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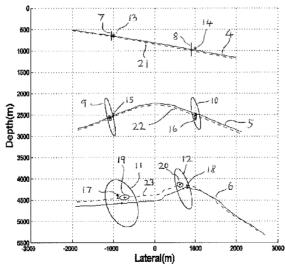


Figure 4

(57) Abstract: A method is provided for forming a geological model of a region of the earth. Seismic data are obtained from the region and include seismic traveltime uncertainty. A seismic velocity model of the region is also provided and includes velocity uncertainty. Ray tracing is performed on the seismic data using the velocity model to determine the three dimensional positions of a plurality of points of the region. The three dimensional positional uncertainties (7-12) of at least some of the points are calculated from the traveltime uncertainty, the velocity uncertainty, and uncertainty in the ray propagation direction. This is combined with the positions determined by the ray tracing to form a geological model.



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Forming A Geological Model

The present invention relates to a method of forming a geological model.

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Seismic traveltime data and well marker data are integrated in every petroleum reservoir for improved knowledge of oil-in-place, hydrocarbon heterogeneities, risk evaluation, and in general for making better decisions about both drilling and drainage strategies. The way seismic and well data are integrated differs dramatically and depends heavily on the main objective of study. To obtain the best out of the data, one must take into account the uncertainty associated with each data type. Consider for instance the thickness of an oil reservoir; One data source (wells) tells you it is 30m, the second (seismic) says 50m. How much is this reservoir worth in terms of net present value? Should we start producing hydrocarbons? If the critical thickness based on the cost and expected revenues is 40m, we would have to trust the first source less than the second to start production.

Seismic data are acquired by emitting sound from a source such as an air gun and then monitoring the reflected signal at a set of receivers. There is a huge literature on converting such reflection data to a structural model for the subsurface, represented in (east, north and depth) coordinates. The most common method is to process manually picked reflection times (traveltimes) from main geological interfaces by collecting them to fixed surface reference positions, and then stretching the traveltimes (measured in seconds) according to a priori known velocity. One caveat with this method is its lack of ability to capture the three dimensional uncertainty in the structural model. Another is the implicit assumption that each surface reference point represents a reflection point directly underneath, and not from another reflector to the east or north of the surface location. The second assumption (referred to as 'vertical stretch' since only the depth dimension is influenced in the structural imaging) can be bypassed with more complicated depth conversion methods, for instance by using ray tracing, but the problem of capturing the three dimensional structural uncertainty remains.

Well marker data consists of geographical (east, north, depth) picks as the well goes through a geological marker. These markers typically include the interfaces detected on seismic data. Traditionally, well data have been treated as fixed, known measurements, or at least relatively so compared to the noisy seismic data. However,

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with the aid of modern computers, seismic processing is more reliable and the signal to noise ratio is improved. At the same time, well technology has caused a major increase in the number of deviated and deep (5 km depth) wells. The measured positions of wells are then less reliable. This means that the well marker data cannot be treated as fixed, known geographical positions, simply used to scale the seismic data from time to depth domain. Nowadays, the uncertainties of well marker positions logged while drilling and vary according to the equipment used. This has improved the risk analysis during drilling operations. The main limitation of current technology is including the well marker position and position accuracy into the broader picture of three dimensional positioning. This entails integrating the geographical reference interfaces in east, north, depth coordinates from well markers with the seismic reflection data. Wells are sparse (10-50 wells per oil field) and carry little information about the lateral continuity of a reservoir. Seismic data, on the other hand, are abundant and laterally informative, but are not directly comparable at the well marker east, north, depth scale.

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Optimal methods for integrating diverse data at a common scale are known. This is text book statistics, in broad terms referred to as least squares estimation. Tools for representing seismic data in east, north and depth coordinates and integrating these data with geographical well marker data have been lacking, particularly at the level where one can deduce the three dimensional positioning uncertainty. The traditional way of updating is in the vertical direction. For almost flat horizons, this gives a reliable method but, for dipping layers, curved surfaces or faults, this can introduce bias. Methods for orthogonal shifting of dipping surfaces have been proposed, but this is still an ad-hoc technique that does not capture intrinsic direction variability that can actually be physically modelled using, for instance, ray-tracing. Moreover, consistent assessment of uncertainties is important to make fast decisions in high dimensional reservoir systems. The current state of the art is driven by a search for the 'best' structural model, without controlling the data going into the estimation. Hence, updating the geographical model is by current standards a tedious process with too much work being done on reiterating the data and trying to match information that cannot be unified.

EP1306694 discloses a method of combining first and second models of a common region of space, such as a region of the earth below the surface, to form a third model. Common points have different positions in the first and second models. A

predetermined correlation exists between the positions of the common points in the first model and the positions of points of interest in the first model. The positions of the common points in the third model are derived from the common point positions in the first and second models. The positions in the third model of the points of interest are derived from the positions of the common points in the third model and from the predetermined correlation.

GB 2352746A discloses a method of producing impact point position probability maps for a well. A fixed target point is defined at an initial location of a surface with the aid of a grid composed of nodes and of grid cells. An uncertainty vector is assigned to each node and is determined by applying a Monte-Carlo statistical method. When the values for all nodes have been calculated, a resulting occurrence of location is found. A target point is projected onto each occurrence of location so as to determine a point of impact. The distribution for the set of input points is transferred to the surface and the density of the impact points gives the probably that any point of the surface is a point of impact. The probability density is mapped as level curves.

GB2325523A discloses a method of producing maps of the risks in positioning a well in an environment. The method uses a first interpreted horizon extracted from a seismic block migrated with at least a first value of velocity including a velocity uncertainty. A second interpreted horizon is formed by migration of the first horizon using a second value of the velocity equal to the first value plus the uncertainty. A third interpolated horizon is formed by migration of the first horizon using a third value of velocity equal to the first value minus the uncertainty. A positioning point for the well is selected on the first horizon and a vertical is plotted which passes through the point and intersects the second and third horizons at migrated points. On the second interpreted horizon, the positions are determined corresponding to the migrated points, the first portion of the interpreted horizon located between the said positions constituting the locus of the potential positions of the well for the uncertainty.

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WO97/38330 discloses a 3-D geological modelling technique.

US 2004/0220789A1 discloses a method of calculating meshed realisations of a hydrocarbon reservoir.

According to a first aspect of the invention, there is provided a method of forming a geological model of a region of the Earth, comprising the steps of:

- "i." providing seismic data obtained from the region and including seismic travel time uncertainty;
- "ii." providing a seismic velocity model of the region including velocity uncertainty;
 - "iii". performing image ray tracing on the seismic data using the velocity model to determine the three dimensional positions of a plurality of points of the region;
 - "iv." calculating three dimensional positional uncertainties of at least some of the points from the travel time uncertainty, the velocity uncertainty and uncertainty in ray propagation direction; and
 - "v." combining the positions determined in the step "iii" with the uncertainties calculated in the step "iv" to form a first geological model.
- At least some of the points may be disposed at at least one interface, identified from the seismic date, between sub-regions of the region of different seismic velocities.
 - At least some of the points may be disposed at faults identified from the seismic data.
- 20 The travel time uncertainty may be determined from the seismic wavelength used to obtain the seismic data.

The velocity uncertainty may be determined from knowledge of the geology of the region.

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The step "iii" may comprise determining the position of each of the points as a function of: the position at a shallower interface where a ray incident at the point intersects the shallower interface: the seismic velocity from the position to the point obtained from the velocity model; and the travel time from the position to the point obtained from the seismic data. The step "iv" may comprise differentiating the function. The function may include a first sub-function representing Snell's law and a second sub-function representing dip at the position and the step "iv" may comprise determining the derivatives of the first and second sub-functions.

35 The step "v" may include assigning correlations among at least some of the points.

The method may further comprise assigning correlations among velocity values in the velocity model.

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"vi" providing non-seismically obtained three dimensional position data and three dimensional positional uncertainty data about the region; and

"vii" adjusting the first geological model by means of the data provided in the step "vi" to obtain a second geological model. The non-seismically obtained data may comprise well marker data.

The step "vii" may comprise selecting at least one common point of the region which is common to the first geological model and to the non-seismically obtained data and determining the position and the positional uncertainty of the common point in the second geological model from the positions and the positional uncertainties of the common point in the first geological model and in the non-seismically obtained data. The at least one common point may represent common or adjacent geological features. The at least one common point may represent a location on one interface in the first geological model and a location in the non-seismically obtained data where a well passes through the interface. The step "vii" may comprise moving the location of the common point in the first geological model substantially parallel to a ray path at or adjacent the location.

The at least one common point may represent a location on a fault in the first model and a location in the non-seismically obtained data where a well passes through the fault. The step "vii" may comprise moving the location of the common point in the first geological model substantially perpendicularly to the fault surface.

The method may further comprise updating the non-seismically obtained data by moving the location of the common point in the non-seismically obtained data in a direction substantially opposite the direction of movement in the first geological model.

The step "vi" may comprise providing non-seismically obtained velocity data and velocity uncertainty data about the region. The method may further comprise forming

and/or updating the velocity model in accordance with the non-seismically obtained velocity and velocity uncertainty data.

The step "vii" may be performed with a constraint that interface/fault intersections are preserved in the second geological model.

The step "vii" may comprise selecting a plurality of common points and adjusting the first geological model in a single step.

The step "vii" may comprise adjusting the first geological model in a first step, in respect of the at least one common point on the interface, and then in a second step, in respect of the at least one common point on the fault.

The step "vii" may comprise adjusting the first geological model recursively layer by layer.

According to a second aspect of the invention, there is provided a computer program arranged to program a computer to perform a method according to the first aspect of the invention.

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According to a third aspect of the invention, there is provided a computer containing or programmed by a program according to the second aspect of the invention.

According to a fourth aspect of the invention, there is provided a computer-readable storage medium containing a program according to the second aspect of the invention.

According to a fifth aspect of the invention, there is provided transmission of a program according to the second aspect of the invention.

According to a sixth aspect of the invention, there is provided a method of drilling a bore in a region of the earth, comprising performing a method according to the first aspect of the invention and controlling drilling in accordance with the geological model.

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It is thus possible to provide a technique which provides improved knowledge of the geology of a region of the earth. This may be used, for example, to allow better decisions about drilling and drainage strategies to be made.

5 The invention will be further described, by way of example, with reference to the accompanying drawings, in which:

Figure 1 is a graph of seismic traveltime in milliseconds against lateral distance in metres illustrating three subsurface horizons picked from the seismic traveltime data;

Figure 2 is a graph of depth in metres against lateral distance in metres illustrating the result of ray tracing on the data shown in Figure 1;

Figure 3 is a graph of depth in metres against lateral distance in metres showing interfaces between layers obtained from the data shown in Figure 2 and 95% uncertainty ellipsoids;

Figure 4 is a graph similar to Figure 3 showing the interfaces and ellipsoids of Figure 3 and the interfaces and ellipsoids after processing by a method constituting an embodiment of the invention;

Figure 5 illustrates diagrammatically the selection of common point pairs at a horizon;

Figure 6 illustrates diagrammatically updating a geological model using a constraint in the incident ray direction of a common point pair;

Figure 7 illustrates diagrammatically the selection of common point pairs at a fault;

Figure 8 illustrates diagrammatically updating a geological model using a constraint in the fault surface normal of a common point pair;

Figures 9a to 9c are diagrams illustrating different types of seismic velocity models; and

Figure 10 is a diagram illustrating constraining of the velocity model and hence the geological model based on well bore velocity measurements.

- 30 In a method constituting an embodiment of the invention, the inputs required are
 - i) Seismic traveltime data for the horizons and faults of interest. This is given as a number of point locations on a lateral north, east grid. We assume that these data are processed so that they represent the traveltime a seismic wave would use when emitted from the surface point and reflected from the horizon of interest. Such processing is a first step of any seismic

interpretation scheme. The uncertainty associated with traveltime picking can be a default parameter, typically related to the wavelength of the seismic signal, say a standard deviation of 10msec. For faults, the manual picking uncertainty is generally larger, because the signal is weaker and thus more geological interpretations involved.

- ii) Velocity values for each interval in the subsurface. This is taken from a priori geological knowledge. The standard deviation of interval velocity values can also be deduced from a priori notion of uncertainty or homogeneity in the geographical zone of interest. Velocity uncertainty typically increases in deeper intervals. For instance, sea water velocity is 1500m/sec, with standard deviation about 1m/sec. In deep layers, velocity can be 3000m/sec, with standard deviation about 100m/sec.
- iii) Well marker data for all wells going through the main horizons interpreted from seismic traveltime data. The uncertainty of well markers is typically a built-in attribute in data acquisition schemes. For vertical wells, the east, north uncertainties are small; for deviated wells the east, north uncertainties are larger. The uncertainty also depends on the logging equipment used in the well. Common methods for positioning of wells include magnetic instrumentation, gyro devices, and gravitational indicators.

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The outputs from such a method are

- i) Structural model for geographical positions in three dimensions: east, north and depth. This three dimensional position output is an optimal estimate based on the input data and the fixed parameters set from a priori knowledge.
- ii) Structural uncertainty and correlation for all positions in three dimensions: east, north and depth. This output is the standard deviation of the three coordinates of all positions and the correlations between them. Some locations may have a larger uncertainty in the depth direction, whereas others may have a largest uncertainty in the north-east direction. Note that the correlation between two different points is also available, indicating what will happen to point B if point A is shifted in one direction.
- iii) Velocity model constrained by seismic data and well marker information, and correlation between interval velocity and all geographical points in the

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structural model. This indicates what will happen to points if the interval velocity changes.

iv) A unified model in terms of constraints included in the updating. Less need for manual processing.

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Based on the outputs, a number of important decisions can be made, such as optimal placement of wells, distance to target, predicting high pressure zones ahead of the well bore, computing the net present value of oil or gas within a reservoir zone while drilling, model updating in integrated operations, and velocity update for iterated processing of seismic data.

The following example illustrates the method for a relatively simple case with three horizon interfaces, three values of interval velocities and two well markers in each interface. The first step in the method is to convert the seismic time measurements to east, north and depth coordinates with associated uncertainties and correlations. This is done by image raytracing, using the idea that geographical reflection point of time migrated seismic data is located by tracing a ray straight down from the surface. As this ray hits an interface, it bends according to the relative velocity change across the two layers. The transmission angle can then be calculated from Snell's law. Within each layer, the ray is traced for the time indicated by the seismic traveltime data. Altogether, this gives one reflection point at each interface for every surface reference point.

The main steps of the conversion to depth, east, north are as follows: Start in the surface coordinates and step down in depth for the distance indicated by the velocity in the top interval and the time to the first interface 1 shown in Figure 1. At the first interface, there are a number of reflection points. The local dip of the first horizon can be computed using local neighbourhoods of points. This dip and the downgoing ray make the angle of incidence, and Snell's law says that the sine of the angle of transmission is given by the relative velocity difference between the two layers multiplied by the sine of the incidence angle. We use this law to trace a ray from the first interface 1 to the second interface 2, this time using the velocity of the second layer and the time indicated by the seismic traveltime data for this layer.

As shown in Figure 2, the ray is now no longer vertical, unless the velocities in the two layers are equal or the dip angle of the first surface is zero. The process of applying

Snell's law at an interface continues for the second layer, and takes us to geographical points in the bottommost third layer. Figure 1 shows picked seismic traveltime data for the three horizons. The vertical axis is in time (msec). Figure 2 shows the rays going down from the surface and bending at interfaces. The resulting depth converted horizons 4, 5 and 6 are quite different from the horizons 1, 2 and 3 obtained from vertical stretch. This shows the bias imposed by the assumption of no bending at interfaces. Note also that the rays bend more if the local dip is larger. This is a consequence of Snell's law.

In the depth, east, north conversion described above, each depth point is computed as a function of the velocities, traveltime data and from the reflection points in the interfaces in shallower interfaces. The associated uncertainty is calculated by differentiating this functional relationship, i.e. using linearization of the nonlinear functional relations. Error propagation based on the linearized operator is used to propagate the uncertainty in the functional input variable to the output variable. By taking derivatives of all the functional relationships involved in Snell's law and the computation of dip angle, we can thus also compute the standard deviation of all points in depth, the correlation between all points, and the correlation between the interval velocity parameters and all points. In practice, this means that not only are the reflection points calculated as we trace the rays deeper and deeper, but in addition the derivatives of all calculations are carried out. The output from the seismic traveltime conversion is then i) expected reflection points in depth, east and north coordinates, and ii) uncertainty and correlations between all these reflection points and the velocities.

Figure 3 shows the uncertainty of two depth, east and north locations in each layer. These uncertainty ellipsoids 7 to 12 are obtained from traveltime data, using no well information at this stage. These ellipsoids are 95 percent regions, indicating that there is a 95 percent probability that the true reflection point is within this ellipse. Note that uncertainty aggregates as we go deeper and so the ellipses become bigger for the deepest interface. As the rays pass through an area with large dip, the underlying interface gets larger horizontal (east, north) uncertainty. This is natural as the uncertainty is highly connected to the sine of the transmission angle via Snell's law.

Finally, well markers are used along with their associated uncertainty. Before updating the structural model from seismic, we now introduce the concept of 'common points': these are geographical coordinates that are common for well measurements and seismic depth, east and north coordinates. Since neither well marker data nor the points obtained from seismic data are noise free, the common points are not known. Nevertheless, we know that the well marker and the seismic geographical coordinates represent the same geological feature; thus a seismic commonpoint to a well marker can be chosen. We assign constraints to these common points. The constraints are informative about the direction in which the seismic depth, east and north coordinates should be updated. The constraints form a way of integrating the common points and all other points in the model. While the number of points can be several thousand, the number of common points is typically small (around 100 well markers).

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The optimal estimate for geographical positions is calculated as a standard least squares solution, but the notion of common points and three dimensional updating gives an extra degree of flexibility. In particular, updating points along the original ray path seems intriguing. The uncertainty of all points is updated as an intrinsic part of the least squares methodology. This is smallest near common points since there are two sources of information here. It is largest far from common points and at large depths.

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In Figure 4 the well marker data are shown at 13 to 18. The common points are updated and the integrated estimate is marked along with the uncertainty ellipsoids, such as 19 and 20, in Figure 4. Note that the updated uncertainty ellipsoids (19, 20) are smaller than the ones (11, 12) from seismic data alone as the uncertainty of the well picks is quite small in this case. The broken lines in Figure 4 represent the updated horizons 21, 22 and 23 from both seismic data and well picks. These are somewhat shifted from the estimated horizons 4, 5 and 6, respectively, using seismic data alone, but mostly locally due to a correlation window in the statistical model.

In the following, it is assumed that the image ray tracing has been executed, so that all fault and horizon data are converted into north, east and depth coordinates. The velocity model used in the image ray tracing is also present. A covariance matrix describing the uncertainty and the correlations (dependency) of all data, (velocities, spatial seismic positions and well markers), is present. For updating this model using well markers, statistical computation based on least squares mathematics are used.

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The various types of constraints are described below. Any combinations of the types of constraints and numbers of well markers could be used. The statistical update could be executed in three ways.

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- 5 i) An update using all well markers in one go, selecting all common points (described later) from the original ray traced data set.
 - ii) A two step update. First adjust the model using the velocity and horizon well markers. Then calculate the fault common points in the adjusted model, and use these to update the well and horizon adjusted model using the fault well markers.
 - iii) A sequential update. In this form, the model is first adjusted by the well markers belonging to the uppermost horizon and the uppermost velocity layer. Thereafter the resulting model is used to calculate the common points for the well markers for velocities and horizons belonging to the next layer, and adjusted using the well markers belonging to the second layer. This process is continued until all velocities and horizons have been traversed. The model resulting from this process is used to calculate the common points of the fault well markers, and is further adjusted using the fault constraints
- No matter which of these strategies is selected, uncertainty is treated in a coherent way through the adjustment, resulting in updated uncertainties for all inputs, which are derived from all input uncertainties and correlations.

Since a well marker of a horizon is only a single point position, we do not know exactly which seismic horizon point matches it. Assuming that the difference between the two common points is mainly due to inaccuracy in the interval velocities used in the initial ray tracing, the horizon point whose prolonged incidence ray passes closest to the well marker is chosen to be the matching seismic common point to each well marker. These two positions are thus chosen to be a common point pair as shown at 24 and 25 in Figure 5.

To update the seismic model using a common point pair 24, 25, a constraint between the two points is set. As stated earlier, we do not know exactly which seismic horizon point matches the well marker, only that inaccuracy of the along-incidence ray velocity is the most likely cause for the well marker and horizon not intersecting. Due to this

fact, the constraint between the two identified common points is set only in the direction of the ray tracing incidence ray 26 of the selected horizon common point 25. Thus, the update from a single common point pair 24, 25 adjusts the seismic model only in the direction of the incidence ray at the seismic common point. This is shown in Figure 6.

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The update constraints using fault points in the common point pairs differs slightly from the constraints using horizon points. This is basically due to how a fault, such as 30 in Figure 7, is depicted in the seismic. In the original seismic data, the exact location of a fault is not shown; only a blurred area in the seismic data shows that a fault is present somewhere within that area. The seismic interpreter then does his best to interpret the fault into that area based on intuition and prior knowledge and experience. For this reason, the fault point 31 through which the corresponding fault surface normal 32 lies closest to the corresponding well marker 33 is chosen as the seismic point in the common point pair, as shown in Figure 7.

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The constraint between the two common points 31, 33 is to affect only the seismic model in the direction of the fault surface normal 32 through the seismic common point 31, as shown in Figure 8. The adjusted fault position is shown at 34 and the adjusted common point positions at 35 and 36. Other common point pairs may however adjust the model in other directions.

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The image ray tracing uses interval velocities to convert seismic time data to 3D positional data in north, east and depth coordinates. We are thus dividing the full velocity model up in sections in which neighbouring horizons are borders for each interval. Within each such interval, the bedrock velocity is modelled in various ways. For example, as shown in Figure 9a, a single velocity, such as V1 and V2, may be allocated to each interval, such as 40 and 41, and it is assumed that this velocity applies to all points within the interval. Alternatively, a respective velocity Vij may be assigned to each jth trace of the ray tracing within each of ith interval as shown in Figure 9b.

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In another alternative, a set of velocities Vij may be assigned to the jth positions or points, in the ith intervals. The velocity at any arbitrary point may then be found from an interpolation function. For example, the velocity V1X at the point 42 is given by the interpolation function illustrated as F(V11,V12,V13,V14) in Figure 9c. The interpolation

function may, for example, form a weighted average of the velocities at a set of positions in the neighbourhood of the point.

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Measurements of the bedrock velocity are also available from wells drilled through the modelled area. For each such velocity measurement chosen to be a part of the adjusted model, a constraint is set up between the wellbore measurement and the corresponding velocity from the initial seismic velocity model. In the case where the interval velocity is modelled as a set of spatially fixed velocities combined with an interpolation function, the seismic velocity chosen is the velocity modelled through the interpolating function at the point chosen to match the wellbore velocity measurement.

As shown in Figure 10, the velocities V1, V2, V3 measured during drilling through the region may be used in the ray tracing or may be used subsequently to update the seismic model by "correcting" the ray tracing. The updated horizons are shown at 44 to 46. For the example shown in Figure 9a, the velocity in each interval may be made equal to a measured value, or an average of measured values, in the interval. For the examples shown in Figures 9b and 9c, some form of inverse interpolation function may be used to update the model values from the measured values.

- To ensure that intersections between horizons and faults still intersect after the adjustment, constraints between intersecting horizon and fault points can be added, making sure that each selected horizon/fault point pair still intersect after the adjustment.
- 25 Further information about the background to and embodiments of the invention is provided in the following paper.

Introduction

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30 Reliable prediction of subsurface faults and horizons is of major importance for the petroleum industry. Both the best estimates and the uncertainty of positions are of high importance in several decision processes. One such process is well planning where this information influences the shape of well trajectories and also the shape and position of drilling targets (Haarstad et al. 2002; Prange et al., 2004). The positional uncertainty of structures is crucial information both in planning the acquisition of new

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subsurface data for better subsurface understanding, and in the process of planning the drainage strategy of a reservoir. Estimates of horizon and fault positions, as well as their uncertainties, is an important input for prediction of in place volume estimates.

Today most well calibration methods rely on changing the seismic velocity model until it mostly fits a set of well-measured velocities. This is a time consuming process with a lot of human interaction. The misfit between the depth converted model and well markers is then corrected using Kriging methods which adjust the depth converted horizons to fit wells only in the vertical direction. Positional uncertainty is similarly calculated only in the vertical direction (Abrahamsen 1992; Abrahamsen and Benth, 2001).

In several cases, the lateral positioning and subsequent uncertainty of structures are of importance for decisions to be made, especially in well planning. Examples of such structures are areas near and in erosion surfaces, areas close to faults, and also where horizons have changing DIP angle. Holden et al. 2003 extend the standard models for treating horizons to also include fault objects, but faults are only modelled using objects moveable in one dimension. In geo modelling, see e.g. (Caumon et al; 2004), it has been common to represent zone boundaries and update these as more data become available. One such technique, based on triangulated surfaces, was presented in Thore et al. 2002, and discussed several aspects of multidisciplinary integration and quantification of uncertainty.

In this paper we present a new method for predicting subsurface horizon and fault positions incorporating lateral and depth position uncertainties with applications to well planning and structural model update. The approach integrates seismic traveltime data and well position markers, and converts these into predicted lateral and depth positions along with associated uncertainties and spatial correlations. Integration of diverse data leads to desirable properties: i) Main lateral structures are maintained in the depth predictions because of the large scale lateral continuity in interpreted seismic data. ii) Important corrections in depth uncertainty and smaller scale fluctuations are incorporated via well picks. Since both seismic data and well data are measured with noise, statistical integration of both data types provides prediction that captures the level of uncertainty of depth and lateral positions.

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The method used in this paper is briefly described as follows. Interpreted seismic traveltime data are converted into depth and lateral positions using ray-tracing (see e.g. Hubral, 1977). Faults and horizons are treated as point objects in three dimensions, but the uncertainty of the fault objects might be different from that of horizon objects due to interpretation issues in seismic processing. Well markers correct the initial seismic depth model using the wellbore position measurements along with a set of constraints for geological boundaries. We use a Gaussian model for positions in 3D and the corrections are made based on the modelled covariance matrices, (see e.g. Cressie, 1993).

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The outline of this document is as follows. We introduce the concept of seismic ray-tracing for time domain to depth domain conversion in Section 2, while the uncertainty calculation associated with this method is presented in Section 3. In Section 4 we describe our proposed model for including fault points. Section 5 is dedicated to well updating of the subsurface model. Several options are discussed for integrating the well marker data. Numerical examples of the methodology are presented in Section 6. The mathematical details are postponed to Appendices.

Seismic Image Ray Migration

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The simplest approach for converting seismic traveltime picks into depth and lateral positions is vertical stretch depth conversion. We then assume that time migration has positioned all reflectors at their correct lateral position and simply stretch the traveltime picks in the vertical direction using interval velocities. A more realistic approach, which is considered here, is to depth convert seismic traveltime picks using image ray tracing (map migration). A ray is then traced downwards for the time indicated by the time migrated data at that particular lateral location. This image ray starts along the vertical axis at the surface and bends at subsurface interfaces according to Snell's law. If time migration has been done correctly, the results after image ray tracing will coincide with that of more sophisticated depth migration. The aspects of seismic depth conversion have been discussed extensively in geophysical literature (Hubral, 1977; Parkes and Hatton, 1987; Black and Brzostowski, 1994;Bube et al., 2004; Kane et al., 2004). The method of choice depends on the geological complexity of the subsurface. The methodology described in this document is meant for geological settings of moderate

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complexity. This means that the simplest vertical stretch might cause bias, but raytracing supposedly is sufficiently realistic.

Suppose have two-way seismic traveltime picks. denoted $k = 1, K, n_h, l = 1, K, m$, where m is the number of picked reflecting interfaces and n_h the number of traveltime picks in each horizon. The case with different number of picks in various layers is possible, but requires some technical details. We return to this topic in chapter 0. Fixed surface locations $(N_{k,0}, E_{k,0}, D_{k,0}), k = 1, K, n_h$, are given as the common depth point locations (inlines / crosslines) used in time processing of seismic data. (The typical case is $D_{k,0} = 0$.) Interval velocities are v_1 , K, v_m . Positions $\left(N_{k,l}, E_{k,l}, D_{k,l}\right)$ are geometric reflection points for the respective traveltime picks $t_{\mathbf{k},l}$. For the topmost geological interface, rays are vertical and reflection positions are represented by

$$\begin{split} N_{k,1} &= N_{k,0} \\ E_{k,1} &= E_{k,0} \\ D_{k,1} &= D_{k,0} + \frac{1}{2} v_1 t_{k,1} \end{split}, \qquad k = 1, \text{K}, n_h. \end{split}$$

which can be written in short form as

$$(N_{k,1}, E_{k,1}, D_{k,1})^T = f_{k,1}[V], \quad V = v_1, K, v_m$$
 (1)

where $f_{k,1}: \Re^m \to \Re^3$, keeping the surface inline and crossline locations and the two-way seismic traveltimes fixed. Arranging all points in the top horizon together gives a vector:

$$h_1 = (N_{1,1}, E_{1,1}, D_{1,1}, K, N_{n,1}, E_{n,1}, D_{n,1})^T$$

For the deeper layers l=2,K, m, the reflection positions are computed using Snell's law at interfaces. If the incidence angle with an interface is θ_i and the velocities in the upper and lower layers are given by v_i and v_{i+1} , respectively, the transmission angle with this interface is $\theta_i = \arcsin\left(\frac{v_{i+1}}{v_i}\sin(\theta_i)\right)$. The reflection points in the lower layer can then be calculated by a nonlinear function of the velocities and the points in the

above layers (giving the incidence angle). Geometric positions are in this way calculated recursively, going deeper at each step. The mathematical relationship can be written in short form as:

The details of this raytracing formulation are postponed to the Appendix. For the understanding of the method, it is important to note that the variables of interest include

- 1) Layer velocities: $V = (v_1, K, v_m)$,
- 2) Positions (north, east and depth) for all horizons: $H = (h_1, K, h_m)$.

These two types of variables will be used for well updating below.

Seismic Uncertainty Propagation

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In this section we describe the method used for calculating the uncertainty in depth converted lateral and depth positions. The calculation is an elementary exercise in mean and covariance calculation under a linearized model. Suppose generally that y=f(x) for some function $f(\cdot)$. In our case this function $f(\cdot)$ is built up of sequential ray tracing defined by equation (2). Suppose further that Σ is the covariance matrix of x. The covariance matrix Ψ of y can be approximated by Taylor expansion and equals $\Psi=F\Sigma F^T$, where $F=\frac{df(x)}{dx}$ is evaluated at the mean value of x. Following this scheme, the expressions in the Equations (1) and (2) can be differentiated to give

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$$F_{k,l} = \frac{\partial f_{k,l} \left[v_1, \mathbf{K}, v_L, (N_{k,j}, E_{k,j}, D_{k,j}), 1 \le j \le l, 1 \le k \le n_g \right]}{\partial \left[v_1, \mathbf{K}, v_L, (N_{k,j}, E_{k,j}, D_{k,j}), 1 \le j \le l, 1 \le k \le n_g \right]} = \frac{\partial f_{k,l} \left[v, h_j, 1 \le j \le l \right]}{\partial \left[v, h_j, 1 \le j \le l \right]}$$

$$= \left\{ \frac{\partial f_{k,l} \left[V, h_j, 1 \le j \le l \right]}{\partial V}, \frac{\partial f_{k,l} \left[V, h_j, 1 \le j \le l \right]}{\partial h_l^T}, \mathbf{K}, \frac{\partial f_{k,l} \left[V, h_j, 1 \le j \le l \right]}{\partial h_l^T} \right\}. \tag{3}$$

Here, many elements will be zero because the predicted geometric positions depend only on a few variables. We collect all columns in Equation (3) as a matrix denoted by F_l . Note that this matrix contains all partial derivatives when predicting positions in layer l from the above layers and the velocity values. This matrix is used to construct the covariance matrix Ψ of the geometric positions in layer l obtained by ray tracing. The uncertainties in velocities are specified initially and the covariance is built sequentially, layer by layer. For the first layer:

$$\boldsymbol{\Psi}_{h,1} = \begin{bmatrix} \boldsymbol{\Sigma}_{V} & \boldsymbol{\Sigma}_{V} \cdot \boldsymbol{F}_{1}^{T} \\ \boldsymbol{F}_{1} \cdot \boldsymbol{\Sigma}_{V} & \boldsymbol{F}_{1} \cdot \boldsymbol{\Sigma}_{V} \cdot \boldsymbol{F}_{1}^{T} + \boldsymbol{\Sigma}_{\varepsilon,1} \end{bmatrix},$$

where $\Sigma_{\scriptscriptstyle V}$ is the specified covariance for velocities, while $\Sigma_{\scriptscriptstyle \epsilon,1}$ is the covariance matrix for traveltime picks in layer 1. We assume that the traveltime picks are spatially correlated according to their distance on the surface and this is represented by a spatial correlation function and a Kronecker product for $\Sigma_{\scriptscriptstyle \tau,1}$. The deeper layers are constructed recursively by

$$\Psi_{h,l+1} = \begin{bmatrix} \Psi_{h,l} & \Psi_{h,l} F_l^T \\ F_l \Psi_{h,l} & F_l \Psi_{h,l} F_l^T + \Sigma_{\varepsilon,l+1} \end{bmatrix}, \qquad l = 1, K, m-1.$$

$$(4)$$

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At l+1=m we have the entire covariance matrix for all layer velocities and geometric positions in the model (north, east and depth).

Modelling of Faults

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In this section we present the approach for integrating faults. The assessment of fault positions in depth coordinates and their position uncertainties can be done in several ways depending on the geological setting. We have focused on 'normal' faults, i.e. faults that dip in the direction of the horizon. For such faults we assume that the points that 'fill' holes in the horizons are merged into the horizons and positioned using ray tracing. These fault positions are referred to as 'merged' points. The remaining fault points are referred to as 'non-merged' points. The non-merged points are positioned based on the depth of merged points and on surface (inline / crossline) positions relative to the merged points in the seismic traveltime data. Fault position uncertainties are mainly assessed from the seismic error propagation, but uncertainty is also added based on the interpreter's prior judgements.

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We briefly describe the mathematical approach used for assessing the non-merged points, assuming that the position of merged points is reliably obtained from ray tracing. Based on the set of 'merged' points, the centre point (N_c, E_c, D_c) , the dip and the azimuth of the fault are calculated. This is obtained by simply calculating the mean of all merged points and the principal components of the merged points. The calculation for principal components goes as follows: Let Ψ_f denote the covariance matrix of the 'merged' fault points, in North, East and Depth coordinates. This subset of points is defined by picking the points that are merged fault points among all points. This matrix is a sub-matrix with indexes picked from Ψ_m in equation (4). The principal components defined by Π with associated singular values Λ are such that:

$$\Psi = \Pi \Lambda \Pi^T \,. \tag{5}$$

From the principal components we can calculate the dip azimuth and dip inclination of the 'merged' fault points. Moreover, we use the centre point and principal components along with the surface reference positions in the time interpretation to assign geometric coordinates to the 'non-merged' fault points. The 'non-merged' points (N_f, E_f, D_f) are given by a functional relationship which in short form is:

$$(N_f, E_f, D_f) = f_f(\Pi, (N_c, E_c, D_c)), \tag{6}$$

where the surface reference locations N_c , E_c , D_c in the interpreted seismic traveltime data are treated as fixed. The function f_f is in this case an inverse of the calculation of the principal components from the 'merged' points.

After the assessment of these fault points, the geological positions can be represented by G = (H, F), where H are the original horizon points without the removed merged fault points, and where F are the fault points, both merged and non-merged. In addition, an associated covariance matrix for all positions is provided. The covariance matrix for H is set from the ray tracing error propagation, while the covariance matrix for F is set using Monte Carlo simulations for this small set of fault points based on the Equations (5) and (6). For the fault points, we also assume that the traveltime picking is quite unreliable and the lateral entries are assigned a large uncertainty to account for this picking uncertainty of faults. We assume no cross-correlation between horizon points H and fault points F.

Model adjustment based on well position markers

After the faults and horizons have been converted from the time domain into depth using seismic velocities, additional measurements of their positions are being introduced to the system from borehole measurements. These additional point based measurements effectively reduce the uncertainty of the entire model due to their low uncertainty compared to the initial depth converted model. The constraining of the model on borehole measurements is made using a least squares adjustment approach based on conditional equations. All measurement errors and thus all linear combinations of these are assumed to be Gaussian. The method is described in detail in App B. Derived from this method are the equations:

$$\hat{L} = (I - \sum_{L_0 L_0} B^T (B \sum_{L_0 L_0} B^T)^{-1} B) L_0$$

and

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$$\Sigma_{\hat{L}\hat{L}} = \Sigma_{L_0L_0} - \Sigma_{L_0L_0} B^T (B\Sigma_{L_0L_0} B^T)^{-1} B\Sigma_{L_0L_0},$$

where

 L_0 is the initial measurement vector

 $\Sigma_{L_0L_0}$ is the covariance matrix of the initial measurement vector

20 *B* is the matrix of constraining equations

 \hat{L} is the estimated measurement vector (constrained using the B matrix)

 $\Sigma_{\hat{L}\!\hat{L}}$ is the covariance matrix of the estimated measurement vector, \hat{L}

Every stochastic variable involved, and hence any linear combination of these, is assumed to be normally distributed. The vector L consists of three types of measurements:

- ullet interval velocities, contained in the vector V
- point positions making up the geological surfaces, contained in the vector G
- well marker positions used to constrain the geological surfaces, contained in W

Each modelled position (both well markers and the geological points) consists of coordinate triplets $P = \begin{bmatrix} N & E & D \end{bmatrix}^T$. Combining the three types of measurements into the common measurement vector L, gives:

where M is the number of velocities (and horizons) modelled, S is the total number of geological surfaces (horizons and faults), n is the number of geological points in each surface, and T is the total number of well markers. The total number of geological points is denoted by the letter O.

Each row of the $\it B$ - matrix consists of the coefficients of one constraining equation, put on the set of measurements given by $\it L_0$. The full constraining equations are formulated by:

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$$B \cdot L = \vec{0}$$
.

The rotation matrix,

$$R = \begin{bmatrix} R_U & R_V & R_W \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{21} & r_{32} & r_{33} \end{bmatrix},$$

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plays an important in role in the following sections. This matrix describes the transformation between two rotated coordinate systems with the same origin. A point $P_{\mathit{UVW}} = \begin{bmatrix} u & v & w \end{bmatrix}$ described in the UVW - coordinate system is thus converted to the point $P_{\mathit{XYZ}} = \begin{bmatrix} x & y & z \end{bmatrix}$ in the XYZ -coordinate system through the multiplication:

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$$P_{XYZ} = R_{IJVW \to XYZ} \cdot P_{IJVW},$$

and inversely a point in the XYZ - coordinate system is transformed into the UVW - system through:

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$$P_{UVW} = R_{UVW \to XYZ}^T \cdot P_{XYZ}$$

If we look at the individual column vectors of $R_{UVW \to XYZ} = \begin{bmatrix} R_U & R_V & R_W \end{bmatrix}$, they represent the unit vectors of the UVW -axes seen in the XYZ - coordinate system. Due to this last property, the column vectors of a rotation matrix are useful for specifying constraining equations in arbitrary spatial directions.

Well adjustment constrained in vertical direction

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In this case, the constraints set between the D coordinates of well markers and their respective geological common-points are only specified in the vertical direction. For each pair of points a constraining equation can be formulated by:

$$CE(P_{Gk}) - CE(P_{Wl}) = 0,$$

where $C=\begin{bmatrix}0&0&1\end{bmatrix}$, P_{Gk} are the coordinates of the k-th geological point in G, and P_{Wl} the coordinates of the l-th well marker in the well marker vector W.

20 Putting these conditions into the *B* -matrix gives:

$$B_1 = \begin{bmatrix} 0 & 0 & \Lambda & C_1 & \Lambda & 0 & 0 & \Lambda & -C_1 & \Lambda & 0 \\ \frac{1 \times M}{1 \times 3} & \frac{1 \times 3}{1 \times 3} \\ M & M & M & M & M & M & M & M \\ 0 & 0 & \Lambda & C_T & \Lambda & 0 & 0 & \Lambda & -C_T & \Lambda & 0 \\ \frac{1 \times M}{1 \times 3} & \frac{1 \times 3}{1 \times 3} \end{bmatrix}$$

Each row of the B_1 matrix corresponds to the measurement vector $L = \begin{bmatrix} V & G & W \end{bmatrix}^T$. Since no constraints are specified for the interval velocities in V, the M first numbers of each row vector in B_1 are set to 0. The next $3 \cdot O$ row posts correspond to the geological points in G, O being the number of geological points in G. The three row posts matching to the geological point, P_{Gk} , in G are set to the vector C_k ; the rest of

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the posts matching to G are set to 0. The last $3 \cdot T$ posts of each row in B_1 correspond to the well markers in W, where T is the number of well markers included. Of these, only the three posts matching to the well marker P_{Wl} are filled in with the vector $-C_l$, whereas the rest of the posts are set to 0. The total number of rows in B_1 equals the number of constraints T.

Well adjustment constrained along surface normal

To set a constraint perpendicular to the geological surface in the vicinity of a certain geological common-point, the eigenvector of the n closest points to the common-point are used, specified through the rotation matrix R:

$$R = \begin{bmatrix} R_U & R_V & R_W \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{21} & r_{32} & r_{33} \end{bmatrix} = eig \begin{bmatrix} N_1 - \overline{N} & \Lambda & N_n - \overline{N} \\ E_1 - \overline{E} & \Lambda & E_n - \overline{E} \\ D_1 - \overline{D} & \Lambda & D_n - \overline{D} \end{bmatrix} \cdot \begin{bmatrix} N_1 - \overline{N} & \Lambda & N_n - \overline{N} \\ E_1 - \overline{E} & \Lambda & E_n - \overline{E} \\ D_1 - \overline{D} & \Lambda & D_n - \overline{D} \end{bmatrix}^T$$

In the following it is assumed that the eigenvectors are sorted in such a way that $R_{\scriptscriptstyle W}$ is the eigenvector corresponding to the smallest belonging eigenvalue. $R_{\scriptscriptstyle W}$ is an approximate unit vector perpendicular to the geological surface. Thus multiplying $R_{\scriptscriptstyle W}^{}$ with an arbitrary vector gives the component of the arbitrary vector in the direction of $R_{\scriptscriptstyle W}$.

20 Using this we can formulate a condition between a pair of common-points as:

$$R_W^T \big(E(P_{Gk}) - E(P_{Wl}) \big) = 0,$$

where P_{Gk} are the coordinates of the k-th geological point in G, and P_{Wl} the coordinates of the l-th well marker in the well marker vector W.

Combining several conditions into a common matrix, \boldsymbol{B}_1 , gives

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$$B_{1} = \begin{bmatrix} 0 & 0 & \Lambda & R_{W1}^{T} & \Lambda & 0 & 0 & \Lambda & -R_{W1}^{T} & \Lambda & 0 \\ \frac{1 \times M}{1 \times 3} & \frac{1 \times 3}{1 \times 3} \\ M & M & M & M & M & M & M & M \\ 0 & 0 & \Lambda & R_{WT}^{T} & \Lambda & 0 & 0 & \Lambda & -R_{WT}^{T} & \Lambda & 0 \\ \frac{1 \times M}{1 \times 3} & \frac{1 \times 3}{1 \times 3} \end{bmatrix},$$

which correspond to the measurement vector $L = [V \ G \ W]^T$. The M first numbers of each row vector in B_1 are set to 0, followed on each row the $3 \cdot O$ numbers corresponding to the geological points in G, M being the number of interval velocities in V and O being the number of geological points in G. The three row posts matching to the geological point, P_{Gk} , in G are set to the vector R_{Wk}^{-T} ; the rest of the posts matching to G are set to 0. The last G0 posts of each row in G1 correspond to the well markers in G1, where G2 is the number of well markers included. Of these, only the three posts matching to the well marker G3 are filled in with the vector G4, whereas the rest of the posts are set to 0. As we specify one constraint for each well marker included, the total number of rows in G1 is equal to G2.

Well adjustment constrained in image ray direction

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In this case, the constraints between the coordinates of the common points (i.e. well markers and geological points) are set in the direction of the incident angle of the ray trace. This constraint can be expressed by:

$$E(\mathbf{r}^{T}[X_{w}-X_{g}Y_{w}-Y_{g}Z_{w}-Z_{g}]^{T}) = E(r_{1}(X_{w}-X_{g})+r_{2}(Y_{w}-Y_{g})+r_{3}(Z_{w}-Z_{g})) = 0$$

where $\mathbf{r} = [\mathbf{r}_1 \ \mathbf{r}_2 \ \mathbf{r}_3]^T$ is the unit vector of the incident ray on the surface, (XYZ)_w and (XYZ)_g are the coordinates of the well markers and geological points respectively.

The above mentioned constraint can be expressed by the following matrix:

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$$B_{l} = \begin{bmatrix} 0 & 0 & \Lambda & r_{lk}^{-T} & \Lambda & 0 & 0 & \Lambda & -r_{ll}^{-T} & \Lambda & 0 \\ l\times M & l\times 3 & & l\times 3 & & l\times 3 & & l\times 3 \\ M & M & & M & & M & M & & M \\ 0 & 0 & \Lambda & r_{Tk}^{-T} & \Lambda & 0 & 0 & \Lambda & -r_{Tl}^{-T} & \Lambda & 0 \\ l\times M & l\times 3 & & l\times 3 & & l\times 3 & & l\times 3 \\ & & & & & & & & & & & & & & & & & \\ T\times (M+3\cdot O+3\cdot T) & & & & & & & & & & & & & \\ T\times (M+3\cdot O+3\cdot T) & & & & & & & & & & & & \\ \end{bmatrix}$$

where the indexes k and l correspond respectively to the points P_{Gk} and P_{Wl} of the L vector. T is the number of common point pairs.

Constraints between faults and horizons

Constraints between faults and horizons can be added to make horizon and fault crossings fit together also after update. For a single pair of points consisting of a horizon point and a fault point, such a condition is stated as:

$$IE(P_{Hk}) - IE(P_{Fl}) = 0$$
,

stating that the horizon point $P_{\!\scriptscriptstyle Hk}$ on the border between a horizon and a fault shall be identical to the corresponding fault point $P_{\!\scriptscriptstyle Fl}$.

Similar fault-fault intersection constraints can be stated as.

$$IE(P_{Ek}) - IE(P_{El}) = 0$$

Sets of such constraints can be added to the $\it B$ -matrix forming the constraining equation set:

$$B \cdot L = \begin{bmatrix} B_1 \\ B_2 \end{bmatrix} \cdot L = 0$$

where

$$B_2 = \begin{bmatrix} 0 & 0 & \Lambda & I_1 & \Lambda & 0 & 0 & \Lambda & -I_1 & \Lambda & 0 \\ \frac{3 \times M}{3 \times 3} & \frac{3 \times 3}{3 \times 3} \\ M & M & M & M & M & M & M \\ 0 & 0 & \Lambda & I_S & \Lambda & 0 & 0 & \Lambda & -I_S & \Lambda & 0 \\ \frac{3 \times M}{3 \times 3} & \frac{3 \times 3}{3 \times 3} \end{bmatrix}.$$

Each row of the B_2 matrix corresponds to the measurement vector $L = \begin{bmatrix} V & G & W \end{bmatrix}^T$.

The first M posts of each row as well as the last $3 \cdot T$ are set to 0, since interval velocities and well markers are not included in these constraints. M is the number of interval velocities, and T is the number of well markers. For each horizon and fault point pair, there are three constraining equations; their coefficients are represented by $two 3 \times 3$ unit matrices in B_2 . Making the total number of rows in B_2 , $3 \cdot S$. S is the number of horizon/fault point pairs.

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Picking of common points

As mentioned earlier, the least squares adjustment is based on setting constraints between wellmarkers and geological points. The wellmarker and the geological point constitute a common point. For a given wellmarker, the method for choosing the best suited geological point may depend on the applied constraining principle.

In this section, four methods for picking of common points will be presented. Three of these methods are especially suited for the constraining principles disclosed hereinbefore. The fourth method may be applicable for all constraining principles.

1.1.1 Constraint in vertical directions

When constraints between well marker and geological points are to be set in the vertical direction, the geology point with the closest lateral Euclidean distance to the well marker is used as common point. The lateral distance d_h is calculated by:

$$d_h = \sqrt{(N_W - N_G)^2 + (E_W - E_G)^2}$$

where N_W and N_G denote the north coordinates of the wellmarker and the geological point respectively.

1.1.2 Constraints along surface normal

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As geological common point in this case, the geological point that lies closest to the approximate geological surface normal through the well marker is used. To calculate this distance, we need to transform both geology points and well marker into a coordinate system in which one of the axes lies along the surface normal. This is done using the eigenvectors of the n closest geology points to the surface as rotation matrix, to transform between the NED- coordinate system and the- UVW system, in which the W direction lies along the surface normal. The rotation matrix is calculated as follows:

$$R_{UVW \to NED} = \begin{bmatrix} R_U & R_V & R_W \end{bmatrix} = eig \begin{bmatrix} N_1 - \overline{N} & \Lambda & N_n - \overline{N} \\ E_1 - \overline{E} & \Lambda & E_n - \overline{E} \\ D_1 - \overline{D} & \Lambda & D_n - \overline{D} \end{bmatrix} \cdot \begin{bmatrix} N_1 - \overline{N} & \Lambda & N_n - \overline{N} \\ E_1 - \overline{E} & \Lambda & E_n - \overline{E} \\ D_1 - \overline{D} & \Lambda & D_n - \overline{D} \end{bmatrix}^T ,$$

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$$R_{NED \to UVW} = R_{UVW \to NED}^T$$

It is assumed that the column vectors of $R_{\mathit{NED} \to \mathit{UVW}}$, are sorted in such a way that the R_{W} vector is the eigenvector corresponding to the smallest eigenvalue. In the transformations the midpoint $\overline{P}_{\!G}$ of the n closest geology points to the well marker, $P_{\!\mathit{W}}$, is used as origin for the UVW- coordinate system.

Thus the transformations of arbitrary P_G and P_W points into the UVW system are formulated as:

$$P_{G,UVW} = \begin{bmatrix} U_G \\ V_G \\ W_G \end{bmatrix} = R_{NED \to UVW} \left(P_{G,NEV} - \overline{P}_G \right)$$

and

$$P_{W,UVW} = \begin{bmatrix} U_W \\ V_W \\ W_W \end{bmatrix} = R_{NED \rightarrow UVW} \left(P_{W,NEV} - \overline{P}_G \right)$$

The perpendicular distance d_{UV} between the surface normal through the well marker and the various geological points is then calculated by the formula:

$$d_{UV} = \sqrt{(U_W - U_G)^2 + (V_W - V_G)^2}$$

1.1.3 Constraints in image ray direction

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A suitable geological point can be found by comparing the perpendicular distances between the actual wellpick and all the nearby incident ray traces of the geological points. The geological point corresponding to the perpendicularly closest ray trace will then be the candidate for common point.

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The following approach can be used to find the shortest perpendicular distance between a wellpick and the nearby incident ray traces. First, a subset of the closest geological points to the wellmarker is found by comparing horizontal coordinates. Then, we have to calculate the shortest perpendicular distance from the wellpick to every unit ray-trace vector.

Let the wellmarker and the geological point be denoted by:

$$P_W = [X_W Y_W Z_W]$$
 and $P_G = [X_G Y_G Z_G]$

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The vector \vec{w} from the wellmarker P_w to the geological point P_G is given by:

$$\overset{\mathbf{P}}{w} = \begin{bmatrix} X_W - X_G & Y_W - Y_G & Z_W - Z_G \end{bmatrix}$$

The perpendicular distance D from the wellmarker to the unit vector \vec{u} of the incident ray trace is simply the length of the cross product of \vec{w} and \vec{u} . This length can be calculated by:

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$$D = \begin{bmatrix} \mathbf{p} \times \mathbf{p} \\ w \times u \end{bmatrix} = (\begin{bmatrix} \mathbf{p} \times \mathbf{p} \\ w \times u \end{bmatrix} \begin{bmatrix} \mathbf{p} \times \mathbf{p} \\ w \times u \end{bmatrix}^T)^{\frac{1}{2}}$$

The above-mentioned procedure has to be repeated for all the wellmarkers in the actual area.

10 1.1.4 "Most likely" geological common point

This method uses the uncertainty ellipsoids of the well marker and geological points to decide the "most likely" geological common point. A weighted distance measure is calculated by:

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$$d_{weighted} = \sqrt{(P_W - P_G) \cdot inv(\Sigma_W + \Sigma_G) \cdot (P_W - P_G)^T}$$

The summation of the covariance matrix Σ_w of the well marker and the covariance matrix Σ_G of the geological point is possible since the original seismic interpretation is assumed to be uncorrelated with the well marker.

Well marker uncertainty model

The coordinates of the wellmarkers are important input. Another important input is the variances of the coordinates of the wellmarkers and the covariances between them. A wellbore consists of several survey points and some of these survey points are chosen as wellmarkers.

The coordinates of wellmarkers are calculated from directional surveys and measured depths performed at several stations along the wellbore. The directional surveys are correlated between survey stations. This is also the case for the measured depths. These correlations should be taken into account to ensure a proper variance and covariance matrix propagation.

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Modelling of variances and covariances of wellmarkers

Depth measurements are a significant contributor to the wellbore position uncertainty when surveying both with magnetic and gyroscopic instruments. Correlations between depth measurements are considered to be the most important correlation in wellbore surveying. Another source to strong correlations is the declination error.

A detailed overview of the most important error sources in depth measurements is 10 given in Ekseth, R 1998. The following procedure is found appropriate to investigate of the effects of depth correlations.

For prediction of the correlation behaviour of depth measurements between survey points along the wellbore, a correlation function may be used. A correlation function can for instance be expressed in terms of an exponential function:

$$\rho = e^{D_i - D_j / \xi}$$

where ρ_{ij} is the correlation coefficient, ξ is the a suitable correlation length, and D_i and D_j are the measured depth in unit metres at the points i and j respectively. The correlation length ξ is defined as the length needed for the correlation between two wellmarkers to fall below a certain value.

The covariance σ_{ij}^2 between the wellmarkers i and j can be predicted by the following formula:

$$\sigma_{ij}^2 = \rho_{ij} \sqrt{\sigma_{ii}^2 \sigma_{jj}^2}$$

where ρ_{ij} is the correlation coefficient, and σ_{ii} and σ_{jj} are the variances of the wellmarkers number i and number j, respectively.

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5 App A Image ray tracing

Image raytracing is defined by starting a ray vertically at the surface and applying Snell's law at interfaces. At every interface of two horizons l and l+1, and for every point k=1,K, n_k the following is needed for raytracing:

1) The unit vector of the incidence ray:

$$u_{k,i} = \frac{\left(N_{k,l} - N_{k,l-1}, E_{k,l} - E_{k,l-1}, D_{k,l} - D_{k,l-1}\right)}{\sqrt{\left(N_{k,l} - N_{k,l-1}\right)^2 + \left(E_{k,l} - E_{k,l-1}\right)^2 + \left(D_{k,l} - D_{k,l-1}\right)^2}},$$
(A1)

2) The unit normal vector at point k of interface l:

$$u_{k,n} = \frac{\left(-\alpha_x, -\alpha_y, 1\right)}{\sqrt{\alpha_x^2 + \alpha_y^2 + 1}},\tag{A2}$$

where

$$\alpha_{x} = \frac{\sum_{j \in \partial k} (D_{j,l} - \overline{D})(N_{j,l} - \overline{N})}{\sum_{j \in \partial k} (N_{j,l} - \overline{N})^{2}}$$

$$\alpha_{y} = \frac{\sum_{j \in \partial k} (D_{j,l} - \overline{D})(E_{j,l} - \overline{E})}{\sum_{j \in \partial k} (E_{j,l} - \overline{E})^{2}},$$

$$\overline{N} = \sum_{j \in \partial k} N_{j,l}, \quad \overline{E} = \sum_{j \in \partial k} E_{j,l}, \quad \overline{D} = \sum_{j \in \partial k} D_{j,l}.$$
(A3)

and ∂k is a specified neighbourhood of point k.

3) The incidence angle at point k of layer l:

$$\theta_{k,i} = \arccos(u_{k,i} u_{k,i}^T), \tag{A4}$$

20 where

15

$$u_{k,n}u_{k,i}^{T} = u_{k,n}(1) \cdot u_{k,i}(1) + u_{k,n}(2) \cdot u_{k,i}(2) + u_{k,n}(3) \cdot u_{k,i}(3). \tag{A5}$$

4) The transmission angle at point k into layer l+1 calculated using Snell's law:

5

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$$\theta_{k,t} = \arcsin \left[\frac{\sin(\theta_{k,t}) v_{l+1}}{v_l} \right], \tag{A6}$$

5) The transmission unit vector at point k into layer l+1:

$$u_{k,t} = \frac{v_{l+1}}{v_l} u_{k,i} + \left(\cos(\theta_{k,t}) - \frac{v_{l+1}}{v_l} \cos(\theta_{k,i}) \right) u_{k,n}, \tag{A7}$$

where the scalar coefficients in front of $u_{\mathbf{k},\mathbf{i}}$ and $u_{\mathbf{k},\mathbf{n}}$ are evaluated by ensuring that

$$\cos(\theta_{k,t}) = u_{k,n} u_{k,t}^{T},$$

$$||u_{k,t}|| = 1,$$
(A8)

is valid, that $\sin^2(\theta) = 1 - \cos^2(\theta)$ and Snell's law in Eqn. (10).

6) The predicted point k in layer l+1:

$$N_{k,l+1} = N_{k,l} + \frac{1}{2} v_{l+1} (t_{k,l+1} - t_{k,l}) u_{k,t} (1)$$

$$E_{k,l+1} = E_{k,l} + \frac{1}{2} v_{l+1} (t_{k,l+1} - t_{k,l}) u_{k,t} (2), \qquad k = 1, K, N,$$

$$D_{k,l+1} = D_{k,l} + \frac{1}{2} v_{l+1} (t_{k,l+1} - t_{k,l}) u_{k,t} (3)$$
(A9)

where components of the transmission unit vector are given by

$$u_{k,t} = [u_{k,t}(1), u_{k,t}(2), u_{k,t}(3)].$$

Steps 1)-6) described in Eqn. (5-13) can be written in short form as:

15
$$(N_{k,l+1}, E_{k,l+1}, D_{k,l+1})^T = f_{k,l}[v_1, K, v_m, (x_{k,j}, y_{k,j}, z_{k,j}), 1 \le j \le l, 1 \le k \le n_h],$$
 (A10)

where the function $f_{k,l}: \Re^{m+3mn_k} \to \Re^3$ summarizes all the relationships.

App B Deduction of the least squares adjustment formulas B.1Definitions

Measured values: $L = [l_1, l_2, l_3, \dots]^T$

The measurement errors are considered to be normal distributed, and therefore all linear combinations of these are also normal distributed.

5

Cofactor matrix: $Q_{LL} = P_{LL}^{-1}$

If the measured values are weighted using their initial measurement uncertainties then $Q_{LL} = P_{LL}^{-1} = \Sigma_{LL} \text{, where } \Sigma_{LL} \text{ denotes the initial covariance matrix of the measured}$ values.

Unknowns: $X = [x_1, x_2, x_3,]^T$

Residuals: $\varepsilon = L - L_{true}$

15

Model: $AX - L_{true} = c$, which gives $\varepsilon = AX - F$ where F = L + c. c is a constant vector. In statistical terms from [2]:

$$E[L] = AX - c$$
 ; $E\{(L - E\{L\})(L - E\{L\})^T\} = \Sigma_{IJ}$

20

Condition equation: $BX - W_c = 0$, where W_c is a constant vector.

Error propagation law: If we have the model y = Ax then $Q_{\hat{y}\hat{y}} = AQ_{\hat{x}\hat{x}}A^T$

25 B.2 Generating normal equations

Using the condition equation, we can construct the help function h, in which the weighted sum of squares is conditioned on the condition equation, using Lagrange multipliers:

$$h = \varepsilon^T P_{II} \varepsilon + 2K(BX - W_c)$$

K is a vector of Lagrange multipliers. Filling in for ε gives:

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$$h = X^{T} A^{T} P_{LL} A X - 2 A^{T} P_{LL} F X + F^{T} P_{LL} F + 2 K (B X - W_{c})$$

Using the derivatives of the help function with respect on the unknowns K and X, we can create a set of normal equations containing the least squares estimates of K and X as unknown sizes:

$$\frac{\partial h}{\partial X} = 0 \Rightarrow A^T P_{LL} A \hat{X} - A^T P_{LL} F + B^T \hat{K} = 0$$

$$\frac{\partial h}{\partial K} = 0 \Rightarrow B\hat{X} - W_c = 0$$

15 Rearranging the normal equations into a matrix equation, gives a straightforward way to calculate \hat{X} and \hat{K} :

$$\begin{bmatrix} \hat{X} \\ \hat{K} \end{bmatrix} = \begin{bmatrix} A^T P_{LL} A & B^T \\ B & 0 \end{bmatrix}^{-1} \begin{bmatrix} A^T P_{LL} F \\ W_c \end{bmatrix}$$

20 Using the error propagation law, the cofactor matrix for \hat{X} and \hat{K} becomes:

$$\begin{bmatrix} Q_{\hat{X}\hat{X}} & Q_{\hat{X}\hat{K}} \\ Q_{\hat{X}\hat{K}}^T & Q_{\hat{K}\hat{K}} \end{bmatrix} = \begin{bmatrix} A^T P_{LL} A & B^T \\ B & 0 \end{bmatrix}^{-1} \begin{bmatrix} A^T P_{LL} A & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} A^T P_{LL} A & B^T \\ B & 0 \end{bmatrix}^{-1}.$$

B.3 Direct calculation of the estimate for X

25

As it is only \hat{X} and $Q_{\hat{X}\hat{X}}$ we are interested in, it opens for direct calculation of these. Starting with:

$$A^{T}P_{LL}A\hat{X} - A^{T}P_{LL}F + B^{T}\hat{K} = 0$$
,

we substitute $\boldsymbol{A}^{\mathrm{T}}(P_{\!\scriptscriptstyle LL})\boldsymbol{A}$ with $N_{\scriptscriptstyle 0}$, and rearrange equation to:

5

$$\hat{X} = N_0^{-1} A^T P_{LL} F - N_0^{-1} B^T \hat{K}$$

Substituting for \hat{X} in:

$$10 \qquad B\hat{X} - W_c = 0,$$

gives:

$$\hat{K} = (BN_0^{-1}B^T)^{-1}BN_0^{-1}A^TP_{LL}F - (BN_0^{-1}B^T)^{-1}W_c.$$

15

Substituting this result into the equation for \hat{X} , gives:

$$\hat{X} = N_0^{-1} A^T P_{LL} F - N_0^{-1} B^T (B N_0^{-1} B^T)^{-1} B N_0^{-1} A^T P_{LL} F + N_0^{-1} B^T (B N_0^{-1} B^T)^{-1} W_c$$

20 B.4 Direct calculation of the estimate for Q_{XX}

Applying the error propagation law on:

$$\hat{X} = N_0^{-1} A^T P_{LL} F - N_0^{-1} B^T (B N_0^{-1} B^T)^{-1} B N_0^{-1} A^T P_{LL} F + N_0^{-1} B^T (B N_0^{-1} B^T)^{-1} W_c,$$

25

gives:

$$Q_{\hat{X}\hat{X}} = N_0^{-1} - N_0^{-1} B^T (B N_0^{-1} B^T)^{-1} B N_0^{-1}.$$

30 B.5 The statistical model: X-L=0.

Looking at the statistical model: AX-L=c, which gives $\varepsilon=AX-F$ where F=L+c. c is a constant vector. It can be easily transformed into the model X-L=0, by setting A=I, and $c=\overset{\mbox{\ensuremath{\omega}}}{0}$, which leads to F=L, and $N_0=P_{LL}$. We still want to keep the condition equation: $BX-W_c=0$.

5

Applying these changes to:

$$\hat{X} = N_0^{-1} A^T P_{LL} F - N_0^{-1} B^T (B N_0^{-1} B^T)^{-1} B N_0^{-1} A^T P_{LL} F + N_0^{-1} B^T (B N_0^{-1} B^T)^{-1} W_c$$

10 gives:

$$\hat{X} = L - P_{LL}^{-1} B^{T} (B P_{LL}^{-1} B^{T})^{-1} B L + P_{LL}^{-1} B^{T} (B P_{LL}^{-1} B^{T})^{-1} W_{c}.$$

And applying them to:

15

$$Q_{\hat{X}\hat{X}} = N_0^{-1} - N_0^{-1} B^T (B N_0^{-1} B^T)^{-1} B N_0^{-1},$$

gives:

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$$Q_{\hat{X}\hat{X}} = P_{LL}^{-1} - P_{LL}^{-1} B^T (BP_{LL}^{-1} B^T)^{-1} BP_{LL}^{-1}.$$

CLAIMS:

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- 1. A method of forming a geological model of a region of the Earth, comprising the steps of:
- "i." providing seismic data obtained from the region and including seismic travel time uncertainty;
 - "ii." providing a seismic velocity model of the region including velocity uncertainty;
 - "iii".performing image ray tracing on the seismic data using the velocity model to determine the three dimensional positions of a plurality of points of the region;
 - "iv." calculating three dimensional positional uncertainties of at least some of the points from the travel time uncertainty, the velocity uncertainty and uncertainty in ray propagation direction; and
- 15 "v." combining the positions determined in the step "iii" with the uncertainties calculated in the step "iv" to form a first geological model.
 - 2. A method as claimed in claim 1, in which at least some of the points are disposed at at least one interface, identified from the seismic date, between subregions of the region of different seismic velocities.
 - 3. A method as claimed in claim 1 or 2, in which at least some of the points are disposed at faults identified from the seismic data.
- 4. A method as claimed in any one of the preceding claims, in which the travel time uncertainty is determined from the seismic wavelength used to obtain the seismic data.
- 5. A method as claimed in any one of the preceding claims, in which the velocity uncertainty is determined from knowledge of the geology of the region.
 - 6. A method as claimed in any one of the preceding claims, in which the step "iii" comprises determining the position of each of the points as a function of: the position at a shallower interface where a ray incident at the point intersects the shallower interface: the seismic velocity from the position to the point obtained from the

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velocity model; and the travel time from the position to the point obtained from the seismic data.

- 7. A method as claimed in claim 6, in which the step "iv" comprises differentiating the function.
 - 8. A method as claimed in claim 7, in which the function includes a first subfunction representing Snell's law and a second sub-function representing dip at the position and the step "iv" comprises determining the derivatives of the first and second sub-functions.
 - 9. A method as claimed in any one of the preceding claims, in which the step "v" includes assigning correlations among at least some of the points.
- 15 10. A method as claimed in any one of the preceding claims, further comprising assigning correlations among velocity values in the velocity model.
 - 11. A method as claimed in any one of the preceding claims, comprising the further steps of:
- 20 "vi" providing non-seismically obtained three dimensional position data and three dimensional positional uncertainty data about the region; and
 - "vii" adjusting the first geological model by means of the data provided in the step "vi" to obtain a second geological model.
- 25 12. A method as claimed in claim 11, in which the non-seismically obtained data comprise well marker data.
 - 13. A method as claimed in claim 11 or 12, in which the step "vii" comprises selecting at least one common point of the region which is common to the first geological model and to the non-seismically obtained data and determining the position and the positional uncertainty of the common point in the second geological model from the positions and the positional uncertainties of the common point in the first geological model and in the non-seismically obtained data.

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14. A method as claimed in claim 13, in which the at least one common point represents common or adjacent geological features.

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- 15. A method as claimed in claim 14 when dependent directly or indirectly on claim 12, in which the at least one common point represents a location on one interface in the first geological model and a location in the non-seismically obtained data where a well passes through the interface.
- 16. A method as claimed in claim 15, in which the step "vii" comprises movingthe location of the common point in the first geological model substantially parallel to a ray path at or adjacent the location.
 - 17. A method as claimed in any one of claims 14 to 16, in which the at least one common point represents a location on a fault in the first model and a location in the non-seismically obtained data where a well passes through the fault.
 - 18. A method as claimed in claim 17, in which the step "vii" comprises moving the location of the common point in the first geological model substantially perpendicularly to the fault surface.

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19. A method as claimed in claim 16 or 18, further comprising updating the non-seismically obtained data by moving the location of the common point in the non-seismically obtained data in a direction substantially opposite the direction of movement in the first geological model.

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- 20. A method as claimed in any one of claims 11 to 19, in which the step "vi" comprises providing non-seismically obtained velocity data and velocity uncertainty data about the region.
- 30 21. A method as claimed in claim 20, further comprising forming and/or updating the velocity model in accordance with the non-seismically obtained velocity and velocity uncertainty data.

- 22. A method as claimed in any one of claims 11 to 21, in which the step "vii" is performed with a constraint that interface/fault intersections are preserved in the second geological model.
- A method as claimed in any one of claims 13 to 19 or in any one of claims 20 to 22 when dependent directly or indirectly on claim 13, in which the step "vii" comprises selecting a plurality of common points and adjusting the first geological model in a single step.
- 10 24. A method as claimed in claim 18 when dependent on claim 16 or in any one of claims 19 to 22 when dependent directly or indirectly on claims 16 and 18, in which the step "vii" comprises adjusting the first geological model in a first step, in respect of the at least one common point on the interface, and then in a second step, in respect of the at least one common point on the fault.

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- 25. A method as claimed in any one of claim 11 to 22, in which the step "vii" comprises adjusting the first geological model recursively layer by layer.
- 26. A computer program arranged to program a computer to perform a method as claimed in any one of the preceding claims.
 - 27. A computer containing or programmed by a program as claimed in claim 26.
- 28. A computer-readable storage medium containing a program as claimed in claim 26.
 - 29. Transmission of a program as claimed in claim 26.
- 30. A method of drilling a bore in a region of the earth, comprising performing a
 30 method as claimed in any one of claims 1 to 25 and controlling drilling in accordance with the geological model.

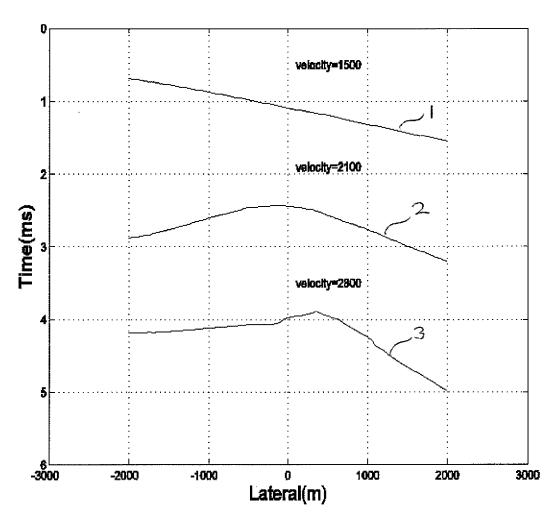
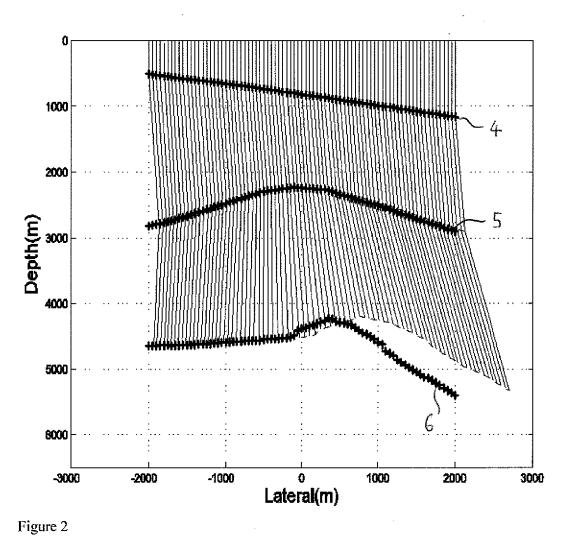


Figure 1



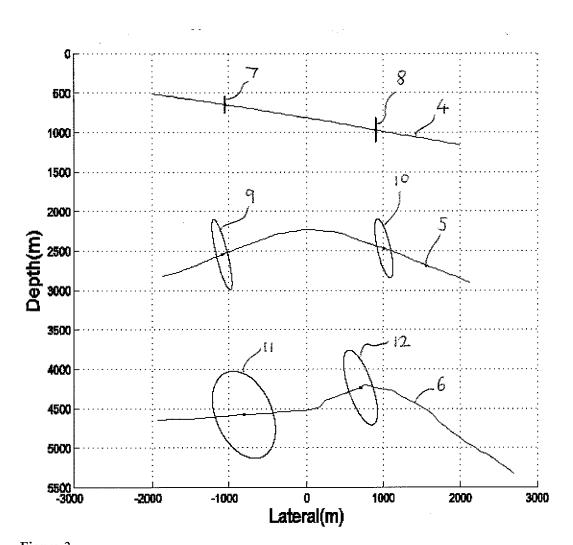


Figure 3

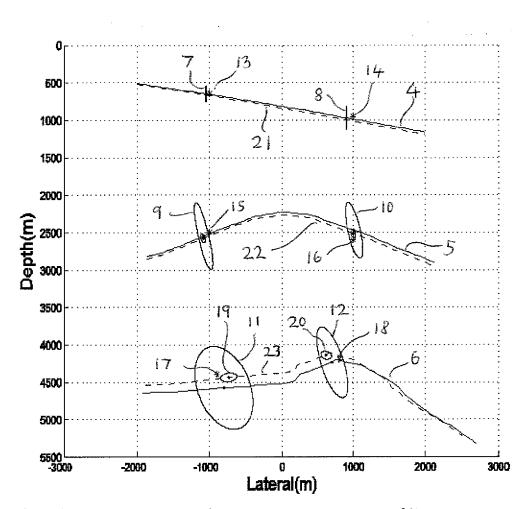


Figure 4

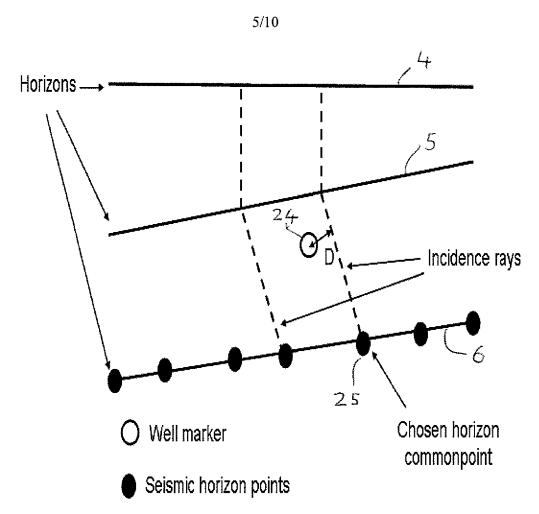


Figure 5

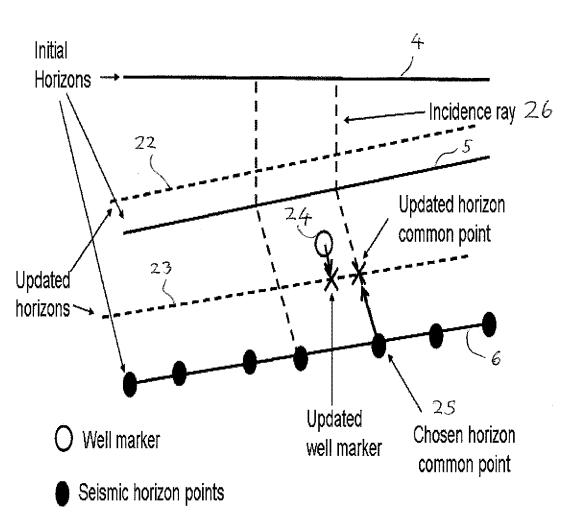


Figure 6

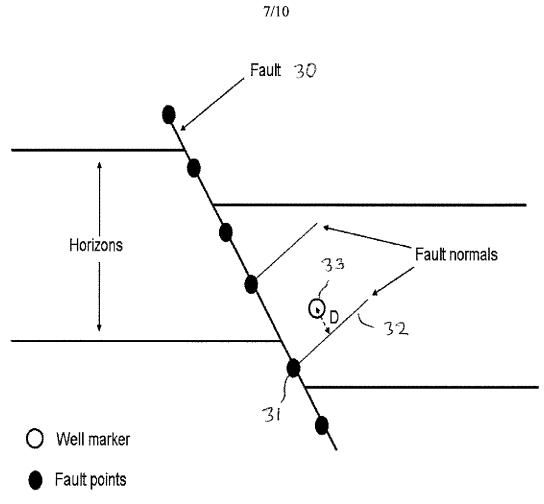


Figure 7

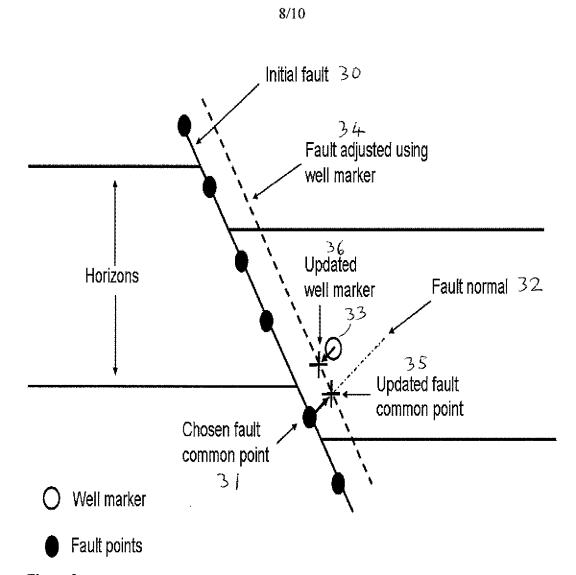
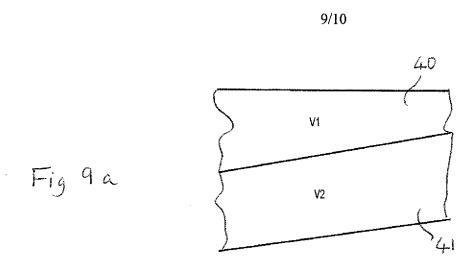
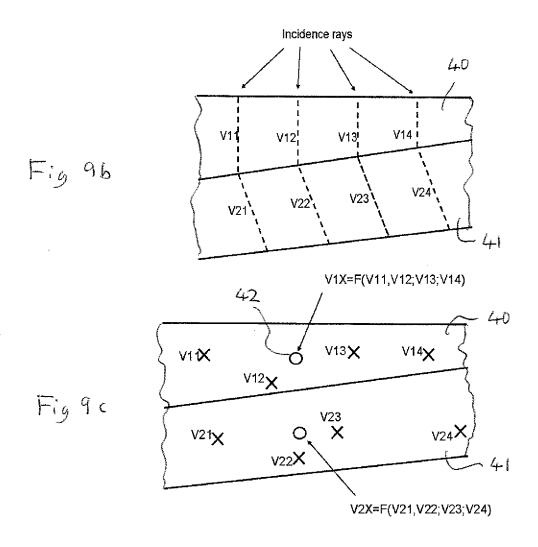


Figure 8.





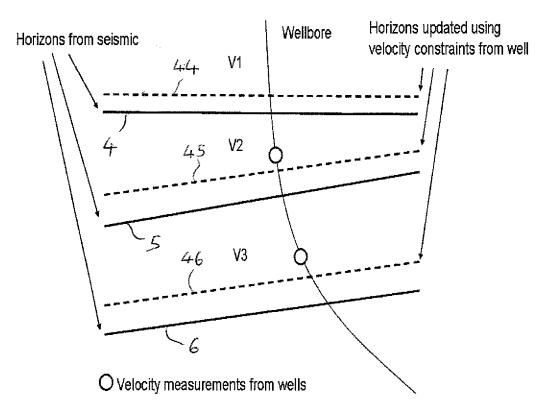


Figure 10

INTERNATIONAL SEARCH REPORT

International application No PCT/EP2008/065331

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| X Furti | ner documents are listed in the continuation of Box C. | X See patent family annex. | | | | | |
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INTERNATIONAL SEARCH REPORT

International application No
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| | column 1, line 1 - column 2, line 67 column 3, line 65 - column 5, line 33 column 6, line 30 - column 8, line 33 column 9, line 8 - column 10, line 39 column 12, line 16 - line 46 claims 1-19 | | | |
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