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| <p>(51) International Patent Classification:
 G06T 7/00 (2006.01) G06T 17/00 (2006.01)</p> <p>(21) International Application Number:
 PCT/EP2014/052396</p> <p>(22) International Filing Date:
 7 February 2014 (07.02.2014)</p> <p>(25) Filing Language:
 English</p> <p>(26) Publication Language:
 English</p> <p>(30) Priority Data:
 13305164.9 12 February 2013 (12.02.2013) EP
 13305792.7 12 June 2013 (12.06.2013) EP</p> <p>(71) Applicant: THOMSON LICENSING [—/FR]; 1-5 rue Jeanne d'Arc, F-92130 Issy-les-Moulineaux (FR).</p> <p>(72) Inventors: LECOCQ, Pascal; Technicolor R&d France, 975 Avenue Des Champs Blancs, F-35576 Cesson Sevigne Cedex (FR). GAUTRON, Pascal; Technicolor R&d France, 975 Avenue Des Champs Blancs, F-35576 Cesson Sevigne Cedex (FR). MARVIE, Jean-eudes; Technicolor R&d France, 975 Avenue Des Champs Blancs, F-35576 Cesson Sevigne Cedex (FR).</p> | <p>(74) Agents: HUCHET, Anne et al.; 1 rue Jeanne d'Arc, F-92443 Issy-les-Moulineaux Cedex (FR).</p> <p>(81) Designated States (<i>unless otherwise indicated, for every kind of national protection available</i>): AE, AG, AL, AM, AO, AT, AU, AZ, BA, BB, BG, BH, BN, BR, BW, BY, BZ, CA, CH, CL, CN, CO, CR, CU, CZ, DE, DK, DM, DO, DZ, EC, EE, EG, ES, FI, GB, GD, GE, GH, GM, GT, HN, HR, HU, ID, IL, IN, IR, IS, JP, KE, KG, KN, KP, KR, KZ, LA, LC, LK, LR, LS, LT, LU, LY, MA, MD, ME, MG, MK, MN, MW, MX, MY, MZ, NA, NG, NI, NO, NZ, OM, PA, PE, PG, PH, PL, PT, QA, RO, RS, RU, RW, SA, SC, SD, SE, SG, SK, SL, SM, ST, SV, SY, TH, TJ, TM, TN, TR, TT, TZ, UA, UG, US, UZ, VC, VN, ZA, ZM, ZW.</p> <p>(84) Designated States (<i>unless otherwise indicated, for every kind of regional protection available</i>): ARIPO (BW, GH, GM, KE, LR, LS, MW, MZ, NA, RW, SD, SL, SZ, TZ, UG, ZM, ZW), Eurasian (AM, AZ, BY, KG, KZ, RU, TJ, TM), European (AL, AT, BE, BG, CH, CY, CZ, DE, DK, EE, ES, FI, FR, GB, GR, HR, HU, IE, IS, IT, LT, LU, LV, MC, MK, MT, NL, NO, PL, PT, RO, RS, SE, SI, SK, SM, TR), OAPI (BF, BJ, CF, CG, CI, CM, GA, GN, GQ, GW, KM, ML, MR, NE, SN, TD, TG).</p> |
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- (54) Title:** METHOD AND DEVICE FOR ENRICHING THE CONTENT OF A DEPTH MAP

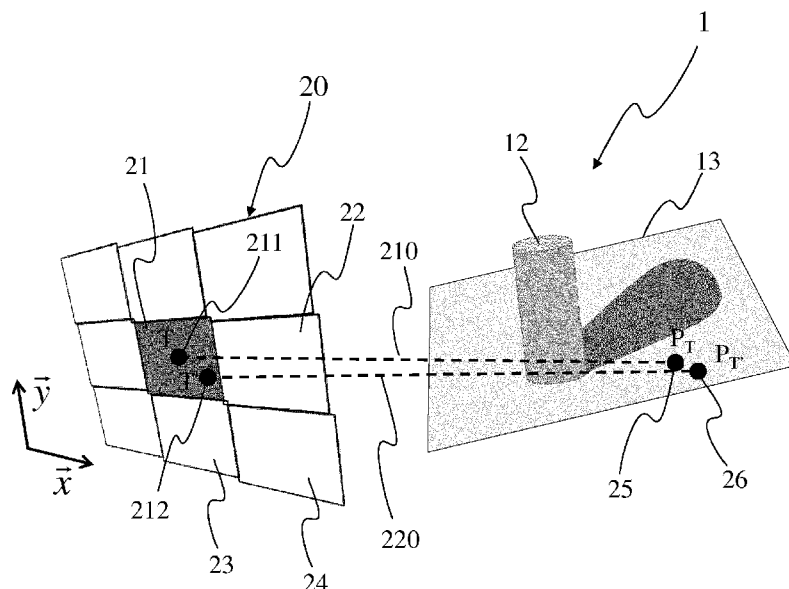


Fig 2

- (57) Abstract:** A method for enriching the content associated with a first element (21) of a depth map (10) the depth map (10) being associated with a scene (1) according to a point of view. Thereafter, at least a first information representative of a variation of depth in the first element (21) in the space of the depth map is established.

**Declarations under Rule 4.17:**

— *as to applicant's entitlement to apply for and be granted a patent (Rule 4.17(ii))*

Published:

— *without international search report and to be republished upon receipt of that report (Rule 48.2(g))*

METHOD AND DEVICE FOR ENRICHING THE CONTENT OF A DEPTH MAP

1. Domain of the invention.

5 The invention relates to the domain of depth map and more specifically to the enriching of the content of depth map(s). The invention is also understood in the context of Computer Generated Image (CGI or 3D-CGI).

2. Prior art

10 According to the prior art, it is known to associate a depth map with an image representing a scene, the image being either a synthesis image representing a virtual scene or an image of a real scene shot by a camera. It is also known to use the depth information comprised in the depth
15 map to perform visibility tests, i.e. to determine which fragment of the scene is hidden by another fragment of the scene according to a camera field of view. A depth map typically corresponds to an array of N lines and M columns of elements, also called pixels or texels, a single depth information being associated with each element of the depth map. The finite resolution of
20 the depth map leads to some approximations when determining if a first fragment of the scene is hidden by (or in the shadow of) a second fragment of the scene, the depth of which with regard to the camera field of view being stored in an element (also called pixel or texel) of the depth map. The resulting aliasing is known as bias aliasing. This aliasing may particularly
25 occur when the first and second fragments belong to the same surface of an object of the scene as viewed from the camera field of view associated with the depth map.

 As to overcome at least partially this bias aliasing artifact, it is known to use a bias value that a fragment is considered occluded or in
30 shadow when its distance to the camera field of view associated with the depth map is above the depth stored in an element of the depth map associated with this fragment plus the bias. However, the introduction of a bias value may lead to another aliasing known as peter-panning artifact.

3. Summary of the invention

35 The purpose of the invention is to overcome at least one of these disadvantages of the prior art.

More specifically, the purpose of the invention is to establish depth information associated with one or more elements of a depth map with a better precision than in the state of the art.

5 The invention relates to a method for enriching the content associated with a first element of a depth map, the depth map being associated with a scene according to a point of view. Thereafter, the method comprises a step of establishing at least a first information representative of a variation of depth in said first element in the space of the depth map.

10 According to a particular characteristic, the at least a first information is established from depth information associated with the first element and from depth information associated with at least a second element, the first element and the at least a second element belonging to a same surface element of the scene projected into the depth map.

15 Advantageously, the first element and the at least a second element are adjacent.

According to a specific characteristic, the at least a first information is established by computing the ratio of the difference of depth between the first element and the at least a second element to the distance between the first element and the at least a second element.

20 Advantageously, the at least a first information is established from an equation of a surface element of the scene projected into the space of a camera field of view associated with the depth map, the projected surface element comprising the first element.

25 According to another characteristic, the at least a first information is expressed under the form of a slope angle representative of the variation of depth in the first element.

Advantageously, the at least a first information expressed under the form of a slope angle is encoded in odd power function.

30 According to a particular characteristic, one first information is established for each dimension of the space of the depth map.

According to another characteristic, the method further comprises a step of storing the at least a first information associated with the first element in the depth map.

35 Advantageously, the content associated with the first element comprises a second information representative of the depth between the point of view and a fragment of the scene, the fragment corresponding to the

closest fragment visible from the point of view along a viewing direction passing through the first element.

The invention also relates to a device configured for enriching the content associated with a first element of a depth map, the depth map being associated with a scene according to a point of view, the device comprising at least one processor configured for establishing at least a first information representative of a variation of depth in the first element in the space of the depth map.

Advantageously, the at least one processor is a Graphical Processor Unit (GPU).

According to a specific characteristic, the at least a first information is established from depth information associated with the first element and from depth information associated with at least a second element, the first element and the at least a second element belonging to a same surface element of the scene projected into the depth map.

According to another characteristic, the at least one processor is further configured for expressing the at least a first information under the form of a slope angle representative of the variation of depth in said first element and for encoding in odd power function the at least a first information expressed under the form of a slope angle.

The invention also relates to a computer program product comprising instructions of program code for execution by at least one processor to perform the method for enriching the content associated with a first element of a depth map, when the program is executed on a computer.

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4. List of figures

The invention will be better understood, and other specific features and advantages will emerge upon reading the following description, the description making reference to the annexed drawings wherein:

- 30 - figure 1 shows an image and a depth map associated with a scene, according to the prior art;
- figure 2 shows a part of the depth map of figure 1, according to a particular embodiment of the invention;
- figures 3A, 3B and 4 show the projection of a surface element of the scene of figure 1 projected onto the depth map of figure 1, according to two particular embodiments of the invention;

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- figure 5 shows depth information stored in an element of the depth map of figure 1, according to a particular embodiment of the invention;
- figures 6A and 6B illustrate the encoding of depth information comprised in the depth map of figure 1, according to a particular embodiment of the invention;
- figure 7 diagrammatically shows a device implementing a method for enriching the content of the depth map of figure 1, according to a particular embodiment of the invention;
- figure 8 shows a method for enriching the content of the depth map of figure 1, according to a particular embodiment of the invention.

5. Detailed description of embodiments of the invention.

The invention will be described in reference to a particular embodiment of a method for enriching the content of a first element of a depth map. The depth map advantageously corresponds to an array of L lines and M columns of elements, L and M being integers greater than 0, and is associated with a scene which is rendered in one or more images. The number of elements comprised in the depth map corresponds for example to the number of pixels of the image(s) of the scene. The depth map is advantageously enriched with one or more first information representative of the variation of depth in the first element in the space of the depth map.

The additional first information thus enables to retrieve, if needed, the depth associated with any point of the first element whereas, in depth map according to the prior art, the depth associated with any point of an element of a depth map is the same and corresponds to the depth of the closest visible fragment of the scene associated with the first element, or with its centre.

Figure 1 shows a scene 1 rendered in an image 11 with an associated depth map 10, according to a particular and non-limitative embodiment. The image 11 represents the scene 1 as viewed from a given point of view (also called camera field of view, not represented on Figure 1) and the depth map is generated according to another point of view 100 (i.e. another camera field of view). The scene corresponds for example to a virtual scene and comprises several virtual objects, i.e. a first object 12 and a second object 13. The objects 12 and 13 are modelled according to any method known to those skilled in the art, for example by polygonal modelling,

in which the model is assimilated with a set of polygons (mesh elements) each defined by the list of summits and edges that compose it, by NURBS (Non uniform rational basic spline) type curve modelling in which the model is defined by a set of curves created via control vertices, by modelling by subdivision of surfaces. By virtual object is understood any virtual representation (obtained by modelling) of an object (real or fictitious) composing a real environment / real scene (for example the ground, a house or a house front, a person, a car, a tree, that is to say any element composing an environment such as a part of a house, a street, a town, the countryside, etc.) or an imaginary element. Each object 12, 13 of the scene 1 is characterized by a surface covering it, the surface of each object having reflectance properties (corresponding to the proportion of incident light reflected by the surface in one or several directions) that are specific to it.

The depth map 10 comprises n elements $10_1 \dots 10_{p'} \dots 10_n$, n being an integer greater than 0 that defines the resolution of the depth map 10, the resolution being for example equal to 512×512 pixels, 1024×1024 pixels or 4096×4096 pixels. A depth information is advantageously associated with each element of the depth map 10. This depth information corresponds to the distance between the point of view 100 and the closest visible fragment of the scene 1 along a viewing direction passing through an element of the depth map, this element of the depth map being associated with the closest visible fragment of the scene. By taking the element $10_{p'}$ as an example, the depth information associated with this element $10_{p'}$ corresponds to the distance between the point of view 100 and the fragment P'_{121} of the scene 1 along the viewing direction $100_{p'}$ having as origin the point of view 100 and passing through the element $10_{p'}$, advantageously passing through the centre of the element $10_{p'}$. The fragment P'_{121} corresponds to the first element of the scene crossed by the viewing direction $100_{p'}$ when starting from the point of view 100. The depth information is associated with the centre of the corresponding element of the depth map. A first information representative of the variation of depth inside an element of the depth map 10 is advantageously further associated with each element of the depth map, this first information being established as described with regard to figures 2 to 4.

The image 11 comprises m pixels $11_1 \dots 11_p \dots 11_m$, m being an integer greater than 0 that defines the resolution of the image 11. Advantageously, m is different from n , for example n is greater than m or m is

greater than n (the resolution of the depth map is for example 512x512 pixels, 1024x1024 pixels or 4096x4096 pixels whereas the resolution for the image 11 is for example 1024x768 pixels, 1280x720 pixels or 1920x1200 pixels). According to a variant, m is equal to n , both depth map 10 and image 5 11 having the same resolution. Attributes are advantageously associated with each pixel of the image 11, the attributes comprising for example color information (for example RGB information) and/or the translucent character of the fragment of the scene associated with a pixel of the image. A fragment advantageously corresponds to a surface element associated with a point of 10 the scene 1, the size of which being equal to the size of a pixel of the image 11 that may be displayed to represent the scene 1 on a display screen. A fragment of the scene 1 becomes a pixel in the image if the fragment is visible from the point of view associated with the image 11. For clarity purpose, an element (for example a point) of the scene 1 will be called a 15 fragment when positioning in the space of the 3D scene (the world space) and the same element visible from the point of view associated with the image 11 will be called pixel when positioning in the space of the image 11. A fragment visible from the point of view associated with the image 11 and the corresponding pixel in the image thus refers to one and a same element of 20 the scene 1 and may be mixed up in the rest of the description. Advantageously the fragment is defined by a set of data grouping together one or several of the following data items:

- the rasterization position of the fragment,
- the depth of the fragment at the viewpoint,
- 25 - attributes (for example the colour, the texture coordinates),
- the alpha channel representative of the translucent character of the fragment.

As to determine whether a fragment of the scene is visible from the point of view of the image 11, the well-known z-buffer method (also known as z-buffer 30 algorithm) is used in association with one or more depth maps having the same point of view as the image 11 and having a structure similar to the depth map 10. The one or more depth maps having the same point of view as the image 11 and being used in the z-buffer algorithm are also called z-buffer(s). According to this method and by taking the pixel 11p of the image 35 11 as an example, the depths of the fragments of the scene located along the viewing direction 110p having as origin the point of view of the image 11 and passing through the centre of the pixel 11p are compared, and the fragment

P 131 having the smallest depth (i.e. the shortest distance from the point of view along the viewing direction 110p) is the one whose attributes are associated with the pixel 11p. According to a variant, the well-known painter's algorithm is used for solving the visibility problem as to determine which
5 fragment of the scene is visible for each pixel of the image 11 from the point of view of the image 11.

According to the example of figure 1, the point of view 100 advantageously corresponds to the light source of the scene 1 and the depth map 10 is used to determine which fragment of the scene 1 is lit by the light
10 source and which fragment of the scene is in shadow. According to this example, the depth map 10 may also be called a shadow map. Then, as to determine whether the fragment P 131 (corresponding to the pixel 11p of the image 11) is lit or in the shadow of an object of the scene 1, the fragment P 131 is projected into the depth map along a viewing direction linking the point
15 of view 100 and the fragment P 131. The distance $||LP||$ between the point of view 100 and the fragment P 131 is compared to the depth information $||LP'||$ associated with the centre of the element 10p' corresponding to the projection of the fragment P 131 into the depth map 10. If $||LP||$ is greater than $||LP'||$, then the fragment P 131 is in the shadow of the fragment P' 121
20 (i.e. the fragment P 131 is not directly lit by the light source L). If $||LP||$ is less than or equal to $||LP'||$, then the fragment P 131 is directly lit by the light source L. In an advantageous way, the depth information with which the distance $||LP||$ is compared is retrieved from the depth information associated with the centre of the element 10p' and from the first information representing
25 the variation of depth inside the element 10p'. This enables to determine with a better precision whether the fragment P 131 is lit or not by another fragment of the scene, especially when the projection point of the fragment P' 131 into the depth map does not coincide with the centre of the element 10p' while belonging to the element 10p'. This enables to correct some defects
30 related to the finite resolution of the depth map 10. Determining whether a fragment is lit enables to associate video information (e.g. RGB data) with the considered fragment in harmony with the character lit or not lit of the fragment when rendering the scene in the image 11, i.e. when rendering the pixels of the image 11 associated with the considered fragment. The
35 rendering of the pixels of the image is then more precise with less or no artefact when compared to rendering method using depth maps of the prior art.

According to a variant, the scene 1 is a real scene shot by a camera device generating the image 11 and advantageously one or more other images according to different points of view as to generate a stereoscopic image of the scene. According to this variant, a depth map is generated according to the same point of view as the image 11, the depth map and the image 11 being associated with each other. Depth maps associated with the other images of the scene may also be generated. The depth information associated with the centre(s) of the element(s) of the depth map is for example generated via a depth sensor associated with the camera. According to another example, the depth map is generated by comparing two images of the scene 1 acquired according to two different points of view (for example a left image and a right image of the scene), a disparity information being retrieved by comparing on a pixel basis the two images for making a match between the pixels of each view by pairs of two, the disparity information corresponding to the difference in pixels according to the horizontal axis between the location of a pixel in the left image and the location of its corresponding pixel in the right image. The depth map according to this example is called a disparity map. The disparity map associated with the image 11 is representative of the disparity between image 11 (corresponding for example to a left image of a stereoscopic image) and another image of the stereoscopic image (for example the right image), another disparity map may be associated with the right image, this another disparity map being representative of the disparity between the right image and the left image 11. Each disparity map is advantageously estimated by comparison and pairing of the pixels of the left image 11 (respectively right image) to the pixels of the right image (respectively left image 11). The disparity associated with a pixel of the left image 11 (respectively right image) advantageously corresponds to the pixel distance between this pixel of the left image 11 (respectively right image) and the corresponding (or paired) pixel of right image (respectively left image 11), that is to say, the pixel of the right image (respectively left image 11) having video information (that is to say, color information) identical or similar to that of the pixel of left image 11 (respectively right image). The first information representative of the variation of depth is established and associated with the elements of the depth map 10 (disparity map) as it will be described with more details with regard to figures 2 to 4.

Figure 2 shows a part 20 of the depth map 10 of figure 1, according to a particular and non-limitative embodiment. This part of the depth map is centred on a first element 21, which is surrounded by 8 elements of the depth map 10, among them the elements 22, 23 and 24, called second elements. A depth information $p_{z,21}$ representative of the distance between the point of view 100 (not represented on Figure 2) and the fragment P_T 25 is associated with the centre T 211 of the first element 21. The point T 211 of the first element corresponds to the projection point of the fragment P_T 25 along the viewing direction 210 which passes through the first element 21. The point T' 212, which belongs to the first element 21, corresponds to the projection point of the fragment P_T 26 along the viewing direction 220 having as origin the point of view 100 associated with the depth map 10 and passing through the first element 21. The first fragment 25 and the second fragment are advantageously close to each other (for example adjacent) and belongs to the same surface of an object of the scene, i.e. the surface of the object 13 which is lit by the light source L (not represented on figure 2) corresponding to the point of view 100 associated with the depth map 10. As to determine whether the fragment P_T 26 is lit, the depth of the fragment P_T 26 according to the point of view 100 is compared with the depth information associated with the point T' 212, which is computed by using the depth information associated with the first element 21 (or with the centre T 211 of the first element 21) and the one or more first information representative of the variation of depth in the first element 21 that is (are) associated with the first element 21. With the depth maps of the prior art, the depth of the fragment P_T 24 would have only been compared with the depth information $p_{z,21}$ associated with the centre T 211 of the first element 21, which may have led to visible artefacts. Indeed, by considering that the surface of the object 13 to which the two fragments 25 and 26 belong is nearly tangent to the viewing directions 210 and 220 of the first and second fragments (or in another words, the angle formed by the surface normal of the object 13 and by one viewing direction 210 or 220 is high, i.e. greater than a predetermined threshold angle, for example greater than 45°), the comparison of the distance $\|LP_T\|$ with the depth associated with the centre T 211 of the first element 21 (and which actually corresponds to the distance $p_{z,21} = \|LP_T\|$) could establish that the second fragment P_T 26 is in the shadow of the first fragment P_T 25, especially when the second fragment P_T 26 is behind the first fragment P_T 25 with regard to the point of view, or when

the second fragment P_T 26 is located further from the first fragment P_T 25 with regard to the point of view. This is of course an erroneous consideration due to the imprecision of the depth information stored in depth map of the state of the art that do not comprise the first information established as it will
5 described with regards to Figures 3A, 3B, 4 and 5. Indeed, both fragments P_T 25 and P_T 26 are lit by the light source L (or visible from the point of view 100) as they belong to one and same surface of the object 13 and as their projection points T 211 and T' 212 in the depth map belong to the same first element 21.

10 **Figures 3A and 3B** show a first method to establish the one or more first information representative of the variation of depth in the first element 21, according to a particular and non-limitative embodiment of the present principles. Common elements of figures 2 and 3A and 3B have the same reference numbers. **Figure 3A** illustrates a first surface element 30
15 which corresponds to the projection of a second surface element belonging to the scene 1, the second surface element corresponding for example to a mesh element (a polygon, for example a triangle) if the scene has been modelled by polygonal modelling or to a subdivision of a surface if the scene 1 has been modelled by subdivision of surfaces. According to the example of
20 figure 3, the first surface element takes the form of a triangle and is defined in the space (x, y) of depth map 10. The first surface element 30 comprises at least 4 elements 21, 22, 23, 24 forming a 2x2 square of elements. The element 21 corresponds to the first element 21 of figure 2, the elements 22, 23 and 24 being called second elements. dx represents the distance between
25 the centre of the first element 21 and the centre of the second element 22 along the horizontal axis x, in the space (x, y) of the depth map. dy represents the distance between the centre of the first element 21 and the centre of the second element 23 along the vertical axis y, in the space (x, y) of the depth map. The first information representative of the variation of depth
30 in the first element 21 in the space (x, y) of the depth map is advantageously established (i.e. computed or generated) during the rasterization process (which enables to determine which fragments of the scene 1 are part of the second surface elements of the scene 1 and thus of the corresponding first surface elements of the depth map) of the first surface element 30 in the
35 depth map, the rasterization process being performed by the geometry shader of a graphics hardware pipeline associated with a GPU (Graphics Processing Unit) as described hereinafter with respect to figure 5. The first

information representative of the variation of depth in the first element along the x axis is established from the depth information associated with the centre of the first element 21 and from the depth information associated with the centre of the second element 22, which is advantageously adjacent to the first element 21 along the x axis, by taking into account the distance dx separating the centre of the first element 21 and the centre of the second element 22 along the x axis. **Figure 3B** illustrates the first element 21 and the second element 22 and the depth information d1 and d2 associated with their respective centres. d1 and d2 are represented with dashed arrows, the depth difference between the first element 21 and the second element 22 being represented with a line segment 31, the distance dx between the centres of respectively the first element 21 and the second element 22 being represented by a double arrow. The first information representative of the variation of depth in the first element 21 corresponds to the slope of this line segment 31, which is obtained by establishing the partial derivative of the function of the straight line 31.

The first information representative of the variation of depth in the first element in the space of the depth map along the x axis may be established with the following equation:

$$\frac{dp_{z,21}}{dx} = \frac{p(21-dx) - p(21)}{dx} = \frac{p(22) - p(21)}{dx} \quad \text{equation 1}$$

with $\frac{dp_{z,21}}{dx}$ corresponding to the first information along the x axis associated with the first element 21, also corresponding to the partial depth derivative along the x axis,
 p(21) corresponding to the depth information associated with the centre T 211 of the first element 21,
 p(21 - dx) = p(22) corresponding to the depth information associated with the centre of the second element 22.

In a same way, a first information representative of the variation of depth in the first element along the y axis is established from the depth information associated with the centre of the first element 21 and from the depth information associated with the centre of the second element 23, which is advantageously adjacent to the first element 21 along the y axis, by taking into account the distance dy separating the centre T 211 of the first element 21 and the centre of the second element 23 along the y axis. The first

information representative of the variation of depth in the first element 21 in the space of the depth map along the y axis may be established with the following equation:

$$\frac{dp_{z,21}}{dy} = \frac{p(21-dy) - p(21)}{dy} = \frac{p(23) - p(21)}{dy} \quad \text{equation 2}$$

with $\frac{dp_{z,21}}{dy}$ corresponding to the first information associated with the first element 21 along the y axis, also corresponding to the partial depth derivative along the y axis,

10 p(21) the depth information associated with the centre T 211 of the first element 21,

p(21 - dy) = p(23) corresponding to the depth information associated with the centre of the second element 23.

15 According to a variant, only one of the two first information (either along the x axis or along the y axis) is established as to minimize the computation amount performed in the rendering pipeline of the GPU.

The first information associated with the other elements 22, 23 and 24 is advantageously established with the same group of elements 21 to 24. For example, the first information $\frac{dp_{z,22}}{dx}$ representative of the variation of depth in the element 22 along the x axis is established from the depth information p(22) associated with the centre of the element 22 and from the depth information p(21) associated with the centre T 211 of the element 21, by taking into account the distance dx 32 separating the centre of the element 22 and the centre of the element 21. The first information $\frac{dp_{z,22}}{dy}$ representative of the variation of depth in the element 22 along the y axis is established from the depth information p(22) associated with the centre of the element 22 and from the depth information p(24) associated with the centre of the element 24, by taking into account the distance dy separating the centre of the element 22 and the centre of the element 24. Both first information (along the x axis and the y axis respectively) may be established via the following equations:

$$\frac{dp_{z,22}}{dx} = \frac{p(22) - p(22-dx)}{dx} = \frac{p(22) - p(21)}{dx} \quad \text{equation 3}$$

$$\frac{dp_{z,22}}{dy} = \frac{p(22-dy) - p(22)}{dy} = \frac{p(24) - p(22)}{dy} \quad \text{equation 4}$$

Figure 4 show a second method to establish the one or more first information representative of the variation of depth in the first element 21 of figure 2, according to a particular and non-limitative embodiment. Figure 4 illustrates a first surface element 41 which corresponds to the projection of a second surface element 42 belonging to the scene 1, the second surface element corresponding for example to a mesh element (a polygon, for example a triangle) if the scene has been modelled by polygonal modelling or to a subdivision of a surface if the scene 1 has been modelled by subdivision of surfaces. The second surface element 42 is represented in the world space, i.e. the space of the scene 1. The first surface element 41 corresponds to the projection of the second surface element 42 in the tri-dimensional space 40 associated with an orthographic camera associated with the depth map 10. Using an orthographic camera enables to project the second surface element, which belong to the world space, into a tri-dimensional space (x, y, z) of the camera field of view associated with the depth map 10. As to establish the one or more first information representative of the variation of depth in a first element of the depth map in the 2D-space of the depth map 10, the function representative of the plane associated with the first surface element 41 in the 3D space of the orthographic camera 40 is determined and is as follow:

$$ax + by + cz + d = 0 \quad \text{equation 5}$$

with a, b, c and d the plane factors,

x, y and z being the coordinates of points of the plane, z corresponding to the depth.

$$z = \frac{-(ax+by+d)}{c} \quad \text{equation 6}$$

which enables to establish the first information ($dp_{z,21}/dx$) along the x axis of the space of the depth map and/or the first information ($dp_{z,22}/dy$) along the y axis of the space of the depth map:

$$\frac{dp_{z,21}}{dx} = -\frac{a}{c} \quad \text{equation 7}$$

$$\frac{dp_{z,22}}{dy} = -\frac{b}{c} \quad \text{equation 8}$$

Figure 5 diagrammatically illustrates the structure 5 of a memory element (or combination of memory elements) that represents the first

element 21 of the depth map 10, according to a particular and non limitative embodiment of the present principles. The structure 5 comprises 3 memory blocks 50, 51, 52. The depth information $p_{z,21}$ associated with the centre of the first element is stored in the first block 50, the first information $dp_{z,21}/dx$ representative of the variation of depth along the x axis of the space of the depth map is stored in the second block 51 and the first information $dp_{z,21}/dy$ representative of the variation of depth along the y axis of the space of the depth map is stored in the third block 52. The structure of the depth map is for example a 32-bits RGBA buffer, 16 bits being used for the block 50, 8 bits for the second block 51 and 8 bits for the third block 52. According to another example, the structure of the depth map is a 64-bits data array stored in a RGBA buffer with 32 bits for the first block 50 and 16 bits for each block 51 and 52. If only one first information is established (either along axis x or axis y), one of the block 51 and 52 is empty and the freed space memory may be used for storing the only one first information with more precision.

The first information stored in the depth map 10 and associated with the first element 21 of figure 2 may then be used for computing the depth information associated with the point T' 212 of the first element 21. The depth information $p_{z,T'}$ associated with point T' 212 is computed with the following equation:

$$p_{z,T'} = p_T + (x_{T'} - x_T) \frac{dp_{z,21}}{dx} + (y_{T'} - y_T) \frac{dp_{z,21}}{dy} \quad \text{equation 9}$$

with $p_T = p_{z,21}$ the depth information associated with the centre T 211 of the first element 21,
 $x_{T'}$ and $y_{T'}$ the coordinated of the point T' 212 in the space (x, y) of the depth map 10,
 x_T and y_T the coordinated of the point T 211 in the space (x, y) of the depth map 10,
 $\frac{dp_{z,21}}{dx}$ the first information representative of the variation of depth in the first element 21 along the x axis,
 $\frac{dp_{z,21}}{dy}$ the first information representative of the variation of depth in the first element 21 along the y axis.

As to determine whether the fragment $P_{T'}$ 26 is lit or hidden from the light by the fragment P_T 25, the distance $||LP_T||$ between the point of view 100 and

the fragment P_T 26 is compared with the depth information $p_{z,T}$ associated with the point T' 212 and computed via the equation 9. If $||LP_T||$ is less than or equal to $p_{z,T}$ then the fragment P_T 26 is lit by the light source L 100 (not illustrated on figure 2 but illustrated on figure 1). If $||LP_T||$ is greater than $p_{z,T}$ then the fragment P_T 26 is not lit by the light source L 100.

Figures 6A and 6B illustrate the encoding of the first information representative of the variation of depth in the first element 21 of the depth map 10, according to a particular and non-limitative embodiment. Values of the first information representative of the variation of depth in a first element of a depth map may be significantly small in presence of front facing surfaces (i.e. surfaces of object(s) having a normal parallel or roughly parallel with the viewing direction passing through the center of the first element 21 of the depth map) and conversely very large in presence of grazing angle surfaces (i.e. surfaces of object(s) of the scene having a normal perpendicular or roughly perpendicular to the normal of the depth map). Such amplitude requires high precision float storage and may significantly increase the depth map storage. On the other hand, as the first information represents slopes of linear function of x (along x axis of the depth map) and y (along y axis of the depth map), it may be represented by slope angles as follow:

$$\theta_x(p_{z,21}) = \arctan\left(\frac{dp_{z,21}}{dx}\right) \quad \text{equation 10}$$

$$\theta_y(p_{z,21}) = \arctan\left(\frac{dp_{z,21}}{dy}\right) \quad \text{equation 11}$$

These angular functions are defined in the boundary range $[-\frac{\pi}{2}, \frac{\pi}{2}]$ and may be stored in an unsigned 8 bits integer values for example, with a precision of $\frac{\pi}{256}$, i.e approximately 0.703 degrees.). Figure 4A shows such a angular function 60, the range $[-\frac{\pi}{2}, \frac{\pi}{2}]$ being normalized into $[-1.0; 1.0]$.

It may be observed in figure 6A that for low angles, the first information values (i.e. the derivative or rate) vary slowly and the angular precision is not critical. Conversely it becomes critical near domain bounds, i.e. near $-\frac{\pi}{2}$ and $\frac{\pi}{2}$. A small angular variation represent high derivative variation that may lead to erroneous depth reconstruction. Having higher precision may require an increasing data storage of 16 or 32 bits size for instance. According to one specific and non-limitative embodiment of the invention, the angular functions representative of the variation of depth in a first element of the depth map in

the space of the depth map along axis x and y, i.e. the functions $\theta_x(p_{z,21})$ and $\theta_y(p_{z,21})$, are encoded in odd power functions x^y (for example x^3 or x^5) in order to compress the angular domain around 0 and give higher precision for area near the domain bounds, i.e. near $-\frac{\pi}{2}$ and $\frac{\pi}{2}$. Such function 61 and effective
 5 compression is showed in figure 6B with an odd power function (figure 6B illustrating a normalized angular domain compression using odd power function (i.e. x^3 in the example of figure 6B)). Such an embodiment allows to record the first information (i.e. the derivatives) with a good precision with an only 8 bits data storage for each first information value. The final encoded
 10 first information values $E_{dx}(p_{z,21})$ and $E_{dy}(p_{z,21})$ (along the x axis and the y axis respectively) in an unsigned 8 bits integer are obtained as follow:

$$E_{dx}(p_{z,21}) = \left(0.5 + 0.5 \left(\frac{2 \times \theta_x(p_{z,21})}{\pi} \right)^n \right) \times 255 \quad \text{equation 12}$$

$$E_{dy}(p_{z,21}) = \left(0.5 + 0.5 \left(\frac{2 \times \theta_y(p_{z,21})}{\pi} \right)^n \right) \times 255 \quad \text{equation 13}$$

15 with n representing a positive odd integer.

The decoding as to obtain the first information values is advantageously performed in scene rendering pass where depth comparison takes place as to determine whether a fragment is lit (or whether a fragment is visible). Decoded first information values $\frac{dp_{z,21}}{dx}$ and $\frac{dp_{z,21}}{dy}$ are obtained as
 20 follow:

$$\frac{dp_{z,21}}{dx} = \tan \left(\frac{\pi}{2} \times \left(2 \times \frac{E_{dx}(p_{z,21})}{255} - 1 \right)^{\frac{1}{n}} \right) \quad \text{equation 14}$$

$$\frac{dp_{z,21}}{dy} = \tan \left(\frac{\pi}{2} \times \left(2 \times \frac{E_{dy}(p_{z,21})}{255} - 1 \right)^{\frac{1}{n}} \right) \quad \text{equation 15}$$

25

Figure 7 diagrammatically shows a hardware embodiment of a device 7 configured for enriching the content associated with a first element of a depth map. The device 7 is also configured for the creation of display signals of one or several synthesis images representative of the scene 1. The device 7 corresponds for example to a personal computer (PC), a laptop, a tablet, a Smartphone or a games console.
 30

The device 7 comprises the following elements, connected to each other by a bus 75 of addresses and data that also transports a clock signal:

- a microprocessor 71 (or CPU),

- a graphics card 72 comprising:
 - several Graphical Processor Units (or GPUs) 720,
 - a Graphical Random Access Memory (GRAM) 721,
- a non-volatile memory of ROM (Read Only Memory) type 76,
- 5 - a Random Access Memory or RAM 77,
- one or several I/O (Input/Output) devices 74 such as for example a keyboard, a mouse, a webcam, and
- a power source 78.

The device 7 also comprises a display device 73 of display screen
10 type directly connected to the graphics card 72 to display synthesized images calculated and composed in the graphics card, for example live. The use of a dedicated bus to connect the display device 73 to the graphics card 72 offers the advantage of having much greater data transmission bitrates and thus reducing the latency time for the displaying of images composed by the
15 graphics card. According to a variant, a display device is external to the device 7 and is connected to the device 7 by a cable or wirelessly for transmitting the display signals. The device 7, for example the graphics card 72, comprises an interface for transmission or connection (not shown in figure 7) adapted to transmit a display signal to an external display means
20 such as for example an LCD or plasma screen or a video-projector.

It is noted that the word "register" used in the description of memories 721, 76, and 77 designates in each of the memories mentioned, both a memory zone of low capacity (some binary data) as well as a memory zone of large capacity (enabling a whole program to be stored or all or part of
25 the data representative of data calculated or to be displayed).

When switched-on, the microprocessor 71 loads and executes the instructions of the program contained in the RAM 77.

The random access memory 77 notably comprises:

- in a register 770, the operating program of the microprocessor
30 71 responsible for switching on the device 7,
- parameters 771 representative of the scene (for example modelling parameters of the object(s) of the scene, lighting parameters of the scene.).

The algorithms implementing the steps of the method specific to
35 the invention and described hereafter are stored in the memory GRAM 721 of the graphics card 72 associated with the device 7 implementing these steps. When switched on and once the parameters 771 representative of the

environment are loaded into the RAM 77, the graphic processors 720 of the graphics card 72 load these parameters into the GRAM 721 and execute the instructions of these algorithms in the form of microprograms of "shader" type using HLSL (High Level Shader Language) language or GLSL (OpenGL Shading Language) for example.

The random access memory GRAM 421 notably comprises:

- in a register 7211, the parameters representative of the scene,
- in a register 7212, the depth information associated with the centres of the elements of the depth map,
- in a register 7213, the one or two first information representative of the variation of depth in an element of the depth map in the space of the depth map.

According to a variant, the first and second identifiers and the distances are stored in the RAM 77 and processed by the microprocessor 71.

According to another variant, a part of the RAM 77 is assigned by the CPU 71 for storage of the identifiers and the distances if the memory storage space available in GRAM 721 is insufficient. This variant however causes greater latency time in the composition of an image comprising a representation of the environment composed from microprograms contained in the GPUs as the data must be transmitted from the graphics card to the random access memory 77 passing by the bus 75 for which the transmission capacities are generally inferior to those available in the graphics card for transmission of data from the GPUs to the GRAM and vice-versa.

According to another variant, the power supply 78 is external to the device 7.

Figure 8 shows a method for enriching the content associated with a first element of a depth map implemented for example in a device 7, according to a first non-restrictive particularly advantageous embodiment of the invention.

During an initialisation step 80, the different parameters of the device 7 are updated. In particular, the parameters representative of the scene 1 represented in the image 11 as well as the depth information comprised in the depth map 10 are initialised in any way.

Then during a step 81, at least a first information representative of the variation of the depth in a first element (for example a texel or a pixel) of a depth map is established in the space of the depth map. The first

information is used for enriching the content of depth map of the state of the art which only comprises one depth information (called second information representative of the depth), associated with the centre of the first element, corresponding to the depth of the fragment of the scene that is visible from
5 the point of view associated with the depth map along a viewing direction having as origin the point of view of the depth map and passing through the first element. In an advantageous way, two first information are established, i.e. one first information representative of the variation of the depth along the horizontal axis of the space of the depth map and another first information
10 representative of the variation of the depth along the vertical axis (which is perpendicular to the horizontal axis) of the space of the depth map. According to a variant, only one of the two first information is established, either the first information representative of the variation of the depth along the horizontal axis of the space of the depth map or the first information
15 representative of the variation of the depth along the vertical axis of the space of the depth map. The first information is advantageously used in addition to the depth information associated with the centre of the centre of the first element to establish the depth information associated with any point of the first element, using the coordinates of this point expressed in the space
20 of the depth map, instead of associated the depth information of the centre of the first element with any point of the first element as it is done according to the state of the art.

The first information is for example established from the depth information associated with the centre of the first element and with the depth
25 information associated with the centre of a second element of the depth map. The first and second elements belongs to a same surface element resulting from the projection of a surface element of the scene into the depth map. The first and second elements used to establish the first information representative of the variation of the depth along the horizontal axis of the
30 space of the depth map are advantageously adjacent along the horizontal axis. The first and second elements used to establish the first information representative of the variation of the depth along the vertical axis of the space of the depth map are advantageously adjacent along the vertical axis. The first information advantageously corresponds to the ratio of the
35 difference of depth between the first element and the second element to the distance between the first element and the second element (for example to

the distance between the centre of the first element and the centre of the second element).

According to another example, the first information is established by using the equation of a surface element comprising the first element and obtained by projecting a surface element of the scene into the space of a camera field of view associated with the depth map. The first information corresponds to the slope(s) of this surface element, the equation of which being expressed in the space of the camera field of view of the depth map, with regard to the horizontal axis and/or vertical axis of the space of the depth map.

According to a variant, the one or two first information is expressed under the form of a slope angle representing the variation of the depth in the first element.

According to another variant, this (these) angular representation(s) of the first information is (are) encoded in odd power function.

According to a further variant, the first information is stored in a buffer associated with the depth map, in association with the first element.

According to another variant, an image of the scene is rendered by displaying pixels associated with fragments of the scene which are visible from the point of view (i.e. the camera field of view) associated with the image. The color information (e.g. RGB information) associated with the displayed pixels of the image corresponds to the color information associated with the fragments associated with the pixels of the image. The depth of a fragment associated with a pixel of the image is advantageously compared to the depth associated with the point of projection of the fragment into the depth map associated with the scene along a viewing direction having as origin the point of view of the depth map and as end the considered fragment, the depth associated with the point of projection being retrieved from the first information and the second information associated with the element of the depth map comprising the point of projection. This comparison enables to determine whether the considered fragment is lit (when the light source of the scene corresponds to the point of view of the depth map), which may have an impact on the color information associated with the fragment and thus on the color information associated with the pixel of the image to be rendered.

The step 81 is advantageously reiterated for each element of the depth map and for each depth map associated with any image of the scene.

Naturally, the invention is not limited to the embodiments previously described.

In particular, the invention is not limited to a method for enriching
5 the content of a depth map but also extends to any device implementing this method and notably any devices comprising at least one GPU. The implementation of calculations necessary to the generation of elementary geometries, to the determination of index values to be assigned to the elementary geometries is not limited either to an implementation in shader
10 type microprograms but also extends to an implementation in any program type, for example programs that can be executed by a CPU type microprocessor.

The use of the invention is not limited to a live utilisation but also extends to any other utilisation, for example for processing known as
15 postproduction processing in a recording studio for the display of synthesis images for example.

The invention also relates to a method (and a device configured) for encoding depth information representative of the variation of depth in an element of a depth map in the space of the depth map. The invention further
20 relates to a method and device for determining the depth information associated with a point of a first element of depth map based on the depth information associated with the centre of the first element and on the additional depth information representative of the variation of the depth along the horizontal and/or vertical axis of the depth map.

Advantage is taken of the programmable rendering pipeline present in GPU (Graphic Processor Unit) to encode the first information (also called derivatives) in a first pass (shadow map rendering), decode them in a second pass (scene rendering) and use them to perform the depth comparison. The GPU implementation for a whole process combining several
25 embodiments of the invention works as follow:

1. A first pass renders the scene from the light view in for example one
32 bits render target (1 or 2 components) representing the depth/shadow map;
2. At vertex processing stage, a vertex shader is set up to transform
35 mesh element (e.g. triangle) vertex from object space to light clip space.
3. At fragment processing stage, a fragment shader is setup. The fragment's depth p_z is obtained in light clip space (i.e. the space of the

depth/shadow map) for the texel being rasterized. p_z is written in the higher 16 bits of the 32 bits final value.

4. The first information (the depth derivatives $\frac{dp_z}{dx}$ and $\frac{dp_z}{dy}$) is computed.

5 Depth derivatives are either computed from a surface (for example a triangle) plane equation or directly obtained from the derivative function available in most GPUs ($dFdx$ (OpenGL) or ddx (DirectX)). They are then encoded in the final value in the 2 lower 8 bits of the depth buffer. The final value is written in the depth/shadow map.

10 5. A second pass renders the scene from the camera view. The depth/shadow map is bind to a GPU texture unit.

6. At fragment processing stage, a fragment shader is setup. The view sample P is projected in light space (space of the depth/shadow map) giving its depth p_z in clip space, its projection location in shadow map space (p_x, p_y) and the texel (i, j) where it belongs to.

15 7. A texture lookup is performed in the shadow map to retrieve the stored value. The higher 16 bits is read to retrieve p_z and dp_z/dx and dp_z/dy from the 2 lower 8 bits value.

8. The depth dz of occluder that coincides with P projection is then retrieved.

20 9. If $dz < p_z$ then P is shadowed. It is unshadowed otherwise. Test result is either written in a shadow buffer for later used (deferred) or combine with surface lighting in the same fragment shader;

The implementations described herein may be implemented in, for example, a method or a process, an apparatus, a software program, a data stream, or a signal. Even if only discussed in the context of a single form of implementation (for example, discussed only as a method or a device), the implementation of features discussed may also be implemented in other forms (for example a program). An apparatus may be implemented in, for example, appropriate hardware, software, and firmware. The methods may be implemented in, for example, an apparatus such as, for example, a processor, which refers to processing devices in general, including, for example, a computer, a microprocessor, an integrated circuit, or a programmable logic device. Processors also include communication devices, such as, for example, Smartphones, tablets, computers, mobile phones, portable/personal digital assistants ("PDAs"), and other devices that facilitate communication of information between end-users.

Implementations of the various processes and features described herein may be embodied in a variety of different equipment or applications, particularly, for example, equipment or applications associated with data encoding, data decoding, view generation, texture processing, and other processing of images and related texture information and/or depth information. Examples of such equipment include an encoder, a decoder, a post-processor processing output from a decoder, a pre-processor providing input to an encoder, a video coder, a video decoder, a video codec, a web server, a set-top box, a laptop, a personal computer, a cell phone, a PDA, and other communication devices. As should be clear, the equipment may be mobile and even installed in a mobile vehicle.

Additionally, the methods may be implemented by instructions being performed by a processor, and such instructions (and/or data values produced by an implementation) may be stored on a processor-readable medium such as, for example, an integrated circuit, a software carrier or other storage device such as, for example, a hard disk, a compact diskette ("CD"), an optical disc (such as, for example, a DVD, often referred to as a digital versatile disc or a digital video disc), a random access memory ("RAM"), or a read-only memory ("ROM"). The instructions may form an application program tangibly embodied on a processor-readable medium. Instructions may be, for example, in hardware, firmware, software, or a combination. Instructions may be found in, for example, an operating system, a separate application, or a combination of the two. A processor may be characterized, therefore, as, for example, both a device configured to carry out a process and a device that includes a processor-readable medium (such as a storage device) having instructions for carrying out a process. Further, a processor-readable medium may store, in addition to or in lieu of instructions, data values produced by an implementation.

As will be evident to one of skill in the art, implementations may produce a variety of signals formatted to carry information that may be, for example, stored or transmitted. The information may include, for example, instructions for performing a method, or data produced by one of the described implementations. For example, a signal may be formatted to carry as data the rules for writing or reading the syntax of a described embodiment, or to carry as data the actual syntax-values written by a described embodiment. Such a signal may be formatted, for example, as an electromagnetic wave (for example, using a radio frequency portion of

spectrum) or as a baseband signal. The formatting may include, for example, encoding a data stream and modulating a carrier with the encoded data stream. The information that the signal carries may be, for example, analog or digital information. The signal may be transmitted over a variety of different
5 wired or wireless links, as is known. The signal may be stored on a processor-readable medium.

A number of implementations have been described. Nevertheless, it will be understood that various modifications may be made. For example, elements of different implementations may be combined, supplemented,
10 modified, or removed to produce other implementations. Additionally, one of ordinary skill will understand that other structures and processes may be substituted for those disclosed and the resulting implementations will perform at least substantially the same function(s), in at least substantially the same way(s), to achieve at least substantially the same result(s) as the
15 implementations disclosed. Accordingly, these and other implementations are contemplated by this application.

The present invention may be used in video game applications for example, whether via programs that can be executed in a PC or portable type computer or in specialised game consoles producing and displaying
20 images live. The device 7 described with respect to figure 7 is advantageously equipped with interaction means such as a keyboard a mouse, a joystick or any other modes for introduction of commands such as for example vocal recognition being also possible.

CLAIMS

1. Method for enriching the content associated with a first element (21) of
5 a depth map (10), the depth map (10) being associated with a scene (1)
according to a point of view (100), characterized in that the method
comprises a step (81) of establishing at least a first information (51, 52)
representative of a variation of depth in said first element (21) in the space of
the depth map.
10
2. Method according to claim 1, wherein the at least a first information
(51, 52) is established from depth information (50) associated with the first
element (21) and from depth information associated with at least a second
element (22, 23), the first element and the at least a second element
15 belonging to a same surface element of the scene projected into the depth
map.
3. Method according to claim 2, wherein the first element (21) and the at
least a second element (22, 23) are adjacent.
20
4. Method according to one of claims 2 to 3, wherein the at least a first
information (51, 52) is established by computing the ratio of the difference of
depth between the first element (21) and the at least a second element (22)
to the distance (32) between the first element (21) and the at least a second
25 element (22).
5. Method according to claim 1, wherein the at least a first information is
established from an equation of a surface element (41) of the scene
projected into the space of a camera field of view (40) associated with the
30 depth map (10), said projected surface element (41) comprising the first
element.
6. Method according to one of claims 1 to 5, wherein the at least a first
information is expressed under the form of a slope angle (60) representative
35 of the variation of depth in said first element.

7. Method according to claim 6, wherein the at least a first information expressed under the form of a slope angle is encoded in odd power function (61).
- 5 8. Method according to one of claims 1 to 7, wherein one first information is established for each dimension of the space of the depth map.
9. Method according to one of claims 1 to 8, wherein the method further comprises a step of storing the at least a first information associated with the
10 first element in said depth map.
10. Method according to one of claims 1 to 9, wherein the content associated with said first element comprises a second information (50) representative of the depth between the point of view (100) and a fragment of
15 the scene (25), said fragment corresponding to the closest fragment visible from the point of view (100) along a viewing direction (210) passing through the first element (21).
11. Device (7) configured for enriching the content associated with a first
20 element of a depth map, the depth map being associated with a scene according to a point of view, characterized in that the device comprises at least one processor (720) configured for establishing at least a first information representative of a variation of depth in said first element in the space of the depth map.
- 25 12. Device (7) according to claim 10, wherein the at least one processor (720) is a Graphical Processor Unit (GPU).
13. Device (7) according to one of claims 11 and 12, wherein the at least a
30 first information is established from depth information associated with the first element and from depth information associated with at least a second element, the first element and the at least a second element belonging to a same surface element of the scene projected into the depth map.
- 35 14. Device (7) according to one of claims 11 to 13, wherein the at least one processor is further configured for expressing the at least a first information under the form of a slope angle representative of the variation of

depth in said first element and for encoding in odd power function the at least a first information expressed under the form of a slope angle.

15. Computer program product, characterized in that it comprises
5 instructions of program code for executing steps of the method according to one of claims 1 to 10, when said program is executed on a computer.

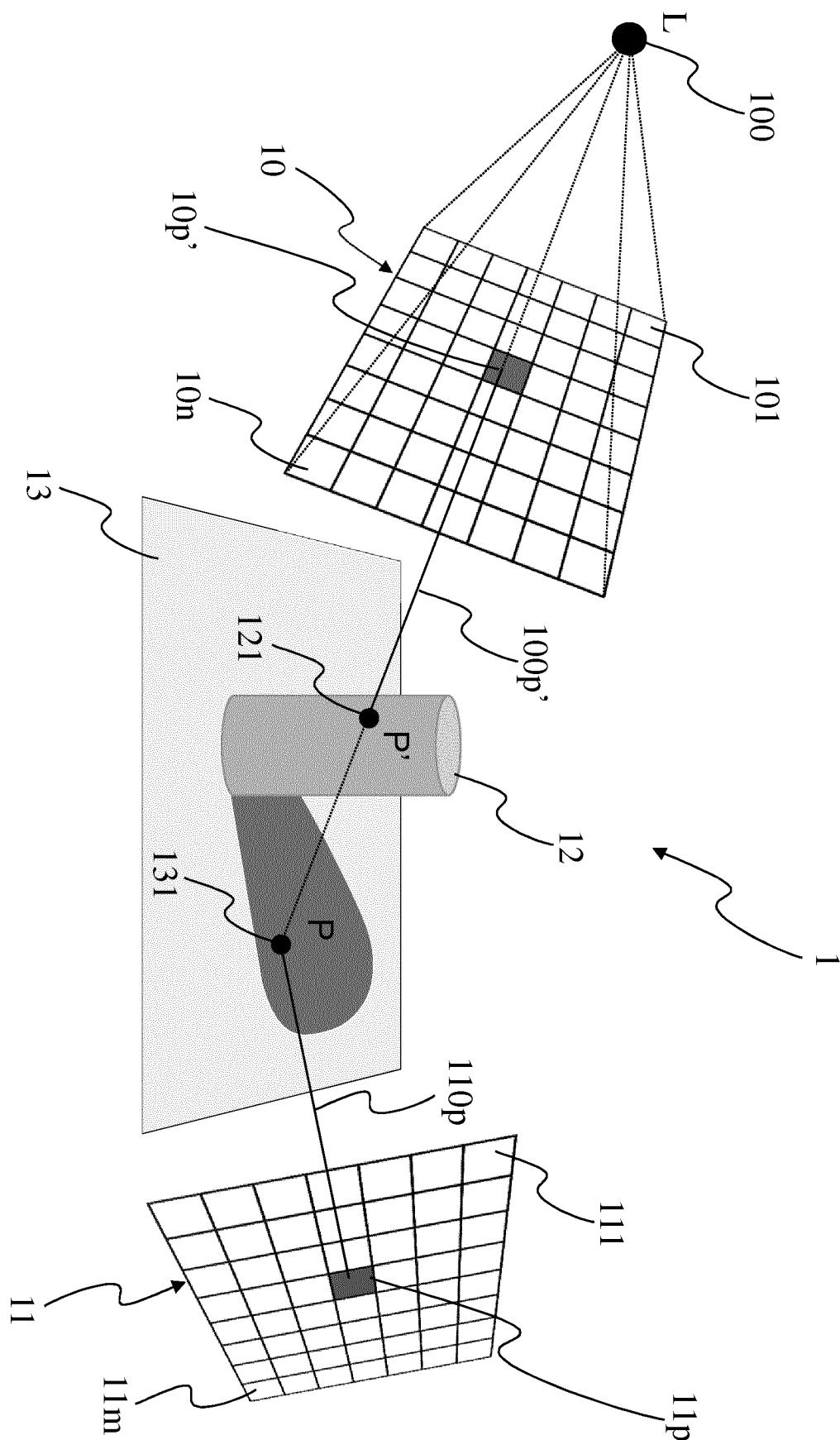


Fig 1

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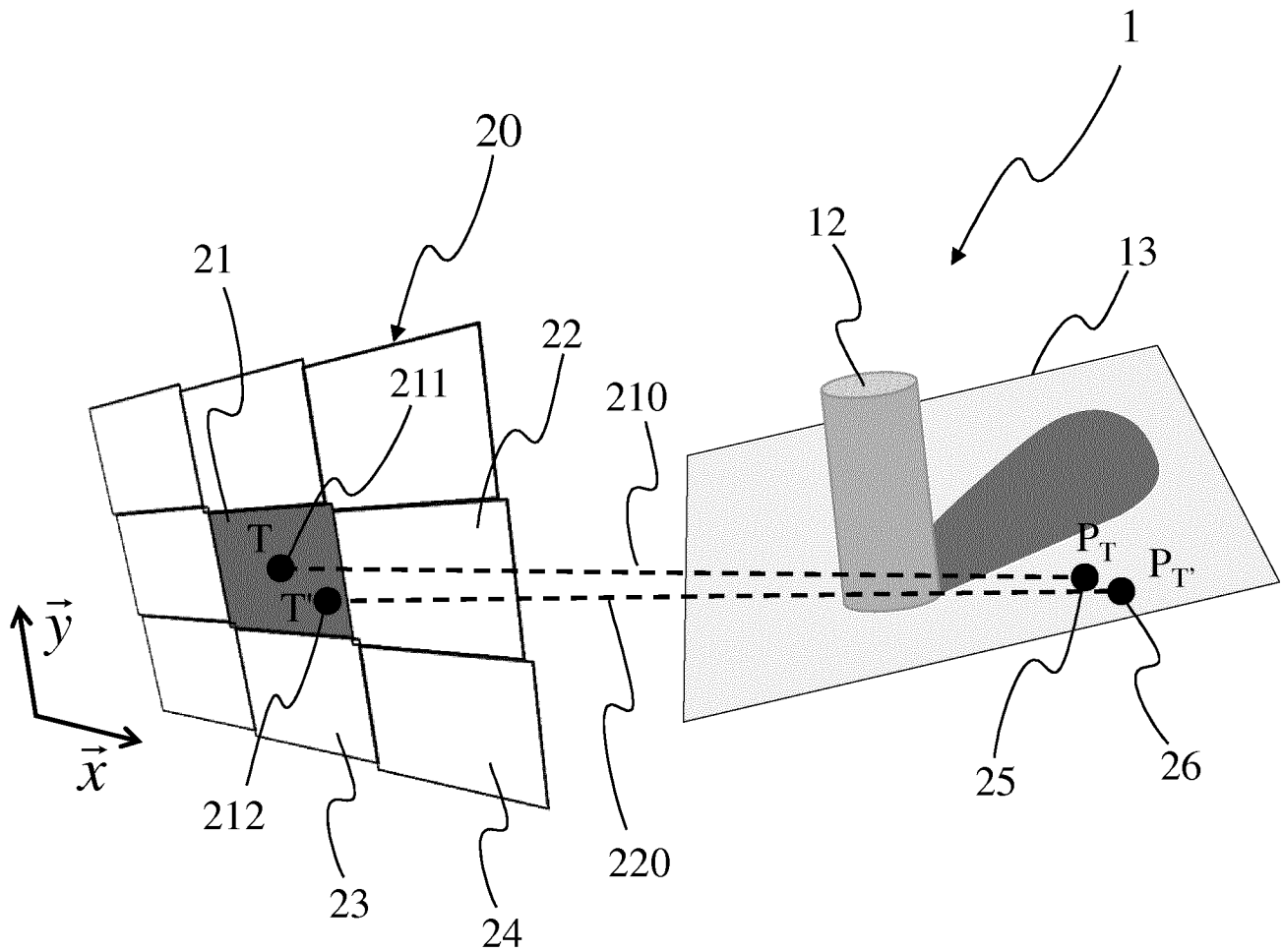


Fig 2

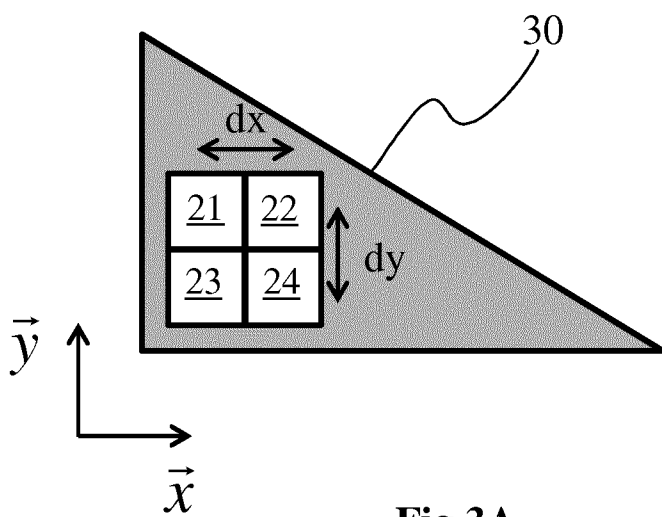


Fig 3A

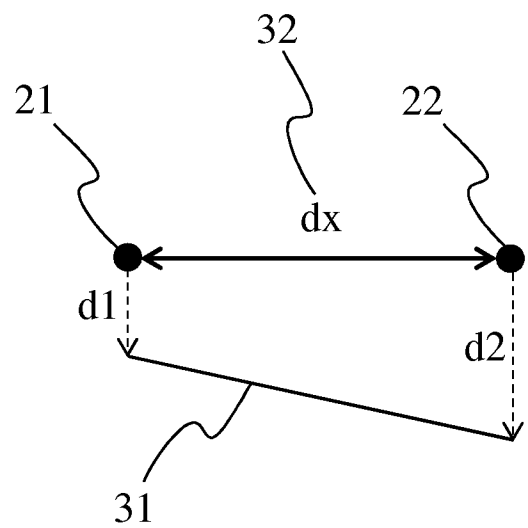


Fig 3B

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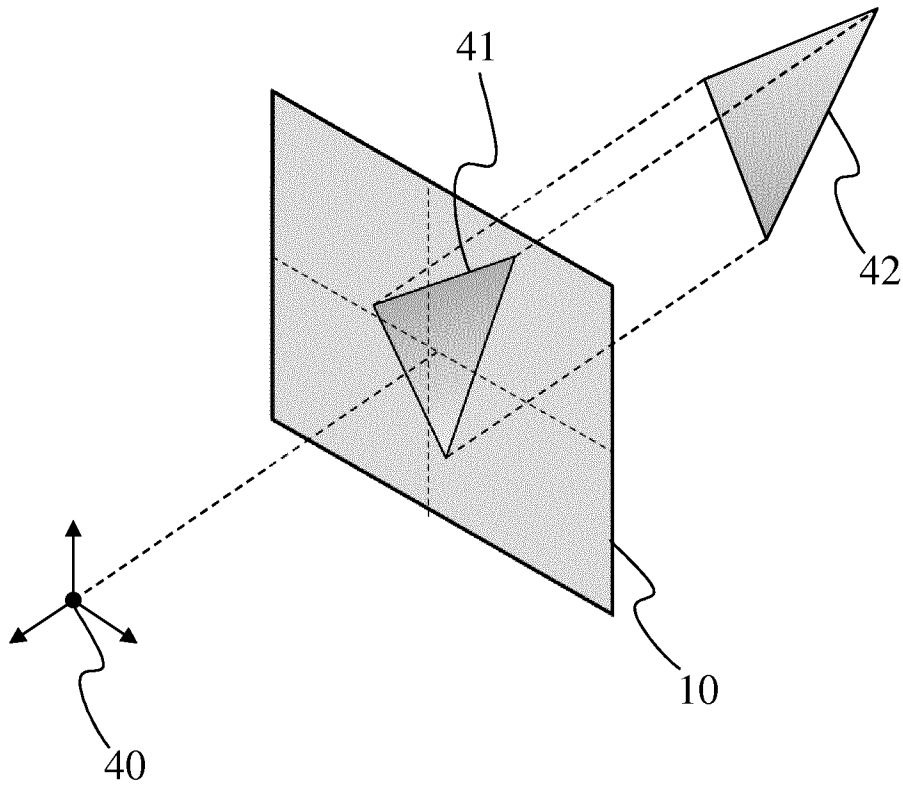


Fig 4

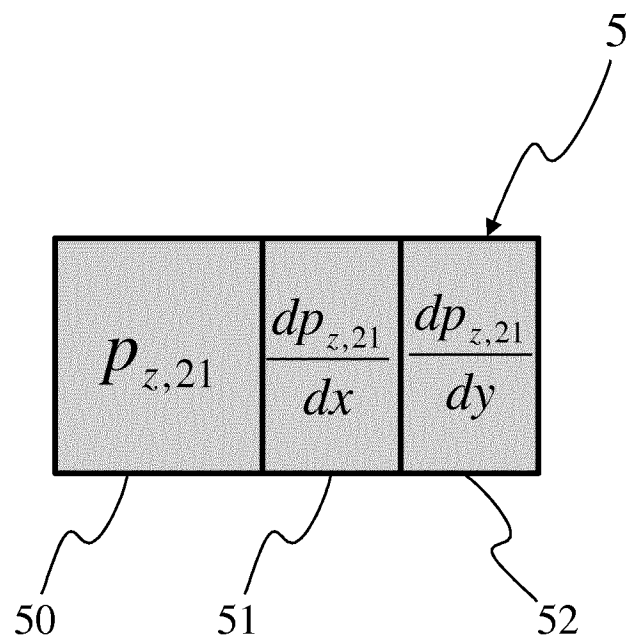


Fig 5

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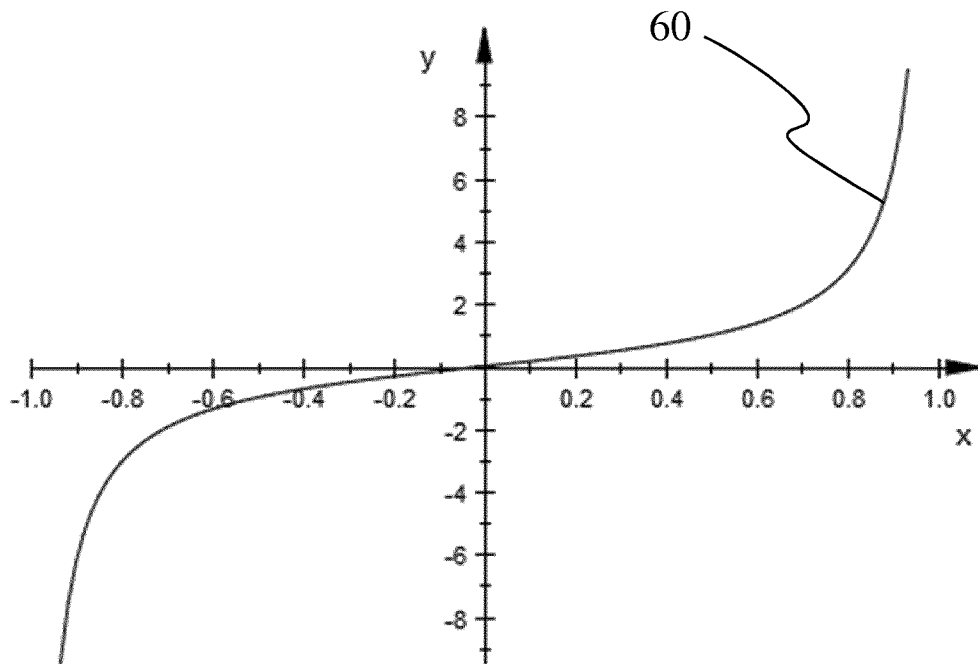


Fig 6A

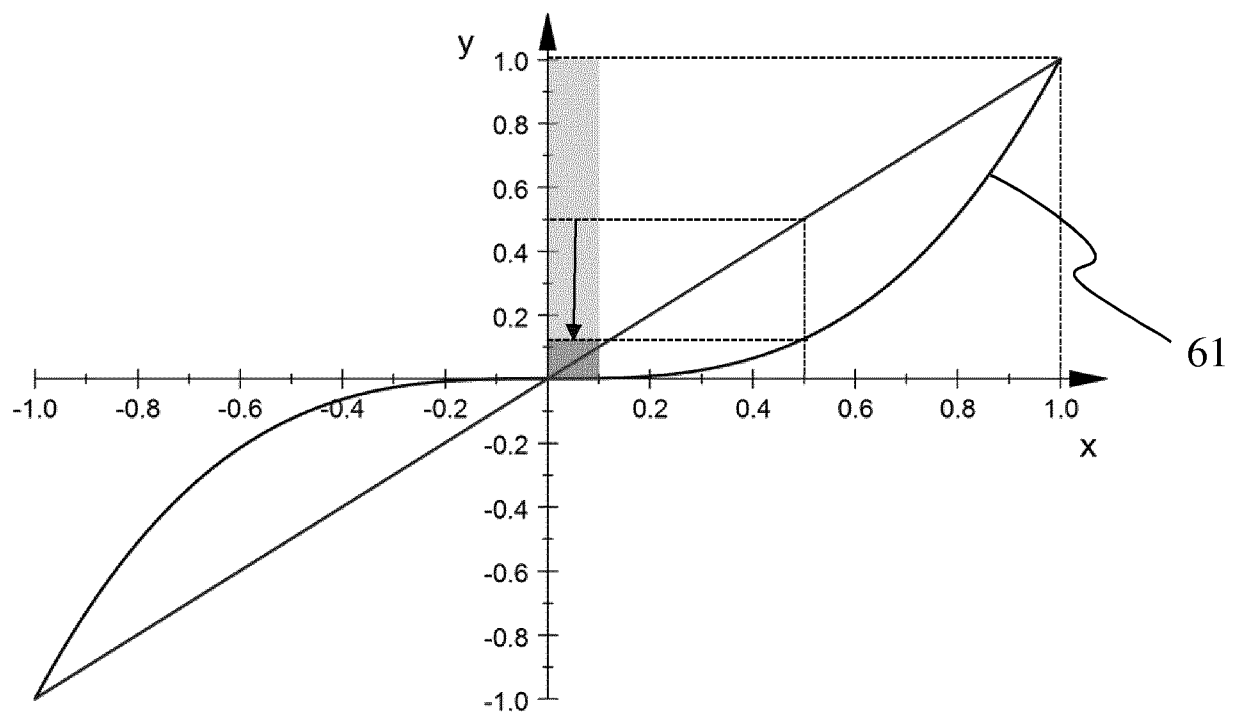


Fig 6B

5/6

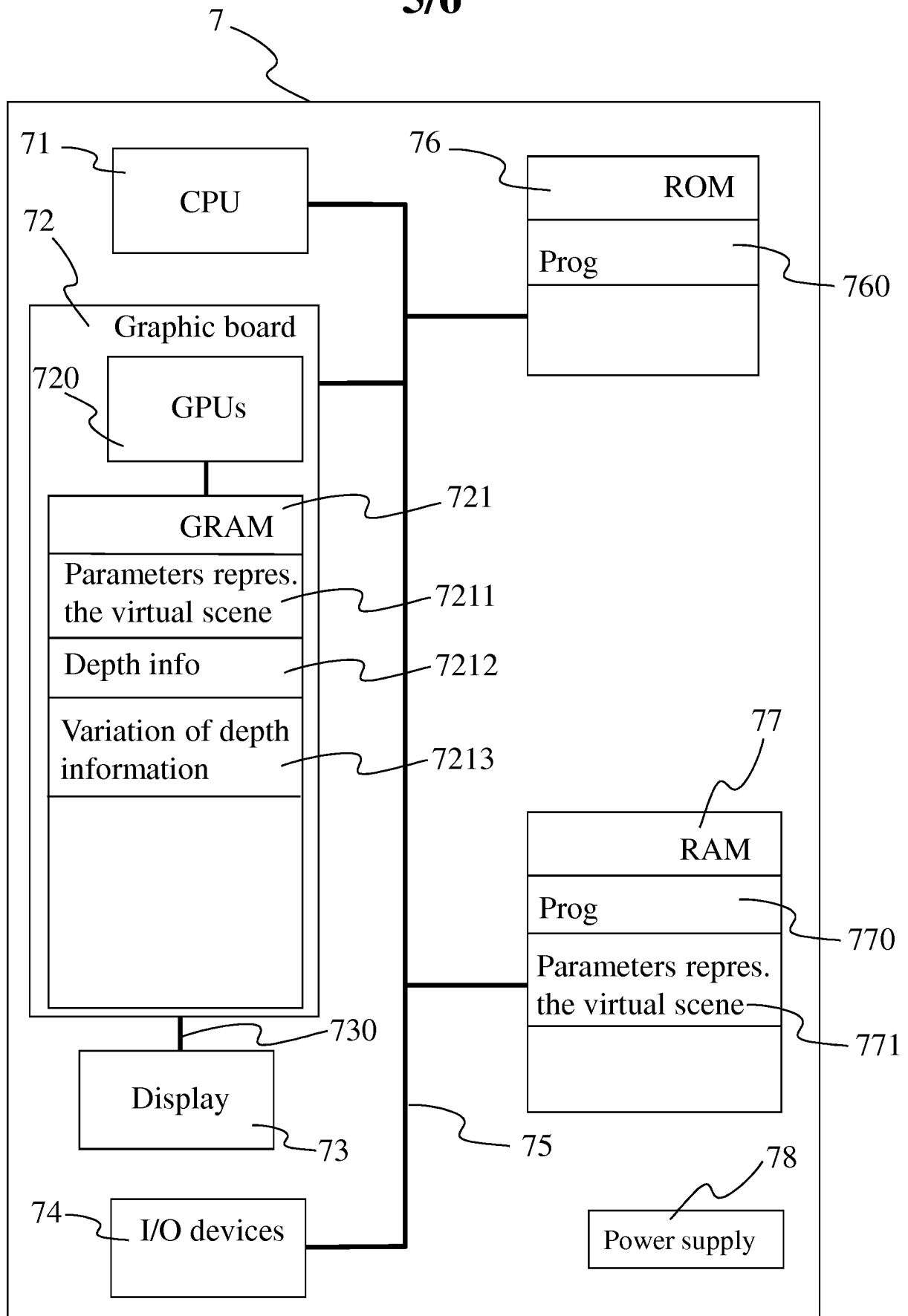


Fig 7

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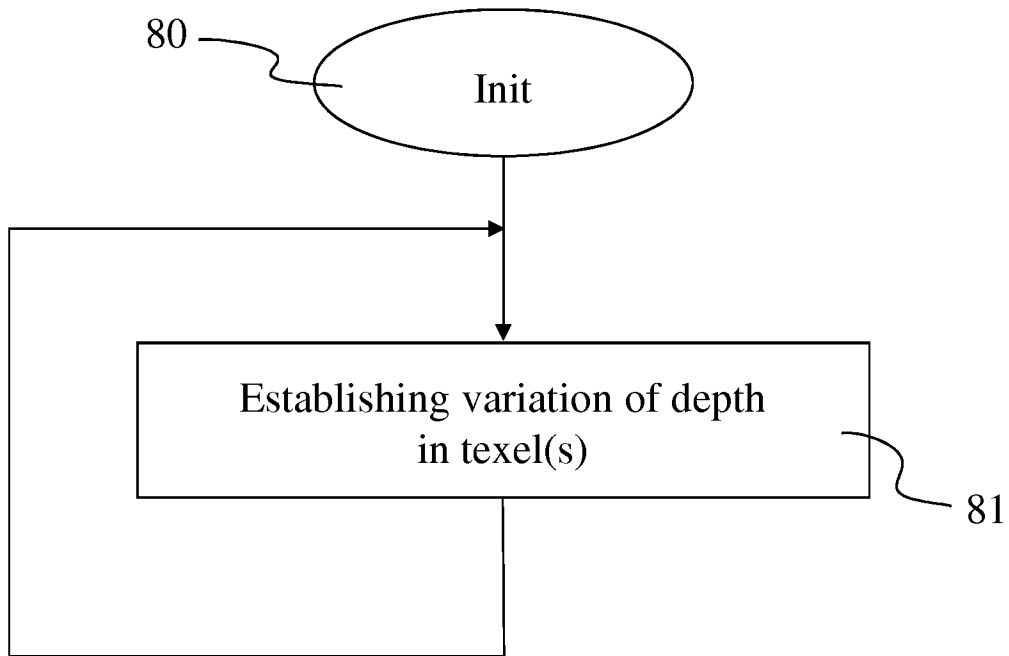


Fig 8