	NM	NS	ZE	PS	PM	PB
	NB	NS	NS	NM	NM	NM	NB	NB
	NM	ZE	NS	NM	NM	NB	NB	NB
	NS	PS	ZE	ZE	NS	NS	NM	NB
	ZE	PS	PS	PS	ZE	ZE	NS	NS
	PS	PM	PM	PS	PS	ZE	NS	NS
	PM	PB	PM	PM	PS	PS	ZE	NS
	PB	PB	PB	PB	PM	PM	PS	ZE

25

Table 1(a) Fuzzy rules for adaptive control of table feedrate before rule reduction

**CP**

<b>EP</b>		NB	NM	NS	ZE	PS	PM	PB
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	NB	PM	PM	PM	PB	PB	PB	PM
	NM	PS	PS	PM	PB	PB	PB	PB
	NS	NS	ZE	ZE	PS	PS	PM	PM
	ZE	NS	NS	ZE	ZE	ZE	PS	PM
5	PS	NM	NM	NS	ZE	ZE	PS	PS
	PM	NB	NM	NM	NS	NS	ZE	PS
	PB	NB	NB	NM	NM	NM	NS	ZE

10 Table 1(b) Fuzzy rules for adaptive control of spindle speed before rule reduction

### Fuzzy Inference Engine 88

In this stage of the process, the fuzzy rules and the membership degree of the fuzzy inputs will determine the fuzzy outputs. A technique called max-min inference is used to calculate a numerical value representing the aggregate effect of all the rules triggered by a pair of input values (CP(t) and EP(t)). The result is a fuzzy output for each type of consequent action.

It has been determined that the union of fuzzy sets A and B is expressed as

$$C := A \vee B : \quad (6)$$

and the membership function of C is given by

$$20 \quad \mu_C(x) =_{\text{def}} \text{MAX}\{\mu_A(x), \mu_B(x)\} \text{ for all } x \in X \quad (7)$$

Similarly, the intersection of fuzzy sets A, B, is written as

$$D := A \wedge B : \quad (8)$$

and the membership function of D is

$$\mu_D(x) =_{\text{def}} \text{MIN}\{\mu_A(x), \mu_B(x)\} \text{ for all } x \in X \quad (9)$$

25 For the two-input, two-output fuzzy system, the operation can be described as follows, and illustrated in Figure 8:

Premise 1: If EP is  $a_1$  AND CP is  $b_1$  Then f is  $c_1$  also v is  $d_1$

Premise 2: If EP is  $a_2$  AND CP is  $b_2$  Then f is  $c_2$  also v is  $d_2$

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30 Premise n (Knowledge): If EP is  $a_n$  AND CP is  $b_n$  Then f is  $c_n$  and v is  $d_n$

Premise n+1 (Fact): EP is A AND CP is B

Consequence 1: f is C

Consequence 2: v is D

Figure 7 shows the MAX-MIN inferencing process for the crisp input values  $EP_0$  and  $CP_0$  which are regarded as fuzzy singletons.

In general, for an n-rule controller with inputs  $A = EP_0$  and  $B = CP_0$ , the consequences C and D can be expressed as:

$$\mu C(f') = (\mu_{A1}(EP_0) \wedge \mu_{B1}(CP_0) \wedge \mu_{C1}(f') \vee \dots (\mu_{An}(EP_0) \wedge \mu_{Bn}(CP_0) \wedge \mu_{Cn}(f')) \quad (10)$$

$$\mu C(S') = (\mu_{A1}(EP_0) \wedge \mu_{B1}(CP_0) \wedge \mu_{C1}(v') \vee \dots (\mu_{An}(EP_0) \wedge \mu_{Bn}(CP_0) \wedge \mu_{Cn}(v')) \quad (11)$$

### Defuzzification 90

Defuzzification is the process of mapping the inferred fuzzy control actions to crisp control actions. A defuzzification strategy is aimed at producing a non-fuzzy control action that best represents the possibility distribution of the inferred fuzzy control action. This can be expressed by:

$$f_0 = \text{Defuzzifier } f' \quad (12)$$

where  $f'$  is the fuzzy control action,  $f_0$  the crisp control action, and Defuzzifier is the defuzzification operator.

The Center of Area (COA) method is the most commonly used defuzzification strategy in real-time implementations of fuzzy logic control. The COA method generates the centre of gravity of the possible distribution of a control action. The crisp output,  $f_0$ , associated with the centre of gravity for the resulting fuzzy set C is obtained using the COA method as follows:

$$f_0 = \frac{\int f' \mu_c(f') df'}{\int \mu_c(f') df'} \quad (13)$$

Figure 8 Illustrates defuzzification of table feedrate recommendations  $f_0$  for two fuzzy sets  $c1$  and  $c2$ . The calculation for the spindle speed is similar to that described above for feedrate.

Given the crisp output values  $f_0$  and  $v_0$ , the control commands can be calculated for each sampling period. The feedrate and spindle speed commands for the period  $i$  are obtained as follows:

$$f_{com}(t) = f_{com}(t-1) + K_{f(t)}f_{0t}(t) \quad (14)$$

$$v_{com}(t) = v_{com}(t-1) + K_{v(t)}v_0(t) \quad (15)$$

where  $f_{com}(t-1)$  and  $v_{com}(t-1)$  are the control commands of the previous sampling period,  $K_f$  and  $K_v$  are the scaling factors for feedrate and spindle speed deviations respectively.

### Scaling Factor Tuning

10 There are several adaptation techniques for fuzzy controllers, such as:

- (a) membership function tuning,
- (b) input, output scaling factors tuning, and
- (c) linguistic rule tuning.

The second technique, also referred to as gain coefficient tuning, was adopted as it  
 15 appears to be more effective and simpler for implementation of a control policy. The other two techniques usually require additional algorithms such as neural networks and genetic algorithms, as well as an off-line learning procedure. For information about this second technique, the reader is directed to the article "Adaptive Fuzzy Logic  
 20 and Engineering Application of Artificial Intelligence, 1991, pp. 62-70, which is incorporated herein by reference.

Tuning the scaling factors of the output parameters, feedrate and spindle speed deviations, provides better response to the changes in the cutting process. In other words, this technique leads to the development of an adaptive fuzzy controller whose  
 25 control actions change with respect to the machining processes and the environments in which it operates.

The tuning procedure involves the adjustment of the scaling factors 62, 72, 74 and 76 (Figure 3) for the feedrate and spindle speed in order to avoid, or minimize, overshoots when sudden changes in a cutting process occur. Also, it prevents the power  
 30 from continuous decline below the reference level  $P_{ref}$ . This is achieved by examining the trend of the power error  $EP(t)$  and the change of power  $CP(t)$ . Based on the trend of power error  $EP(t)$  and the change of power  $CP(t)$ , the tuning mechanism 86 (Figure

3) adjusts the scaling factors  $K_{ft}$  and  $K_{vt}$  in Equations (14) and (15) according to the expressions:

$$K_{ft} = \lambda_t K_{ft-1} \quad (16)$$

$$K_{vt} = \lambda_t K_{vt-1} \quad (17)$$

5 To determine  $\lambda_t$ , two consecutive power errors are defined by

$$\begin{aligned} EP(t) &= P_{ref} - P(t-1) \\ EP(t-1) &= P_{ref} - P(t-2) \end{aligned} \quad (18)$$

and the two consecutive changes of power by:

$$\begin{aligned} CP(t) &= P(t) - P(t-1) \\ CP(t-1) &= P(t-1) - P(t-2) \end{aligned} \quad (19)$$

$\lambda_i$  can be tuned as follows

$$\text{if } \left| \frac{CP(t)}{CP(t-1)} \right| > 1$$

$$\text{if sign } CP(t) \neq \text{sign } CP(t-1) \quad \text{set } \lambda_t = 1$$

$$\text{else if } |EP(t)| \leq |EP(t-1)| \quad \text{set } \lambda_t = \left| \frac{CP(t-1)}{CP(t)} \right|^a$$

$$15 \quad \text{else if } |EP(t)| > |EP(t-1)| \quad \text{set } \lambda_t = \left| \frac{CP(t)}{CP(t-1)} \right|^a$$

$$\text{else set } \lambda_t = 1$$

where  $0 \leq a \leq 1$ .

The main idea of this algorithm is to allow adjustments to be based upon the latest trend of power error  $EP(t)$  and power change  $CP(t)$ . If the current situation is worse than before, or, in other words, the trend is away from the reference level  $P_{ref}$ , more adjustment should be made, i.e.,  $\lambda_i$  should be greater than 1. If the current situation is the same as before, or no clear trend can be observed, it is desirable to keep  $K_f$  or  $K_v$

unchanged, i.e.,  $\lambda_t = 1$ . For example, the condition specified by  $\left| \frac{CP(t)}{CP(t-1)} \right| > 1$ ,

$\text{sign}(CP(t)) = \text{sign}(CP(t-1))$ , and  $|EP(t)| \leq |EP(t-1)|$  simply means that the situation between sampling points (t) and (t-1) is better than that between sampling points (t-1) and (t-2), and the actual or current power level  $P$  is approaching the reference level  $P_{ref}$  at

a faster pace. Apparently a smaller  $\lambda_t$  is preferred to avoid over-adjustment. The

opposite is true, i.e. if a situation occurs such that  $\left| \frac{CP(t)}{CP(t-1)} \right| > 1$ ,

$\text{sign}(CP_t) \cong \text{sign}(CP_{t-1})$  and  $|EP(t)| > |EP(t-1)|$ .

The selection of  $\alpha$  in the above algorithm is often situation-dependent. From  
5 experiments, it appears  $\alpha=0.15$  fits the tuning process very well. The initial values of  $K_f$  and  $K_v$  were found, by trial and error, to be 0.86 and 120 respectively.

In the meantime, the input scaling factors  $K_e$  and  $K_c$ , for power error and power  
error change, were adjusted offline for different types of machines. This was  
accomplished by selecting appropriate scaling factors to normalize the inputs. In this  
10 case, the minimum actual power when the machine was idle at the lower spindle speed  
limit, which was set to 200 rpm, was recorded to be 0.50 HP. The power reference was  
set to 0.90 HP, and the maximum actual power was selected as 1.30 HP. Accordingly,  
the absolute value of the difference between the power reference  $P_{ref}$  and each power  
limit, minimum and maximum, was 0.4. Therefore, the scaling factor,  $K_e$ , for mapping  
15  $EP(t)$  values into the interval of -1 and 1 of the universe of discourse was calculated as  
2.5. Similarly for  $CP(t)$ , when minimum actual power was 0.50 HP and maximum  
actual power was 1.30 HP, the absolute value of the difference was 0.8, hence  $K_c =$   
1.30.

## 20 Experimental Implementation

The performance of the control system described above was examined by implementing  
the adaptive fuzzy controller of Figures 3 and 4 with a Servo 2000 vertical CNC milling  
machine built by Servo Products Co. and using the machine to perform experiments on  
various workpieces with different cutter immersion rates. The microcontroller 44 was  
25 implemented using a Pentium personal computer equipped with an A/D converter and  
a D/A converter. A low-pass filter was also used, as an anti-aliasing filter, before the  
A/D converter.

The spindle shaft was driven by a three-phase G3, 31-IP AC motor. The machine had  
a gear box which provided 2 speed systems, high and low. In the high gear the motor  
30 output power was transmitted to the spindle shaft directly from the spindle shaft hub,  
providing a range of spindle speed from 450 to 5,100 RPM. In the low gear, the power

from the spindle shaft hub was transmitted to the spindle shaft through a set of pulleys and gears. The spindle speed for the low gear ranged from 45 to 510 RPM.

The machine had three sliding axes, with the X (table) and Y (cross) axes being driven by axis drive motors and lead screws, and Z axis being operated manually. The axis  
5 drive motors were 3-phase Variable Reluctance stepping motors with resolution of 84 primary steps per revolution.

#### **Power Sensor and Signal Processing**

A PH-3A power sensor marketed by Loads Controls was used to measure the spindle power signals through three cables from the spindle motor passing through the  
10 cells. The power sensor had a full-scale power capacity of 10HP and a voltage output in the range of 0 to 10 volts, leading to sensitivity of 1 Volt/HP. The output signals from the power sensor were filtered by a 4-th order Butterworth low-pass filter with cut-off frequency of 100Hz to remove aliasing.

#### **15 A/D, D/A Converter**

The filtered signals from the power sensor were digitized by a 12 bit A/D converter, which was a part of an analog to digital and digital to analog converter PC card. The digital signals were the crisp inputs for the fuzzy logic controller. The outputs of the controller, spindle speed and feedrate, were routed through the D/A section of the  
20 converter and then to the feedrate drive controller and spindle speed controller box. The command feedrate, in the form of an overriding percentage of the full scale feedrate and the command spindle speed in actual rpm were converted to analog voltage signals of 0 to 5V and 0 to 10V respectively by the 12 bit D/A converter.

The following fuzzy logic rules were stored in the fuzzy rule base 96:-

25 The value ranges corresponding to power error (EP):

NB = [-1.3333, -1.0000, -0.5000]

NM = [-1.0000, -0.5000, -0.3000]

NS = [-0.5000, -0.3000, -0.0600]

ZE = [-0.3000, 0.0000, 0.3000]

30 PS = [0.0600, 0.3000, 0.5000]

PM = [0.3000, 0.5000, 1.0000]

PB = [0.5000, 1.0000, 1.3333]

The value ranges corresponding to power change (CP):

NB = [-1.3333, -1.0000, -0.6000]

NM = [-1.0000, -0.6000, -0.3600]

5 NS = [-0.6000, -0.3600, -0.0600]

ZE = [-0.3600, 0.0000, 0.3600]

PS = [0.0600, 0.3600, 0.6000]

PM = [0.3600, 0.6000, 1.0000]

PB = [0.6000, 1.0000, 1.3333]

10

The value ranges corresponding to feed rate:

NB = [-1.3333, -1.0000, -0.6300]

NM = [-1.0000, -0.6300, -0.3000]

15 NS = [-0.6300, -0.3000, 0.0000]

ZE = [-0.3000, 0.0000, 0.3000]

PS = [0.0000, 0.3000, 0.6300]

PM = [0.3000, 0.6300, 1.0000]

PB = [0.6300, 1.0000, 1.3333]

20

The value ranges corresponding to spindle speed:

NB = [-1.3333, -1.0000, -0.6300]

NM = [-1.0000, -0.6300, -0.3000]

25 NS = [-0.6300, -0.3000, 0.0000]

ZE = [-0.3000, 0.0000, 0.3000]

PS = [0.0000, 0.3000, 0.6300]

PM = [0.3000, 0.6300, 1.0000]

PB = [0.6300, 1.0000, 1.3333]

30

5. The reference power was 0.90 horsepower and the maximum and minimum power limits are respectively 1.30 and 0.50 horsepower. The 1.30 hp corresponds to -

1.3333 and 0.50 hp corresponds to +1.3333. The -1 and 1 of the universe of discourse are mapped as 1.20 and 0.60 hp respectively.

Accordingly, other values in the universe of discourse were calculated using the following equation

$$\begin{aligned}
 5 \quad X &= \frac{\text{upper limit of universe of discourse}}{P_{\max} - P_{\text{ref}}} (P_{\text{ref}} - P(t)) \\
 &= \frac{1.333}{1.30 - 0.90} (P_{\text{ref}} - P(t)) = 3.33325 (P_{\text{ref}} - P(t))
 \end{aligned}$$

where  $X$  = the value in the universe of discourse,  $P$  = actual spindle power (measured),  $P_{\max}$  = maximum allowable spindle power (1.30 hp in our test),  $P_{\text{ref}}$  = reference spindle power.

10 Programmed with these functions and rules, the machine described above was used with a High Speed Steel (HSS) 14.3 mm end milling cutter with four helical flutes and 30° helix angles to perform slot milling (i.e., full immersion) and 3/4 immersion milling on 1018 cold rolled steel workpieces. A sampling frequency of 200 samples per second was used in the cutting tests. The maximum and minimum feedrate commands  
 15 were set to 120 mm/min and 25 mm/min respectively. The upper spindle speed was set to 350 RPM and the lower limit was determined based on workpiece material and cutter specifications. The following relation was used to specify the lower limit of the spindle speed to avoid tool breakage:

$$\frac{f}{zV} \leq f_{t(\text{Max})}$$

20 where  $z$  is the number of cutter teeth, and  $f_{t(\text{Max})}$  is the maximum feed per tooth which is tool-workpiece dependent. This condition states that the feed/speed relation is restricted by the maximum allowable feed per tooth. According to a metal cutting handbook for 1018 cold rolled material and a high speed steel cutter, the value of  $f_{t(\text{Max})}$  was set to 0.08 mm/tooth.

25 The experiments showed that adjusting both spindle speed and feed rate resulted in a reduction of as much as 20-30 per cent in the cutting time, a compared with the cutting time when only feed rate was adjusted. It was also shown that the spindle power was well regulated around the reference level. Though no significant overshoots were

observed in either case, dual-parameter adjustment showed a better transient performance when step changes in thickness were encountered.

It should be appreciated that, although the preferred embodiments of the various aspects of the invention detect one variable, i.e. power level at the drive means and use  
5 a control system which controls at least two variables of the drive means, the invention comprehends detecting power level and controlling only one variable; or detecting a single variable other than power level and controlling more variables than the or those detected. More specifically, the invention comprehends the use of a dynamometer to produce the signal representing force between the cutting tool and the workpiece, and  
10 using a fuzzy logic control system to control two or more variables of the drive means in dependence thereupon.

It should be appreciated that, although the foregoing description is of a complete machine, it would be possible to modify an existing machine to implement the invention. Thus, the invention also encompasses an assemblage or kit of items for converting an  
15 existing computer-numerically controlled machine, the assemblage or kit comprising a power sensor and software for reprogramming the microcontroller, or even an additional microcontroller, so as to implement the required functions. The invention also encompasses the software *per se*, conveniently carried by a storage medium, for use where the existing machine already has the required sensor, or the owner prefers to add  
20 one.

Although the above-described embodiment is a milling machine, the invention encompasses various other configurations. For example, a drill would have a rotatable cutting tool which was also linearly-movable relative to the carrier/workpiece. The carrier/workpiece could be rotatable and the cutting tool holder moved linearly, as in a  
25 lathe; or both the carrier/workpiece and the cutting tool holder could be moved linearly, as in a shaping machine.

It is preferred to derive the signal representing energy consumption rate by measuring drive unit power level rather than supply current because power is linearly related to drive motor load, whereas supply current is related non-linearly.  
30 Nevertheless, it would be possible to measure supply current and derive energy consumption rate therefrom.

INDUSTRIAL APPLICABILITY

Computer numerically-controlled machine control systems embodying the present invention are robust, relatively inexpensive and do not require modifications to the machine structure, such as the machine table, or extensive mathematical modelling. The power sensor is not exposed to the harsh environment adjacent the cutting tool. Control  
5 of both spindle speed and feed rate reduces vibration and improves tool life. Embodiments are relatively insensitive to changes in the machine, cutting tool, workpiece and cutting tool immersion rate, and can be applied to material removal machines or cutting machines generally. Embodiments allowing multi-parameter adjustment, specifically adjustment of both spindle speed and feed rate, have been shown to increase  
10 material removal rates by as much as 25 per cent compared with machines employing single parameter, i.e. feed rate only, adjustment.

## CLAIMS:

1. A material removal machine comprising:
  - (i) a carrier for carrying a workpiece fixed relative thereto;
  - (ii) a holder for a cutting tool;
  - 5 (iii) drive means for effecting relative movement between the carrier and the holder to effect material removal;
  - (iv) a sensor for monitoring energy consumption rate of an element of the drive means;
  - (v) a control unit responsive to the sensor for controlling the drive means to  
10 vary said relative movement so as to tend to maintain energy consumption rate substantially at a predetermined level.
2. A machine according to claim 1, wherein the drive means comprises first drive means for moving the carrier and second drive means for moving the cutting tool and  
15 the control unit controls both the first drive means and the second drive means.
3. A machine according to claim 2, wherein the first drive means comprises one or more motors for moving the carrier linearly relative to the cutting tool holder and the second drive means comprises a motor for rotating the cutting tool holder.  
20
4. A machine according to claim 1, 2 or 3, wherein the control unit uses two variables in controlling a speed of the cutting tool holder and/or a feed rate of the carrier.
- 25 5. A machine according to claim 1, 2 or 3, wherein the control unit determines a difference ( $P - P^{\text{ref}}$ ) between a current actual energy consumption rate and the reference energy consumption rate and the difference ( $P - P(t-1)$ ) between the current actual energy consumption rate and a recent actual energy consumption rate, compares the variables ( $P - P^{\text{ref}}$ ) and ( $P - P(t-1)$ ) with a table of predetermined values to extract therefrom a  
30 corresponding speed or feed rate to adjust the actual energy consumption rate to correspond substantially with the desired energy consumption rate.

6. A machine according to claim 5, wherein, in the table, one of the ordinates comprises a range of values of one of the variables ( $P_{ref} - P(t)$ ) and the other ordinate comprises a range of values of the other of the variables ( $P(t-1)$ ), and the control unit uses the instant values of the two variables to select the corresponding recommended  
5 value for cutting tool speed and/or feed rate.

7. A material removal machine according to claim 5, wherein the control unit has two tables, one containing possible recommendations for feed rate and the other containing possible recommendations for cutting tool speed, each table having one  
10 ordinate comprising a range of values of one of the variables ( $P_{ref} - P(t)$ ) and the other ordinate comprises a range of values of the other of the variables ( $P(t-1)$ ), and the control unit uses the same instant values of the two variables to extract recommended values ( $\Delta f$  and  $\Delta v$ ) for feed rate and cutting tool speed from respective ones of the tables for controlling the carrier movement and cutting tool holder movement, respectively.

15

8. A material machine according to claim 7, wherein the control unit employs fuzzy logic to determine the recommended adjustments.

9. A machine according to claim 6, 7 or 8, wherein the table contains values derived  
20 empirically using a selection from the group comprising predetermined data for the workpiece material, type of machine, experience and experiment.

10. A control system for a material removal machine comprising a carrier for carrying a workpiece fixed relative thereto, a holder for a cutting tool, and drive means  
25 for effecting relative movement between the carrier and the holder to effect material removal, the system comprising:

(i) a sensor for monitoring energy consumption rates of an element of the drive means; and

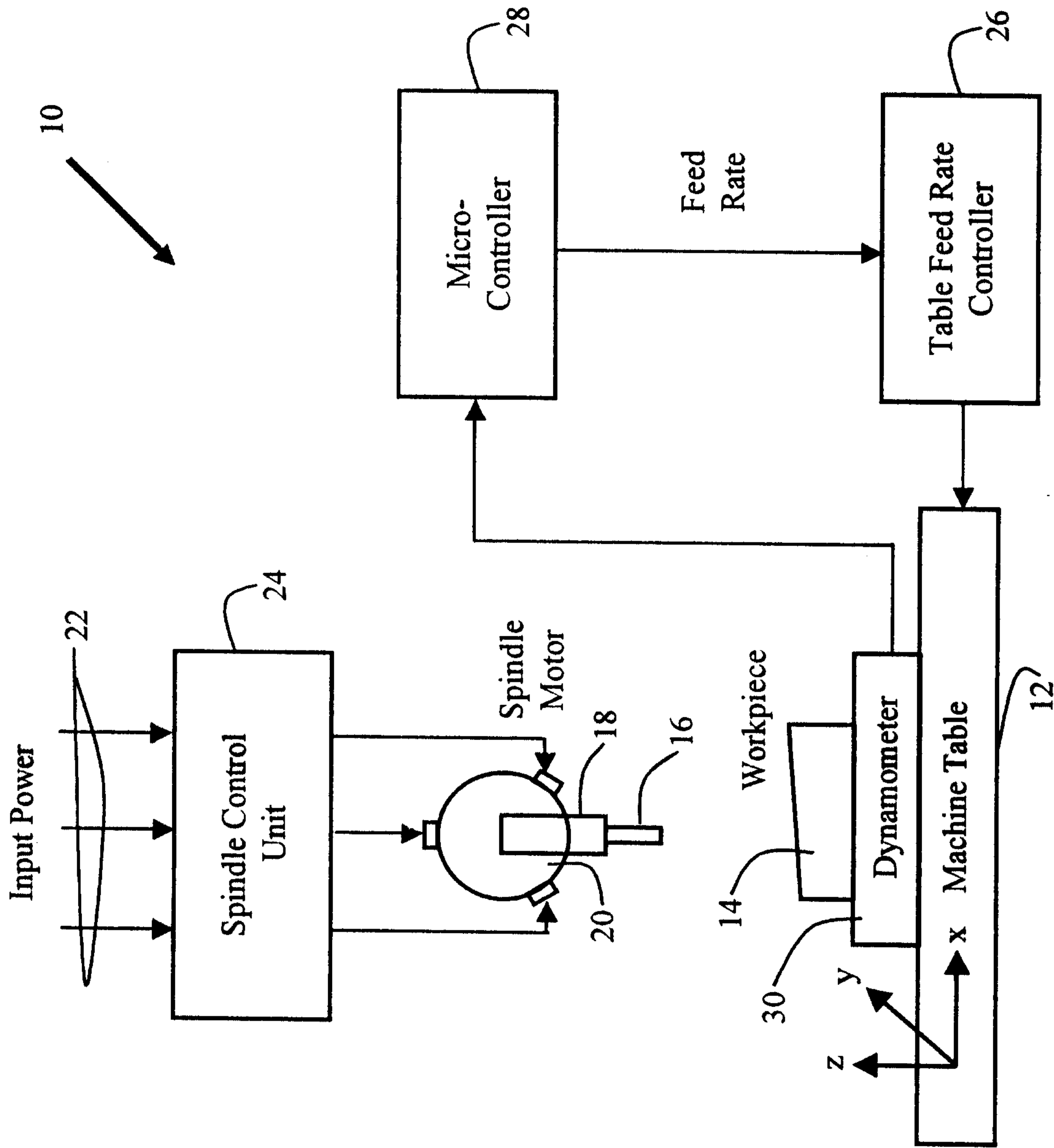
(ii) a control unit responsive to the sensor for controlling the drive means to vary said  
30 relative movement so as to maintain energy consumption rate substantially at a predetermined level.

11. A control system according to claim 10, wherein the control unit uses two variables in controlling a speed of the cutting tool holder and/or a feed rate of the carrier.
- 5 12. A control system ( $P_{ref} - P(t)$ ) according to claim 10 or 11, wherein the control unit determines a difference ( $P - P^{ref}$ ) between a current actual energy consumption rate and the reference energy consumption rate and the difference ( $P(t) - P(t-1)$ ) between the current actual energy consumption rate and a recent actual energy consumption rate, compares the variables ( $P_{ref} - P(t)$ ) and ( $P(t) - P(t-1)$ ) with a table of predetermined  
10 values to extract therefrom a corresponding speed or feed rate to adjust the actual energy consumption rate to correspond substantially with the desired energy consumption rate.
13. A control system according to claim 5, wherein, in the table, one of the ordinates comprises a range of values of one of the variables ( $P_{ref} - P(t)$ ) and the other ordinate  
15 comprises a range of values of the other of the variables ( $P(t-1)$ ), and the control unit uses the instant values of the two variables to select the corresponding recommended value for cutting tool speed and/or feed rate.
14. A control system according to claim 5, wherein the control unit has two tables,  
20 one containing possible recommendations for feed rate and the other containing possible recommendations for cutting tool speed, each table having one ordinate comprising a range of values of one of the variables ( $P_{ref} - P(t)$ ) and the other ordinate comprises a range of values of the other of the variables ( $P(t-1)$ ), and the control unit uses the same instant values of the two variables to extract recommended values ( $\Delta f$  and  $\Delta v$ ) for feed  
25 rate and cutting tool speed from respective ones of the tables for controlling the carrier movement and cutting tool holder movement, respectively.
15. A control system according to claim 14, wherein the control unit employs fuzzy logic to determine the recommended adjustments.
- 30
16. A control system according to claim 12, 13 or 14, wherein the table contains values derived empirically using a selection from the group comprising predetermined data for the workpiece material, type of machine, experience and experiment.

17. A material removal machine comprising:
- (i) a carrier for carrying a workpiece fixed relative thereto;
  - (ii) a holder for a cutting tool;
  - (iii) drive means for effecting relative movement between the carrier and the  
5 holder to effect material removal;
  - (iv) a sensor operable to provide a signal representing energy consumption rate  
of the drive means or force exerted between a cutting tool carried by the holder and a  
workpiece carried by the carrier;
  - (v) control means for comparing said signal with a reference and controlling  
10 two different parameters of the drive means to maintain said energy consumption rate or  
the force substantially equal to a desired value.
18. A control system for a material removal machine comprising a carrier for  
carrying a workpiece fixed relative thereto, a holder for a cutting tool, and drive means  
15 for effecting relative movement between the carrier and the holder to effect material  
removal, the control system comprising:
- (i) a sensor operable to provide a signal representing energy consumption rate  
of the drive means or force exerted between a cutting tool carried by the holder and a  
workpiece carried by the carrier;
  - (ii) control means for comparing said signal with a reference and controlling  
20 two different parameters of the drive means to maintain the said energy consumption rate  
or force substantially equal to a desired value.
19. An assemblage of parts for converting a material removal machine comprising a  
25 carrier for carrying a workpiece fixed relative thereto, a holder for a cutting tool, drive  
means for effecting relative movement between the carrier and the holder to effect  
material removal, and a microcontroller for controlling the relative movement in  
response to a control signal, the assemblage comprising:
- (i) a sensor for connection to the drive means for providing a signal representing  
30 energy consumption rate or force exerted between a cutting tool carried by the holder  
and a workpiece carried by the carrier, and

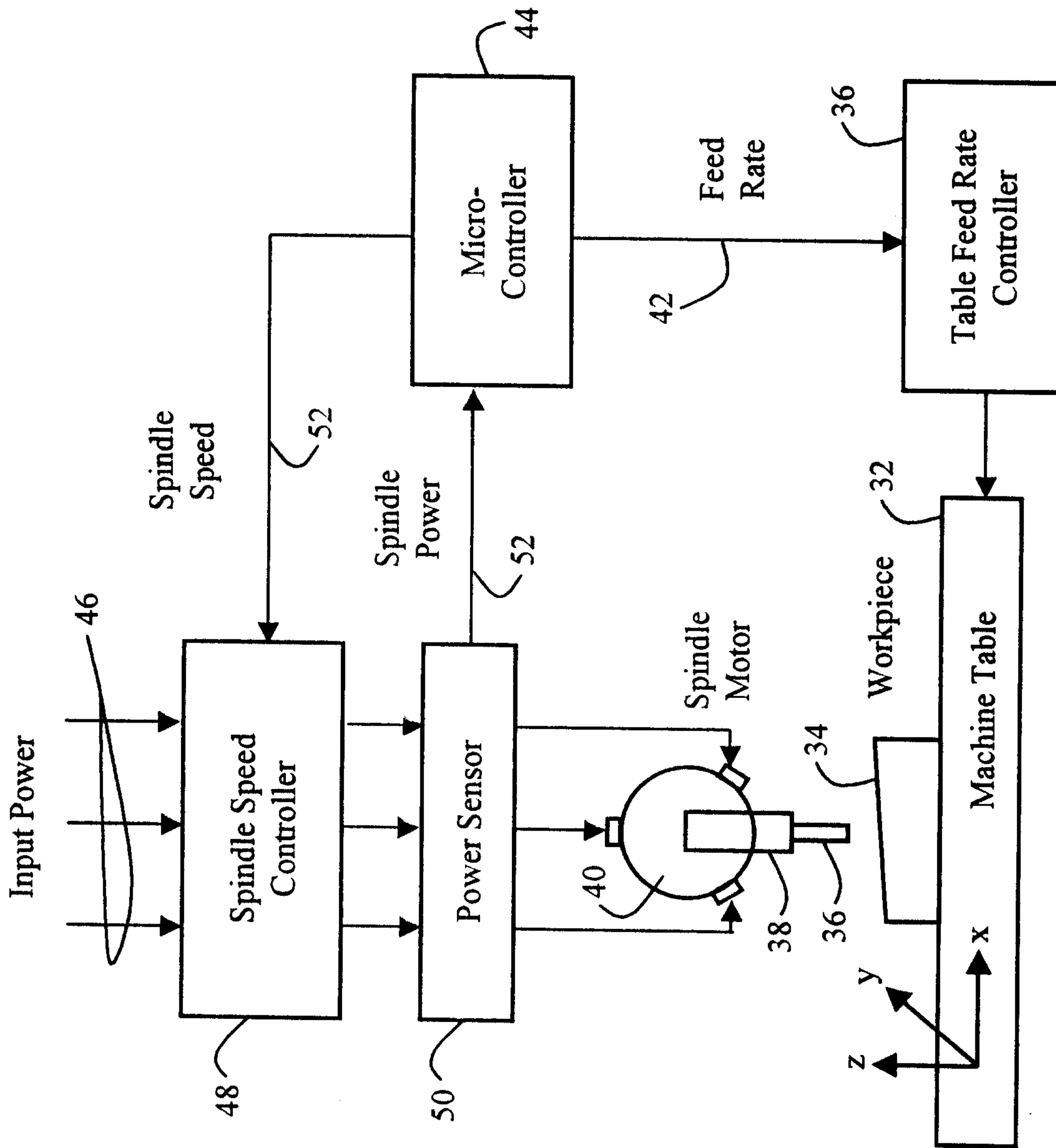
(ii) software for programming the microcontroller to compare the signal with a reference level and, in dependence thereupon, control the drive means to reduce said difference.

5 20. A storage medium carrying a computer program for use with a material removal machine comprising a carrier for carrying a workpiece fixed relative thereto, a holder for a cutting tool, drive means for effecting relative movement between the carrier and the holder to effect material removal, and a microcontroller for controlling the relative movement in response to a control signal, the program controlling the microcontroller  
10 to compare the signal with a reference level and, in dependence thereupon, cause the microcontroller to control the drive means to reduce said difference.



**Fig. 1 Prior Art**

*Thomas Adams & Assoc.*  
**AGENT FOR APPLICANT**



**Fig. 2**

*Thomas Adams & Assoc.*  
**AGENT FOR APPLICANT**

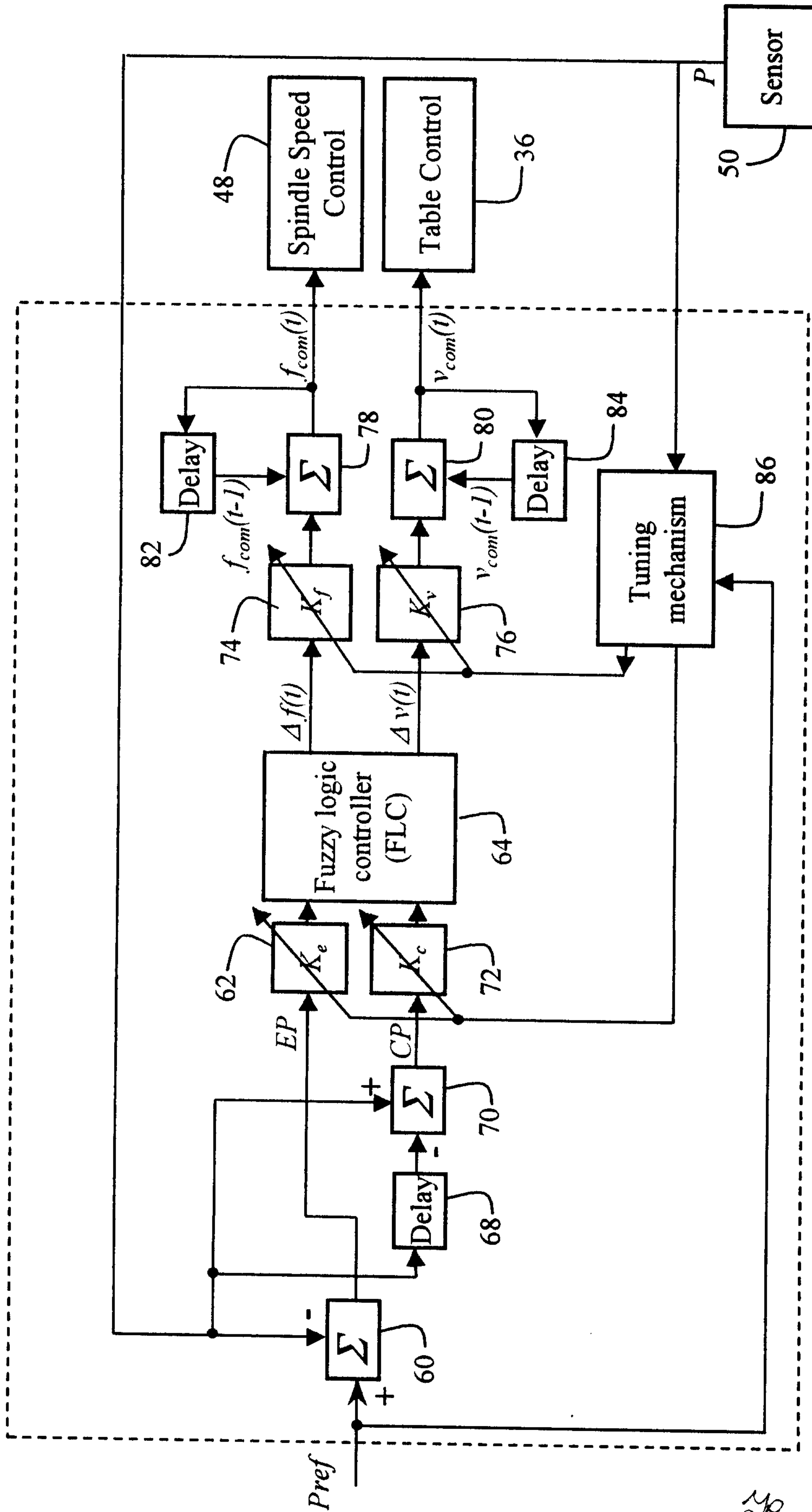
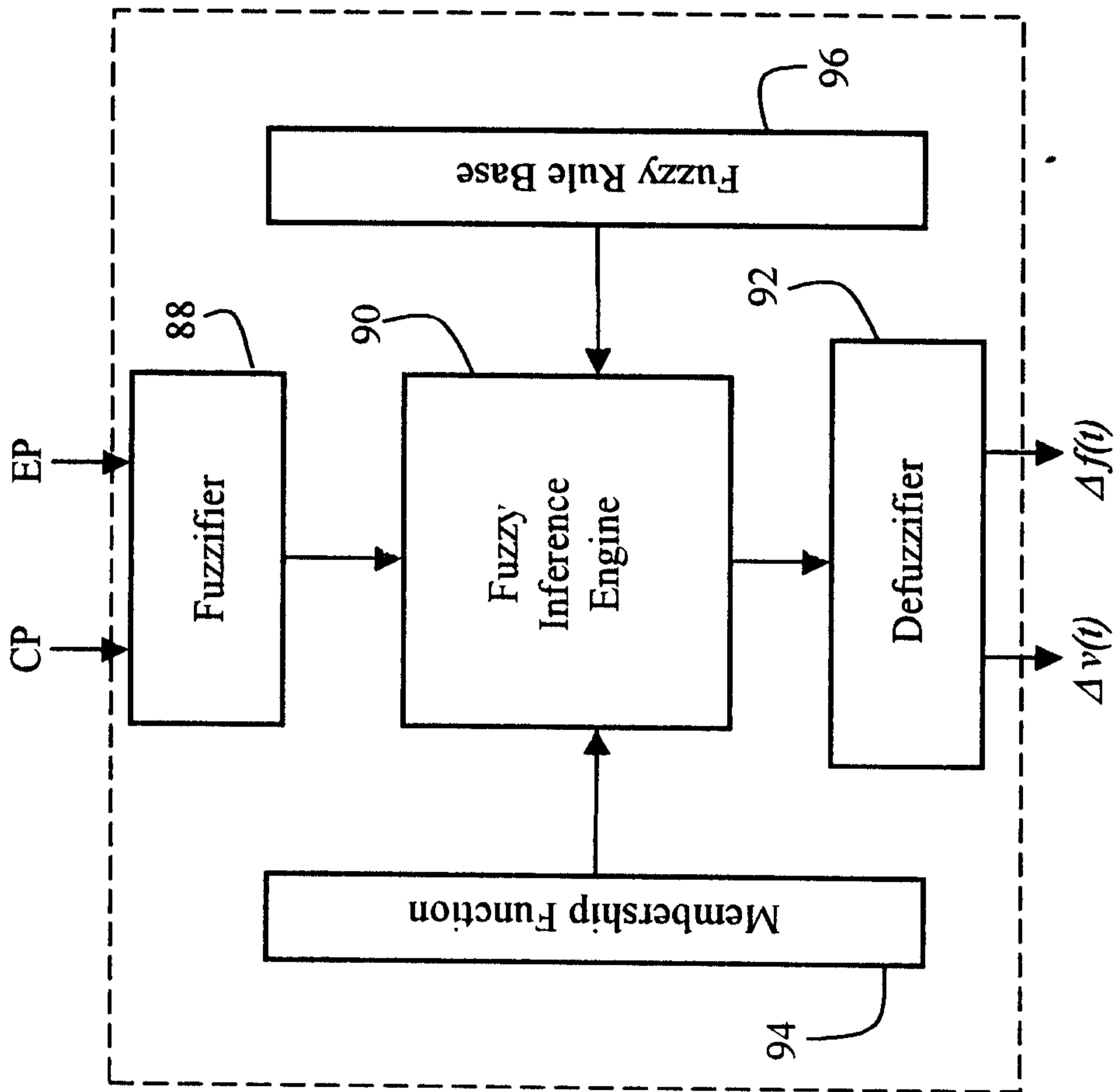


Fig. 3

Thomas Adams & Warr  
AGENT FOR APPLICANT



**Fig. 4**

*Thomas Adams & Assoc*  
**AGENT FOR APPLICANT**

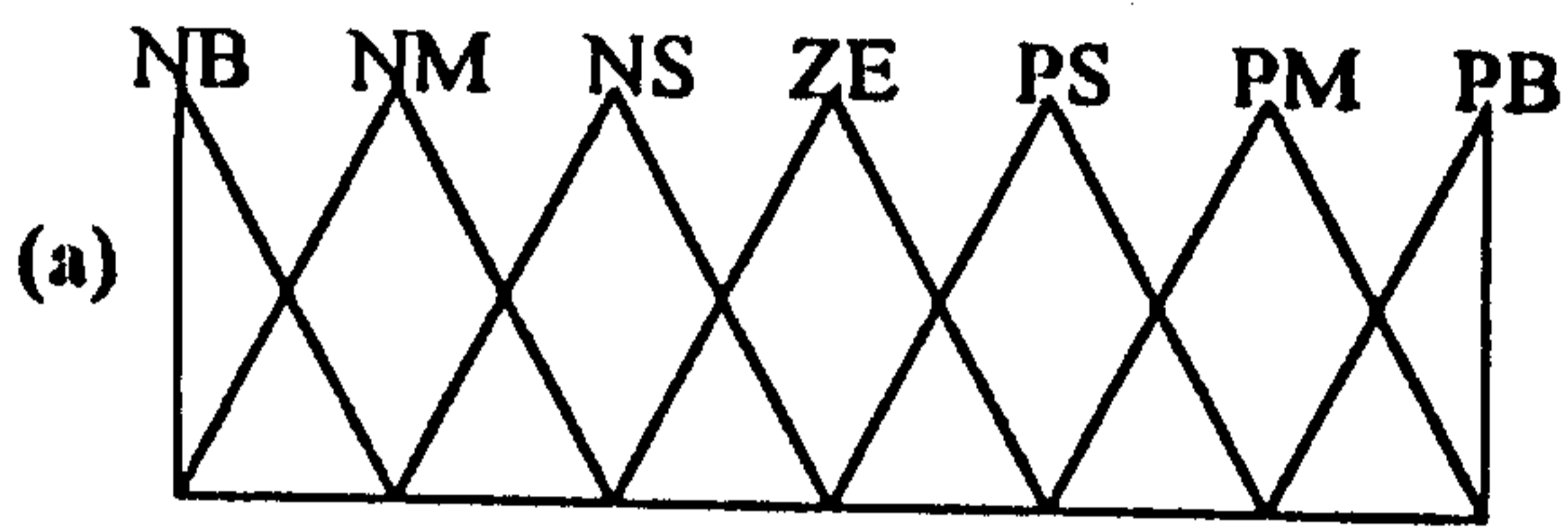


FIG. 5(a)

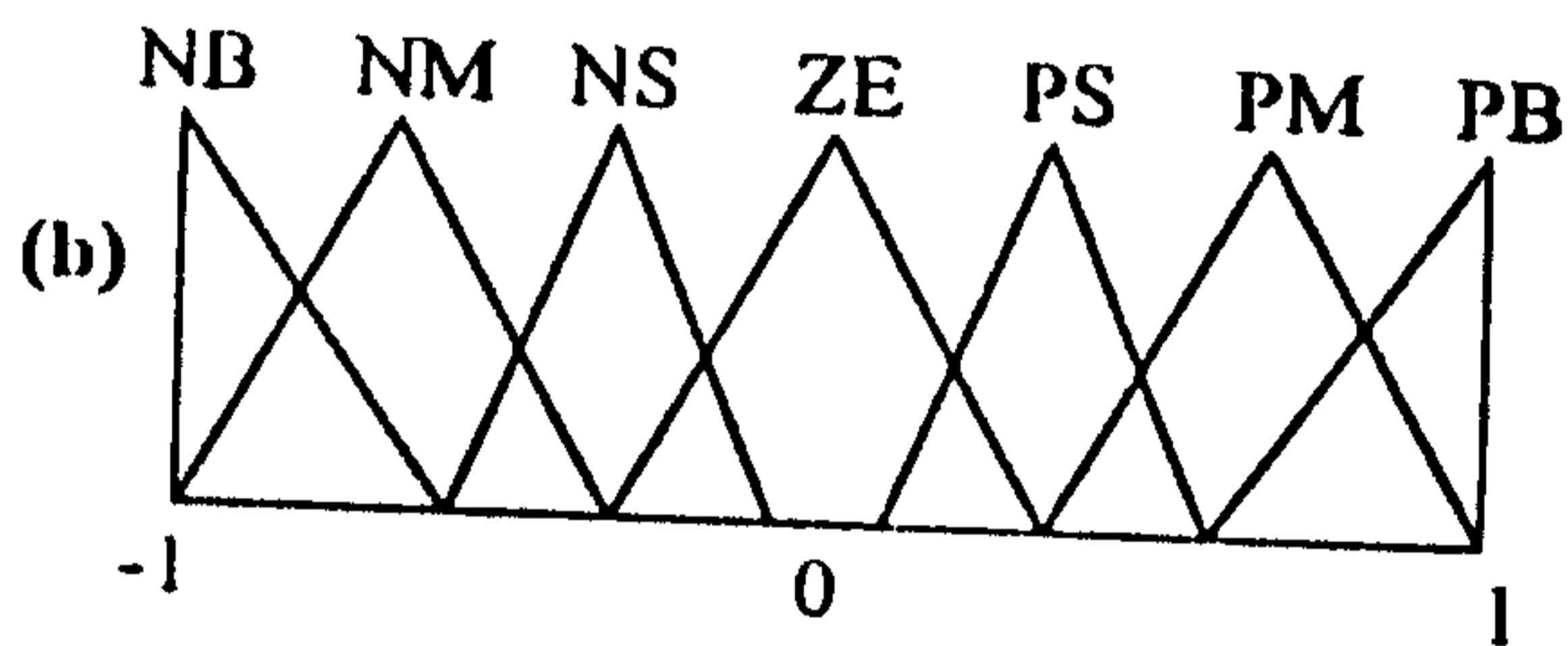


FIG. 5(b)

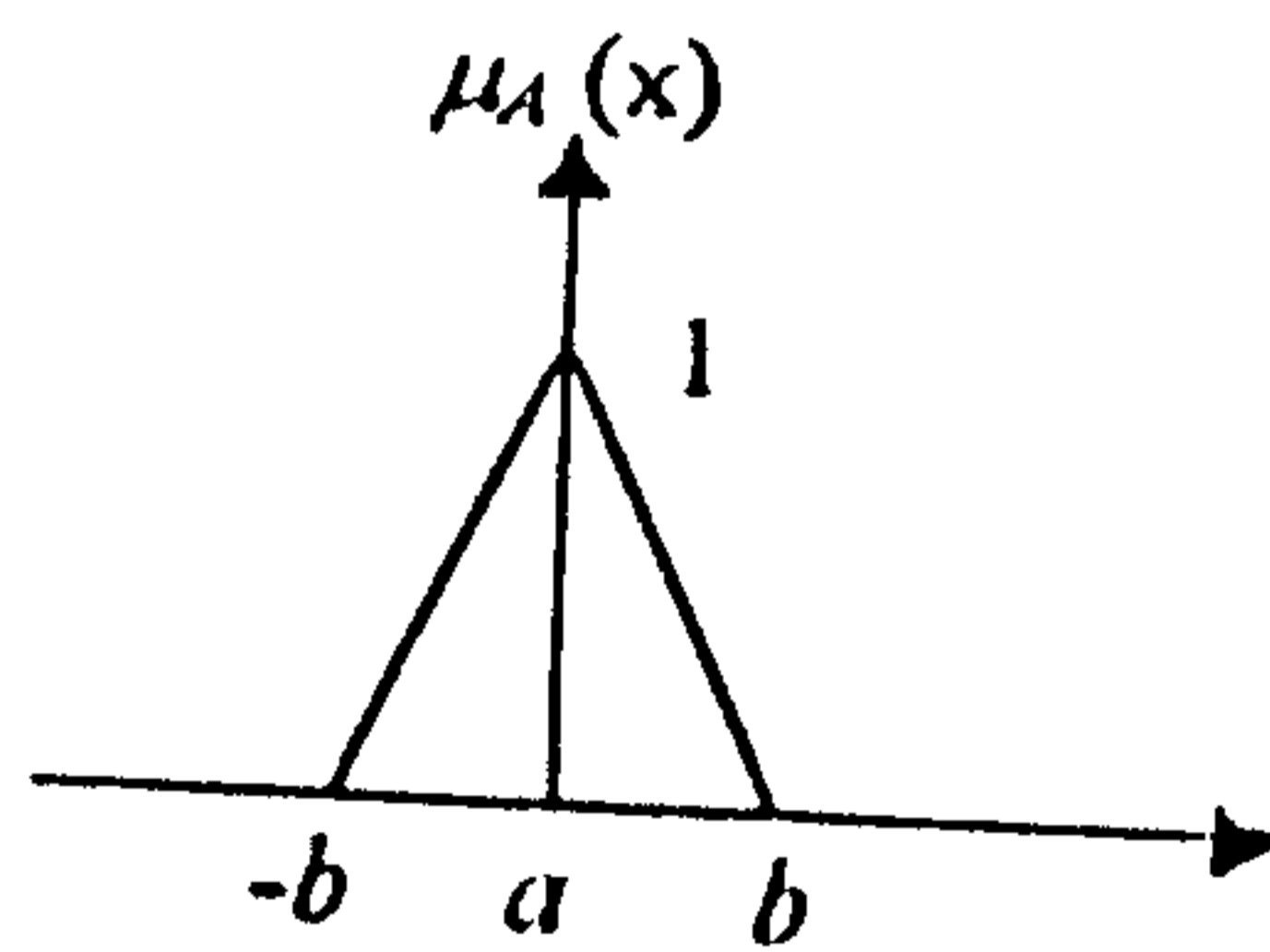


FIG. 6

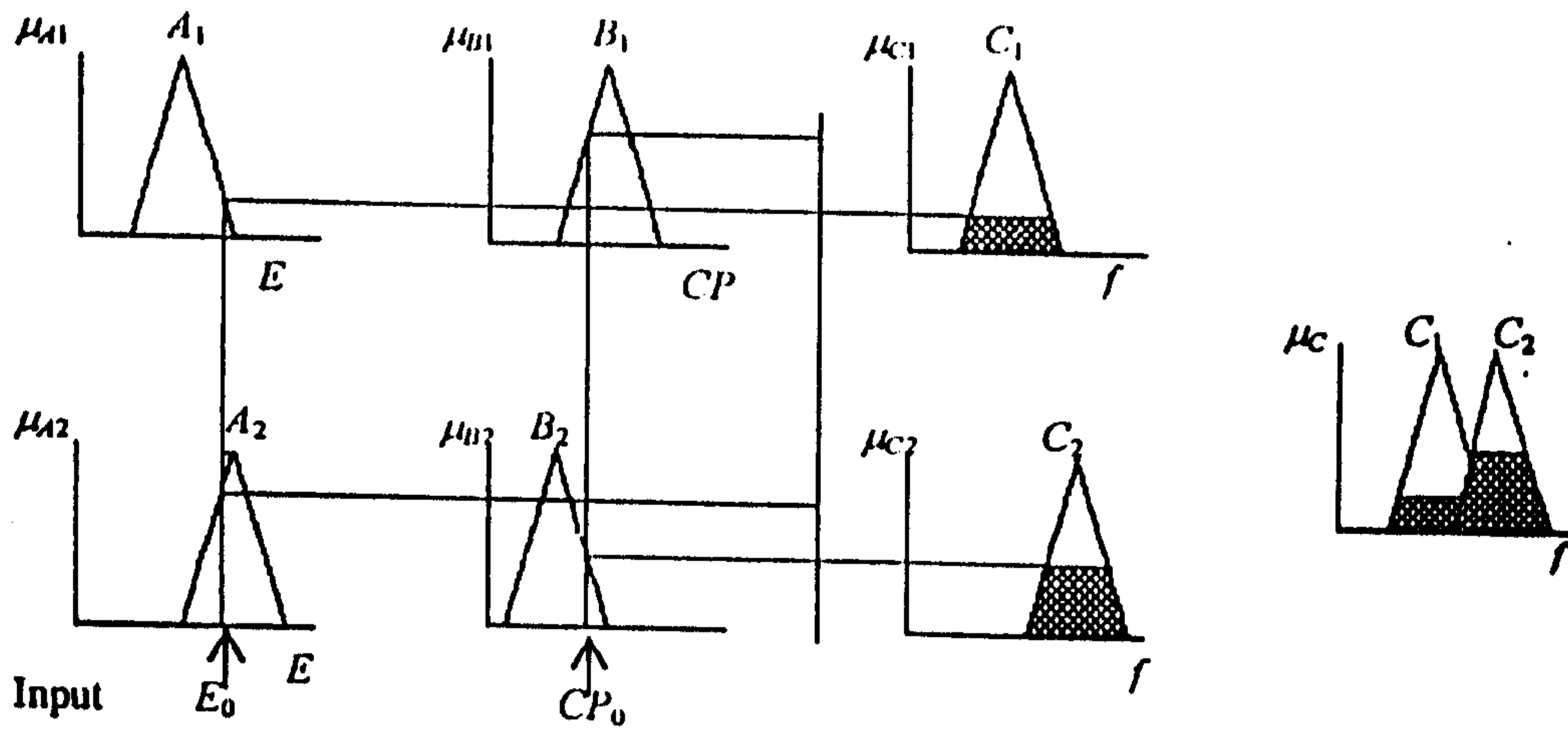


FIG. 7

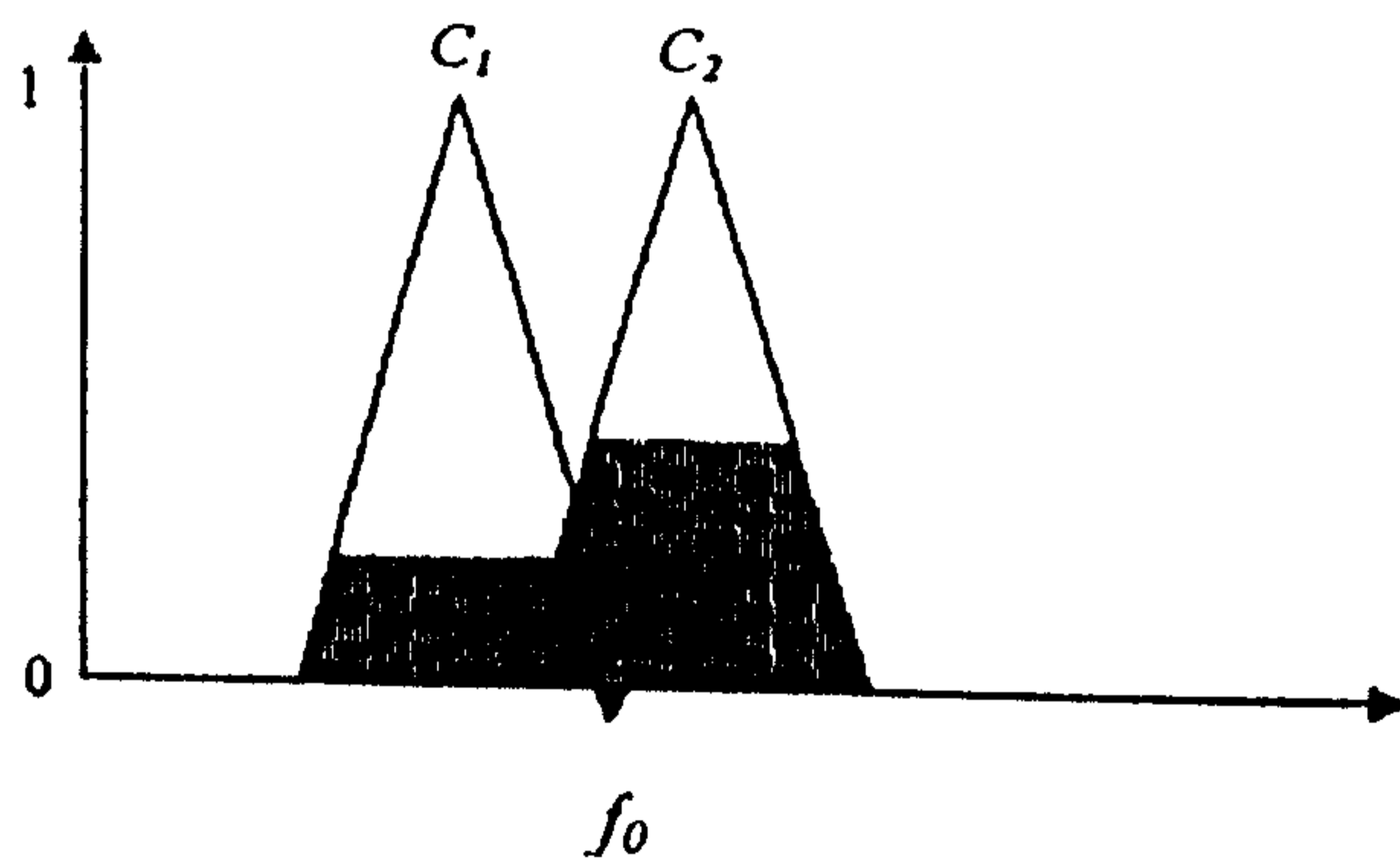


FIG. 8

