Title: PROCESSOR WITH APPROXIMATE COMPUTING FUNCTIONAL UNIT

Abstract: A processor includes an indicator configured to indicate a first mode or a second mode and a functional unit configured to perform computations with a full degree of accuracy when the indicator indicates the first mode and to perform computations with less than the full degree of accuracy when the indicator indicates the second mode.
PROCESSOR WITH APPROXIMATE COMPUTING FUNCTIONAL UNIT

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CROSS REFERENCE TO RELATED APPLICATION(S)

[0001] This application claims priority to U.S. Non-Provisional Application No. 14/522,530, filed 10/23/2014, which claims priority based on U.S. Provisional Application, Serial No. 61/937,741, filed 02/10/2014, entitled PROCESSOR THAT PERFORMS APPROXIMATE COMPUTING INSTRUCTIONS; PROCESSOR THAT RECOVERS FROM EXCESSIVE APPROXIMATE COMPUTING ERROR; PROCESSOR WITH APPROXIMATE COMPUTING FUNCTIONAL UNIT, which is hereby incorporated by reference in its entirety.

BACKGROUND

[0002] There has been a considerable amount of theoretical work in the area of approximate computing. Approximate computing attempts to perform computations in a manner that reduces power consumption in exchange for potentially reduced accuracy. Although approximate computing has been a favorite topic of academia, little has been produced regarding how to use approximate computing in a commercially viable processor.

BRIEF SUMMARY

[0003] In one aspect the present invention provides a processor. The processor includes an indicator configured to indicate a first mode or a second mode and a functional unit
configured to perform computations with a full degree of accuracy when the indicator indicates the first mode and to perform computations with less than the full degree of accuracy when the indicator indicates the second mode.

[0004] In another aspect, the present invention provides a method to be performed by a processor having an indicator and a functional unit. The method includes setting the indicator to indicate a first mode or a second mode and performing, by the functional unit, computations with a full degree of accuracy when the indicator indicates the first mode and to perform computations with less than the full degree of accuracy when the indicator indicates the second mode.

[0005] In yet another aspect, the present invention provides a functional unit. The functional unit includes an input configured to indicate a first mode or a second mode and computation logic configured to perform computations with a full degree of accuracy when the indicator indicates the first mode and to perform computations with less than the full degree of accuracy when the indicator indicates the second mode.

BRIEF DESCRIPTION OF THE DRAWINGS

[0006] FIGURE 1 is a block diagram illustrating an embodiment of a processor.

[0007] FIGURE 2 is block diagrams illustrating three embodiments of the approximating functional units of Figure 1.

[0008] FIGURE 3 is a block diagram illustrating approximation instructions.

[0009] FIGURE 4 is a flowchart illustrating operation of the processor of Figure 1 according to one embodiment.

[0010] FIGURE 5 is a flowchart illustrating operation of the processor of Figure 1 within a computer system.

[0011] FIGURE 6 is a block diagram illustrating three different computing systems.

[0012] FIGURE 7 is a flowchart illustrating operation of the systems of Figure 6.

[0013] FIGURE 8 is a flowchart illustrating a process for the development of software to run on an approximate computing-aware processor.

[0014] FIGURE 9 is a flowchart illustrating an alternate process for the development of software to run on an approximate computing-aware processor.
[0015] FIGURE 10 is a flowchart illustrating operation of the processor of Figure 1 to run a program that performs approximate computations.

[0016] FIGURE 11 is a flowchart illustrating in greater detail operation of block 1014 of Figure 10 according to one embodiment.

[0017] FIGURE 12 is a flowchart illustrating in greater detail operation of block 1014 of Figure 10 according to an alternate embodiment.

DETAILED DESCRIPTION OF THE EMBODIMENTS

[0018] Embodiments are described in which a processor performs approximate computations. Approximate computations occur when a computation is performed with a degree of accuracy that is less than the full accuracy that may be specified by the instruction set architecture of the processor.

[0019] Referring now to Figure 1, a block diagram illustrating an embodiment of a processor 100 is shown. The processor 100 comprises a programmable data processor that performs stored instructions, such as a central processing unit (CPU) or a graphics processing unit (GPU). The processor 100 includes an instruction cache 102; an instruction translator 104 coupled to the instruction cache 102; one or more approximating functional units 106 coupled to receive microinstructions from the instruction translator 104; architectural registers 108 coupled to provide instruction operands 166 to the approximating functional units 106; an approximation control register 132 coupled to the approximating functional units 106; a data cache memory 138 coupled to the approximating functional units 106; and a snapshot storage 134 coupled to the approximating functional units 106. The processor 100 may also include other units, for example, a renaming unit, instruction scheduler and/or reservation stations may be employed between the instruction translator 104 and the approximating functional units 106 and a reorder buffer may be employed to accommodate out-of-order instruction execution.

[0020] The instruction cache 102 caches architectural instructions 174 fetched from memory and performed by the processor 100. The architectural instructions 174 may include approximate computing instructions, such as embodiments of approximate
computing instructions 399 described with respect to Figure 3. The approximate computing instructions 399 control the approximate computing policies of the processor 100, namely, whether the approximating functional units 106 perform computations with a full degree of accuracy or with less than a full degree of accuracy and the degree less than the full degree. The approximate computing instructions 399 also control the clearing of an error amount associated with each of the general purpose registers of the processor 100, as described herein. Preferably, the processor 100 includes other functional units that are not approximating. In one embodiment, the architectural instructions 174 substantially conform to the x86 instruction set architecture (ISA) modified to include embodiments of the approximate computing instructions 399 described herein. Other embodiments are contemplated in which the ISA of the processor 100 is other than the x86 ISA.

[0021] The instruction translator 104 receives the architectural instructions 174 from the instruction cache 102. The instruction translator 104 includes an instruction decoder that decodes the architectural instructions 174 and translates them into microinstructions. The microinstructions are defined by a different instruction set than the architectural instruction set, namely the microarchitectural instruction set. The microinstructions implement the architectural instructions 174.

[0022] Preferably, the instruction translator 104 also includes microcode 136 that comprises microcode instructions, preferably stored in a read-only memory of the processor 100. In one embodiment, the microcode instructions are microinstructions. In an alternate embodiment, the microcode instructions are translated into microinstructions by a micro-translator. The microcode 136 implements a subset of the architectural instructions 174 of the processor 100 ISA that are not directly translated into microinstructions by a programmable logic array of the instruction translator 104. Additionally, the microcode 136 handles microarchitectural exceptions, such as are generated when the cumulative error bound generated by approximate computations exceeds an error bound, according to one embodiment.

[0023] The architectural registers 108 provide instruction (e.g., microinstruction) operands 166 to the approximating functional units 106 and receive the results generated
by the approximating functional units 106, preferably via a reorder buffer (not shown). Associated with each of the architectural registers 108 is error storage 109 that holds an indication of an amount of error in the result stored in the associated register 108. Each time an approximating functional unit 106 generates a result 164 (which is written to an architectural register 108), the approximating functional unit 106 also generates an indication of the amount error 168 associated with the result 164 that has accumulated due to approximating computations. The error 168 is written to the error storage 109 associated with the destination register 108. Furthermore, each time a register 108 provides an operand to an approximating functional unit 106, the associated error storage 109 provides to the approximating functional unit 106 the error 162 associated with the operand. This enables the approximating functional unit 106 to accumulate both the error of the input operands 166 of the computation and the error introduced by the approximating functional unit 106 when performing the approximate computation.

[0024] The snapshot storage 134 holds a snapshot of the state of the processor 100. Before the processor 100 begins to perform approximate computations, it writes its state to the snapshot storage 134 so that if the accumulated error of a result of an approximate computation exceeds an error bound, the processor 100 may restore its state from the snapshot 134 and re-perform the computations without approximation, as described in more detail below according to one embodiment. In one embodiment, the snapshot storage 134 comprises a private memory of the processor 100. Preferably, the snapshot 134 includes the address of the first instruction in a set of instructions that perform approximate computations. In an embodiment (e.g., Figure 10) in which the microcode 136 causes re-execution of the set of instructions but without approximation, the microcode 136 causes a branch to the address of the first instruction held in the snapshot 134.

[0025] The data cache 138 caches data from system memory locations. In one embodiment, the data cache 138 is a hierarchy of cache memories that includes a first-level data cache and a second level cache that backs the instruction cache 102 and the first-level cache. In one embodiment, the program that employs the approximate computations must insure that its data does not overflow the data cache 138 if it is to
enjoy the recovery after exceeding the error bound feature provided by the processor 100.

[0026] In one embodiment, the approximation control register 132 holds information that specifies the approximation policy 176 for the processor 100 that is provided to the approximating functional units 106. Preferably, the approximation control register 132 includes an approximation flag, an approximation amount, and an error bound (or error threshold). The approximation flag indicates whether computations performed by the approximating functional units 106 should be full accuracy computations or approximate computations, i.e., in full accuracy mode or approximate computation mode (or approximating mode). The approximation amount tells the approximating functional units 106 the degree of accuracy less than the full degree they may employ to perform their approximate calculations. The error bound specifies the amount of accumulated error 168 that may be tolerated in a result 164 of an approximate computation, and beyond which the processor 100 signals that the error bound has been exceeded, preferably so that the computations may be performed again without approximation. In one embodiment, the approximating functional units 106 perform computations according to the approximation policy stored in the approximation control register 132. In an alternate embodiment, each instruction specifies the approximation policy to the approximating functional units 106, such as in a prefix. In one embodiment, the approximation control register 132 is writable by an instruction of the instruction set architecture of the processor 100.

[0027] The approximating functional units 106 are capable of selectively performing normal computations (i.e., with the full degree of accuracy specified by the instruction set architecture) or approximate computations (i.e., with less than the full degree of accuracy specified by the instruction set architecture). Each of the approximating functional units 106 is hardware or a combination of hardware and microcode within the processor 100 that performs a function associated with the processing of an instruction. More specifically, the hardware or combination of hardware and microcode performs a computation to generate a result. Examples of functional units include, but are not limited to, execution units, such as an integer unit, a single issue multiple data (SIMD)
unit, a multimedia unit, and a floating point unit, such as a floating point multiplier, floating point divider and floating point adder. Advantageously, the approximating functional units 106 consume less power when performing approximate computations than when performing normal computations. Embodiments of the approximating functional units 106 are described in more detail with respect to Figure 2.

[0028] Referring now to Figure 2, block diagrams illustrating three embodiments of the approximating functional units 106 of Figure 1 are shown. The three embodiments are an approximating floating point multiplier 106A, an approximating transcendental function computation unit 106B, and an approximating divider 106C.

[0029] The approximating floating point multiplier 106A receives input operands 166 from the registers 108 and generates the result 164 of Figure 1. The approximating floating point multiplier 106A includes gates 202 that perform multiplication on the most significant bits of the input operands 166 and gates 204 that perform multiplication on the least significant bits of the input operands 166. The approximating floating point multiplier 106A also includes power control logic 206 that controls the selective provision of power to the least significant bit multiplication gates 204 based on the approximation policy 176. For example, if the approximation mode is full accuracy, the power control 206 causes power to be provided to the transistors of the least significant bit multiplication gates 204; whereas, if the approximation mode is less than the full accuracy, the power control 206 causes power not to be provided to the transistors of the least significant bit multiplication gates 204. In one embodiment, the least significant bit multiplication gates 204 are grouped such that the power control 206 powers off the gates associated with the multiplication of lesser or fewer of the least significant bits based on the approximation amount indicated in the approximation policy 176. Preferably, the approximating floating point multiplier 106A is configured such that intermediate results of the least significant bit multiplication gates 204 are provided to the most significant bit multiplication gates 202 (e.g., carries), and when the least significant bit multiplication gates 204 are powered-off in approximate computation
mode, default values (e.g., zeroes) are provided as the intermediate results to the most significant bit multiplication gates 202.

[0030] Generally speaking, the approximating multiplier 106A is capable of multiplying N bits of each of two factors 166, where N bits is the full accuracy specified by the instruction set architecture. However, the approximating multiplier 106A is also capable of multiplying fewer than the N bits of each of the two factors 166 to generate a less accurate result 164 than the full accuracy. Preferably, the multiplier excludes M of the least significant bits of the factors 166 when performing the multiplication, where M is less than N. For example, assume the mantissas of the factors 166 are each 53 bits, then the transistors of the gates 204 of the approximating multiplier that would normally be used in the multiplication of the lower N bits of the 53 bits of the factors 166 are turned off such that the lower M bits of the factors 166 are not included in the approximate multiply, where the number of bits M is specified in the approximation policy, e.g., in the approximation control register 132. In this manner, the approximating multiplier 106A potentially uses less power in the approximating mode than in the full accuracy mode because it may turn off transistors that would normally be used to multiply the excluded bits. Preferably, the number of excluded bits M is quantized such that only a limited number of values of M may be specified by the approximation policy in order to reduce the complexity of the power gating logic 206.

[0031] The approximating transcendental function unit 106B receives input operands 166 from the registers 108 and generates the result 164 of Figure 1. The approximating transcendental function computation unit 106B includes transcendental computation logic 214 that performs transcendental functions on the input operands 166 to generate the result 164 based on a polynomial. The polynomial is selected from a mux 216 that selects either a high order polynomial 212A or a low order polynomial 212B based on a select control input from the computation policy 176, such as the approximation mode. That is, the mux 216 selects the high order polynomial 212A when the approximating mode is full accuracy and selects the low order polynomial 212B when the approximating mode is less than the full accuracy. Generally speaking, the approximating transcendental function computation unit 106B uses a polynomial of
order $N$ to perform transcendental functions with full accuracy and uses a polynomial of
order $M$, where $M$ is less than $N$, to perform transcendental functions with less than the
full accuracy, and where $M$ is specified by the approximation policy. Advantageously,
by employing a lower order polynomial to perform the transcendental function
computations when in approximating mode, the approximating transcendental function
computation unit 106B may consume less power and perform better than when operating
in full accuracy mode. This is because employing a lower order polynomial requires
fewer multiplies and adds than a higher order polynomial.

[0032] The approximating divider 106C receives input operands 166 from the registers
108 and generates the result 164 of Figure 1. The approximating divider 106C includes
dividing logic 222 and iteration control logic 224. The dividing logic 222 performs a
division computation on the input operands 166 to generate an intermediate result 164
and an indication 226 of the accuracy of the intermediate result 164 during a first
iteration. The intermediate result 164 is fed back as an input to the dividing logic 222,
and the accuracy indication 226 is provided to iteration control logic 224. On
subsequent iterations, the dividing logic 222 performs a division computation on the
input operands 166 and intermediate result 164 of the previous iteration to generate
another intermediate result 164 and an indication 226 of the accuracy of the intermediate
result 164 during the present iteration, and the intermediate result 164 is fed back as an
input to the dividing logic 222, and the accuracy indication 226 is provided to iteration
control logic 224. The iteration control 224 monitors the accuracy 226 and stops the
iterating once the accuracy 226 has reached an acceptable level indicated in the
approximation policy 176. Advantageously, by performing fewer iterations in exchange
for less than the full accuracy when the approximation policy indicates approximation
mode, a reduction in power consumption may be accomplished by the approximating
divider 106C.

[0033] In one embodiment, each of the approximating functional units 106 includes a
lookup table that outputs the amount of error 168 associated with the result 164
generated by the approximating functional unit 106 based on the input error 162 and
approximating amount of the approximation policy. Preferably, the amount of error 168
output by the lookup table is itself an approximation that specifies a maximum amount of error associated with the result 164.

In one embodiment, the approximating functional units 106 include an instruction decoder that decodes microinstructions generated by the instruction translator 104 when translating the approximating instructions 399 in order to determine all or a portion of the approximation policy rather than, or in addition to, the approximation policy provided by the approximation control register 132. In another embodiment, the instruction decoder decodes the approximating instructions 399 themselves, e.g., in an embodiment in which the instruction translator 104 simply decodes instructions 174 for the purpose of routing to the appropriate approximating functional unit 106, and the approximating functional unit 106 decodes the instructions 174 to determine the approximation policy.

Referring now to Figure 3, a block diagram illustrating approximation instructions 399 is shown. More specifically, the approximation instructions include a computation instruction with an approximation prefix 300, an approximate computation instruction 310, a computation instruction with a start approximation prefix 320, a start approximation instruction 330, a computation instruction with a stop approximation prefix 340, a stop approximation instruction 350, a computation instruction with a clear error prefix 360, a clear error instruction 370, and a load register instruction 380.

The computation instruction with an approximation prefix 300 includes an opcode and other fields 304 such as generally found in the instruction set of the processor 100. The opcode 304 may specify any of various computations that may be performed by the approximating functional units 106, such as addition, subtraction, multiplication, division, fused multiply add, square root, reciprocal, reciprocal square root, and transcendental functions, for example, that are susceptible to generating a result that has less accuracy than the full accuracy with which the approximating functional units 106 are capable of performing the computation, i.e., according to the full accuracy mode. The computation instruction with an approximation prefix 300 also includes an approximation prefix 302. In one embodiment, the approximation prefix
302 comprises a predetermined value whose presence within the stream of instruction bytes and preceding the opcode and other fields 304 instructs the processor 100 to perform the specified computation in an approximating manner. In one embodiment, the predetermined value is a value not already in use as a prefix value in the ISA, such as the x86 ISA. In one embodiment, a portion of the approximation prefix 302 specifies the approximation policy, or at least a portion thereof, such as the approximation amount and/or error bound, to be employed in the computation specified by the opcode and other fields 304. In another embodiment, the approximation prefix 302 simply indicates that the computation specified by the opcode and other fields 304 should be performed approximately, and the approximation policy is taken from the overall approximation policy previously communicated by the to the processor 100, which may be stored, for example, in a register, such as the approximation control register 132. Other embodiments are contemplated in which the approximation policy for the instruction 300 is derived from a combination of the prefix 302 and the overall approximation policy.

[0037] In an alternate embodiment, the approximate computation instruction 310 includes an approximate computation opcode and other fields 312. The approximate computation opcode value is distinct from other opcode values in the instruction set of the processor 100. That is, the approximate computation opcode value is distinct from other opcode values that normally (e.g., in the absence of a prefix, such as approximation prefix 302) instruct the processor 100 to perform a computation with full accuracy. Preferably, the instruction set includes multiple approximate computation instructions 310, one for each type of computation, e.g., one for addition with its own distinct opcode value, one for subtraction with its own distinct opcode value, and so forth.

[0038] The computation instruction with start approximation prefix 320 includes an opcode and other fields 314 such as generally found in the instruction set of the processor 100. The opcode 314 may specify any of various computations, or it may be a non-computation instruction. The computation instruction with start approximation prefix 320 also includes a start approximation prefix 322. In one embodiment, the start
approximation prefix 322 comprises a predetermined value whose presence within the stream of instruction bytes and preceding the opcode and other fields 324 instructs the processor 100 to perform subsequent computations (including the computation specified in the instruction 320, if present) in an approximating manner until instructed to stop performing computations in an approximating manner (e.g., by instructions 340 and 350 described below). In one embodiment, the predetermined value is a value not already in use as a prefix value in the ISA, such as the x86 ISA, and is distinct from the other prefixes described herein (e.g., approximation prefix 302, stop approximation prefix 342 and clear error prefix 362). Embodiments of the start approximation prefix 322 are similar to the approximation prefix 302 in that a portion of the start approximation prefix 322 may specify the approximation policy, or simply indicate that subsequent computations should be performed approximately using the overall approximation policy, or a combination thereof.

[0039] In an alternate embodiment, the start approximation instruction 330 includes a start approximation opcode 332. The start approximation instruction 330 instructs the processor 100 to perform subsequent computations in an approximating manner until instructed to stop performing computations in an approximating manner. Embodiments of the start approximation opcode 332 are similar to the approximation prefix 302 regarding specification of the approximation policy. The start approximation opcode 332 value is distinct from other opcode values in the instruction set of the processor 100.

[0040] The computation instruction with stop approximation prefix 340 includes an opcode and other fields 344 such as generally found in the instruction set of the processor 100. The opcode 344 may specify any of various computations, or it may be a non-computation instruction. The computation instruction with stop approximation prefix 340 also includes a stop approximation prefix 342. In one embodiment, the stop approximation prefix 342 comprises a predetermined value whose presence within the stream of instruction bytes and preceding the opcode and other fields 344 instructs the processor 100 to stop performing computations (including the computation specified in the instruction 340, if present) in an approximating manner (until instructed to perform computations in an approximating manner, e.g., by instructions 300, 310, 320 or 330).
In one embodiment, the predetermined value is a value not already in use as a prefix value in the ISA, such as the x86 ISA, and is distinct from the other prefixes described herein.

[0041] In an alternate embodiment, the stop approximation instruction 350 includes a stop approximation opcode 352. The stop approximation instruction 350 instructs the processor 100 to stop performing computations in an approximating manner (until instructed to perform computations in an approximating manner). The stop approximation opcode 352 value is distinct from other opcode values in the instruction set of the processor 100. In one embodiment, the generation of an exception by the processor 100 also instructs the processor 100 to stop performing computations in an approximate manner, i.e., causes the approximation mode to be set to full accuracy.

[0042] The computation instruction with clear error prefix 360 includes an opcode and other fields 364 such as generally found in the instruction set of the processor 100. The opcode 364 may specify any of various computations. The computation instruction with clear error prefix 360 also includes a register field 366 that specifies a destination register to which the processor 100 writes the result of the computation. The computation instruction with clear error prefix 360 also includes a clear error prefix 362. In one embodiment, the clear error prefix 362 comprises a predetermined value whose presence within the stream of instruction bytes and preceding the opcode and other fields 364 instructs the processor 100 to clear the error 109 associated with the register 108 specified by the register field 366. In one embodiment, the predetermined value is a value not already in use as a prefix value in the ISA, such as the x86 ISA, and is distinct from the other prefixes described herein.

[0043] In an alternate embodiment, the clear error instruction 370 includes a clear error opcode 372 and a register field 376. The clear error instruction 370 instructs the processor 100 to clear the error 109 associated with the register 108 specified by the register field 376. The clear error opcode 372 value is distinct from other opcode values in the instruction set of the processor 100.

[0044] The load register and clear error instruction 380 includes a load register opcode 382, memory address operand fields 384 and a register field 386. The opcode 382
instructs the processor 100 to load data from a memory location specified by the memory address operands 384 into the destination register specified in the register field 386. The opcode 382 also instructs the processor 100 to clear the error 109 associated with the register 108 specified by the register field 386.

[0045] In one embodiment, the clear error instruction 370 clears the error 109 for all registers 108, rather than a single register 108. For example, the register field 376 value may a predetermined value to indicate to clear all registers 108. A similar embodiment is contemplated with respect to the computation instruction with a clear error prefix 360 and the load register and clear error instruction 380.

[0046] In one embodiment, the instruction translator 104 maintains a flag that indicates whether the processor 100 is in approximate computation mode or full accuracy mode. For example, the instruction translator 104 may set the flag in response to encountering a start approximation instruction 330 or a computation instruction with start approximation prefix 320 and may clear the flag in response to encountering a stop approximation instruction 350 or a computation instruction with stop approximation prefix 340. Each microinstruction includes an indicator that indicates whether the computation specified by the microinstruction should be performed with full accuracy or in an approximate manner. When the instruction translator 104 translates an architectural instruction 166 into one or more microinstructions, the instruction translator 104 populates the indicator accordingly based on the current value of the mode flag. Alternatively, in the case of an architectural approximate computation instruction such as 300 or 310, the instruction translator 104 populates the indicator of the microinstruction according to the prefix 302 or opcode 312, respectively. In yet another embodiment, the indicator of the microinstruction comprises a microinstruction opcode (distinct within the microarchitectural instruction set) that specifies an approximate computation.

[0047] Referring now to Figure 4, a flowchart illustrating operation of the processor 100 of Figure 1 according to one embodiment is shown. Flow begins at block 402.
[0048] At block 402, the processor 100 decodes an architectural instruction 166. Flow proceeds to decision block 404.

[0049] At decision block 404, the processor 100 determines whether the instruction 166 is a start approximation instruction, e.g., 320 or 330 of Figure 3. If so, flow proceeds to block 406; otherwise, flow proceeds to decision block 414.

[0050] At block 406, the processor 100 performs subsequent computations according to the approximation policy (e.g., specified in the start approximation instruction, the approximation policy specified in the approximation control register 132, or a combination thereof) until it encounters a stop approximation instruction, e.g., 340 or 350 of Figure 3. Flow ends at block 406.

[0051] At decision block 414, the processor 100 determines whether the instruction 166 is a stop approximation instruction, e.g., 340 or 350 of Figure 3. If so, flow proceeds to block 416; otherwise, flow proceeds to decision block 424.

[0052] At block 416, the processor 100 stops performing computations in an approximate manner and instead performs them with full accuracy (until it encounters a start approximation instruction, e.g., 320 or 330 or approximate computation instruction 300 or 310 of Figure 3). Flow ends at block 416.

[0053] At decision block 424, the processor 100 determines whether the instruction 166 is a clear error instruction, e.g., 360 or 370 or 380 of Figure 3. If so, flow proceeds to block 426; otherwise, flow proceeds to decision block 434.

[0054] At block 426, the processor 100 clears the error 109 associated with the register 108 specified in the register field 366/376/386. Flow ends at block 426.

[0055] At decision block 434, the processor 100 determines whether the instruction 166 is a computational instruction 166. If so, flow proceeds to block 452; otherwise, flow proceeds to block 446.

[0056] At block 446, the processor 100 performs the other instruction 166, i.e., the instruction of the instruction set architecture other than the computational instructions 399. Flow ends at block 446.

[0057] At block 452, the relevant approximating functional unit 106 receives the computational instruction 166 and decodes it. Flow proceeds to decision block 454.
[0058] At decision block 454, the approximating functional unit 106 determines whether the approximation policy is approximating or full accuracy. If approximating, flow proceeds to block 456; if full accuracy, flow proceeds to block 458.

[0059] At block 456, the approximating functional unit 106 performs the computation in an approximating manner, e.g., as described herein, such as above with respect to Figure 2. Flow ends at block 456.

[0060] At block 458, the approximating functional unit 106 performs the computation in a non-approximating manner, i.e., with full accuracy. Flow ends at block 458.

[0061] Referring now to Figure 5, a flowchart illustrating operation of the processor 100 of Figure 1 within a computer system is shown. Flow begins at block 502.

[0062] At block 502, a program (e.g., operating system or other program) executing on the processor 100 determines an approximation policy to be used by the processor 100 to perform computations. Preferably, the approximation policy specifies the tolerable error bound and the approximation amount in the computations themselves, i.e., the amount of approximation each approximating functional unit 106 should employ in each approximated calculation. The program determines the approximation policy based, at least in part, on the current system configuration. For example, the program may detect whether the computer system is operating from battery power or from an effectively limitless source, such as A/C wall power. Additionally, the program may detect the hardware configuration of the computer system, such as the display size and speaker quality. The program may consider such factors in determining the desirability and/or acceptability of performing certain computations approximately rather than with full accuracy, such as audio/video-related computations. Flow proceeds to block 504.

[0063] At block 504, the program provides the approximation policy to the processor 100. In one embodiment, the program writes the approximation policy to the approximation control register 132. In one embodiment, the program executes an x86 WRMSR instruction to provide the processor 100 with the new approximation policy. Flow ends at block 504.
[0064] Preferably, when the system configuration changes, e.g., the system gets plugged into a wall socket or unplugged from a wall socket, or plugged into an external monitor of different size, then the program detects the configuration change and changes the approximation policy at block 502 and communicates the new approximation policy to the processor 100 at block 504.

[0065] Referring now to Figure 6, a block diagram illustrating three different computing systems is shown. Each of the systems includes an approximation computation-capable processor 100 of Figure 1, a display 606, and a buffer containing data 604 upon which the processor 100 performs computations to render pixels to be shown on the display 606 using, for example, the approximate computation instructions 399 of Figure 3.

[0066] The first system is a desktop computer 602A that includes a large display 606A (e.g., 24-inch or larger) and receives power from an essentially limitless power source, e.g., a wall outlet. The second system is a laptop computer 602B that includes a medium size display 606B (e.g., 15-inch) and receives power either from a wall outlet or from a battery, depending upon the choice of the user. The third system is a hand-held computer, such as a smartphone or table computer 602C that includes a relatively small display (e.g., 4.8-inch) 606C and receives its power primarily from a battery. In the illustrative examples, it is assumed the displays all have approximately the same resolution such that the amount of approximation that may be tolerated/accepted is primarily based on the display size, although it should be understood that the amount of approximate computation may also vary based on variation in the display resolution. The three systems, referred to collectively as systems 602, are intended to be representative of systems that may include the approximation computation-capable processor 100 and are provided with different characteristics for comparison to illustrate the varying uses of the approximate computing embodiments described herein; however, other embodiments are contemplated, and the use of the approximation computation-capable processor 100 is not limited to the embodiments shown.

[0067] The first system 602A tends to be intolerant of approximation and demand high accuracy because visual distortion caused by approximation of the pixel rendering would
likely be readily apparent on the large display 602A, and the power source likely renders the need for power savings due to approximate computations less necessary.

[0068] The second system 602B tends to demand a moderate amount of accuracy and tolerate a moderate amount of approximation, particularly when running on battery power, because the visual distortion caused by a moderate amount of approximation that may be apparent, although less than on a larger display with a similar resolution, may be an acceptable tradeoff for the advantage in battery life. Other the other hand, when the system 602B is plugged into a wall power source, the preferred approximation policy may be similar to that of the first system 602A.

[0069] The third system 602C tends to demand the least accuracy since the visual distortion due to approximation may be non-apparent, or largely unapparent, on a small display 606C at a nominal zoom level, and the need to save battery power is relatively great.

[0070] Referring now to Figure 7, a flowchart illustrating operation of the systems 602 of Figure 6 is shown. Flow begins at block 702.

[0071] At block 702, a program detects the type of display 606 in the system 602, such as when the system 602 is powered-on or reset. Alternatively, the program may detect a change in the display 606, e.g., when an external monitor is plugged into or unplugged from a laptop 602B. Still further, the program may detect a change in the power source, such as plugging into or unplugging from a wall outlet. Flow proceeds to block 502.

[0072] At block 502, the program determines the approximation policy based on the system configuration, as described above with respect to Figure 5. Flow proceeds to block 504.

[0073] At block 504, the program provides the processor 100 with the approximation policy, as described above with respect to Figure 5. Flow proceeds to block 708.

[0074] At block 708, the processor 100 performs calculations based on the received approximation policy as described herein, e.g., with respect to Figures 4 and 10 through 12. Flow ends at block 708.
[0075] Alternatively, the software running on the processor 100 (e.g., the graphics software) includes different routines of code (that include computation instructions 399) associated with different approximation policies (e.g., for each of the different approximation policies associated with the different system configurations of Figure 6), and the software branches to the appropriate routine based on the current system configuration.

[0076] Referring now to Figure 8, a flowchart illustrating a process for the development of software to run on an approximate computing-aware processor 100 such as described herein is shown. Flow begins at block 802.

[0077] At block 802, a programmer develops a program, such as graphics software, with a conventional programming language, such as the C language, and invokes an approximation-aware compiler with an approximation directive. The approximation-aware compiler knows the approximate computing capabilities of the target processor 100, more specifically, the set of approximation instructions 399 supported by the processor 100. The approximation directive may be a command-line option or other method of communicating to the compiler that the object code generated by the compiler should include approximation instructions 399 to perform approximate computations. Preferably, the approximation-aware compiler is invoked with the approximation directive only to compile routines in which the computations specified by the programming language are tolerant of approximate computations; whereas, other routines that are not tolerant of approximate computations are compiled without the approximation directive; and the object files generated by the respective methods are linked together into an executable program. The approximation-tolerant routines may tend to be relatively specialized routines. For example, pixel-rendering routines may include calculations on floating point data that are susceptible to approximate computations for which the approximation-aware compiler generates approximating instructions 399; whereas, loop control variables may be integer data, and the approximation-aware compiler does not generate approximating instructions 399 to
perform calculations that update the loop control variables, for example. Flow proceeds to block 804.

[0078] At 804, the approximation-aware compiler compiles the program and generates machine language instructions that include approximation instructions 399 that instruct the processor 100 to perform approximate computations as object code. In one embodiment, the machine code generated by the compiler is similar to the machine code that would otherwise be generated without the use of the approximation directive, but in which some of the instructions are preceded by an approximation-related prefix, such as the approximation prefix 302, the start approximation prefix 322, the stop approximation prefix 342, or the clear error prefix 362 of Figure 3. In one embodiment, the approximation-aware compiler generates approximate computation instructions 310 in place of normal computation instructions that it would otherwise generate in the absence of the approximation directive. In one embodiment, the approximation-aware compiler generates normal instruction sequences punctuated with start/stop approximation instructions 330/350 and/or start/stop approximation prefixes 322/342. In one embodiment, the approximation-aware compiler generates multiple code routines each of which employs a different approximation policy, as described above, and the compiler generates code that calls the appropriate subroutine based on the current system configuration, which the program may determine itself or may obtain from the operating system. Flow ends at block 804.

[0079] Referring now to Figure 9, a flowchart illustrating an alternate process for the development of software to run on an approximate computing-aware processor 100 such as described herein is shown. Flow begins at block 902.

[0080] At block 902, a programmer develops a program similar to the description at block 802 and invokes an approximation-aware compiler. However, the programming language and compiler support approximation directives and/or approximation-tolerant data types. For example, a dialect of the C language may support such directives and/or data types. The approximation directives may include compiler directives (e.g., similar to the C language #include or #define directives) that the programmer may include in the
source code to mark selective program variables as approximation-tolerant data. Similarly, the programmer may include in the source code program variables declared as approximation-tolerant data type variables for which the compiler knows to generate instructions 399 that cause approximate computations to be performed on the variables. Flow proceeds to block 904.

[0081] At block 904, the approximation-aware compiler compiles the program to generate object code similar to the manner described above with respect to block 804, but in response to the approximation directives and/or approximation-tolerant data types included in the source code being compiled. Flow ends at block 904.

[0082] Referring now to Figure 10, a flowchart illustrating operation of the processor 100 of Figure 1 to run a program that performs approximate computations is shown. Flow begins at block 1002.

[0083] At block 1002, the program provides an approximation policy to the processor 100, similar to the manner described above. Alternatively, the program itself provides the approximation policy (and restores the current approximation policy upon exit). Additionally, an alternate code path is specified that does not perform approximate computations that may be executed in the event that the error threshold is exceeded, as described below. Flow proceeds to block 1004.

[0084] At block 1004, the processor 100 takes a snapshot of its current state by writing its state to the snapshot storage 134 of Figure 1. In one embodiment, the processor 100 takes the snapshot in response to encountering an instruction executed by the program. In one embodiment, the instruction comprises an x86 WRMSR instruction. In one embodiment, taking the snapshot includes writing back to memory dirty cache lines that will be touched by the set of approximate computations of the program so that clean copies of the cache lines reside in the cache 138 and then marking the cache lines as special to denote they may be the target of approximate computations. Because the cache lines are marked as special, as they are modified by the results of approximate computations, they are not written back to memory – at least not until it has been verified that the program can complete without exceeding the acceptable error bound.
Consequently, if subsequently the processor 100 determines that the error bound has been exceeded (e.g., at block 1012), then the special cache lines are invalidated and marked as non-special, and the pre-approximate computation state of the cache lines is then available in memory for the subsequent non-approximate set of computations (e.g., at block 1014). In such an embodiment, the programmer must be aware that the special cache lines must not spill out of the cache 138; otherwise, the processor 100 treats such a condition as exceeding the error bounds. Preferably, in a multi-core processor embodiment, the cache 138 must be local to the core executing the set of approximate computations. Flow proceeds to block 1006.

[0085] At block 1006, the processor 100, in particular an approximating functional unit 106, performs an approximate computation specified by a program instruction based on the approximation policy to generate an approximate result 164. The approximating functional unit 106 also approximates the error 168 of the result 164 based on the error values 162 of the input operands and the error introduced by the approximate calculation, as described above. Flow proceeds to block 1008.

[0086] At block 1008, the approximating functional unit 106 writes the cumulative error 168 to the error storage 109 associated with the destination register 108 that receives the approximate result 164. Flow proceeds to decision block 1012.

[0087] At decision block 1012, the processor 100 determines whether the error 168 generated at block 1008 exceeds the error bound of the approximation policy. If so, flow proceeds to block 1014; otherwise, flow returns to block 1006 to execute another approximate computation of the program.

[0088] At block 1014, the processor 100 restores the processor 100 state to the snapshot that is stored in the snapshot storage 134 and re-runs the program without approximation, or at least a portion thereof after the taking of the snapshot at block 1004 that involved computations performed in an approximate manner that exceeded the error bound. Embodiments of the operation of block 1014 are described below with respect to Figures 11 and 12. Flow ends at block 1014.
[0089] Referring now to Figure 11, a flowchart illustrating in greater detail operation of block 1014 of Figure 10 according to one embodiment is shown. Flow begins at block 1102.

[0090] At block 1102, control is transferred to the microcode 136 of the processor 100 via a micro-exception (i.e., a non-architectural exception) generated in response to detecting that the error bound was exceeded at decision block 1012. The microcode 136 restores the processor 100 state to the snapshot as described above with respect to Figure 10. Additionally, the microcode 136 generates an architectural exception. Flow proceeds to block 1104.

[0091] At block 1104, the architectural exception handler transfers control to the alternate code path specified at block 1002 of Figure 10 so that the set of approximate computations are performed with full accuracy. In one embodiment, the exception handler sets the approximation policy to disable approximation (i.e., sets the approximation policy to full accuracy) and then jumps to the same code that was previously executed when approximation was enabled and which will now be executed with approximation disabled. Flow ends at block 1104.

[0092] Referring now to Figure 12, a flowchart illustrating in greater detail operation of block 1014 of Figure 10 according to an alternate embodiment is shown. Flow begins at block 1202.

[0093] At block 1202, control is transferred to the microcode 136 of the processor 100 via a micro-exception generated in response to detecting that the error bound was exceeded, and the microcode 136 restores the processor 100 state to the snapshot. Flow proceeds to block 1204.

[0094] At block 1204, the microcode 136 sets the approximation policy (e.g., writes the approximation control register 132) to full accuracy. The microcode 136 also clears the error values 109 associated with all the registers 108. The microcode 136 also causes re-execution of the program, e.g., from the point after the taking of the snapshot at block 1004. In one embodiment, the microcode 136 re-runs the program from an instruction address stored in the snapshot storage 134. Flow ends at block 1204.
[0095] Although embodiments have been described in which approximate computations are performed for audio and video purposes, other embodiments are contemplated in which approximate computations are performed for other purposes, such as sensor calculations used in computer game physics calculations. For example, the analog-to-digital converter values used in the calculations may only be accurate to 16 bits, such that game physics analysis using 53 bits of precision, for example, is unnecessary.

[0096] While various embodiments of the present invention have been described herein, it should be understood that they have been presented by way of example, and not limitation. It will be apparent to persons skilled in the relevant computer arts that various changes in form and detail can be made therein without departing from the scope of the invention. For example, software can enable, for example, the function, fabrication, modeling, simulation, description and/or testing of the apparatus and methods described herein. This can be accomplished through the use of general programming languages (e.g., C, C++), hardware description languages (HDL) including Verilog HDL, VHDL, and so on, or other available programs. Such software can be disposed in any known computer usable medium such as magnetic tape, semiconductor, magnetic disk, or optical disc (e.g., CD-ROM, DVD-ROM, etc.), a network, wire line, wireless or other communications medium. Embodiments of the apparatus and method described herein may be included in a semiconductor intellectual property core, such as a processor core (e.g., embodied, or specified, in a HDL) and transformed to hardware in the production of integrated circuits. Additionally, the apparatus and methods described herein may be embodied as a combination of hardware and software. Thus, the present invention should not be limited by any of the exemplary embodiments described herein, but should be defined only in accordance with the following claims and their equivalents. Specifically, the present invention may be implemented within a processor device that may be used in a general-purpose computer. Finally, those skilled in the art should appreciate that they can readily use the disclosed conception and specific embodiments as a basis for designing or modifying other
structures for carrying out the same purposes of the present invention without departing from the scope of the invention as defined by the appended claims.
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CLAIMS

1. A processor, comprising:

   an indicator, configured to indicate a first mode or a second mode; and

   a functional unit, configured to perform computations with a full degree of
   accuracy when the indicator indicates the first mode and to perform
   computations with less than the full degree of accuracy when the
   indicator indicates the second mode.

2. The processor of claim 1, wherein the functional unit is configured to consume
   less power when performing the computations with the less than the full degree
   of accuracy than when performing the computations with the full degree of
   accuracy.

3. The processor of claim 1, wherein to perform the computations with the less than
   the full degree of accuracy, the functional unit powers off transistors that are
   powered on to perform the computations with the full degree of accuracy.

4. The processor of claim 3, wherein the transistors are associated with a plurality
   of least significant bits of input operands to the functional unit upon which the
   computations are performed.

5. The processor of claim 4, wherein the functional unit comprises a floating point
   multiplication unit, wherein the transistors powered-off when performing the
   computations with the less than the full degree of accuracy are transistors of the
   multiplication unit that multiply the plurality of least significant bits of the input
   operands when performing the computations with the full accuracy.

6. The processor of claim 1, wherein the functional unit is configured to perform
   transcendental function computations with the full degree of accuracy using a
   polynomial of degree M and to perform the transcendental function computations
   with the less than the full degree of accuracy using a polynomial of degree N,
   wherein N is less than M.
7. The processor of claim 1, wherein the functional unit is configured to perform
division computations in an iterative manner, wherein to perform the
computations with the less than the full degree of accuracy the functional unit
ceases to iterate when a result of a current iteration reaches a predetermined level
of accuracy that is less than the full degree of accuracy with which the functional
unit is capable of performing the computations.

8. The processor of claim 1, wherein the functional unit is configured to estimate an
amount of error associated with a result generated by the functional unit when
performing the computation with the less than the full degree of accuracy.

9. The processor of claim 8, wherein the amount of error associated with the result
comprises an accumulation of an amount of error associated with input operands
to the functional unit and an amount of error introduced by the functional unit
when performing the computation with the less than the full degree of accuracy.

10. The processor of claim 1, further comprising:

    a plurality of architectural general purpose registers, wherein associated with
    each register of the plurality of architectural general purpose registers is
    an indication of an amount of error associated with a result of an
    approximate computation held in the associated register.

11. The processor of claim 10, wherein when the functional unit receives as an input
operand the result from a register of the plurality of architectural general purpose
registers the functional unit also receives the associated indication of the amount
of error associated with the result.

12. The processor of claim 10, wherein the processor is configured to clear the
indication associated with the register in response to encountering an instruction
that instructs the processor to clear the indication.

13. The processor of claim 1, wherein the indicator is set to the first mode in
response to encountering a first predetermined instruction of an instruction set
architecture of the processor and remains set for instructions subsequent to the
first predetermined instruction until encountering a second predetermined
instruction of the instruction set architecture that instructs the processor to stop
performing computations with the less than the full degree of accuracy.

14. The processor of claim 1, wherein the indicator is set to the first mode only for
an instruction in response to which one of the computations is performed with
the less than the full degree of accuracy.

15. The processor of claim 14, wherein the instruction comprises a prefix that
instructs the processor to perform the one of the computations with the less than
the full degree of accuracy.

16. A method to be performed by a processor having an indicator and a functional
unit, the method comprising:

setting the indicator to indicate a first mode or a second mode; and

performing, by the functional unit, computations with a full degree of accuracy
when the indicator indicates the first mode and to perform computations
with less than the full degree of accuracy when the indicator indicates the
second mode.

17. The method of claim 16, wherein said performing the computations with the less
than the full degree of accuracy comprises powering off transistors that are
powered on to perform the computations with the full degree of accuracy.

18. The method of claim 16, wherein said performing the computations with the full
degree of accuracy comprises performing transcendental function computations
with the full degree of accuracy using a polynomial of degree M, wherein said
performing the computations with the less than the full degree of accuracy
comprises performing the transcendental function computations with the less
than the full degree of accuracy using a polynomial of degree N, wherein N is
less than M.

19. The method of claim 16, wherein the functional unit is configured to perform
division computations in an iterative manner, wherein said performing the
computations with the less than the full degree of accuracy comprises ceasing to iterate when a result of a current iteration reaches a predetermined level of accuracy that is less than the full degree of accuracy with which the functional unit is capable of performing the computations.

20. The method of claim 16, further comprising:

approximating an amount of error associated with a result generated by the functional unit when said performing the computation with the less than the full degree of accuracy.

21. The method of claim 16, further comprising:

setting the indicator to the first mode in response to encountering a first predetermined instruction of an instruction set architecture of the processor; and

maintaining the indicator set for instructions subsequent to the first predetermined instruction until encountering a second predetermined instruction of the instruction set architecture that instructs the processor to stop performing computations with the less than the full degree of accuracy.

22. A functional unit, comprising:

an input, configured to indicate a first mode or a second mode; and

computation logic, configured to perform computations with a full degree of accuracy when the indicator indicates the first mode and to perform computations with less than the full degree of accuracy when the indicator indicates the second mode.

23. The functional unit of claim 22, wherein to perform the computations with the less than the full degree of accuracy, the functional unit powers off transistors that are powered on to perform the computations with the full degree of accuracy.
FIG. 1

INSTRUCTION CACHE 102

174 INSTRUCTIONS
(MAY INCLUDE APPROXIMATE COMPUTING INSTRUCTIONS)

INSTRUCTION TRANSLATOR 104

MICROCODE 136

172 EXCEPTION

ERROR 109

REGISTERS 108

APPROXIMATION CONTROL REG. 132

APPROXIMATING FUNCTIONAL UNITS 106
(CAPABLE OF SELECTIVELY PERFORMING NORMAL COMPUTATIONS OR APPROXIMATE COMPUTATIONS, I.E., WITH FULL DEGREE OF ACCURACY OR WITH LESS THAN FULL DEGREE OF ACCURACY)

168 ERROR

164 RESULT

SNAPSHOT 134

CACHE 138
FIG. 3

300 COMPUTATION INSTRUCTION WITH APPROXIMATION PREFIX

APPROXIMATION PREFIX 302
OPCODE AND OTHER FIELDS 304

310 APPROXIMATE COMPUTATION INSTRUCTION

APPROXIMATE COMPUTATION_OPCODE AND OTHER FIELDS 312

320 COMPUTATION INSTRUCTION WITH START APPROXIMATION PREFIX

START APPROXIMATION PREFIX 322
OPCODE AND OTHER FIELDS 324

330 START APPROXIMATION INSTRUCTION

START APPROXIMATION_OPCODE 332

340 COMPUTATION INSTRUCTION WITH STOP APPROXIMATION PREFIX

STOP APPROXIMATION PREFIX 342
OPCODE AND OTHER FIELDS 344

350 STOP APPROXIMATION INSTRUCTION

STOP APPROXIMATION_OPCODE 352

360 COMPUTATION INSTRUCTION WITH CLEAR ERROR PREFIX

CLEAR ERROR PREFIX 362
OPCODE AND OTHER FIELDS 364
REGISTER 366

370 CLEAR ERROR INSTRUCTION

CLEAR_ERROR_OPCODE 372
REGISTER 376

380 LOAD REGISTER AND CLEAR ERROR INSTRUCTION

LOAD REGISTER_OPCODE 382
ADDRESS OPERANDS 384
REGISTER 386
FIG. 4A

DECODE INSTRUCTION 402

START APPROXIMATION INSTR.? 404

PERFORM COMPUTATIONS ACCORDING TO APPROXIMATION POLICY UNTIL ENCOUNTER STOP APPROXIMATION INSTRUCTION 406

STOP APPROXIMATION INSTR.? 414

PERFORM COMPUTATIONS WITH FULL ACCURACY 416

ERROR CLEARING INSTR.? 424

CLEAR ERROR ASSOCIATED WITH REGISTER 426

COMPUTATIONAL INSTR.? 434

A

DO OTHER INSTR. 446
**FIG. 4B**

A

APPROXIMATING FUNCTIONAL UNIT RECEIVES COMPUTATIONAL INSTRUCTION 452

APPROXIMATING? 454

NO

YES

APPROXIMATING FUNCTIONAL UNIT PERFORMS APPROXIMATE COMPUTATION (E.G., POWERS OFF LOWER BITS INDICATED BY APPROXIMATION POLICY AND PERFORMS COMPUTATION SPECIFIED BY COMPUTATIONAL INSTRUCTION) 456

APPROXIMATING FUNCTIONAL UNIT PERFORMS COMPUTATION WITH FULL DEGREE OF ACCURACY (E.G., POWERS ON ALL BITS AND PERFORMS COMPUTATION SPECIFIED BY COMPUTATIONAL INSTRUCTION) 458

**FIG. 5**

DETERMINE APPROXIMATION POLICY (E.G., ERROR BOUND AND AMOUNT OF COMPUTATION APPROXIMATION) BASED ON CURRENT SYSTEM CONFIGURATION (E.G., (1) CURRENT POWER CONFIGURATION, E.G., BATTERY VS. WALL, AND (2) CURRENT HARDWARE CONFIGURATION, E.G., HIGH/MEDIUM/LOW RESOLUTION/SCREEN SIZE, GOOD/BAD SPEAKER QUALITY) 502

PROVIDE PROCESSOR WITH APPROXIMATION POLICY 504
FIG. 6

POLICY #1 – HIGH ACCURACY/LOW APPROXIMATION

DESKTOP COMPUTER 602A

APPROXIMATE COMPUTATION-CAPABLE PROCESSOR 100

DATA UPON WHICH PROCESSOR PERFORMS COMPUTATIONS TO RENDER PIXELS FOR DISPLAY 604

24" DISPLAY 606A

POLICY #2 – MEDIUM ACCURACY/MEDIUM APPROXIMATION

LAPTOP COMPUTER 602B

APPROXIMATE COMPUTATION-CAPABLE PROCESSOR 100

DATA UPON WHICH PROCESSOR PERFORMS COMPUTATIONS TO RENDER PIXELS FOR DISPLAY 604

15" DISPLAY 606B

POLICY #3 – LOW ACCURACY/HIGH APPROXIMATION

HAND-HELD COMPUTER 602C

APPROXIMATE COMPUTATION-CAPABLE PROCESSOR 100

DATA UPON WHICH PROCESSOR PERFORMS COMPUTATIONS TO RENDER PIXELS FOR DISPLAY 604

4.8" DISPLAY 606C
FIG. 7

DETECT DISPLAY CONFIGURATION (OR CHANGE THERE TO) 702

DETERMINE APPROXIMATION POLICY BASED ON SYSTEM CONFIGURATION 502

PROVIDE PROCESSOR WITH APPROXIMATION POLICY 504

PERFORM CALCULATIONS BASED ON APPROXIMATION POLICY 708

FIG. 8

DEVELOP PROGRAM WITH CONVENTIONAL PROGRAMMING LANGUAGE AND INVOKE APPROXIMATION-AWARE COMPILER WITH APPROXIMATION DIRECTIVE 802

APPROXIMATION-AWARE COMPILER COMPILES PROGRAM AND GENERATES APPROXIMATION PREFIXES AND/OR APPROXIMATION INSTRUCTIONS FOR THE OBJECT CODE 804

FIG. 9

DEVELOP PROGRAM WITH PROGRAMMING LANGUAGE THAT SUPPORTS APPROXIMATION DIRECTIVES AND/OR APPROXIMATION-TOLERANT DATA TYPES AND INVOKE APPROXIMATION-AWARE COMPILER 902

APPROXIMATION-AWARE COMPILER COMPILES PROGRAM AND GENERATES APPROXIMATION PREFIXES AND/OR APPROXIMATION INSTRUCTIONS FOR THE OBJECT CODE 904
FIG. 10

1. Specify approximation policy and alternate code path (e.g., non-approximating code path) 1002
2. Take snapshot of current processor state 1004
3. Perform approximate computation using approximation policy and generate approximate result and approximate cumulative error of result based on error value of source registers and error introduced by approximate calculation 1006
4. Write cumulative error to destination register error 1008
5. Error bound exceeded? 1012
   - No
   - Yes
6. Restore processor state to snapshot and re-run without approximation 1014
FIG. 11

MICROCODE_restores_STATE_to_SNAPSHOT_and_generates_ARCHITECTURAL_EXCEPTION_1102

ARCHITECTURAL_EXCEPTION_HANDLER_TRANSFERS_CONTROL_TO_ALTERNATE_CODE_PATH_THAT_DOES_NOT_USE_APPROXIMATION_1104

FIG. 12

MICROCODE_restores_STATE_TO_SNAPSHOT_1202

MICROCODE_SETS_APPROXIMATION_POLICY_TO_USE_FULL_ACCURACY,_CLEARS_ERROR, AND_CAUSES_RE-EXECUTION_OF_INSTRUCTIONS BUT_IN_A_NON-APPROXIMATING_MANNER_DISREGARDING WHETHER_THE_INSTRUCTIONS_INSTRUCT_THE_PROCESSOR_TO_USE_APPROXIMATION_1204
INTERNATIONAL SEARCH REPORT

A. CLASSIFICATION OF SUBJECT MATTER
G06F 7/00(2006.01)j

According to International Patent Classification (IPC) or to both national classification and IPC

B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)
G06F

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

Electronic data base consulted during the international search (name of data base and, where practically, search terms used)
WPI;EPDOC;CNPAT;CNKI:IEEE: cpu, processor, mode, approximate, accurate, computing, indicate, instruction, mode, power

C. DOCUMENTS CONSIDERED TO BE RELEVANT

<table>
<thead>
<tr>
<th>Category*</th>
<th>Citation of document, with indication, where appropriate, of the relevant passages</th>
<th>Relevant to claim No.</th>
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<td>CN 102736896 A (INTERNATIONAL BUSINESS MACHINES CORP.) 17 October 2012 (2012-10-17) the whole document</td>
<td>1-23</td>
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Date of the actual completion of the international search
09 June 2015

Date of mailing of the international search report
30 June 2015

Name and mailing address of the ISA/CN

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