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## [57]

## ABSTRACT

This application describes an impedance-matching network comprising two transformers having turns ratios, $1: N$ and $1: M$, where N and M are rational numbers. The first of these transformers senses the signal current flowing in the signal wavepath and induces a secondary current that is proportional thereto. The secondary current, thus induced, energizes the second transformer which injects into said wavepath a component of current that is proportional to the signal current by a factor equal to the product of the turns ratios of the two transformers. When at least one of the two transformers is a two-winding transformer, the effective turns ratio of this network is given by $1: 1 \pm 1 /(\mathrm{NM})$, where the $\operatorname{sign}( \pm)$ is determined by the manner in which the transformers are connected. When two, single-winding transformers, such as autotransformers, are used, the effective turns ratio is given by 1 : $[(\mathrm{N}-1) / \mathrm{N} \pm 1 / \mathrm{MN}]$.

6 Claims, 6 Drawing Figures


FIG. I


## IMPEDANCE-MATCHING NETWORK

This invention relates to impedance-matching networks.

## BACKGROUND OF THE INVENTION

One of the more common problems encountered in a communication system is how to connect portions of said system having different impedance levels. At the lower frequencies, this is conveniently done with transformers whose turns ratios are such as to provide the required impedance transformation. Using conventional transformers, however, the impedance transformations attainable are a direct function of the square of the transformer turns ratio. At the higher frequencies where the absolute number of turns that can be used is limited by parasitic effects to about five or less, the gradation in impedance levels that can be matched by conventional transformers is, as a result, very coarse. For example, it is virtually impossible to provide an acceptable impedance match between 50 ohms and 75 ohms by means of a single transformer when the number of turns that can be used in the primary and secondary of said transformer are thus limited.

It is, accordingly, the broad object of this invention to extend the range of impedance matches that can be obtained by means of transformers.

## SUMMARY OF THE INVENTION

In accordance with the present invention, the range of impedance transformations that can be obtained by means of transformers is greatly extended by using two transformers having turns ratios of $1: \mathrm{N}$ and $1: \mathrm{M}$. The first of these transformers senses the signal current flowing in the signal wavepath and induces a secondary current that is proportional thereto. The secondary current, thus induced, energizes the second transformer which injects into said wavepath a component of current that is proportional to the signal current by a factor equal to the product of the turns ratios of the two transformers. Designating the transformer turns ratios as $1: N$ and $1: M$, respectively, the effective turns ratio of the two transformers, connected in the manner described, is of the form $1: A \pm$ $1 /(N M)$, where $A$ is a parameter which depends upon the type of transformers used, and the sign $( \pm)$ is determined by the manner in which the transformer windings are connected.
In one embodiment of the invention to be described in greater detail hereinbelow, two, two-winding transformers are used. One winding of the first of said transformers is connected in series with the wavepath, while one winding of the second of said transformers is connected in shunt with the wavepath. The other windings of said transformers are connected in series with each other.

In alternate embodiments of the invention, one or the other of said transformers is a single-winding transformer. In all of these configurations $A=1$, and the effective turns ratio is given by $1: 1 \pm 1 / \mathrm{MN}$.
In an alternate embodiment of the invention, in which both transformers are single-windings transformers, $\mathbf{A}=(\mathrm{N}-1) / \mathrm{N}$, and the effective turns ratio is given by $1:[(\mathrm{N}-1) / \mathrm{N} \pm 1 / \mathrm{MN}]$. As a result, it is an advantage of the present invention that very fine changes in the impedance transformation ratio can be realized by making relatively coarse changes in the turns ratios of either or both of said transformers or by cascading pairs of transformers connected in the manner described.
These and other objects and advantages, the nature of the present invention, and its various features, will appear more fully upon consideration of the various illustrative embodiments now to be described in detail in connection with the accompanying drawings.

## BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 shows a transmission system including two portions having unequal impedance levels coupled together by means of an impedance-matching network;

FIG. 2 shows a first embodiment of an impedance-matching network in accordance with the invention, using two, twowinding transformers;

FIG. 3 illustrates a cascade of two impedance-matching networks of the type shown in FIG. 2;
FIGS. 4 and 5 show second and third embodiments of the invention wherein one of the transformers is an autotrans5 former; and

FIG. 6 shows a fourth embodiment of the invention in which both transformers are autotransformers.

## DETAILED DESCRIPTION

Referring to the drawings, FIG. 1 shows, in block diagram, an electrical transmission system comprising a first wavepath 10 , characterized by an impedance level $Z_{1}$, coupled by means of an impedance matching network 12, to a second wavepath 11, characterized by an impedance level $Z_{2}$. In general, the impedance matching network can be any one of the variety of such networks known in the art. In particular, the present invention relates to the use of transformers as impedance matching devices.

As is known, the impedances coupled to the two windings of a transformer are matched when the turns ratio of said windings, $1: N$, is related to the impedance ratio, $Z_{1}: Z_{2}$, such that

$$
\begin{equation*}
\left.\left(Z_{1}\right) / Z_{2}\right)=(1 / N)^{2} \tag{1}
\end{equation*}
$$

As an example, let us consider a $50: 75$ ohm matching transformer which requires a $1: 1.225$ turns ratio. Choosing $M=3 / 2$ and $\mathrm{N}=3$, a transformer in accordance with the invention was built at VHF having a turns ratio of

$$
1+\frac{1}{\left(\frac{3}{2}\right) \cdot(3)}=1.222
$$

This transformer provides a greater than 30 db return loss 70 over the 0.5 to 20 MHz band for which it was designed.

It will be noted that the above-described transformer configuration has the effect of removing the restriction that only impedance transformation ratios that are proportional to the transformer turns ratio can be realized with iron-core transfor5 mers. This softening of the restrictions on the impedance
ratios that can be matched by means of such transformers can be extended further by cascading networks, as illustrated in FIG. 3. In this arrangement, the first network 30, comprising transformers 32 and 33, produces the equivalent of a $1: 1 \pm$ $1 /\left(\mathrm{N}_{1} \mathrm{M}\right)$ turns ratio. The second network 31, comprising transformers 34 and 35 , produces the equivalent turns ratio $1: 1 \pm 1 /\left(\mathrm{N}_{2} \mathrm{M}_{2}\right)$. Together, the cascaded pair produce an equivalent turns ratio given by

$$
\begin{equation*}
1: T=1:\left(1 \pm \frac{1}{N_{1} M_{1}}\right)\left(1 \pm \frac{1}{N_{2} M_{2}}\right) \tag{3}
\end{equation*}
$$

More generally, the turns ratio for $n$ cascaded sections is

$$
\begin{equation*}
1: T=1: \prod_{j=1}^{n}\left(1 \pm \frac{1}{N_{j} M_{j}}\right) \tag{4}
\end{equation*}
$$

In the special case where $n=2, \mathrm{~N}_{1} \mathrm{M}_{1}=\mathrm{N}_{2} \mathrm{M}_{2}$, and wherein we select the positive sign for one network and the negative sign for the other network, equation (4) reduces to

$$
\begin{equation*}
1: T=1: 1-(1 / \mathrm{NM})^{2} \tag{5.}
\end{equation*}
$$

Since $1 / \mathrm{NM}$ can have values close to unity, extremely fine variations in the net effective turns ratio can be obtained by cascading such networks in the manner described.

FIG. 4 shows a second embodiment of the invention wherein one of the transformers is a single-winding transformer, such as an autotransformer. In this particular illustration, the series-connected, signal-sensing transformer 41 is a two-winding transformer and the shunt-connected transformer 40 is the autotransformer. As shown, one end 48 of secondary winding 45 of transformer 41 is connected to the lower end 49 of transformer 40 and to wavepath conductor 43. The other end 47 of winding 45 is connected to a tap on transformer 40.

In the embodiment of FIG. 5, the series-connected, signalsensing transformer 50 is a single-winding transformer and the shunt-connected transformer 51 is a two-winding transformer. One wavepath conductor 52 connects to a tap on transformer 50. The latter is, in turn, connected in series with the primary winding 54 of transformer 51 . In addition, one end 56 of transformer 50 constitutes one of the output wavepath conductors to which secondary winding 57 of transformer 51 connects. The other end of winding 57 connects to the other wavepath conductor 53.

FIG. 6 shows a fourth embodiment of the invention in which both transformers are single-winding transformers. As in FIG. 5 , one wavepath conductor 62 connects to a tap on the seriesconnected transformer 60 . One end 63 of transformer 60 , constituting one of the output wavepath conductors, connects to one end 66 of shunt-connected transformer 61. The other end 67 of transformer 61 connects to the other wavepath conductor 65 while the other end 64 of transformer 60 connects to a tap on transformer 61.

With the transformers connected in the manner indicated, the effective turns ratio $1: T$ is given by

$$
\begin{equation*}
1: T=1:\left(\frac{N-1}{N} \pm \frac{1}{M N}\right) \tag{6}
\end{equation*}
$$

It will be noted that when two, single-winding transformers are used, the first term of the turns ratio is modified slightly from that given by equation (2).

