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(54) **COVARIANCE MATRIX FOR ADAPTIVE BEAMFORMING**

USPC 375/299
See application file for complete search history.

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(57) **ABSTRACT**

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A method and apparatus for generating a covariance matrix during adaptive beamforming of a multi-beam antenna. The method uses an upper right triangle of the covariance and time sharing of complex conjugate multipliers to efficiently compute the covariance matrix. In addition, a variable number of beams may be selected in the covariance matrix according to an operating environment of the multi-beam antenna.

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(52) **U.S. Cl.**
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CPC H04B 7/0617

15 Claims, 7 Drawing Sheets

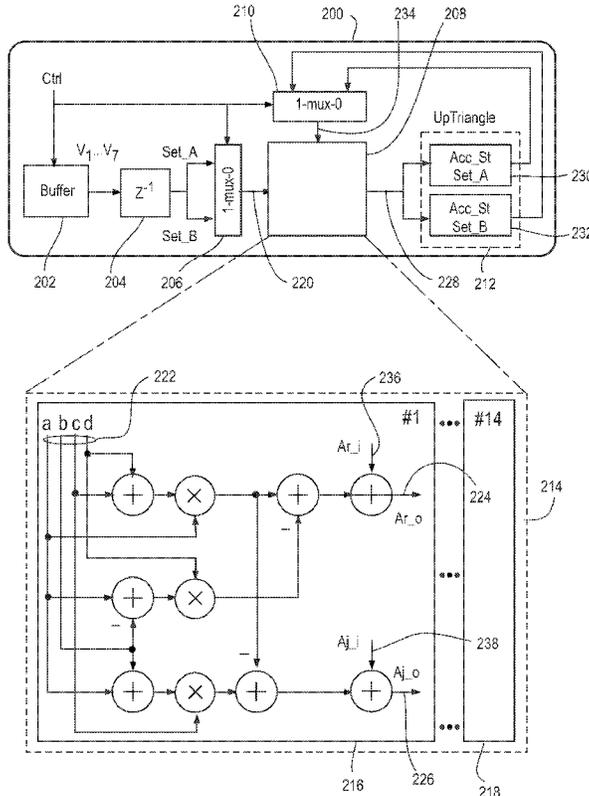


Fig. 1

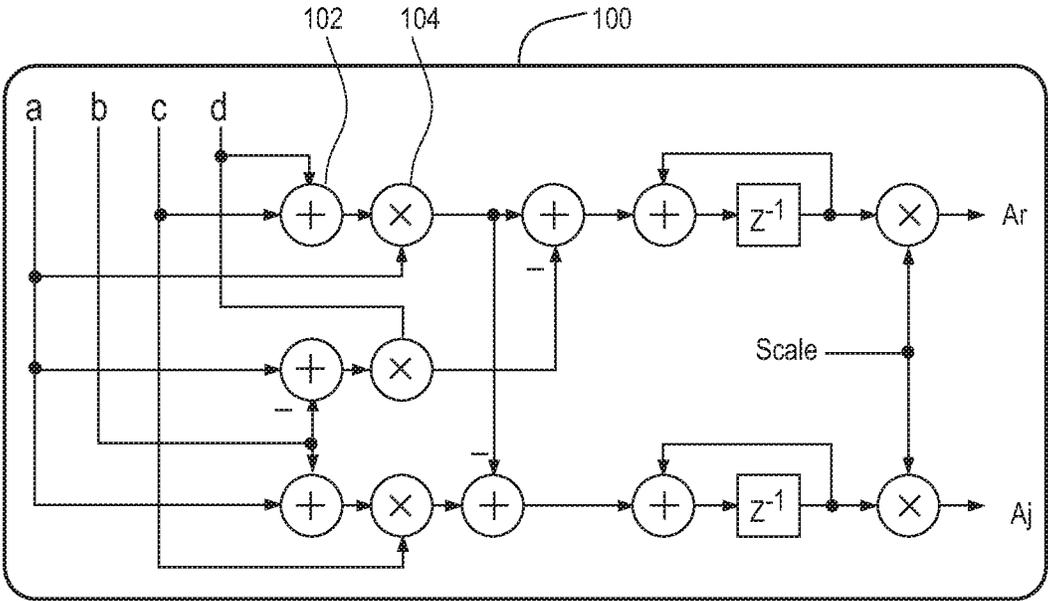


Fig. 2

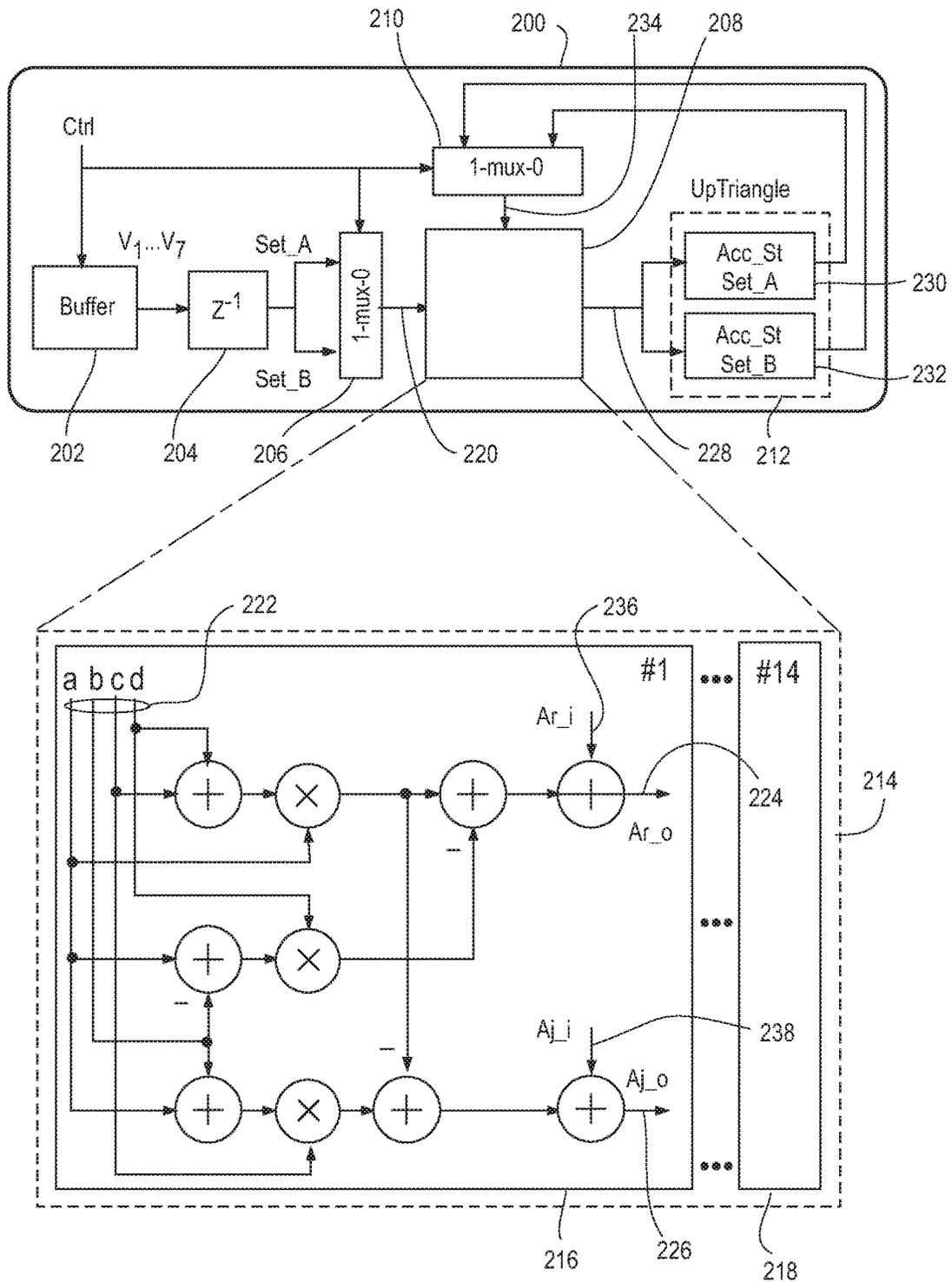


Fig. 3

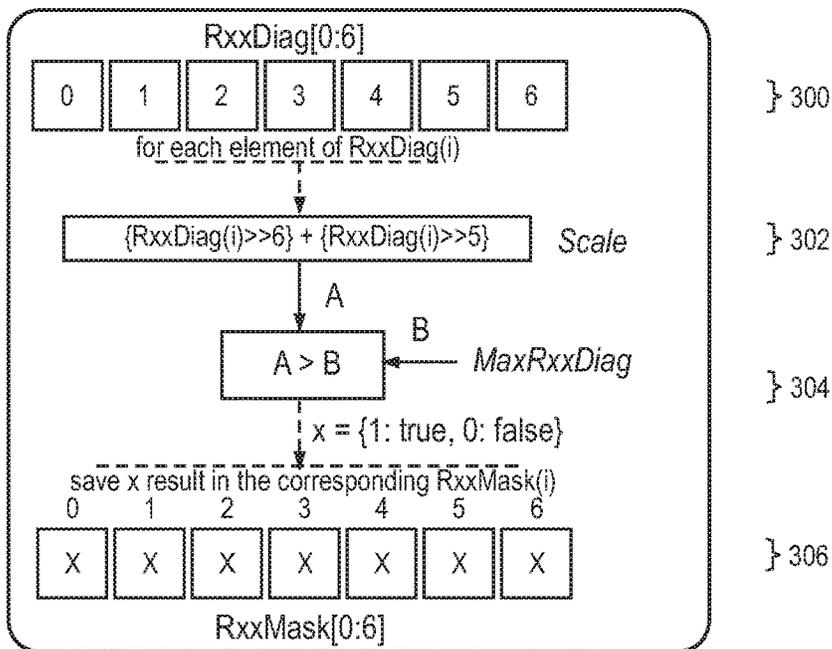


Fig. 4

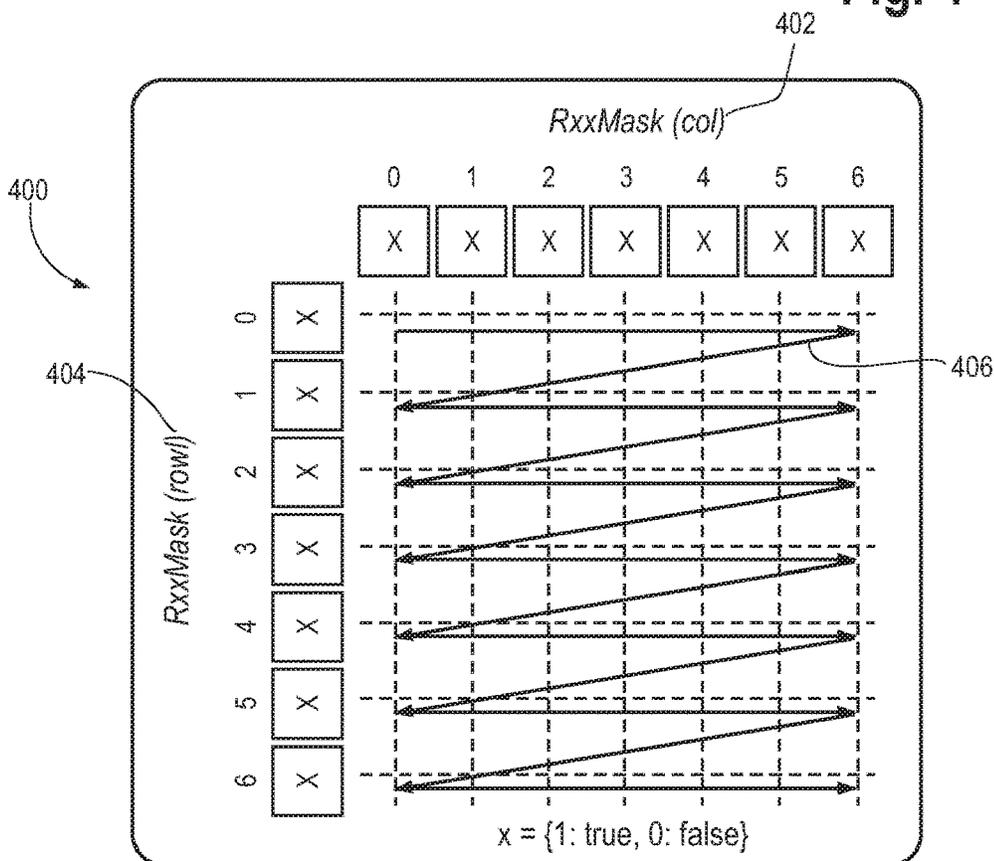


Fig. 5

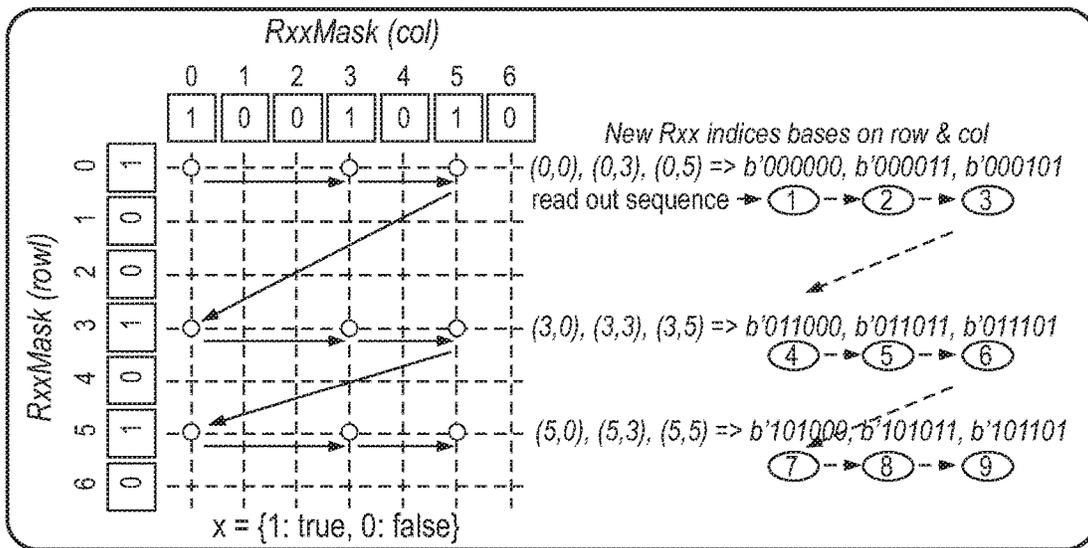


Fig. 6

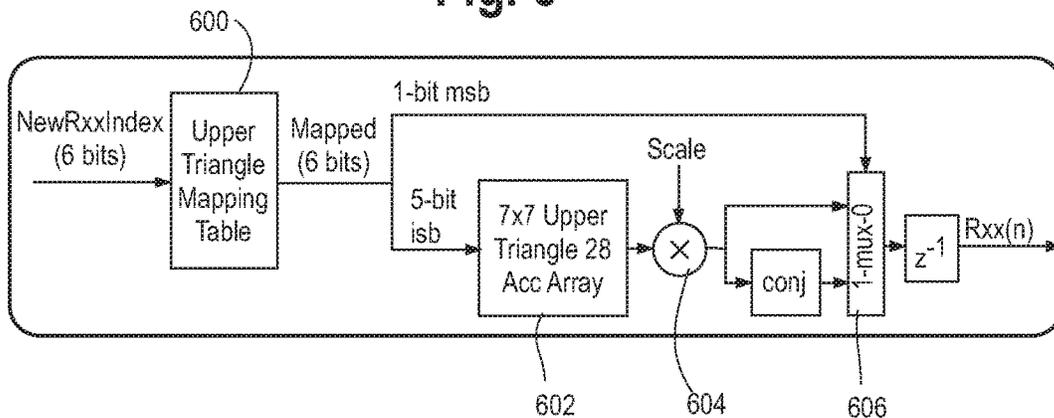


Fig. 7

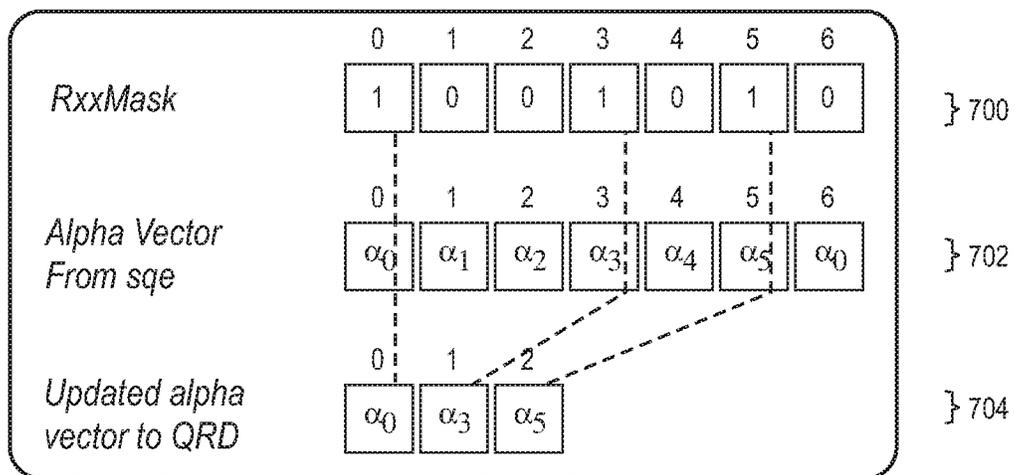


Fig. 8

Table 3

Address In	row	col	Address out	Address In	row	col	Address Out
0	000	000	0	32	100	000	36
1	000	001	1	33	100	001	42
2	000	010	2	34	100	010	47
3	000	011	3	35	100	011	51
4	000	100	4	36	100	100	22
5	000	101	5	37	100	101	23
6	000	110	6	38	100	110	24
8	001	000	33	40	101	000	37
9	001	001	7	41	101	001	43
10	001	010	8	42	101	010	48
11	001	011	9	43	101	011	52
12	001	100	10	44	101	100	55
13	001	101	11	45	101	101	25
14	001	110	12	46	101	110	26
16	010	000	34	48	110	000	38
17	010	001	40	49	110	001	44
18	010	010	13	50	110	010	49
19	010	011	14	51	110	011	53
20	010	100	15	52	110	100	56
21	010	101	16	53	110	101	58
22	010	110	17	54	110	110	27
24	011	000	35				
25	011	001	41				
26	011	010	46				
27	011	011	18				
28	011	100	19				
29	011	101	20				
30	011	110	21				

Fig. 9

802 

Table 4

		000	001	010	011	100	101	110
	Row/col	0	1	2	3	4	5	6
000	0	0	1	2	3	4	5	6
001	1	33	7	8	9	10	11	12
010	2	34	40	13	14	15	16	17
011	3	35	41	46	18	19	20	21
100	4	36	42	47	51	22	23	24
101	5	37	43	48	52	55	25	26
110	6	38	44	49	53	56	58	27

COVARIANCE MATRIX FOR ADAPTIVE BEAMFORMING

GOVERNMENT CONTRACT

The United States Air Force has rights in this invention pursuant to Government Contract No. F04701-02-C-0002.

TECHNICAL FIELD

Various example embodiments relate generally to adaptive beam-forming and more particularly to obtaining optimal combining weights using a covariance matrix.

BACKGROUND

Adaptive beamforming is a technique of using spatial signal processing to combine signals from an array of antennas to increase signal strength to or from a preferred location. It is used in both transmitting and receiving signals. Spatial signal processing involves determining optimal weights for each signal, or beam, before they are combined and thus maximizing the signal-to-noise ratio (SNR) of the signal sent to or received from a particular direction.

Spatial signal processing may include the use of a covariance matrix, which stores correlation statistics of the variation between signals. Calculating a covariance matrix is very resource intensive for a processing system. For example, for a 4x4 array of 16 elements, 136 correlations must be calculated. This may require significant hardware capability, in other words, multipliers and/or memory. It may also require a powerful common processor or a complicated multiplexing scheme.

Thus, a need exists for simplifying the hardware for calculation of a covariance matrix during adaptive beam-forming.

SUMMARY

A method and apparatus for generating a covariance matrix during adaptive beamforming of a multi-beam antenna is disclosed. The method uses an upper right triangle of the covariance and time sharing of complex conjugate multipliers to efficiently compute the covariance matrix. In addition, a variable number of beams may be selected in the covariance matrix according to an operating environment of the multi-beam antenna.

The invention in one implementation encompasses a method of generating a covariance matrix for digital beam-forming in a computer processor on input signals from antenna beams stored in a buffer. The method includes steps of receiving a set of N_B input signals from the buffer where N_B = the number of antenna beams; generating a temporary $N_B \times N_B$ covariance matrix; dividing the N_B input signals into Set A and Set B; performing a complex-conjugate multiplication operation on Set A, adding the result to previous Set A accumulator results and storing in Set A accumulators; performing a complex-conjugate multiplication operation on Set B, adding the result to previous Set B accumulator results and storing in Set B accumulators; and combining the Set A and Set B results to form an $N_B \times N_B$ covariance matrix.

In a further embodiment, each input signal further includes a plurality of data symbols and the method is repeated for each of the plurality of symbols.

In another embodiment, the Set A and Set B accumulators are cleared after the covariance matrix is generated.

In several embodiments, the number of data symbols may be, for example, 42, 84 or 168.

In any of the above embodiments, the number of antenna beams may be 7.

In a further embodiment, the method includes the steps of determining a set of N_B diagonal elements of the $N_B \times N_B$ covariance matrix; for each element in the set of diagonal elements: scaling the element with a constant; comparing the scaled result with a maximum element of the set of diagonal elements; and marking a corresponding element in masking index as true or false; and using the masking index to select elements in the $N_B \times N_B$ covariance matrix.

In another embodiment, the masking index may be used on both rows and columns of the $N_B \times N_B$ covariance matrix.

In a further embodiment, the constant may be a variable beam threshold based on an operating environment of the antenna.

In another embodiment, the invention encompasses a computer processor apparatus configured to perform a method of generating a covariance matrix for digital beam-forming the input signals from one or more elements of multi-beam antenna. The computer processor apparatus includes a buffer for storing N_B input signals where N_B = the number of antenna beams; a logic element for generating a temporary $N_B \times N_B$ covariance matrix from the N_B input signals; a set of $N_B(N_B+1)/4$ complex conjugate multipliers; a first multiplexer for receiving $N_B(N_B+1)/2$ elements of the temporary covariance matrix further comprising an upper right triangle of the temporary covariance matrix and alternately coupling half of the $N_B(N_B+1)/2$ elements to the set of complex conjugate multipliers; a set of $N_B(N_B+1)/2$ accumulators divided into first and second sets of $N_B(N_B+1)/4$ accumulators which alternately receive outputs from the set of complex conjugate multipliers; and a second multiplexer alternately coupling the output of the first and second sets of $N_B(N_B+1)/4$ accumulators to an input of the set of $N_B(N_B+1)/4$ complex conjugate multipliers.

In a further embodiment, N_B may be 7.

In another embodiment, the apparatus also includes an N_B buffer for storing a set of diagonal elements of the covariance matrix; a scaling logic element for scaling each element in the set of diagonal elements by a constant value; a comparator for comparing each scaled element with a maximum element of the set of diagonal elements and generating a true or false output corresponding to the result of the comparison; and an N_B mask buffer for storing the output of the comparator for each element in the set of diagonal elements.

In yet another embodiment, the apparatus includes a selection device for using the N_B mask buffer to select elements of the covariance matrix.

In another embodiment, the constant value may be a variable beam threshold based on an operating environment of the multi-beam antenna.

DESCRIPTION OF THE DRAWINGS

Features of example implementations of the invention will become apparent from the description, the claims, and the accompanying drawings in which:

FIG. 1 depicts an accumulator for calculating a covariance matrix.

FIG. 2 depicts an apparatus for calculating a covariance matrix.

FIG. 3 depicts a method of variable beam selection using the covariance matrix of FIG. 2.

FIG. 4 depicts an updated covariance matrix using the mask of FIG. 3.

FIG. 5 depicts an example of variable beam selection with a covariance matrix.

FIG. 6 depicts a further method of processing a covariance matrix.

FIG. 7 depicts a process of using a covariance matrix mask to select elements in an alpha vector;

FIG. 8 is table used for QR decomposition processing; and

FIG. 9 is another table used for QR decomposition processing.

DETAILED DESCRIPTION

Reference will now be made in detail to one or more embodiments of the invention. While the invention will be described with respect to these embodiments, it should be understood that the invention is not limited to any particular embodiment. On the contrary, the invention includes alternatives, modifications, and equivalents as may come within the spirit and scope of the appended claims. Furthermore, in the following description, numerous specific details are set forth to provide a thorough understanding of the invention. The invention may be practiced without some or all of these specific details. In other instances, well-known structures and principles of operation have not been described in detail to avoid obscuring the invention.

In general, beamforming combines signals from an array of antennas to transmit and receive directional signals using the principles of constructive and destructive interference. Signals detected by each antenna in the array are phased, or weighted, by varying amounts so as to transmit or receive a desired signal from a terminal. In an embodiment, this may be accomplished with an algorithm that uses a frequency-hopped system as the target environment. A frequency-hopped system transmits signals by rapidly switching between different frequency channels. This approach is capable of operating in scenarios including both an AWGN (Additive White Gaussian Noise) and an AWGN with jamming environment. Additionally, this approach can also be used in the presence of non-hostile interference such as that which often occurs in a crowded telecommunications environment. A beamforming algorithm and apparatus may include, for example, a maximum likelihood alpha estimator, a symbol quality estimator and an optimal combining algorithm with dynamic noise loading. QR decomposition as well as a covariance matrix and an alpha estimate generated from beam antenna input signals are some of the intermediate steps used to generate combining weights for beamforming.

In an embodiment, a multi-beam antenna includes seven antennas, although any number of antennas may be used. For the following discussion, reference will be made to a seven beam antenna solely for purposes of illustration. Beamforming is performed on an input signal X where X is a matrix of $N_B \times N_{sym}$, $N_B = \#$ antenna beams and $N_{sym} = \#$ of symbols from each beam. In an embodiment of 7 beams, for example, matrix X may be defined as having dimensions of 7×42 although other values for N_{sym} may be used, for example, 84 or 168. The input signal is given by:

$$X = \begin{bmatrix} x_{1,N_{sym}} & \dots & x_{1,1} \\ \vdots & \ddots & \vdots \\ x_{7,N_{sym}} & \dots & x_{7,1} \end{bmatrix} \quad (1)$$

There are $N_{sym}[7 \times 1]$ column vectors in a representative 7 beam embodiment. The column vector for the first symbol, for example, is given by:

$$v_1 = \begin{bmatrix} x_{1,1} \\ \vdots \\ x_{7,1} \end{bmatrix} \quad (2)$$

As each column vector v is read out (starting from the first defined column), a temporary covariance matrix is computed as

$$TmpR_{XX} = (\text{Scale Factor}) \cdot \begin{bmatrix} (v_1 v_1') & (v_1 v_2') & (v_1 v_3') & \dots & (v_1 v_7') \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ (v_7 v_1') & (v_7 v_2') & (v_7 v_3') & \dots & (v_7 v_7') \end{bmatrix} \quad (3)$$

where $v_x' = \text{conjugate}(v_x)$ and $R_{XX} = R_{XX} + TmpR_{XX}$, initialize $R_{XX} = \text{zeros}(7,7)$. In an embodiment, since $v_a v_b' = (v_b v_a')$, only the right upper triangle of $TmpR_{XX}$ needs to be computed and summed because the lower triangle is computed directly from the accumulated results of the upper triangle due to the symmetric conjugate property of R_{XX} . In an embodiment, there are a total of 28 accumulators for the upper right triangle from Acc[1] to Acc[28]; each accumulator corresponds to an element of the R upper triangle starting from top to bottom and left to right. This principle is illustrated by Table 1:

TABLE 1

Upper Triangle (R_{XX})		ACC[.]	Lower Triangle (R_{XX})		
row	col	#	row	col	
0	0	0	0	0	x
0	1	1	1	0	conj(Acc[1])
0	2	2	2	0	conj(Acc[2])
0	3	3	3	0	conj(Acc[3])
0	4	4	4	0	conj(Acc[4])
0	5	5	5	0	conj(Acc[5])
0	6	6	6	0	conj(Acc[6])
1	1	7	1	1	x
1	2	8	2	1	conj(Acc[8])
1	3	8	3	1	conj(Acc[9])
1	4	10	4	1	conj(Acc[10])
1	5	11	5	1	conj(Acc[11])
1	6	12	6	1	conj(Acc[12])
2	2	13	2	2	x
2	3	14	3	2	conj(Acc[14])
2	4	15	4	2	conj(Acc[15])
2	5	16	5	2	conj(Acc[16])
2	6	17	6	2	conj(Acc[17])
3	3	18	3	3	x
3	4	19	4	3	conj(Acc[19])
3	5	20	5	3	conj(Acc[20])
3	6	21	6	3	conj(Acc[21])
4	4	22	4	4	x
4	5	23	5	4	conj(Acc[23])
4	6	24	6	4	conj(Acc[24])
5	5	25	5	5	x
5	6	26	6	5	conj(Acc[26])
6	6	27	6	6	x

A representation of a complex-conjugate multiplier-accumulator **100** for covariance R_{XX} computation with dynamic loading is shown in FIG. 1. Multiplier-accumulator **100** performs the calculation of $\text{Acc} = \text{Ar} + \text{jAj}$. Given that $v_x = a + \text{j}b$ and $v_y = c + \text{j}d \rightarrow v_y' = c - \text{j}d$ then $v_x v_y' = (a + \text{j}b)(c - \text{j}d) = (ac + bd) + \text{j}(bc - ad)$. Since $(ac + bd) = a(c + d) - d(a - b)$ and $(bc - ad) = c(a +$

b)-a(c+c), multiplier-accumulator **100** is designed with adders, represented at **102** and multipliers, represented at **104**, to calculate Ar and Aj. A scale factor depends on N_{sym} , as does the number of accumulated iterations. Accumulators are cleared at the beginning of each hop.

In an embodiment, a covariance matrix is iteratively calculated as shown in FIG. 2 according to the following steps: (1) read $v_1 \dots v_7$ column vector from the input data buffer **202**; (2) generate $TmpR_{xx}$ in logic element **204** and send to multiplexer **206**; (3) perform complex-conjugate multiply in shared multipliers **208**, add to previous results from multiplexer **210**; (4) store the new 7x7 results into accumulator registers **212** to get ready for next iteration, (5) repeat step 1 to step 5 until 42^{nd} iteration.

As explained above with reference to Table 1, a 7x7 covariance matrix may be calculated using only an Upper Right Triangle of 28 elements. In an embodiment, an implementation of the invention is optimized by reducing the number of complex-conjugate multipliers by half and using a time-sharing scheme. The Upper Right Triangle of a covariance matrix as shown in the left three columns of Table 1 may be further divided into SET A and SET B as shown in Table 2. Referring to FIG. 2, the column vector is divided into SET A and SET B and input to multiplexer **206**. Multipliers **208** are shown in an expanded view at **214** which depicts multiplier #1 at **216** and multiplier #14 at **218**. Multipliers #2-#13 are implied. Output **220** of multiplexer **206** is connected to input **222** of each of multipliers #1-#14 in a time-sharing way so that first the results for Set A as shown in Table 2 are calculated, then the result for Set B is calculated. Outputs **224** and **226** of each multiplier are likewise sent on output **228** to so that the results of Set A are sent to SET A accumulators **230** while the results for SET B are sent to SET B accumulators **232**. Previous results are sent from accumulators **230** and **232** through multiplexer **210**. Output **234** of multiplexer **210** is coupled to inputs **236** and **238** of each multiplexer #1-#14.

TABLE 2

SET A		Acc[.]	SET B		Acc[.]
row	col	#	row	col	#
0	0	0	2	3	14
0	1	1	2	4	15
0	2	2	2	5	16
0	3	3	2	6	17
0	4	4	3	3	18
0	5	5	3	4	19
0	6	6	3	5	20
1	1	7	3	6	21
1	2	8	4	4	22
1	3	9	4	5	23
1	4	10	4	6	24
1	5	11	5	5	25
1	6	12	5	6	26
2	2	13	6	6	27

In a further embodiment, the beamforming speed and other characteristics may be further optimized using a variable beam selection depicted in FIGS. 3-4. As describe above, after an initial 7x7 covariance matrix R is computed, an Upper Triangle Array of 28 entries is generated. From this array, a variable beam selection may be computed in the following steps, illustrated in FIG. 3:

Save the seven diagonal elements from R_{xx} as $R_{xx}Diag[0:6]$, shown as **300** in FIG. 3.

Select a Variable Beam Selection threshold, $VarBeamTh$. This value may be a constant or a programmable variable

that changes based on the operating signal environment such as whether or not a jamming signal is present. In an embodiment, $VarBeamTh=96$.

For each element in $R_{xx}Diag[0:6]$, perform the steps of scaling the element with the constant $VarBeamTh$ at **302** of FIG. 3, comparing the scaled result with $MaxR_{xx}Diag$ as shown at **304** and marking a corresponding element in $R_{xx}Mask[0:6]$ index as true or false, shown at **306**.

This $R_{xx}Mask[0:6]$ will be used to form indices for the new updated R for QR decomposition (QRD). It will also be used to select the correct alpha elements from alpha vector produced by Alpha Estimate and Alpha Update processors for QRD.

In an embodiment using variable beam selection, a new updated R covariance matrix is generated using the $R_{xx}Mask$ as depicted in FIG. 4.

The $R_{xx}Mask[0:6]$ is used for both columns and rows to determine what elements to use for the new updated Rxx in the following steps illustrated in FIG. 4.

(1) Use the $R_{xx}Mask$ to form the 2-D array **300**. The same $R_{xx}Mask$ is used in both the column and rows as $R_{xx}Mask(col)$ **402** and $R_{xx}Mask(row)$ **404**.

(2) Select the elements that have both row & col intersection that are true according to $R_{xx}Mask(col)$ **402** and $R_{xx}Mask(row)$ **404**.

(3) Form a 6-bit index (3-bit rowx3-bit col) to be used to extract an element from the Upper Triangle array initially computed.

Note that QR decomposition (QRD) only needs one element at a time for SGR processing, it goes from top to bottom and from left to right (dotted lines **406** of FIG. 4). For QRD to process the updated Rxx, this rule remains true, but some of the elements are not used. Essentially, only a subset of the original 7x7 array is used.

The updated new Rxx can be from 7x7 (if all intersection are true) to 1x1 (only 1 intersection is true). This variation is determined by $VarBeamTh$.

An example of this method is illustrated in FIG. 5. In this example, $VarBeamTh$ is selected to extract a 3x3 Rxx from an initial 7x7 Rxx. In this example, it is assumed that $R_{xx}Mask$ has Beam 0, 3 and 5 set as being true. The new Rxx 2D-array indices are (0,0), (0,3), (0,5), (3,0), (3,3), (3,5), (5,0), (5,3) and (5,5) as shown in FIG. 5.

After all the new Rxx indices are determined based on $R_{xx}Mask$, the next step is to extract the corresponding elements from the initial 7x7 Upper Triangle Accumulated Array (28 entries) as shown in FIG. 6. The new Rxx indices are usually read out according to the QRD scheduler as shown in previous figure. The followings steps are taken to extract the new R_{xx} element for QRD processing:

(1) Take the new R 6-bit index to the Upper Triangle Mapping Table **600** as shown in FIG. 6 and Table 3 (FIG. 8, **800**). In this table, the Address In column is the new R 6-bit index while the Address Out is the mapped 6-bit index. Note that a 6-bit input results in 63 (0-63) possible entries, however, since the table shown only has 7x7=49 entries, then input address that are not used can never happen and are ignored. The range of input addresses based on row and column values may go from 0 to 54; however, certain values are not used such as 7, 15, 23, 31, 39 and 47. The values that are used are derived from the concatenation of 3-bit row and 3-bit column. A comparison of Tables 3 and 4 shows the corresponding elements of the initial 7x7 Upper Triangle accumulated array.

(2) Use the lower 5 least significant bits of the mapped 6-bit to index to the 7x7 Upper Triangle Array **602** of FIG. 6 and Table 4 (28 entries) (FIG. 9, **802**) to obtain the correct

element. Since there are only 28 (0 to 27) entries for the Upper Triangle, and that 5 bits means 32 possible entries, so values 28 to 31 of Table 4 are not used/ignored.

(3) After scaling the output element at 604 of FIG. 6, the most significant bit of the mapped 6-bit is used to select in multiplexer 606 between conjugate and non-conjugate values for QRD for processing as shown in FIG. 6.

The Variable Beam selection method may also be used to select alpha elements to process with QR Decomposition (QRD). As illustrated in FIG. 7, alpha vector elements are selected based on R_{xx} Mask from FIG. 3. For each position or index of the mask bit in R_{xx} Mask 700, it is set to be true, then a corresponding alpha element 702 is selected. In other words, the same index is used to extract the alpha element from the input alpha vector 704 sent to QRD. If variable beam selection is not used, in other words, if processing was performed with all 7 beams, the alpha element selection is not needed. A representation based on the example of FIG. 3 is shown in Table 5, which shows how to map the input indices to the Upper Triangle Table 4 to obtain the correct elements to send to QRD based on the 5-bit lsb (least significant bits) of the address output. Note that QRD processes one element at a time. Whenever the 1-bit msb (most significant bit) is true, take the conjugate of the scaled output.

TABLE 5

Read Order	Address In	Row	Col	Address Out	1b-msb	5b-lsb
1, (0,0)	0	000	000	0	0	00000
2, (0,3)	3	000	011	3	0	00011
3, (0,5)	5	000	101	5	0	00101
4, (3,0)	24	011	000	35	1	00011
5, (3,3)	27	011	011	18	0	10010
6, (3,5)	29	011	101	20	0	10100
7, (5,0)	40	101	000	37	1	00101
8, (5,3)	43	101	011	52	1	10100
9, (5,5)	45	101	101	25	0	11001

If used and unless otherwise stated, the terms “upper,” “lower,” “front,” “back,” “over,” “under,” and similar such terms are not to be construed as limiting the invention to a particular orientation. Instead, these terms are used only on a relative basis.

The apparatus described above in one example comprises a plurality of components such as one or more of electronic components or hardware components. A number of such components can be combined or divided in the apparatus. The apparatus in one example comprises any (e.g., horizontal, oblique, or vertical) orientation, with the description and figures herein illustrating one example orientation of the apparatus, for explanatory purposes.

The steps or operations described herein are just for example. There may be many variations to these steps or operations without departing from the spirit of the invention. For instance, the steps may be performed in a differing order, or steps may be added, deleted, or modified. Although example implementations of the invention have been depicted and described in detail herein, it will be apparent to those skilled in the relevant art that various modifications, additions, substitutions, and the like can be made without departing from the spirit of the invention and these are therefore considered to be within the scope of the invention as defined in the following claims.

What is claimed is:

1. A method of generating a covariance matrix for digital beamforming in a computer processor on input signals from antenna beams stored in a buffer, comprising:

receiving a set of N_B input signals from the buffer where N_B =the number of antenna beams;

generating a temporary $N_B \times N_B$ covariance matrix; dividing the N_B input signals into Set A and Set B; performing a complex-conjugate multiplication operation on Set A, adding the result to previous Set A accumulator results and storing in Set A accumulators; performing a complex-conjugate multiplication operation on Set B, adding the result to previous Set B accumulator results and storing in Set B accumulators; combining the Set A and Set B results to form an $N_B \times N_B$ covariance matrix; and performing digital beamforming of the antenna beams using the $N_B \times N_B$ covariance matrix.

2. The method of claim 1 where each input signal further comprises a plurality of data symbols and the method is repeated for each of the plurality of symbols.

3. The method of claim 2, wherein the Set A and Set B accumulators are cleared after the covariance matrix is generated.

4. The method of claim 2, wherein the number of data symbols is 42.

5. The method of claim 2, wherein the number of data symbols is 84.

6. The method of claim 2, wherein the number of data symbols is 168.

7. The method of claim 1, wherein the number of antenna beams is 7.

8. The method of claim 1, further comprising the steps of: determining a set of N_B diagonal elements of the $N_B \times N_B$ covariance matrix;

for each element in the set of diagonal elements:

scaling the element with a constant;

comparing the scaled result with a maximum element of the set of diagonal elements; and

marking a corresponding element in masking index as true or false; and

using the masking index to select elements in the $N_B \times N_B$ covariance matrix.

9. The method of claim 8 wherein the masking index is used on both rows and columns of the $N_B \times N_B$ covariance matrix.

10. The method of claim 8 wherein the constant is a variable beam threshold based on an operating environment of the antenna.

11. A computer processor apparatus configured to perform a method of generating a covariance matrix for digital beamforming the input signals from one or more elements of multi-beam antenna, comprising:

a buffer for storing N_B input signals where N_B =the number of antenna beams;

a logic element for generating a temporary $N_B \times N_B$ covariance matrix from the N_B input signals;

a set of $N_B (N_B+1)/4$ complex conjugate multipliers;

a first multiplexer for receiving $N_B (N_B+1)/2$ elements of the temporary covariance matrix further comprising an upper right triangle of the temporary covariance matrix and alternately coupling half of the $N_B (N_B+1)/2$ elements to the set of complex conjugate multipliers;

a set of $N_B (N_B+1)/2$ accumulators divided into first and second sets of $N_B (N_B+1)/4$ accumulators which alternately receive outputs from the set of complex conjugate multipliers; and

a second multiplexer alternately coupling the output of the first and second sets of $N_B (N_B+1)/4$ accumulators to an input of the set of $N_B (N_B+1)/4$ complex conjugate

multipliers, the logic element performing digital beam-forming of the antenna beams using the $N_B \times N_B$ covariance matrix.

12. The apparatus of claim 11 wherein N_B is 7.

13. The apparatus of claim 11, further comprising: 5
an N_B buffer for storing a set of diagonal elements of the covariance matrix;

a scaling logic element for scaling each element in the set of diagonal elements by a constant value;

a comparator for comparing each scaled element with a 10
maximum element of the set of diagonal elements and generating a true or false output corresponding to the result of the comparison; and

an N_B mask buffer for storing the output of the comparator 15
for each element in the set of diagonal elements.

14. The apparatus of claim 13 further comprising a selection device for using the N_B mask buffer to select elements of the covariance matrix.

15. The apparatus of claim 13 wherein the constant value is a variable beam threshold based on an operating environ- 20
ment of the multi-beam antenna.

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