METHOD AND APPARATUS FOR DYNAMIC LEVELING

A method and apparatus for dynamically leveling the attitude of a vehicle (102) using a low power fully active suspension system (100). The system (100) connects the front and rear suspensions (114 and 104) and body (103) of the vehicle (102) and includes a hydraulic damper (110) having a pressure cylinder (144) forming a working chamber (146) in which a piston and rod assembly (148) is movably disposed. The system (100) further comprises a flow control device (130) fluidly communicating with the working chamber (146) on one side of the piston (148) for adding and exhausting damping fluid therefrom to a central pressure source (132), and an accumulator (128) fluidly communicating with the working chamber (146) on the opposite side of the piston (148). The system (100) having flow restriction valving (156) for selectively controlling the flow of fluid with said working chamber (146). The flow restriction valving (156) located between the flow control device (130) and the accumulator (128). The low power fully active suspension system (100) is adapted to produce a desired suspension force output through selective actuation of the flow control device (130) and the flow restriction valving (156) for limiting the duty cycle and power requirements of the central pressure source (132).
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METHOD AND APPARATUS FOR DYNAMIC LEVELING

BACKGROUND OF THE INVENTION

This invention relates to vehicle suspension systems, and more particularly to a method and apparatus for a low power active suspension system for dynamic leveling of a motor vehicle.

In recent years, substantial interest has grown in motor vehicle suspension systems which can offer improved comfort and road holding over the performance offered by conventional passive suspension systems. In general, such improvements are achieved by utilization of an "intelligent" suspension system capable of electronically controlling the suspension forces generated by hydraulic actuators provided at each corner of the motor vehicle.

Suspension systems are provided to filter or "isolate" the vehicle body from vertical road surface irregularities as well as to control body and wheel motion. In addition, it is desirable that the suspension system maintain an average vehicle attitude to promote improved platform stability during maneuvering. The classic passive suspension system includes a spring and a damping device in parallel which are located between the sprung mass (vehicle body) and the unsprung mass (wheel and axles).

Hydraulic actuators, such as shock absorbers and/or struts are used in conjunction with conventional passive suspension systems to absorb unwanted vibration which occurs during driving. To absorb this unwanted vibration, the hydraulic actuators are
automobile. A piston is located within the actuator and is connected to the body of the automobile through a piston rod. Because the piston is able to limit the flow of damping fluid within the working chamber of the actuator when the actuator is telescopically displaced, the actuator is able to produce a damping force which counteracts the vibration which would otherwise be directly transmitted from the suspension to the vehicle body. The greater the degree to which the flow of damping fluid within the working chamber is restricted by the piston, the greater the damping forces which are generated by the actuator.

In selecting the amount of damping that an actuator is to provide, three vehicle performance characteristics are often considered: ride comfort, vehicle handling and road holding ability. Ride comfort is often a function of the spring constant of the main suspension springs of the vehicle, as well as the spring constant of the seat, tires, and the actuator. Vehicle handling is related to the variation in the vehicle's attitude (i.e., roll, pitch and yaw). For optimum vehicle handling, relatively large damping forces are required to avoid excessively rapid variation in the vehicle's attitude during cornering, acceleration, and deceleration. Road holding ability is generally a function of the amount of contact between the tires and the ground. To optimize road holding ability, large damping forces are required when driving on irregular surfaces to prevent
loss of contact between the wheels and the ground for an excessive period of time.

To optimize ride comfort, vehicle handling, and road holding ability, it is generally desirable to have the damping forces generated by the actuator be responsive to the input frequency from the road. When the input frequency from the road is approximately equal to the natural frequency of the body of the automobile (e.g., approximately between 0-2 Hz), it is generally desirable to have the actuator provide large damping forces to avoid excessively rapid variation of the vehicle's attitude during cornering, acceleration and deceleration. When the input frequency from the road is between 2-10 Hz, it is generally desirable to have the actuator provide low damping forces so as to produce a smooth ride and allow the wheels to follow changes in road elevation. When the input frequency from the road is approximately equal to the natural frequency of the automobile suspension (i.e., approximately 10-15 Hz), it may be desirable to have relatively low damping forces to provide a smooth ride, while providing sufficiently high damping forces so as to prevent excessive loss of contact between the wheels and the ground.

To obtain the desired damping characteristics over a wide range of driving conditions, efforts have been made toward the development of continuously variable damper valving. Such variable damper valving is able to adjust or vary the damping characteristics of a hydraulic actuator in response to rapid variations which occur during cornering, acceleration, and deceleration.
Recent advancements in sensor and microprocessor technology have created substantial interest in the application of "active" suspension systems in motor vehicles. An "active" suspension is defined as a suspension system with real time control of body and wheel motion. An actuator or force generator replaces or is added to the conventional passive suspension member. The dynamic behavior of a motor vehicle can be dramatically modified through application of an "active" suspension system.

Referring to Figure 1, a diagrammatical illustration of a simplified control scheme for an active suspension is shown to include a closed loop control system 10 wherein the behavior of vehicle 12 is measured by multiple sensors 14 (i.e. accelerometers, gyroscope, potentiometers). A microprocessor-based controller 16 processes the sensed signals and calculates a demanded suspension force "U" for each actuator 18. Actuators 18 are provided at each corner of the vehicle and are independently controlled. Vehicular Inputs 20, which effect the dynamic behavior of vehicle 12, include disturbances such as road undulations, inertia forces generated during cornering and breaking, and aerodynamic forces. The active suspension is designed to compensate for these disturbances while providing improved ride isolation, improved road handling, reduced pitch and roll angles, control of lateral load transfer between front and rear axles, and control of the vehicle ride height above the road.

In general, active suspension systems are technically complex due to the demand for fast response and accuracy from the
hydraulic system, the actuators and the control system. Heretofore, application of active suspension systems in motor vehicles has been limited due to the excessive cost associated with the complex hardware and controls.

The demanded force signal "U" can be described as a function of state variables describing the vertical motion of vehicle 12 and of the road conditions. Figure 2 illustrates a simplified 1/4 model of vehicle 12 having two degrees of freedom (DOF) which is described by four state space variables. The state variables include body displacement \( (X_b) \), body velocity \( (\dot{X}_b) \), wheel displacement \( (X_w) \) and velocity \( (\dot{X}_w) \). Inputs from road 22 are identified as \( (X_{road}) \). An active suspension actuator 18 is diagrammatically illustrated as suspended between body 24 and wheel 26 relative to road 22 and in parallel with a passive suspension member 28. Control law for the calculation of the demanded force "U" for the single active actuator 26 shown is:

\[
U = -G \cdot X
\]

(1)

where:

\[
U = g_1(\dot{X}_b) + g_2(X_b) + g_3(\dot{X}_w) + g_4(X_w) + g_5(X_{road})
\]

(2)

Gains \( g_1 \) and \( g_3 \) represent inertial damping and \( g_2 \) and \( g_4 \) reflect inertial stiffness for the body and wheel, respectively. Feedback of the road \( g_5 \) is provided to tie wheel 26 to the road 22. Various techniques are known for defining a feedback gain matrix (i.e., Linear Quadratic Gaussian) to best fulfill specific design objectives associated with dynamically controlling the behavior of vehicle 12.
In general, active suspension systems can be divided into three basic classes; "semi-active", "low power" active, and "fully" active. A primary difference between each of the aforementioned active suspension classes relates to the hardware requirements to be hereinafter described. In general, "low power" active and "fully" active suspension systems each use a central hydraulic system to power each suspension actuator. "Semi-active" systems, however, only have the ability to dissipate power by varying the damped resistance to motion.

Semi-active damping systems are based on continuous, real time modulation of damping rates, separately in compression and extension. Semi-active control strategy is based on the principle that a suspension actuator is only capable of dissipating power. Referring to FIGS. 3 and 4, an actuator 32 for a semi-active suspension system is illustrated. In practical terms, semi-active actuator 32 is equipped with infinitely variable damper valving 34. A self-contained source of damping fluid is confined within working chambers 36 and 38 provided on opposite sides of piston 40. Compared to a conventional passive damper, semi-active actuator 32 can dissipate power to provide a demanded force "U". However, the control strategy for semi-active suspension systems must be simplified from that of equation (2) to include only velocity of the vehicle body ($\dot{X}_b$) and the relative suspension velocity ($\dot{X}_u - \dot{X}_b$).

For power dissipation:

$$U = g_1(\dot{X}_b) + g_2(\dot{X}_u - \dot{X}_b) \quad \text{ (Quadrants I and III)}$$  \hspace{1cm} (3)
For power demand:

\[ U = 0 \quad \text{(Quadrants II and IV)} \]  

In "ideal" semi-active systems, the demanded force "U" is set to zero \((U = 0)\) if the relative velocity \((\dot{X}_a - \dot{X}_b)\) is of the opposite sign and/or the demanded force "U" is out of "reach" for actuator 32. These conditions are reflected as Quadrants II and IV of the Force "U" versus relative velocity \((\dot{X}_a - \dot{X}_b)\) graph of Figure 4. Therefore, as is readily apparent, semi-active systems are capable of dissipating power (Quadrant I and III) but are not capable of generating all demanded force requirements (i.e. Quadrant II and IV) associated with dynamically controlling vehicle behavior.

Modernly, "low power" active systems have heretobefore been used almost exclusively on race cars. Unfortunately, the frequency response of low power active systems is restricted to a undesirably narrow frequency range \((0-5 \text{ Hz})\) as well as a significantly lower power output than required for "fully" active systems. Figure 5 schematically illustrates a single-acting hydro-pneumatic actuator 42 applicable for low power active suspension systems. Because of the low frequency response of actuator 42, the control strategy of Equation (2) is limited to a narrower frequency range which necessitates exclusion of high frequency control of the wheel. Therefore the control equation is defined as:

\[ U = g_1(X_b) + g_2(X_b) \]  

\(5\)
Low power systems have a central pump 50 supplying high pressure to each corner actuator 42. Hydro-pneumatic actuator 42 communicates with an accumulator 44 through a fixed flow damper valve 46 for damping the suspension motion. A servo valve 48 is either supplying actuator 42 with high pressure fluid provided from a central pump 50 or emptying actuator 42 of fluid which is then returned to a central reservoir 52. The suspension stiffness is supplied by a passive spring member (not shown) and the pressure in accumulator 44. In low power active systems, hydraulic damping fluid is selectively controlled to flow between central reservoir 52 and actuator 42 in response to changes in the vehicle's attitude.

"Fully" active suspension systems are designed to control both wheel and body motion over the entire frequency range (approximately 0 - 30Hz). A "fully" active suspension actuator 60 is schematically illustrated in Figure 6. Specifically, the central hydraulic system (i.e., pump 50 and reservoir tank 52) is basically the same as the one used for the low power active but designed to provide higher flow rates for increased peak power consumption. Actuator 60 is basically a double-acting hydraulic device having an upper working chamber 62 and a lower working chamber 64 defined by opposite sides of piston 66. A four port servo valve 68 connects each working chamber 62 and 64 to the high supply pressure source (pump 50) or back to central reservoir 52. The controlling formula, that is, equation (2) can be used to its full merits to include control of both vehicle body and wheel motion.
However, the current costs associated with "fully" active suspension systems are extremely high, primarily because of the fast frequency response requirements of servo valve 68 and the high peak flow rates associated with the central hydraulic system. Actuator 60 is not equipped with damper valving through piston 66 whereby system power requirements are extremely high to generate movement of the piston and rod directly from the pressure difference generated across piston 66. Therefore, high system pressure requirements, large peak power and peak fluid flow requirements are associated with conventional "fully" active suspension systems. Furthermore, the duty cycle of such a "fully" active suspension system is almost continuous due to constant modulated actuation of servo valve 68 to control fluid flow to and from actuator 60. Accordingly, there is a need to reduce the complexity, size of the components, system cost, peak system working pressure, and peak power requirements, while effectively generating superior operational durability characteristics.

It is to be understood that the terms "height", "distance", "attitude", and derivatives thereof are used interchangeable herein as well as throughout the automotive art, as referring to the magnitude of spacing between a vehicle's sprung and unsprung portions (e.g., between a vehicle frame and its associated axles or independent wheels).
SUMMARY OF THE INVENTION

Accordingly, it is a primary object of the present invention to provide a method and apparatus for dynamic leveling of a motor vehicle which overcomes the disadvantages of the various active suspension systems herebefore described, and which is fully active yet has relatively low power consumption and low peak flow requirements.

Another object of the present invention is to provide a method and apparatus for dynamic leveling which is operable to change the attitude of a vehicle through a controlled adjustment of the suspension damping force so as to compensate for vehicle body height variation.

Another object of the present invention is to provide a method and apparatus for dynamic leveling which generates improved reaction time while reducing system working pressure parameters and peak power and flow requirements.

A further object of the present invention to provide a method and apparatus in which a continuously variable flow restriction is used to dissipate power for limiting the duty cycle of the dynamic leveling suspension system.

Yet another object of the present invention is to provide a method and apparatus for dynamic leveling which independently adjusts the vehicle height for each corner by selectively controlling the fluid pressure and flow between the upper and lower portions of a working chamber of the hydraulic actuator.

A further object of the present invention is to provide an improved active suspension control scheme. The control scheme
includes a "dynamic leveling" loop and a "load leveling" loop. The "dynamic leveling" loop is divided into signal processing and vehicle controller circuits. Outputs from the vehicle's sensors are received by the signal processing circuit for estimating the state variables which are not measured directly. The estimated state variables are delivered to the full state feedback vehicle controller for multiplication with the feedback gain matrix to generate a demanded force signal for each of the actuators.

It is a further object of the present invention to accurately define the dynamic behavior characteristics of the vehicle and suspension by applying a method of estimating the state variables which are not measured directly. As such, the sensor configuration associated with the present invention is commercially feasible and relatively inexpensive.

It is another object of the present invention to provide a frequency dependent adaptive gain circuit for automatically tuning the vehicle controller circuit. Adaptive gain regulation is a continual process of identifying and modifying the feedback gain matrix of the vehicle controller for actively suspending the vehicle at relatively low frequency road inputs and passively at wheel hop frequencies. The adaptive circuit is simple in structure for convenient implementation to the full feedback regulation of the active control scheme.

It is yet a further object of the present invention to provide an actuator control strategy for driving each of the corner actuators of the low power dynamic leveling suspension system of the present invention.
It is another object of the present invention to provide a method and apparatus for dynamic level which has a high degree of flexibility with respect to installation on different vehicle models. In this regard, a related object of the present invention is to provide a method and apparatus for dynamic leveling which is relatively low in cost as compared to other active suspension systems known in the art.

**BRIEF DESCRIPTION OF THE DRAWINGS**

Various advantages of the present invention will become apparent to one skilled in the art upon reading the following specification and by reference to the following drawings in which:

Figure 1 diagrammatically illustrates a simplified control system for active suspension systems;

Figure 2 is a schematic representation of a 1/4 vehicle model for an active suspension system and the control law associated therewith;

Figure 3 is a schematic representation of an actuator for a "semi-active" suspension system;

Figure 4 is a graphical illustration of the range of the demanded suspension forces "U" which can be generated by the semi-active actuator of Figure 3;

Figure 5 is a schematic representation of a "low power" active suspension actuator and hydraulic system;

Figure 6 is a schematic illustration of a "fully" active suspension actuator and hydraulic system;
Figure 7A illustrates a dynamic leveling suspension system according to the teachings of the present invention shown in operative association with a typical motor vehicle;

Figure 7B is a schematic representation of the dynamic leveling and hydraulic systems of the present invention;

Figure 8 is a schematic representation of a single dynamic leveling actuator and its associated hydraulic system components according to a first embodiment of the present invention;

Figures 9 through 13 are schematic representations of dynamic leveling systems according to alternative embodiments of the present invention;

Figure 14 is a schematic of a simplified vehicle model with the state variables for identifying the dynamic behavior of a vehicle;

Figure 15 is a block diagram of a vehicle control system in accordance with the teachings of the present invention;

Figure 16 is a block diagram illustrating the signal processing and vehicle controller circuits of the "dynamic leveling" control loop of Figure 15;

Figure 17 illustrates a representative gain matrix "G" for the "dynamic leveling" control loop;

Figure 18 is a plot of the pole placement in the S-plane for exemplary body and wheel damping performance goals;

Figure 19 is a plot of the pole placement for the feedback gain regulation system of the present invention;

Figure 20 is a block diagram illustrating a derivating circuit for estimating suspension velocity;
Figure 21 graphically illustrates the frequency response of the derivating filters of Figure 20;

Figure 22 is a comparison of the estimated and ideal time response for suspension velocity;

Figure 23 is a block diagram of the circuit for estimating roll rate and angle from roll acceleration;

Figure 24 illustrates the frequency response of the integrating filter circuit of Figure 23;

Figure 25 is a block diagram of the adaptive control circuit of the present invention;

Figure 26 graphically illustrates the effect of the gain adaptation circuit on pole placement;

Figure 27 is a block diagram of a circuit for calculating the gain weighting coefficient;

Figure 28 is an exemplary plot of road profile versus time;

Figure 29 is a plot of suspension velocity from Figure 28;

Figure 30 is a plot of the gain weighting coefficient (C) generated from the suspension velocity of Figure 29;

Figure 31 is a block diagram of an actuator control system according to the present invention;

Figure 32 is a graphical illustration of demanded force "U" versus relative flow $Q_{rel}$;

Figure 33 is another plot of demanded force "U" versus the relative flow $Q_{rel}$;

Figure 34 is a block diagram of a control system for the actuator controller of the present invention;
Figure 35 is a graphical illustration of the power identification function of the actuator controller;

Figure 36 is a block diagram of the control structure for the servo valves;

Figure 37 is a plot of piston force versus relative flow;

Figure 38 illustrates an exemplary duty cycle for selective actuation of the servo valve;

Figure 39 is a block diagram of the control circuit for the continuously variable damper valve; and

Figure 40 is a graphical illustration plotting piston force versus relative flow for various road input frequencies.

DESCRIPTION OF THE PREFERRED EMBODIMENT

The excessively high power consumption and peak flow requirements associated with the "fully" active suspension system described in reference to Figure 6 predicated the development of a lower power "fully" active suspension system adapted for application over the entire frequency range (0-30 Hz). The present invention relates to such a "dynamic or fast leveling" suspension system. In particular, the present invention is a dynamic leveling system which includes an actuator provided at each corner of the vehicle having continuously variable damping regulation and static load leveling capability. The improved active suspension system of the present invention is constructed as a "fully" active suspension which only requires the addition of external energy to compensate for vehicle body motion. By leaving the wheels passively controlled, the required frequency
of external energy to compensate for vehicle body motion. By leaving the wheels passively controlled, the required frequency response of the system hardware is substantially reduced. The system actuators, to be hereinafter described in greater detail, are a combination of a continuously variable damper and a fast acting hydraulic leveling actuator.

System Hardware

Referring to Figures 7A and 7B, a dynamic leveling system 100 in accordance with the present invention is shown. The dynamic leveling system 100 is depicted in operative association with a conventional automobile 102 having vehicle body 103. Automobile 102 includes a rear suspension 104 having a transversely extending rear axle assembly 106 adapted to support rear wheels 108. Rear axle assembly 106 is operably connected to automobile 102 by means of a pair of hydraulic actuators 110 as well as by helical coil springs 112. Similarly, automobile 102 has a front suspension system 114 including a transversely extending front axle assembly 116 adapted to support front wheels 118. Front axle assembly 116 is connected to automobile 102 by means of a second pair of hydraulic actuators 110 and by a second pair of helical coil springs 120. While automobile 102 has been depicted as a passenger car, the dynamic leveling system 100 may be used with other types of motor vehicles as well. Furthermore, the structural association of the front and rear axle assemblies are exemplary in nature and are not intended to limit the scope of the present invention.
For controlling the damping and leveling characteristics of hydraulic actuators 110, a central electronic control module (ECM) 124 is provided. A visual screen 122 may be located within passenger compartment 126 of automobile 102. Visual screen 122 provides the occupant with a visual readout display of the dynamic control parameters and characteristics of suspension system 100. Electronic control module 124 receives output from various sensors for generating control signals for selectively controlling the damping (dissipative) and dynamic leveling (power addition) characteristics of hydraulic actuators 110. In fluid communication with each actuator 110 is an accumulator 128 and a supply valve such as servo flow control valve 130. Servo valves 130 are in fluid communication with a closed-loop centralized high pressure hydraulic system 132, (schematically shown in Figure 7A), which includes a pump 138, central accumulator 136, and reservoir tank 140.

The electronics associated with dynamic leveling system 100 preferably include a central control module (not shown) interfaced with ECM 124, position sensors 134, accelerometer 135, and driving circuitry for controlling actuators 110 and servo values 130. The closed-loop hydraulic system 132 includes central pump 138 and accumulator 136 for generating a high supply pressure to each actuator 110, reservoir tank 140, and the various high pressure supply lines 139 and low pressure return lines 141 interconnecting the components. The supply of high supply pressure fluid to each actuator 110 is controlled by energization of its respective servo valve 130 which, preferably,
is located in close proximity thereto. While supply valve 130 is illustrated as a servo valve, it is to be understood that other suitable direct acting valves are within the fair scope of the present invention.

As will be detailed hereinafter, dynamic leveling system 100 employs a central control strategy having a state space variable format for full feedback gain regulation, state variable estimating means and adaptive gain control. In general, the feedback gain regulation is specified by performance goals defining stiffness and damping for different modes of dynamic motion. To minimize the number of transducers required, the variable estimating means calculates estimated values from the transducer signals actually measured. The adaptive scheme changes some of the damping gain values when road conditions interfere with the natural frequency of the wheel. Furthermore, by sensing the dynamic behavior of the body and suspension, the microprocessor-based controller calculates the demanded force "U" for each actuator. In order to compensate for non-linearities of the actuator hardware, the actual force generated by each actuator "F_{actuator}" is measured and fed back to the central control system. Preferably, actuator 110 is capable of dissipating power through use of continuously variable piston valving to limit the demanded power requirements associated with actuation of servo valves 130. Therefore, by using the internal continuously variable piston valve for all dissipated power demands, the total power consumption and, therefore, the duty cycle of system 100 is substantially minimized.
With particular reference to Figure 8, a schematic representation of dynamic leveling system 100 according to a first embodiment is shown. While only one actuator 110 is illustrated, it is to be understood that an actuator and its corresponding accumulator 128 and servo valve 130 are located at each corner of vehicle 102. Hydro-pneumatic actuator 110 is a single-acting device comprising an elongated tubular pressure cylinder 144 having a working chamber 146 which is adapted to store hydraulic damping fluid. Disposed within working chamber 146 is a reciprocable piston 148 that is secured to one end of an axially extending piston rod 150 so as to define an upper portion 152 and a lower portion 154 of working chamber 146. As illustrated in reference to Figure 7, actuators 110 are connected between the sprung and unsprung masses of vehicle 102. Those skilled in the art will appreciate that, upon reciprocal movement of piston 148, damping fluid within pressure cylinder 144 is transferred between upper portion 152 and lower portion 154 of working chamber 146 through piston damper valving. By selectively controlling the flow of damping fluid between upper and lower portions of working chamber 146, hydro-pneumatic actuators 110 are able to controllably dampen relative movement between the sprung and unsprung portions of automobile 102 so as to optimize both ride comfort and road handling ability.

To provide means for controlling the flow of damping fluid between upper portion 152 and lower portion 154 of working chamber 146, piston 148 includes continuously variable flow restriction valving 156. The variable flow restriction piston
valve 156 is actuated to selectively meter the flow of damping fluid between upper portion 152 and lower portion 154 for modulating the damping characteristic of actuator 110 through the dissipation of energy. One such continuously variable flow restriction valve and its corresponding electronic control system and hardware is disclosed in PCT International Publication, Serial No. WO 88/06983, filed September 22, 1988 having a common assignee with the instant application and which is explicitly incorporated by reference hereto. It is contemplated, however, that the present invention may be used with other suitable variable flow restricting valving arrangements adapted for selectively controlling the damping characteristic of actuator 110.

To provide means for changing the fluid pressure in at least one portion of working chamber 146, flow control means is provided. The flow control means comprise electrohydraulic proportional/servo flow control valves 130 which are illustrated as being fluidly connected to lower portion 154 of working chamber 146. In general, servo valve 130 is either supplying actuator 110 with high pressure fluid or emptying actuator 110 of fluid which is then returned to reservoir 140. The actual force \( F_{\text{actuator}} \) generated by each actuator 110 is dependent on the pressure in accumulator 128 and the pressure drop across piston 148. More specifically, servo flow control valve 130 is actuated to selectively control the flow between direct acting pump 138 and lower portion 154 of working chamber 146. Likewise, servo flow control valve 130 is also able to control the flow of
damping fluid from lower portion 154 of the working chamber 146 to fluid reservoir 140. Preferably, an actuator controller circuit to be described hereinafter, controls the selective actuation of piston valving 156 and servo valve 130.

According to the first embodiment shown, accumulator 128 is connected to upper portion 152 of working chamber 146 so as to maintain a pressure differential in upper portion 152 across piston 148 during actuation of servo flow control valve 130. Because piston 148 includes variable flow restriction valving 156 in conjunction with servo flow control means 130, dynamic leveling system 100 is able to operate with relatively low use of pump 138 when compared to the conventional fully active suspension systems of Figure 6. This is accomplished since variable flow restriction valving 156 is used for generating the commanded force "U" when it is within the flow limits of valve 156 thereby minimizing the power requirements of central hydraulic system 136.

Referring now to FIGS. 9 through 13, alternative structural configurations of the present invention are disclosed. In general, each embodiment is adapted to provide a continuously variable flow restriction between servo flow control valve 130 and accumulator 128. More preferably, the embodiments illustrate use of variable flow restriction valve 156 within cylinder 144. For the sake of clarity, like reference numerals are used hereinafter for like components.

With specific reference now to Figure 9, a dynamic leveling system 100(B) is similar to dynamic leveling system 100 shown in
Figure 8. However, damping fluid is able to flow between central hydraulic system 136 and lower portion 154 of working chamber 146 through an axial passage 160 extending through piston rod 148.

The dynamic leveling system 100(C) shown in Figure 10 is similar to dynamic leveling system 100 of Figure 8, with the exception that damping fluid is able to flow between upper portion 152 of working chamber 146 and accumulator 128 through axial passage 162 extending through piston rod 148. Flow passage 162 extends from the upper portion of hollow piston rod 148 to upper portion 152 of working chamber 146. Preferably, accumulator 128 can be mounted directly to an axial end of piston rod 148 or in close proximity thereto.

The dynamic leveling system 100(D) shown in Figure 11 is similar to dynamic leveling system 100 shown in Figure 8 except that the orientation of piston rod 150 with respect to piston 148 has been inverted so that piston rod 150 extends from a lower portion of tubular cylinder housing 144.

The dynamic leveling system 100(E) shown in Figure 12 is similar to dynamic leveling system 100(D) shown in Figure 11 with the exception that accumulator 128 is disposed on, and in direct fluid communication with, an upper axial end of hydraulic actuator 110. This embodiment represents the application of an actuator having an accumulator secured as an integral extension thereof. In this manner, high pressure lines can be readily eliminated.

The dynamic leveling system 100(F) shown in Figure 13 is similar to the dynamic leveling system 100(E) shown in Figure 12.
However, accumulator 128 is disposed within upper portion 152 of working chamber 146 inside of tubular housing 144.

The various alternative embodiments disclosed illustrate the flexibility and applicability of the present invention to modern automotive suspension rattle space and layout requirements. Furthermore, it is to be understood that accumulator 128 can be remotely located from actuator 110 for packaging reasons, but preferably, is provided in close proximity to actuators 110. Similarly, it is preferable that each servo valve 130, or suitable supply valve, be located as near as practical to its corresponding actuators 110. The closed loop central hydraulic system 132 illustrates that pump 138, central accumulator 136 and reservoir 140 are fluidly connected to each servo valve 130.

Preferably, all of the dynamic leveling systems of the present invention include a sensor configuration which is practical in light of present technology. More preferably, the sensor configuration is adapted to directly measure heave, pitch, and roll acceleration of the vehicle body as well as the relative displacement between the wheel and the vehicle body at each corner of the vehicle. The dynamic movement of a motor vehicle can be adequately described by a seven degree of freedom (DOF) model which defines the heave, pitch and roll motion of the vehicle body and the vertical motion for each of the four wheels. More particularly, the vehicle's dynamic behavior is described by fourteen (14) state variables associated with the model.
location of the poles is given by the performance requirements of the vehicle. Figure 14 is a simplified vehicle model illustrating the fourteen (14) state variables associated with identifying the dynamic behavior of vehicle 102.

The first seven state variables are velocities and the final seven state variables are displacements:

<table>
<thead>
<tr>
<th>VELOCITY</th>
<th>DISPLACEMENT</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x_1 = \ddot{z}$, heave velocity of C. G.</td>
<td>$x_8 = z$, heave displacement</td>
</tr>
<tr>
<td>$x_2 = \dot{\theta}$, Pitch angular velocity</td>
<td>$x_9 = \theta$, Pitch angle</td>
</tr>
<tr>
<td>$x_3 = \dot{\phi}$, Roll angular velocity</td>
<td>$x_{10} = \phi$, Roll angle</td>
</tr>
<tr>
<td>$x_4 = \dot{X}_L$, Left Front suspension vel.</td>
<td>$x_{11} = LF$ suspension displ.</td>
</tr>
<tr>
<td>$x_5 = \dot{X}_F$, Right Front suspension vel.</td>
<td>$x_{12} = RF$ suspension displ.</td>
</tr>
<tr>
<td>$x_6 = \dot{X}_R$, Right Rear suspension vel.</td>
<td>$x_{13} = RR$ suspension displ.</td>
</tr>
<tr>
<td>$x_7 = \dot{X}_L$, Left Rear suspension vel.</td>
<td>$x_{14} = LR$ suspension displ.</td>
</tr>
</tbody>
</table>

In reference again to Figure 7, relative position sensors 134 are located between the unsprung and sprung masses for measuring the relative displacement at each corner. A tri-axial accelerometer 135, located in the close proximity to the vehicle's center of gravity, directly measures heave, pitch and roll acceleration. However, it is contemplated that individual accelerometers can be used which are located at each corner of the vehicle.

In addition to the input sensors, a force transducer (not shown) is provided at each corner to measure the actual output force $F_{\text{actuator}}$ generated by each actuator which is fed back to the actuator controller to verify that $F_{\text{actuator}}$ is closely tracking the commanded force $U$. However, it is contemplated that the force transducers can be readily substituted with absolute pressure sensors for measuring the actuator pressure across the variable damping restriction. The force transducer or the
pressure sensors are preferably located within damper valve 156 as disclosed in the PCT application herebefore incorporated by reference. As will be described hereinafter in greater detail, the signals from sensors 134 and 135 are amplified and fed into the D/A convertor of a microprocessor. Exemplary non-limiting sampling times for the relative displacement and the accelerations are approximately in the range of about 100 to 500 Hz and the sampling time for the force transducers is in the range of about 1,000 to 2,000 Hz.

**System Control Structure**

Referring to Figure 15, a simplified vehicle control system 200 is illustrated for the present invention. Preferably, the control system 200 is interfaced with the electronic control module 124 of vehicle 102. In general, control system 200 includes an inner closed loop 202 and an outer closed loop 204, each closing around vehicle 102. Outer loop 204 is referred to as the "load leveling" control circuit which compensates only for the vehicle's ride height relative to a vertical plane upon different static loading conditions. Inner loop 202, referred to as the "dynamic leveling" control circuit provides improvements in the isolation of the vehicle from the road, body platform stability, and in the maintenance of improved road holding capability. Preferably, control system 200, which will be described hereinafter in greater detail, is structured as a full state feedback regulation system with feedback gain values representative of specified vehicle performance criteria.
Each of the four corner actuators 110 is commanded by control system 200 to generate the four distinct suspension forces "U". Preferably, sensors, schematically identified herein as numeral 206 in Figure 16, directly measure the seven (7) sensed signals. Sensors 206 also represents the corresponding amplification and filtering required for sampling of the measured signals by the microprocessor. Outer loop 204 is adapted so as not to affect inner loop 202 since the time delay of "load leveling" outer loop 204 is extremely large when vehicle 102 is in operation. However, when vehicle 102 is stopped, quicker response time is contemplated for vehicle attitude height compensation through the "load leveling" circuit.

Figure 16 is a diagrammatical illustration of inner loop 202 which includes signal processor 208 and vehicle controller 210. Signal processor 208 estimates the remaining state variables based on input of the directly measured sensor signals. Vehicle controller 210 includes a feedback gain regulation format for using the feedback gain for each state variable to calculate the desired dynamic behavior. The output $U_{\text{dyn}}$ is a vector of a component of the four demanded "U" forces for the actuators 110.

In particular, heave acceleration ($\ddot{z}$), pitch acceleration ($\ddot{\theta}$) and roll acceleration ($\ddot{\phi}$) are directly measured by tri-axial accelerometer 135 and suspension displacements $x_1$ through $x_4$ are measured directly by the position sensors 134. From these seven (7) actual measurements, signal processor 208 estimates ten (10) state variables. As is apparent, the dynamic behavior of vehicle 102 is described through a seven degree of freedom (DOF) model.
with the state space variable selected such that feedback gains can be defined as additional stiffness and damping acting on the vehicle.

The differential equations for the "dynamic leveling" control system are written in the following standard form:

\[
\dot{X} = A \cdot X + B_1 \cdot U_{dyn} + B_2 \cdot E \tag{6}
\]

where:
- \( X \) is the vector of the 14 state variables
- \( U_{dyn} \) is the vector of the four control forces
- \( E \) is the vector of \( m \) disturbances
- \( A \) is the 14x14 vehicle system matrix
- \( B_1 \) is the feed back input matrix 14x4
- \( B_2 \) is the disturbance matrix 14x\( m \)

The outputs are defined as:

\[ y = C \cdot X \tag{7} \]

where:
- \( y \) is the vector of \( n \) outputs
- \( C \) is the \( nx14 \) output matrix

The "commanded" force for each actuator is:

\[ U_{dyn} = -G \cdot X \tag{8} \]

where:
- \( U_{dyn} \) is the vector of the four actuator forces
- \( X \) is the vector of the 14 state variables
- \( G \) is the 4x14 feedback gain matrix

\( U_{dyn} \) can be replaced by \((-G \cdot X)\) in equation (6). Therefore, the closed-loop control system equation can be rewritten to:

\[ \dot{X} = (A - B_1 \cdot G) \cdot X + B_2 \cdot E \tag{9} \]

The poles of the closed loop are determined by the eigenvalues of the matrix \( A_{active} = (A - B_1 \cdot G) \). The purpose is to assign magnitudes to the feedback matrix so that all poles assume prescribed values.
Vehicle Performance Goals

The feedback gain values of the "dynamic leveling" control scheme 202 are specified to give vehicle 102 a very stable platform and a good ride performance. Preferably, this is achieved through utilization of low rate passive support springs and the addition of active roll stiffness and body damping. Body damping is the damping of the three modes of motion: heave, pitch and roll. The body damping is set at a percentage of the critical damping for each mode for quickly stabilizing vehicle 102 after a road disturbance. Preferably, body damping is selected to be about 0.71 of the critical damping for each mode.

To meet various road conditions, wheel damping of the vehicle is selected for two distinct cases of vehicle performance, the first where the wheels are relatively softly damped and the second where the wheels are relatively firmly damped. The vehicle body should be damped to the same degree in both cases. For example, the soft wheel damping is set at 0.1 of the unsprung mass critical damping with the objective to give a smooth ride. The firm wheel damping is set at 0.5, with the objective to improve road holding and to minimize the relative displacement.

The vehicle 102 is designed to behave as a regular passive vehicle but with improved performance and body isolation. A non-limiting example of a set of predetermined vehicle performance requirements can be summarized in eight statements:

a: Natural frequency in the front (passive) 0.9 Hz
b: Natural frequency in the rear (passive) 1.0 Hz
c: Heave and pitch uncoupled in C.G

d: Roll stiffness at max. 0.8g [m/s²] 4°/g
e: Front to rear roll stiffness ratio
f: Unsprung mass damped for soft Ewheel
g: Unsprung mass damped for firm Ewheel
h: Damping for body modes of motions

Feedback Gain Regulation

The feedback gains are specified by the vehicle performance in terms of stiffness and damping. "Active" stiffness is added to the vehicle body to satisfy the roll stiffness and to decouple the heave and pitch motion. "Active" damping, including body and wheel damping, is added to satisfy the requirement of damping the body (0.71) and the wheels (0.1 and 0.5) at the preferred predetermined percentage of their critical damping. Since wheel motion is coupled to the body, computing the eigenvalues for the closed loop matrix $A_{active}$ verifies the correct amount of damping.

Referring to Figure 17, the format for a representative gain matrix "G" is shown as a 4 by 14 matrix wherein each row represents the gain values for one actuator. Columns 1 - 7 represent the active "damping" and columns 8 - 14 the active "stiffness". Two distinct gain matrixes ($G_{soft}$ and $G_{firm}$) are developed to satisfy the desired performance requirements (a through h) and which includes gains corresponding to lower and upper limits of variable piston valve 156 in actuator 110.

Figure 18 shows the location of the poles in the S-plane for the vehicle. The real axis represents the corresponding damping $Ew_o$ where $E$ is the relative damping and $w_o$ the undamped natural frequency. The imaginary axis represent the damped natural frequency $w_n$ defined as $w_o\sqrt{1-E^2}$. A relative damping of 0.71 locates the poles along a line with the inclination of 45° to the
negative real axis. A relative damping of 0.1 is represented by an 84° inclination and relative 0.5 is reflected as a 60° inclination. The active feedback control system locates the poles of the vehicle body along the 0.7 line and the poles for the wheels along the 0.1 and 0.5 lines.

An adaptive strategy, to be described hereinafter, continuously modifies the gain values of each matrix upon changes in road conditions.

Vehicle Pole Placement

The poles are the eigenvalues of the characteristic equation for the dynamic leveling system. The vehicle poles present information on the natural frequency and damping for each mode of motion. The pole placement of the closed loop system verifies whether the feedback gain matrix generates satisfactory results. The characteristic equation is derived by solving the determinant:

$$\text{Det}(sI - (A - B_1 \cdot G)) = 0$$  \hspace{1cm} (10)

For a system with 14 state variables there are 14 eigenvalues that satisfy equation (10). When, as in this case, the system is underdamped, the eigenvalues are in pairs with a positive and a negative imaginary root.

The eigenvalues for three exemplary cases are shown in Figure 19. The first case is based on a passive vehicle with the two remaining cases based on feedback gains $G_{soft}$ and $G_{firm}$. The passive vehicle would have a passive damper, giving the unsprung mass a relative damping of about $E_{wheel}=0.3$, and a roll bar
representing the same roll stiffness as in both the active cases. The poles of the wheels are on the same radius from the origin for both active cases because of a difference in damping but not in stiffness.

The full state feedback regulation method of the present invention has a well-defined structure, which simplifies the understanding of control system 200. Since the gain varies are specified in terms of stiffness and damping, communication between the vehicle ride specialist and the controls engineer is made easier.

**Estimation of State Variables**

The "dynamic leveling" control loop 202 is divided into signal processing circuit 208 and vehicle controller 210. Analog signals from sensors 206 are filtered and sampled in signal processor 208. Observer 209 estimates the state variables and vehicle controller 210 multiplies the state variable vector $X_n$ with the gain matrix "G" to generate the "$U_{\text{dyn}}" output signal.

In practical terms, the choice of sensor configuration is limited by the cost of each transducer and the quantity used. The goal is to describe all the state variables of the vehicle's motion with a sensor configuration which reliably uses a minimal number of relatively inexpensive transducers.

Efforts to directly measure all the state variables is extremely unrealistic. Therefore, signal processing of the sensed signals for estimating a number of the state variables is advantageous. Such a process is provided by "observer" 209. In
the preferred microprocessor-based control system 200, signal processor 208 includes anti-aliasing filters and noise filtering. Anti-aliasing filters ensure that the highest frequency input seen by the A/D signal converter is at least about one-half the sampling frequency. The noise filtering eliminates undesirable information and can be either analog or digital.

As previously noted, the directly measured signals are heave $\ddot{z}$, pitch $\dot{\theta}$ and roll $\hat{\phi}$ body accelerations plus the relative displacements $x_{i1}$ through $x_{i4}$ for each suspension corner. The three modes of body acceleration can be measured simultaneously with tri-axial accelerometer 135 located at the center of gravity or, alternatively, with four accelerometers located at each corner of the vehicle body for measuring the vertical acceleration. Regardless, the accelerometer is capable of measuring acceleration at very low frequencies.

For position sensors 134, the vehicle's static height is defined as zero output, compression is defined as positive and extension is negative. The vehicle static height is maintained by the slower load leveling control loop 204. A preferred location of position sensor 134, from an environmental standpoint, would be inside actuator 110 itself. In addition to sensing the vehicle motion, it is also necessary to measure the force $F_{\text{actuator}}$ generated by each actuator. Preferably, the actuator force is feedback to the actuator control circuit to compensate for nonlinearities of actuator 110 itself.

Given the preferred sensor configuration, observer 208 estimates ten state variables ($x_1$ to $x_{10}$). The method of
estimation employs signal filtering techniques, which can be
classified into three distinct categories:

I. Derivation of suspension relative displacement \(x_{11}
through x_{14}\) to suspension velocity \(\hat{x}_4\)
through \(\hat{x}_7\);

II. Integration of body accelerations (\(\ddot{z}, \ddot{\theta},
\ddot{\phi}\)) to body velocity and angular rates
(\(\dot{x}_1, \dot{x}_2, \dot{x}_3\)); and

III. Integration of body velocity and angular rates
(\(\dot{x}_1, \dot{x}_2, \dot{x}_3\)) to body displacement and angles
(\(x_8, x_9, x_{10}\)).

The four suspension velocities (\(\dot{x}_4\) through \(\dot{x}_7\)) are estimated
by derivation of the suspension displacement (\(x_{11}\) through \(x_{14}\)).
Referring to Figure 20, the derivation is performed by a first
order high-pass filter 220 scaled to act as a "derivator" at
relatively low frequencies. Filter 220 should neither show any
major phase delay nor attenuation of the real velocity up to a
frequency of at least about 25 Hz. Disturbances at higher
frequencies are absorbed by the tire and the suspension bushings.

The analog to digital transfer function is:

\[
G(s) = \frac{s}{(T_d s + 1)} \quad H(z) = \frac{0.5(1 - z^{-1})/\Delta T}{(1 - 0.5z^{-1})}
\]

\(T_d = 0.004\)

\(f_s = 512\) Hz, \(\Delta T = 1/f_s\)

With the time constant \(T_d\) set at 4 msec., filter 220 rolls
off at around 40 Hz to a constant amplification. Using bilinear
transformation, the digital equivalent has a simplified form for
fast computation by the microprocessor. An exemplary sampling
time for digital filter 220 is about 512 Hz with the cut-off
frequency for the anti-aliasing filter (not shown) at about 250
Hz. The frequency response for filter 220 is shown in Figure 21.
As is apparent, filter 220 closely follows the "ideal" derivation curve "w" up to the desired high system frequency level of up to at least about 25 Hz.

As seen from the exemplary plot of Figure 22, an acceptable time delay of only about 3 msec. in the time response exists between the "ideal" and the estimated suspension velocity at the given sampling time.

Integration is sensitive to drift because of low frequency or steady state errors. An exemplary non-limiting integration control circuit for integrating roll acceleration \( \dot{\hat{x}_3} \) to roll rate \( \hat{x}_3 \) and roll angle \( \hat{x}_{10} \) is shown in Figure 23. The first integration is performed by a filter 222 having a constant or high-pass characteristics for low frequencies. Above a certain predetermined design point, the frequency response of filter 222 follows the "ideal" slope of an integrator. (See Figure 24).

The body velocities for heave \( \dot{\hat{x}}_1 \), pitch \( \dot{\hat{x}}_2 \) and roll \( \dot{\hat{x}}_3 \) are estimated by "integrating" their corresponding acceleration \( \ddot{z} \), \( \ddot{\theta} \), \( \ddot{\phi} \) respectively. Since the velocity estimates represent the inertial damping of the vehicle body, the integration has to be highly accurate within the relatively low natural frequency range associated with body motion (i.e. 0.5 to 5 Hz).

The analog and digital transfer functions for filter 22 are:

\[
G(s) = \frac{1}{(s + 1/T_1)} \quad H(z) = \frac{0.5(1 + z^{-1})/\Delta T}{(1 - a_1 z^{-1})} \tag{12}
\]

\[
T_1 = 2.0 \quad \Delta t = 128 \text{ Hz} \quad \Delta T = 1/f_t \quad a_1 = 1 - \Delta T/T_1
\]

Filter 222 is a low-pass filter scaled within the operating range above its cut off frequency. The time constant \( (T_1) \) is set
to about 2.0 sec. which permits filter 222 to behave substantially as an "ideal" integrator within the specified frequency range. In order to "zero out" accelerometer 135 from its static offset, the input signal is high-pass filtered through a digital filter 223 having a relatively long time constant. Figure 24 shows the effects of integrating filter 222 including high-pass filter 223 with a time constant of 10 sec. The "ideal" integration has a transfer function with the magnitude of 1/w and is included for comparison.

An improvement in the body velocity estimation scheme is provided to compensate each integration calculation with its respective low frequency component of the "average" suspension velocity (\( \dot{Z}_{\text{susp}} \)), average suspension pitch rate (\( \dot{\theta}_{\text{susp}} \)), and "average" suspension roll rate (\( \dot{\phi}_{\text{susp}} \)). Such compensation has effect only at very low frequencies, for instance from disturbances like lane changes, braking or long wavelength undulation on a highway. The "average" suspension velocity and angular rates are calculated based on the estimated suspension velocities (\( \hat{x}_4 \) through \( \hat{x}_7 \)) as follows:

\[
\begin{bmatrix}
Z_{\text{susp}} \\
\theta_{\text{susp}} \\
\phi_{\text{susp}}
\end{bmatrix} = \begin{bmatrix}
-1/4 & -1/4 & -1/4 & -1/4 \\
2/1 & 2/1 & -2/1 & -2/1 \\
-2/tw & 2/tw & 2/tw & -2/tw
\end{bmatrix}
\begin{bmatrix}
\hat{x}_4 \\
\hat{x}_5 \\
\hat{x}_6 \\
\hat{x}_7
\end{bmatrix}
\] (13)

The summation 224 for the average suspension roll rate (\( \dot{\phi}_{\text{susp}} \)) has the same time constant as low-pass filter 222 used for
integrating the roll acceleration (Q). Similarly, vertical body (heave) velocity x₁, and pitch rate x₂ can be estimated through substantially identical integration filtering of their corresponding acceleration signal.

The final three state variables estimated are vertical displacement (\( \hat{x}_9 \)), pitch angle (\( \hat{x}_p \)) and roll angle (\( \hat{x}_{10} \)). As shown in Figure 23, the estimation is performed by a second integrating filter 230 which performs substantially identical to the first integration procedure herebefore presented with the input now being estimated roll angular velocity (\( \hat{x}_3 \)) being integrated and "average" suspension roll angle (Q_{susp}) being low-pass filtered and added thereto. Since the suspension displacements (x₁₁ through x₁₄) are measured directly, the "average" suspension displacement (Z_{susp}) and the angles (O_{susp}, Q_{susp}) can be expressed as:

\[
\begin{bmatrix}
Z_{susp} \\
O_{susp} \\
Q_{susp}
\end{bmatrix} = \begin{bmatrix}
-1/4 & -1/4 & -1/4 & -1/4 \\
2/1 & 2/1 & -2/1 & -2/1 \\
-2/tw & 2/tw & 2/tw & -2/tw
\end{bmatrix} \cdot \begin{bmatrix}
x_{11} \\
x_{12} \\
x_{13} \\
x_{14}
\end{bmatrix}
\]

(14)

Preferably, the time constant (T₃) of integrating filter 230 for heave and pitch is about 1.0 sec. and for roll is about 0.25 sec. The time constant stimulates how fast a reference plane follows the road in each mode of motion. The shorter time constant for determination of the roll angle relates to the fact
that roll angle $\hat{x}_{10}$ must converge faster for calculation of the "average" suspension roll angle.

The full state feedback regulation structure associated with "vehicle controller" 210 is obtained by feeding back the estimated state variables derived by the signal processor 208 to vehicle controller 210. The dynamics of observer 209 should not affect the dynamics of the vehicle specified by the feedback gains. This simplifies the analysis as the two control circuits for "dynamic leveling" loop 202 are now separable.

The poles of observer 209 are given by the time constants for the derivation and integration filters. The determination of the observer poles is a compromise between sensitivity to measurement errors and the need for rapid recovery from initial errors. In order to ensure that the integrating filters 222 and 230 correspond satisfactorily with an "ideal" integration, the poles should be located close to origin but should be located along the negative real axis for rapid recovery from initial errors. Furthermore, the derivateing filter 220 should be located as far out along the negative real axis as is possible for sensitivity to measurement errors.

An analysis of the impact of observer 209 on the vehicle dynamics can be made by expanding the A-matrix, describing the vehicle, with the ten state variables $X_1$ through $X_{10}$ estimated by observer 209. The feedback gain matrix is "shifted" over to the estimated state variables and the gains for each of the state variables are set to zero. The eigenvalues computed with the
feedback matrix $G_{\text{soft}}$ (Figure 19) for the closed loop A-matrix and the closed loop "expanded" A-matrix are shown in the table.

<table>
<thead>
<tr>
<th></th>
<th>Full state feedback $\xi_0 \pm \omega_0 \sqrt{1-\xi^2}$</th>
<th>Estimated state feedback $\xi_0 \pm \omega_0 \sqrt{1-\xi^2}$</th>
<th>Observer poles $\xi \omega_0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Heave:</td>
<td>-4.23 $\pm 4.23i$</td>
<td>-4.19 $\pm 4.24i$</td>
<td>-0.5, -1</td>
</tr>
<tr>
<td>Pitch:</td>
<td>-4.46 $\pm 4.46i$</td>
<td>-4.43 $\pm 4.48i$</td>
<td>-0.5, -1</td>
</tr>
<tr>
<td>Roll:</td>
<td>-12.2 $\pm 12.3i$</td>
<td>-12.4 $\pm 11.7i$</td>
<td>-0.5, -4</td>
</tr>
<tr>
<td>Wheel:</td>
<td>-7.74 $\pm 73.7i$</td>
<td>-7.68 $\pm 74.0i$</td>
<td>-250</td>
</tr>
<tr>
<td>Wheel:</td>
<td>-7.75 $\pm 73.7i$</td>
<td>-7.71 $\pm 73.9i$</td>
<td>-250</td>
</tr>
<tr>
<td>Wheel:</td>
<td>-8.1 $\pm 72.6i$</td>
<td>-7.70 $\pm 73.1i$</td>
<td>-250</td>
</tr>
<tr>
<td>Wheel:</td>
<td>-7.46 $\pm 74.3i$</td>
<td>-7.46 $\pm 74.3i$</td>
<td>-250</td>
</tr>
</tbody>
</table>

The observer's 10 poles are all real poles and ordered to the related mode of motion. Comparison of the vehicle poles shows a maximum overall difference of 5% in roll motion, due to the pole of its second integrating filter being located at -4. This is due to the more rapid recovery of the roll angle towards the average suspension roll angle.

Observer 209 is based on input from a sensor configuration which includes transducers that are commercially available within a reasonable price range. As an alternative, a gyroscope located in the center of gravity for directly measuring the pitch and roll would minimize the need of a single accelerometer for vertical heave measurement.

Adaptive Control

According to the present invention, an "adaptive" circuit is provided for tuning the "dynamic leveling" control loop 202. "Adaptive" control is the automatic self-tuning process of
control loop 202 which is independent of the sensor configuration employed. With particular reference to Figure 25, an additional self-tuning loop 240 is added to the control system 200. In general, the "adaptive" control loop 240 is employed to overcome the compromise between road holding and comfort. In short, the gains of feedback matrix "C" are being continuously recalculated to maintain "optimal" behavior.

Herebefore, several design techniques have been employed for suspension systems in which the adaptivity scheme was based on phase and/or amplitude margins, pole-placement control or LQG-control. What each has in common is that the parameters of the vehicle controller circuit are adjusted by an additional outer loop, which is composed of a recursive parameter estimator for describing the dynamic motion, and a calculator for calculating the new regulator gains.

Adaptive control scheme 240 according to the present invention is provided for maintaining good road holding over a wide range of road conditions. Since the frequency dependency of wheel damping is included in the feedback regulation of active suspension control structure 200, the adaptive scheme 240 is simple in structure for convenient implementation therein.

In particular, the adaptive scheme 240 for "dynamic leveling" control loop 202 is of a reversed character in comparison with conventional adaptive scheme. According to this invention, disturbances (the road) are identified and thereafter the dynamics of the vehicle are modified to "adapt" to the changes in environmental conditions.
As is known, soft suspension damping generates good road isolation but relatively poor road holding at frequencies around the wheel's natural frequency. Adaptation scheme 240 improves road holding by using the frequency dependency of the feedback gain matrix. Therefore, the adaptive scheme of the present invention combines good road holding from a "firm" suspension with good comfort from a "soft" suspension. In short, the adaptive mechanism 240 adjusts the gains for each corner actuator to increase or decrease only the suspension damping characteristics.

Adaptive loop 240 is divided into "disturbance identifier" 242 and "gain tuner" 244. Disturbance identifier 242 calculates a gain weighting coefficient ($\alpha$) for each corner which is based on the frequency and amplitude of the estimated suspension velocities $x_4$ through $x_7$. As is apparent, any sensor configuration or derived signal which produces suspension velocity outputs can be readily adapted for application of this adaptive concept. Gain tuner 244 contains the two feedback gain matrixes $G_{soft}$ and $G_{firm}$ from which a weighted linear combination "G" is derived and sent to vehicle controller 210.

Adaptive loop 240 is continuously calculating the four gain weighting coefficients ($\alpha_{lf}$, $\alpha_{rf}$, $\alpha_{lr}$, $\alpha_{rr}$), each representing the gain adjustment necessary for the corresponding corner actuator 110 at a given time. The magnitude of the weighting coefficient ($\alpha$) is scaled and saturated to be within the range (0-1).
(\(\alpha\)) is close to zero for frequencies around the natural frequency of the vehicle body and near unity around the natural frequency of the wheel.

The linear combination of the two distinct gain matrices \(G_{\text{soft}}\) and \(G_{\text{firm}}\) within gain tuner 244 is derived from the general formula:

\[
g = (1-\alpha) \, g_{\text{soft}} + \alpha \, g_{\text{firm}}
\]

(15)

Therefore:

\[
G = \begin{bmatrix}
(1-\alpha_{rr}) & 0 & 0 & 0 \\
0 & (1-\alpha_{rr}) & 0 & 0 \\
0 & 0 & (1-\alpha_{rr}) & 0 \\
0 & 0 & 0 & (1-\alpha_{rr})
\end{bmatrix} \cdot G_{\text{soft}} \cdot \begin{bmatrix}
\alpha_{rr} & 0 & 0 & 0 \\
0 & \alpha_{rr} & 0 & 0 \\
0 & 0 & \alpha_{rr} & 0 \\
0 & 0 & 0 & \alpha_{rr}
\end{bmatrix} \cdot G_{\text{firm}}
\]

When \((\alpha)\) has a magnitude of one, the resulting gain "G" is equal to \(G_{\text{firm}}\) and when \((\alpha)\) is zero, "G" is equal to \(G_{\text{soft}}\). The stiffness gains (columns 8 - 14 of Figure 17) are the same for the two matrices, therefore, they remain unchanged independent of the magnitude of \((\alpha)\). The "effective" damping of the body (active inertial damping + wheel suspension damping) is likewise kept constant for both the \(G_{\text{soft}}\) and the \(G_{\text{firm}}\) matrices, with only the distribution between the inertia damping and suspension damping varying depending on the value of \((\alpha)\).

Figure 26 illustrates the effect the adaptivity scheme has on the vehicle pole placement. The poles for the vehicle body remain constant while the poles for the unsprung masses (wheels) move along an arc between the \(E=0.1\) and the \(E=0.5\) line.

Referring now to Figure 27, the frequency dependency of disturbance identifier 242 is generated by first passing the input signals \((\hat{x}_k \text{ through } \hat{x}_r)\) through an underdamped high-pass
filter 250, tuned to set its maximum amplification to about the wheel's resonance frequency. Filter 250 is of second order with relative damping for generating good attenuation of suspension movement around the body frequencies as well as a narrow resonance peak. A vehicle's wheel resonance frequency is a product of the vehicle itself and furthermore is generally different from the front to the rear of the vehicle. High pass filter 250 must therefore be tuned specifically for each vehicular application.

Preferably, filter 250 is a recursive digital filter with a sampling rate set at about 125Hz. Therefore, every 1/8th millisecond the (α) values are updated. The high sampling rate is necessary so that the gains associated with gain tuner 244 are only adjusted in small increments to provide a relatively smooth transition.

Three additional signal processing "blocks" are provided after high pass filter 250. Rectifier block 252 rectifies the filtered signal by taking its absolute value. The next "block" is a second order "real poles" low pass filter 254. The final block 256 saturates the signal for maximizing its output to 1. While Figure 28 illustrates the block diagram for calculating (α₁f) from input of the left front suspension velocity (xₙ), the identical procedure is applied to the other corners of the vehicle. The magnitude of (α) is always positive and can be looked upon as a moving average of the rectified signal.

Simulation of vehicle 102 passing a bump provides a good illustration of the performance of the (α) value. Figures 28
through 30 provide an exemplary situation, with filter 250 having a constant input frequency of 9 Hz and an amplitude of 0.4. The input is a bump of 0.05 meters in height and 2 meters long. The vehicle is driven at 40 km/h, such that the wheels pass the bump in 0.18 sec. (see Figure 28). The desired performance of the suspension is to permit the wheels to absorb the impact of the bump with a soft suspension and then slowly increase the wheel damping to prevent the wheels from bouncing and losing tire to ground contact. The three diagrams in Figures 28 through 30 display the road profile versus time, suspension velocity and the gain weighting coefficient ($\alpha$) respectively. The suspension velocity (Figure 29) is the input to disturbance identifier 242 and ($\alpha$) is the output.

**Actuator Controller**

The actuator control strategy and hardware configuration of the present invention are fundamental to the improved characteristics of low power active suspension system 100. A primary principle of actuator 110 and its control strategy is the division of the power requirements into the "dissipation" and "addition" of power. "Dissipation" of power is controlled by infinitely variable damper valve 156 within actuators 110. The "addition" of power is controlled by selective energization of external servo valve 130. The result is the intermittent opening and closing of servo valve 130 to add or subtract energy to or from actuator 110.
Referring to Figure 31, actuator 110 is a "slave" which is commanded to produce force "U" from a summation of the dynamic leveling force $U_{dyn}$ and the load leveling force $U_0$. Actuator 110 is schematically illustrated as including an actuator controller 300 and its driving circuit hardware 302. Preferably, actuator 110 is physically mounted between the sprung and unsprung masses and can support the sprung mass with or without application of a passive support member such as a helical spring. More preferably, a passive coil spring assists in supporting the vehicle body.

As noted from Figure 8, hydro-pneumatic actuator 110 communicates with accumulator 128. For a given flow through piston 148, the flow restriction through damper valve 156 can be set to generate any force within its upper and lower limit. When a desired force is outside of the limits of damper valve 156, servo valve 130 is actuated. Servo valve 130 is either supplying actuator 110 with high pressure fluid or emptying actuator 110 of fluid which is returned to reservoir 140.

The force generated by actuator 110 is the sum of the accumulator and piston force.

$$F_{\text{actuator}} = F_{\text{acc}} + F_{\text{piston}}$$

Where:

$$F_{\text{piston}} = C \cdot Q_{\text{piston}}$$

$$Q_{\text{piston}} = Q_{\text{rel}} + Q_{\text{serv}}$$

$$Q_{\text{rel}} = V_{\text{rel}} \cdot A_{\text{piston}}$$

$$F_{\text{acc}} = P_{\text{acc}} \cdot A_{\text{rod}}$$

$$P_{\text{acc}} = \text{Konst} / V_{\text{acc}}^k$$

$$F_{\text{piston}} = \text{Actuator force from piston}$$

$$C = \text{Characteristic of damper valve}$$
\( C_{com} \) = Commanded setting of damper valve
\( Q_{piston} \) = Hydr. flow through damper valve
\( Q_{rel} \) = Hydr. flow by suspension velocity
\( Q_{serv} \) = Hydr. flow from servo valve
\( Q_{com} \) = Commanded flow
\( P_{acc} \) = Actuator force from accumulator pressure
\( P_{acc} \) = Accumulator pressure
\( V_{acc} \) = Volume of gas in accumulator

The accumulator pressure \( P_{acc} \) is dependant on the level of compression of the gas confined within accumulator 128. During rapid changes to the gas volume within accumulator 128, the process can be described as adiabatic with the following formula:

\[ P_{acc} \cdot V_{acc}^k = \text{konst}, \text{ where } k = 1.4 \]  \hspace{1cm} (16)

During slower changes in the gas volume within accumulator 128, heat is transferred to the surroundings and the process is regulated by the following formula:

\[ P_{acc} \cdot \frac{V_{acc}}{T} = \text{konst}. \]  \hspace{1cm} (17)

The piston force \( F_{piston} \) is generated by the pressure drop across piston 148 which is caused by the flow restriction generated by valve 156. The flow restriction is a generally linear relationship between force and flow which is denoted as characteristic \( "C" \). Adjustment of damper valve 156 generates an increase or decrease of \( "C" \) between the upper and lower limits \( C_{firm} \) and \( C_{soft} \).

Therefore:

\[ F_{piston} = C \cdot Q_{piston} \]  \hspace{1cm} (18)
The relative flow \( Q_{rel} \) is defined as the volume/second flow of hydraulic fluid associated with the relative movement between actuator cylinder 144 and piston 148. The flow through piston 148 is the sum of the flow caused by the relative velocity of the suspension \( Q_{rel} \) and the flow from the servo valve \( Q_{serv} \).

\[
Q_{piston} = Q_{rel} + Q_{serv}
\] (19)

Therefore, by selectively controlling the flow to or from servo valve 130, flow across piston 148 can be controlled such that the piston force \( F_{piston} \) can be generated independent of suspension movement.

Infinitely variable damper valve 156, located in piston 148, can be continuously controlled within its upper and lower limit \( C_{firm} \) and \( C_{soft} \), respectively. A control signal \( C_{com} \) from the actuator controller 300 energizes the actuator's driving circuit 302 to adjust valve 156 to either characteristic. The "soft" characteristic is performed by valve 156 with its driving circuit inactivated. The "firm" characteristic is performed with maximum output from its driving circuit. In order to save power and avoid unnecessary activation of servo valve 130, the gain values in the "G" matrix (adaptively derived from \( C_{soft} \) and \( C_{firm} \) from gain tuner 244 of adaptive loop 240) relating to suspension velocities \( \dot{x}_4 \) to \( \dot{x}_7 \) must be within the limits of damper valve 156.

Actuator 110 has a passive spring constant \( k_{act} \) which is regulated by the volume of fluid displaced by piston rod 150 within working chamber 146. During compression, rod 150 moves telescopically into housing 144 such that the additional volume
compresses the accumulator gas volume and increases the accumulator pressure. Therefore, the actuator's spring constant \( k_{\text{act}} \) is dependent on the pressure in, and the size of, accumulator 128 and the area of piston rod 150. The spring rate can be approximated as linear for a specific load condition.

The actuator spring constant \( k_{\text{act}} \) generates a force proportional to the suspension displacement without any activation of damper valve 156 or servo valve 130. Since this force is measured by the force transducer or pressure sensor within actuator 110, it must be demanded by the control system. The gain matrices \( G_{\text{soft}} \) and \( G_{\text{firm}} \) include gain values for each suspension displacement \( (x_{11} \text{ to } x_{14}) \), corresponding to the actuator spring constant \( k_{\text{act}} \) in that corner of the vehicle.

The actuator controller 300 is adapted to track the demanded force "U" by simultaneously controlling the setting of servo valve 130 and damper valve 156. Accordingly, power is saved by only using damper valve 156 for "dissipative" power demands and servo valve 130 for the "addition or release" of power when needed.

The demanded force "U" is generated by the accumulator force \( F_{\text{acc}} \) and the piston force \( F_{\text{piston}} \). The difference between the demanded force "U" and the accumulator force \( F_{\text{acc}} \) defines the piston force to be generated by servo valve 130 and damper valve 156. Therefore:

\[
F_{\text{piston}} = U - F_{\text{acc}} \quad (20)
\]
The piston force is generated by flow through piston valving 156 and its corresponding damping characteristic "C", such that:

\[ U - F_{acc} = C\cdot(Q_{rel} + Q_{serv}) \]  \hspace{1cm} (21)

The working principle of actuator controller 300 is to dissipate or add power to the suspension. The energy used is either derived from the kinetic energy of the vehicle's vertical motion or from the central pressure source 132. The working principle of actuator controller can be divided into four cases which correspond to the four quadrants of Figure 32. They are:

I. Suspension is in compression: The kinetic energy of the vehicle's vertical motion is attenuated and converted into heat. (Power is dissipated).

II. Suspension is in expansion: Energy is added to the suspension from central pressure source 132 (fluid flows through servo valve 130). The energy is converted into kinetic energy and accumulated as potential energy in accumulator 128.

III. Suspension is in expansion. The kinetic energy of the vehicle's vertical motion is attenuated and converted into heat. (Power is dissipated).

IV. Stored potential energy in accumulator 128 is released (hydraulic fluid exits actuator 110 and returns to reservoir 134). The potential energy is converted into kinetic energy and heat.

As mentioned, the four cases described each represent one quadrant of Figure 32. The y-axis represents the desired force...
"U", with its origin at the magnitude of the accumulator force. The x-axis represents the relative flow $Q_{rel}$. It should be noted that the accumulator force $F_{acc}$ is not constant, since the working range of damper valve 156 is continuously moving up and down.

Case I and III above represent "dissipation" of power. As such, no flow from servo valve 130 is required and the flow through the piston, $Q_{piston}$ is the same as the flow generated by the relative suspension velocity $Q_{rel}$. Except for supplying additional accumulator force, actuator 110 now works as a semi-active actuator with infinitely variable damping between its upper and lower limit $C_{soft}$ and $C_{firm}$.

Point 1, (Figure 32) is an example of a demanded force "U" which is located in quadrant I. The relative flow $Q_{rel}$ is positive whereby actuator 110 is in compression. Damper valve 156 is capable of increasing the piston force $F_{piston}$ from the level of the accumulator force $F_{acc}$ to the demanded level. Since the relative motion has the same polarity as the desired force, the desired force "U" is achieved by adding resistance to the motion. Therefore, adjustment of damper valve 156 is shown along line "C".

In cases II and IV adjustment of damper valve 156 is not sufficient and external flow through damper valve 156 is required. The effect of the flow from servo valve 130 is shown in Figure 33. Flow from servo valve 130 into actuator 110 is defined as "positive" and acts to shift the working range of damper valve 156 to the left along the x-axis ($Q_{rel}$). Likewise, a "negative" flow out of actuator 110 would shift the working
range to right. Shifting of the working range of damper valve 156 makes it possible to generate the desired force "U" using the upper and lower limits of damper valve 156. With damper valve 156 set to "firm", the desired force is achieved with the lowest piston flow rate and therefore with the lowest flow requirement from servo valve 130.

Point "2" (Figures 32 and 33) illustrates an example of Case II wherein the demanded force "U" is positive and the relative motion is negative, i.e., the actuator in extension. During expansion, the volume in working chamber 146 under piston 148 increases with the rate \( Q_{rel} \). For a regular passive shock absorber, flow would be directed from the upper chamber above the piston to the lower chamber such that the force generated would then be in quadrant III. However, to create a positive force during expansion, flow through piston valving 156 must be directed in the opposite direction. Therefore, flow from servo valve 130 into actuator 110 must be larger than the relative flow \( Q_{rel} \).

In those instances when the demanded force "U" is within quadrants I and III but outside the limits of damper valve 156 (See example points 3 and 4 of Figure 32), external flow through servo valve 130 is required to satisfy the demand.

**Actuator Controller System**

The actuator control system 300 (Figure 31) is designed to perform according to the principle presented by calculating the commanded flow for the servo valve \( Q_{serv} \) and the commanded damper
setting for the damper valve $C_{con}$. Actuator controller circuit
300, illustrated in greater detail in Figure 34, has as inputs
the commanded force "U" and the measured actuator force $F_{actuator}$. The control for servo valve 130 is an open loop with the gain
adjusted according to the power demand. The control for damper
valve 156 is preferably a PI-controller with the actuator force
$F_{actuator}$ as feedback.

Other variables inputted into actuator controller 300 are
the accumulator force $F_{acc}$ and the relative flow $Q_{rel}$. Since both
variables are not directly measured they must be estimated. The
estimation of the accumulator force $F_{acc}$ is made by low-pass
filtering of the actuator force $F_{actuator}$ and by estimating the
accumulator volume change. Relative flow $Q_{rel}$ is estimated by
multiplying the estimated suspension velocities ($\dot{x}_4$ through $\dot{x}_7$,
inputted from "observer" 208) by the area of piston 148.

The actuator controller cycle time is set to be about four
times faster than the "dynamic leveling" loop 202. To follow
the demanded force "U" during each cycle, a new command signal
$Q_{con}$ and $C_{con}$ is calculated for the flow and damper settings,
respectively. To generate the command signals, the actuator
control scheme is divided into three steps:

A. Power identification;
B. Control of servo valve 130; and
C. Control of damper valve 156.

Actuation of servo valve 130 is dependent on the "location"
of the demanded force "U" in relation to the relative flow $Q_{rel}$. The
location is identified by a quotient $C'$, calculated as the
ratio between the desired piston force \((U - F_{acc})\) and the relative flow \(Q_{rel}\), wherein:

\[
C' = \frac{(U - F_{acc})}{Q_{rel}}
\]  

(22)

Referring to Figure 35, the sign and magnitude of the quotient \(C'\) indicates a fictive damping characteristic used as a gain "h" to calculate the commanded force from servo valve 130. However, gain "h" must be within the upper and lower limit of damper valve 156.

If the quotient \(C'\) is negative \((C' < 0)\), the desired piston force is located in quadrants II or IV and external flow through servo valve 130 is required (in or out of actuator 110). In particular, when actuator 110 is in expansion, fluid is added into lower portion 154 of working chamber 146 and when actuator 110 is in compression, fluid is exhausted from lower portion 154 through servo valve 130. Therefore, in order to achieve the required force with a minimum of additional flow, damper valve 156 should be set to "firm" and the gain "h" for servo valve 130 set to \(C_{firm}\).

If the quotient \(C'\) is larger than \(C_{firm}\) \((C' > C_{firm})\), the desired piston force is in quadrants I or III. However, the "firm" characteristic of damper valve 156 is not sufficiently firm and the desired force is only achieved by actively "increasing" flow through piston valve 156 via external flow through servo valve 130. To "increase" flow when actuator 110 is in expansion, fluid is exhausted from lower portion 154 to reservoir 140 through servo valve 130. To "increase" flow during
a compression stroke, fluid is added from hydraulic system 132 into lower portion 154 of working chamber 146 through servo valve 130. Therefore, the gain "h" to servo valve 130 is set to $C_{\text{firm}}$.

If the quotient $C'$ is smaller than $C_{\text{soft}}$ ($C' < C_{\text{soft}}$), the desired piston force is in quadrants I or III. However, the "soft" characteristic of damper valve 156 is not sufficiently soft and the desired force is achieved by actively "decreasing" the piston flow through valve 156. In particular, when actuator 110 is in expansion, "decreased" flow across valve 156 is generated by adding fluid to lower portion 154 of working chamber 146. In addition, "decreased" flow is generated when actuator 110 is in compression by exhausting fluid from lower portion 154 back to reservoir tank 140. Therefore, the gain "h" to servo valve 130 is set to $C_{\text{soft}}$.

If the quotient $C'$ is within the limits of the damper valve 156 itself, the desired piston force can be generated simply by selective adjustment of damper valve 156 and the gain "h" is set to $C'$.

Preferably, servo valve 130 has an open control loop, which uses direct calculations based on the gain "h", relative flow $Q_{\text{rel}}$, and the required piston force ($U - F_{\text{acc}}$). With the gain "h" as the ideal damping characteristic of damper valve 156, the necessary piston flow $Q_{\text{piston}}$ can be calculated based on the equation:

$$Q_{\text{piston}} = (U - F_{\text{acc}})/h$$  \hspace{1cm} (23)
Since the difference between piston flow $Q_{piston}$ and the relative flow $Q_{rel}$ is the commanded flow from servo valve 130 it follows:

$$Q_{com} = (U - F_{acc})/h - Q_{rel}$$  \hspace{1cm} (24)

When the desired force "U" is within the limits of damper valve 156, the gain "h" is assigned the value of the quotient C'. Therefore, by replacing "h" in equation (23) by the right side of equation (22), the commanded flow from servo valve is zero.

Figure 36 illustrates a portion of actuator controller circuit 300 for controlling servo valve 130 using the equations herebefore detailed. Figure 37 is a graph which illustrates the desired piston force plotted against the relative flow which forms an ellipsoidal curve, running clockwise through each quadrant of damper valve's 156 working area. The control strategy for servo valve 130 results in the following modes of actuation:

a-b: Actuator 110 is working as a variable damper;

b-c: Flow "out" of actuator 110 through servo valve 130;

c-d: Actuator 110 is working as a variable damper;

d-a: Flow "into" actuator 110 from the servo valve 130.

An example of the actuation "duty" cycle of servo valve 130 during an entire cycle a-a is shown in Figure 38. The time period d-a represents only about 20% of the complete duty cycle a-a and is the only time when energy is transferred from central pressure source 132 for addition into actuator 110. The dynamics
of servo valve 130 cause a time delay between the commanded flow (dashed line) and the actual flow.

Under "ideal" conditions, the gain "h", used in the control of the servo valve 130, could be used as the commanded damper setting. However, nonlinearities, time delays and estimation errors make it preferable to control damper valve 156 with a closed control loop which feeds back the actual actuator force $F_{\text{actuator}}$.

The block diagram of Figure 39 shows the control scheme associated with actuator controller 300 for damper valve 156. The error "e" between the commanded force "U" and the actuator force $F_{\text{actuator}}$ is corrected to account for the direction of the piston flow (DIR = 1 or -1) in block 320. The second block 322 is a PI-controller and third block 324 saturates the commanded signal $C_{\text{com}}$ to be within the limits of the damper valve 156.

The correction of "e" to the sign of the piston flow is necessary since the flow through piston valve 156 is bidirectional. An incremental change in the damper characteristic results in an incremental increase in the force from a positive piston flow (a flow from lower chamber 154 below piston 148 to upper chamber 152 above the piston). However, if the flow is negative, the resultant incremental change is a decrease in the force.

The PI-controller 324 is tuned for as fast a response as possible. The piston flow $Q_{\text{piston}}$ works in the control loop as a separate gain between the damper setting and the piston force.
The frequency response of the closed control loop is dependent on the current piston flow.

As frequency increases, body movement decreases and suspension movement is derived mainly from the wheel. At road disturbance frequencies above about 6 Hz, the commanded force "U" is generally about 95% within the reach of damper valve 156. At these high frequencies, the force requirement becomes proportional to the relative flow, (see curve C in Figure 40) i.e., the damper setting is close to constant and no flow from servo valve 130 is required.

Power Consumption

The power consumption of actuator 110 is measured as "peak" power consumption and "average" power consumption. Power consumption of actuator 110 is defined as the actuator force multiplied by the relative velocity of the suspension:

\[ P_{\text{actuator}} = F_{\text{act}} \cdot V_{\text{rel}} \quad (25) \]

The power consumption of interest for the dynamic leveling systems of the present invention is the hydraulic power consumption taken from central hydraulic system 136 and consumed by each actuator 110. This occurs only when the demanded force "U" is in quadrant II (Figures 37 and 40) when additional flow is supplied into actuator 110. The power consumption for the "system" is defined as:

\[ P_{\text{system}} = P_{\text{system}} \cdot Q_{\text{serv}} \quad (\text{for } Q_{\text{serv}} > 0) \]
The system pressure \( p_{\text{system}} \) is the pressure which is maintained by central pressure source 132. To minimize power consumption, the system pressure should be designed to be as low as possible yet large enough to support actuators 110 under the most extreme conditions.

The present invention produces a substantial reduction in peak flow and peak power requirements that are necessary to dynamically adjust vehicle body heights variations as compared to conventional active suspension systems. The restricted flow "assists" the flow control means in responding to vehicle attitude changes. This "assistance" promotes reduced system flow and power requirements while generating improved reaction time characteristics. Additionally, utilization of independent actuators 110 at each suspension corner provides improved overall vehicle attitude control in response to both vertical and lateral motion of the vehicle body.

While it is apparent that the preferred embodiments illustrated herein are well calculated to fill the objects stated above, it will be appreciated that the present invention is susceptible to modification, variation and change without departing from the scope of the invention.
CLAIMS

What Is Claimed Is:

1. A low power fully active suspension system for a motor vehicle, comprising:
   a hydraulic damper provided at each corner of the vehicle which is operably connected between the suspension and body of the vehicle, said hydraulic damper having a pressure cylinder forming a working chamber operable to store damping fluid therein and secured to one of the suspension and body of the vehicle, and a piston and rod assembly coaxially disposed within said pressure cylinder for translational movement therein with opposite sides of said piston defining first and second portions of said working chamber, said rod secured at an end opposite said piston to the other of the suspension and body portions of the vehicle;
   variable flow restriction means for varying the flow of damping fluid between said first and second portions of said working chamber;
   sensor means for sensing the dynamic motion of the suspension and body of the vehicle and generating output signals in response thereto;
   fluid supply means for providing an external source of high pressure damping fluid to each of said actuators;
   flow control means associated with each of said actuators for controlling the flow of damping fluid between said actuators and said fluid supply means, said flow control means adapted to
fluidly communicate with one of said first and second portions of said working chamber;

an accumulator associated with each of said actuators and in fluid communication with the other of said first and second portions of said working chamber; and
control means adapted to receive said output signals from said sensor means for calculating a commanded force output signal "U" for each of said actuators, said control means adapted for selectively actuating at least one of said variable flow restriction means and said flow control means for generating said commanded force.

2. The low power fully active suspension system of Claim 1 wherein said control means includes a central control system adapted for passively controlling the dynamic behavior of the vehicle suspension through actuation of said flow restriction means for selectively varying the flow therethrough between a minimum and maximum flow limit, said control system actively controlling the dynamic behavior of the vehicle body through simultaneous actuation of said flow restriction means and said flow control means so as to either add high pressure fluid to said working chamber of said actuator or exhaust fluid from said working chamber to a reservoir.
3. The low power fully active suspension system of Claim 2 wherein said central control system is a full state feedback control system having a closed-loop dynamic leveling controller circuit for generating an output signal $U_{\text{dyn}}$, and a closed-loop load leveling controller circuit for generating an output signal $U_o$ wherein the commanded force signal "U" for each actuator is determined according to the equation "$U = U_{\text{dyn}} + U_o$.

4. The low power fully active suspension system of Claim 3 wherein said load leveling controller circuit is adapted to maintain a predetermined vehicle static height under variable vehicle loading conditions.

5. The low power fully active suspension system of Claim 3 wherein said dynamic leveling controller circuit includes signal processing means for processing said output signals from said sensor means for generating a state variable vector $X_n$ representing the velocity and displacement of the vehicle suspension and body, said dynamic leveling controller circuit further includes vehicle controller means having a feedback gain matrix $G_n$ defining stiffness and damping characteristics based on predetermined vehicle dynamic performance requirements, and wherein said vehicle controller means receives an output from said signal processing means for calculating "$U_{\text{dyn}}$" according to the following equation:

$$U_{\text{dyn}} = -G_n(X_n).$$
6. The low power fully active suspension system of Claim 5 wherein said feedback gains of said gain matrix $G_n$ are determined by the pole placement design method such that the location of the poles is defined by said predefined vehicle performance requirements such that the feedback gains represent stiffness and damping characteristics acting on the vehicle body.

7. The low power fully active suspension system of Claim 6 wherein said sensor means include a relative position sensor located at each corner of the vehicle between the suspension and body measuring the relative displacement of the suspension and accelerometer means adapted for measuring the heave, pitch and roll acceleration of the vehicle body.

8. The low power fully active suspension system of Claim 7 wherein said state variable vector $X_n$ has fourteen state variables for defining the dynamic motion at each of the four corners of the vehicle, wherein:

\[
\begin{align*}
  x_1 &= \dot{z}, \text{ heave velocity of C. G.} & x_4 &= z, \text{ heave displacement} \\
  x_2 &= \dot{\theta}, \text{ Pitch angular velocity} & x_5 &= 0, \text{ Pitch angle} \\
  x_3 &= \dot{\phi}, \text{ Roll angular velocity} & x_{10} &= Q, \text{ Roll angle} \\
  x_4 &= \text{Left Front suspension vel.} & x_{11} &= \text{LF suspension displ.} \\
  x_5 &= \text{Right Front suspension vel.} & x_{12} &= \text{RF suspension displ.} \\
  x_6 &= \text{Right Rear suspension vel.} & x_{13} &= \text{RR suspension displ.} \\
  x_7 &= \text{Left Rear suspension vel.} & x_{14} &= \text{LR suspension displ.}
\end{align*}
\]

9. The low power fully active suspension system of Claim 8 wherein said signal processing means includes means for estimating state variables $x_1$ through $x_{10}$ from the output signals of said position sensors and said accelerometer means.
10. The low power fully active suspension system of Claim 9 wherein said estimating means includes derivating filter means for derivating the suspension displacements $X_{11}$ through $X_{14}$ measured by said position sensors for estimating suspension velocities $X_i$ through $X_7$, and wherein said derivating filter means is scaled to act as a derivator at relatively low frequencies.

11. The low power fully active suspension system of Claim 9 wherein said estimating means comprises first integrating filter means for integrating the heave, pitch and roll accelerations sensed by said accelerometer means to estimate body velocities $X_i$ through $X_3$.

12. The lower power fully active suspension system of Claim 11 wherein the output from said first integrating filter means is added to the output of first low pass filtering means for filtering a low frequency average suspension velocity signal.
13. The low power fully active suspension system of Claim 12 wherein body displacement state variables $X_6$ through $X_{10}$ are estimated using second integrating filter means for integrating the estimated body velocities $X_1$ through $X_3$.

14. The low power fully active suspension system of Claim 13 wherein the output from said second derivating filter means is added to the output of second low pass filtering means provided for filtering a low frequency average suspension displacement signal.

15. The low power fully active suspension system of Claim 14 wherein said estimating means is an observer and wherein the time constant of each of said first and second integrating filter means and said derivating filter means is tuned to a desired frequency response and define the poles of said observer.
16. The low power fully active suspension system of Claim 5 wherein said central control system further comprises gain adaption means for continuously modifying said feedback gain matrix $G_h$ such that the feedback gains corresponding to damping of the vehicle suspension are modified in response to changes in frequency and amplitude of the suspension velocity.

17. The low power fully active suspension system of Claim 16 wherein said gain adaption means is a closed-loop system comprised of disturbance identifier means for identifying disturbances represented by variations in frequency and amplitude of the vehicle suspension velocity and for continuously calculating a gain weighting coefficient ($\alpha$) based thereon corresponding to each corner of the vehicle, said closed-loop system further comprising gain tuner means for receiving said gain weighting coefficient from said disturbance identifier means and calculating a linear combination "$G$" of a first feedback gain matrix $G_{soft}$ and a second feedback gain matrix $G_{firm}$ according to the equation

$$g = (1-(\alpha))g_{soft} + (\alpha)g_{firm}$$

Where: $0<(\alpha)<1$. 
18. The low power fully active suspension system of Claim 17 wherein the first feedback matrix $G_{soft}$ is adapted for relatively soft damping of the vehicle suspension for providing a smooth ride and said second gain matrix $G_{firm}$ is adapted for providing firm damping of the vehicle suspension with the objective to improve road holding and minimize relative displacement between the body and suspension.

19. The low power fully active suspension system of Claim 18 wherein said gain weighting coefficient ($\alpha$) is scaled to be within the range of (0-1) such that ($\alpha$) is about 0 for frequencies near the natural frequency of the vehicle body and ($\alpha$) is about 1 for frequencies near the natural frequency of the suspension.

20. The low power fully active suspension system of Claim 19 wherein said disturbance identifier means receives estimated suspension velocity signals from said signal processor means such that said suspension velocity signals are inputted into high-pass filter means for filtering and sampling said velocity signal, said disturbance identifier means also includes rectifying means for rectifying the filtered signal received from said high-pass filter means and saturation means for maximizing the rectified output value to 1.
21. The low power fully active suspension system of Claim 2 wherein said variable flow restriction means is a continuously variable piston damper valve for generating a variable flow restriction across said piston between said first and second portion of said working chamber.

22. The low power fully active suspension system of Claim 21 wherein said flow control means is a servo flow control valve and said fluid supply means includes a central vehicle hydraulic system having a central pump and an accumulator for supplying high pressure damping fluid to each of said servo valves for delivery into said actuators and a reservoir tank for receiving damping fluid exhausted through said servo valves from said working chamber of said actuators.
23. The low power fully active suspension system of Claim 22 wherein said control means further comprises an actuator controller circuit adapted to receive said commanded force output signal "U" corresponding to each actuator for selectively controlling actuation of said variable piston damper valve and said servo valve for generating an actuator force $F_{\text{actuator}}$ in response thereto which substantially tracks said commanded force "U" and which is calculated according to the equation:

$$F_{\text{actuator}} = F_{\text{acc}} + F_{\text{piston}}$$

Where:

- $F_{\text{piston}} = C Q_{\text{piston}}$
- $Q_{\text{piston}} = Q_{\text{rel}} + Q_{\text{serv}}$
- $Q_{\text{rel}} = V_{\text{rel}} A_{\text{piston}}$
- $F_{\text{acc}} = F_{\text{acc}} A_{\text{rod}}$
- $F_{\text{acc}} = \text{Konst/}V_{\text{acc}}^k$
- $F_{\text{piston}} = \text{Actuator force from piston}$
- $C = \text{Flow characteristic of piston valve}$
- $C_{\text{com}} = \text{Commanded setting of valve}$
- $Q_{\text{piston}} = \text{Hydr. flow through piston valve}$
- $Q_{\text{rel}} = \text{Hydr. flow by suspension velocity}$
- $Q_{\text{serv}} = \text{Hydr. flow from servo valve}$
- $Q_{\text{com}} = \text{Commanded flow}$
- $F_{\text{acc}} = \text{Actuator force from accumulator pressure}$
- $P_{\text{acc}} = \text{Accumulator pressure}$
- $V_{\text{acc}} = \text{Volume of gas in accumulator}$
24. The low power fully active suspension system of Claim 23 wherein said commanded force \( U \) is the sum of the accumulator force \( F_{\text{acc}} \) and piston force \( F_{\text{piston}} \) such that the piston force \( F_{\text{piston}} \) is generated by actuation of said servo valve and said damper piston valve, said piston force \( F_{\text{piston}} \) generated by the flow through said piston damper valve and the flow restriction characteristic of piston valve such that:

\[ U - F_{\text{acc}} = C(Q_{\text{rel}} + Q_{\text{serv}}). \]

25. The low power fully active suspension system of Claim 24 wherein said piston damper valve is infinitely controllably within its minimum and maximum flow restriction limits \( C_{\text{soft}} \) and \( C_{\text{firm}} \) respectively, such that a control signal \( C_{\text{com}} \) from said actuator controller circuit actuates said piston damper valve whereby system power requirements are substantially reduced by actuating only said piston damper valve for dissipative power demands within its limits such that said servo valve is actuated when said power demand is outside of the limits of said piston damper valve for adding or subtracting power to said actuator.
26. The lower power fully active suspension system of Claim 25 wherein said piston damper valve has variable range of control between a low flow restriction limit \( (C_{\text{soft}}) \) and a high flow restriction limit \( (C_{\text{firm}}) \), the flow restriction characteristic \( (C') \) is determined according to the equation \( C' = \frac{(U - F_{\text{acc}})}{Q_{\text{rel}}} \) wherein controlling actuation of said piston damper valve and said flow control means includes:

setting said flow restriction to \( C' \) when \( C_{\text{soft}} < C' < C_{\text{firm}} \) whereby the desired actuator force is generated by selective adjustment of said piston damper valve;

setting said flow restriction to \( C_{\text{firm}} \) when \( C' < 0 \) and concurrently actuating said flow control means to selectively add fluid to said first portion of said working chamber during an expansion stroke and exhausting fluid during a compression stroke, and wherein said flow restriction is set to \( C_{\text{firm}} \) to minimize the flow requirement of said flow control means;

setting said flow restriction to \( C_{\text{soft}} \) when \( C' < C_{\text{soft}} \) and concurrently actuating said flow control means for decreasing the flow through said piston damper valve, such that during an expansion stroke said flow control means is actuation to add fluid to said first portion of said working chamber and during a compression stroke said flow control means is actuation to exhaust fluid from said first portion of said working chamber, and wherein said flow restriction is set to \( C_{\text{soft}} \) to minimize the flow requirement of said flow control means; and

setting said flow restriction to \( C_{\text{firm}} \) when \( C' > C_{\text{firm}} \) such that said flow restriction is not sufficient to generate the
desired output force whereby said flow control means is actuated to increase flow through said piston damper valve, said flow control means is actuated to exhaust fluid from said first portion of said working chamber during an expansion stroke, and said flow control means is actuated to add fluid to said first portion of said working chamber during a compression stroke of said actuator.

27. The low power fully active suspension system of Claim 26 wherein said actuator controller includes means for calculating the commanded flow from said servo valve $Q_{serv}$ and said commanded damper setting $C_{com}$.

28. The low power fully active suspension system of Claim 27 wherein said piston damper valve has a driving circuit adapted for varying the flow restriction upon receiving said commanded setting $C_{com}$ from said actuator controller and wherein said servo valve is adapted to either supply said actuator with high pressure fluid from said fluid supply means or exhaust fluid from said actuator for return to said reservoir based on said commanded flow $Q_{com}$ from said actuator controller.
29. An apparatus for use with an active suspension system of a motor vehicle having a central high pressure fluid source, comprising:

a hydraulic damper adapted to be operably connected between the vehicle suspension and body at each corner thereof, said hydraulic damper having a pressure cylinder forming a working chamber operable to store damping fluid therein and secured to one of the suspension and body of the vehicle, and a piston and rod assembly coaxially disposed within said pressure cylinder for translational movement therein with opposite sides of said piston defining first and second portions of said working chamber, said rod secured at an end opposite said piston to the other of the suspension and body portions of the vehicle;

variable flow restriction means for varying the flow of damping fluid between said first and second portions of said working chamber;

flow control means associated with said actuator and fluidly connecting said actuator to the central high pressure fluid source for controlling the flow of damping fluid therebetween, said flow control means adapted to fluidly communicate with one of said first and second portions of said working chamber; and

an accumulator associated with said actuator and in fluid communication with the other of said first and second portions of said working chamber.
30. The apparatus of Claim 29 wherein said variable flow restriction means comprises infinitely variable flow restriction valving associated with said piston which is selectively variable between a maximum flow restriction to a minimum flow restriction.

31. The apparatus of Claim 30 wherein said flow control means is a servo valve fluidly connected in series intermediate said actuator and said central fluid pressure source.

32. The apparatus of Claim 29 further comprising sensor means for sensing the dynamic motion of the suspension and body of the vehicle and generating output signals in response thereto.

33. The apparatus of Claim 32 further comprising control means adapted to receive said output signals from said sensor means for calculating a commanded force output signal "U" for said actuator, said control means adapted for selectively actuating at least one of said variable flow restriction means and said flow control means for generating an output force $F_{actuator}$ from said actuator.
34. The apparatus of Claim 31 wherein said control means includes a central control system adapted for passively controlling the dynamic behavior of the vehicle suspension through actuation of said variable flow restriction means for selectively varying the flow therethrough between a minimum and maximum flow limit, said control system actively controlling the dynamic behavior of the vehicle body through substantially simultaneous actuation of said flow restriction means and said flow control means so as to either add high pressure fluid to said working chamber of said actuator or exhaust fluid from said working chamber to a reservoir when said commanded force "U" is outside of the limits of said variable flow restriction means.

35. The apparatus of Claim 34 wherein said central control system is a full state feedback control system having a closed-loop dynamic leveling controller circuit for generating an output signal $U_{dyn}$, and a closed-loop load leveling controller circuit for generating an output signal $U_o$ wherein the commanded force signal "U" inputted to said actuator is determined according to the equation "U" = $U_{dyn} + U_o$.

36. The apparatus of Claim 35 wherein said load leveling controller circuit is adapted to maintain a predetermined vehicle static height under variable vehicle loading conditions.
37. The apparatus of Claim 36 wherein said dynamic leveling controller circuit includes signal processing means for processing said output signals from said sensor means for generating a state variable vector $X_n$ representing the velocity and displacement of the vehicle suspension and body, said dynamic leveling controller circuit further includes vehicle controller means having a feedback gain regulation matrix $G_n$ defining stiffness and damping characteristics based on predetermined vehicle dynamic performance requirements, and wherein said vehicle controller means receives an output from said signal processing means for calculating "$U_{dyn}$" according to the following equation:

$$U_{dyn} = -G_n(X_n).$$

38. The apparatus of Claim 37 wherein said feedback gains of said gain matrix $G_n$ are determined by the pole placement design method such that the location of the poles is defined by said predefined vehicle performance requirements such that the feedback gains represent stiffness and damping characteristics acting on the vehicle body.

39. The apparatus of Claim 38 wherein said signal processing means includes means for estimating state variables from the output signals of said sensor means.
40. The apparatus of Claim 38 wherein said state variable vector $X_n$ has fourteen state variables for defining the dynamic motion at each of the four corners of the vehicle, wherein:

- $x_1 = \dot{Z}$, heave velocity of C. G.
- $x_2 = \dot{\phi}$, Pitch angular velocity
- $x_3 = \dot{\psi}$, Roll angular velocity
- $x_4 = \text{Left Front suspension vel.}$
- $x_5 = \text{Right Front suspension vel.}$
- $x_6 = \text{Right Rear suspension vel.}$
- $x_7 = \text{Left Rear suspension vel.}$
- $x_8 = Z$, heave displacement
- $x_9 = \phi$, Pitch angle
- $x_{10} = \psi$, Roll angle
- $x_{11} = \text{LF suspension displ.}$
- $x_{12} = \text{RF suspension displ.}$
- $x_{13} = \text{RR suspension displ.}$
- $x_{14} = \text{LR suspension displ.}$

41. The apparatus of Claim 40 wherein said signal processing means includes means for estimating state variables $X_i$ through $X_{10}$ from the output signals of said sensor means.

42. The apparatus of Claim 38 wherein said central control system further comprises gain adaption means for continuously modifying said feedback gain matrix $G_n$ such that the feedback gain values corresponding to damping characteristics of the vehicle are modified in response to changes in frequency and amplitude of the suspension velocity.
43. The apparatus of Claim 42 wherein said gain adaption means comprises a closed-loop control system including disturbance identifier means for identifying disturbances represented by variations in frequency and amplitude of the vehicle suspension velocity and for continuously calculating a gain weighting coefficient ($\alpha$) based thereon, said gain adaption means further comprising gain tuner means for receiving said gain weighting coefficient ($\alpha$) from said disturbance identifier means and calculating a linear combination "G" of a first feedback gain matrix $G_{soft}$ and a second feedback gain matrix $G_{firm}$ according to the equation:

$$g = (1-(\alpha))g_{soft} + (\alpha)g_{firm}$$

Where: $0 < (\alpha) < 1$

said first feedback matrix $G_{soft}$ is adapted for relatively soft damping of the vehicle suspension for providing a smooth ride and said second gain matrix $G_{firm}$ is adapted for providing firm damping of the vehicle suspension with the objective to improve road holding and minimize relative displacement between the body and suspension.
44. The apparatus of Claim 43 wherein said control means further comprises an actuator controller circuit adapted to receive said commanded force output signal "U" corresponding to said actuator for selectively controlling actuation of said variable flow restriction means and said flow control means for generating said actuator force \( F_{\text{actuator}} \) in response thereto and which is calculated according to the equation:

\[
F_{\text{actuator}} = F_{\text{acc}} + F_{\text{piston}}
\]

Where:

- \( F_{\text{piston}} \) = Actuator force from piston
- \( C \) = Flow characteristic of piston valve
- \( C_{\text{com}} \) = Commanded setting of valve
- \( Q_{\text{piston}} \) = Hydr. flow through piston valve
- \( Q_{\text{rel}} \) = Hydr. flow by suspension velocity
- \( Q_{\text{serv}} \) = Hydr. flow from servo valve
- \( Q_{\text{com}} \) = Commanded flow
- \( F_{\text{acc}} \) = Actuator force from accumulator pressure
- \( P_{\text{acc}} \) = Accumulator pressure
- \( V_{\text{acc}} \) = Volume of gas in accumulator
45. The apparatus of Claim 44 wherein said commanded force "U" is the sum of the accumulator force $F_{acc}$ and piston force $F_{piston}$ such that the piston force $F_{piston}$ is generated by said flow control means and said flow restriction means whereby changes in said piston force $F_{piston}$ are generated by selectively controlling the flow through said flow restriction means and its flow restriction characteristic such that:

$$U - F_{acc} = C(Q_{rel} + Q_{serv})$$

46. The apparatus of Claim 45 wherein said flow restriction means is a piston damper valve which is infinitely controllably within its minimum and maximum flow restriction limits $C_{soft}$ and $C_{firm}$ respectively, such that a control signal $C_{com}$ from said actuator controller circuit actuates said piston damper valve whereby system power requirements are substantially reduced by selectively actuating only said piston damper valve for dissipative power demands within its flow restriction limits, said flow control means actuated when said power demand is outside of the limits of said piston damper valve for adding or subtracting power to said actuator for selectively modifying the flow of fluid through said piston damper valve.
47. The low power fully active suspension system of Claim 46 wherein said piston damper valve has a driving circuit adapted for varying the flow restriction upon receiving said commanded setting $C_{com}$ from said actuator controller and wherein said flow control means is adapted to either supply said actuator with high pressure fluid from said fluid supply means or exhaust fluid from said actuator for return to said reservoir based on said commanded flow $Q_{com}$ from said actuator controller.
48. A method of dynamically leveling the attitude of a vehicle in response to changes in the dynamic behavior of the suspension and body of the vehicle, said method comprising the steps of:

connecting a hydraulic actuator between the suspension and body at each corner of the vehicle, said actuator having a piston and rod assembly disposed within a pressure cylinder such that said piston defines first and second portions of a working chamber adapted for storing damping fluid within said pressure cylinder;

connecting said first portion of said working chamber for each actuator to a high pressure fluid source having a pump and a reservoir;

connecting flow control means intermediate said high pressure fluid source and each of said actuators for controlling the addition or release of fluid from said first portion of said working chamber;

connecting an accumulator to said second portion of said working chamber for each of said actuator;

providing a variable flow restriction between said flow control means and said accumulator, said flow restriction being infinitely variable between an upper and lower limit;

sensing the dynamic behavior of the suspension and body at each corner of the vehicle for generating an electrical sensor output signal in response thereto;

calculating a desired suspension force "U" signal for each actuator in response to said sensor output signals;
inputting said suspension force signal "U" to an actuator controller adapted for controlling actuation of said flow control means and said variable flow restriction for generating a desired output force $F_{\text{actuator}}$ from each actuator;

actuating said variable flow restriction for generating said actuator force $F_{\text{actuator}}$ when said desired suspension force signal "U" is within said upper and lower limits of said variable flow restriction; and

actuating said continuously variable flow restriction to be set at either its upper or lower limit and concurrently actuating said flow control means for intermittently opening and closing a fluid communication path between said high pressure fluid source and said actuator for adding and subtracting energy to and from said actuator respectively, whereby substantially concurrent actuation generates said actuator force $F_{\text{actuator}}$ whenever said desired suspension force "U" is outside of said limits of said flow restriction.

49. The method of Claim 48 wherein said step of calculating force signal "U" comprises providing a closed-loop dynamic leveling control system and a closed-loop load leveling control system such that said suspension force signal "U" is the sum of an output signal from said dynamic leveling system "U$_{\text{dyn}}$" and the output signal from said load leveling system "U$_{\text{o}}$".
50. The method of Claim 49 wherein said dynamic leveling control system includes the steps of:
   receiving said electrical sensor output signals;
   processing said sensor output signals in a signal processor for generating a state variable vector \( X_n \) representing the dynamic motion of the vehicle's suspension and body;
   inputting said state variable vector \( X_n \) into a vehicle controller having a feedback gain regulation matrix \( G_n \) corresponding to vector \( X_n \) defining predetermined vehicle body and suspension stiffness and damping characteristics; and
   calculating \( U_{dy} \) for input to said actuator controller from the following equation:
   \[
   U_{dy} = -G_n (X_n)
   \]

51. The method of Claim 50 wherein said signal processing step further includes the step of estimating at least one state variable of said state variable vector \( X_n \) prior to input into said vehicle controller.

52. The method of Claim 50 wherein said step of estimating state variables includes:
   derivating suspension displacement sensor output signals for deriving estimated suspension velocity state variables;
   integrating acceleration sensor output signals for estimating body velocity state variables; and
   integrating said estimated body velocity state variables for estimating body displacement state variables.
53. The method of Claim 50 wherein said step for calculating \( U_{\text{dyn}} \) further includes the step of adaptively modifying said gain matrix \( G_n \) in response to changes in the frequency and amplitude of the vehicle's suspension velocity.

54. The method of Claim 53 wherein said gain modifying step includes the steps of:
   - inputting suspension velocity state variables from said signal processor into a disturbance identifier;
   - identifying disturbances represented by variations in frequency and amplitude of the suspension velocity state variables;
   - calculating a gain weighting coefficient \( (\alpha) \) for each corner of the vehicle;
   - calculating a linear combination "G" of a first feedback gain matrix \( G_{\text{soft}} \) and a second feedback gain matrix \( G_{\text{firm}} \) according to the equation:
     \[
g = (1-(\alpha))G_{\text{soft}} + (\alpha)G_{\text{firm}}
\]
   Where: \( 0 < (\alpha) < 1 \); and
   - inputting said linear combination "G" into said vehicle controller for use in calculating \( U_{\text{dyn}} \).
55. The method of Claim 54 wherein said step of calculating a gain weighting coefficient comprises the steps of:

- filtering said suspension velocity signals;
- sampling said suspension velocity signals;
- rectifying said filtered and sampled signal; and
- saturating said rectified signal for maximizing the output value to 1 such that the magnitude of said gain weighting coefficient (c₁) is about zero for frequencies near the natural frequency of the vehicle body and about one for frequencies near the natural frequency of the suspension.

56. The method of Claim 48 wherein said actuating steps associated with said actuator controller include generating an actuator force $F_{\text{actuator}}$ according to the equation:

$$F_{\text{actuator}} = F_{\text{acc}} + F_{\text{piston}}$$

Where:

- $F_{\text{piston}} = C Q_{\text{piston}}$
- $Q_{\text{piston}} = Q_{\text{rel}} + Q_{\text{serv}}$
- $Q_{\text{rel}} = \frac{V_{\text{rel}}}{A_{\text{piston}}}$
- $F_{\text{acc}} = P_{\text{acc}} A_{\text{rod}}$
- $P_{\text{acc}} = \text{Konst}/V_{\text{acc}}$
- $F_{\text{piston}} = \text{Actuator force from piston}$
- $C = \text{Flow characteristic of piston valve}$
- $Q_{\text{com}} = \text{Commanded setting of valve}$
- $Q_{\text{piston}} = \text{Hydr. flow through piston valve}$
- $Q_{\text{rel}} = \text{Hydr. flow by suspension velocity}$
- $Q_{\text{serv}} = \text{Hydr. flow from servo valve}$
- $Q_{\text{com}} = \text{Commanded flow}$
- $F_{\text{acc}} = \text{Actuator force from accumulator pressure}$
- $P_{\text{acc}} = \text{Accumulator pressure}$
- $V_{\text{acc}} = \text{Volume of gas in accumulator}$
57. The method of Claim 56 wherein said variable flow restriction has variable range of control between a low flow restriction limit (C_{soft}) and a high flow restriction limit (C_{firm}), the flow restriction characteristic (C') is determined according to the equation C' = (U - F_{acc})/Q_{rel} wherein controlling actuation of said flow restriction and said flow control means includes the steps of:

setting said flow restriction to C' when C_{soft} < C' < C_{firm} whereby the desired actuator force is generated by selective adjustment of said flow restriction;

setting said flow restriction to C_{firm} when C' < 0 and concurrently actuating said flow control means to selectively add fluid to said first portion of said working chamber during an expansion stroke and exhausting fluid during a compression stroke, and wherein said flow restriction is set to C_{firm} to minimize the flow requirement of said flow control means;

setting said flow restriction to C_{soft} when C' < C_{soft} and concurrently actuating said flow control means for decreasing the flow through said flow restriction, such that during an expansion stroke said flow control means is actuation to add fluid to said first portion of said working chamber and during a compression stroke said flow control means is actuation to exhaust fluid from said first portion of said working chamber, and wherein said flow restriction is set to C_{soft} to minimize the flow requirement of said flow control means; and

setting said flow restriction to C_{firm} when C' > C_{firm} such that said flow restriction is not sufficient to generate the
desired output force whereby said flow control means is actuated to increase flow through said flow restriction, said flow control means is actuated to exhaust fluid from said first portion of said working chamber during an expansion stroke, and said flow control means is actuated to add fluid to said first portion of said working chamber during a compression stroke of said actuator.
58. A method of adapting the gains of a full feedback control system for an active suspension system, said system having an actuator connected between the sprung and unsprung mass of the vehicle, said method comprising the steps of:

providing a closed-loop dynamic leveling control circuit adapted to receive output signals from a plurality of transducers for generating a state variable vector \( X_n \) defining the velocity and displacement of the vehicle's sprung and unsprung mass, said dynamic leveling control circuit having a feedback gain matrix \( G_n \) defining stiffness and damping characteristics based on predetermined vehicle performance requirements so as to generate a demanded output force \( U = G_n (X_n) \);

identifying disturbances represented by variations in the frequency and amplitude of the vehicle's relative suspension velocity;

calculating a gain weighting coefficient \((\alpha)\) based on the frequency content of said disturbances;

calculating a linear combination matrix "\( G \)" of a first feedback gain matrix \( G_{soft} \) and a second feedback gain matrix \( G_{firm} \) according to the equation

\[
g = (1 - (\alpha))g_{soft} + (\alpha)g_{firm} \text{ where: } 0 < (\alpha) < 1;
\]

inputting said weighted linear combination "\( G \)" into said feedback gain matrix \( G_n \) for continuously calculating modified demanded output force signals "\( U \)".
59. The method of Claim 58 wherein said step of calculating a linear combination matrix "G" is provided for continuously changing the dynamic behavior of the vehicle following identification of said disturbance.

60. The method of Claim 58 defining a full feedback gain adaption circuit for adjusting the feedback gains for increasing and decreasing suspension damping characteristics associated with said first feedback matrix $G_{\text{soft}}$ and said second feedback matrix $G_{\text{firm}}$, said first feedback matrix $G_{\text{soft}}$ adapted for relatively soft damping of the vehicle suspension for providing a smooth ride and said second feedback matrix $G_{\text{firm}}$ adapted for providing firm damping of the vehicle suspension for improved road holding.

61. The method of Claim 60 wherein said step of calculating a gain weighting coefficient ($\alpha$) includes:

filtering and sampling disturbance input signals representative of the frequency and amplitude of said suspension velocity;

rectifying said filter signal; and

saturating said rectified signal for maximizing the output to 1 wherein said gain weighting coefficient ($\alpha$) is scaled to be within the range of 0 to 1 such that ($\alpha$) has a magnitude of about 0 for frequencies near the natural frequency of the vehicle sprung mass and a magnitude of about 1 for frequencies near the natural frequency of the unsprung mass.
62. The method of Claim 61 wherein said gain weighting coefficient $C$ varies continuously with the frequency content of the vehicle's wheel motion and amplitude.

63. The method of Claim 62 wherein said step of filtering of said suspension velocity input signal is performed by passing the signal through an under-damped high-pass filter tuned to a maximum amplification at about the wheel resonant frequency and having a sampling rate of about 125 Hz for providing relatively small incremental changes in the gains.
64. A dynamic leveling control system for a low power fully active suspension system for generating a commanded force output signal "U" for input to an actuator controller system, comprising:

sensor means for sensing the dynamic motion of the suspension and body of a vehicle and generating sensor output signals in response thereto;

signal processing means for processing said sensor output signals so as to generate a state variable vector $X_n$ representing the dynamic motion of said vehicle's suspension and body, said signal processing means including estimating means for estimating at least one state variable of state variable vector $X_n$ from said sensor output signals;

vehicle controller means having a feedback gain matrix $G_n$ defining stiffness and damping characteristics for said state variable vector $X_n$ based on predetermined vehicle dynamic performance requirements such that said vehicle controller means receives an output from said signal processing means for calculating "$U_{dyn}$" according to the following state matrix equation:

$$U_{dyn} = -G_n(X_n).$$

65. The dynamic leveling control system of Claim 64 wherein said control system is a closed-loop full feedback gain regulation controller.
66. The dynamic leveling control system of Claim 65 wherein said feedback gains of said gain matrix $G_n$ are determined by the pole placement design method such that the location of the poles is defined by said predefined vehicle performance requirements such that said feedback gains represent stiffness and damping characteristics acting on said vehicle body.

67. The dynamic leveling control system of Claim 65 wherein said sensor means include a relative position sensor located at each corner of the vehicle between the suspension and body for measuring the relative displacement of the suspension, and accelerometer means adapted for measuring the heave, pitch and roll acceleration of the vehicle body.

68. The dynamic leveling control system of Claim 67 wherein said state variable vector $X_n$ has fourteen state variables for defining the dynamic motion at each corner of said vehicle, wherein:

$x_1 = \dot{z}$, heave velocity of C. G.  
$x_2 = \theta$, Pitch angular velocity  
$x_3 = \phi$, Roll angular velocity  
$x_4 = \text{Left Front suspension vel.}$  
$x_5 = \text{Right Front suspension vel.}$  
$x_6 = \text{Right Rear suspension vel.}$  
$x_7 = \text{Left Rear suspension vel.}$  
$x_8 = Z$, heave displacement  
$x_9 = \theta$, Pitch angle  
$x_{10} = \phi$, Roll angle  
$x_{11} = \text{LF suspension displ.}$  
$x_{12} = \text{RF suspension displ.}$  
$x_{13} = \text{RR suspension displ.}$  
$x_{14} = \text{LR suspension displ.}$

69. The dynamic leveling control system of Claim 67 wherein said estimating means is an observer for estimating state variables $X_1$ through $X_{10}$ from said output signals from said position sensors and said accelerometer means.
70. The dynamic leveling control system of Claim 69 wherein said estimating means includes derivating filter means for derivating the suspension displacements $X_{11}$ through $X_{14}$ measured by said position sensors for estimating suspension velocities $X_4$ through $X_7$, and wherein said derivating filter means is scaled to act as a derivator at relatively low frequencies.

71. The dynamic leveling control system of Claim 70 wherein said estimating means further comprises first integrating filter means for integrating the heave, pitch and roll accelerations sensed by said accelerometer means to estimate body velocities $X_1$ through $X_3$, and wherein body displacement state variables $X_3$ through $X_{10}$ are estimated using second integrating filter means for integrating the estimated body velocities $X_1$ through $X_3$.

72. The dynamic leveling control system of Claim 65 wherein said central control system further comprises gain adaptation means for continuously modifying said feedback gain matrix $G_n$ such that the feedback gains corresponding to damping of the vehicle suspension are modified in response to changes in frequency and amplitude of the suspension velocity.
73. The dynamic leveling control system of Claim 72 wherein said gain adaption means is a closed-loop system comprised of disturbance identifier means for identifying disturbances represented by variations in frequency and amplitude of the vehicle suspension velocity and for continuously calculating a gain weighting coefficient \((\alpha)\) based thereon corresponding to each corner of said vehicle, said closed-loop system further comprising gain tuner means for receiving said gain weighting coefficient from said disturbance identifier means and calculating a linear combination "\(G\)" of a first feedback gain matrix \(G_{\text{soft}}\) and a second feedback gain matrix \(G_{\text{firm}}\) according to the equation

\[
g = (1-(\alpha))g_{\text{soft}} + (\alpha)g_{\text{firm}}
\]

Where: \(0 < (\alpha) < 1\).

74. The dynamic leveling control system of Claim 73 wherein the first feedback matrix \(G_{\text{soft}}\) is adapted for relatively soft damping of said vehicle suspension for providing a smooth ride and said second gain matrix \(G_{\text{firm}}\) is adapted for providing firm damping of said vehicle suspension with the objective to improve road holding and minimize relative displacement between the body and suspension.
75. The dynamic leveling control system of Claim 74 wherein said gain weighting coefficient (α) is scaled to be within the range of (0-1) such that (α) is about 0 for frequencies near the natural frequency of the vehicle body and (α) is about 1 for frequencies near the natural frequency of the suspension.

76. The dynamic leveling control system of Claim 75 wherein said disturbance identifier means receives estimated suspension velocity signals from said signal processor means such that said suspension velocity signals are inputted into high-pass filter means for filtering and sampling said velocity signal, said disturbance identifier means also includes rectifying means for rectifying the filtered signal received from said high-pass filter means and saturation means for maximizing the rectified output value to 1.
\[ U = g_1 \dot{x}_b + g_2 x_b + g_3 \dot{x}_w + g_4 x_w + g_5 x_{road} \]

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SUBSTITUTE SHEET
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For Power Dissipation (Quarter I and III)

\[ U = 0 \]

For Power Demand (Quarter II and IV)
\[ U = g_1 \cdot \dot{x}_b + g_2 \cdot x_b \]

\[ U = g_1 \cdot \dot{x}_b + g_2 \cdot x_b + g_3 \cdot \dot{x}_w + g_4 \cdot x_w + g_5 \cdot x_{road} \]
**Principle Layout Of The Low Power Active Suspension Hardware**

\[ F_{\text{actuator}} = F_{\text{acc}} + F_{\text{piston}} \]
\[ F_{\text{piston}} = C \cdot Q_{\text{piston}} \]
\[ Q_{\text{piston}} = Q_{\text{rel}} + Q_{\text{serv}} \]
\[ Q_{\text{rel}} = V_{\text{rel}} \cdot A_{\text{piston}} \]
\[ F_{\text{acc}} = P_{\text{acc}} \cdot A_{\text{rod}} \]
\[ P_{\text{acc}} = \text{Konst} / V_{\text{acc}}^k \]

- \( F_{\text{piston}} \): Actuator Force From Piston
- \( C \): Characteristic Of Damper Valve
- \( C_{\text{com}} \): Commanded Setting Of Valve
- \( Q_{\text{piston}} \): Hydr. Flow Through Piston
- \( Q_{\text{rel}} \): Hydr. Flow By Susp. Vel.
- \( Q_{\text{serv}} \): Hydr. Flow From Servo Valve
- \( Q_{\text{com}} \): Commanded Flow
- \( F_{\text{acc}} \): Actuator Force By Acc. Press.
- \( P_{\text{acc}} \): Accumulator Pressure
- \( V_{\text{acc}} \): Volume Of Gas In Acc.
13/17

Road Profile (m) Vs. Time

Bump

0.05 m

2 m

Suspension Velocity (m/s)

(m/s)

-1

-0.5

0

0.5

1

1.5

0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1

Sec.

ALFA

Filter Coefficients:

K = 2, ω₀ = 59 rad/s, ε = 0.25

T = 0.064 sec

G_{firm}

1

0.9

0.8

0.7

0.6

0.5

0.4

0.3

0.2

0.1

0

0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1

Sec.

G_{soft}

α

ALFA

Time History Of Alfa When Passing A Bump At 40 km/h.
The System Is In Rest At Time 0.
The Commanded Force $U$ Vs. The Relative Flow.

$Q_{serv} = 0 \rightarrow Q_{piston} = Q_{rel}$

The Commanded Force $U$ Vs. The Relative Flow.

$Q_{piston} = Q_{rel} + Q_{serve}$
Control Scheme For Left Front Actuator

\[ C' = \frac{(U - F_{acc})}{Q_{rel}} \]

\[
\begin{align*}
\text{if } C' < 0 & \quad \text{Then } h = C_{firm} \\
\text{if } C' > C_{firm} & \quad \text{Then } h = C_{firm} \\
\text{if } C' < C_{soft} & \quad \text{Then } h = C_{soft} \\
\text{Else } & \quad h = C' 
\end{align*}
\]

The Gain Adjustment Related To Requirement.

\[ F_{piston} + \frac{1}{h} Q_{piston} + Q_{com} \]

The Control Of The Servo Valve. (\(^\wedge\) Indicates Estimated Variables)

SUBSTITUTE SHEET
Piston Force \((U-F_{acc})\) Vs. Relative Flow \(Q_{rel}\) [\(m^3/s\)] At 2Hz Heave Road Input

The Flow From The Servo Valve \(Q_{serv}\) At 2Hz Heave Road Input. Positive Flow Is Into the Actuator.
Piston Force Vs. Relative Flow For Heave Road Input At
Frequencies:  A: 1 Hz,  B: 3 Hz,  C: 9 Hz
### III. DOCUMENTS CONSIDERED TO BE RELEVANT

<table>
<thead>
<tr>
<th>Category</th>
<th>Citation of Document, with indication, where appropriate, of the relevant passages</th>
<th>Relevant to Claim No.</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>US, A, 4,747,615, (Yamamoto), 31 May 1988</td>
<td>1,29,58</td>
</tr>
<tr>
<td>A</td>
<td>US, A, 4,825,370, (Kurosawa), 25 April 1989</td>
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<td>A</td>
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<td>A,P</td>
<td>US, A, 4,967,360, (Fukunaga et al.)</td>
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<td>1,29,48,64</td>
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<tr>
<td>A,P</td>
<td>US, A, 4,975,849, (Ema), 04 December 1990</td>
<td>64</td>
</tr>
</tbody>
</table>

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  "4" document member of the same patent family

### IV. CERTIFICATION

Date of the Actual Completion of the International Search: 09 May 1991

Date of Mailing of this International Search Report: 28 Jun 1991

International Searching Authority: ISA/US

Signature of Authorized Officer: [Signature]

Form PCT/ISA/210 (second sheet) (Rev. 11-87)